

# Data Representation and Relational Algebra

January 29, 2019

Data Science CSCI 1951A

Brown University

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HTAs: Wennie Zhang, Maulik Dang, Gurnaaz Kaur

# But first!

- Waitlist
- We are working our way through.
- We've sent out ~90 overrides so far, and will send out another batch soon
- If you don't get one by EOD today, then the chance of getting one is probably "low"
- If you are registered any way other than enthusiastically, be a mensch and please drop :)

# But first!

- There will be no iClicker requirement until after shopping period/empty waitlist
  - iClicker forgiveness for those of you who stayed on Thursday 
- You have time to procrastinate on Assignment 1 until end of shopping period
- Sign the collaboration policy!

But first!

Burning Questions?

# Data Representation and Relational Algebra



Sixth Edition

# Fundamentals of Database Systems

Chapter 7: ER Diagrams  
Chapter 3: Relational Model  
Chapter 6: Relational Algebra

Elmasri • Navathe

# DATABASES FOR DATA SCIENTIST

Requirement  
Engineering

Conceptual  
Modeling

Logical and  
Physical  
Modeling

Asking and  
Answering  
Questions  
(Analysis)

“Book of Duty”

Conceptual  
Design (ER)

Logical Design  
(schema, table names,  
data types),  
Physical Design  
(indices, memory  
layout, optimizations)

Relational Algebra,  
SQL

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# “Book of Duty”/“Miniworld”

- Informal description of data domain
- In natural language:
  - What are the objects you care about?
  - What properties/attributes of those objects are you measuring?
  - What are the relationships between them?
  - What assumptions are we making? (E.g. sizes, cardinalities)
  - What is the workload on the database (Read-only? Read/write?)
  - Permissions and privacy concerns?

# The most distinctive jargon in U.S. job listings



## The most distinctive jargon in U.S. job listings



# Description of “Miniworld”

- Project: We want to analyze political trends surrounding 2020 primary candidates
- Plan: Crawl Twitter for posts from or about 2020 primary candidates. We want to analyze the spread of opinions, through following/follower relationships, share/retweet chains, and language use

# Description of “Mineworld”

- Objects used:
- Domains of attributes of objects:
- Identifiers, references / relationships:
- Cardinalities:
- Distributions:
- Workload:
- Priorities and service level agreements:

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# Description of “Miniworld”

- Objects used: *People, Tweets, Candidates*
- Domains of attributes of objects: *Tweets have timestamps (date), authors (Person), text (max 140 characters), attachments, hashtags...*
- Identifiers, references / relationships:
- Cardinalities:
- Distributions:
- Workload:
- Priorities and service level agreements:

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- Domains of attributes of objects: **Tweets have timestamps (date), authors (Person), text (max 140 characters), attachments, hashtags...**
- Identifiers, references / relationships: **People have unique IDs, People author Tweets, People retweet Tweets, People like Tweets, People follow People, Tweets mention People...**
- Cardinalities:
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- Workload:
- Priorities and service level agreements:

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- Workload: scrape and populate ones, read often
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- Workload: scrape and populate ones, read often
- Priorities and service level agreements: “right to be forgotten” rules...

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Asking and  
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“Book of Duty”

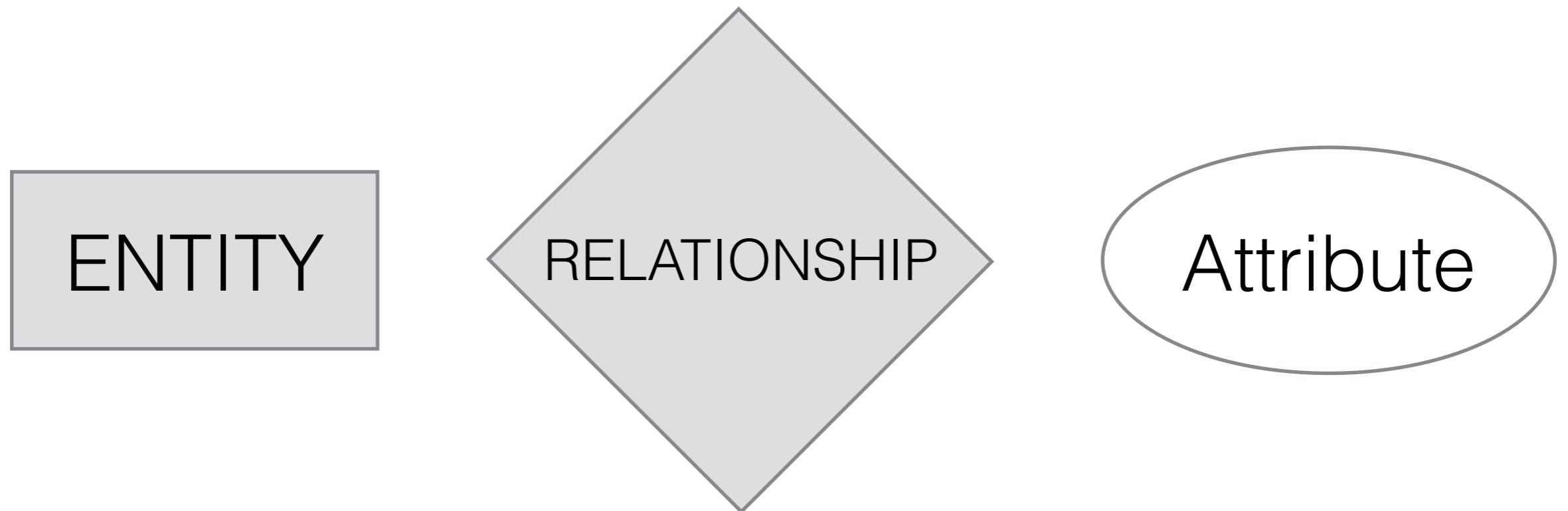
Conceptual  
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(schema, table names,  
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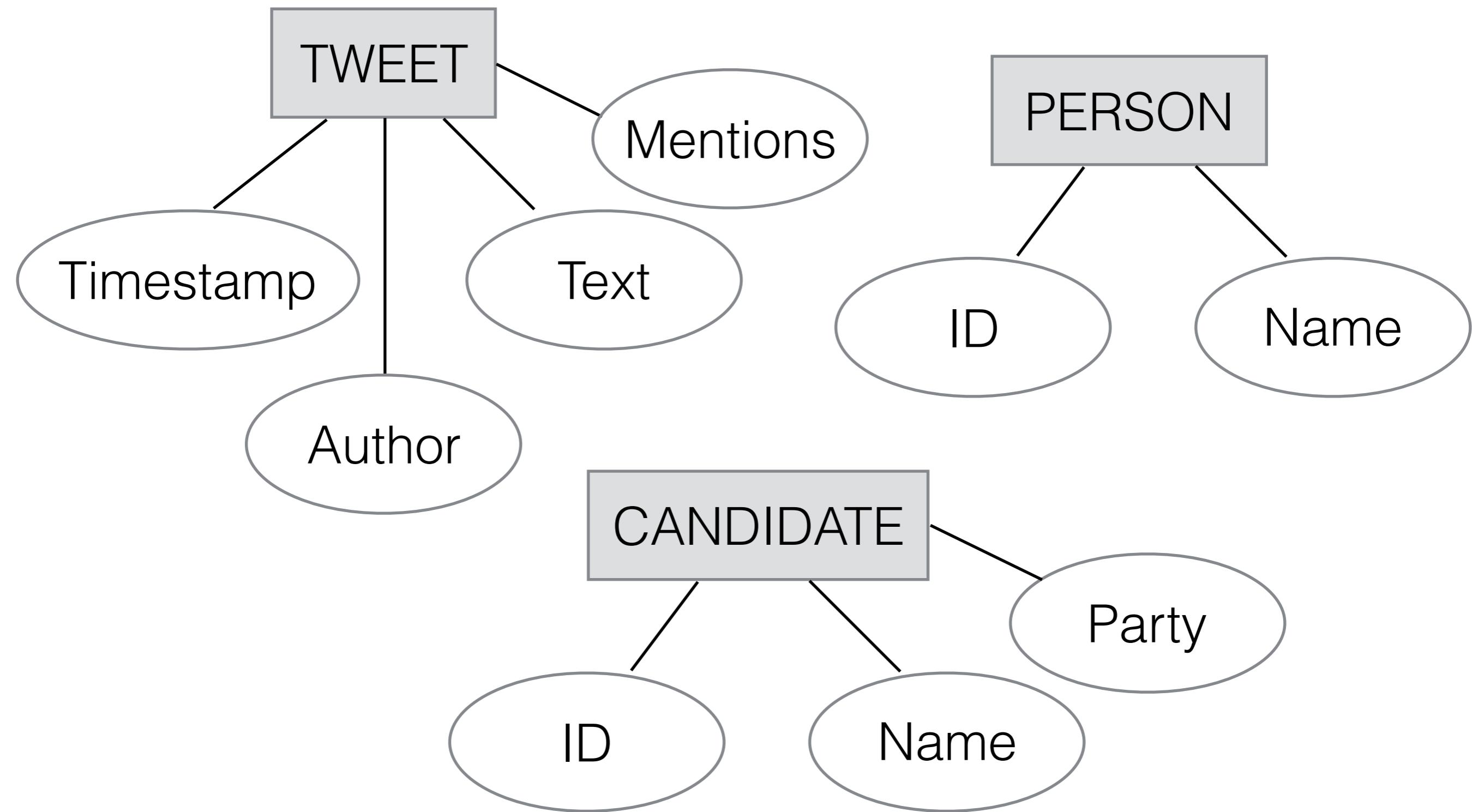
Relational Algebra,  
SQL

# Entity-Relationship (ER) Model

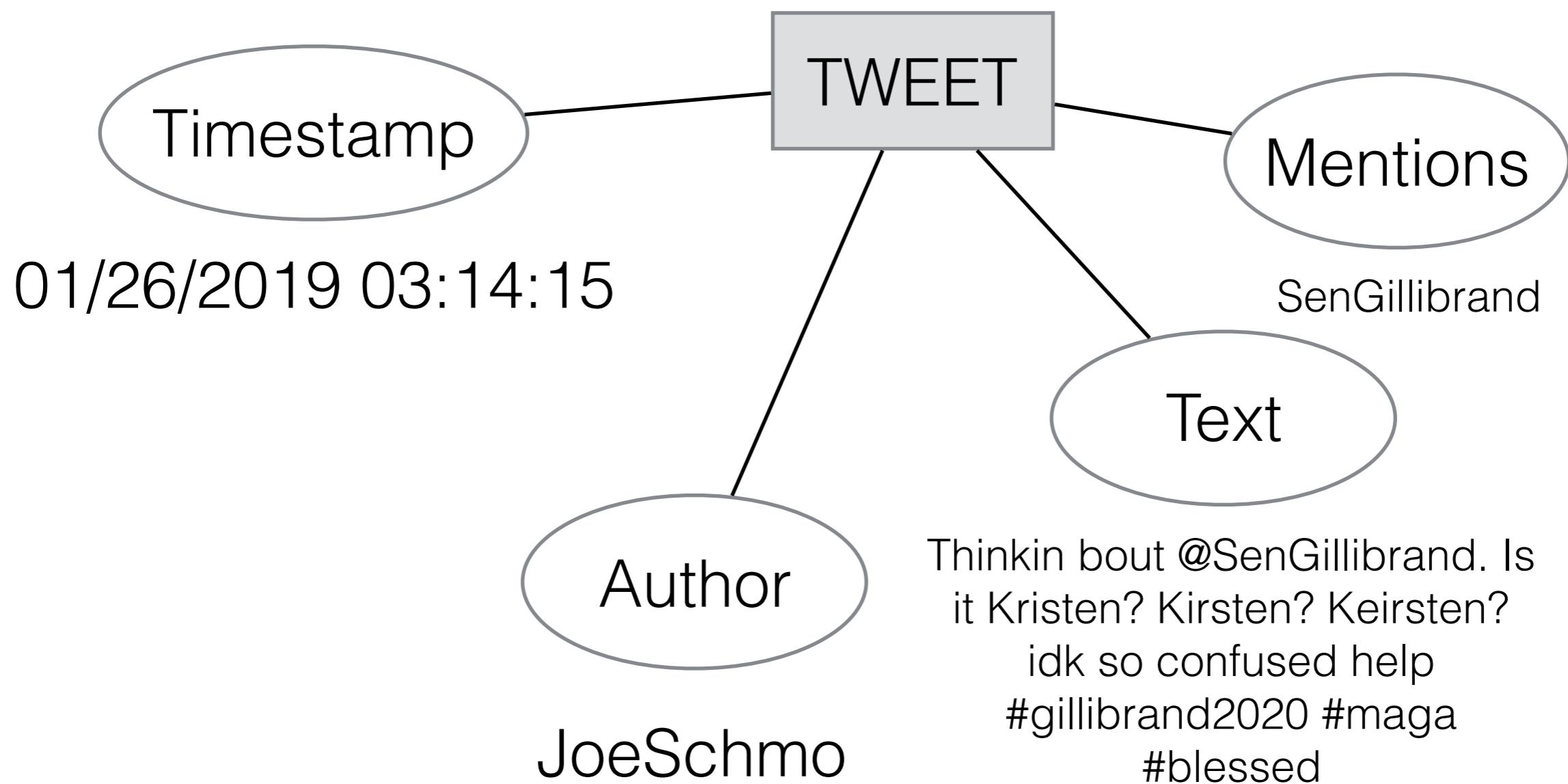
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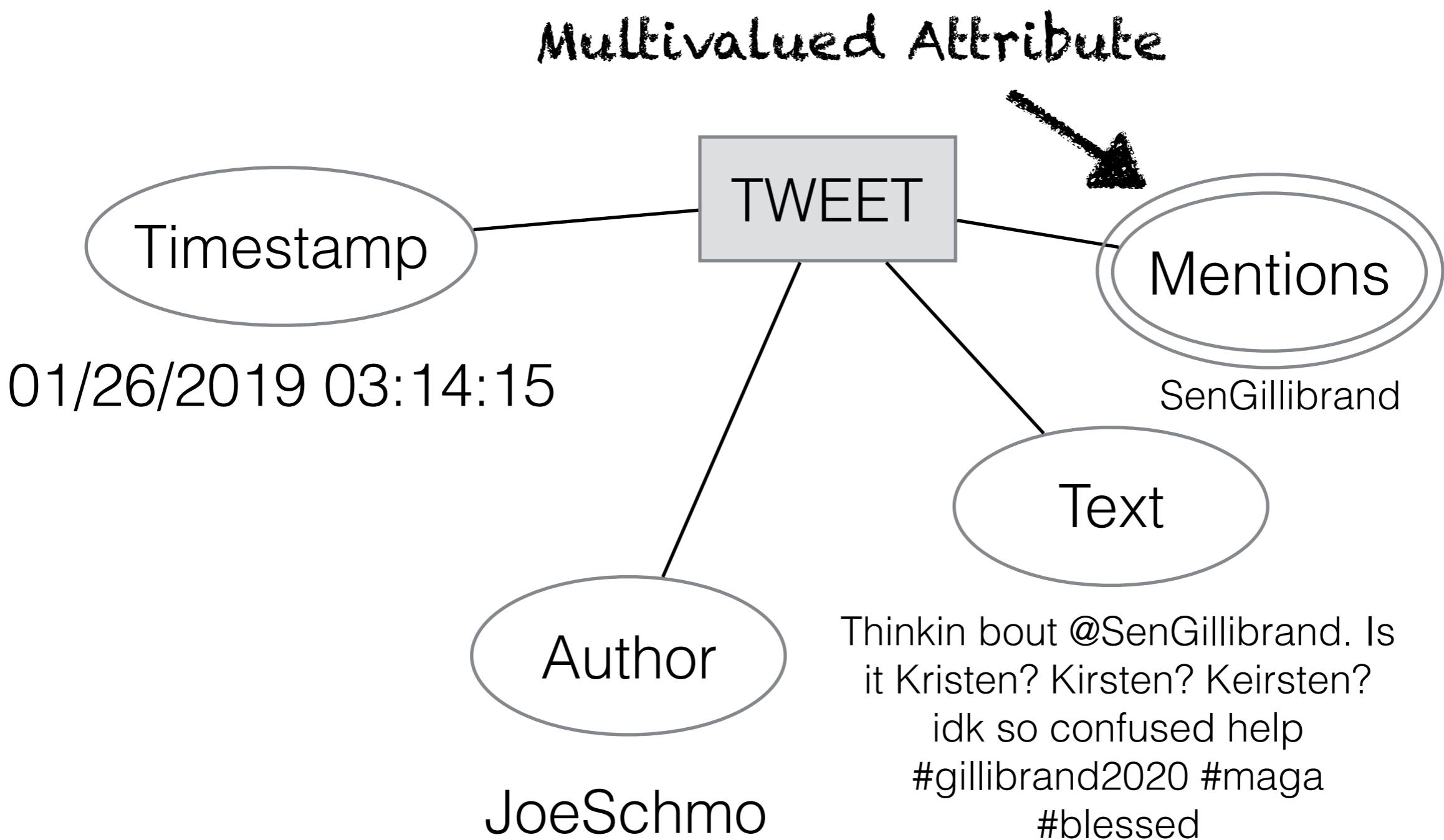
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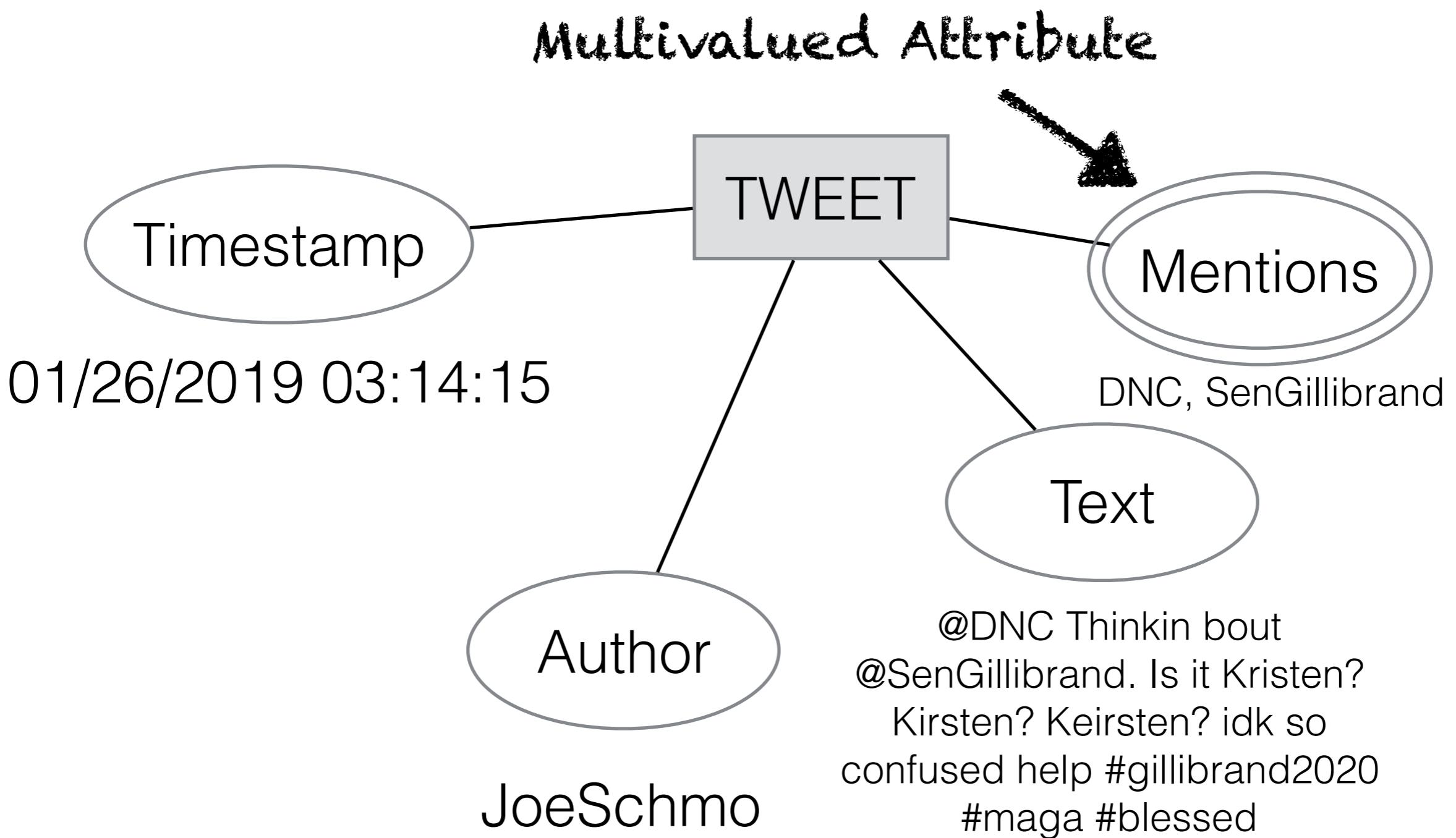
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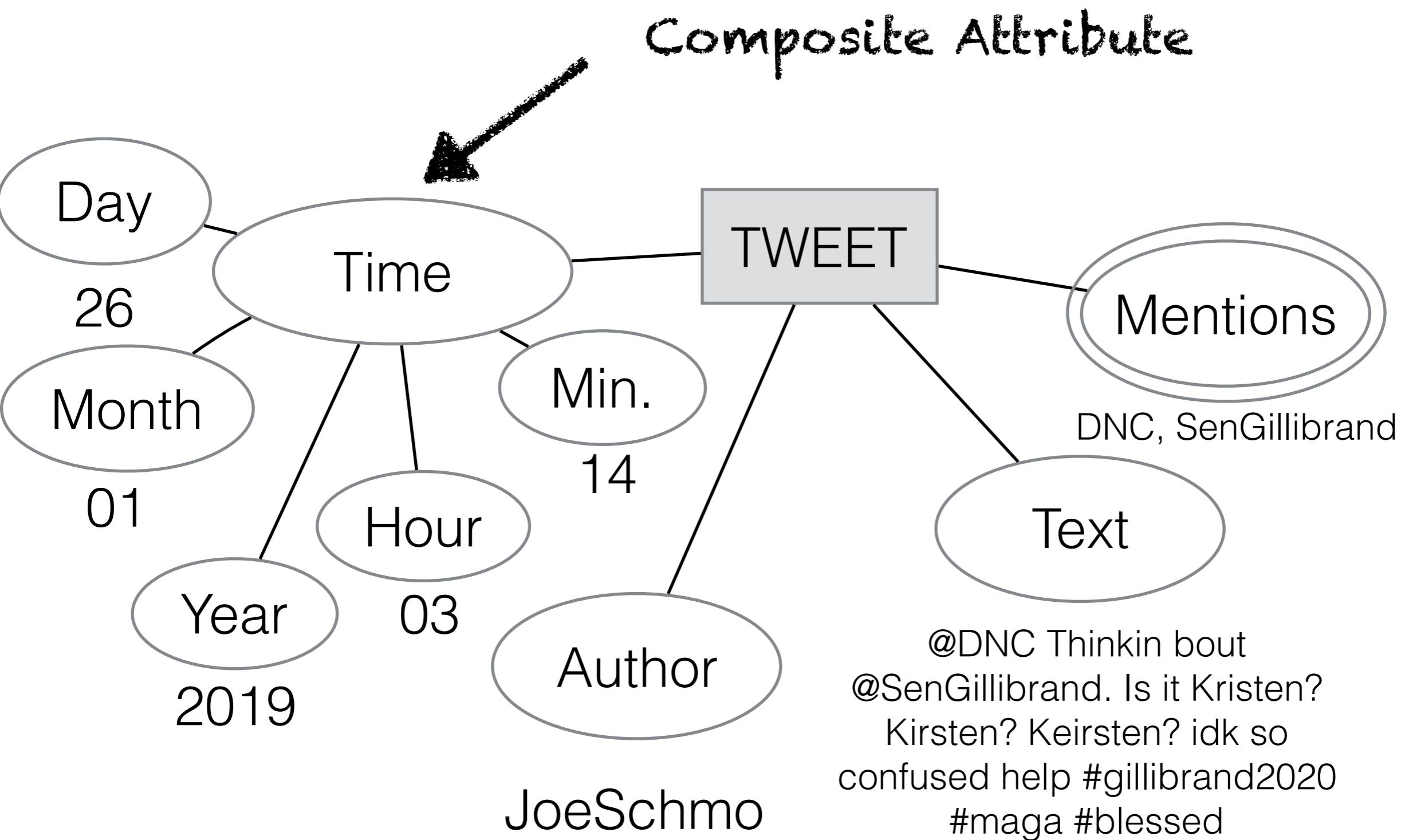
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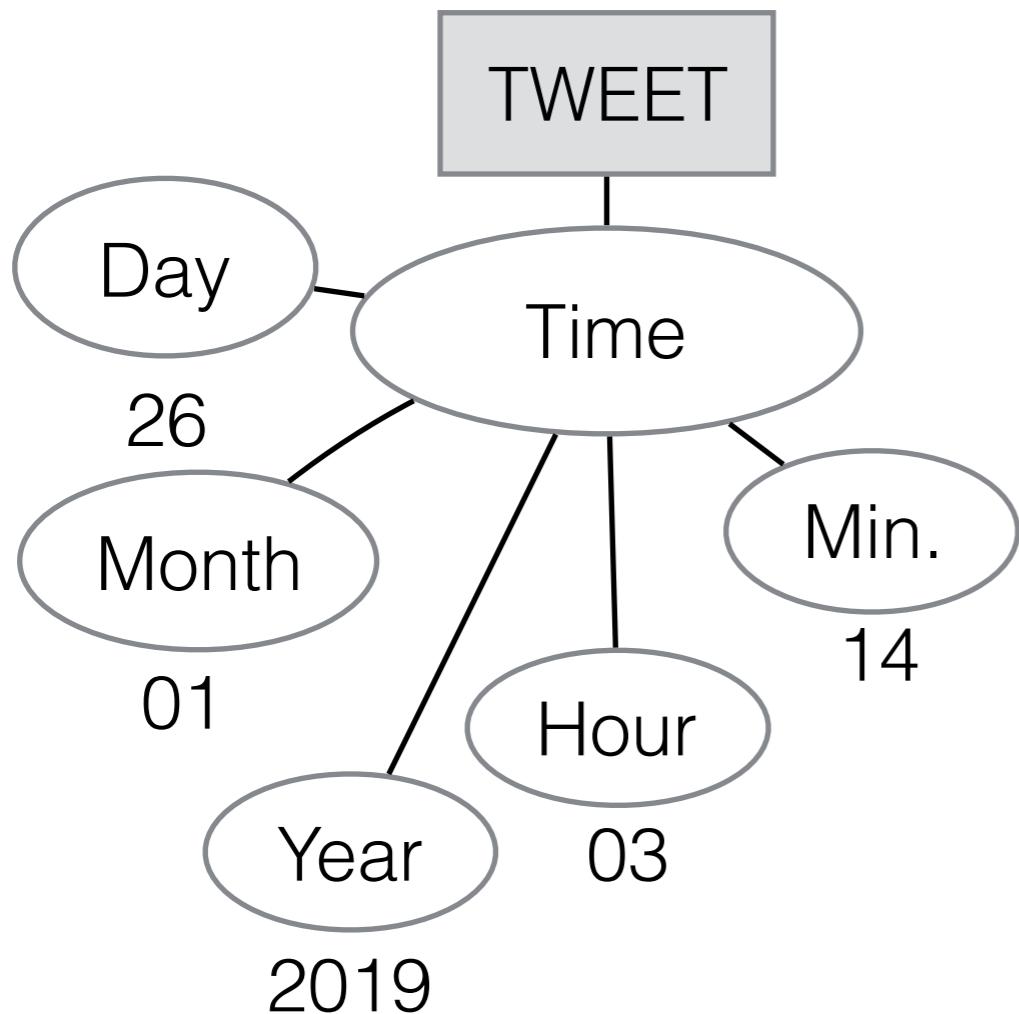


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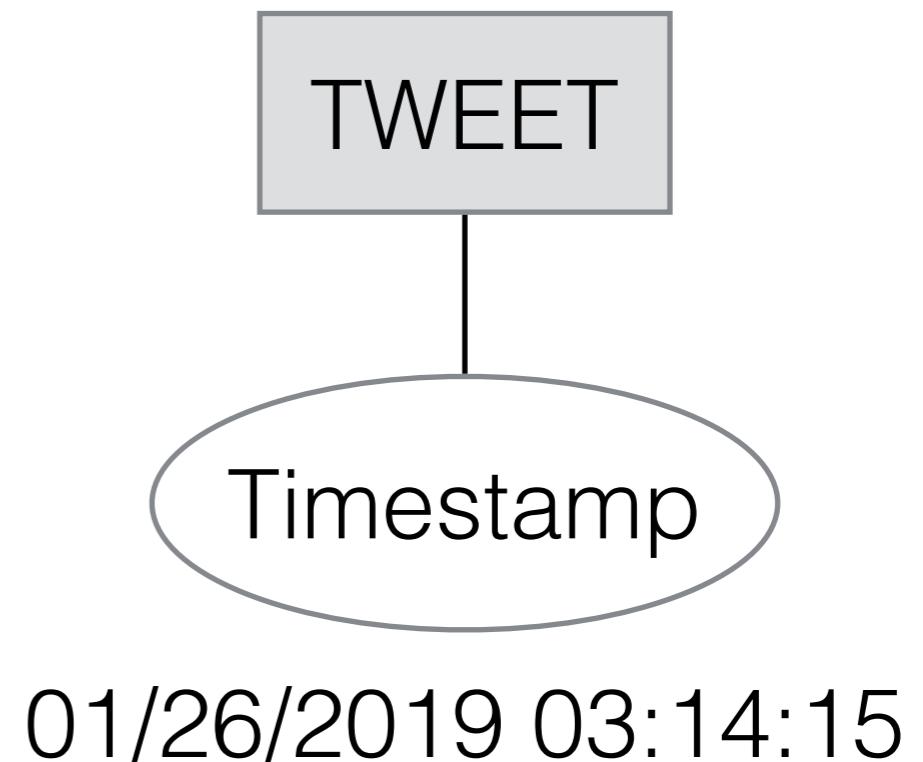


# Entity-Relationship (ER) Model

**Clicker Question!**  
**Which representation is better?**



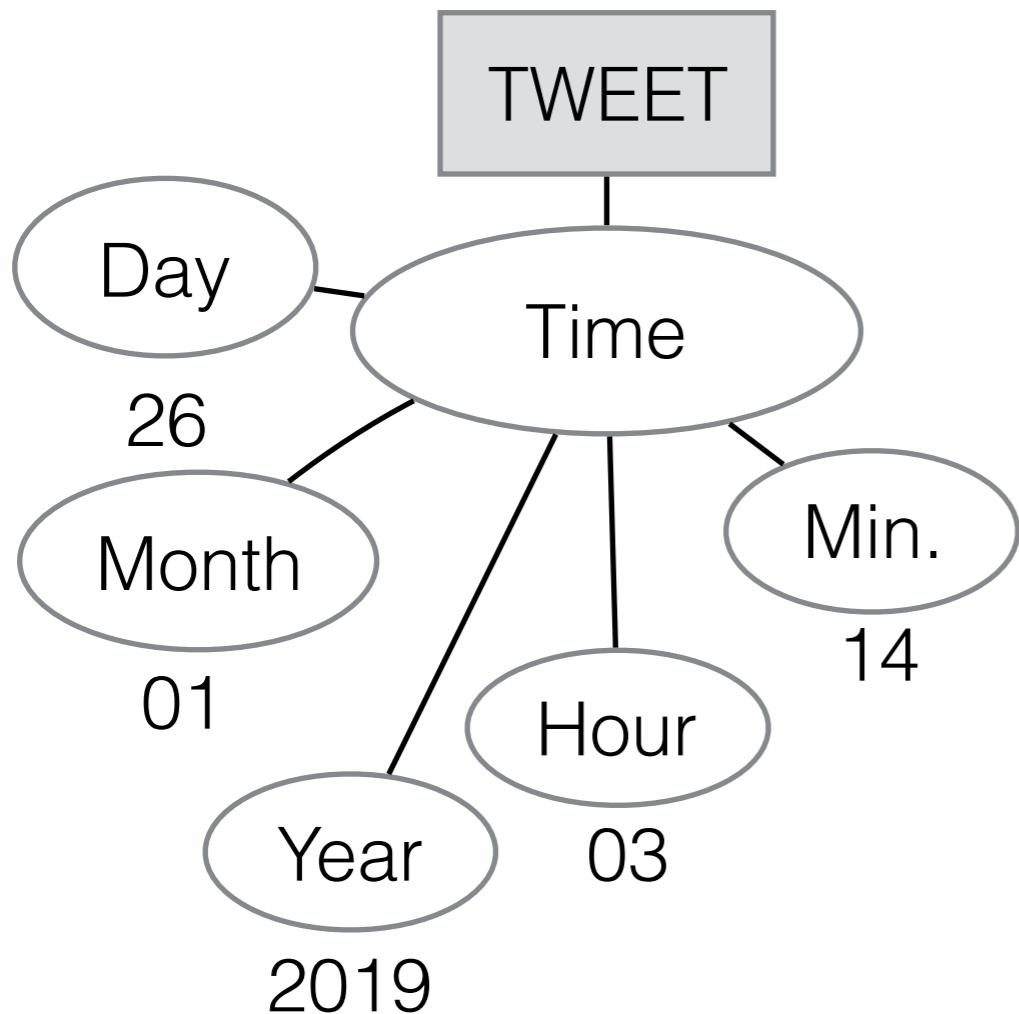
**(a) Composite**



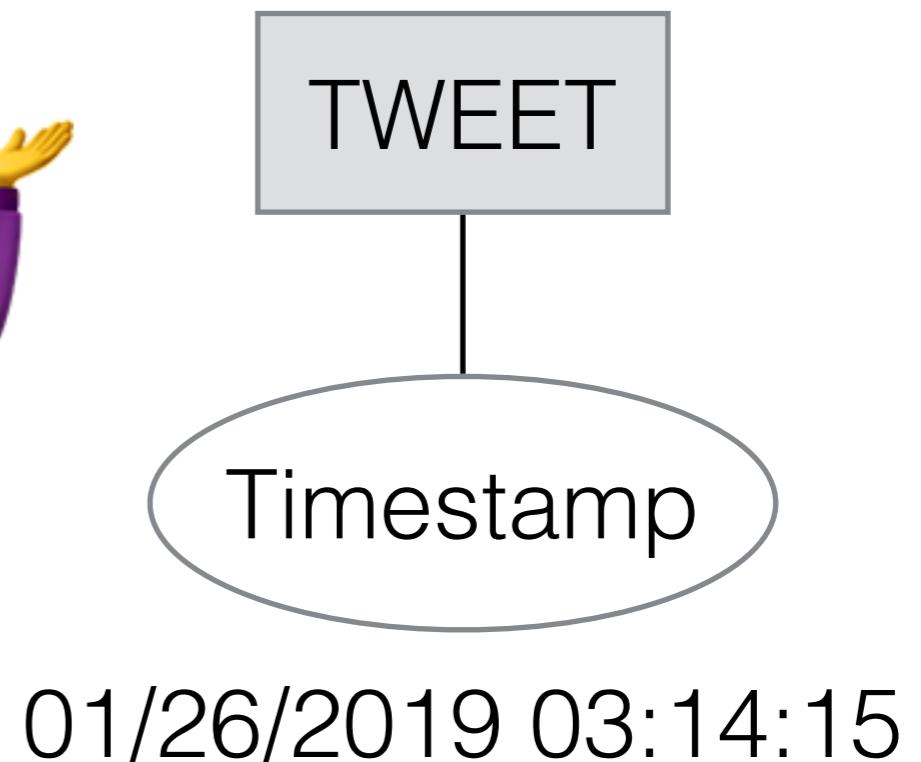
**(b) Normal**

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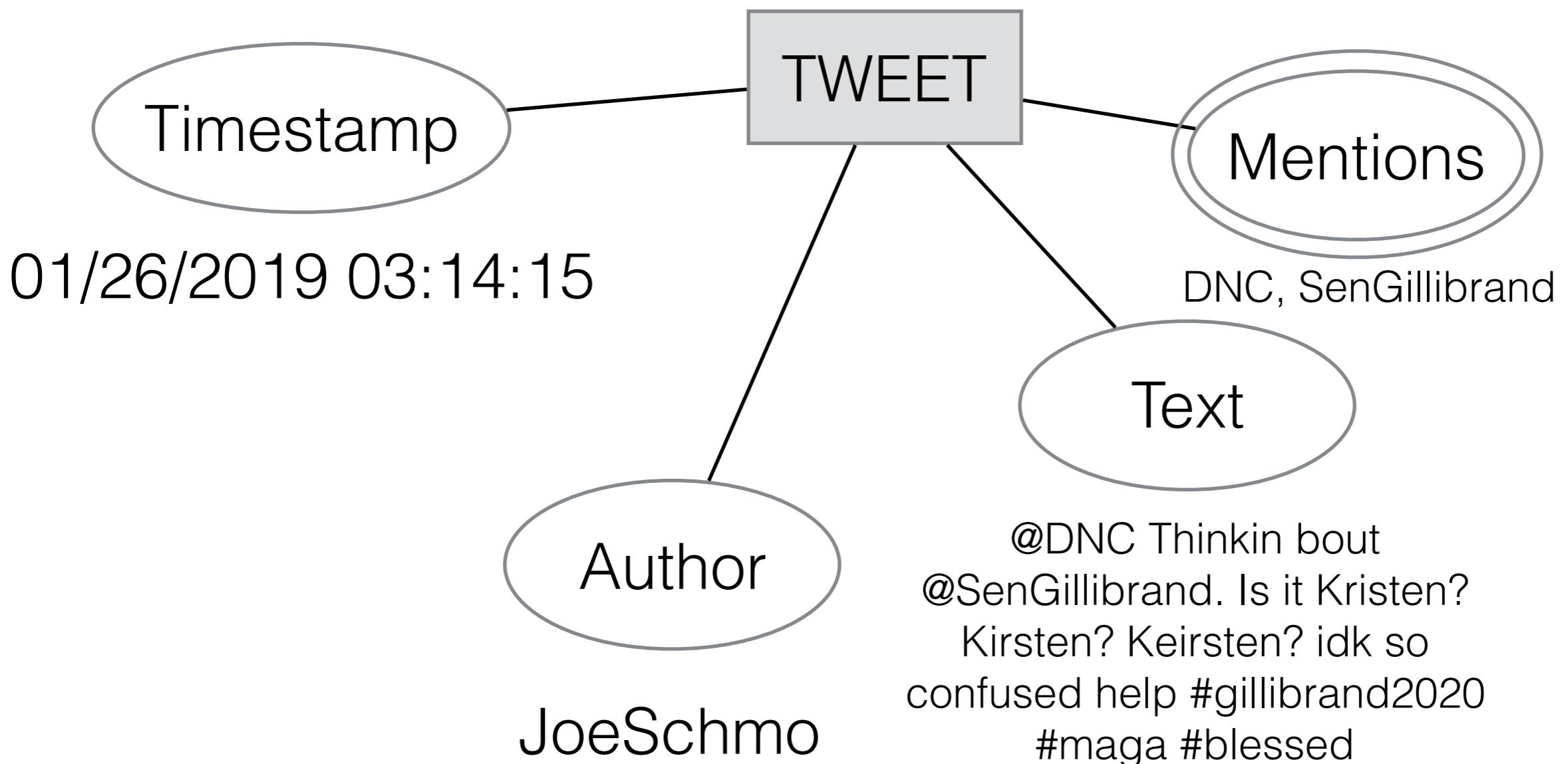
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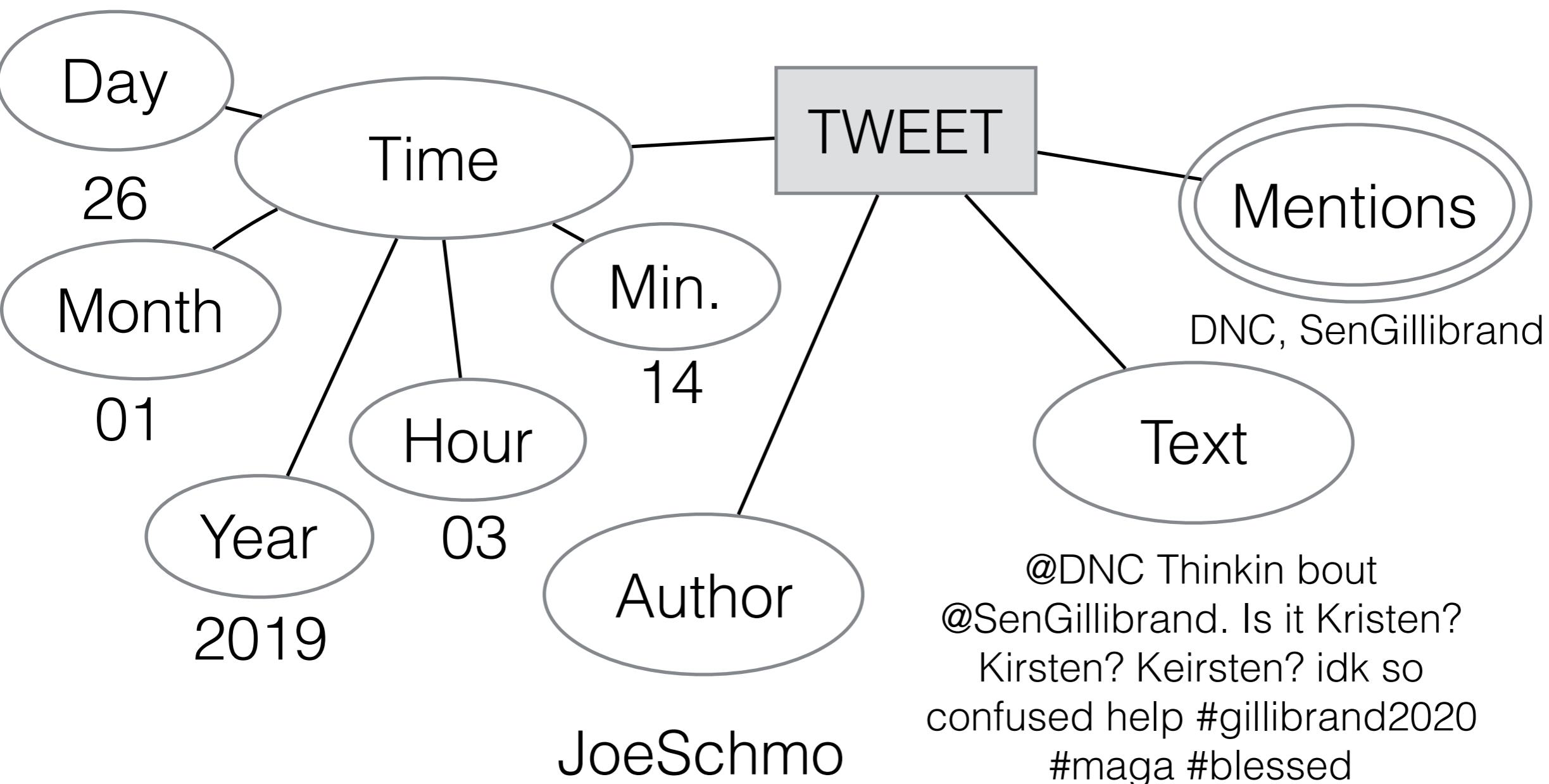
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Find all tweets sent between 2am and 4am that mention democratic primary candidates 



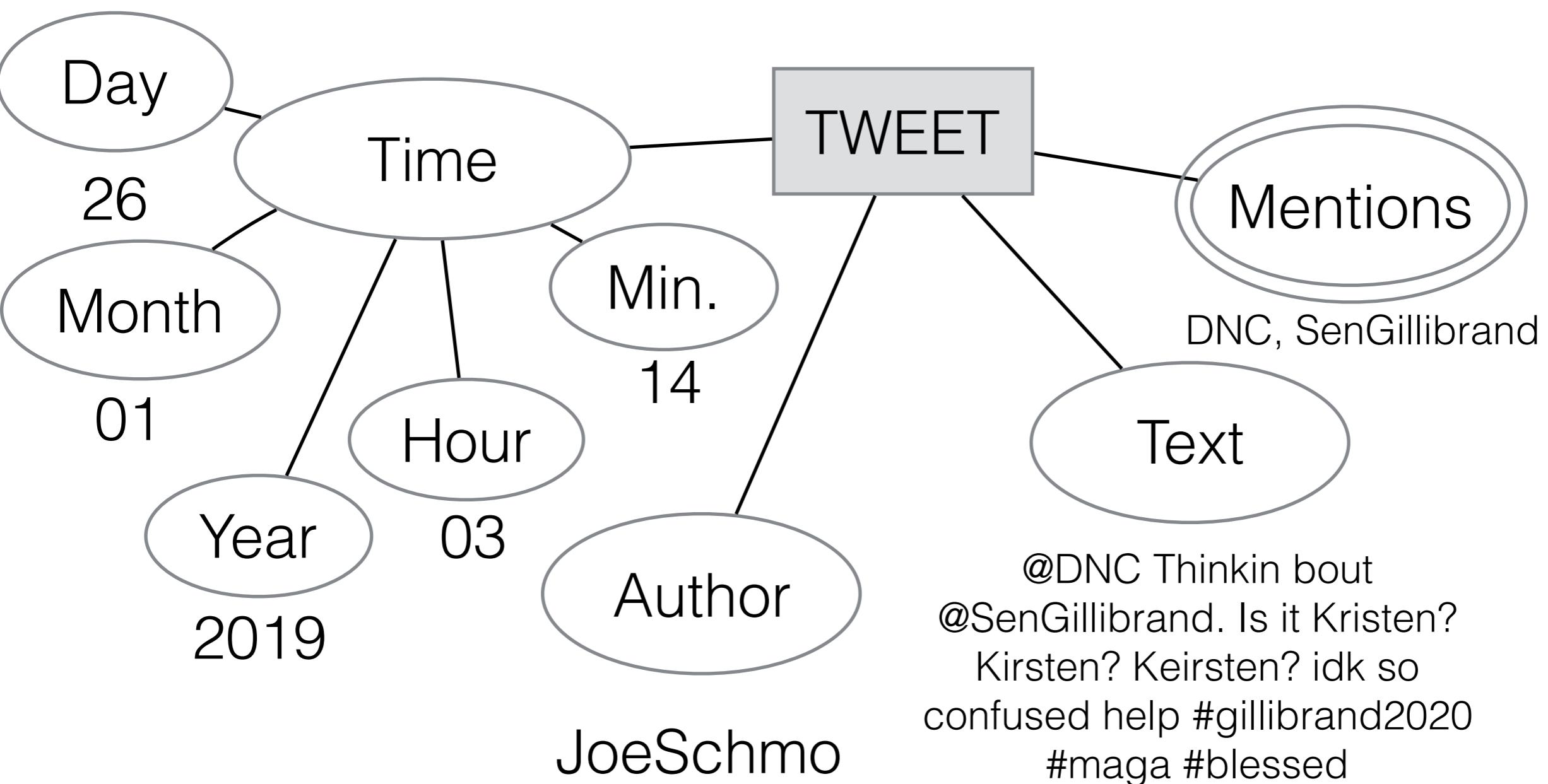
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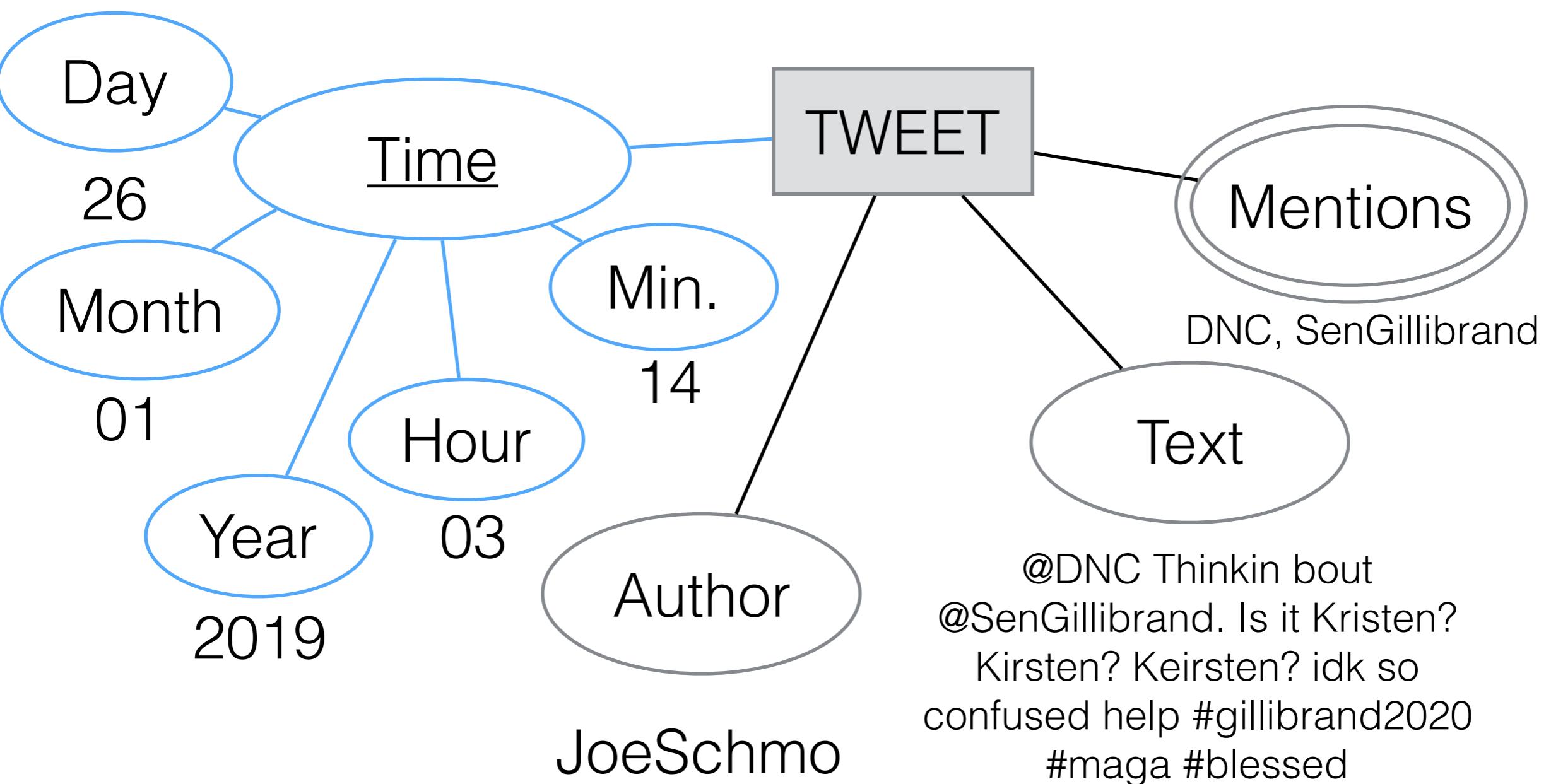
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Key Attribute...?



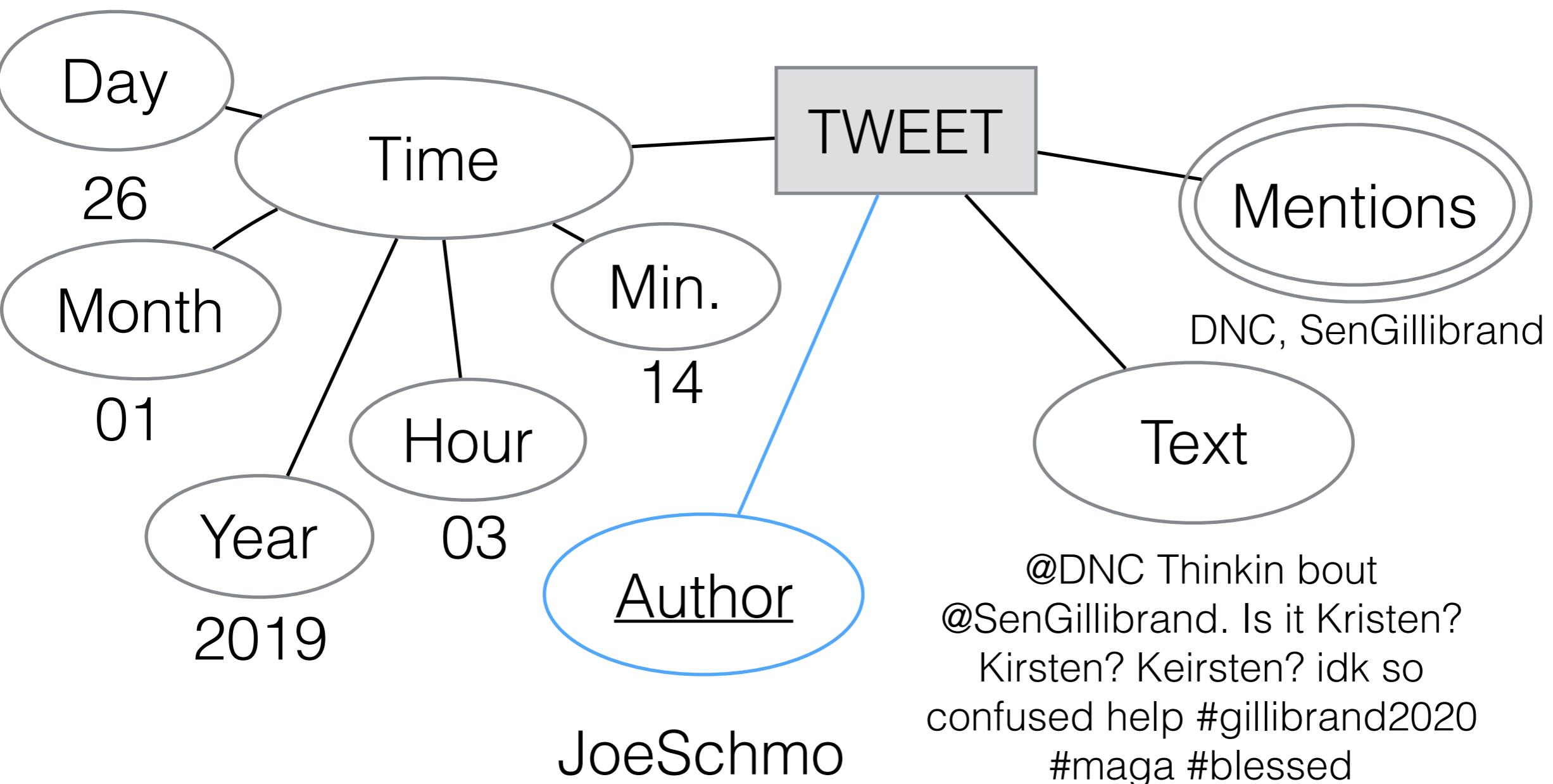
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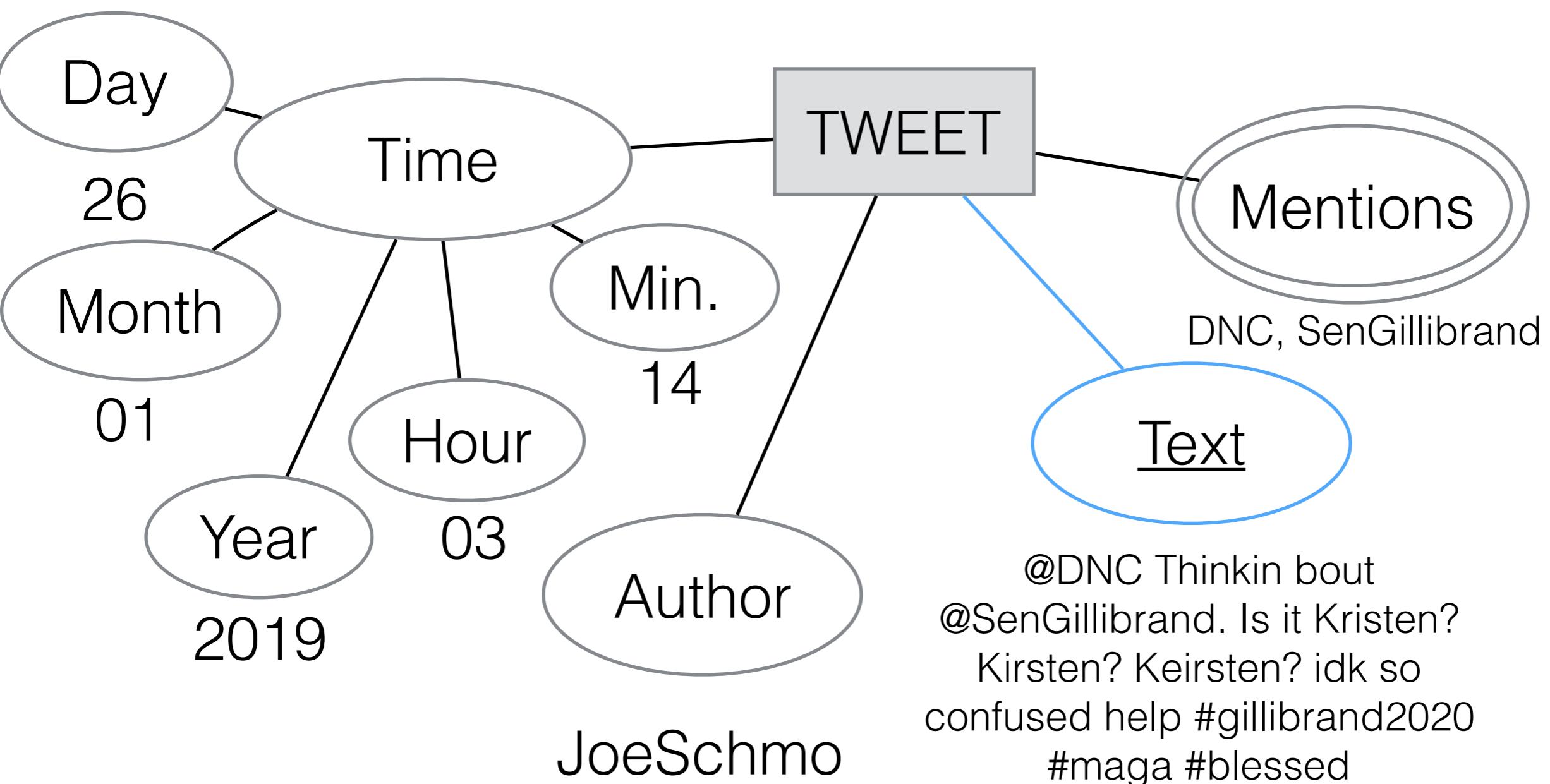
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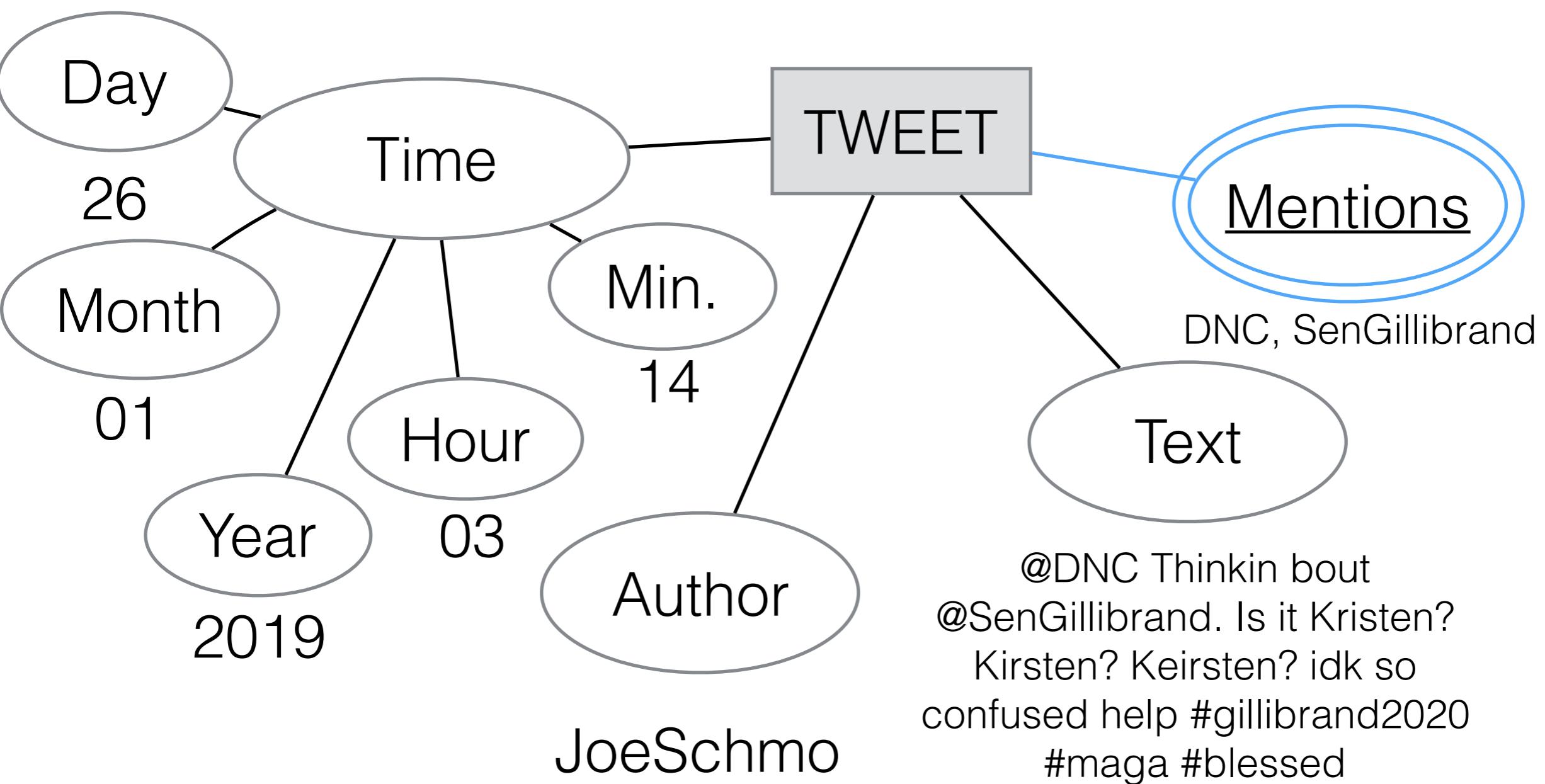
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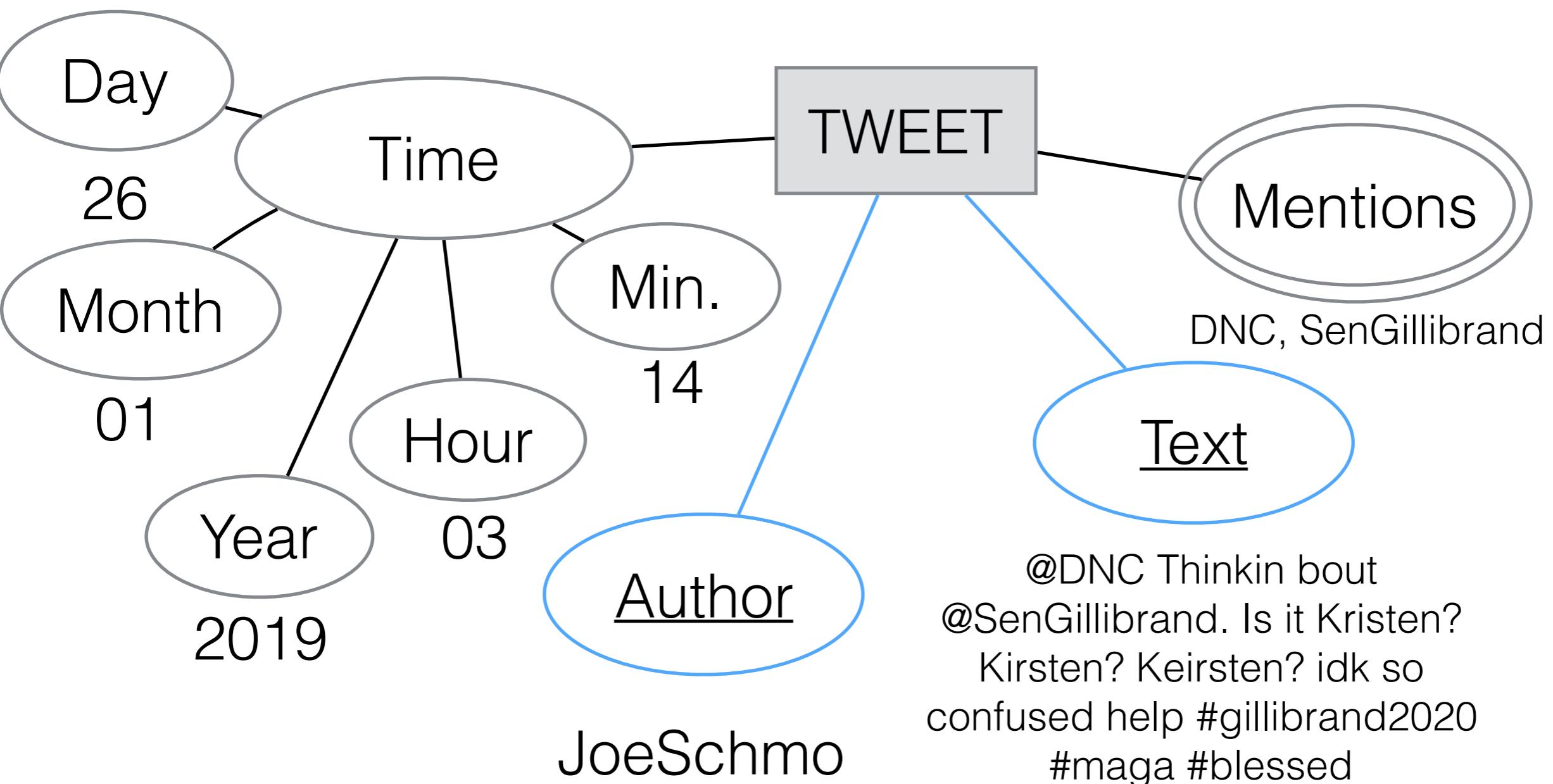
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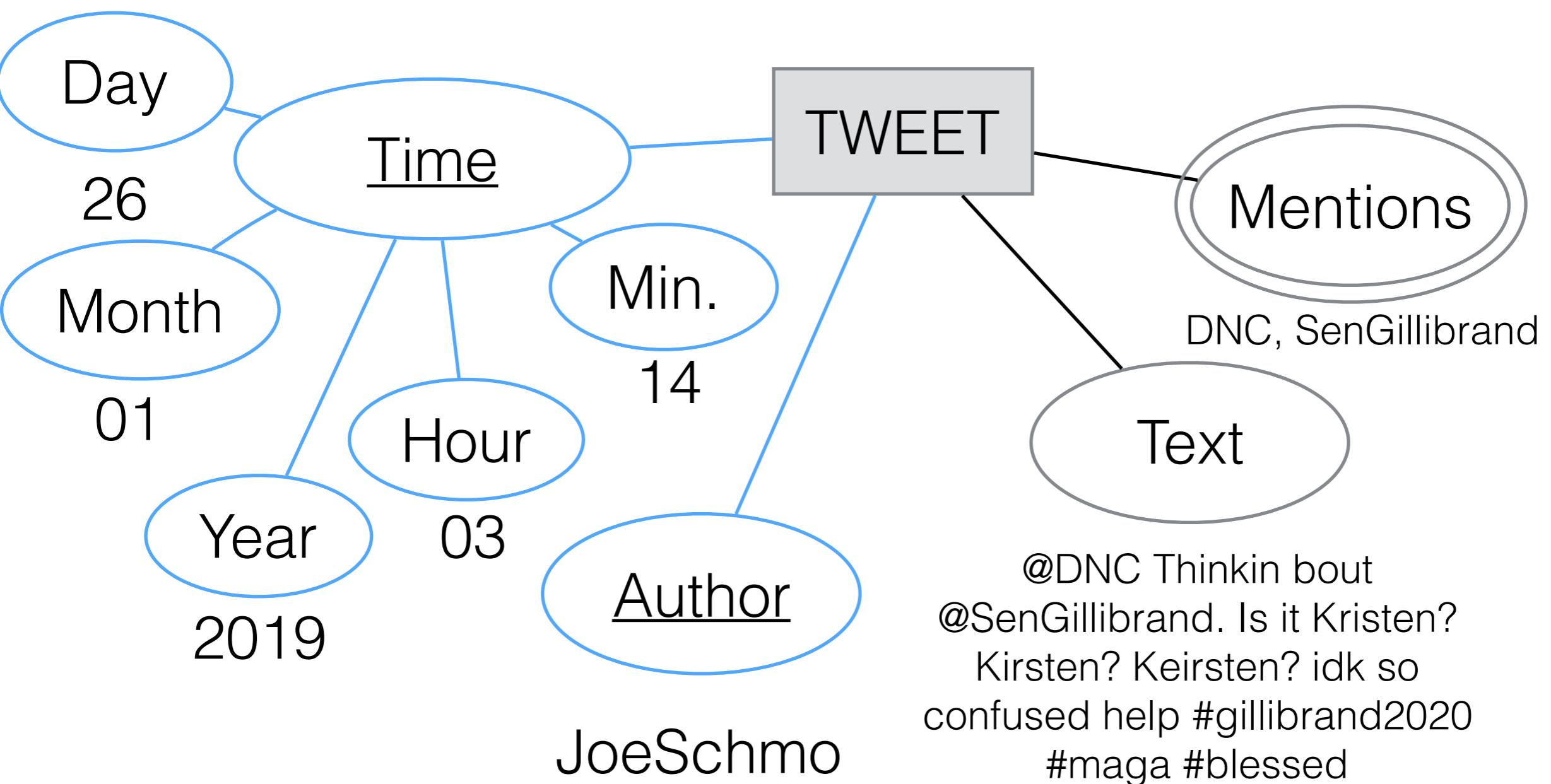
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Key Attribute...?



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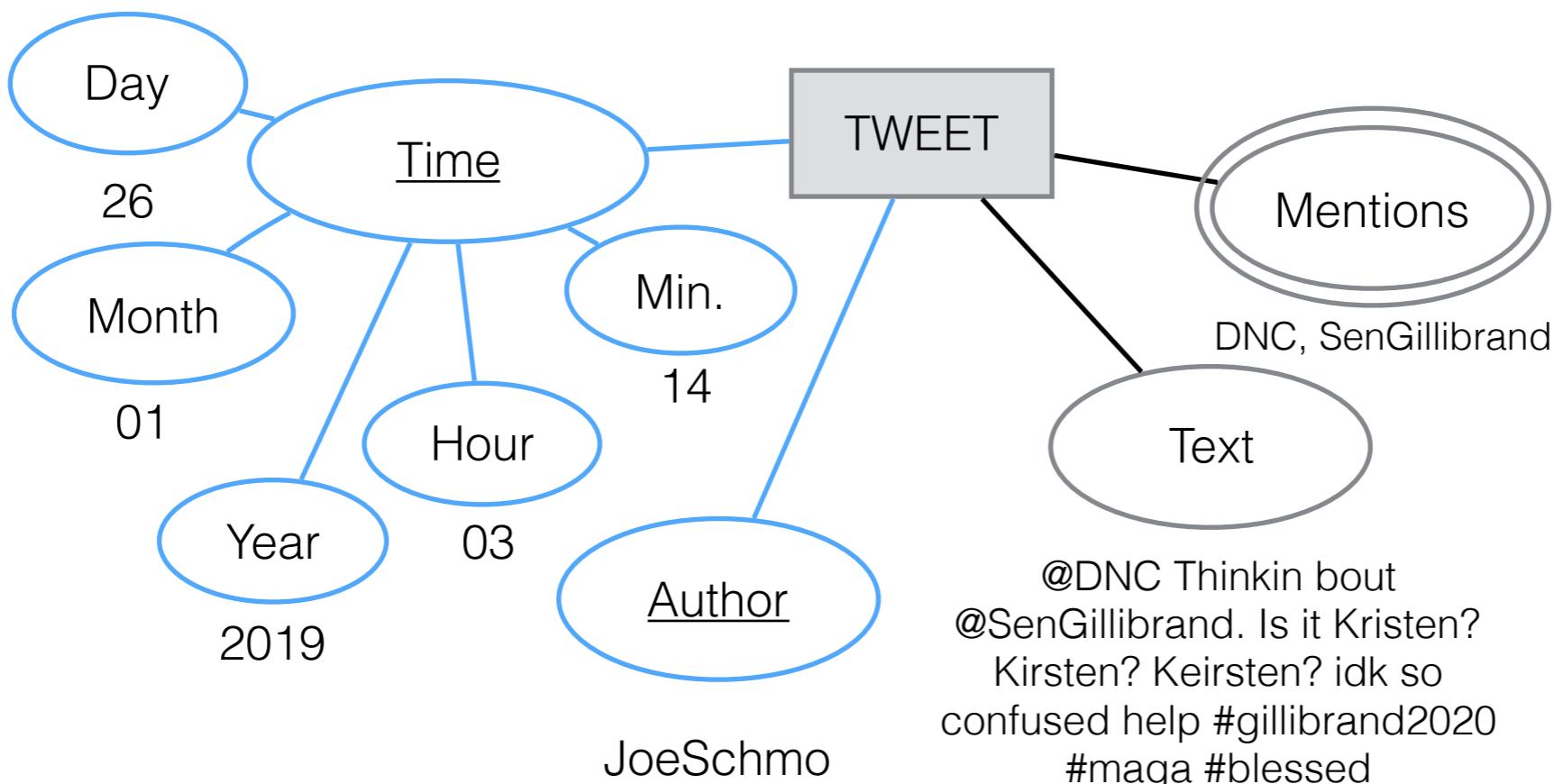
Key Attribute...?



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**Clicker Question!**

**Is it a good idea to use author +timestamp as a key?**



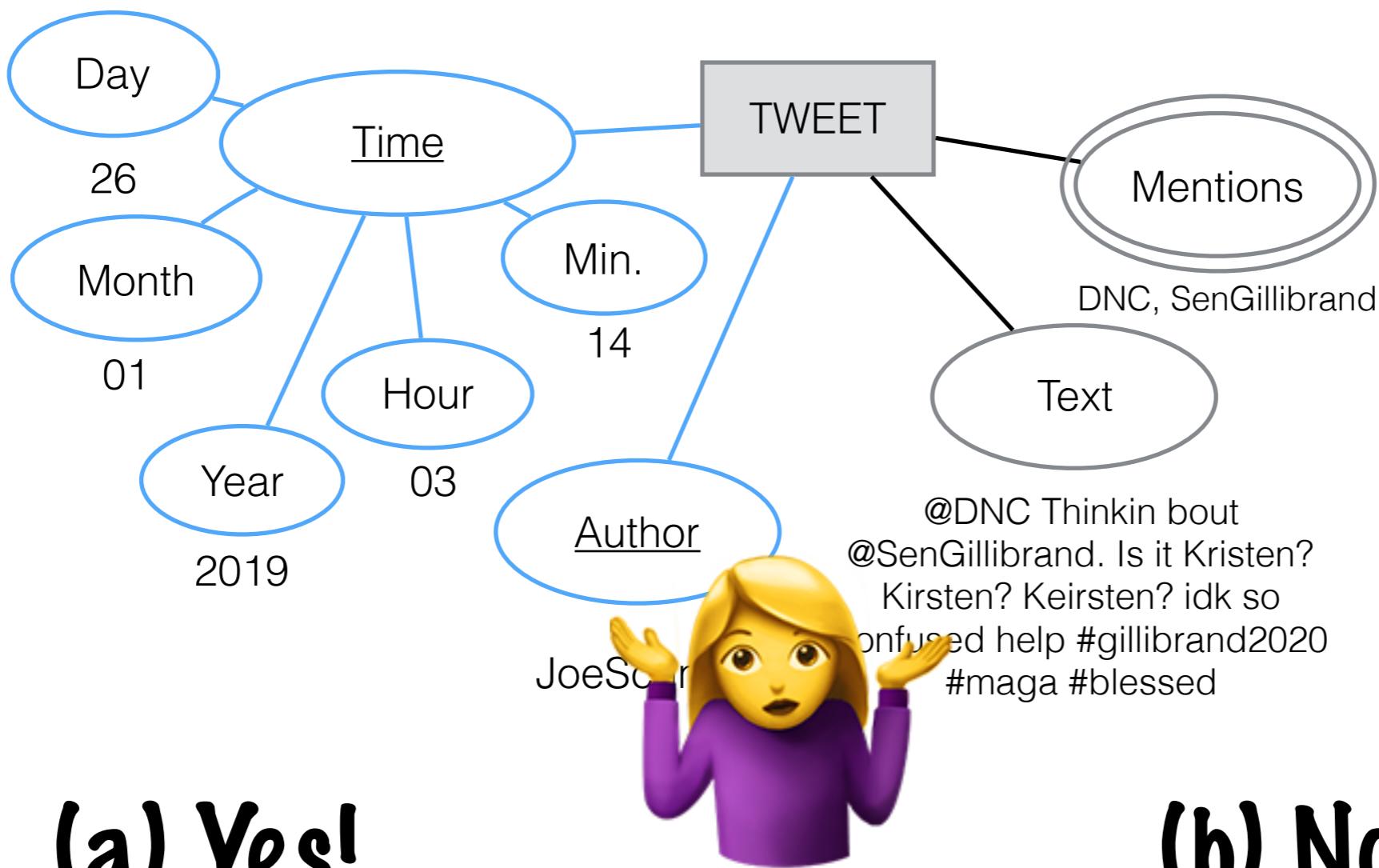
**(a) Yes!**

**(b) No!**

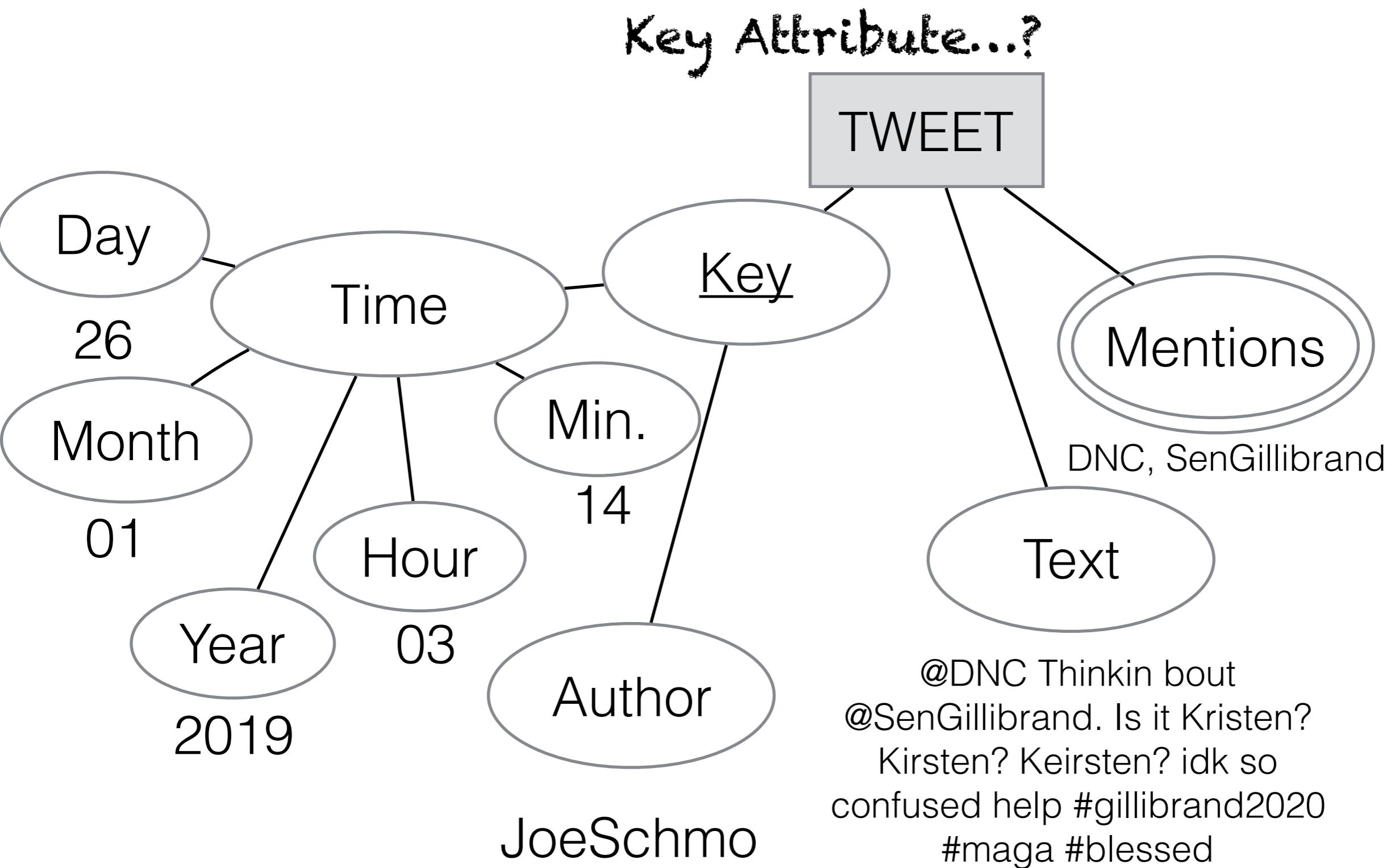
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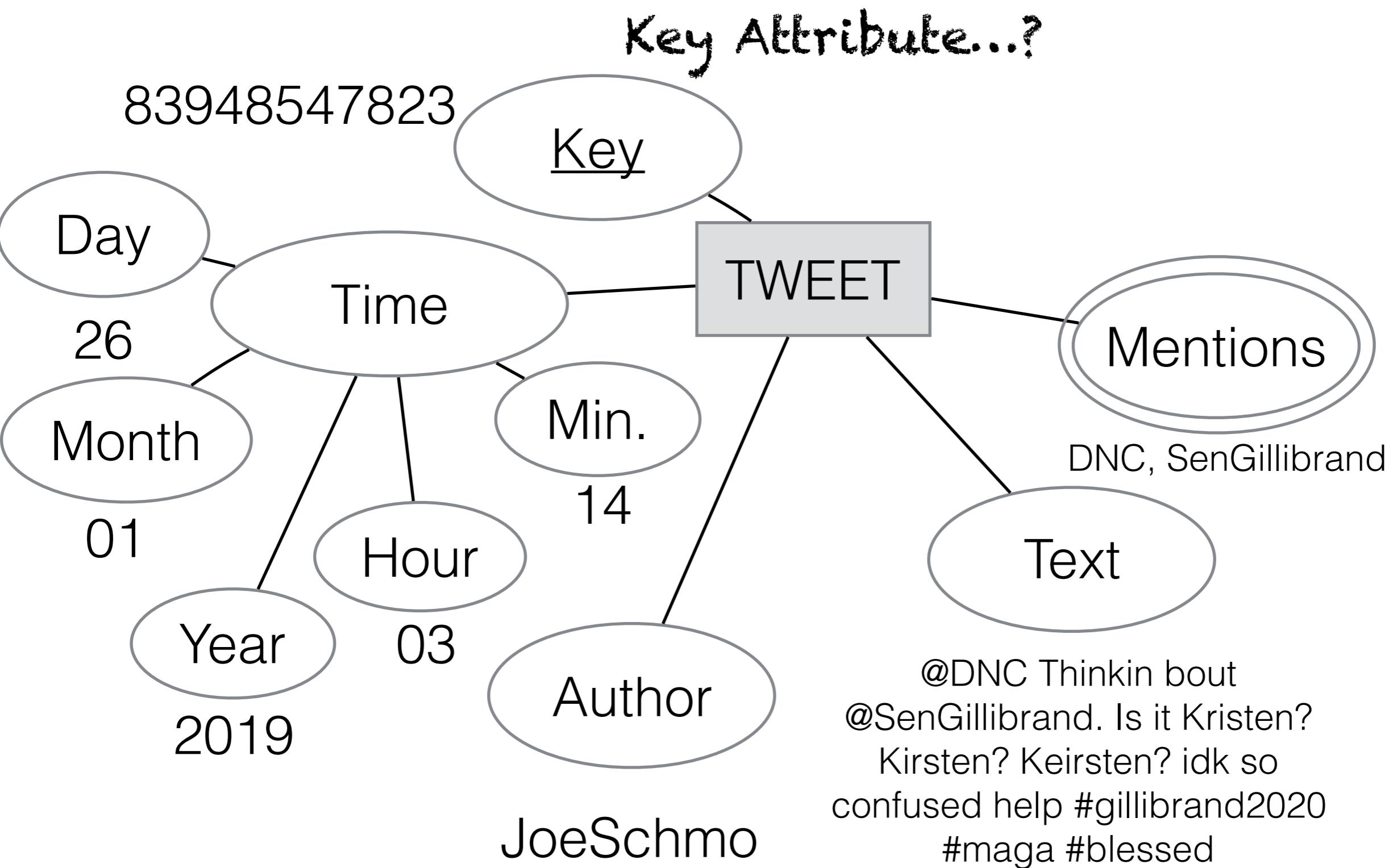
**Is it a good idea to use author +timestamp as a key?**



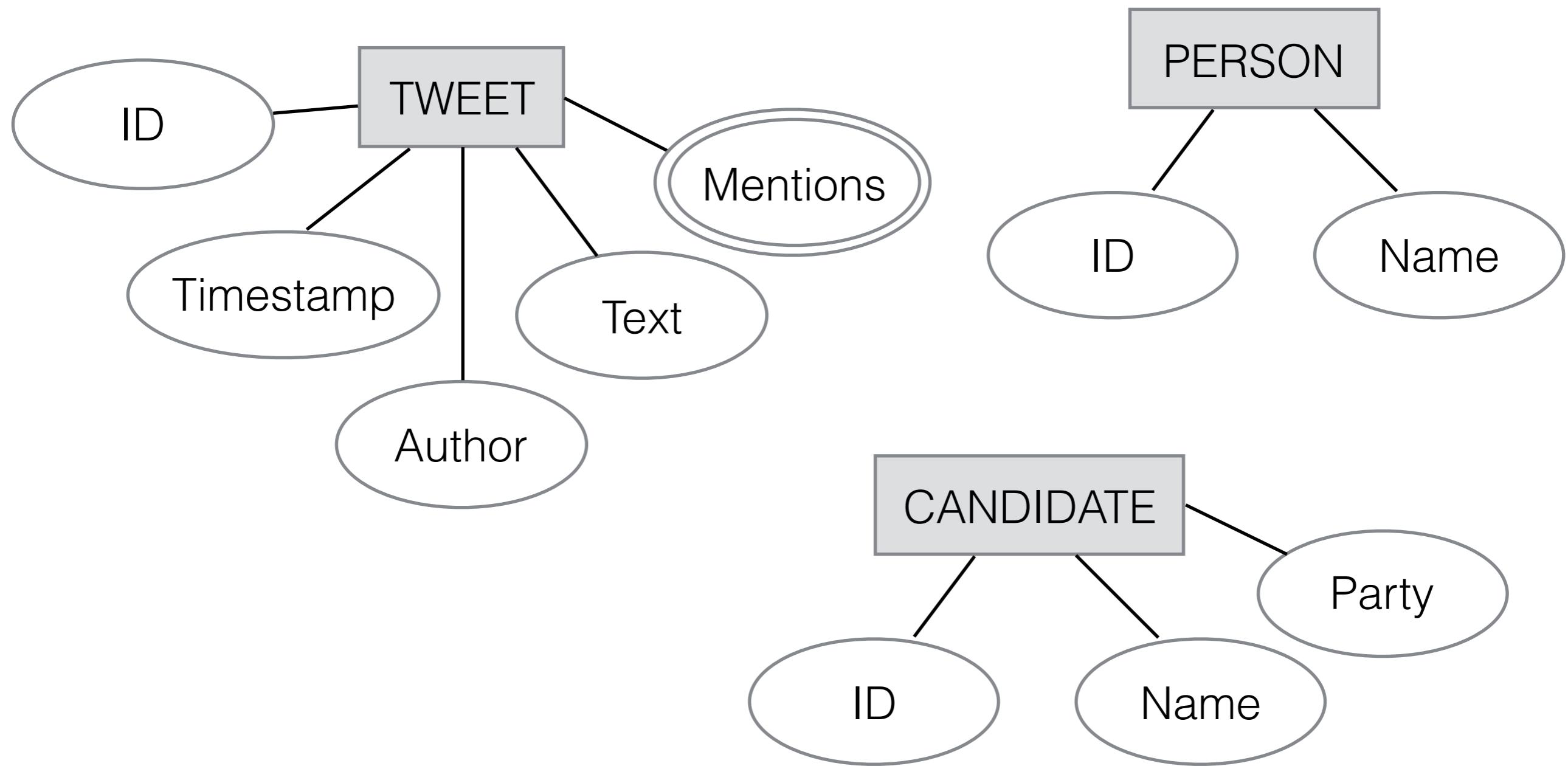
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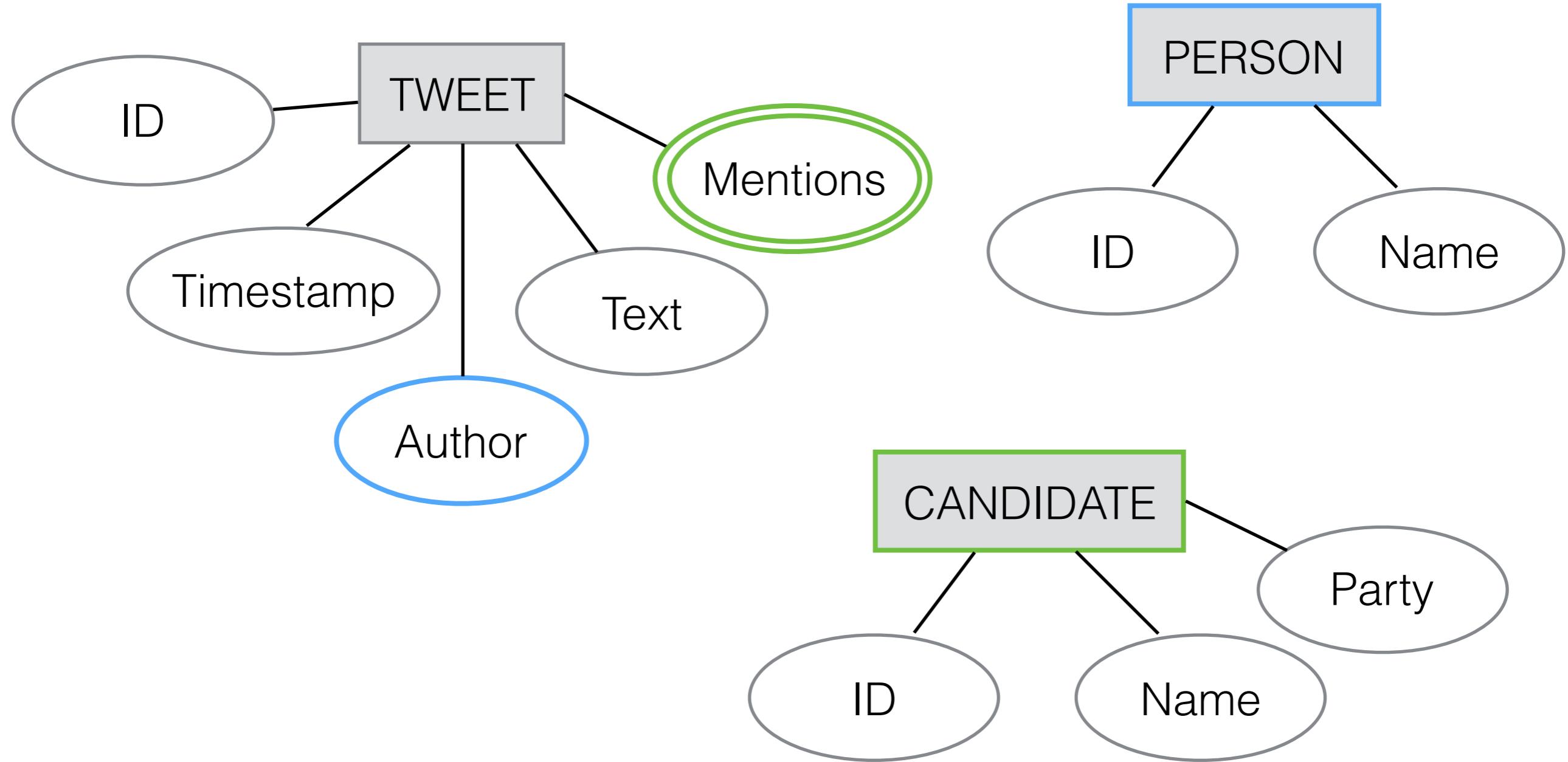
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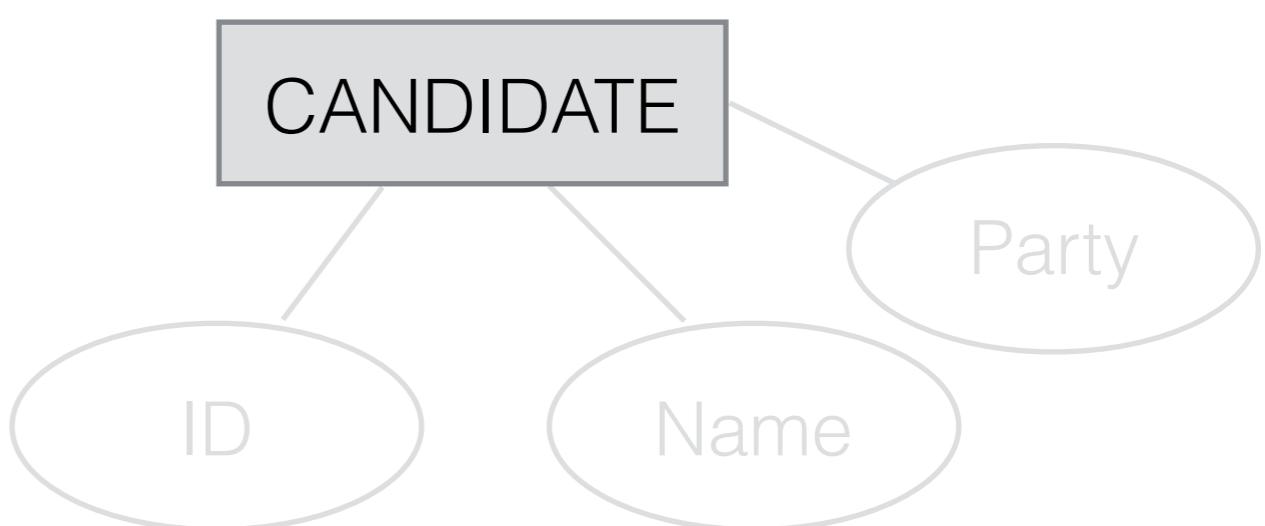
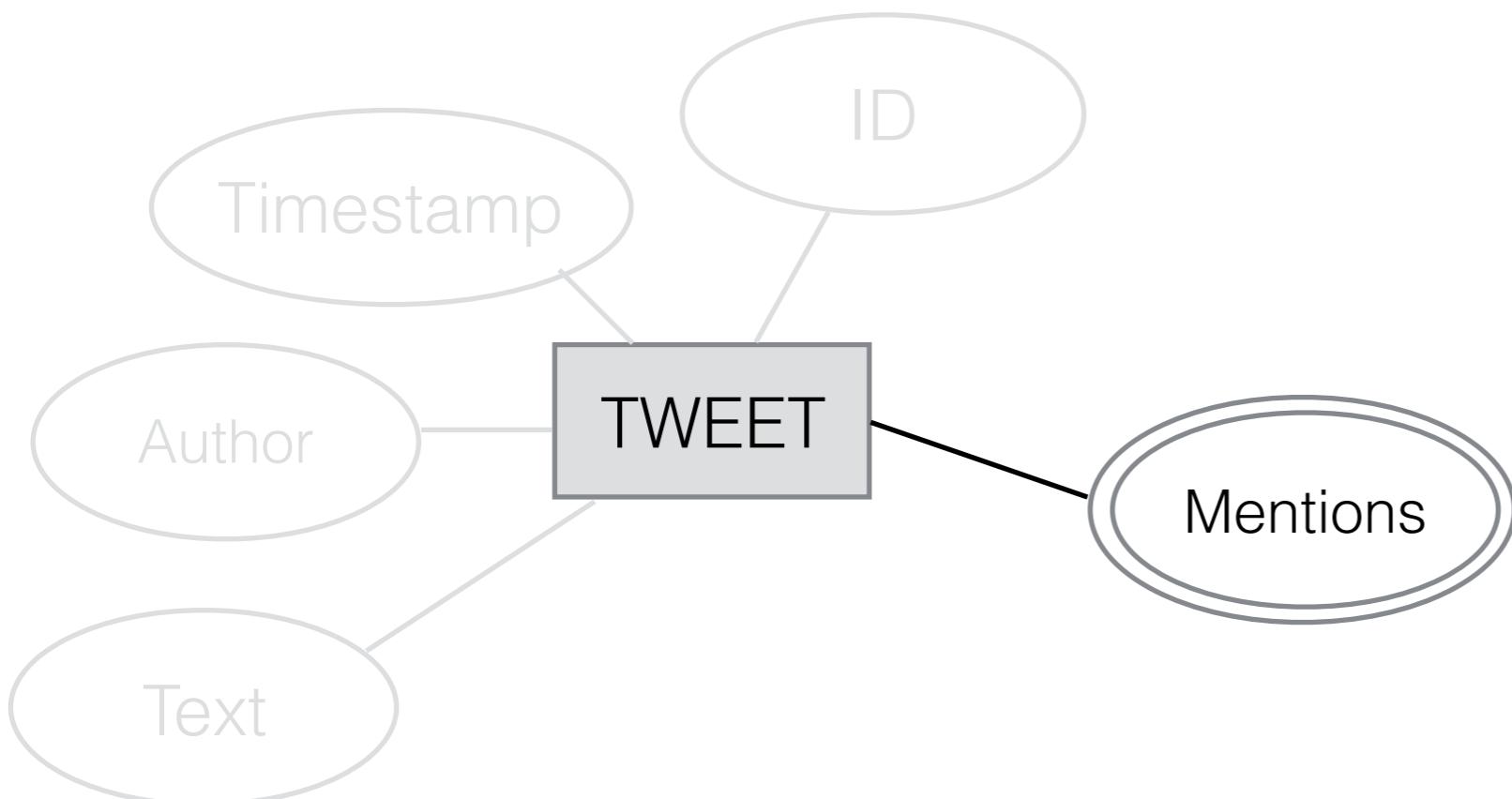
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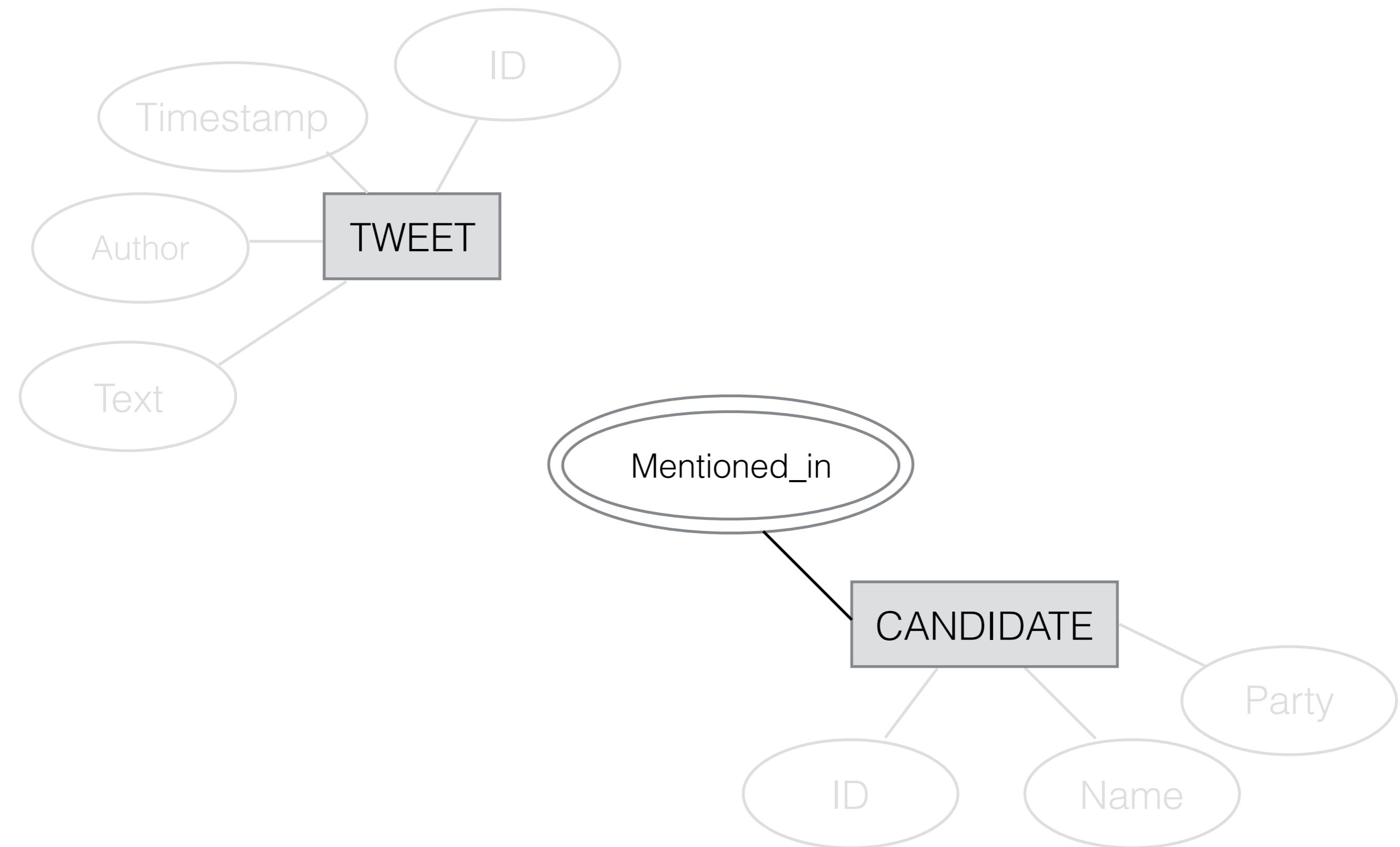
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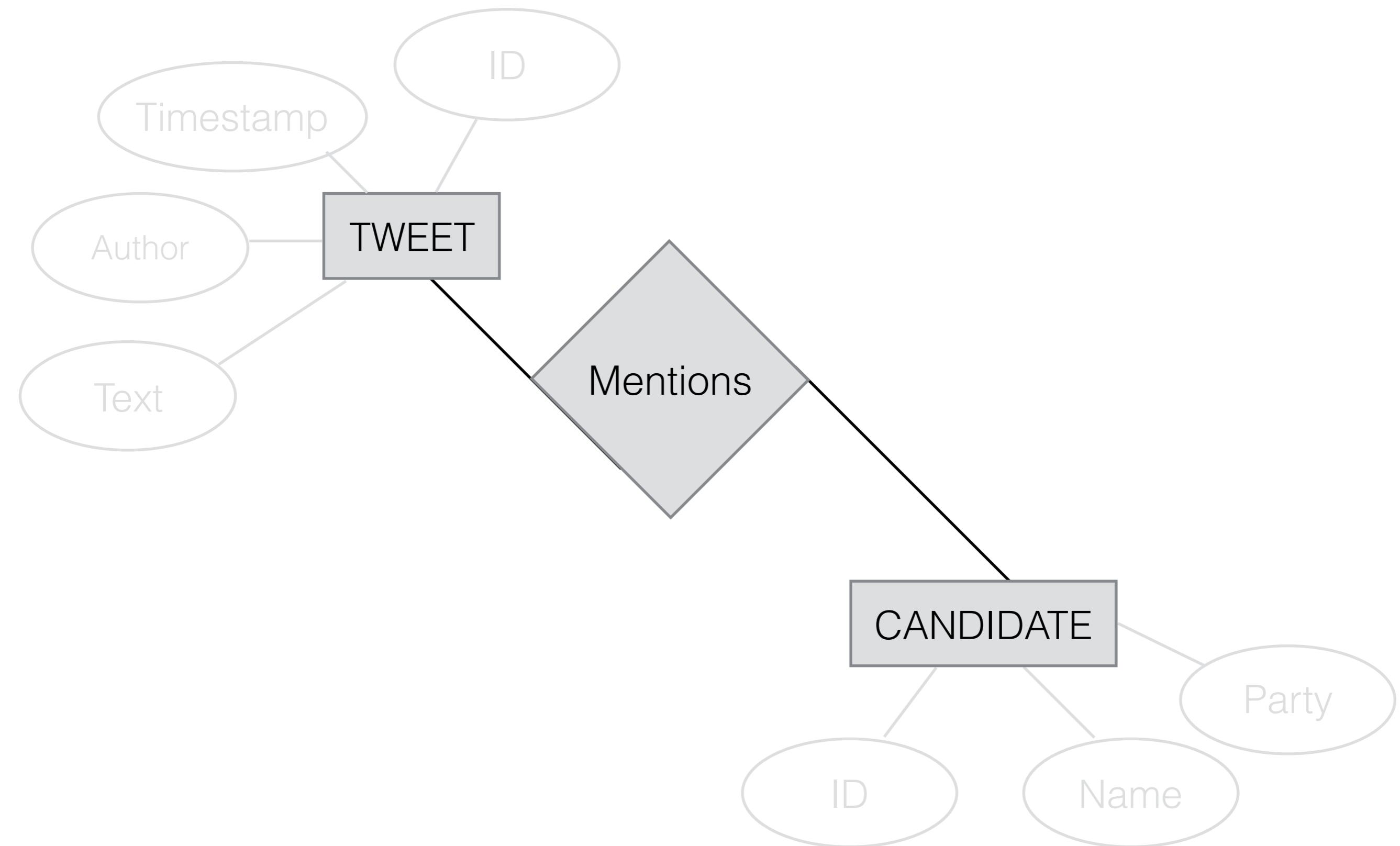
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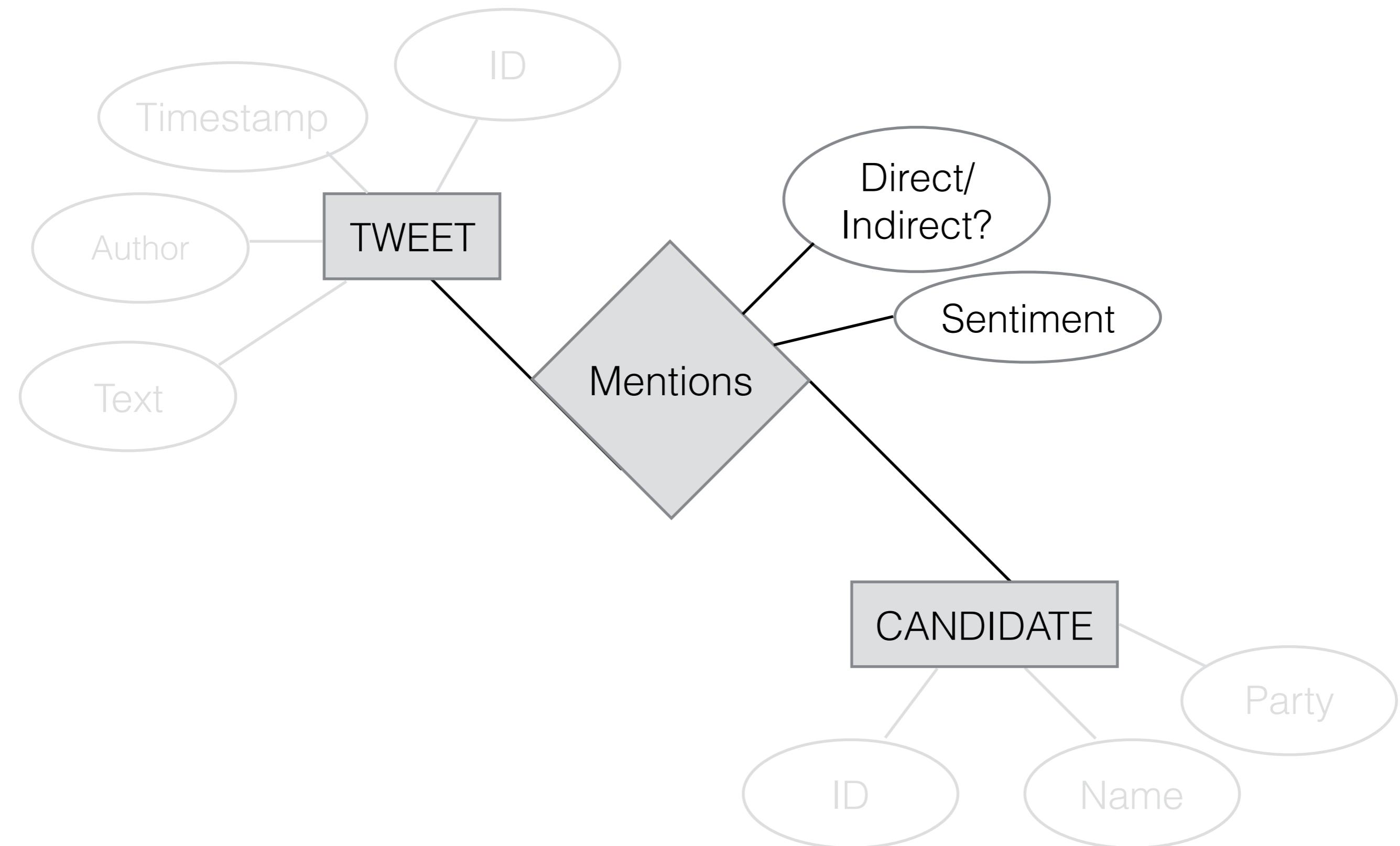
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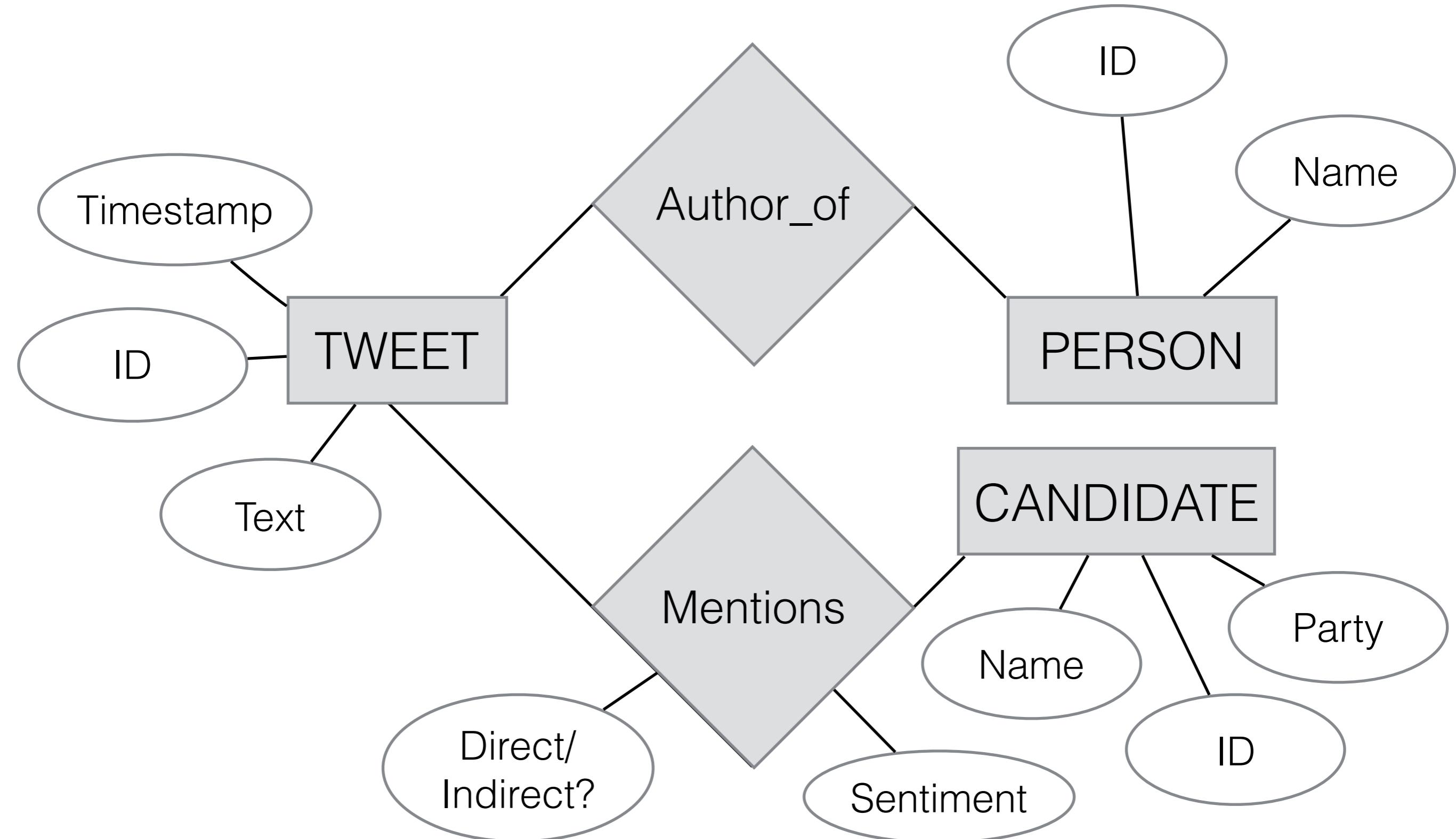
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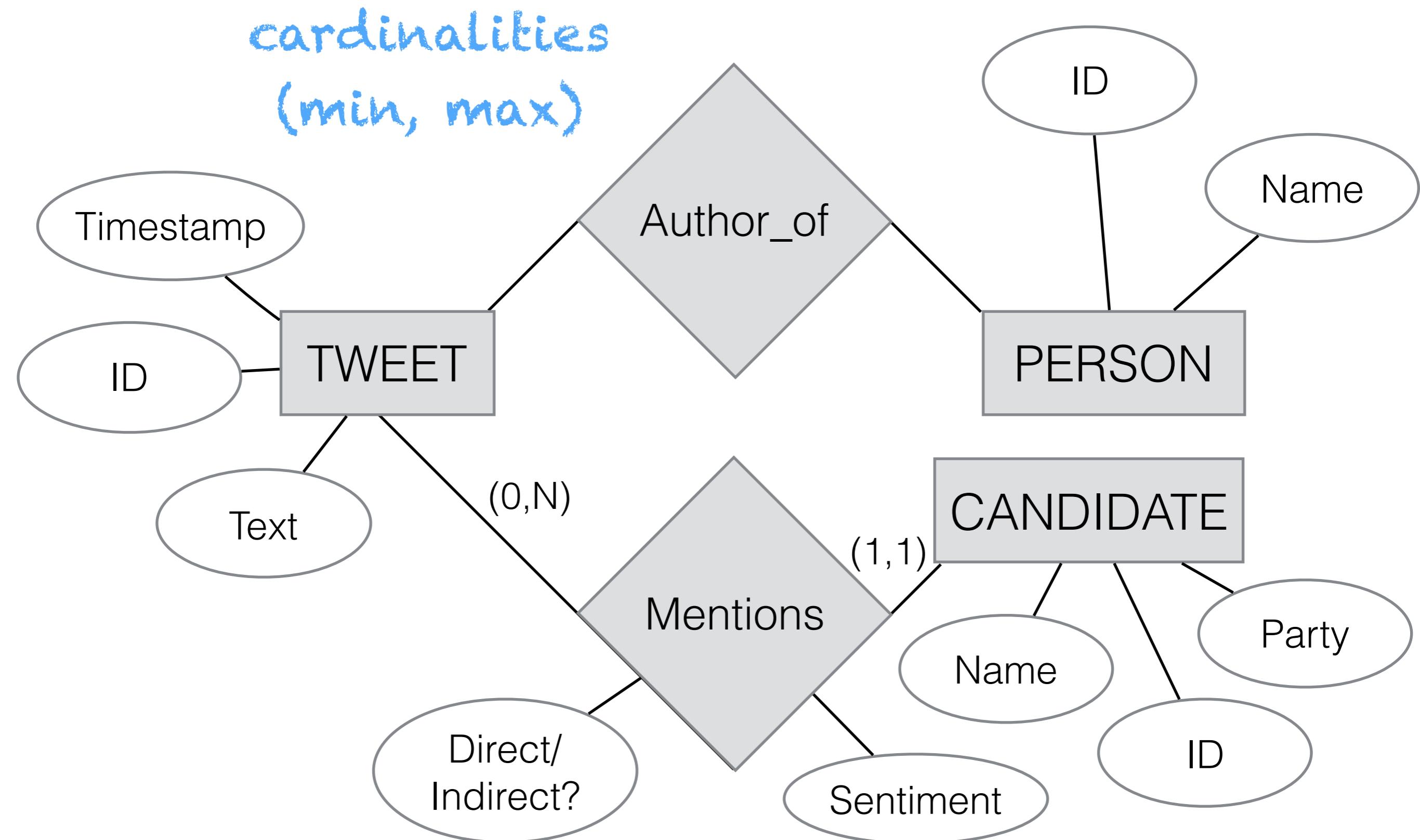
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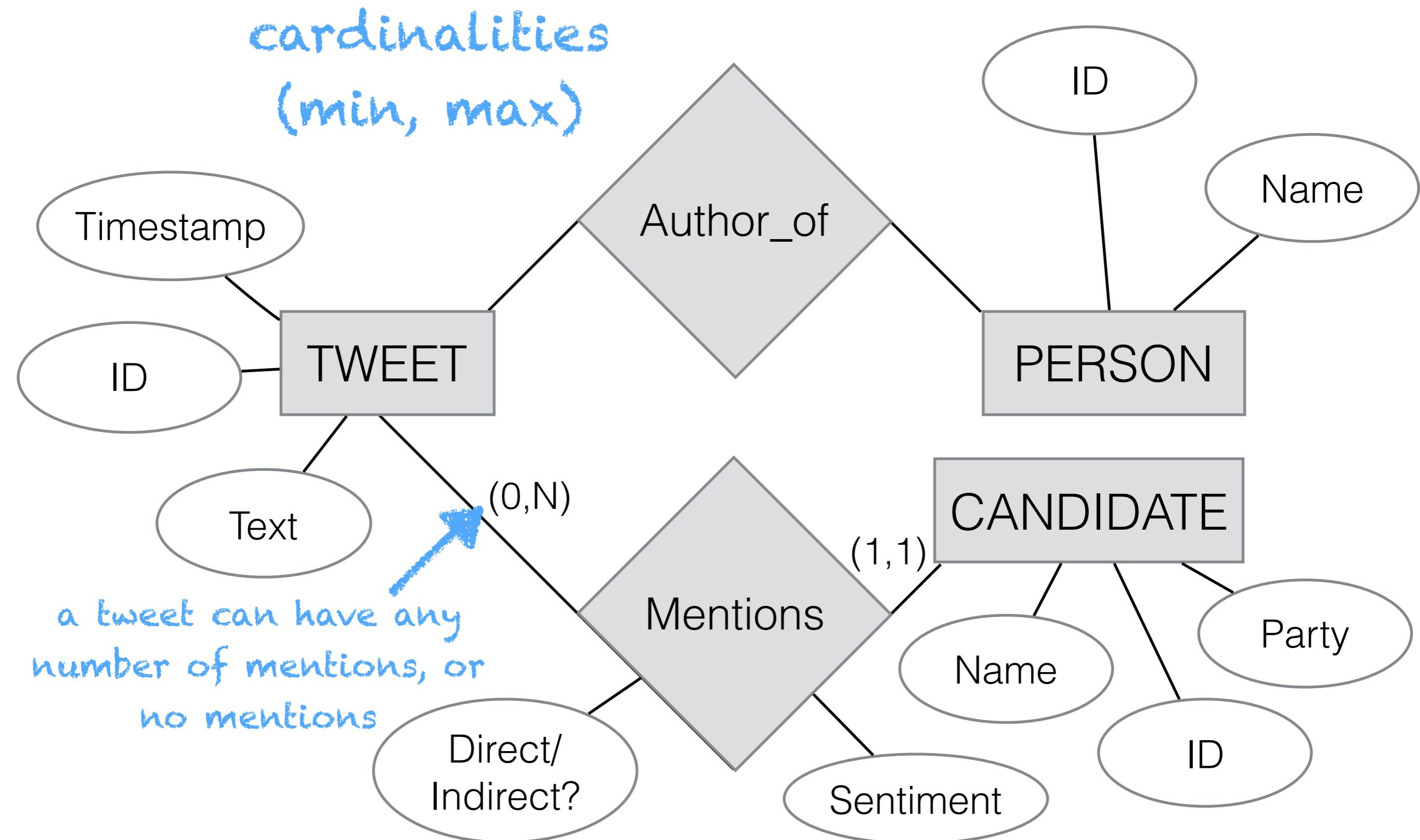
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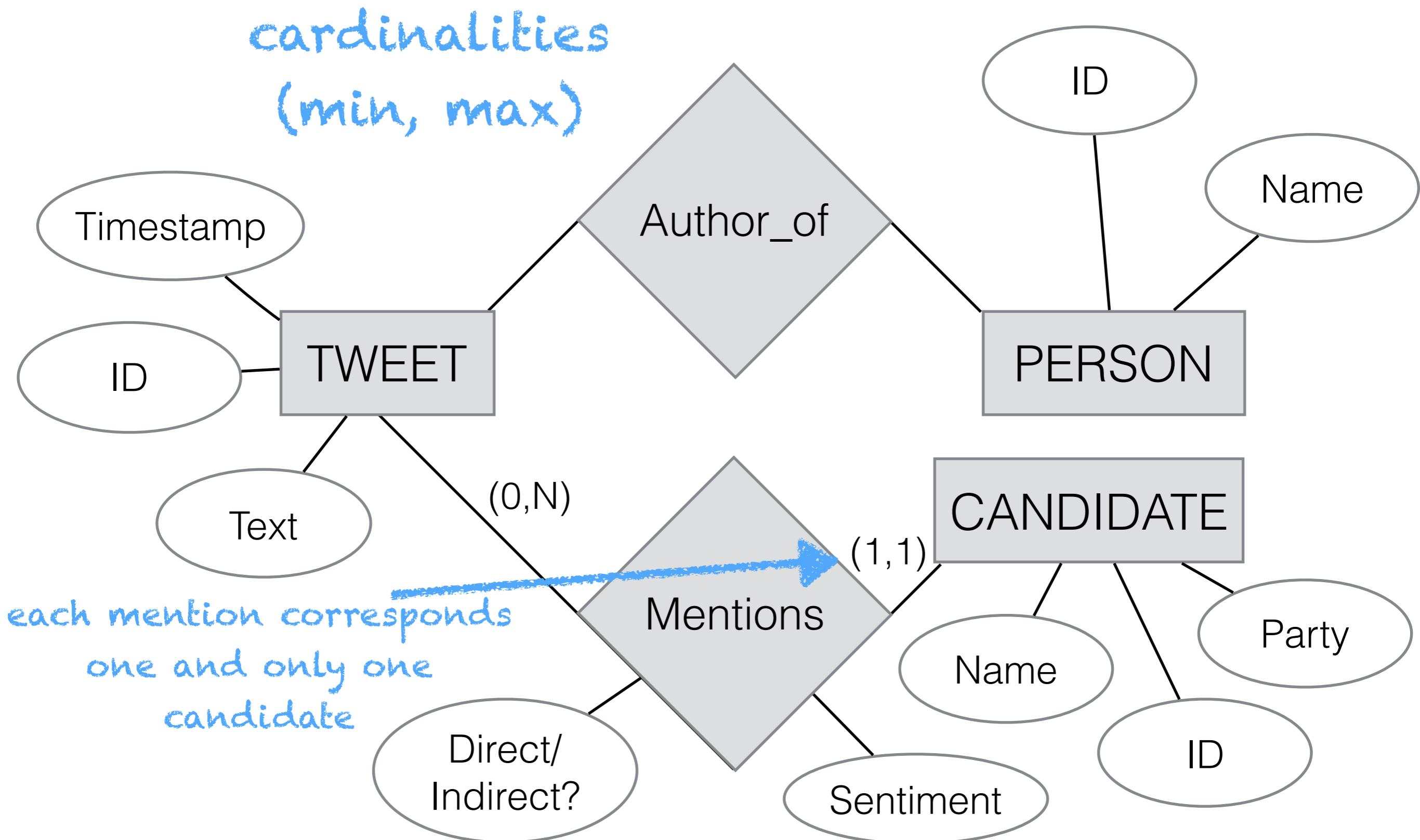
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- Should this concept be an entity? Attribute? Relation?
  - As with most things, there is no good answer
  - Draft, refine, document, iterate...

Before we proceed...

Burning Questions?

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# Relational Model

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TWEET

ID	Timestamp	Author	Text	Mentions
389472	1/1/19 12:34	Bob	hey	NULL
123794	1/1/19 12:32	Maria	lol	{Bob}
596208	1/2/19 1:04	Yu	:-D	NULL

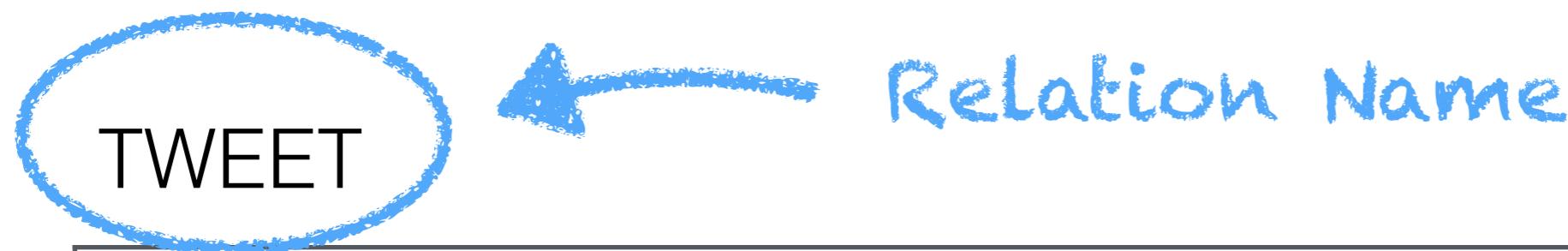
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Relation

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# Relational Model

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Attribute

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Domain:  $D = \text{dom}(\text{Timestamp}) =$   
Valid time strings = ##/##/###/##### ###:###

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tuple

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TWEET:

<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

<389472, 1/1/19 12:34, Bob, hey, {}>

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# Relational Model

*Relation Name*

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<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

*Attribute*

*Domain*

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# Relational Model

*Order Matters!!*

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# Relational Model

*Relation Schema ( $R$ )*

TWEET:

$\langle \text{ID:int}, \text{Timestamp:time}, \text{Author:string}, \text{Text:string}, \text{Mentions:set(string)} \rangle$

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$\langle 596208, 1/2/19\ 1:04, \text{Yu}, \text{:D}, \{\} \rangle$

*Relation State  $r(R)$*

# Relational Model

Intension

TWEET:

<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

<389472, 1/1/19 12:34, Bob, hey, {}>

<123794, 1/1/19 12:32, Maria, lol, {Bob}>

<596208, 1/2/19 1:04, Yu, :-D, {}>

Extension



# Relational Model

Sense

TWEET:

<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

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<596208, 1/2/19 1:04, Yu, :-D, {}>



Reference

Find all the tweets by authors named Maulik.

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<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

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**Find all the tweets by authors named Maulik.**

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SELECT * FROM TWEET WHERE Name is "Maulik"
```

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**"Closed world assumption"**

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<389472, 1/1/19 12:34, Bob, hey, {}>

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Find all the tweets which weight less than 45lbs

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<389472, 1/1/19 12:34, Bob, hey, {}>

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Find all the tweets which weight less than 45lbs

```
SELECT * FROM TWEET WHERE Weight < 45
```

TWEET:

```
<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>
```

```
<389472, 1/1/19 12:34, Bob, hey, {}>
```

```
<123794, 1/1/19 12:32, Maria, lol, {Bob}>
```

```
<596208, 1/2/19 1:04, Yu, :-D, {}>
```

Find all the tweets which weight less than 45lbs

SELECT \* FROM TWEET WHERE Weight < 45

????



TWEET:

<ID:int, Timestamp:time, Author:string, Text:string, Mentions:set(string)>

<389472, 1/1/19 12:34, Bob, hey, {}>

<123794, 1/1/19 12:32, Maria, lol, {Bob}>

<596208, 1/2/19 1:04, Yu, :-D, {}>

# Relational Model

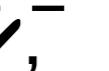
$R: (A_0:\text{dom}(A_0), A_1:\text{dom}(A_1), \dots A_n:\text{dom}(A_n))$

$r(R) \subseteq \text{dom}(A_0) \times \text{dom}(A_1) \times \dots \times \text{dom}(A_n)$

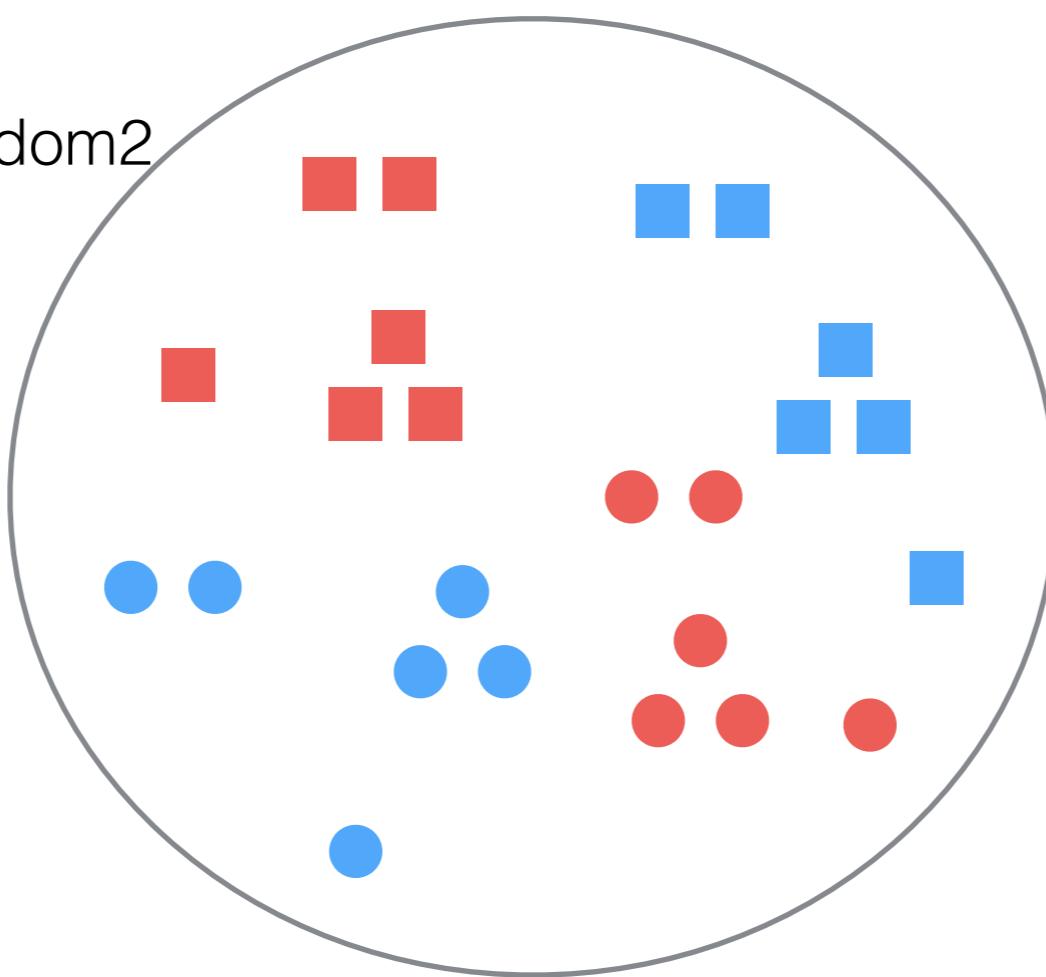
# Relational Model

dom0 = {  ,  }

dom1 = {  ,  }

dom2 = {  ,  ,  }

dom0 × dom1 × dom2

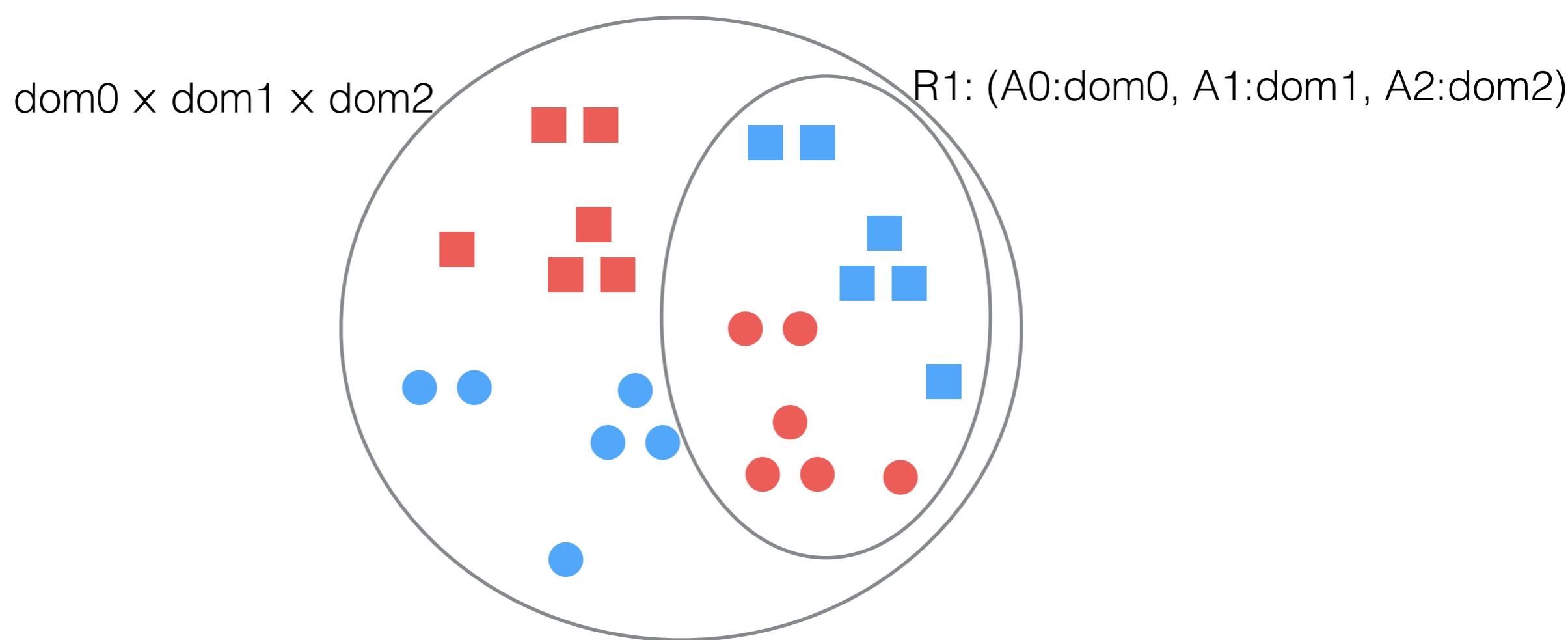


# Relational Model

$\text{dom0} = \{ \text{ } \textcolor{blue}{m}, \textcolor{red}{m} \}$

$\text{dom1} = \{ \textcolor{black}{\circlearrowleft}, \textcolor{black}{\sqsubset} \}$

$\text{dom2} = \{ \checkmark, \textcolor{black}{\checkmark\checkmark}, \textcolor{black}{\checkmark\checkmark\checkmark} \}$

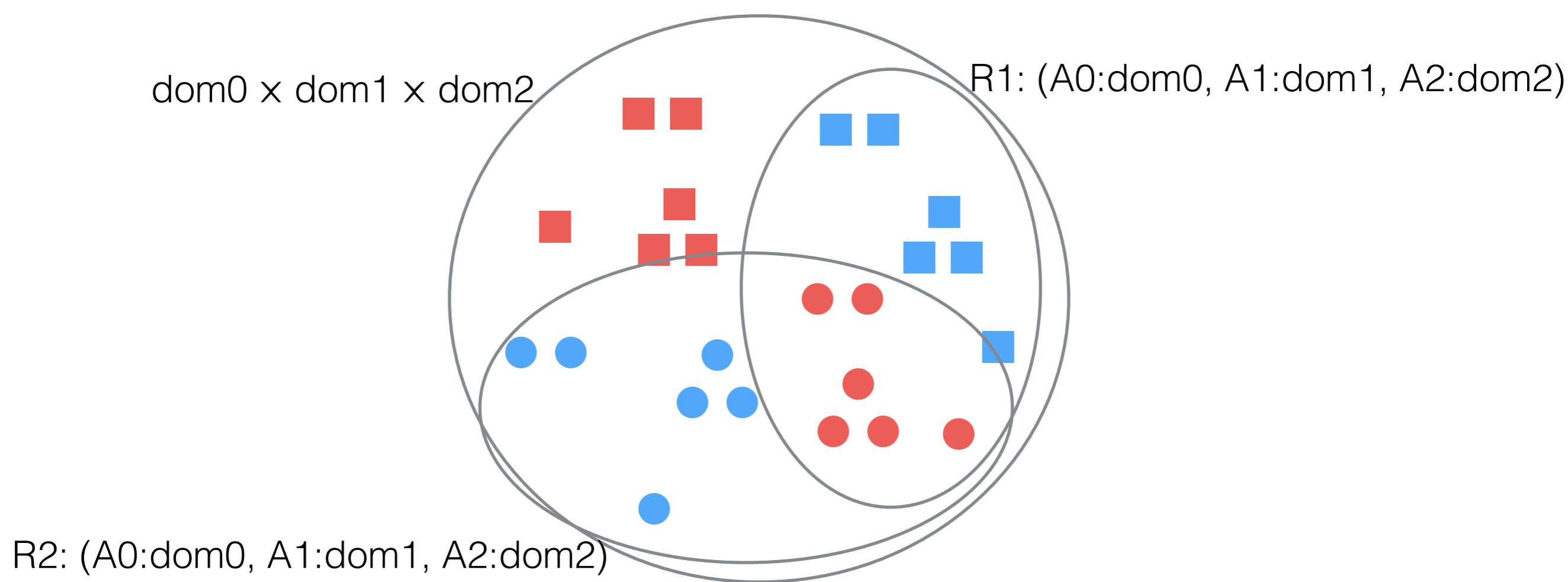


# Relational Model

`dom0 = { 3 , 2 }`

`dom1 = { ( ), [ ] }`

$$\text{dom2} = \{\checkmark, \checkmark\checkmark, \checkmark\checkmark\checkmark\}$$



# Relational Model

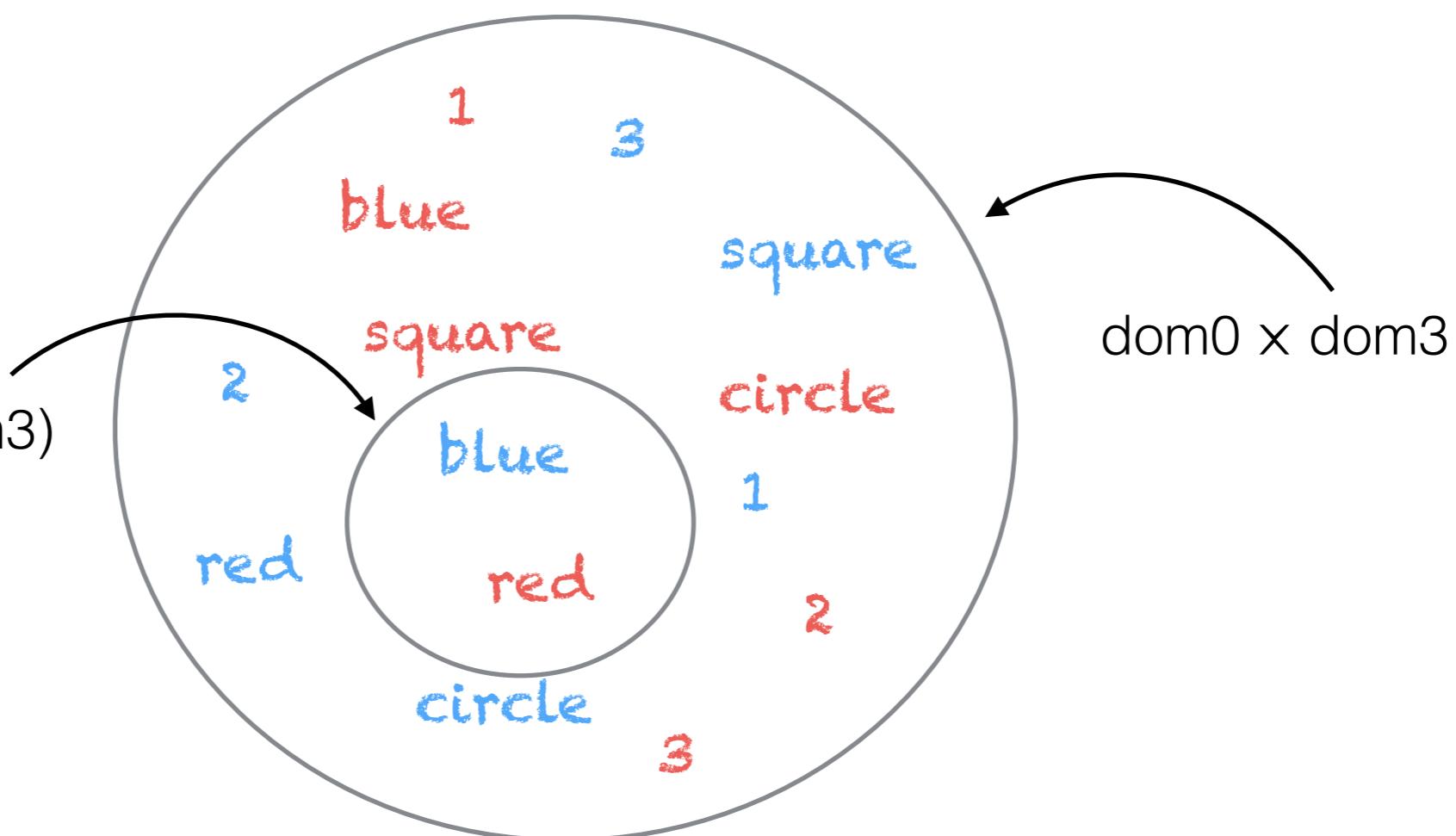
$\text{dom0} = \{ \text{blue}, \text{red} \}$

$\text{dom1} = \{ \text{circle}, \text{square} \}$

$\text{dom2} = \{ 1, 2, 3 \}$

$\text{dom3} = \{ \text{blue, red, circle, square, 1, 2, 3} \}$

$S: (A0:\text{dom0}, A1:\text{dom3})$



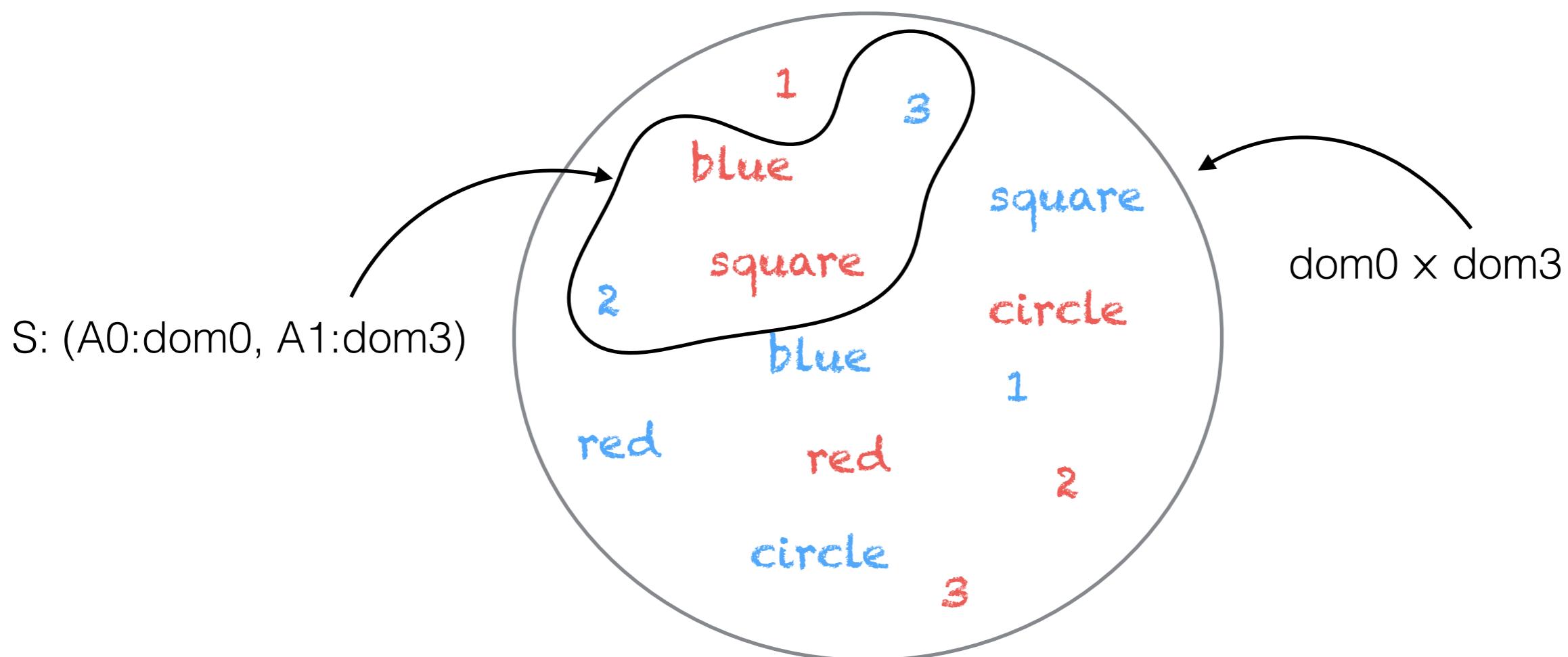
# Relational Model

$\text{dom0} = \{ \text{blue}, \text{red} \}$

$\text{dom1} = \{ \text{circle}, \text{square} \}$

$\text{dom2} = \{ 1, 2, 3 \}$

$\text{dom3} = \{ \text{blue, red, circle, square, 1, 2, 3} \}$



# Relational Model

dom0 = { ,  }

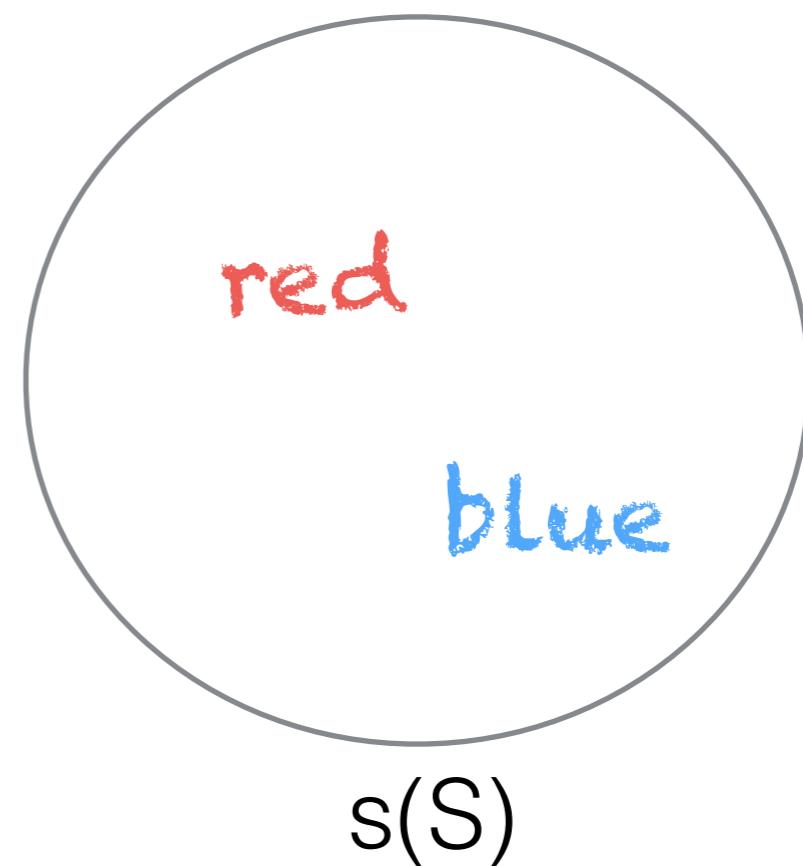
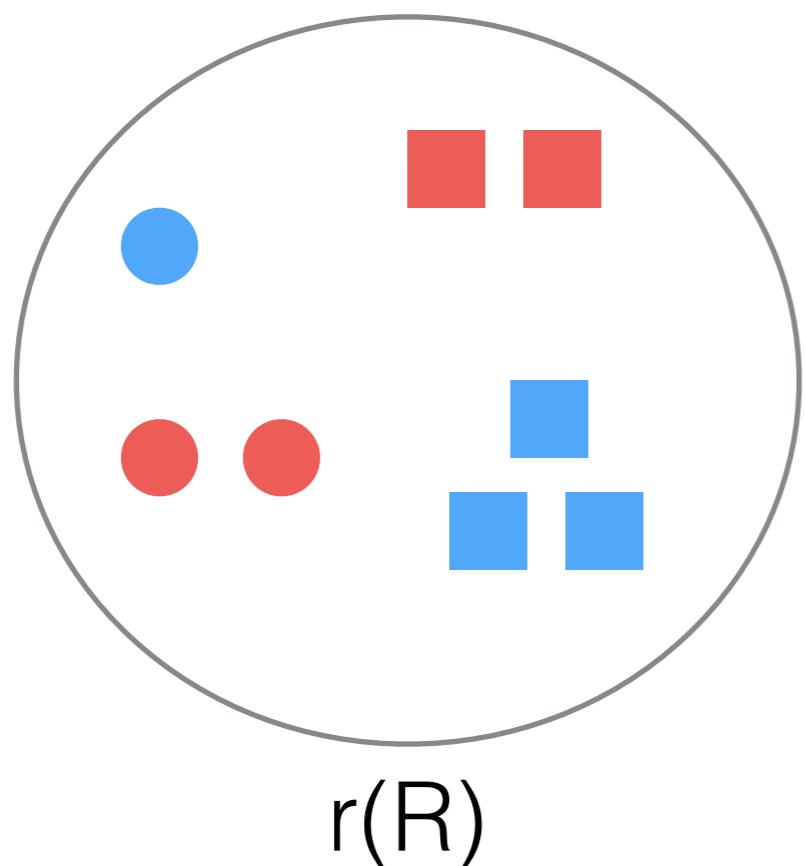
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

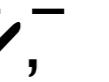
S: (A0:dom0, A1:dom3)



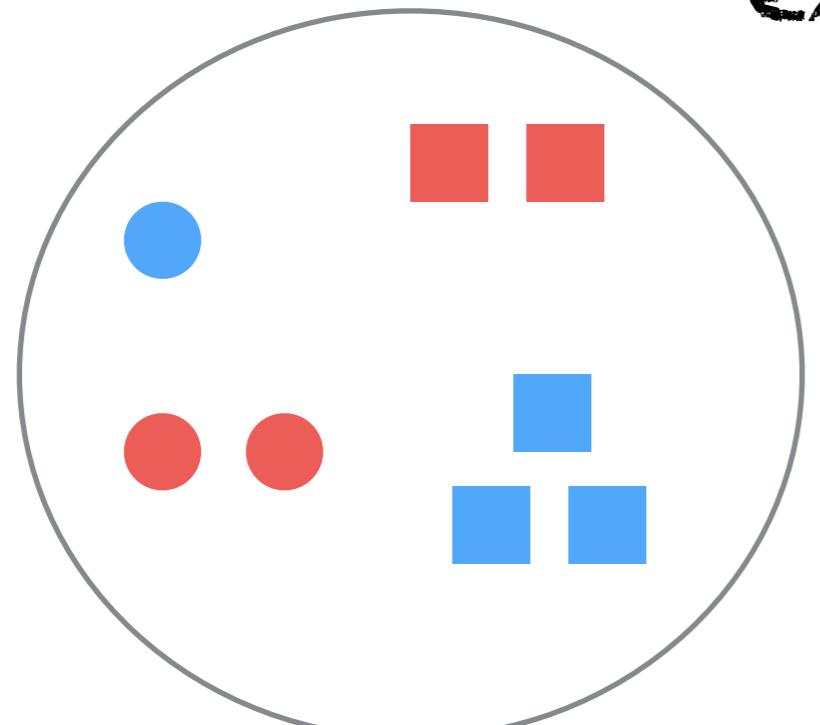
# Relational Model

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

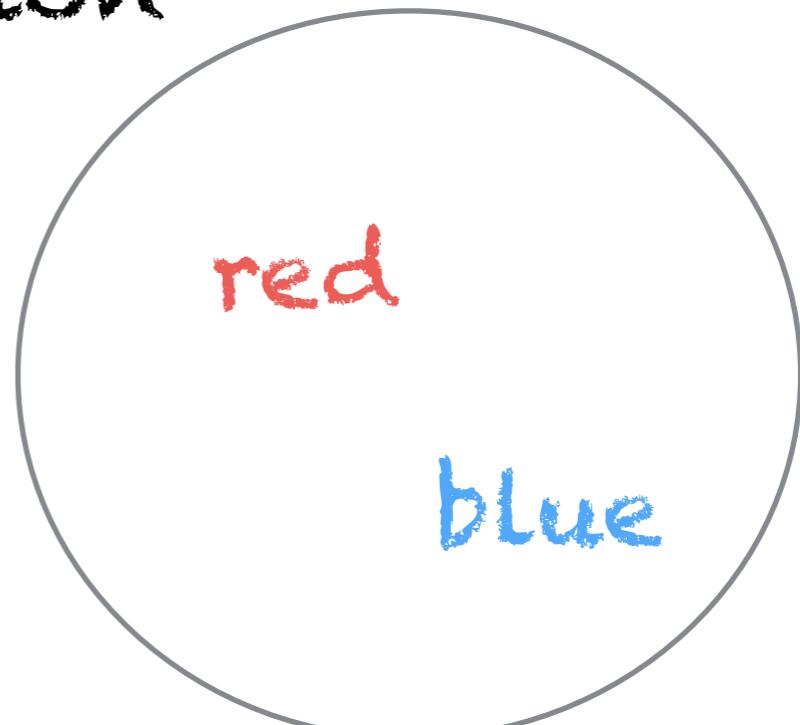
dom3 = {blue, red, circle, square, 1, 2, 3}



extension

R: (A0:dom0, A1:dom1, A2:dom2)  
S: (A0:dom0, A1:dom3)

intension



$s(S)$

dom0 = { ,  }

dom1 = { ,  }

dom2 = {, ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

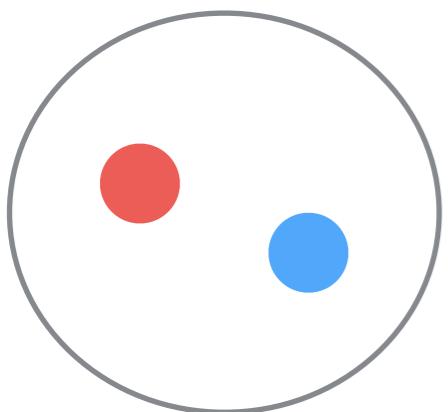
# Clicker Question!

## In which of the following intension/ extension pairs is NOT valid?

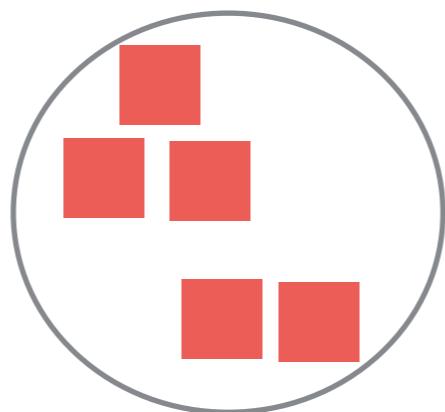
R: (A0:dom0, A1:dom1)

R: (A0:dom0, A1:dom1)

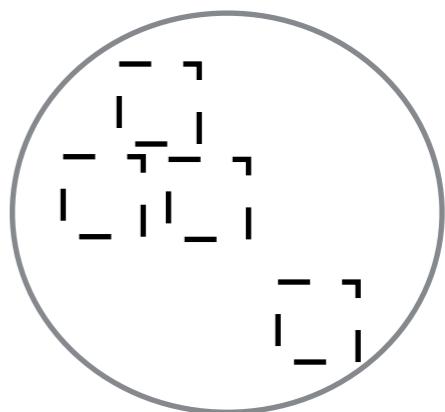
R: (A0:dom1, A1:dom2)



(a)



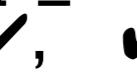
(b)



(c)

dom0 = { ,  }

dom1 = { ,  }

dom2 = {, ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

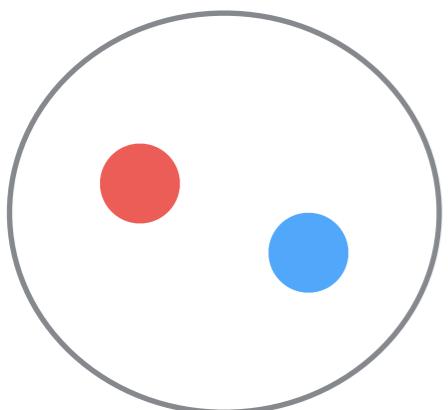
# Clicker Question!

## In which of the following intension/ extension pairs is NOT valid?

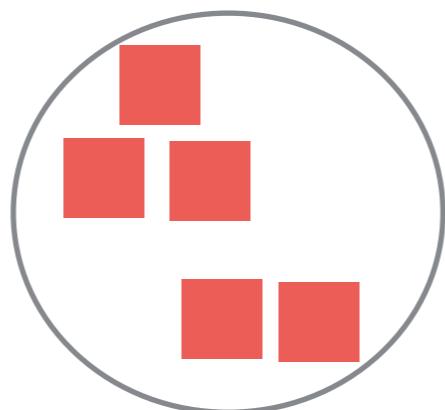
R: (A0:dom0, A1:dom1)

R: (A0:dom0, A1:dom1)

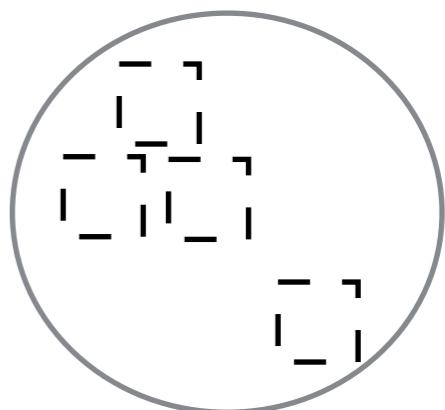
R: (A0:dom1, A1:dom2)



(a)



(b)



(c)

dom0 = { ,  }

dom1 = { ,  }

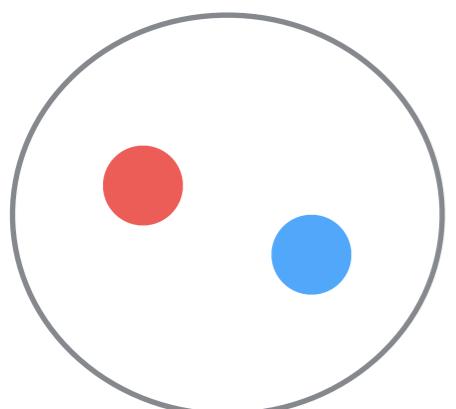
dom2 = {, ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

# Clicker Question!

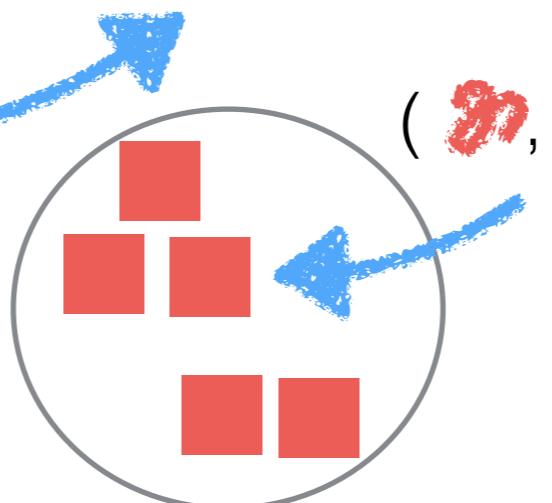
## In which of the following intension/ extension pairs is NOT valid?

R: (A0:dom0, A1:dom1)



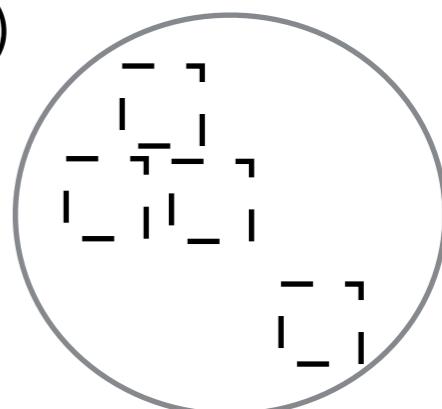
(a)

R: (A0:dom0, A1:dom1)



(b)

R: (A0:dom1, A1:dom2)



(c)

dom0 = { ,  }

dom1 = { ,  }

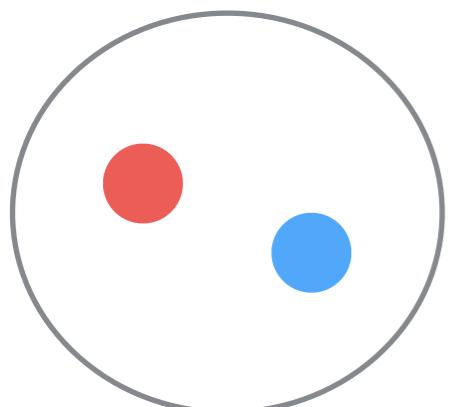
dom2 = {, ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

# Clicker Question!

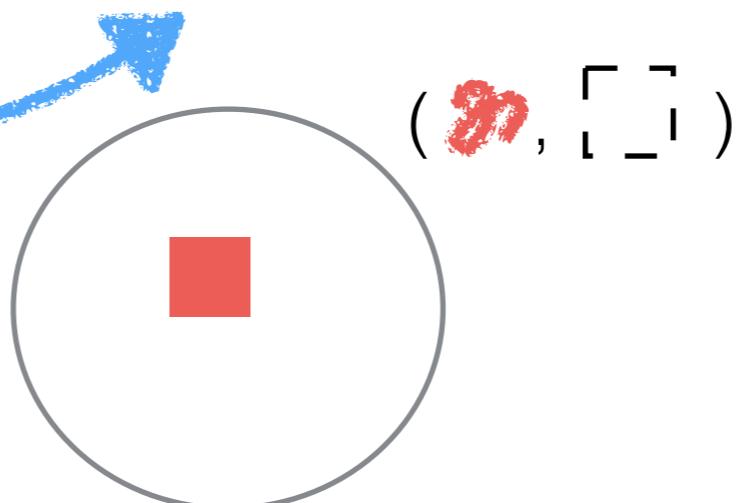
## In which of the following intension/ extension pairs is NOT valid?

R: (A0:dom0, A1:dom1)



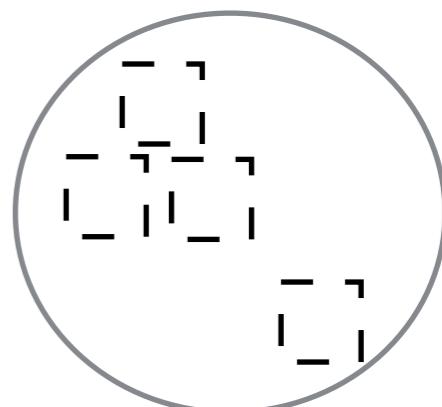
(a)

R: (A0:dom0, A1:dom1)



(b)

R: (A0:dom1, A1:dom2)



(c)

# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

## Select

dom0 = { ,  }

dom1 = { ,  }

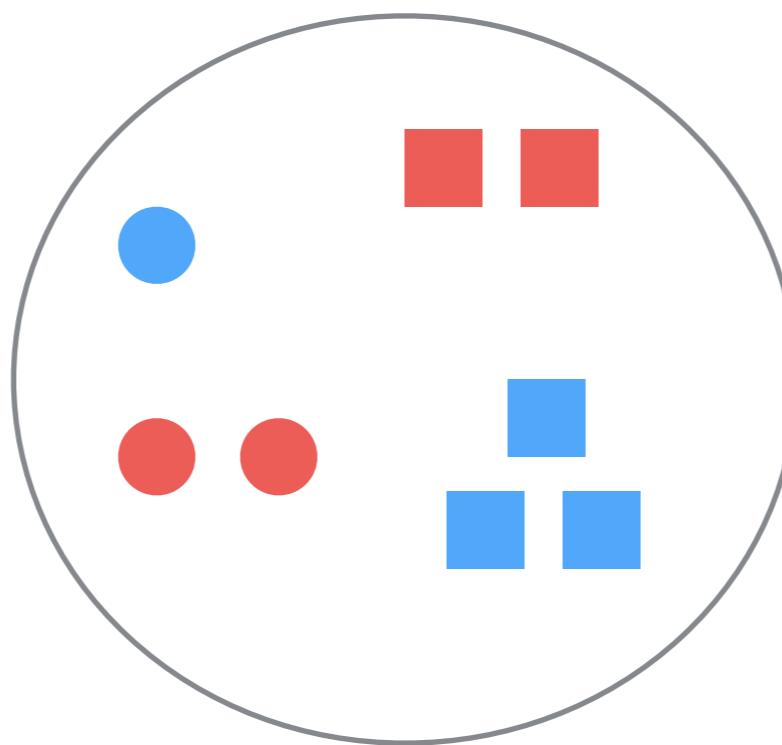
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



# Relational Algebra

## Select

dom0 = {  ,  }

dom1 = {  ,  }

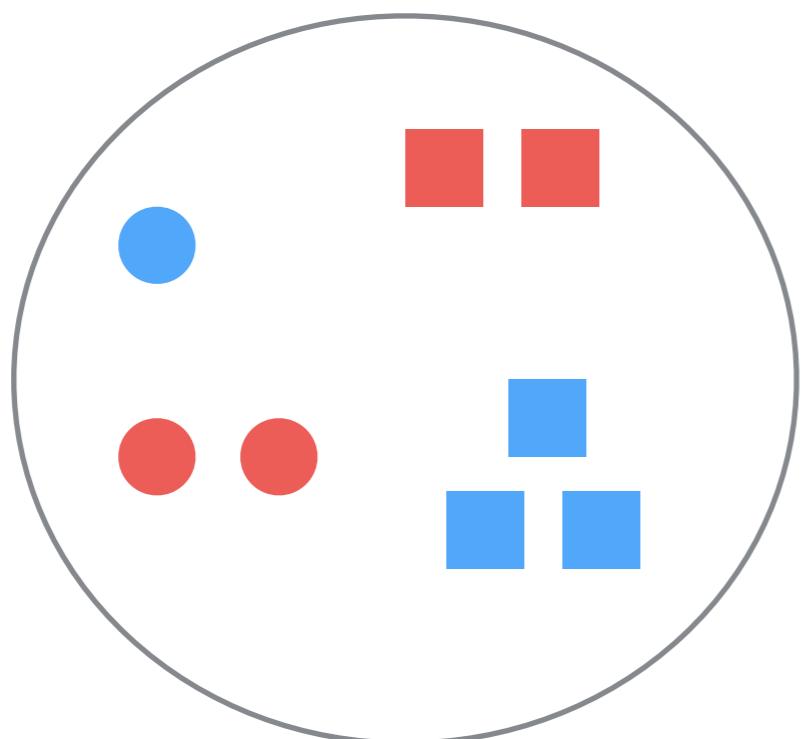
dom2 = {, , 

dom3 = {blue, red, circle, square, 1, 2, 3}

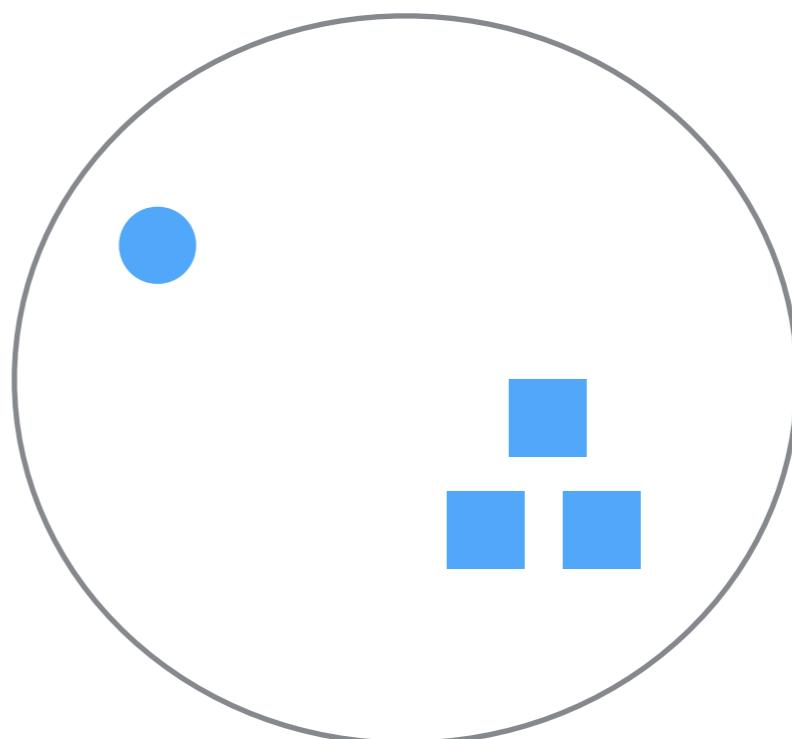
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\sigma_{A0=\text{blue}}(R)$



# Relational Algebra

## Select

dom0 = { ,  }

dom1 = { ,  }

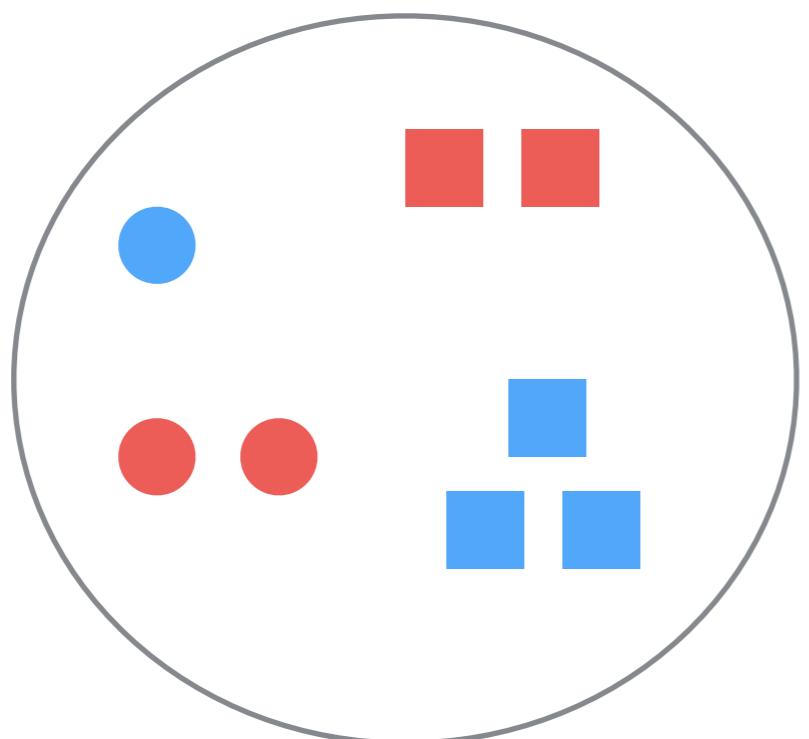
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

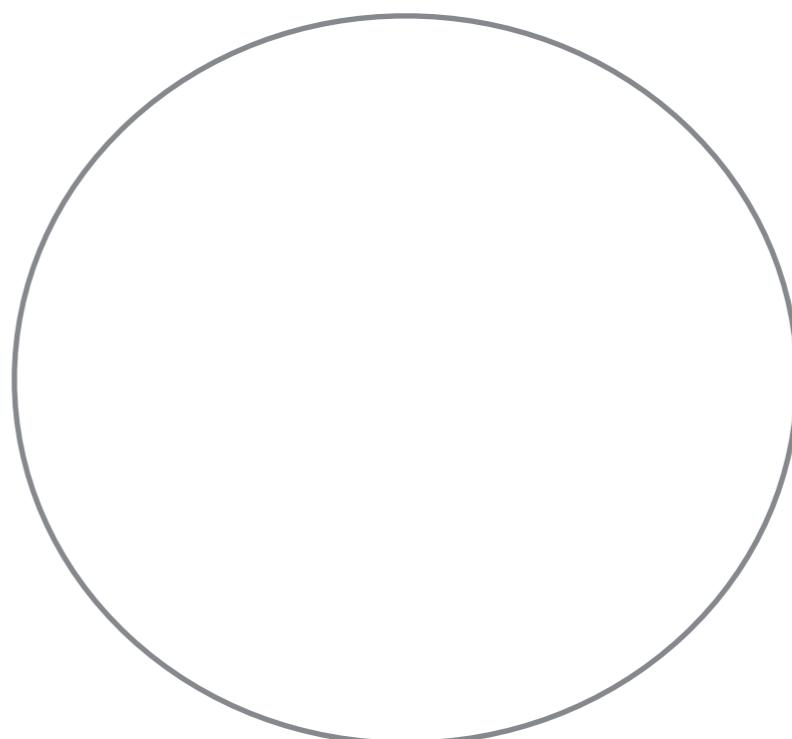
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\sigma_{A1=\text{circle} \text{ or } A2=2}(R)$

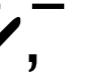


# Relational Algebra

## Select

dom0 = { ,  }

dom1 = { ,  }

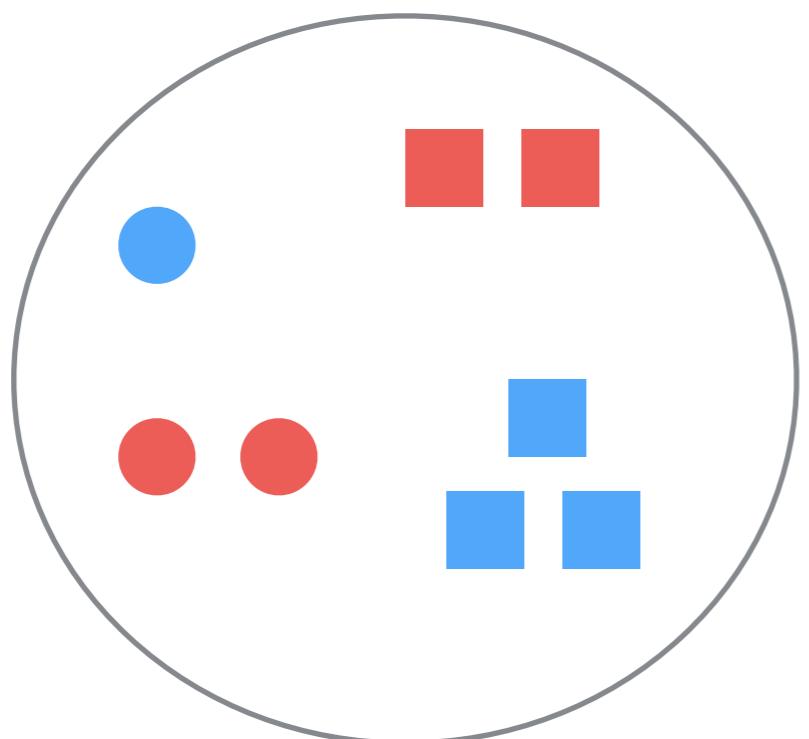
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

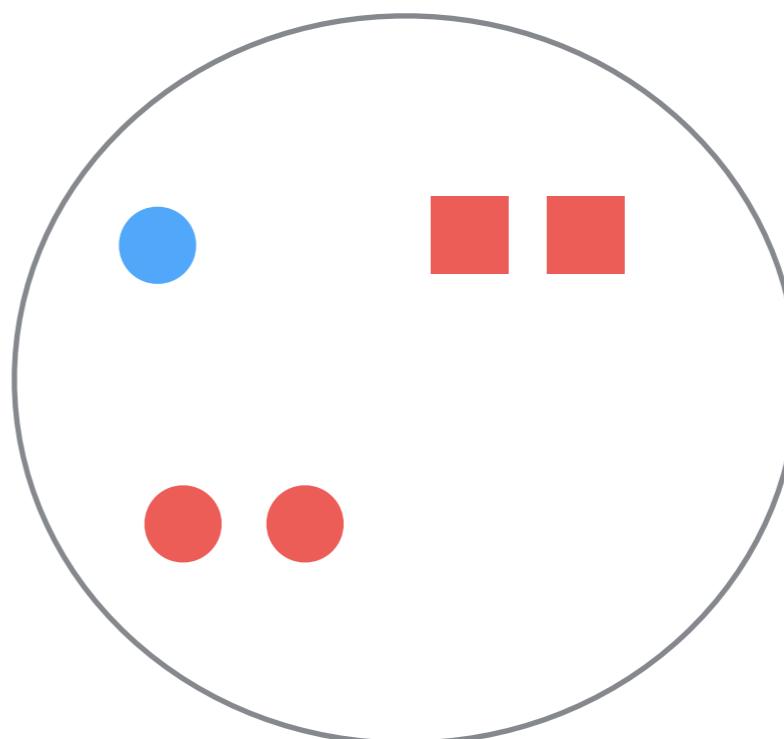
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\sigma_{A1=\text{circle} \text{ or } A2=\text{two checkmarks}}(R)$



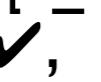
# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra Project

dom0 = { ,  }

dom1 = { ,  }

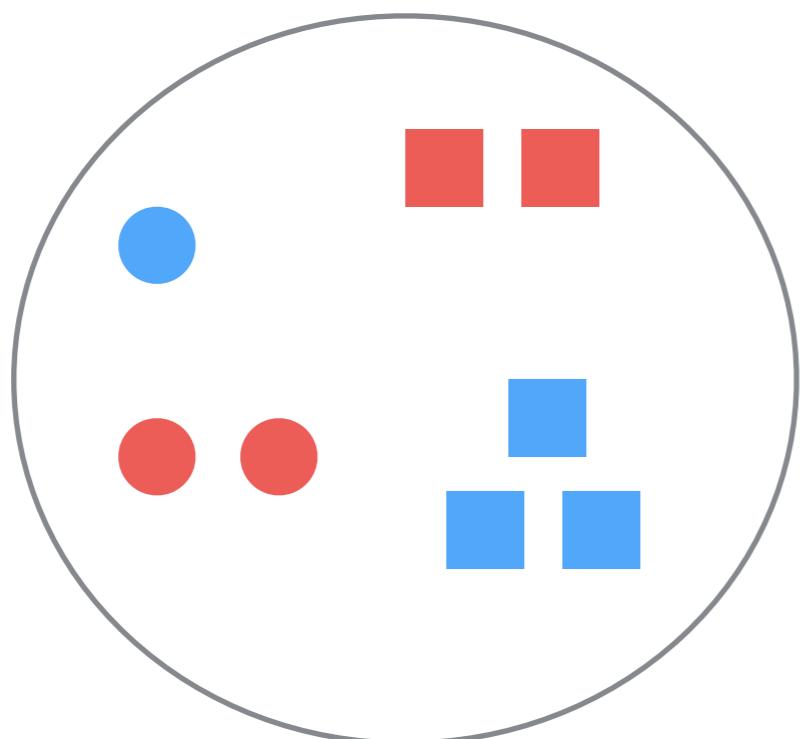
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

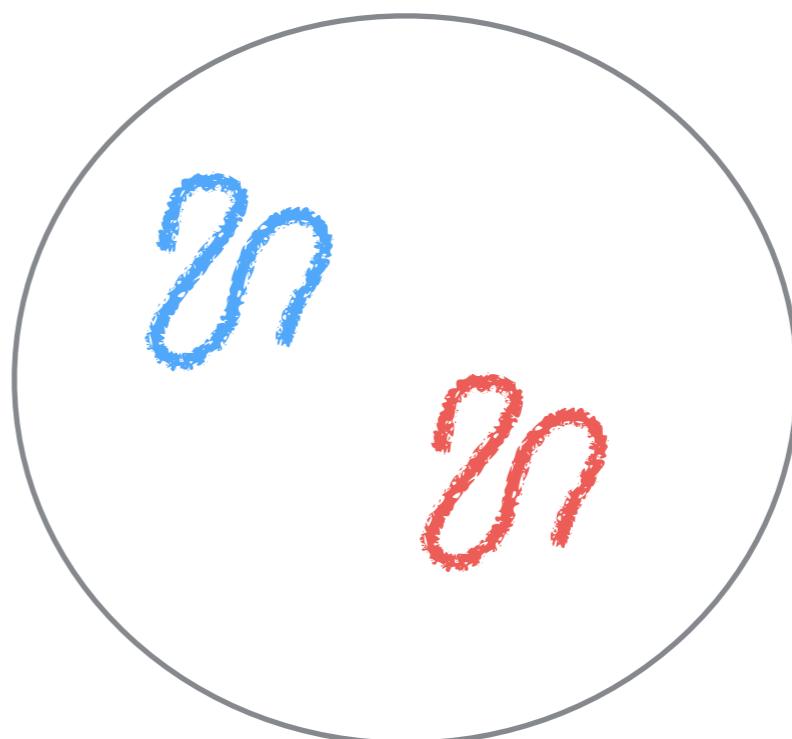
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\pi_{A0}(R)$



# Relational Algebra Project

dom0 = { ,  }

dom1 = { ,  }

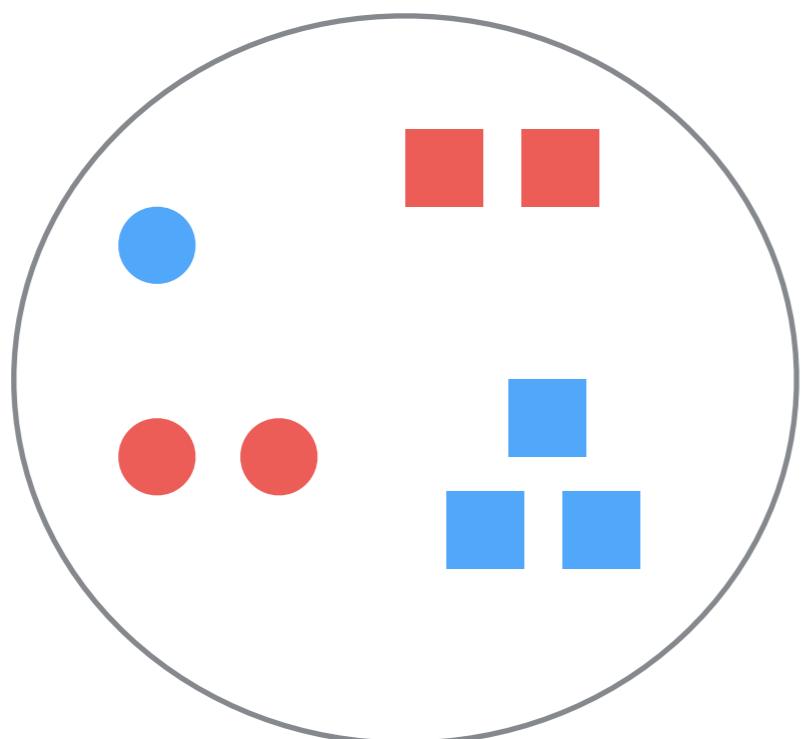
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

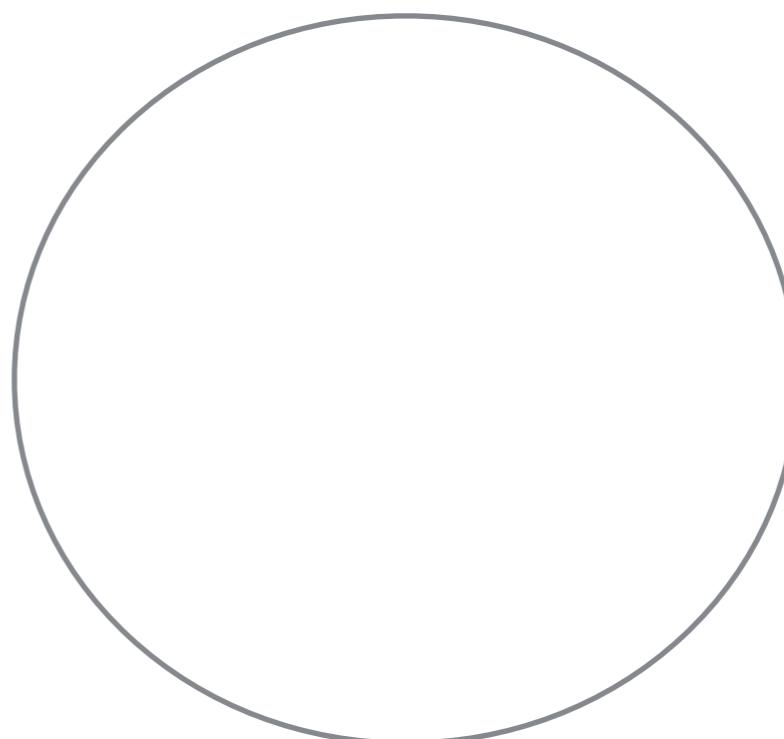
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\pi_{A0, A3}(R)$



# Relational Algebra Project

dom0 = { ,  }

dom1 = { ,  }

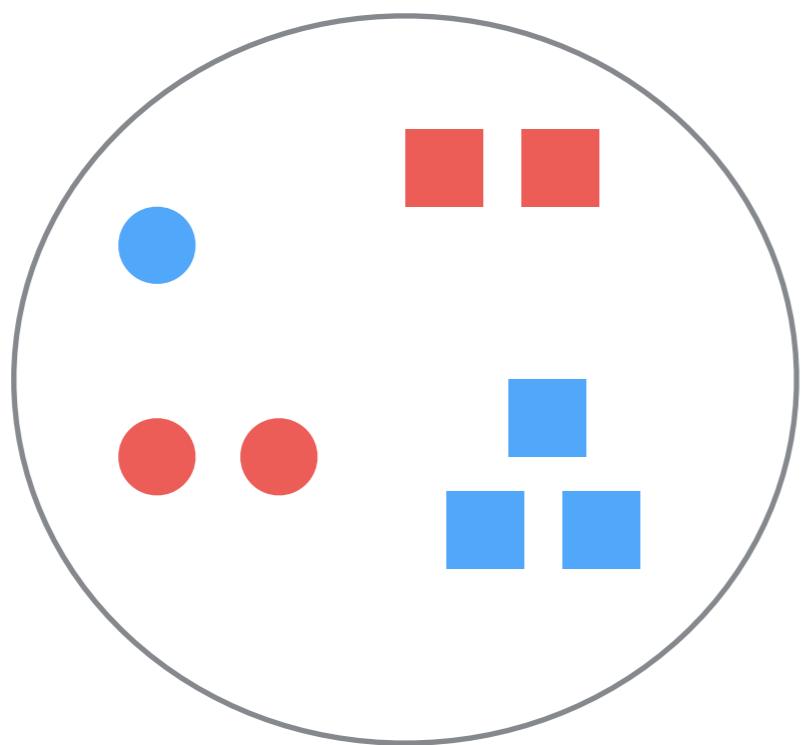
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

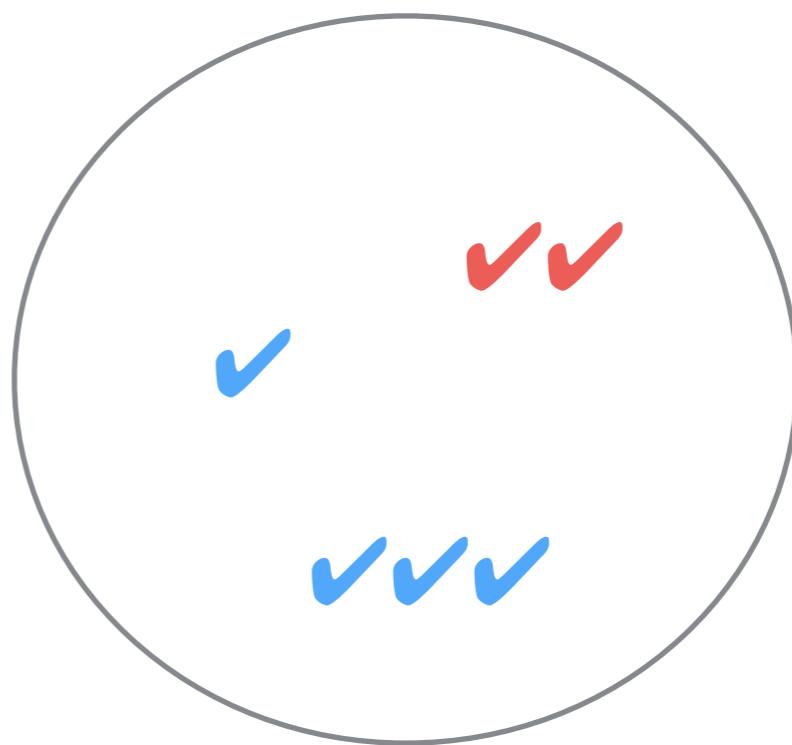
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



$\pi_{A0, A3}(R)$



# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

## Union

dom0 = { ,  }

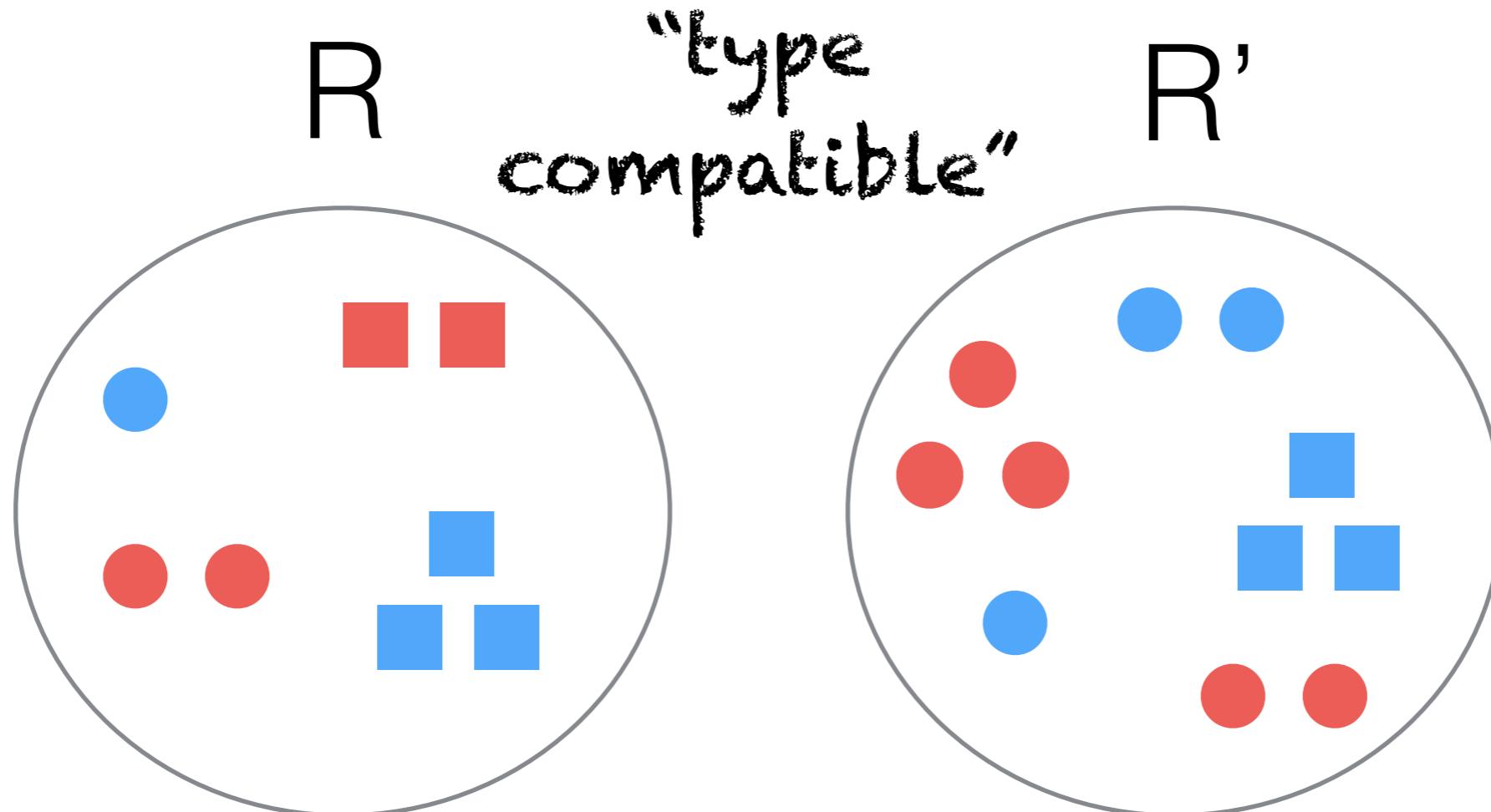
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)



# Relational Algebra

## Union

dom0 = { ,  }

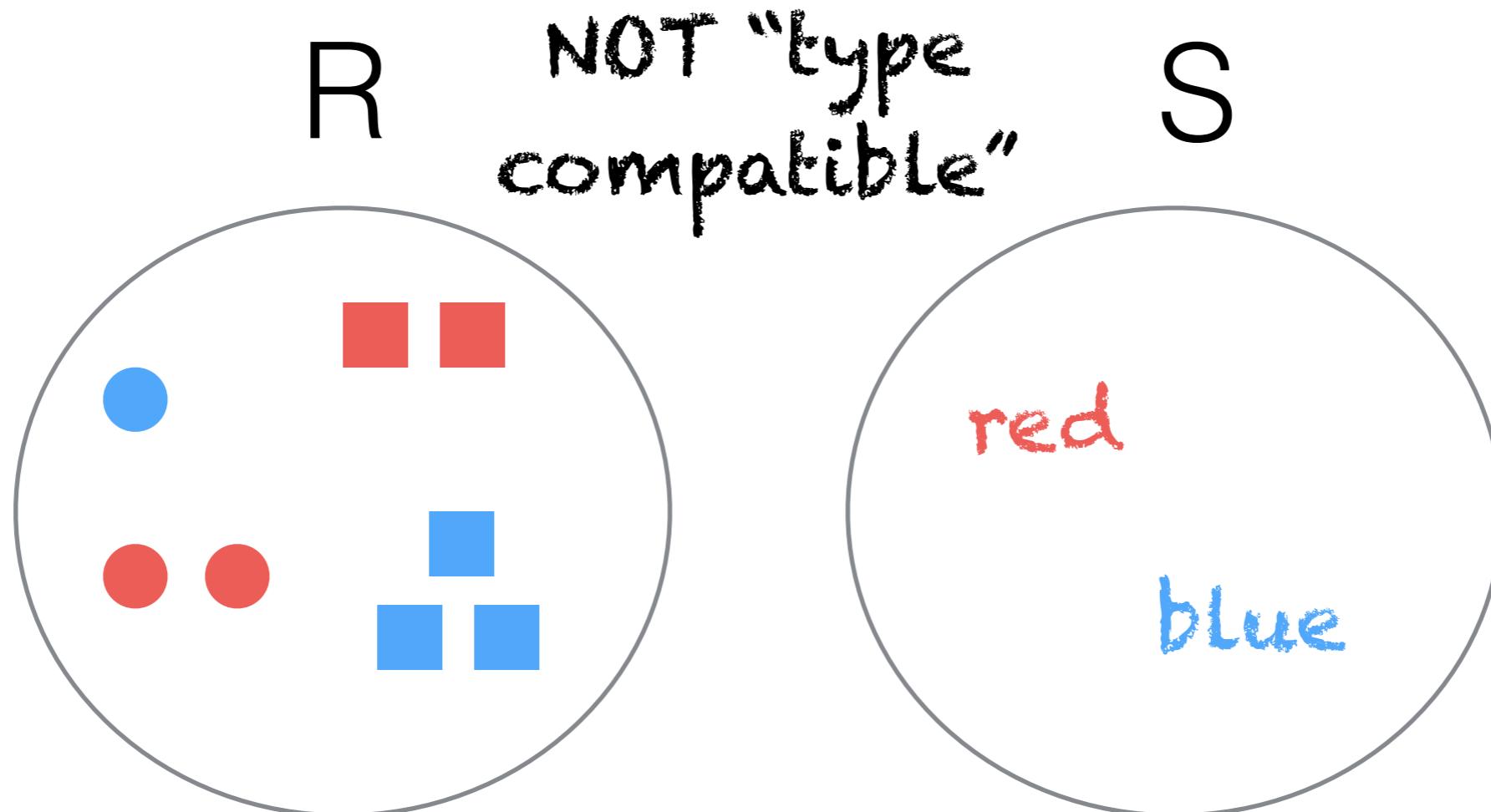
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

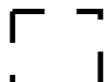
S: (A0:dom0, A1:dom3)

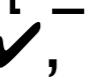


# Relational Algebra

## Union

dom0 = { ,  }

dom1 = { ,  }

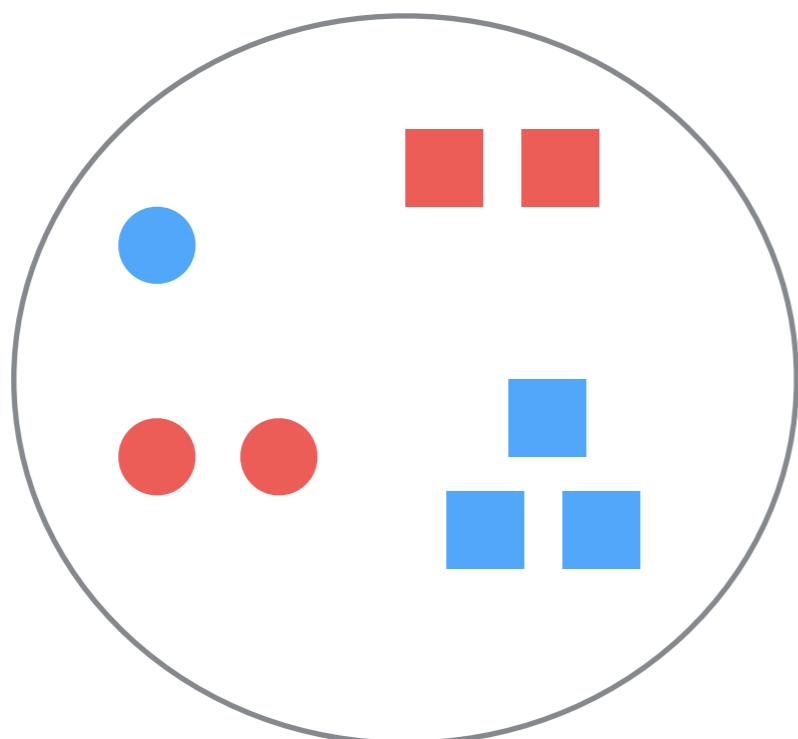
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

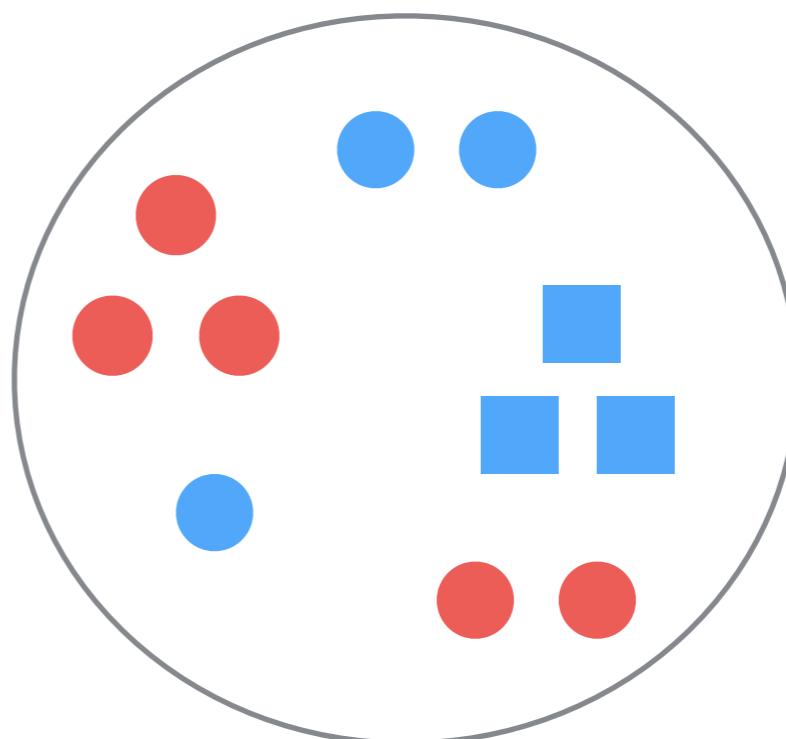
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R



R'

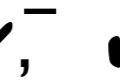
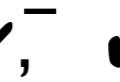


# Relational Algebra

## Union

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

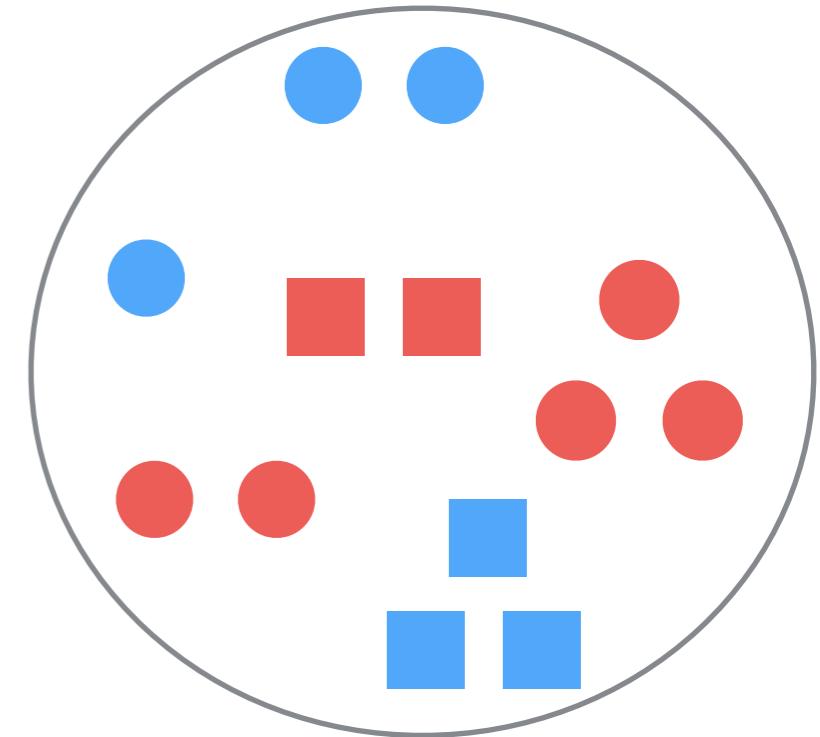
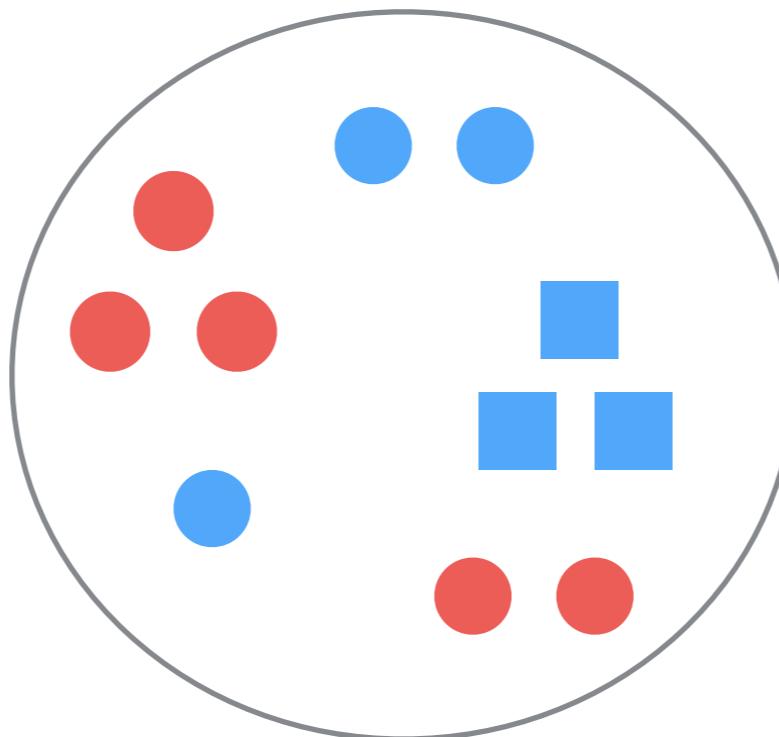
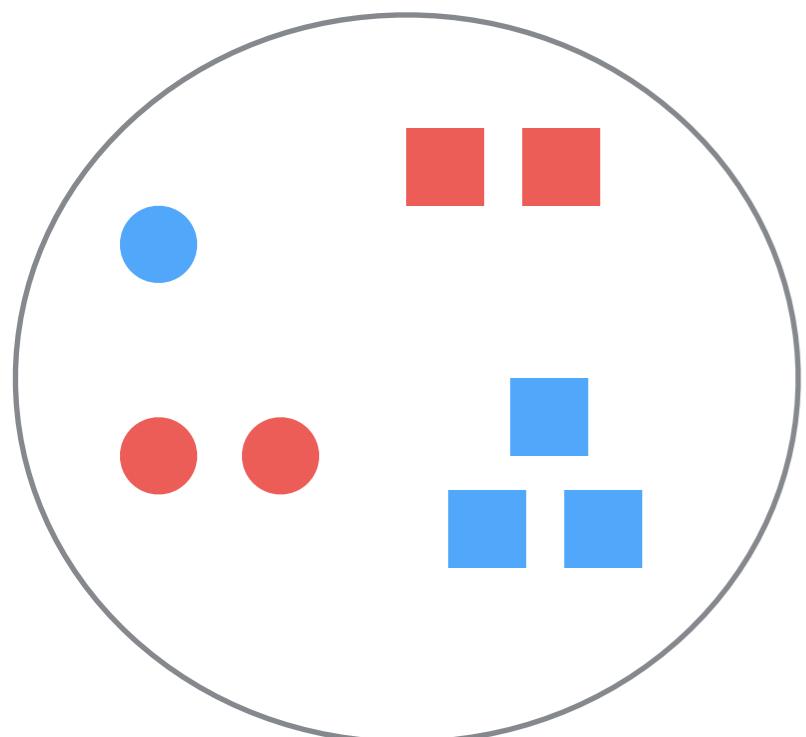
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

R'

R  $\cup$  R'



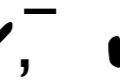
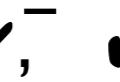
# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra Minus

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

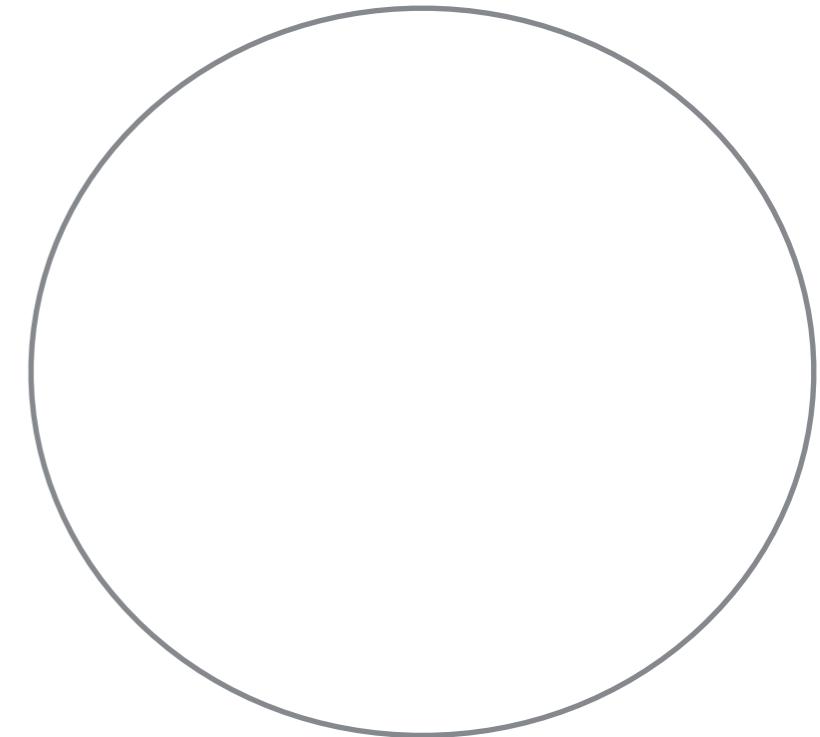
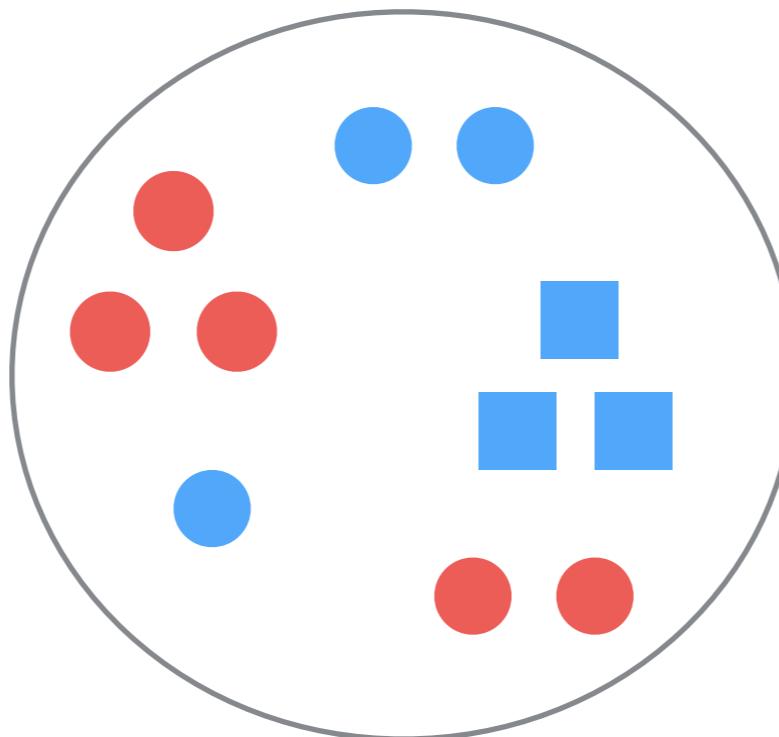
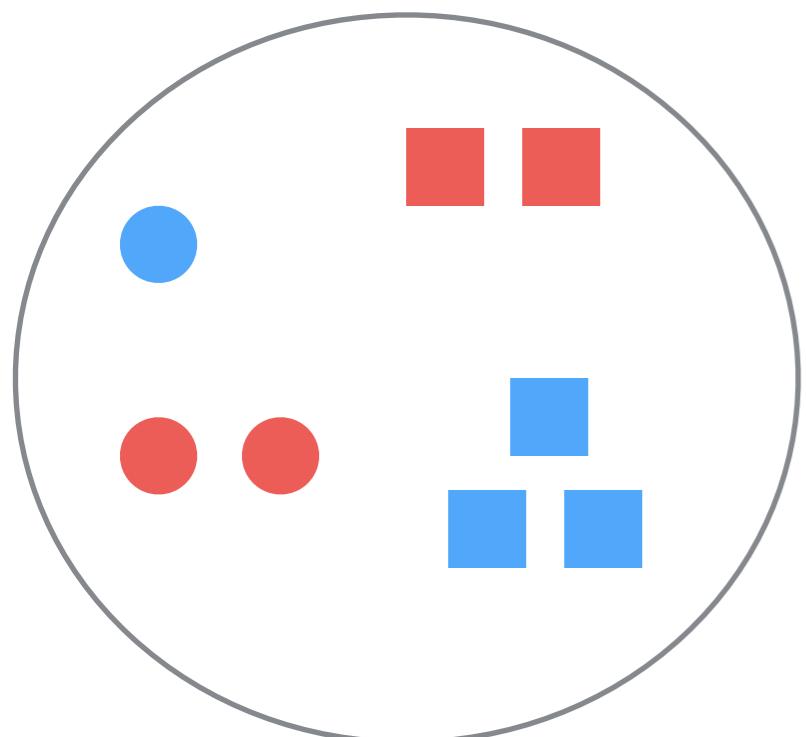
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

R'

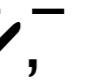
R - R'



# Relational Algebra Minus

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

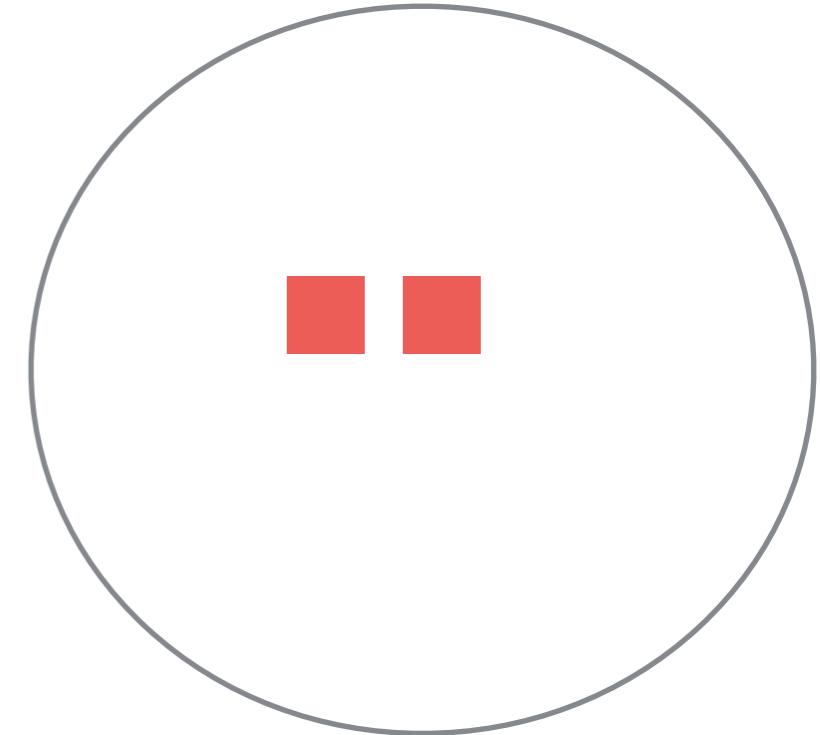
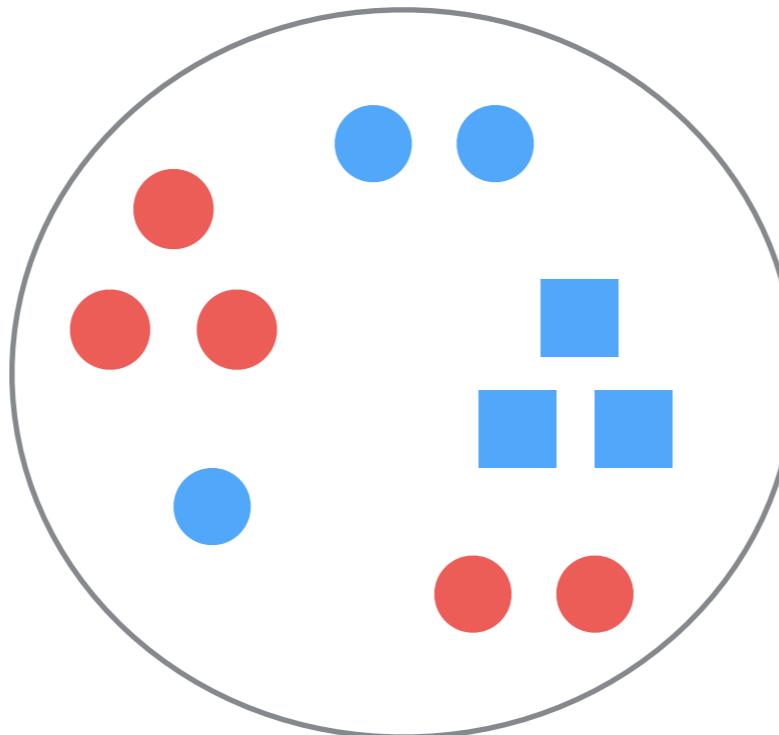
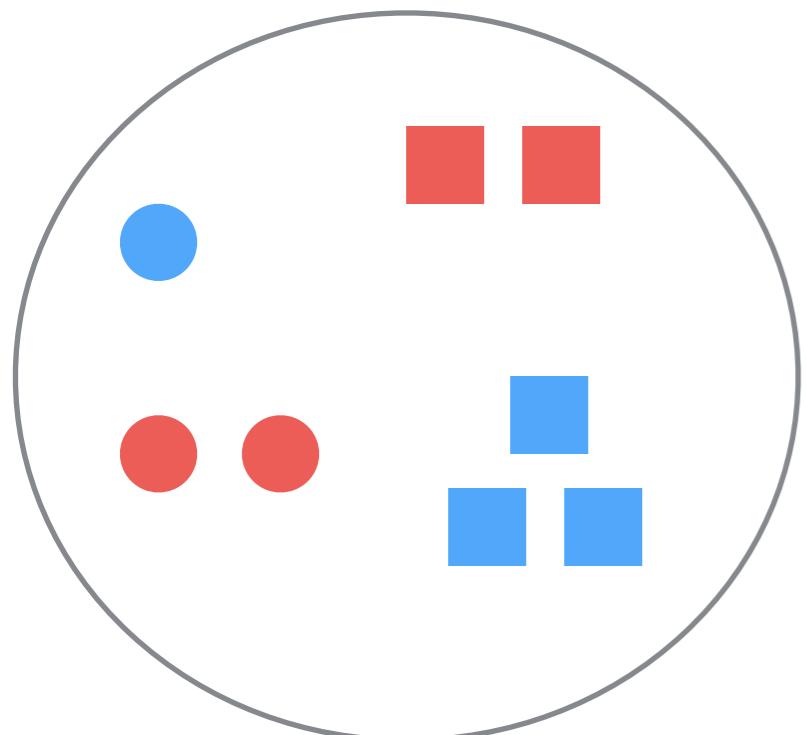
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

R'

R - R'



# Relational Algebra Minus

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

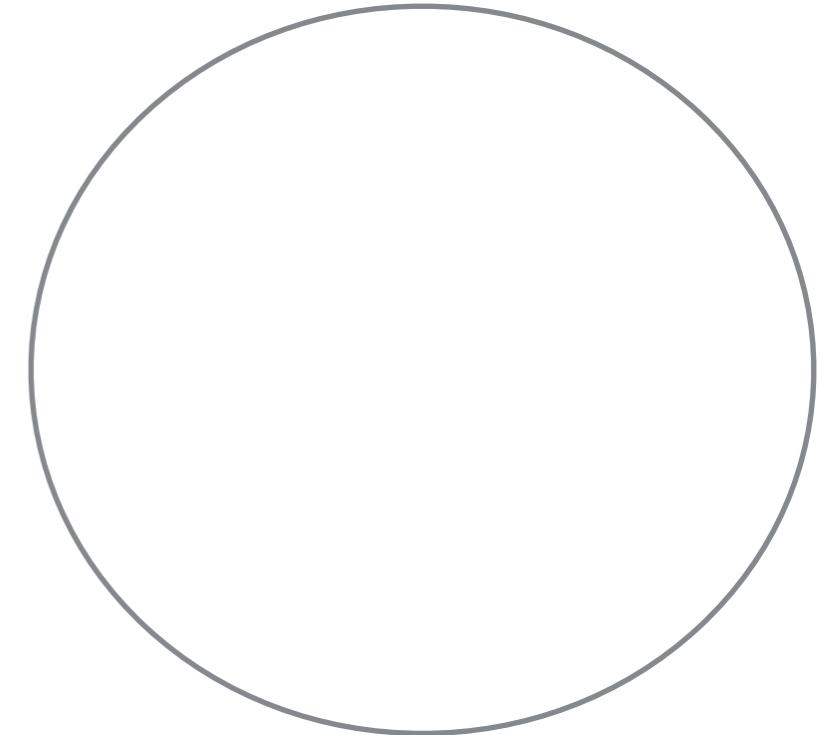
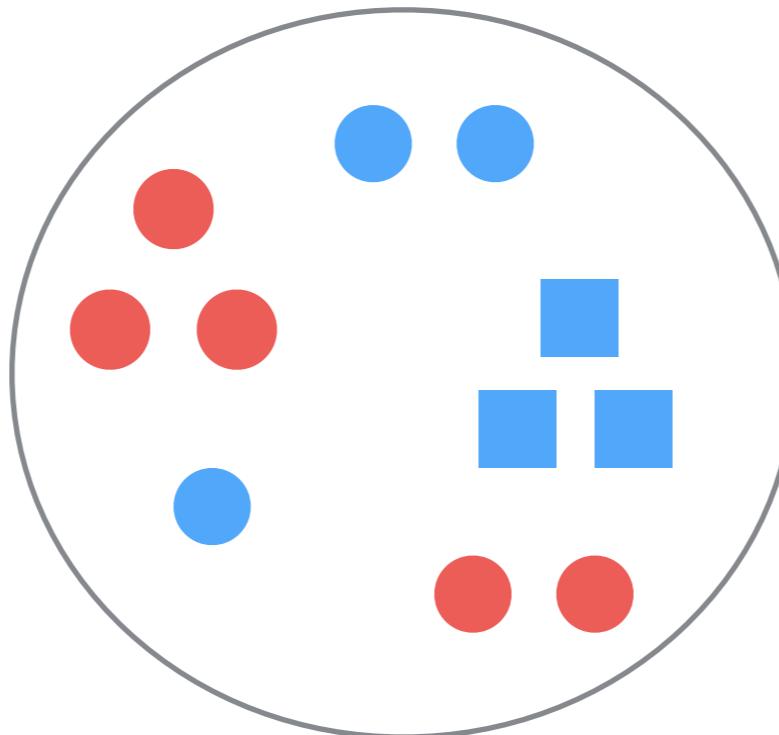
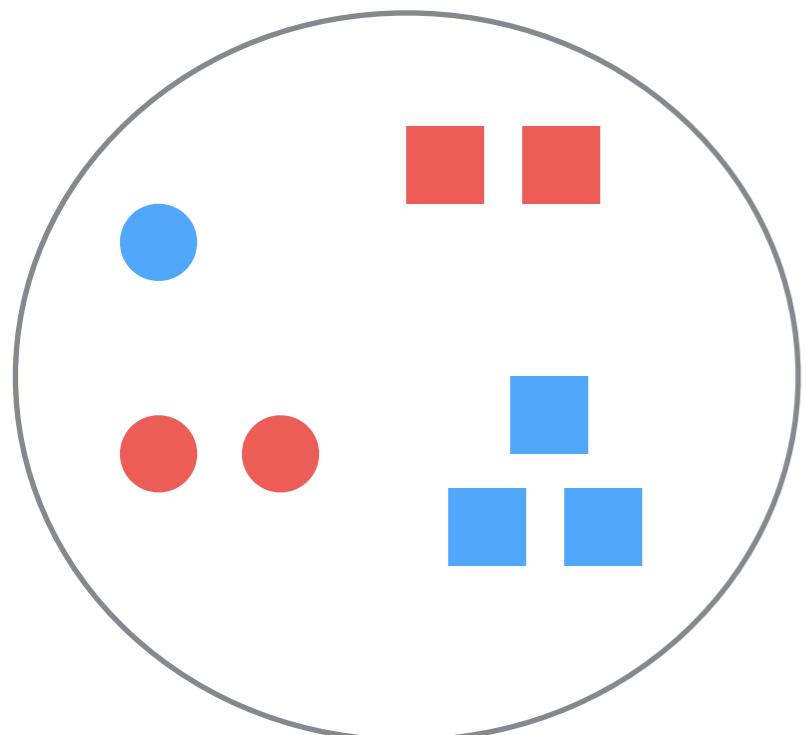
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

R'

R' – R



# Relational Algebra Minus

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

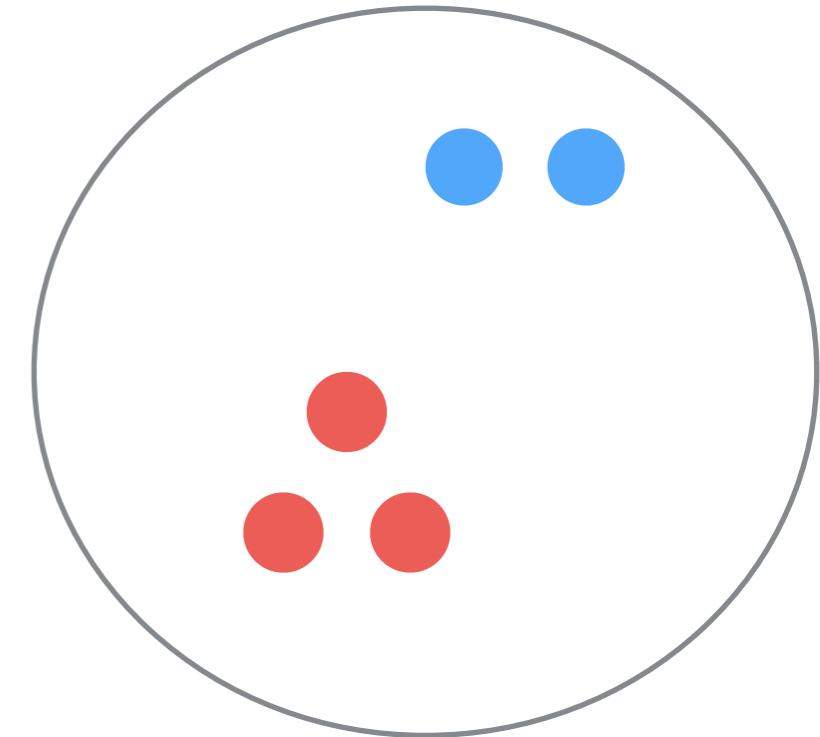
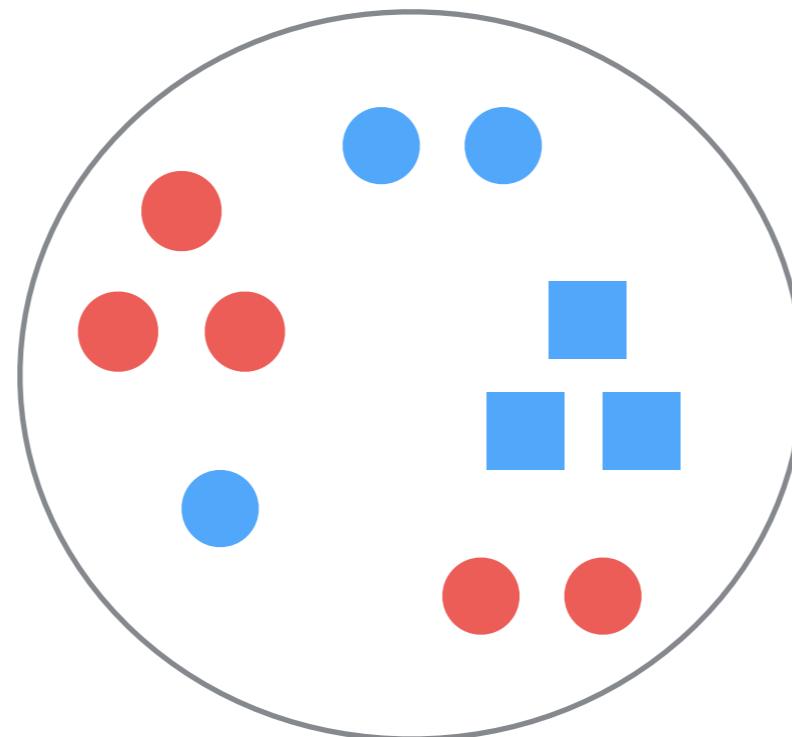
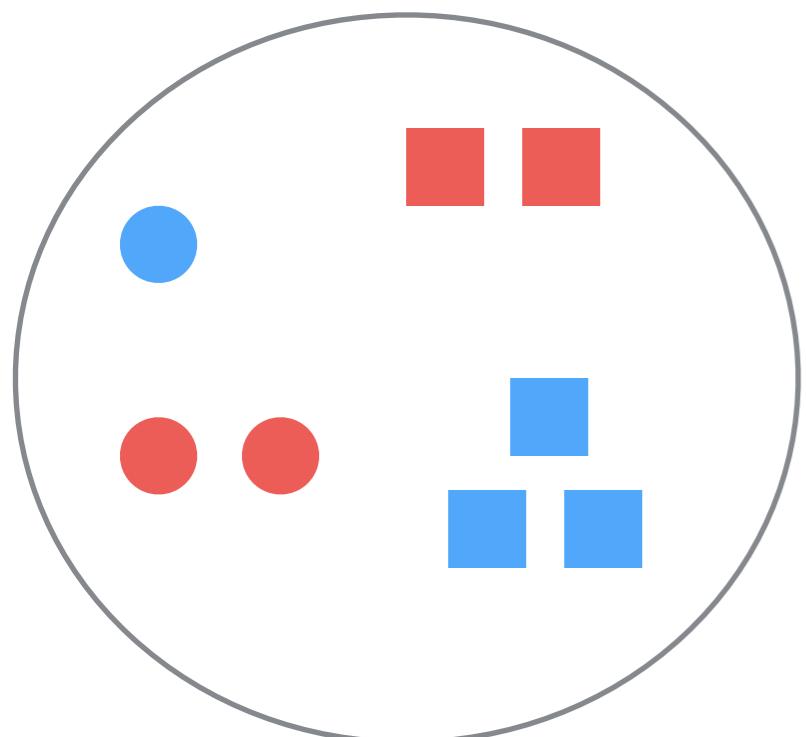
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

R'

R' – R



# Relational Algebra

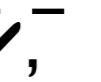
- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

## Cartesian Product

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

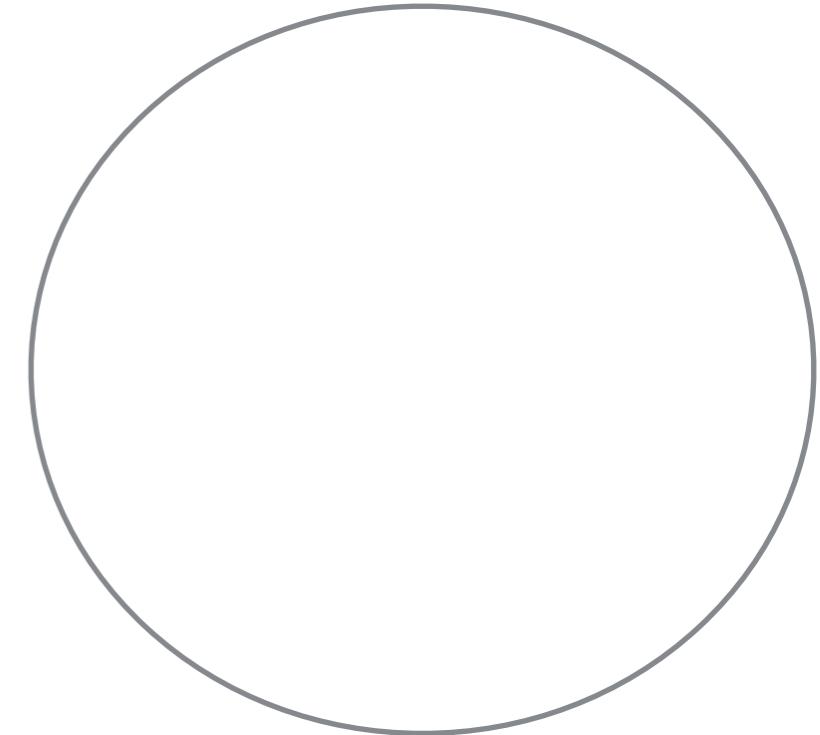
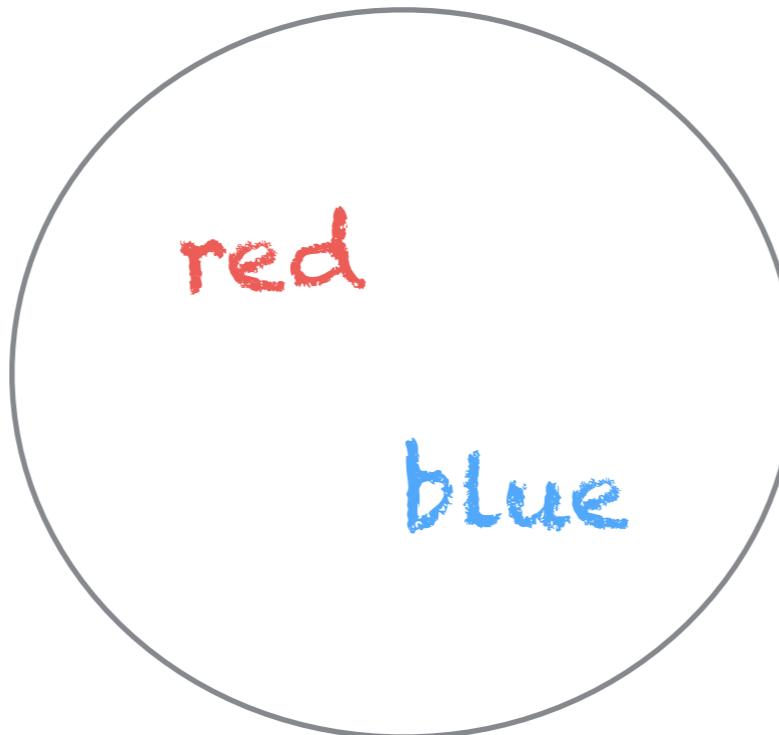
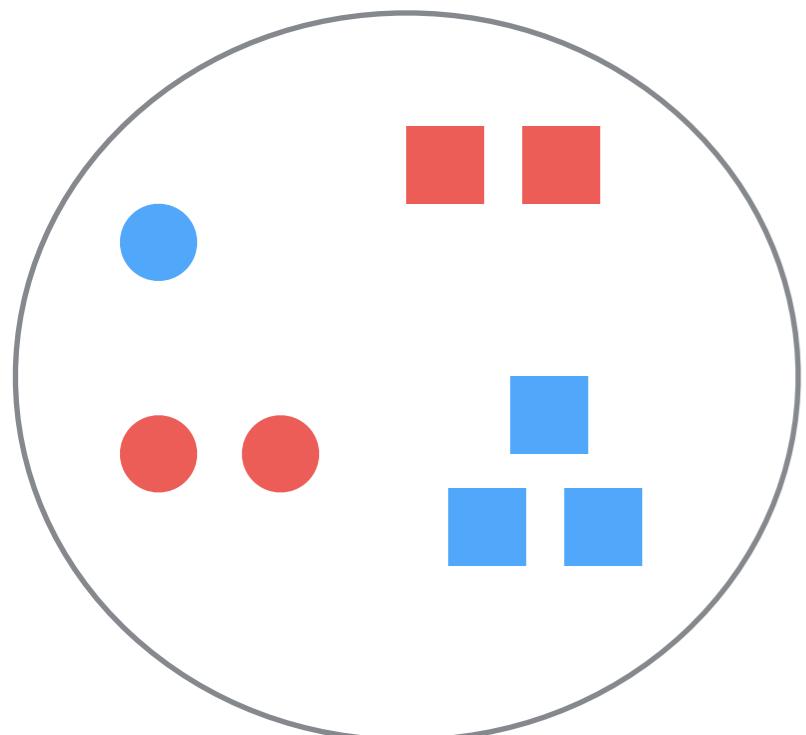
R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

S

$R \times S$



# Relational Algebra

## Cartesian Product

$\text{dom0} = \{ \text{blue}, \text{red} \}$

$\text{dom1} = \{ \text{circle}, \text{square} \}$

$\text{dom2} = \{ 1, 2, 3 \}$

$\text{dom3} = \{ \text{blue}, \text{red}, \text{circle}, \text{square}, 1, 2, 3 \}$

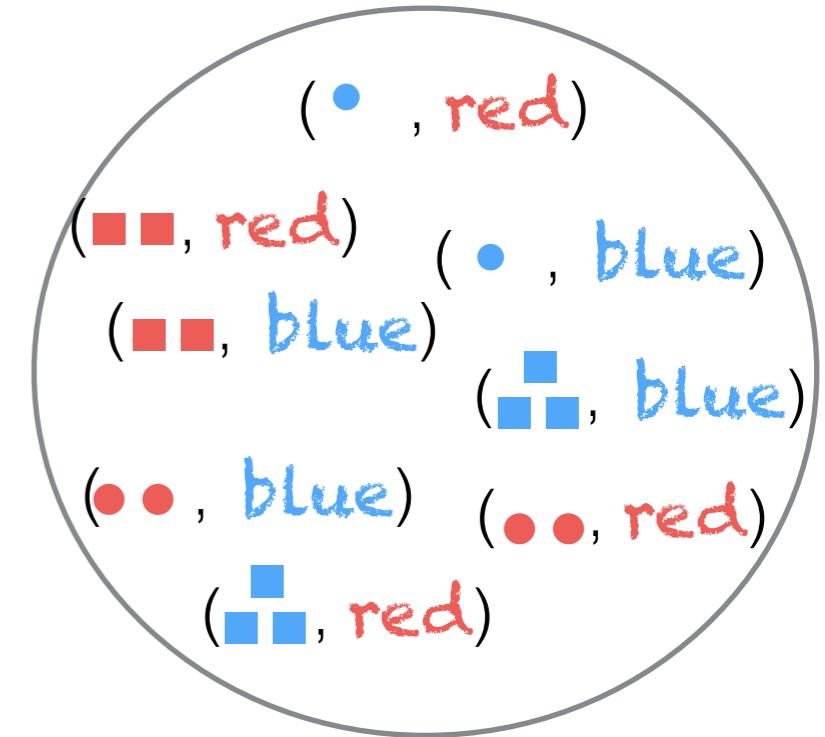
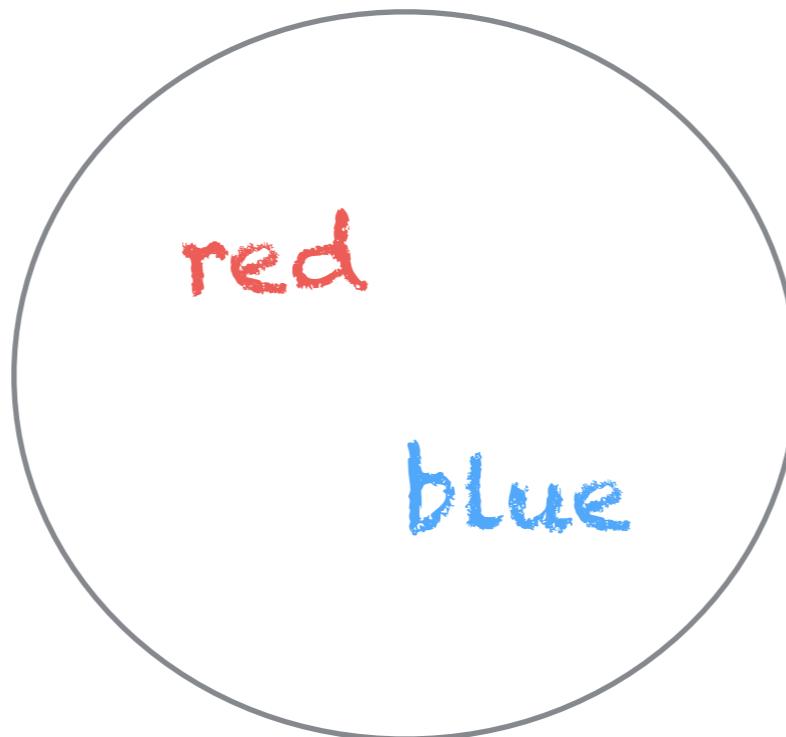
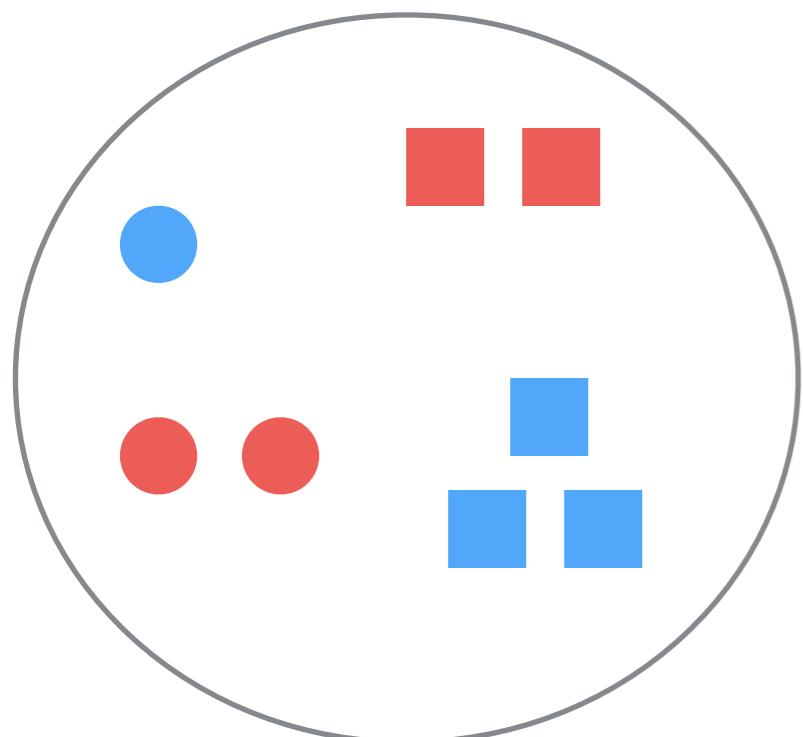
$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$S: (A0:\text{dom0}, A1:\text{dom3})$

$R$

$S$

$R \times S$



# Relational Algebra

## Cartesian Product

$\text{dom0} = \{ \text{blue}, \text{red} \}$

$\text{dom1} = \{ \text{circle}, \text{square} \}$

$\text{dom2} = \{ 1, 2, 3 \}$

$\text{dom3} = \{ \text{blue}, \text{red}, \text{circle}, \text{square}, 1, 2, 3 \}$

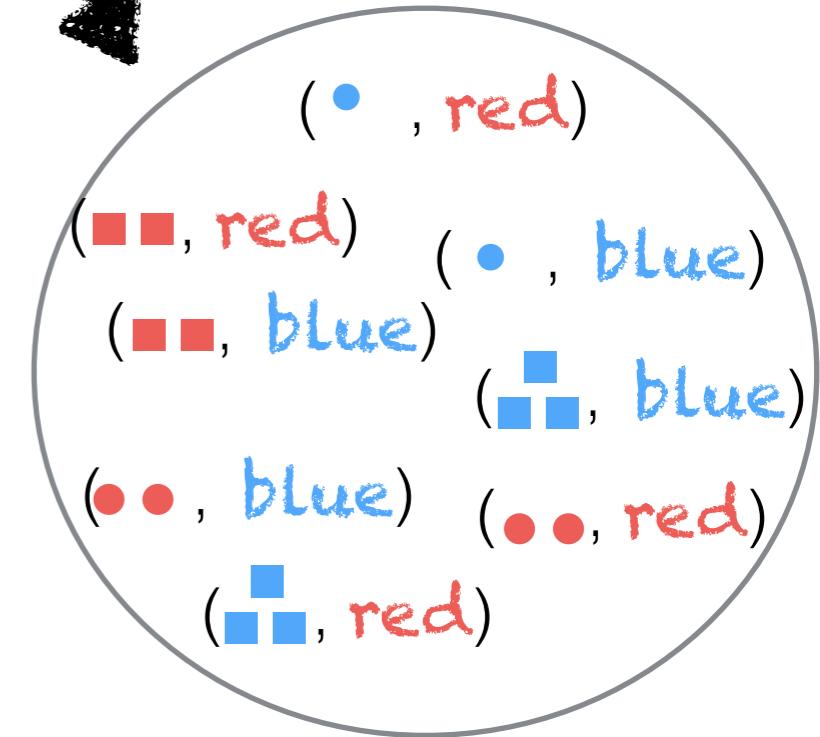
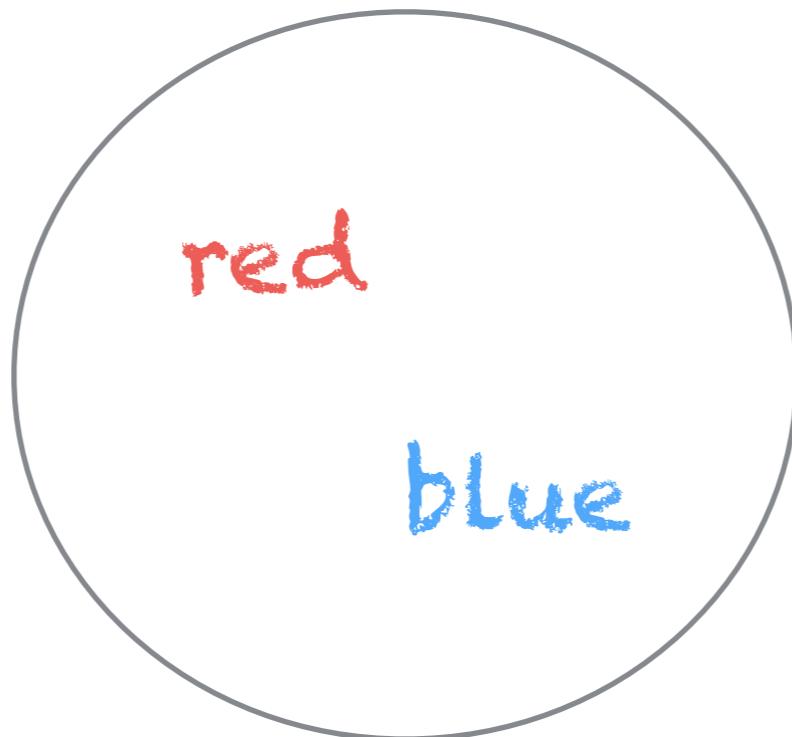
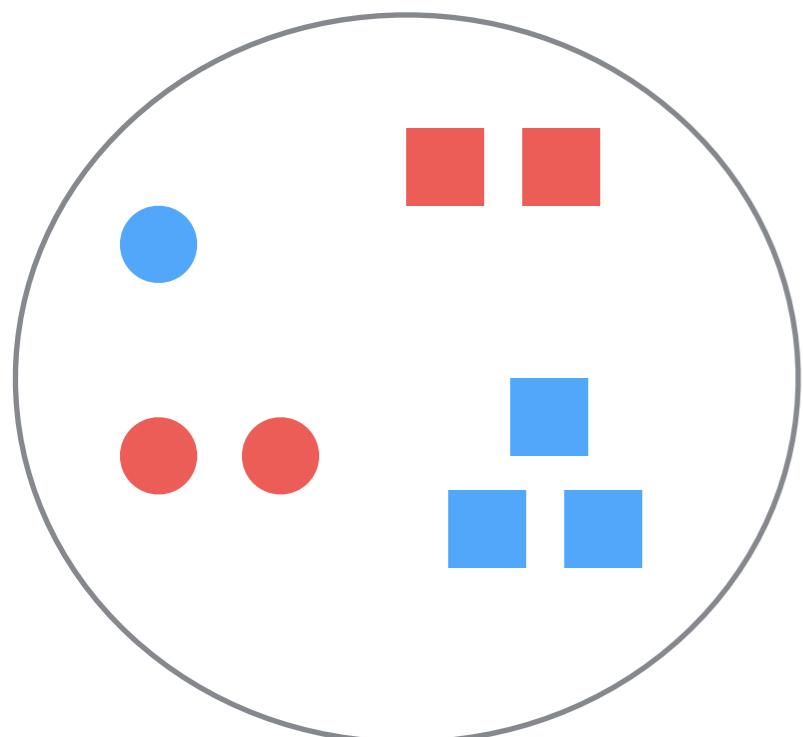
$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$S: (A0:\text{dom0}, A1:\text{dom3})$

$R$

kinda useless

$R \times S$



# Relational Algebra

## Cartesian Product

$\text{dom0} = \{ \text{blue}, \text{red} \}$

$\text{dom1} = \{ \text{circle}, \text{square} \}$

$\text{dom2} = \{ 1, 2, 3 \}$

$\text{dom3} = \{ \text{blue}, \text{red}, \text{circle}, \text{square}, 1, 2, 3 \}$

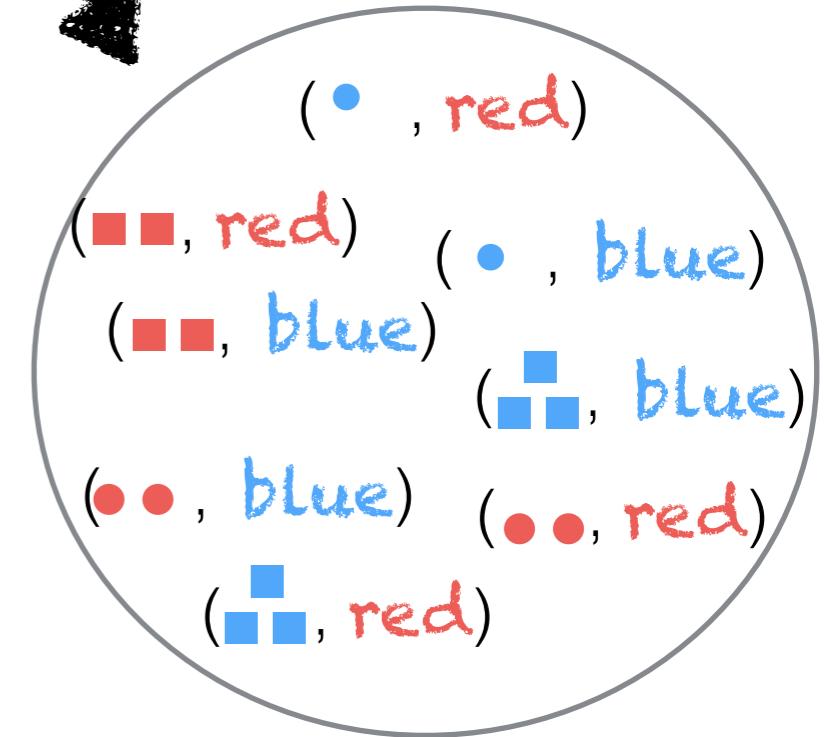
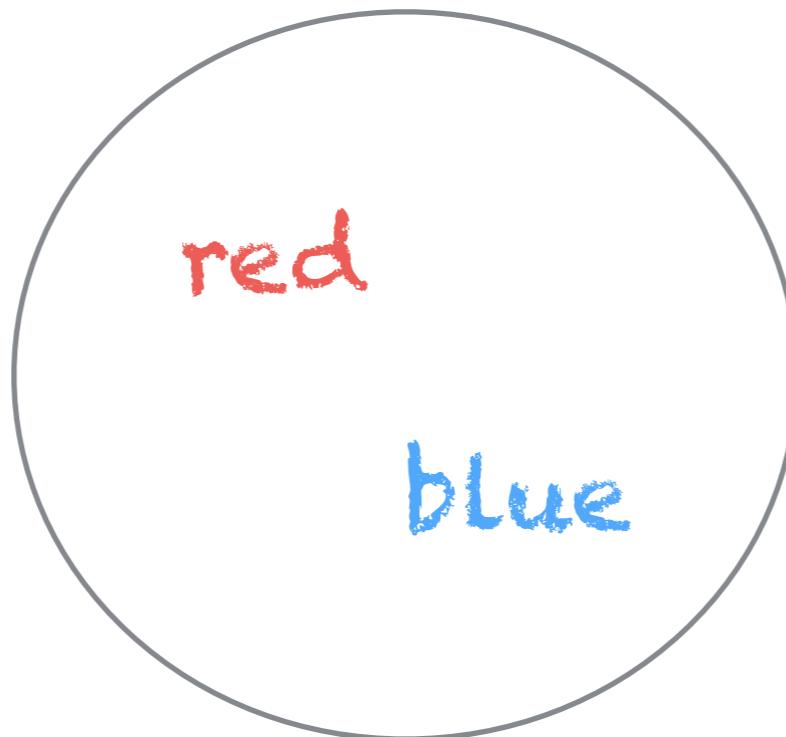
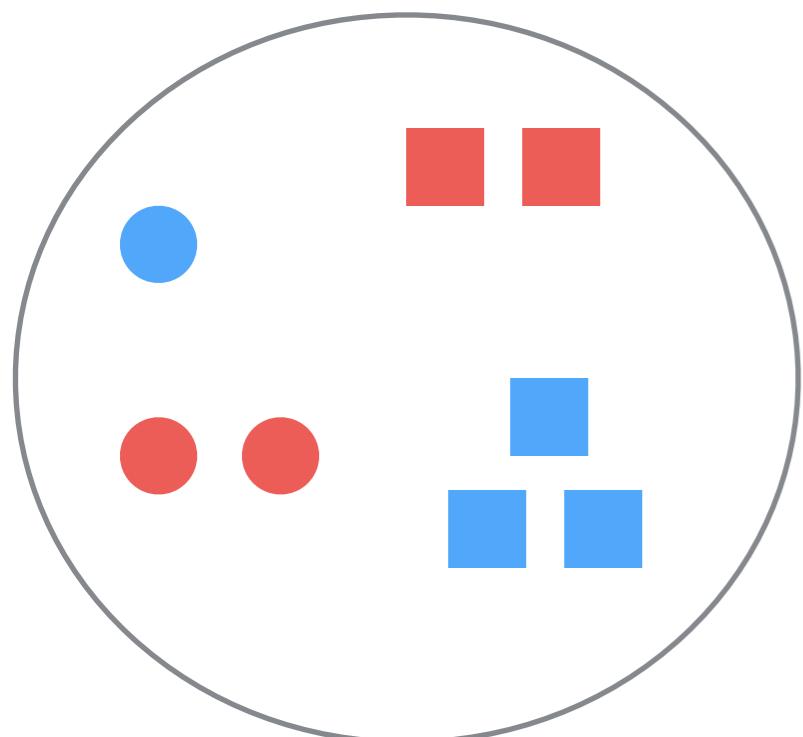
$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$S: (A0:\text{dom0}, A1:\text{dom3})$

$R$

...more later...

$R \times S$



# Relational Algebra

- $\sigma$  selection
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

## Rename

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

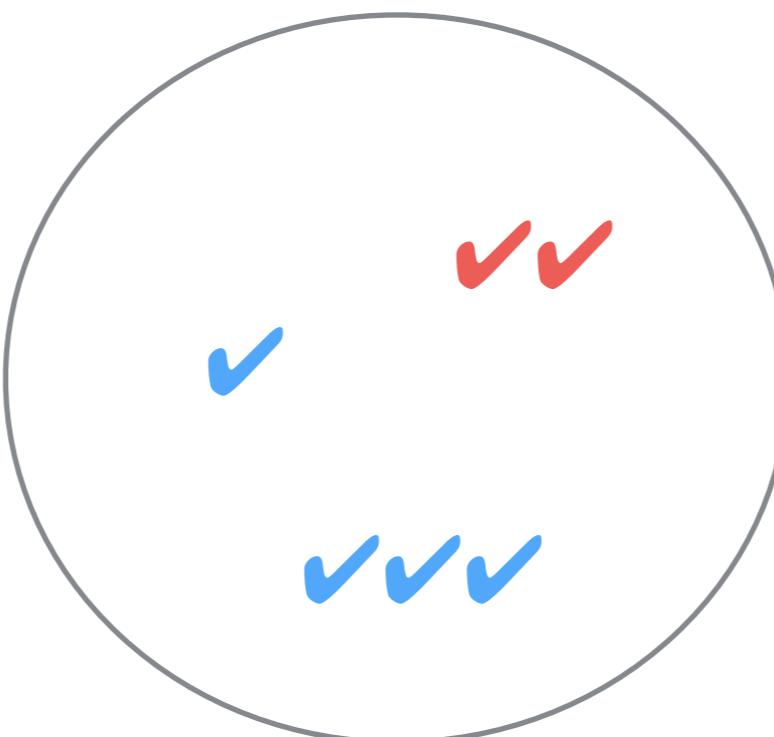
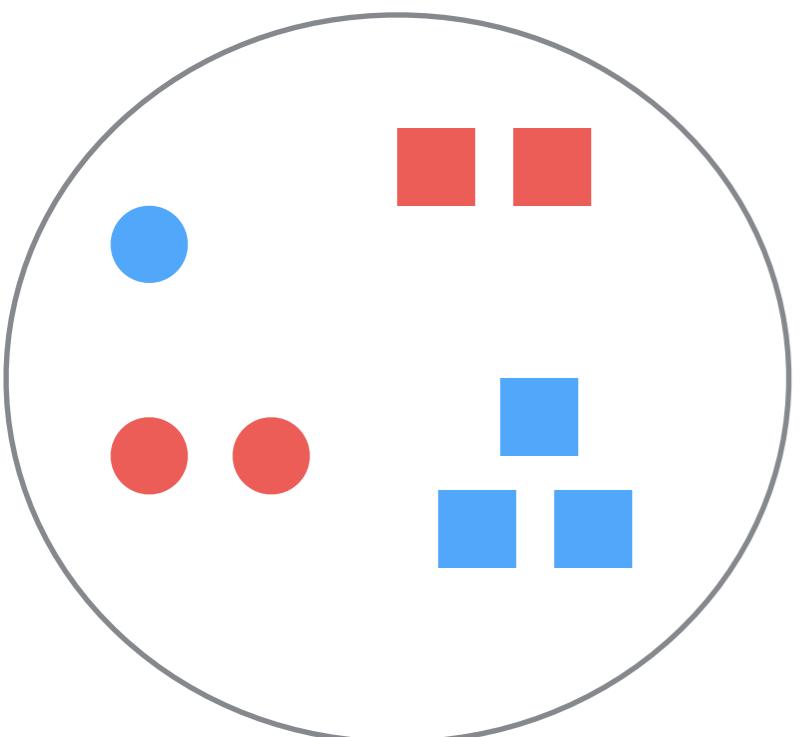
dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

$\pi_{A0,A2}(R)$

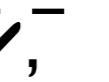


# Relational Algebra

## Rename

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

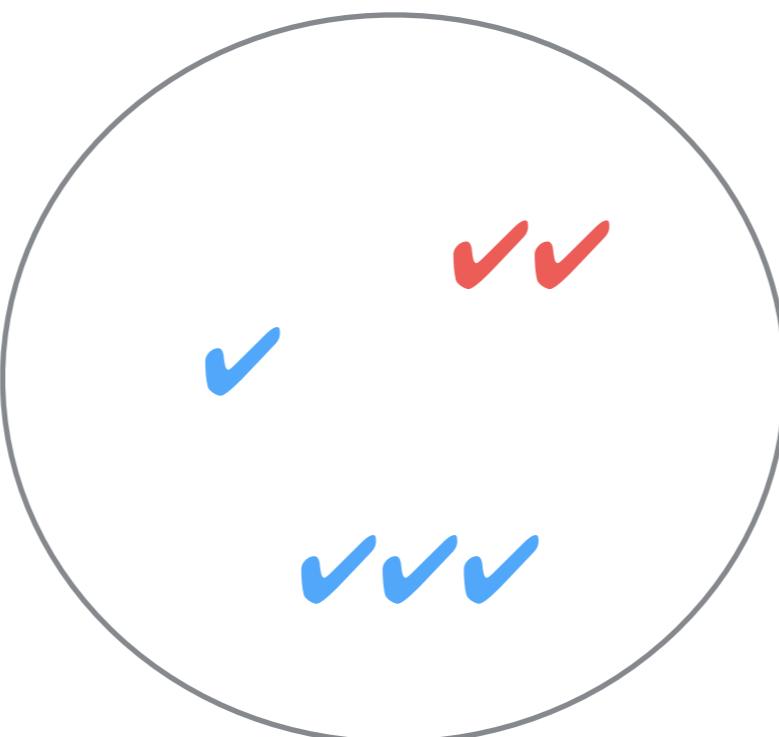
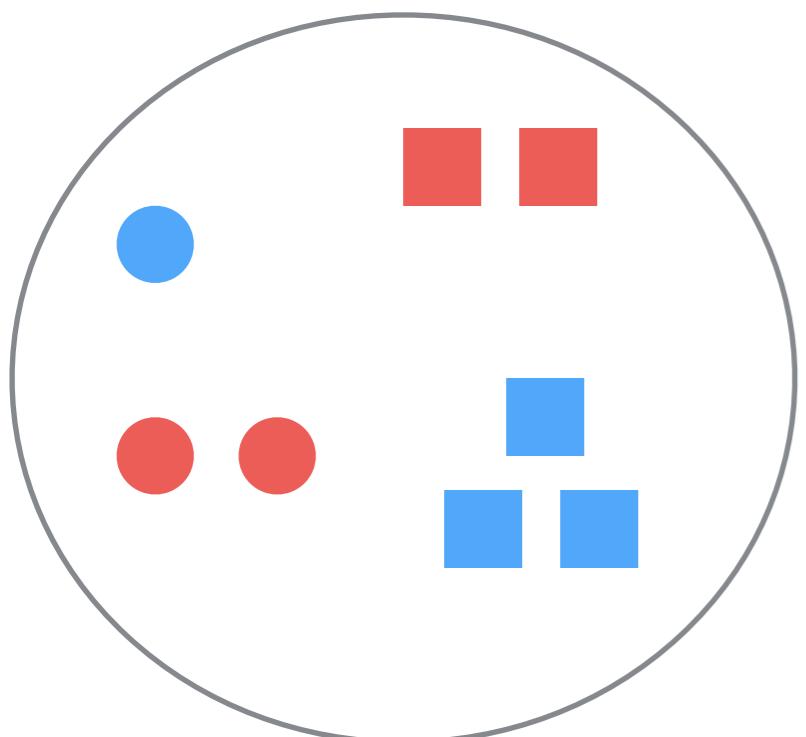
dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

R

new\_R= $\pi_{A0,A2}(R)$

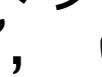


# Relational Algebra

## Rename

dom0 = { ,  }

dom1 = { ,  }

dom2 = { , ,  }

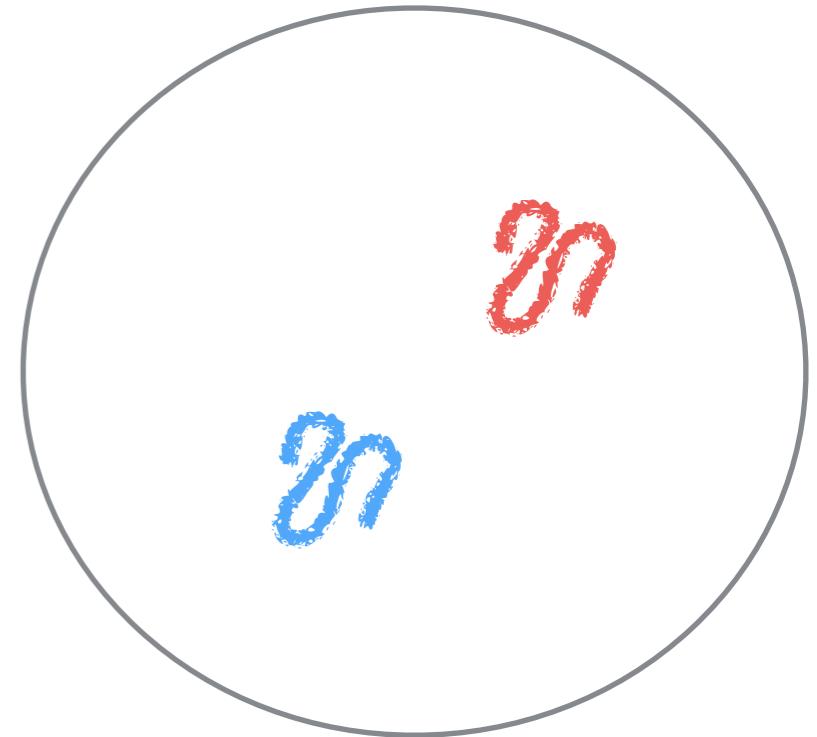
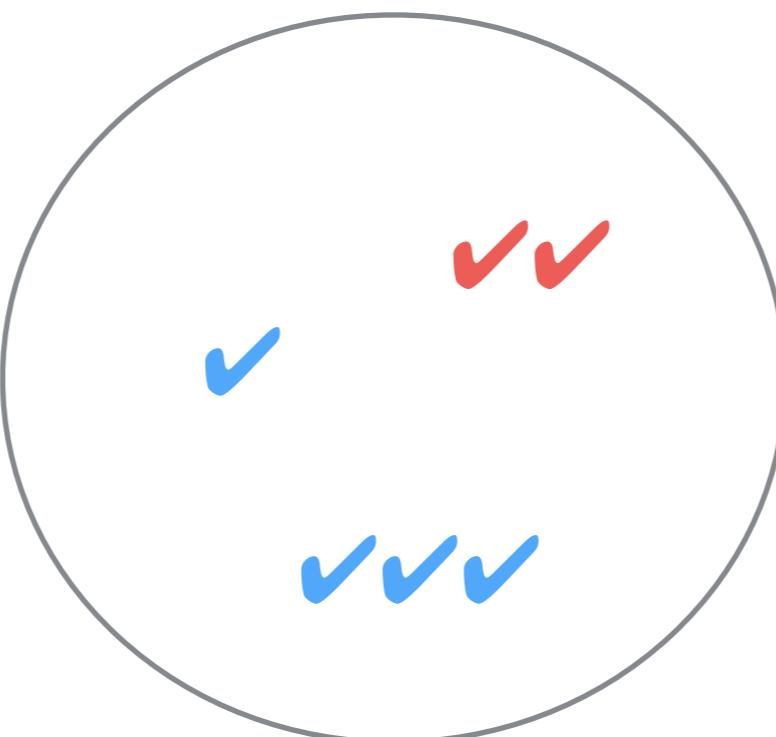
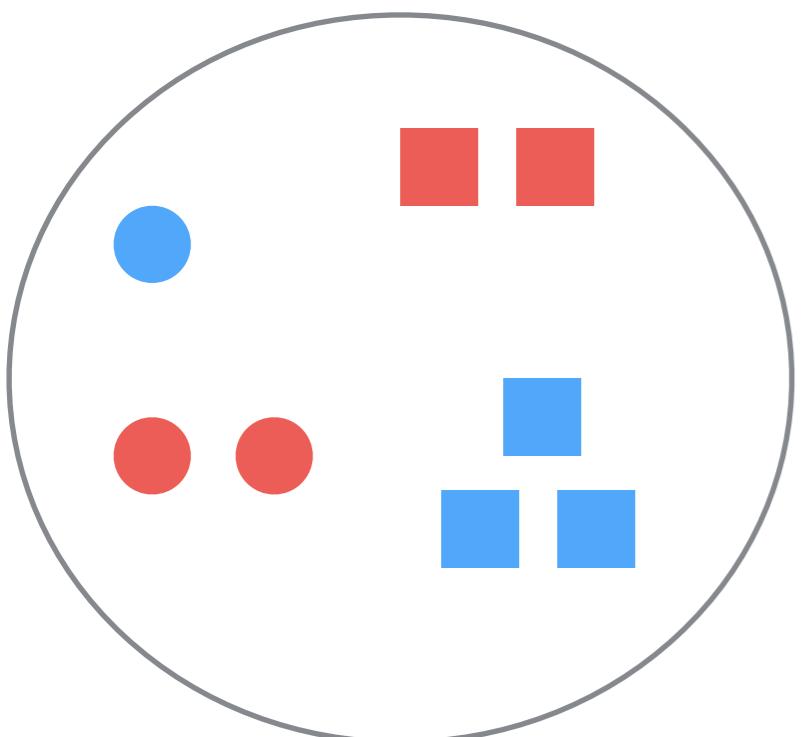
dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

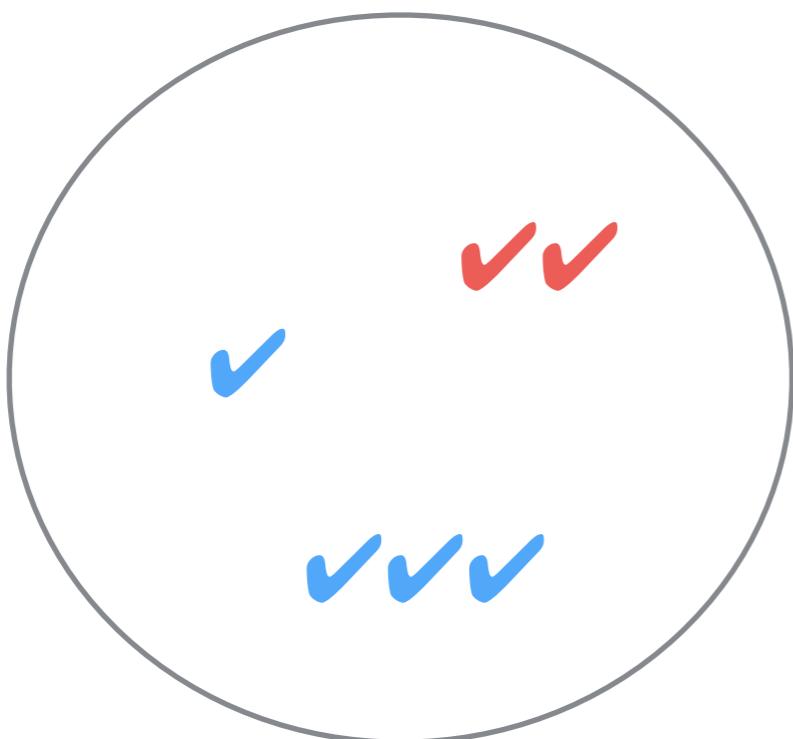
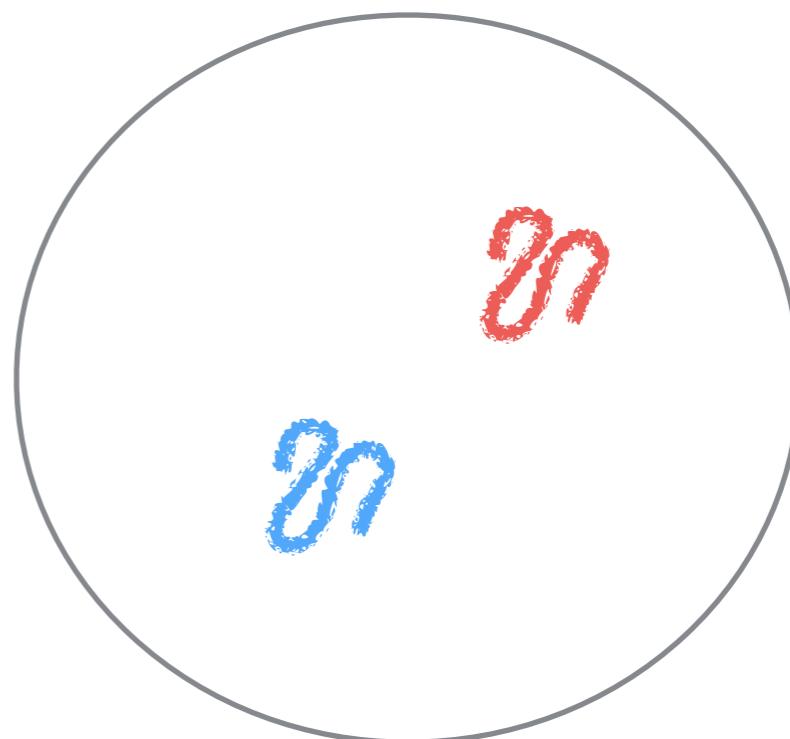
R

new\_R= $\pi_{A0,A2}(R)$   $\pi_{A0}(\text{new\_R})$



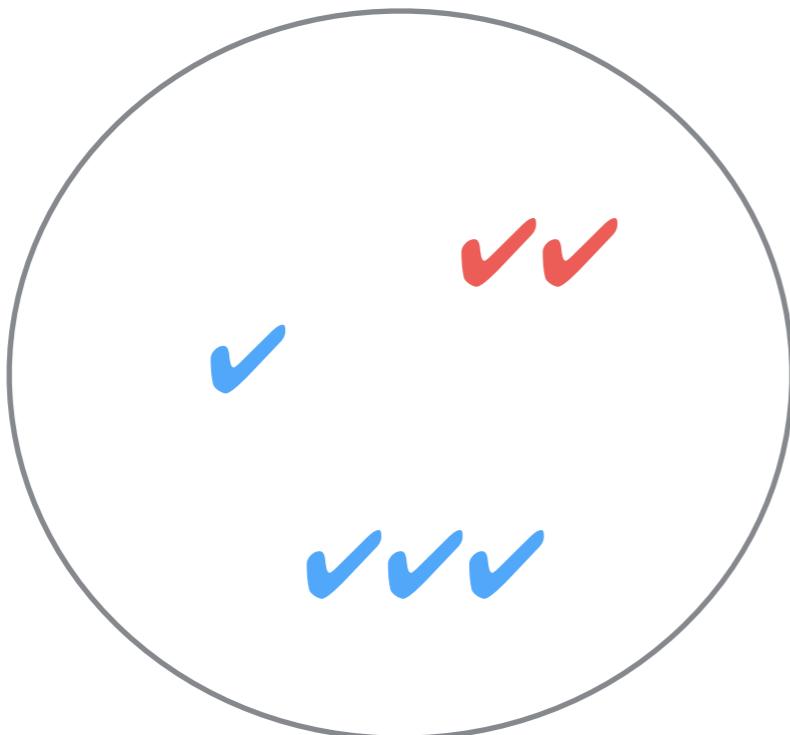
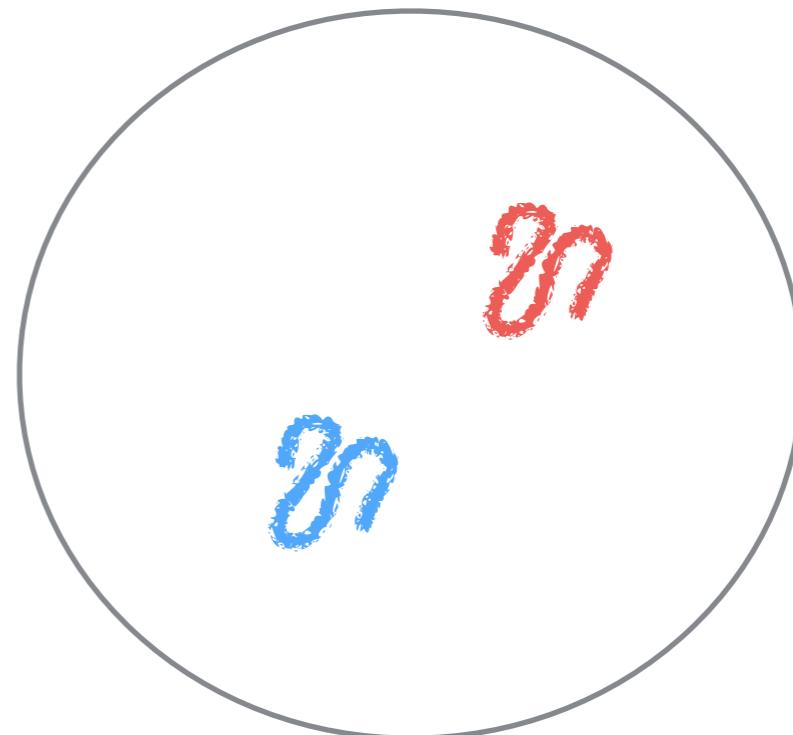
# Relational Algebra

## Rename

$$\rho_{\text{new\_R\_final}}(\text{new\_R})$$

$$\text{new\_R} = \pi_{A0, A2}(R)$$

$$\pi_{A0}(\text{new\_R\_final})$$

# Relational Algebra

## Rename

$$\rho_{\text{new\_R\_final}}(A_0\text{ working jan28 do\_not\_delete\_this\_one}, A_1)(\text{new\_R})$$

$$\text{new\_R} = \pi_{A_0, A_2}(R)$$

$$\pi_{A_0\text{ working jan28 do\_not\_delete\_this\_one}}(\text{new\_R\_final})$$

# Relational Algebra

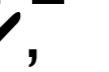
- $\sigma$  selection
  - “complete set”
    - i.e. any of the core relations we want to express can be expressed as a combination of these operations.
- $\pi$  project
- $\cup$  union
- $-$  minus
- $\times$  cross
- $\rho$  rename

# Relational Algebra

## Join

dom0 = { ,  }

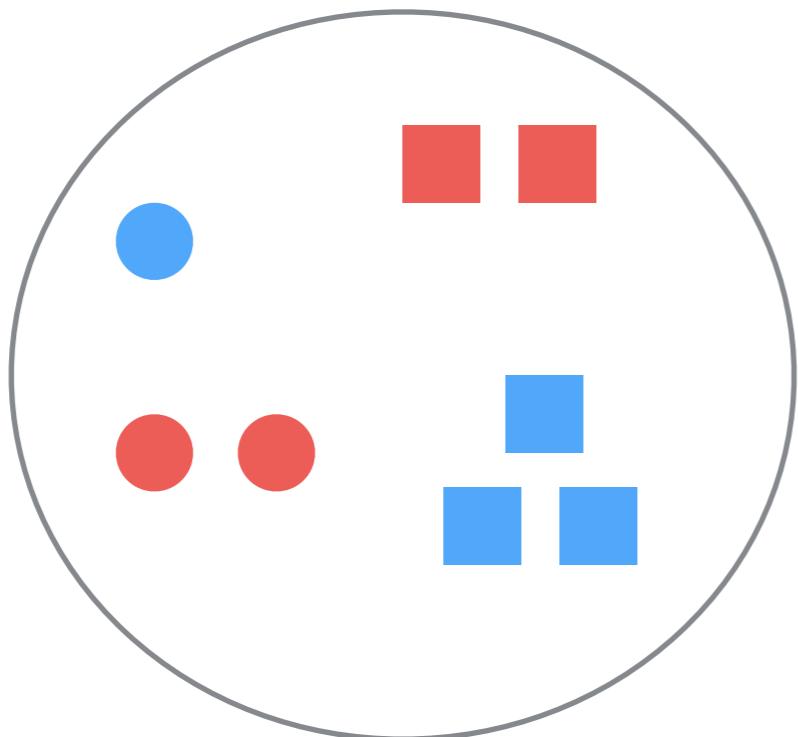
dom1 = { ,  }

dom2 = { , ,  }

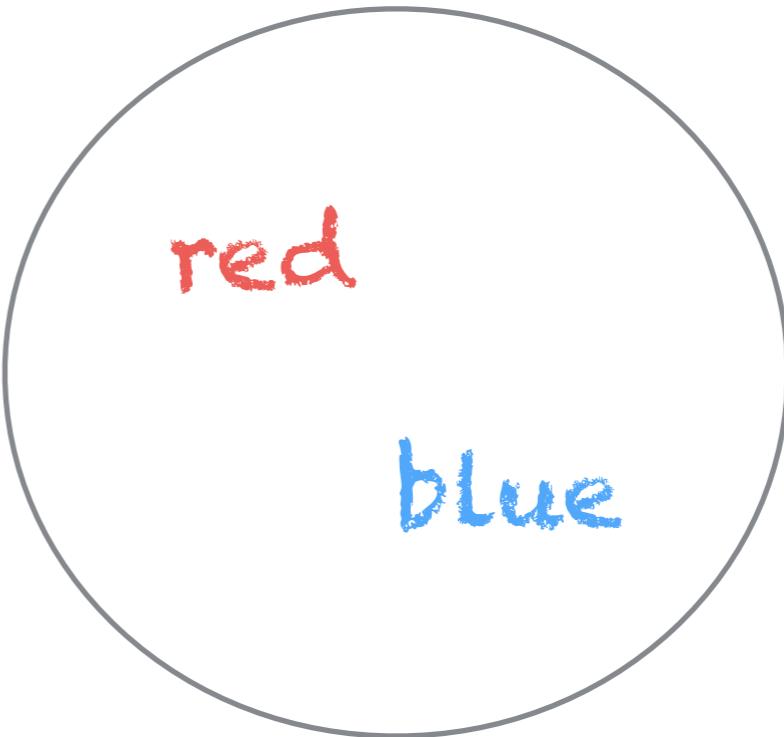
dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)  
S: (A0:dom0, A1:dom3)

R



S



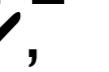
Find the names of the colors of each element of R.

# Relational Algebra

## Join

dom0 = { ,  }

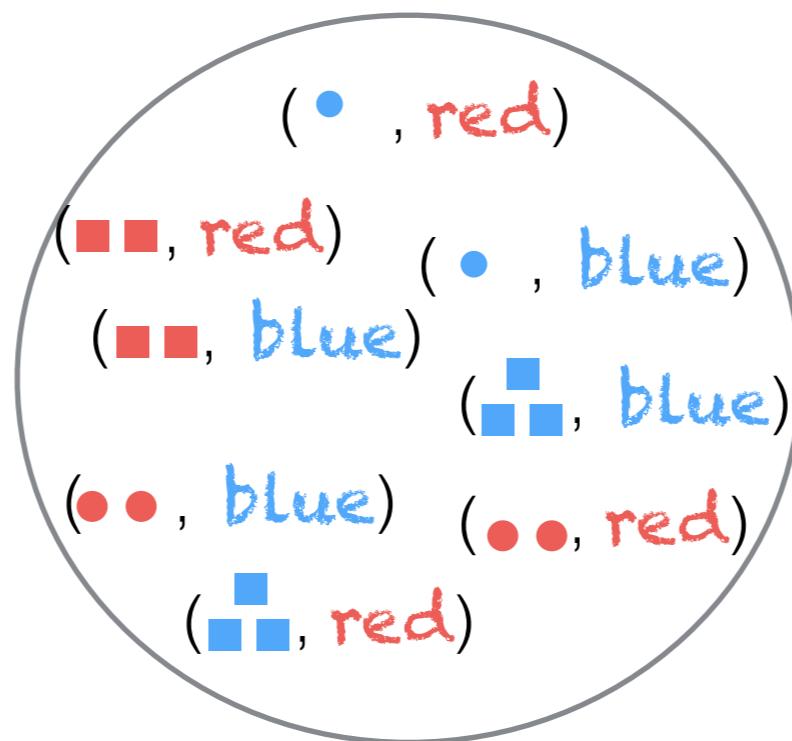
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)  
S: (A0:dom0, A1:dom3)

$R \times S$



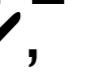
Find the names of the colors of each element of R.

# Relational Algebra

## Join

dom0 = { ,  }

dom1 = { ,  }

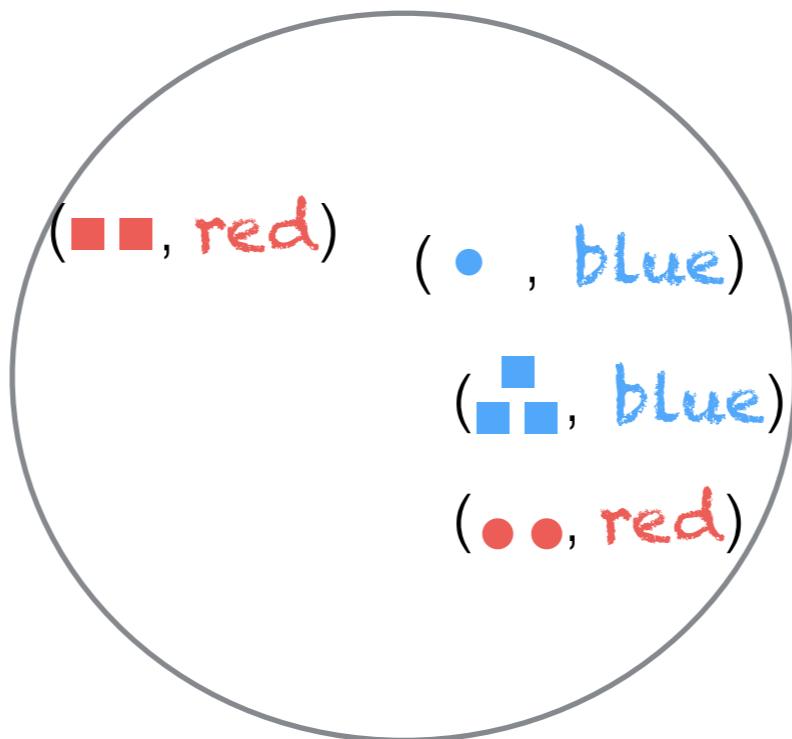
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

S: (A0:dom0, A1:dom3)

$$\sigma_{R.A0 = S.A0}(R \times S)$$



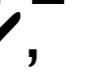
Find the names of the colors of each element of R.

# Relational Algebra

## Join

dom0 = { ,  }

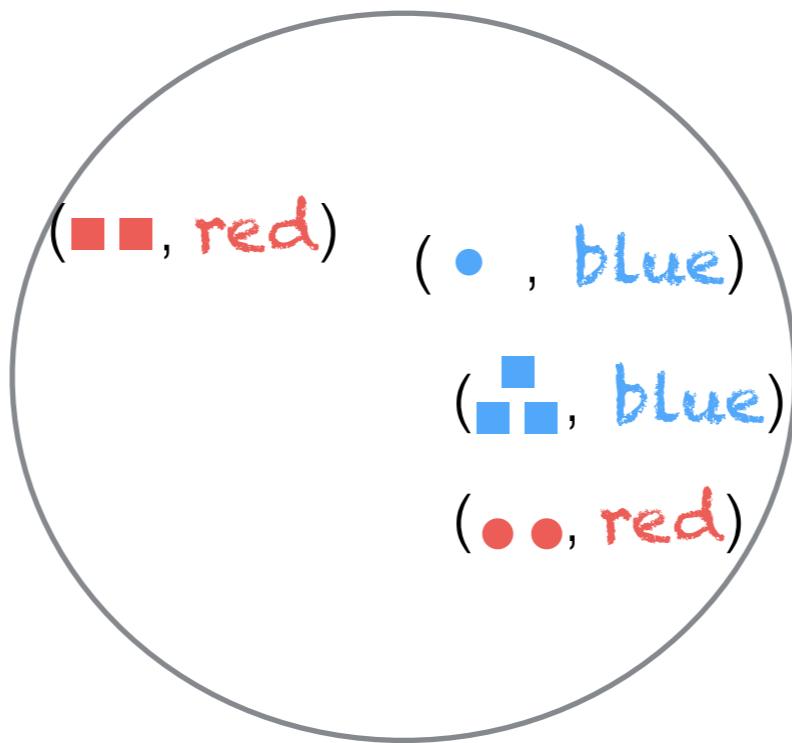
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)  
S: (A0:dom0, A1:dom3)

$$R \bowtie_{R.A0} S.A0 = S.A0$$



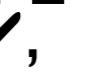
Find the names of the colors of each element of R.

# Relational Algebra

## Intersection

dom0 = { ,  }

dom1 = { ,  }

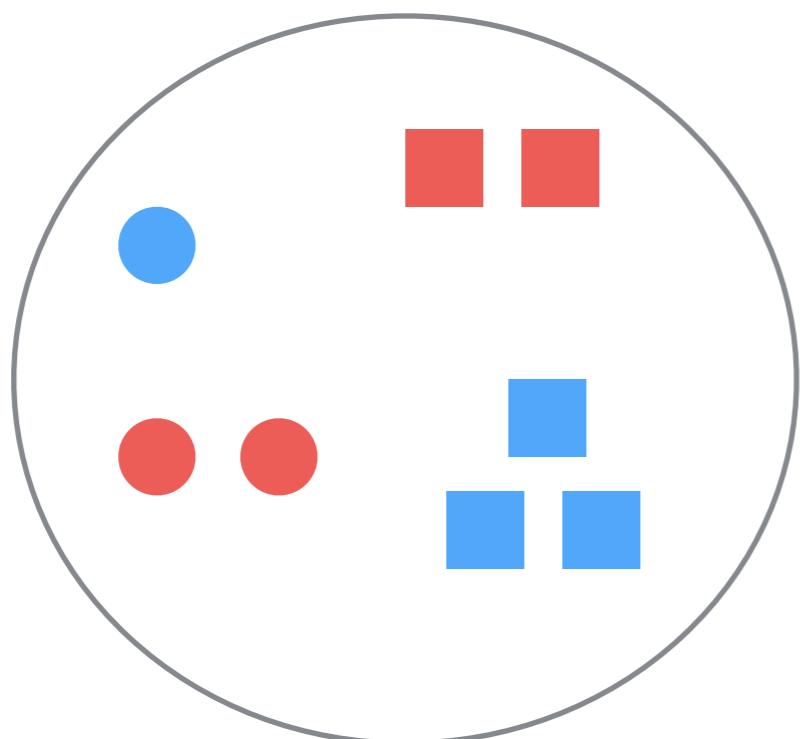
dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

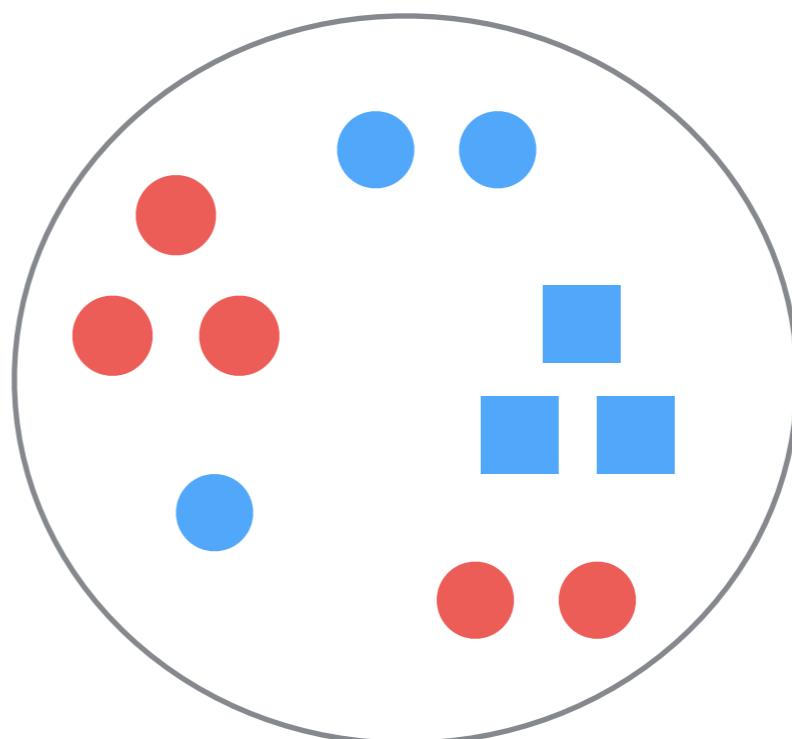
R: (A0:dom0, A1:dom1, A2:dom2)

R': (A0:dom0, A1:dom1, A2:dom2)

R



R'



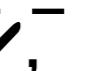
Find the elements appearing in both R and R'.

# Relational Algebra

## Intersection

dom0 = { ,  }

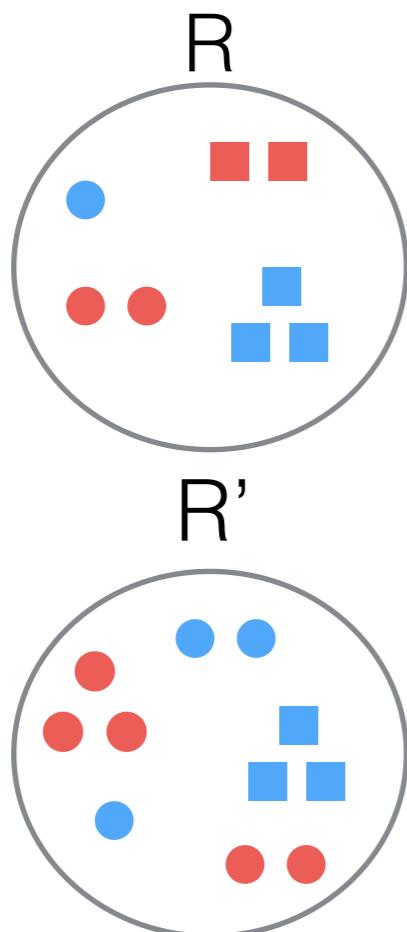
dom1 = { ,  }

dom2 = { , ,  }

dom3 = {blue, red, circle, square, 1, 2, 3}

R: (A0:dom0, A1:dom1, A2:dom2)

R': (A0:dom0, A1:dom1, A2:dom2)



- $\sigma$  selection      •  $-$  minus
- $\pi$  project      •  $\times$  cross
- $\cup$  union      •  $\rho$  rename

Find the elements appearing in both R and R'.

# Relational Algebra

## Intersection

$\text{dom0} = \{ \text{blue, red} \}$

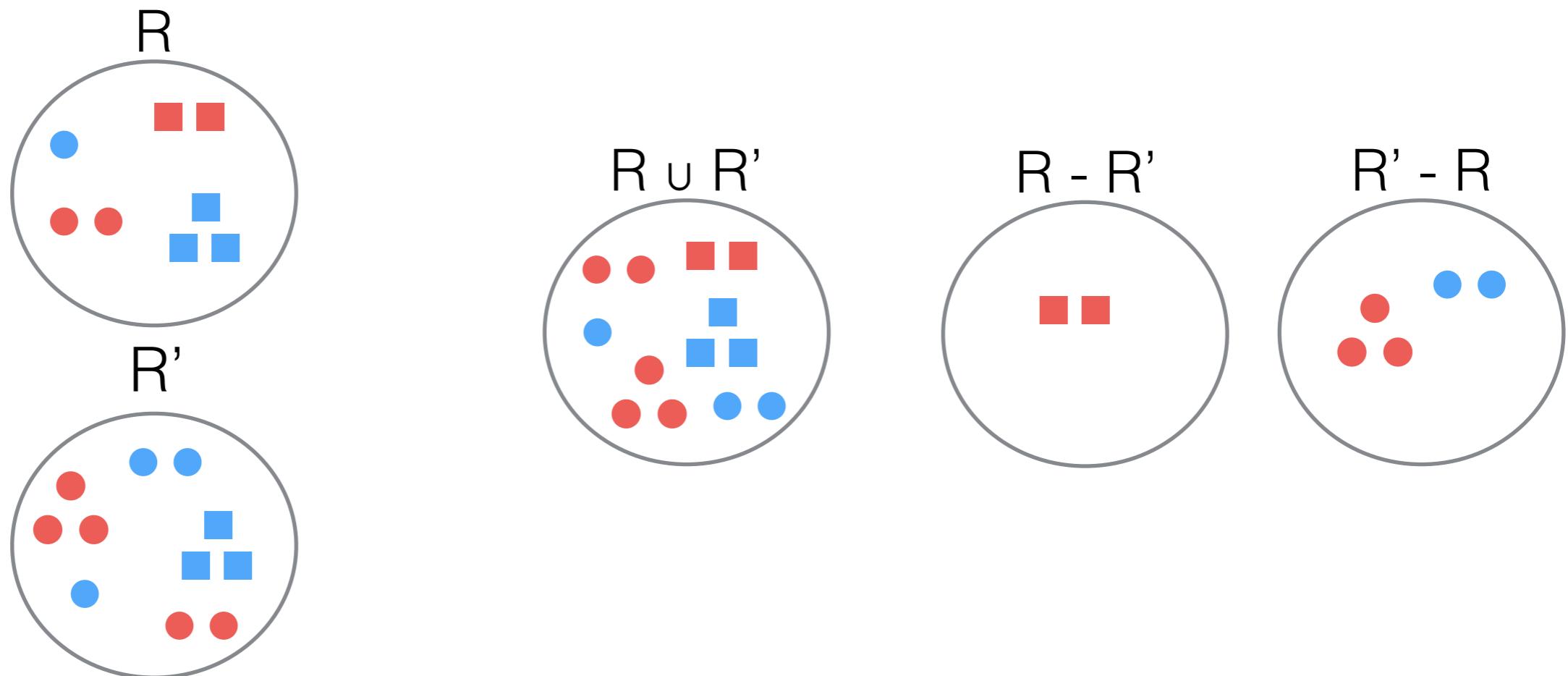
$\text{dom1} = \{ \text{circle, square} \}$

$\text{dom2} = \{ \text{1, 2, 3} \}$

$\text{dom3} = \{ \text{blue, red, circle, square, 1, 2, 3} \}$

$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$R': (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$



Find the elements appearing in both R and R'.

# Relational Algebra

## Intersection

$\text{dom0} = \{ \text{blue, red} \}$

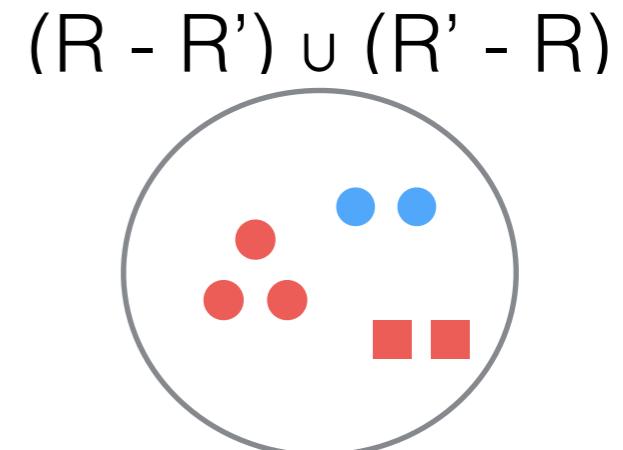
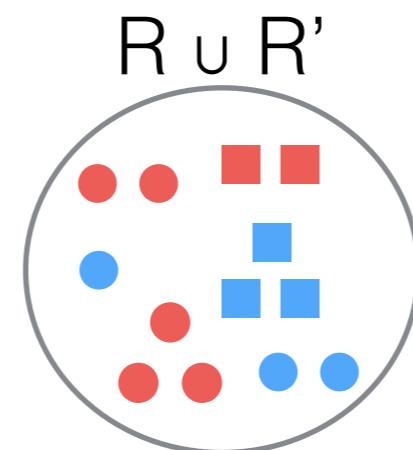
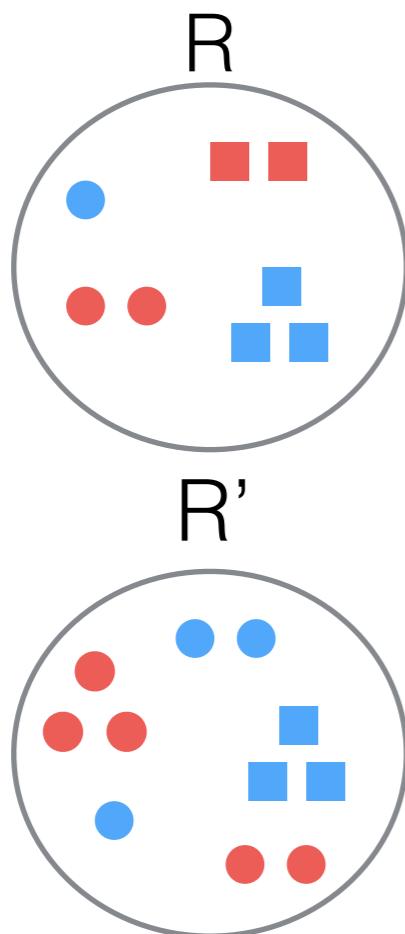
$\text{dom1} = \{ \text{circle, square} \}$

$\text{dom2} = \{ \text{1, 2, 3} \}$

$\text{dom3} = \{ \text{blue, red, circle, square, 1, 2, 3} \}$

$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$R': (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$



Find the elements appearing in both  $R$  and  $R'$ .

# Relational Algebra

## Intersection

$\text{dom0} = \{ \text{blue, red} \}$

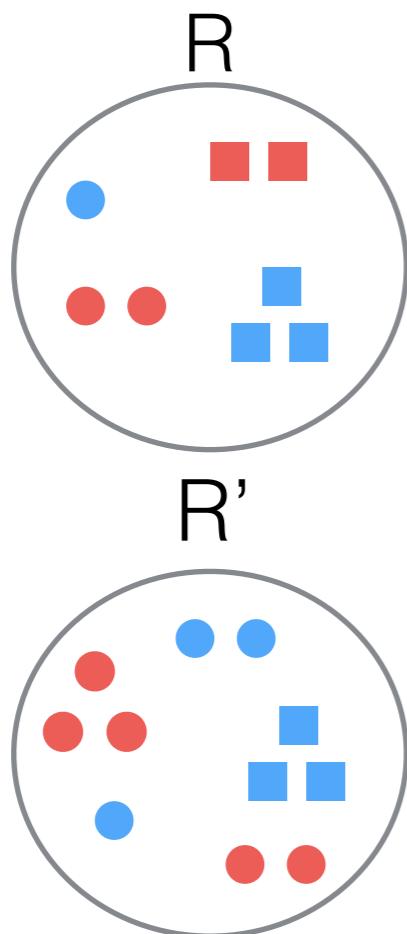
$\text{dom1} = \{ \text{circle, square} \}$

$\text{dom2} = \{ \text{1, 2, 3} \}$

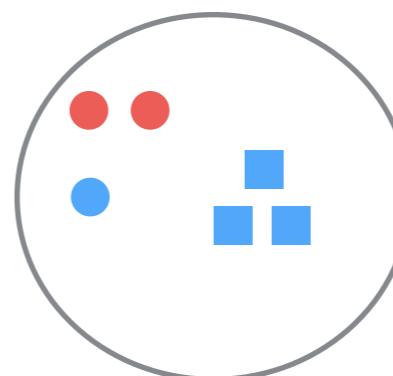
$\text{dom3} = \{ \text{blue, red, circle, square, 1, 2, 3} \}$

$R: (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$

$R': (A0:\text{dom0}, A1:\text{dom1}, A2:\text{dom2})$



$$R \cup R' - (R - R') \cup (R' - R)$$



Find the elements appearing in both R and R'.

k bye