CS236299 Lab 2-3: Language modeling with neural networks

October 19, 2024

```python
# Please do not change this cell because some hidden tests might depend on it.
import os

# Otter grader does not handle ! commands well, so we define and use our
# own function to execute shell commands.
def shell(commands, warn=True):
    """Executes the string `commands` as a sequence of shell commands.

       Prints the result to stdout and returns the exit status.
       Provides a printed warning on non-zero exit status unless `warn`
       flag is unset.
    """
    file = os.popen(commands)
    print (file.read().rstrip('\n'))
    exit_status = file.close()
    if warn and exit_status != None:
        print(f"Completed with errors. Exit status: {exit_status}\n")
    return exit_status

shell("""
ls requirements.txt >/dev/null 2>&1
if [ ! $? = 0 ]; then
 rm -rf .tmp
 git clone https://github.com/cs187-2024/lab2-6.git .tmp
 mv .tmp/tests ./
 mv .tmp/requirements.txt ./
 rm -rf .tmp
fi
pip install -q -r requirements.txt
""")
```

```python
# Initialize Otter
import otter
grader = otter.Notebook()
```

```python
# Please do not change this cell because some hidden tests might depend on it.
import os
```

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```python
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    return exit_status

shell("""
ls requirements.txt >/dev/null 2>&1
if [ ! $? = 0 ]; then
 rm -rf .tmp
 git clone git@github.com:cs236299-2023-spring/lab2-3.git .tmp
 mv .tmp/tests ./
 mv .tmp/requirements.txt ./
 rm -rf .tmp
fi
pip install -q -r requirements.txt
""")
```

In previous labs, you have explored two different language model architectures: the n-gram model and Recurrent Neural Network (RNN) model. Both of these models utilize context to predict the most likely next word in a sequence, but they do so in distinct ways.

The n-gram model bases its predictions solely on the previous n words. This method, though simple, is limited by its fixed context window. On the other hand, the RNN language model uses a hidden state that carries representations from previous time steps, theoretically enabling the model to capture long-range dependencies in text. However, in practice, RNNs often struggle with very long sequences due to issues like vanishing gradients, making them less effective for modeling extended texts.

In the upcoming lab, you will implement and explore the *attention mechanism*, a powerful technique for encoding and utilizing context from previous time steps. This will be your first step toward understanding the Transformer model, one of the most important language model innovations in recent years.

New bits of PyTorch used in the *solution set* for this lab, and which you may therefore find useful:

- `torch.bmm`
- `torch.cumsum`

- `torch.masked_fill`
- `torch.repeat`
- `torch.softmax`
- `torch.transpose`
- `torch.triu`

1 Preparation – Loading packages and data

```python
import json
import math
import random
import wget
import matplotlib.pyplot as plt

import torch
import torch.nn as nn

from math import inf
from tokenizers import Tokenizer
from transformers import PreTrainedTokenizerFast

from tqdm.auto import tqdm
```

```python
# Set random seeds
SEED = 1234
torch.manual_seed(SEED)
random.seed(SEED)

# GPU check, sets runtime type to "GPU" where available
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")
print(device)
```

We use the same data as in lab 2-3 – the *Federalist* papers.

```python
# Prepare to download needed data
def download_if_needed(source, dest, filename):
    if os.path.exists(f"./{dest}{filename}"):
        print (f"Skipping {filename}")
    else:
        print (f"Downloading {filename} from {source}")
        wget.download(source + filename, out=dest)

source_path = "https://github.com/nlp-course/data/raw/refs/heads/master/
 ↪Federalist/"
data_path = "data/"

os.makedirs(data_path, exist_ok=True)
```

```
# Download files, including pretrained language models
for filename in ["federalist_data_raw2.json",
                 "tokenizer.pt",
                 # language models:
                 # Hamilton           Madison
                 "u_attn_lm_h.pt",   "u_attn_lm_m.pt", # uniform attn
                 "attn_lm_h.pt",     "attn_lm_m.pt"    # attention
                ]:
    download_if_needed(source_path, data_path, filename)

# Read in the raw data
dataset = json.load(open(data_path + "federalist_data_raw2.json"))

# Read in the pretrained tokenizer
hf_tokenizer = torch.load(data_path + "tokenizer.pt")
hf_tokenizer.split_special_tokens = False
```

Once again we will split the dataset into training, validation, and test sets. Since we have provided pretrained models, you won't be using the training set in this lab. For the validation set, we have separate ones for papers authored by Hamilton (`validation_hamilton`) and papers authored by Madison (`validation_madison`).

```
[ ]: # Split training, validation, and test sets
     TRAIN_RATIO = 0.9
     # Extract the papers of unknown authorship
     testing = list(filter(lambda ex: ex['authors'] == 'Hamilton or Madison',
                           dataset))
     # Change gold labels in-place
     for ex in testing:
       ex['authors'] = 'Madison'

     # Extract the papers by Madison
     dataset_madison = list(filter(lambda ex: ex['authors']=='Madison', dataset))
     random.seed(SEED)
     random.shuffle(dataset_madison)
     training_size_madison = int(math.floor(TRAIN_RATIO * len(dataset_madison)))
     validation_madison = dataset_madison[training_size_madison:]

     # Extract the papers by Hamilton
     dataset_hamilton = list(filter(lambda ex: ex['authors']=='Hamilton', dataset))
     random.seed(SEED)
     random.shuffle(dataset_hamilton)
     training_size_hamilton = int(math.floor(TRAIN_RATIO * len(dataset_hamilton)))
     validation_hamilton = dataset_hamilton[training_size_hamilton:]

     # We only consider the first 200 tokens of each document for speed
     def truncate(s, k=200):
```

```
   for document in s:
      document['tokens'] = document['tokens'][:k]
truncate(validation_madison)
truncate(validation_hamilton)
truncate(testing)

print (f"Madison validation size:  {len(validation_madison)} documents\n"
       f"Hamilton validation size: {len(validation_hamilton)} documents")
```

Before diving into the *attention mechanism*, we'd like to offer some intuitions about its underlying idea. You'll begin by exploring simple models that will help you understand the basic concepts behind it.

2 A uniform attention model

Recall the forward step in RNN models, starting with converting words to an embedding:

$$\mathbf{x}_t = \mathbf{U}\mathbf{w}_t$$

followed by the RNN layer proper:

$$\mathbf{h}_t = \mathbf{W}\mathbf{h}_{t-1} + \mathbf{V}\mathbf{x}_i$$

and finally, a linear layer and softmax to convert to a distribution over the vocabulary.

$$\mathbf{y}_t = \text{softmax}(\mathbf{X}\mathbf{h}_t)$$

Here,

- $\mathbf{w}_t$ is the word (one-hot or vocabulary index) at time step t,
- $\mathbf{x}_t$ is the corresponding embedding of size D,
- $\mathbf{h}_t$ is the hidden value encapsulating the history of size H, and
- $\mathbf{y}_t$ is the output.

The parameters of the model are just the matrices $\mathbf{U}, \mathbf{V}, \mathbf{W}, \mathbf{X}$.

Notice how $\mathbf{h}_t$ has access to representations from previous time steps only through $\mathbf{h}_{t-1}$. In addition, calculating $\mathbf{h}_t$ requires waiting for the computation of $\mathbf{h}_{t-1}$; for this reason, RNNs are inherently serial in their computations. You will now test a new approach where the context at time step t directly incorporates word embeddings from all previous time steps.

You will first explore a simple and naive model called *The Uniform Attention Model*, so-called because at each time step the model assigns equal attention to all previous words when calculating the distribution for the next word.

At each time step t, $\mathbf{h}_t$ is calculated simply based on the sum of all the previous word embeddings $\mathbf{x}_1, \mathbf{x}_2, \dots \mathbf{x}_t$ as above except that

$$\mathbf{h}_t = \sum_{i=1}^{t} \mathbf{x}_i$$

Now, complete the implementation of the `forward` function. (As usual, the final softmax is handled by the loss function, so you needn't handle that.)

Hint: You might find `torch.cumsum` helpful.

```python
class UATTNLM(torch.nn.Module):
  def __init__(self, hf_tokenizer, embedding_size, hidden_size):
    super().__init__()
    self.hf_tokenizer = hf_tokenizer
    self.pad_index = hf_tokenizer.pad_token_id
    self.hidden_size = hidden_size
    vocab_size = len(hf_tokenizer)

    # In this uniform attention model, the hidden size and the
    # embedding size must be the same, since the former is
    # just a sum over the latter
    assert hidden_size == embedding_size

    # Create modules
    self.embed = torch.nn.Embedding(vocab_size, embedding_size)
    self.hidden2output = torch.nn.Linear(hidden_size, vocab_size)

  def forward(self, context_words):
    """Computes the distribution over the next word given context␣
↪`history_words`.
    Arguments:
      context_words: a list of word strings, could be an empty list when␣
↪generating
                     the first word.
    Returns:
      logits, should be a tensor of size (bsz, vocab_size)
      """
    self.eval()
    context = self.hf_tokenizer(context_words, is_split_into_words=True,␣
↪return_tensors='pt')['input_ids']\
              .long()\
              .to(device) # bsz, context_len
    context_len = context.size(1)

    # For generating the first word, we feed in a special beginning-of-sentence␣
↪symbol <pad>,
    # which is also what we use for padding. In future labs we'll be using␣
↪<bos>, but as long
```

```
    # as training and evaluation use the same beginning-of-sentence symbol, it␣
  ↪doesn't matter
    # which particular symbol we use.
    if context_len == 0:
      context = context.new(1, 1).fill_(self.pad_index)
      context_len = context.size(1)

    hidden = None
    # TODO: calculate output and set logits
    # Logits should be a tensor of size (1, vocab_size)
    # The structure of the network is
    #   embeddings -> output -> hidden2output -> logits

    return logits
```

Question: For uniform attention to work as above, H and D, the hidden size and the embedding size, must be the same. Why?

Type your answer here, replacing this text.

Now, let's load the models for Hamilton and Madison. The model `u_attn_lm_madison` was trained on documents authored by Madison, while `u_attn_lm_hamilton` was trained on documents authored by Hamilton.

```
[ ]: # Create and load uniform attention LM for Madison
     u_attn_lm_madison = UATTNLM(hf_tokenizer,
                                 embedding_size=128,
                                 hidden_size=128,
                                 ).to(device)
     u_attn_lm_madison.load_state_dict(torch.load(data_path + 'u_attn_lm_m.pt',␣
       ↪map_location=device))

     # Create and load uniform attention LM for Hamilton
     u_attn_lm_hamilton = UATTNLM(hf_tokenizer,
                                  embedding_size=128,
                                  hidden_size=128,
                                  ).to(device)
     u_attn_lm_hamilton.load_state_dict(torch.load(data_path + 'u_attn_lm_h.pt',␣
       ↪map_location=device))
```

Let's try to sample from the model. Don't expect a fluent text yet—more improvements are needed in the model.

```
[ ]: def sample(model, context):
         """Returns a token sampled from the `model` assuming the `context`"""
         logits = model(context)[:,-1] # calls internally to model.forward(context)

          # Normalize to get probabilities
         probs = torch.softmax(logits, -1).view(-1) # vocab_size
```

```python
        # Match probabilities with actual word types
        distribution = {}
        for i, prob in enumerate(probs):
          word = model.hf_tokenizer.decode(i, clean_up_tokenization_spaces=True)
          distribution[word] = prob.item()

        prob_remaining = random.random()
        for token, prob in sorted(distribution.items()):
            if prob_remaining < prob:
                return token
            else:
                prob_remaining -= prob
        raise ValueError

def sample_sequence(model, start_context, count=100):
    """Returns a sequence of tokens of length `count` sampled successively
       from the `model` starting with the `start_context`
    """
    random.seed(SEED) # for reproducibility
    context = list(start_context)
    result = list(start_context)
    for i in range(0, count):
        next = sample(model, tuple(context))
        result.append(next)
        context = context + [next]
    return result
```

```python
[ ]: print(' '.join(sample_sequence(u_attn_lm_madison, ('constitution', 'proposed',
     ↪'by', 'the'))), "\n")
     print(' '.join(sample_sequence(u_attn_lm_hamilton, ('constitution', 'proposed',
     ↪'by', 'the'))))
```

Question: In fact, this model should be familiar to you. Do you remember what it's called?

Type your answer here, replacing this text.

In the previous model, we made a simple assumption – that all previous words are equally important. Of course, this simple assumption is wrong in general, as different time steps can have varying levels of importance and dependencies.

Next, you will build a model that differentiates between time steps.

Are you ready? You're about to learn about one of the most important and influential mechanisms invented in recent years.

3   The attention mechanism

The previous model was quite basic and suffered from an obvious problem:

At each time step, we assumed the dependencies on the previous time steps, the context, were static. Ideally, we want the model to determine dynamically at each stage which parts of the context are more relevant and which are less, that is, which parts of the context to *attend to*.

You'll now be introduced to the *attention mechanism* (proposed in this seminal paper), a powerful architecture that allows models to selectively focus on different parts of the input sequence. This mechanism has become a cornerstone in modern natural-language processing, significantly enhancing a model's ability to model language distributions.

Attention works by *querying* a (dynamically sized) sequence of *keys* associated with *values*. Each key-value pair is associated with the context elements of a particular token.

As usual, each query, key, and value is represented as a vector. Attention proceeds as follows: The query is compared to each of the keys, providing a score that specifies how much each key should be attended to. The attention can then be summarized by taking an average of the *values* weighted by the attention score of the corresponding *keys*. This *context vector* can then be used as another input to other processes you will learn about in the next lab.

More formally, let's suppose we have a query vector $\mathbf{q}$ of size D, a set of S keys $\mathbf{k}_i$ each of size D and a set of S values $\mathbf{v}_i$ each of size D, where D is the hidden size. What we want to do through the attention mechanism is to use the query to attend to the keys, and summarize those values associated with the "relevant" keys into a fixed-size context vector $\mathbf{c}_i$ also of size D. Note that this is different from directly compressing the key-value pairs into a fixed-size vector, since depending on the query, we might end up with different context vectors.

We'll turn to implementing this attention mechanism shortly, but first, for concreteness, we show how the mechanism can be used to form a language model. Like the uniform attention mechanism above, we start with an embedding of the vocabulary.

$$\mathbf{x}_t = \mathbf{U}\mathbf{w}_t$$

Next, we construct a query, key, and value for each position with linear transforms for each:

$$\mathbf{q}_t = \mathbf{Q}\mathbf{w}_t$$
$$\mathbf{k}_t = \mathbf{K}\mathbf{w}_t$$
$$\mathbf{v}_t = \mathbf{V}\mathbf{w}_t$$

followed by the attention layer proper:

$$\mathbf{h}_t = \mathrm{attn}(\mathbf{q}_t, \mathbf{k}_1^t, \mathbf{v}_1^t)$$

and finally, a linear layer and softmax to convert to a distribution over the vocabulary.

$$\mathbf{y}_t = \mathrm{softmax}(\mathbf{X}\mathbf{h}_t)$$

We write $\mathbf{k}_1^t$ for the sequence of elements $\langle \mathbf{k}_1, \mathbf{k}_2, ... \mathbf{k}_t \rangle$.

Now back to how the attention calculation works.

To determine the score for a given query and key, it is standard to use a measure of similarity between the query and key. You've seen such similarity measures before, in labs 1-1 and 1-2. A good choice is simply the normalized dot product between query and key. We'll thus take the attention score for query $\mathbf{q}$ and key $\mathbf{k}_i$ to be

$$a_i = \frac{\exp(\mathbf{q} \cdot \mathbf{k}_i)}{Z},$$

where $\cdot$ denotes the dot product (inner product) and exp is exponentiation which ensures that all scores are nonnegative, and

$$Z = \sum_{i=1}^{S} \exp(\mathbf{q} \cdot \mathbf{k}_i)$$

is the normalizer to guarantee the scores all sum to one. (There are multiple ways of parameterizing the attention function, but the form we present here is the most popular one.) You might have noticed that the operation above is essentially a softmax over $\mathbf{q} \cdot \mathbf{k}$.

The attention scores $\mathbf{a}$ lie on a *simplex* (meaning $a_i \geq 0$ and $\sum_i a_i = 1$), which lends it some interpretability: the closer a_i is to 1, the more "relevant" a key k_i (and hence its value v_i) is to the given query.

To compute the result of the attention query – the "context vector" $\mathbf{c}$ – we take the weighted sum of values using the corresponding attention scores as weights:

$$\mathbf{c} = \sum_{i=1}^{S} a_i \mathbf{v}_i$$

The closer a_i is to 1, the higher the weight $\mathbf{v}_i$ receives, and the more the context vector "attends to" the value v_i at position i.

> In usage, the result of attention, the context vector for position t, plays the role of $\mathbf{h}_t$, as above.

Question: Suppose there exists i for which a_i is 1. What will the value of $\mathbf{c}$ be?

Type your answer here, replacing this text.

In practice, instead of computing the context vector once for each query, we want to combine together computations for different queries (for different positions t in the input) to allow for parallel processing on GPUs. This will become especially useful for the transformer implementation in the next lab. We use a matrix $Q \in \mathbb{R}^{T \times D}$ to store T queries, a matrix $K \in \mathbb{R}^{S \times D}$ to store S keys, and a matrix $V \in \mathbb{R}^{S \times D}$ to store the corresponding values. Then we can write down how we compute the attention scores $A \in \mathbb{R}^{T \times S}$ in a matrix form:

$$A = \mathrm{softmax}(QK^{\top}, \mathrm{dim} = -1)$$

and to get the context matrix $C \in \mathbb{R}^{T \times D}$, we have

$$C = AV$$

Question: What is the shape of A? What does A_{ij} represent?

Type your answer here, replacing this text.

Your first job is to implement this calculation by finishing the attention function below, which takes the Q, K, and V matrices and returns the A and C matrices. Note that for these matrices, there is one additional dimension for the batching, so instead of $Q \in \mathbb{R}^{T \times D}$, $K, V \in \mathbb{R}^{S \times D}$, $A \in \mathbb{R}^{T \times S}$, $C \in \mathbb{R}^{T \times D}$, we have $Q \in \mathbb{R}^{B \times T \times D}$, $K, V \in \mathbb{R}^{B \times S \times D}$, $A \in \mathbb{R}^{B \times T \times S}$, $C \in \mathbb{R}^{B \times T \times D}$, where B is the batch size. In addition, the function below also takes an argument `mask` of size $\mathbb{R}^{B \times T \times S}$ to mark where attentions are disallowed. This is useful not only in disallowing attending to padding symbols, but also to efficiently train the model.

> **Hint:** You might find `torch.bmm` helpful for batched matrix multiplications. You might need to transpose and reshape tensors to be able to use this function.

> **Hint:** As mentioned in the beginning of the lab, you might also find `torch.transpose`, `torch.reshape`, `torch.masked_fill`, and `torch.softmax` useful.

> **Hint:** A simple trick for masking an attention score is to set it to negative infinity before normalization.

> **Hint:** Debugging the `attention` function can be tricky. Try defining a very small example of batched **q**, **k**, and **v** values for which you can manually carry out the attention claculation and test the code on those, working your way up to more complex examples.

```
[ ]: #TODO - finish implementing this function.
     def attention(batched_Q, batched_K, batched_V, mask=None):
         """
         Performs the attention operation and returns the attention matrix
         `batched_A` and the context matrix `batched_C` using queries
         `batched_Q`, keys `batched_K`, and values `batched_V`.

         Arguments:
             batched_Q: (bsz, q_len, D)
             batched_K: (bsz, k_len, D)
             batched_V: (bsz, k_len, D)
             mask: (bsz, q_len, k_len). An optional boolean mask *disallowing*
                   attentions where the mask value is *`False`*.
         Returns:
             batched_A: the normalized attention scores (bsz, q_len, k_len)
             batched_C: a tensor of size (bsz, q_len, D).
         """
         # Check sizes
         D = batched_Q.size(-1)
         bsz = batched_Q.size(0)
         q_len = batched_Q.size(1)
         k_len = batched_K.size(1)
```

```
  assert batched_K.size(-1) == D and batched_V.size(-1) == D
  assert batched_K.size(0) == bsz and batched_V.size(0) == bsz
  assert batched_V.size(1) == k_len
  if mask is not None:
    assert mask.size() == torch.Size([bsz, q_len, k_len])


  ...
  batched_A = ...
  batched_C = ...
  # Verify that things sum up to one properly.
  assert torch.all(torch.isclose(batched_A.sum(-1),
                                 torch.ones(bsz, q_len).to(device)))
  return batched_A, batched_C
```

3.1   Causal attention mask

To efficiently train the model, we want to batch the attention operations together such that they can be fully parallelized along the sequence length dimension. (The non-attention operations are position-wise so they are trivally parallelizable.) Each word y_t attends to $t-1$ previous words $y_1, \ldots, y_{t-1}$, which means each word y_t has a different set of key-value pairs. Is it possible to batch them together?

The solution is to use *attention masks*. For every word y_t, we give it all key-value pairs at $y_1, \ldots, y_T$, and we disallow attending to future words $y_t, y_{t+1}, \ldots, y_T$ through an attention mask. (Recall that the `attention` function takes a `mask` argument.) We usually call this attention mask a *causal attention mask*, as it prevents the leakage of information from the future into the past. Since every y_t has the same set of (key, value) pairs, we can batch them and compute the context vectors using a single call to the function `attention`.

What should such a mask be? Implement the `causal_mask` function below to generate this mask.

  Hint: you might find `torch.triu` useful.

```
[ ]: #TODO - implement this function, which returns a causal attention mask
     def causal_mask(T):
       """
       Generate a causal mask.
       Arguments:
           T: the length of target sequence
       Returns:
           mask: a T x T tensor, where `mask[i, j]` should be `True`
           if y_i can attend to y_j, and `False` if y_i cannot
           attend to y_j
       """
       mask = ...
       return mask.to(device)
```

We can visualize the attention mask and manually check if it's what we expected.

```
[ ]: fig, ax = plt.subplots(figsize=(8, 6))

     T = 7
     mask = causal_mask(T)
     ax.imshow(mask.cpu())


     # Uncomment the line below if the plot does not show up
     # Make sure to comment that before submitting to gradescope
     # since there would be some autograder issues with `plt.show()`
     #plt.show()
```

by using causal masks, all positions (at the same layer) can be computed all at once (if the lower
layer has been computed). The parallelizability of the attention mechanism is the key to its success
since it allows for training it on vast amounts of data.

Now we are ready to complete the attention model. > Hint: The causal mask is a 2-D matrix, but
we want to add a batch dimension, and expand it to be of the desired size. For this purpose, you
can use `torch.repeat`.

Complete the `forward` function.

```
[ ]: class ATTNLM(torch.nn.Module):
       def __init__(self, hf_tokenizer, embedding_size, hidden_size):
         super().__init__()
         self.hf_tokenizer = hf_tokenizer
         self.pad_index = hf_tokenizer.pad_token_id
         self.hidden_size = hidden_size
         vocab_size = len(hf_tokenizer)

         # Create modules
         self.embed = torch.nn.Embedding(vocab_size, embedding_size)
         self.q_proj = nn.Linear(hidden_size, hidden_size)
         self.k_proj = nn.Linear(hidden_size, hidden_size)
         self.v_proj = nn.Linear(hidden_size, hidden_size)
         self.hidden2output = torch.nn.Linear(hidden_size, vocab_size)

       def forward(self, context_words):
         """Computes the distribution over the next word given context␣
       ↪`history_words`.
         Arguments:
           context_words: batch a list of word strings, could be an empty list when␣
       ↪generating
                           the first word.
         Returns:
           logits, should be a tensor of size (batch , seq_length , vocab_size)
           """
         self.eval()
```

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```
    context = self.hf_tokenizer(context_words, is_split_into_words=True,␣
 ↪return_tensors='pt')['input_ids']\
            .long()\
            .to(device) # bsz, context_len
    context_len = context.size(1)
    context_bsz = context.size(0)

    # For generating the first word, we feed in a special beginning-of-sentence␣
 ↪symbol <pad>,
    # which is also what we use for padding. In future labs we'll be using␣
 ↪<bos>, but as long
    # as training and evaluation use the same beginning-of-sentence symbol, it␣
 ↪doesn't matter
    # which particular symbol we use.
    if context_len == 0:
      context = context.new(1, 1).fill_(self.pad_index)
      context_len = context.size(1)

    hidden = None
    # TODO: finish feedforward and set logits
    # Logits should be a tensor of size (bsz, seq_length, vocab_size)
    # The structure of the network is
    #   embeddings -> output -> hidden2output -> logits
    output = attention(q, k, v, mask)[1]
    logits = self.hidden2output(output)

    return logits
```

Now, let's load the pretrained models for Hamilton and Madison. The model `attn_lm_madison` was trained on documents authored by Madison, whereas `attn_lm_hamilton` was trained on documents authored by Hamilton.

```
[ ]: # Create and load attention LM for Madison
     attn_lm_madison = ATTNLM(hf_tokenizer,
                              embedding_size=128,
                              hidden_size=128,
                             ).to(device)
     attn_lm_madison.load_state_dict(torch.load(data_path + 'attn_lm_m.pt',␣
      ↪map_location=device))

     # Create and load attention LM for Hamilton
     attn_lm_hamilton = ATTNLM(hf_tokenizer,
                               embedding_size=128,
                               hidden_size=128,
                              ).to(device)
     attn_lm_hamilton.load_state_dict(torch.load(data_path + 'attn_lm_h.pt',␣
      ↪map_location=device))
```

3.2 Sampling from the attention model

Let's try to sample from the models.

```python
print(' '.join(sample_sequence(attn_lm_madison, ('constitution', 'proposed',
    'by', 'the'))), "\n")
print(' '.join(sample_sequence(attn_lm_hamilton, ('constitution', 'proposed',
    'by', 'the'))))
```

3.3 Evaluating text according to the attention model

```python
document_madison = validation_madison[0]['tokens']
document_hamilton = validation_hamilton[0]['tokens']
```

Just like in Lab 2-3, we want to evaluate the models using perplexity.

```python
def neglogprob(tokens, model):
    """Returns the negative log probability of a sequence of `tokens`
       according to a `model`
    """
    score = 0.0
    for i in range(len(tokens)):
        context = tokens[:i]
        token = tokens[i]
        distribution = model(context)
        logits = model(context)[:,-1]
        probs = torch.softmax(logits, -1).view(-1) # vocab_size
        distribution = {}
        for i, prob in enumerate(probs):
            word = hf_tokenizer.decode(i, clean_up_tokenization_spaces=True)
            distribution[word] = prob.item()
        prob = distribution[token] if token in distribution else
    distribution['[UNK]']
        score += -math.log2(prob)
    return score
```

```python
def perplexity(tokens, model):
    """Returns the perplexity of a sequence of `tokens` according to a `model`
    """
    return 2 ** (neglogprob(tokens, model) / (len(tokens)))
```

Calculate the perplexity of each model on each document.

```python
# TODO
attn_ppl_madison_model_madison_document = ...
attn_ppl_hamilton_model_madison_document = ...
attn_ppl_madison_model_hamilton_document = ...
attn_ppl_hamilton_model_hamilton_document = ...
```

Now, let's compare those perplexity values. Do the results make sense to you?

```
[ ]: print (f"Author      Madison Model      Hamilton Model\n"
          f"Madison         {attn_ppl_madison_model_madison_document:5.1f}          ␣
      ↪  {attn_ppl_hamilton_model_madison_document:5.1f}\n"
          f"Hamilton        {attn_ppl_madison_model_hamilton_document:5.1f}          ␣
      ↪  {attn_ppl_hamilton_model_hamilton_document:5.1f}")
```

Although attention is a powerful concept, it alone isn't enough to build a strong model. In the next lab, you will learn about the *Transformer language model*, which is built on the attention mechanism along with several other important components.

4 Lab debrief

Question: We're interested in any thoughts your group has about this lab so that we can improve this lab for later years, and to inform later labs for this year. Please list any issues that arose or comments you have to improve the lab. Useful things to comment on include the following:

- Was the lab too long or too short?
- Were the readings appropriate for the lab?
- Was it clear (at least after you completed the lab) what the points of the exercises were?
- Are there additions or changes you think would make the lab better?

Type your answer here, replacing this text.

End of Lab 2-6

To double-check your work, the cell below will rerun all of the autograder tests.

```
[ ]: grader.check_all()
```