

# Lecture 15 – Domain Specific Accelerators

Stanford CS343D (Winter 2023)  
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# Domain-Specific Software Stack

Domain-Specific Language/Library

Domain-Specific Compiler

Domain-Specific Hardware

# Why Domain-Specific Architectures

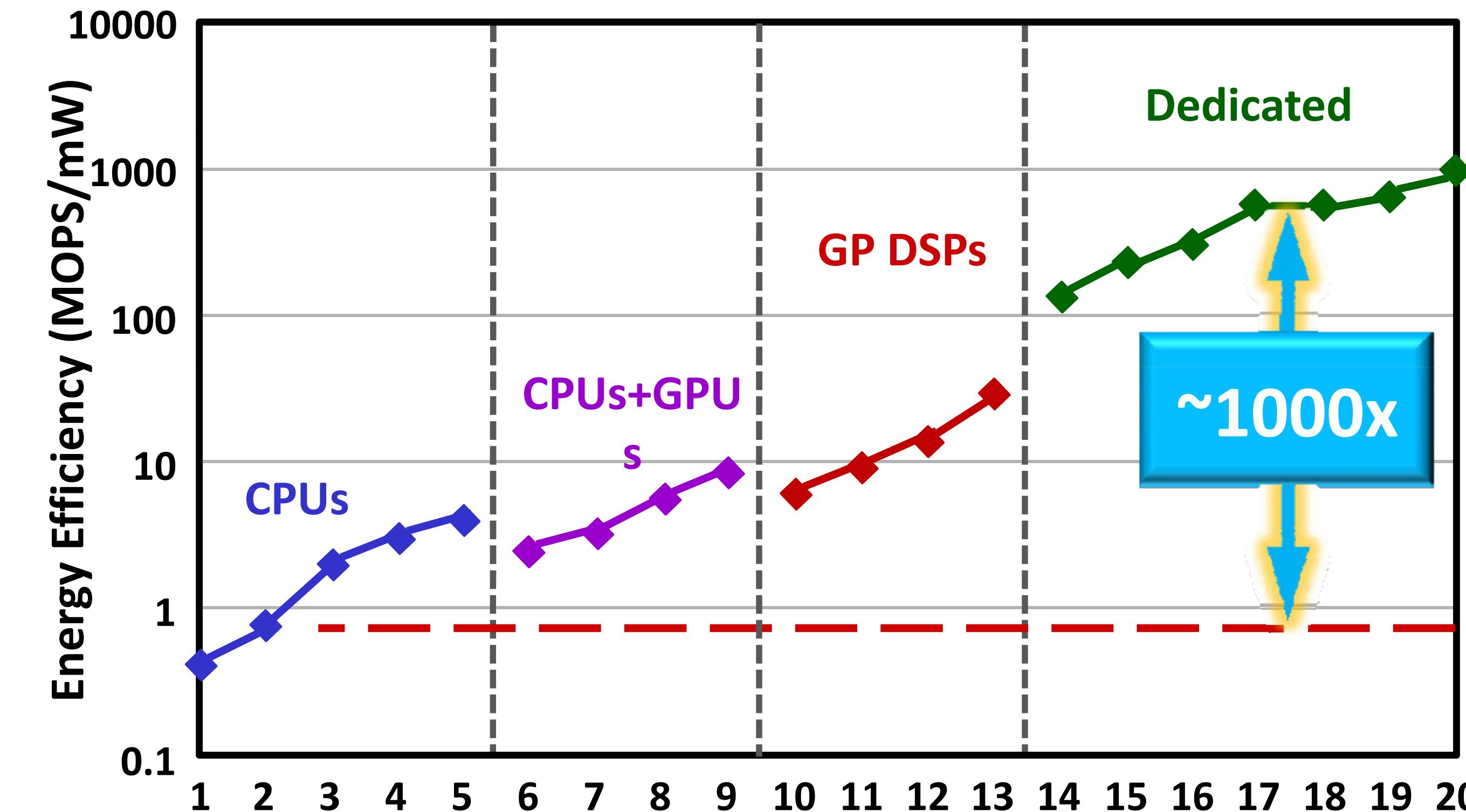
Chip type:

Microprocessor

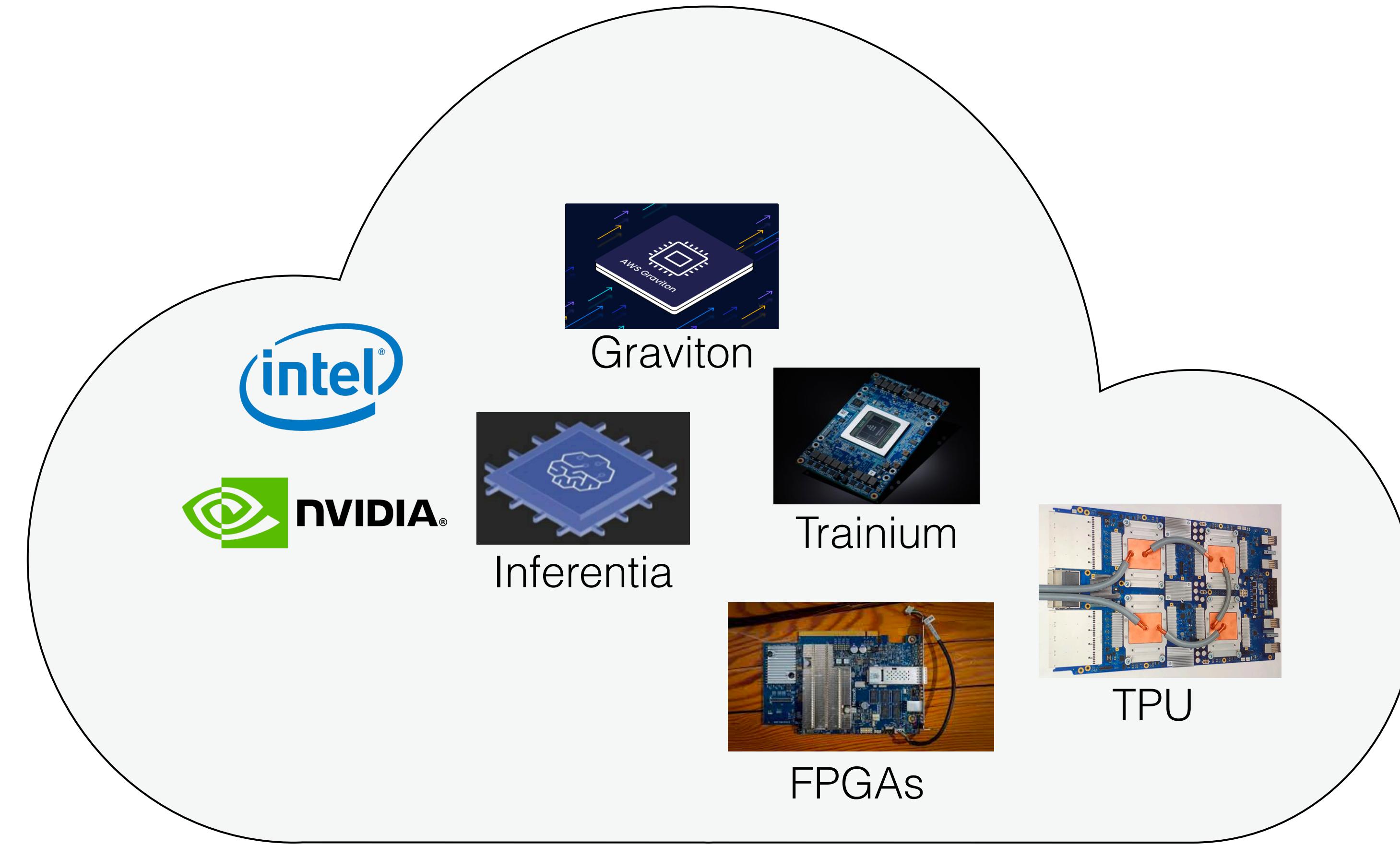
Microprocessor + GPU

General purpose DSP

Dedicated design

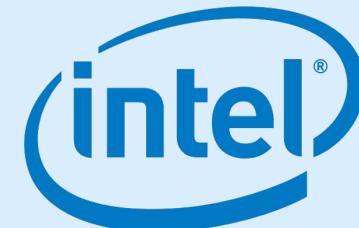


# Hardware in Industry



# Types of Hardware

## Multicore CPUs

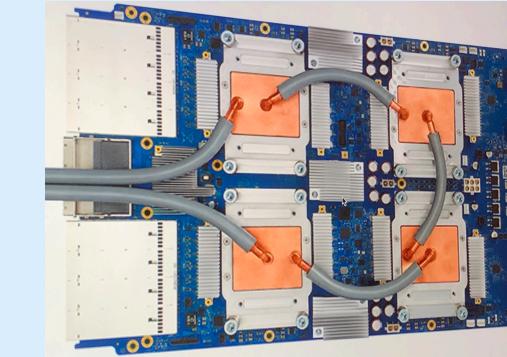


arm

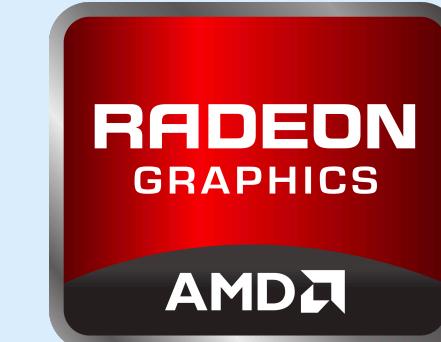


## Fixed-Function ASICs

SIMD



## SIMT GPUs

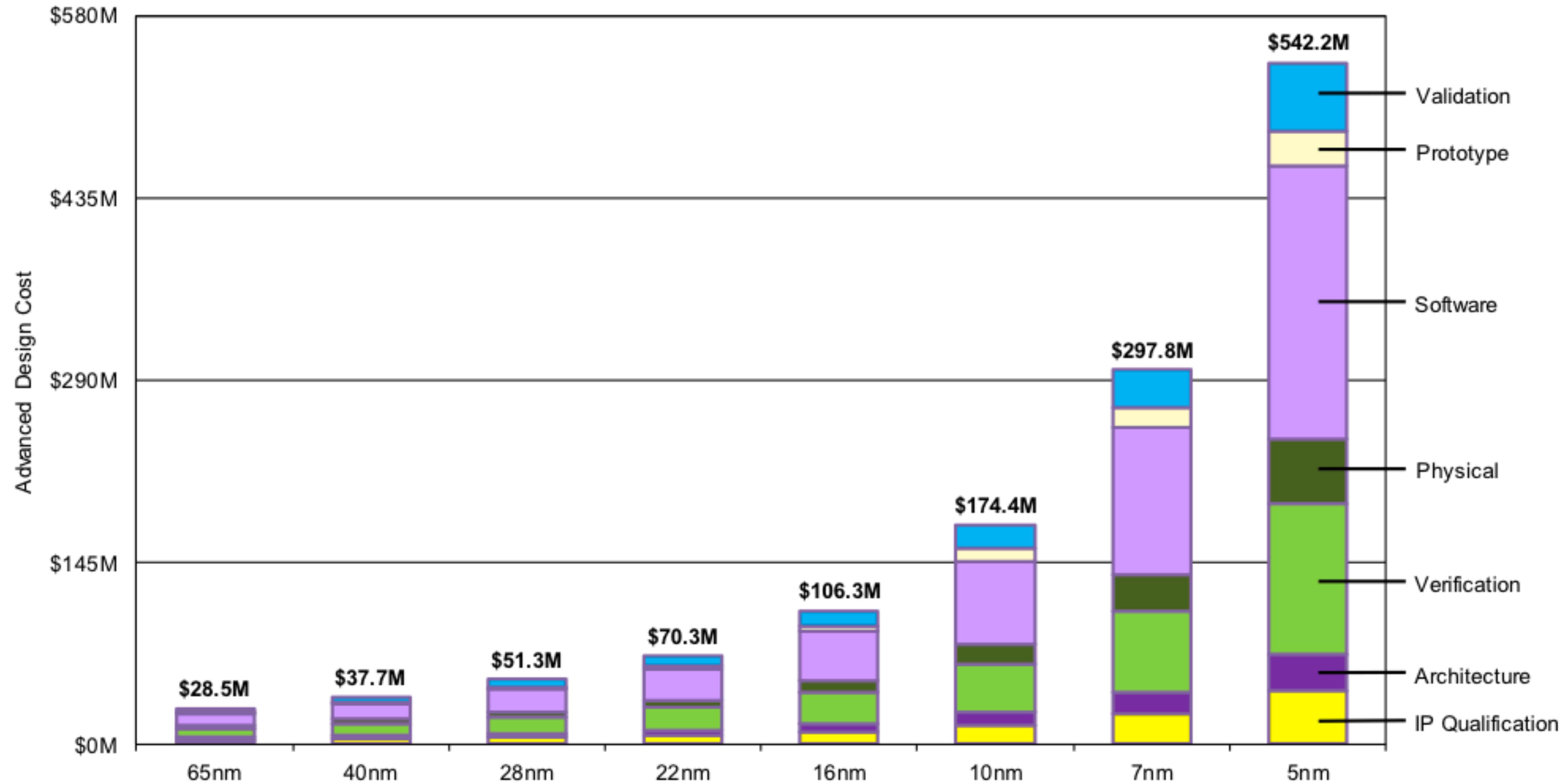


## Programmable Streaming Dataflow

CGRA

RDA

# Economics of Hardware



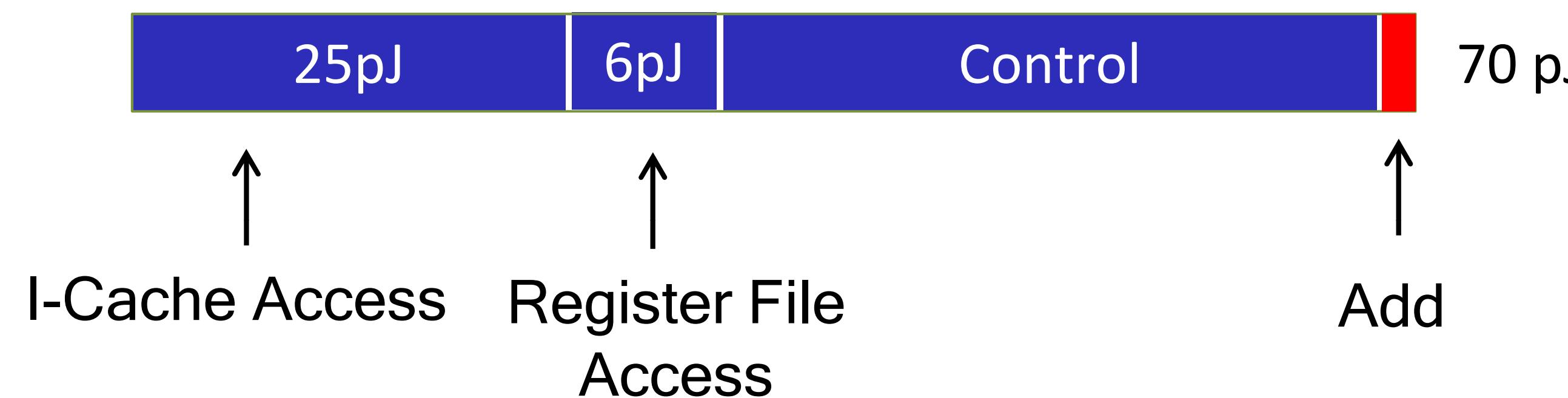
# Economics of Hardware

“That changed in 2013 when a projection showed people searching by voice for three minutes a day using speech recognition DNNs would double our datacenters’ computation demands, which would be very expensive using conventional CPUs.”

# Hardware Design Considerations

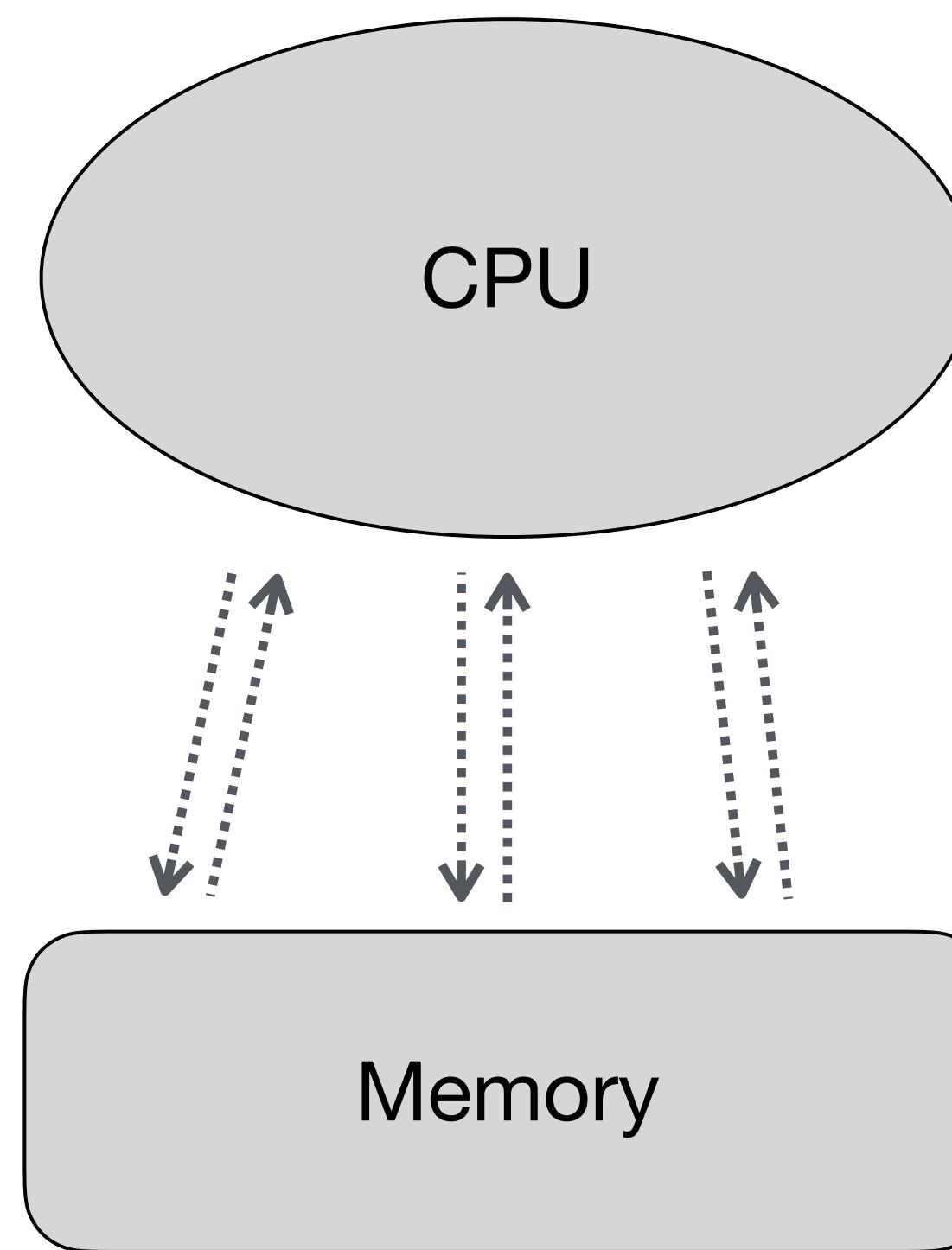
Integer		FP		Memory	
Add		FAdd		Cache (64bit)	
8 bit	0.03pJ	16 bit	0.4pJ	8KB	10pJ
32 bit	0.1pJ	32 bit	0.9pJ	32KB	20pJ
Mult		FMult		1MB	100pJ
8 bit	0.2pJ	16 bit	1.1pJ	DRAM	1.3-2.6nJ
32 bit	3.1pJ	32 bit	3.7pJ		

Instruction Energy Breakdown

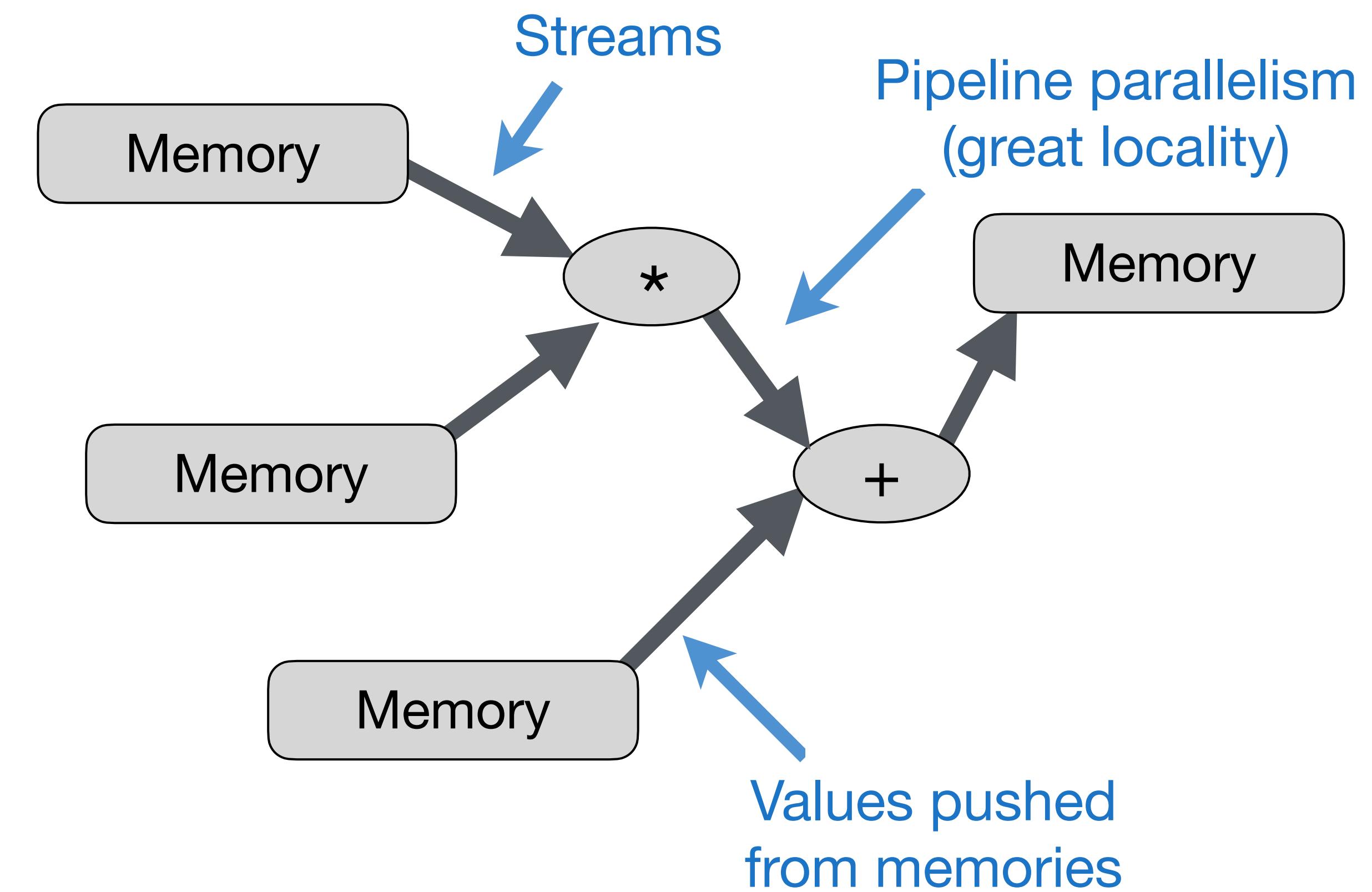


# Spatial Hardware (a.k.a. streaming dataflow hardware)

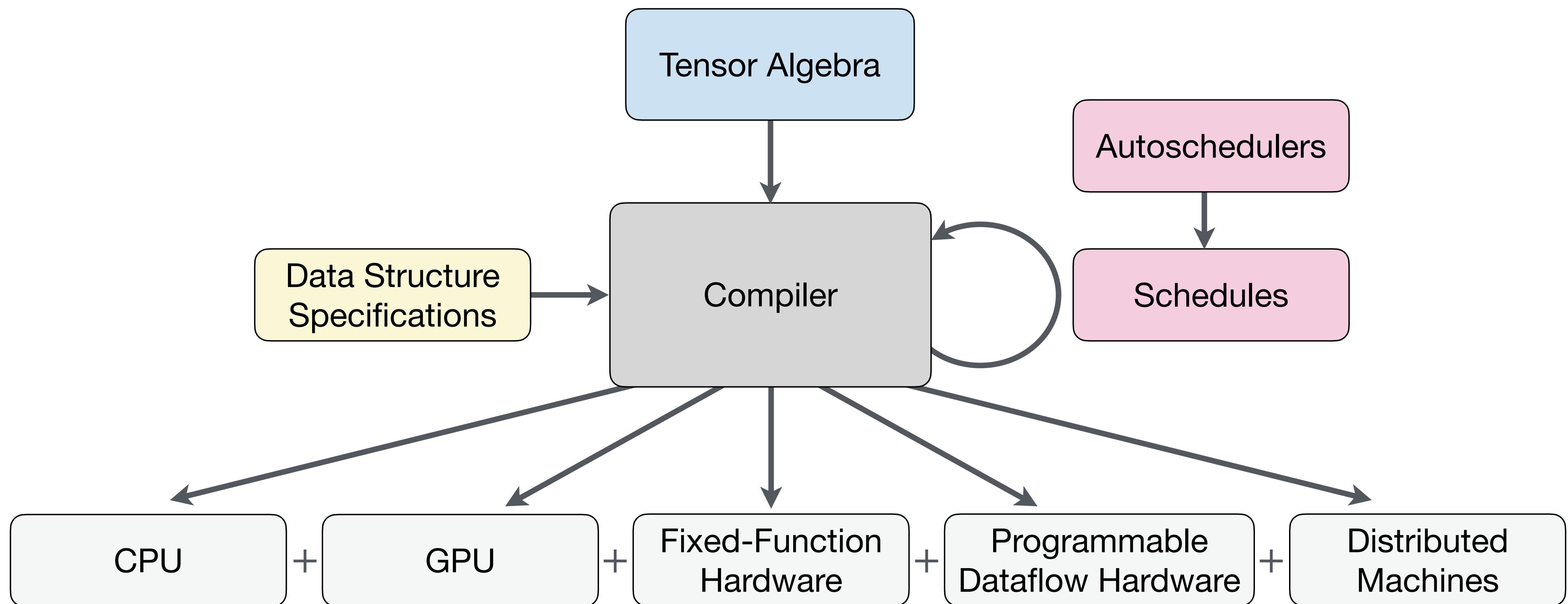
von Neumann architecture



Spatial architecture



# Overview: Sparse Tensor Algebra Compilation



# Hardware design for general sparse tensor operations

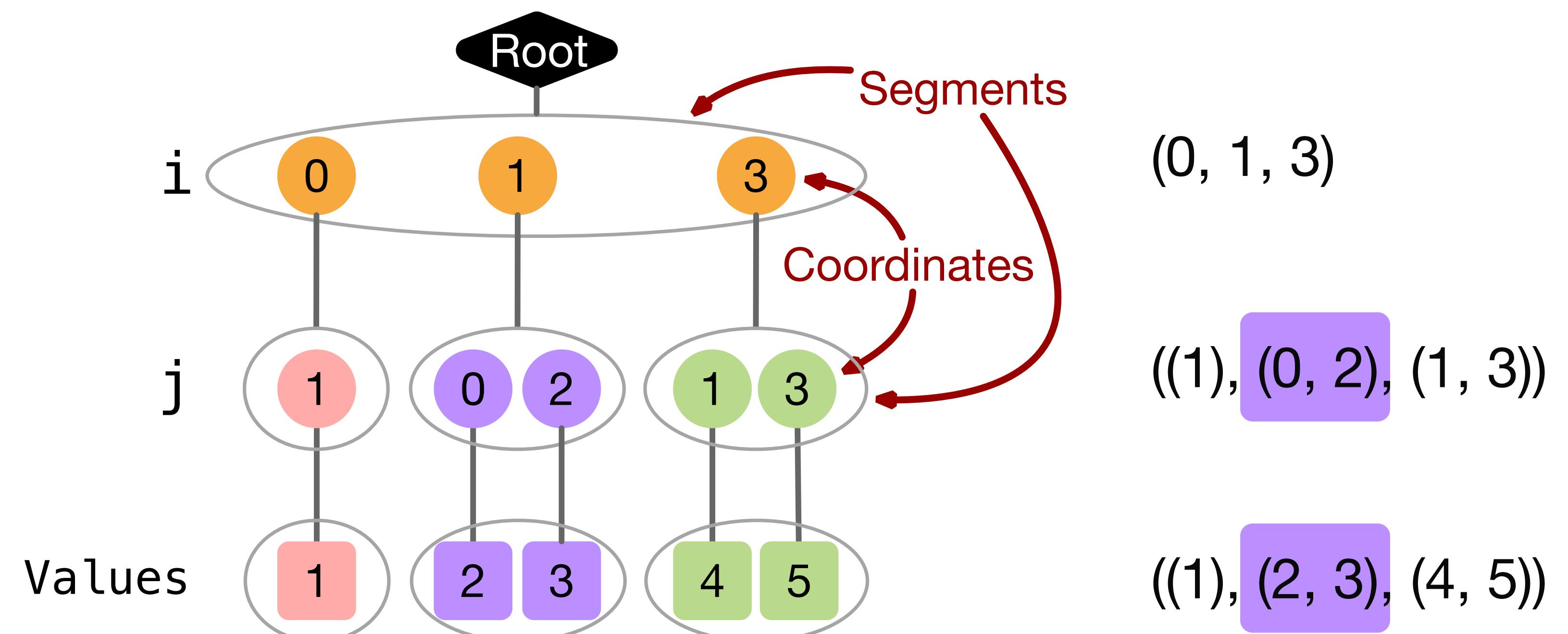
Sparse tensor algebra accelerators must support:

1. **Generality:** arbitrary tensor algebra operations
2. **Data Structures:** dense and sparse data structures
3. **Fusion:** Fusion across operations
4. **Reordering:** Changing the order they process tensor dimensions

# Abstract tensor data model

Dimension j			
0	1	2	3
0	1	0	0
2	0	3	0
0	0	0	0
0	4	0	5

point (3,1)



# Tensors on Wires

(0, 1, 3)

((1), (0, 2), (1, 3))

((1), (2, 3), (4, 5))

Streams (Time)

Arrays (Space)

Segments

0	3
---	---

Coordinates

0	1	3
---	---	---

Segments

0	1	3	5
---	---	---	---

Coordinates

1	0	2	1	3
---	---	---	---	---

Values

1	2	3	4	5
---	---	---	---	---

Non-control tokens

Done token  
denotes end  
of a stream

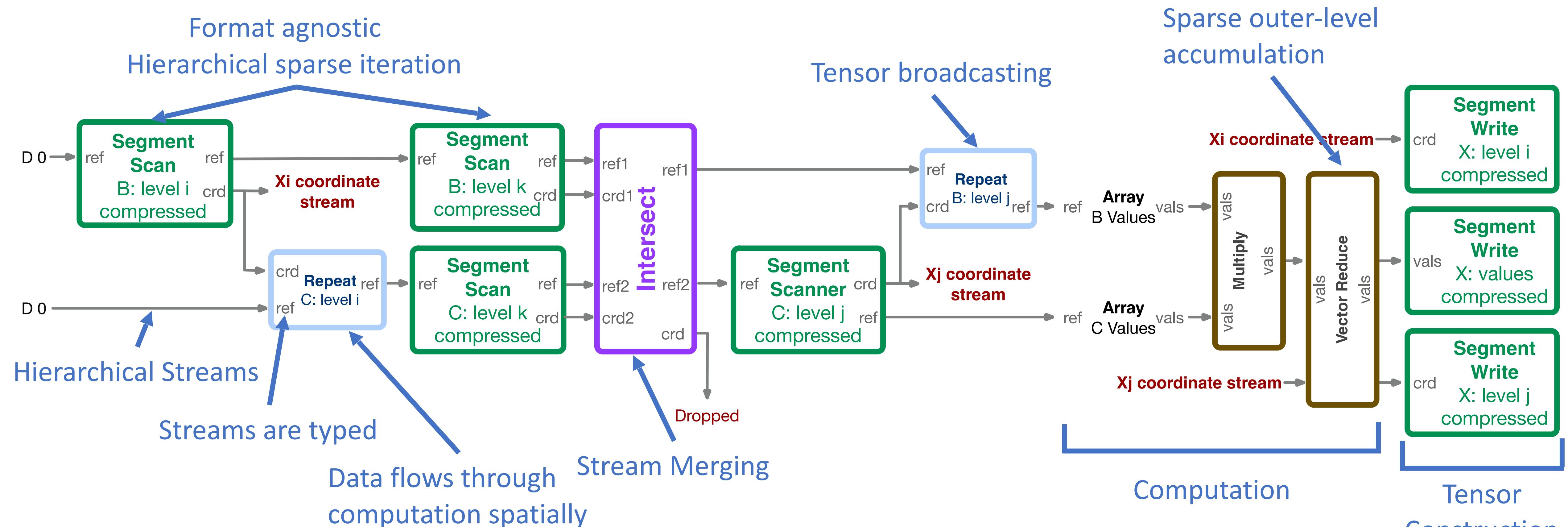
Hierarchical stop token  
denotes end of a segment

D, S<sub>0</sub>, 3, 1, 0

D, S<sub>1</sub>, 3, 1, S<sub>0</sub>, 2, 0, S<sub>0</sub>, 1

D, S<sub>1</sub>, 5, 4, S<sub>0</sub>, 3, 2, S<sub>0</sub>, 1

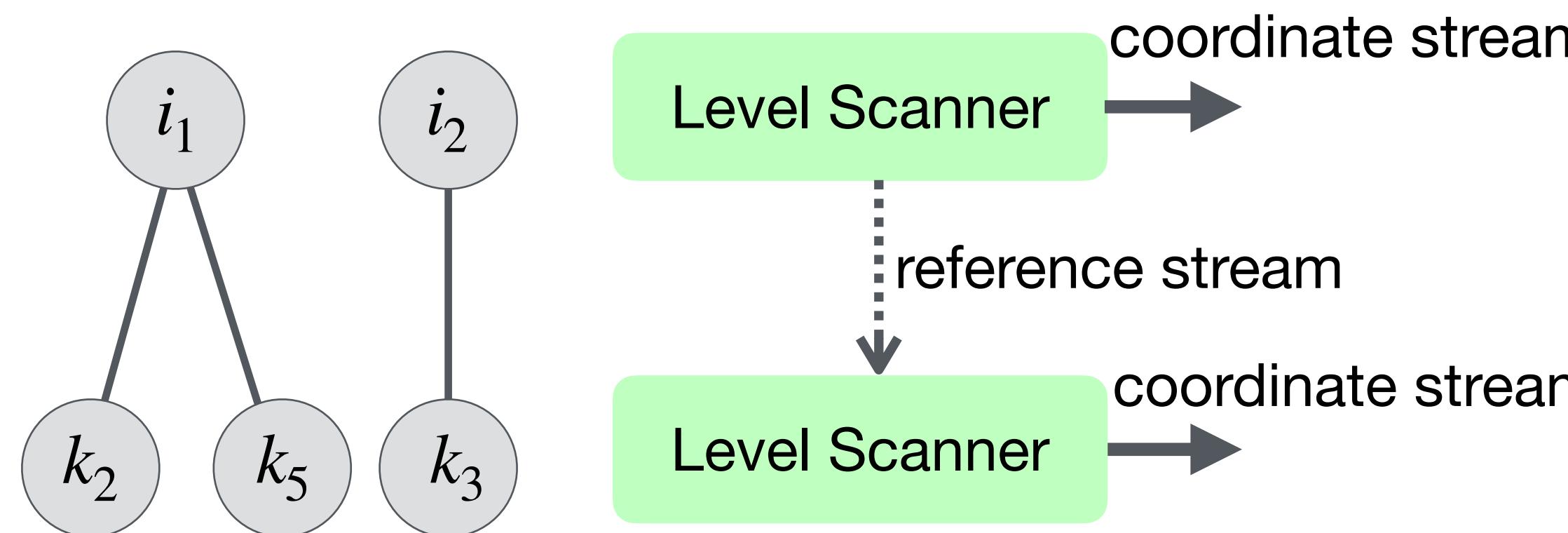
# Sparse-matrix sparse-matrix multiplication



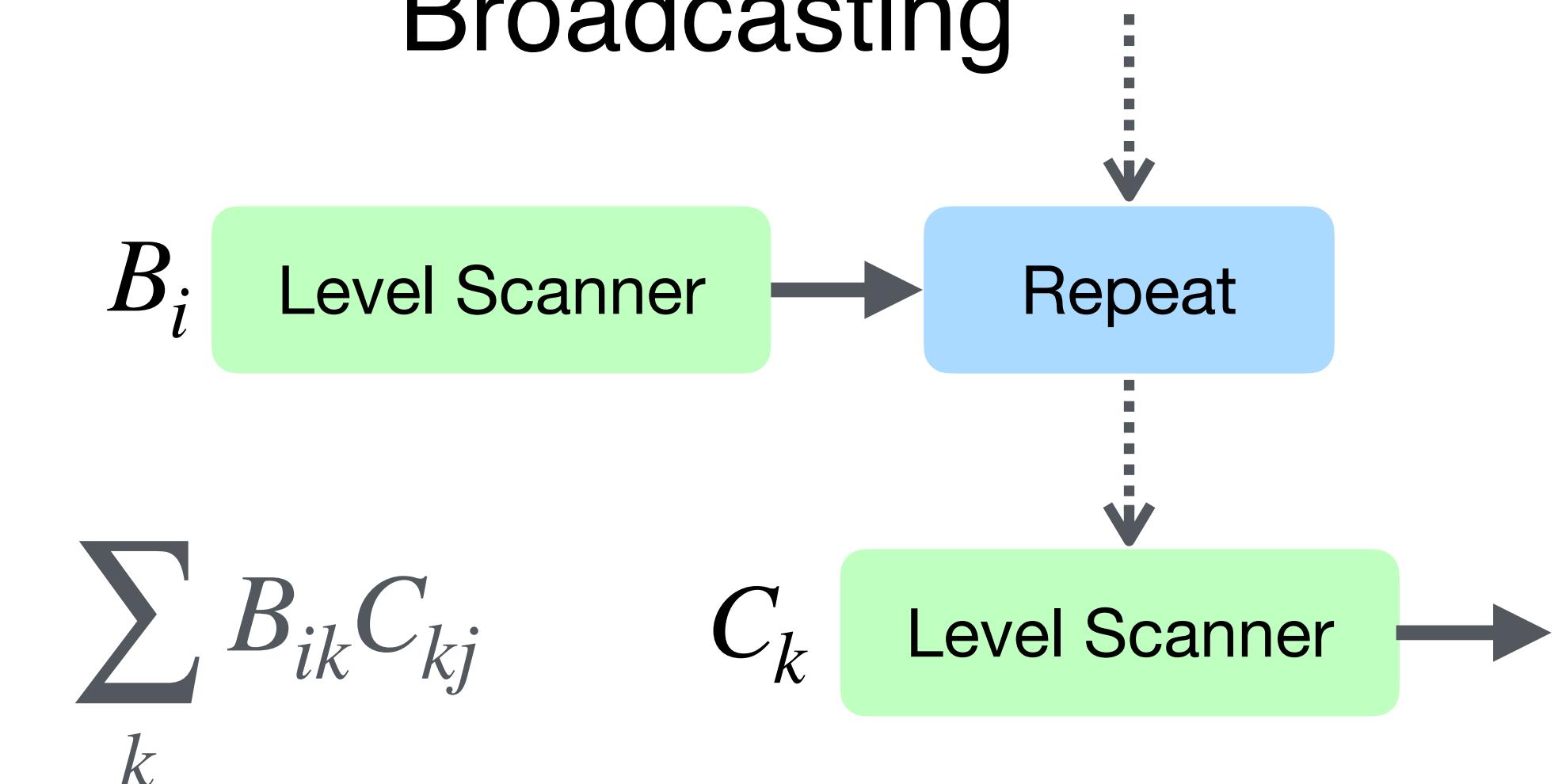
$$\forall_i \forall_k \forall_j X_{ij} += B_{ik} * C_{kj}$$

# Streaming dataflow abstract machine (for sparse tensor algebra)

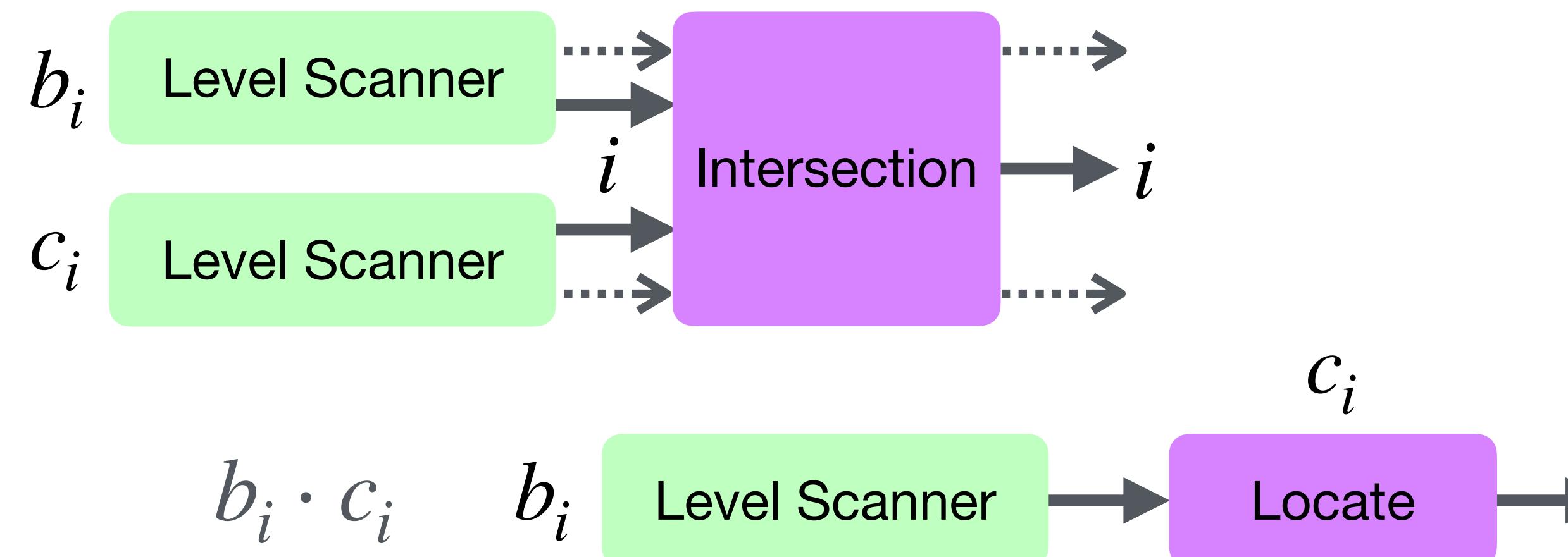
## Hierarchical Iteration



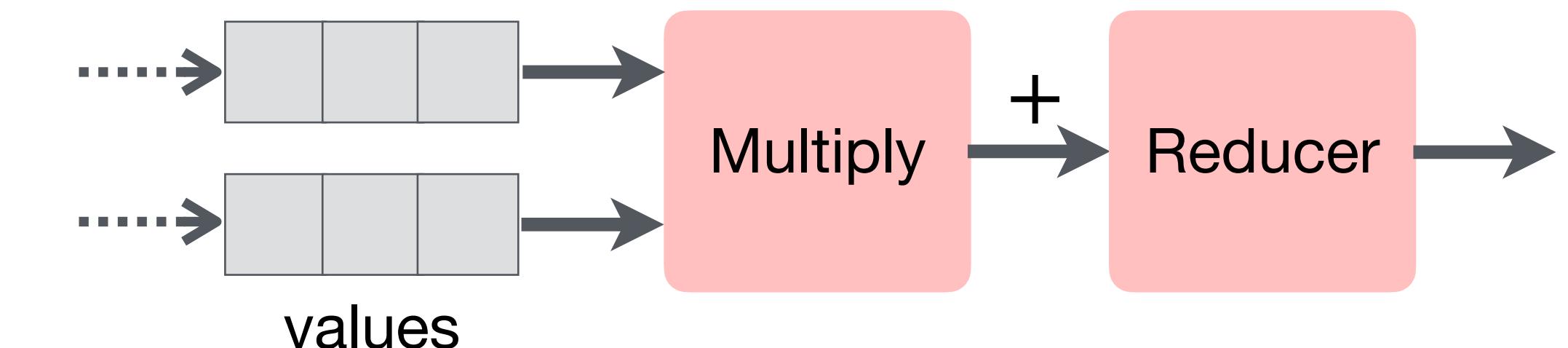
## Broadcasting



## Coiteration / Locate

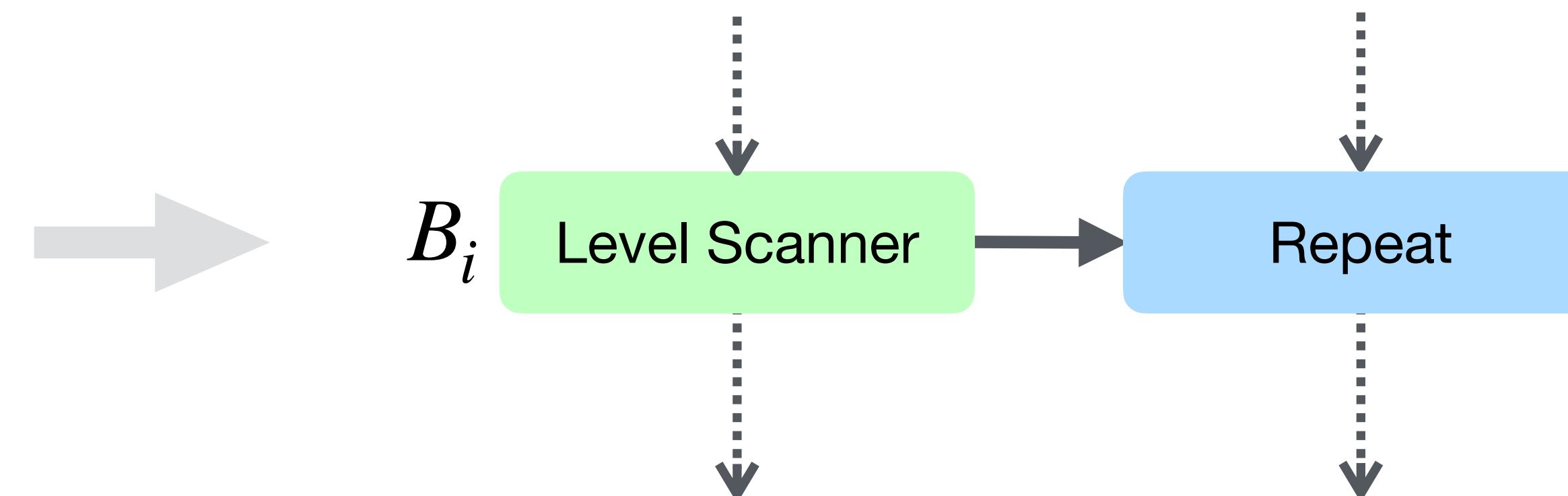


## Computation / Reduction



# Compiling to the streaming dataflow abstract machine

$$\forall_i \in B_i \cap \mathbb{U}_i$$

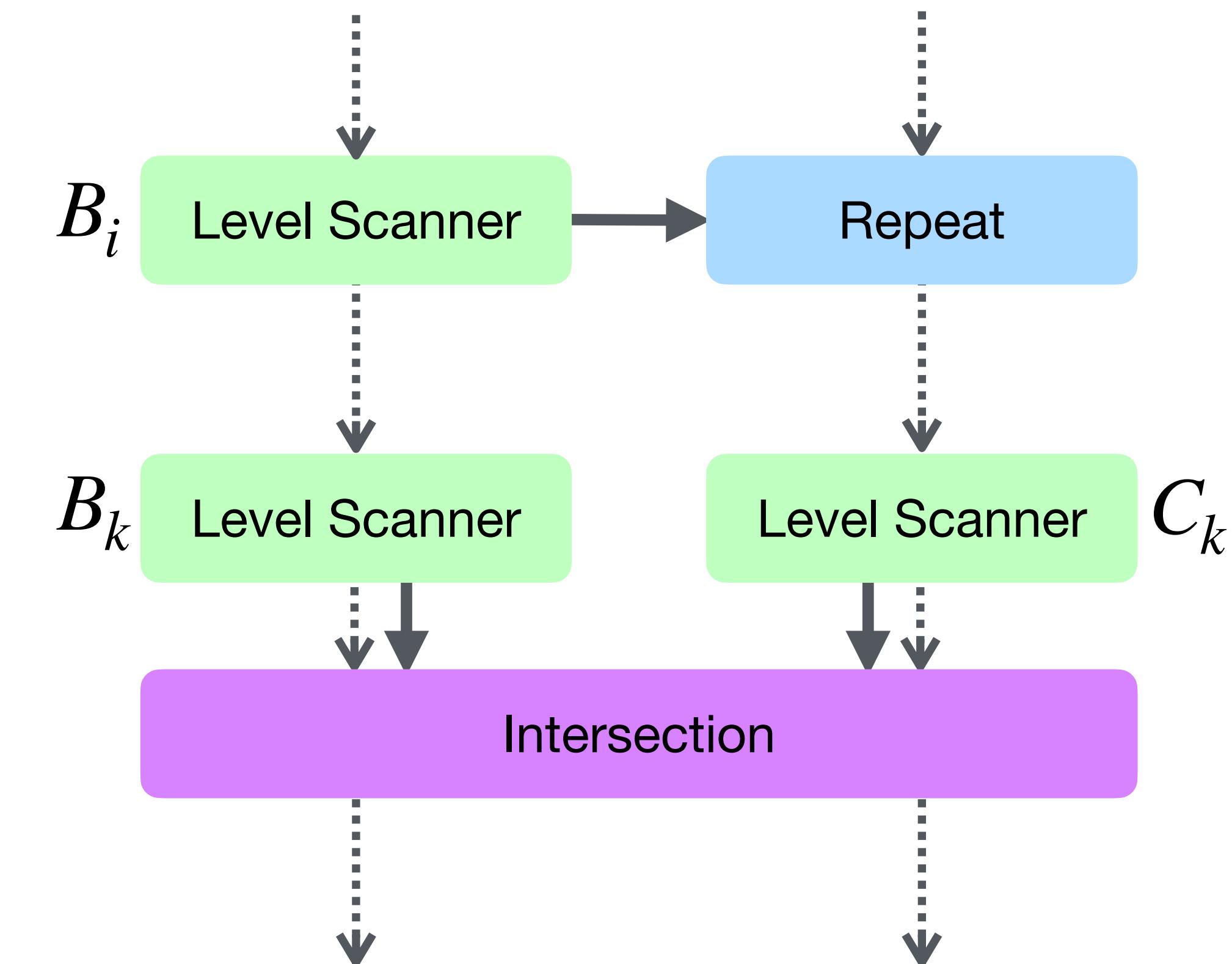


$$\forall_j \in \mathbb{U}_j \cap C_j$$

$$A_{ij} += B_{ik} C_{kj}$$

# Compiling to the streaming dataflow abstract machine

$$\forall_i \in B_i \cap \mathbb{U}_i$$



$$\forall_k \in B_k \cap C_k$$

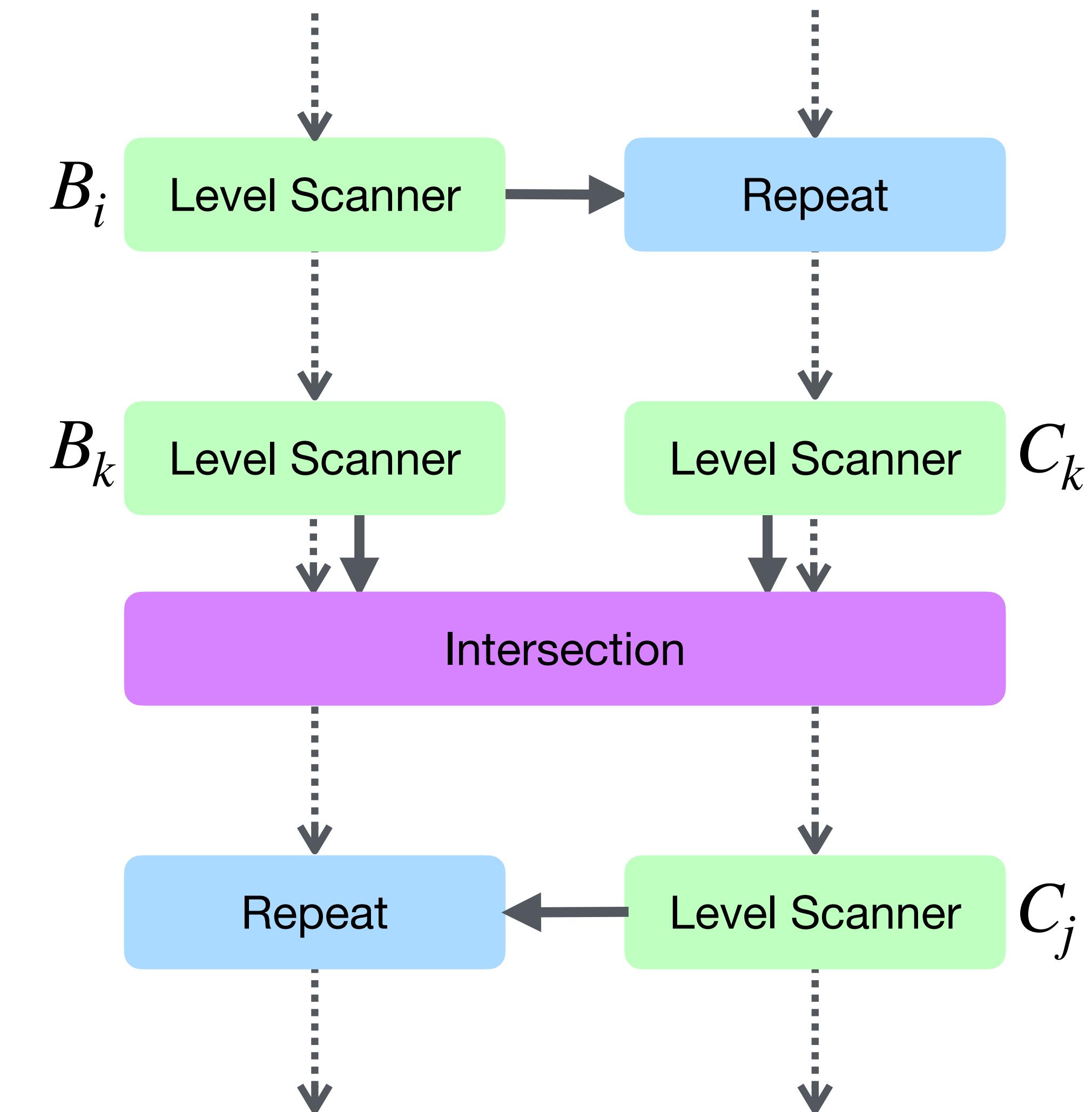


$$\forall_j \in \mathbb{U}_j \cap C_j$$

$$A_{ij} += B_{ik} C_{kj}$$

# Compiling to the streaming dataflow abstract machine

$$\forall_i \in B_i \cap \mathbb{U}_i$$

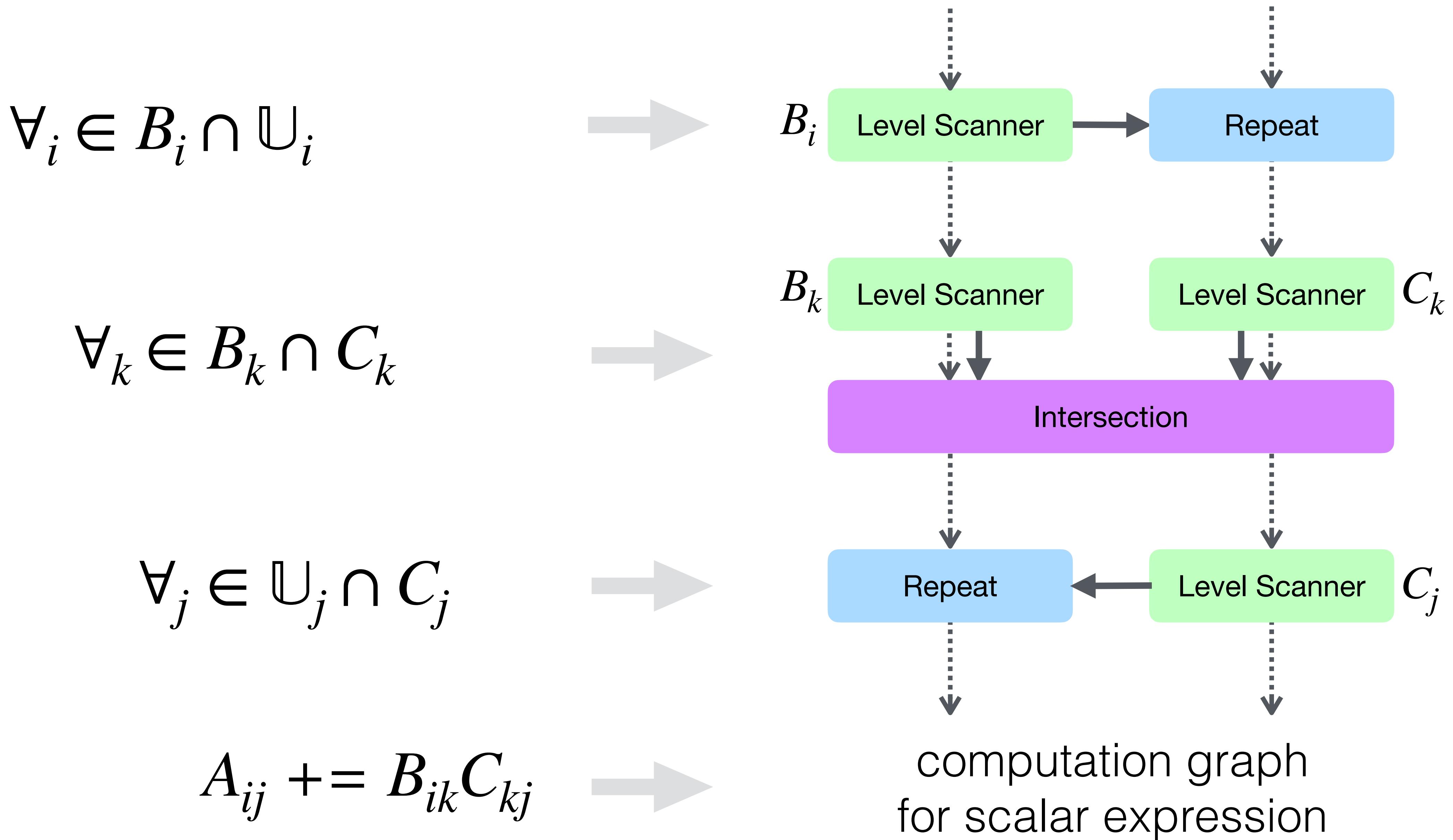


$$\forall_j \in \mathbb{U}_j \cap C_j$$



$$A_{ij} += B_{ik}C_{kj}$$

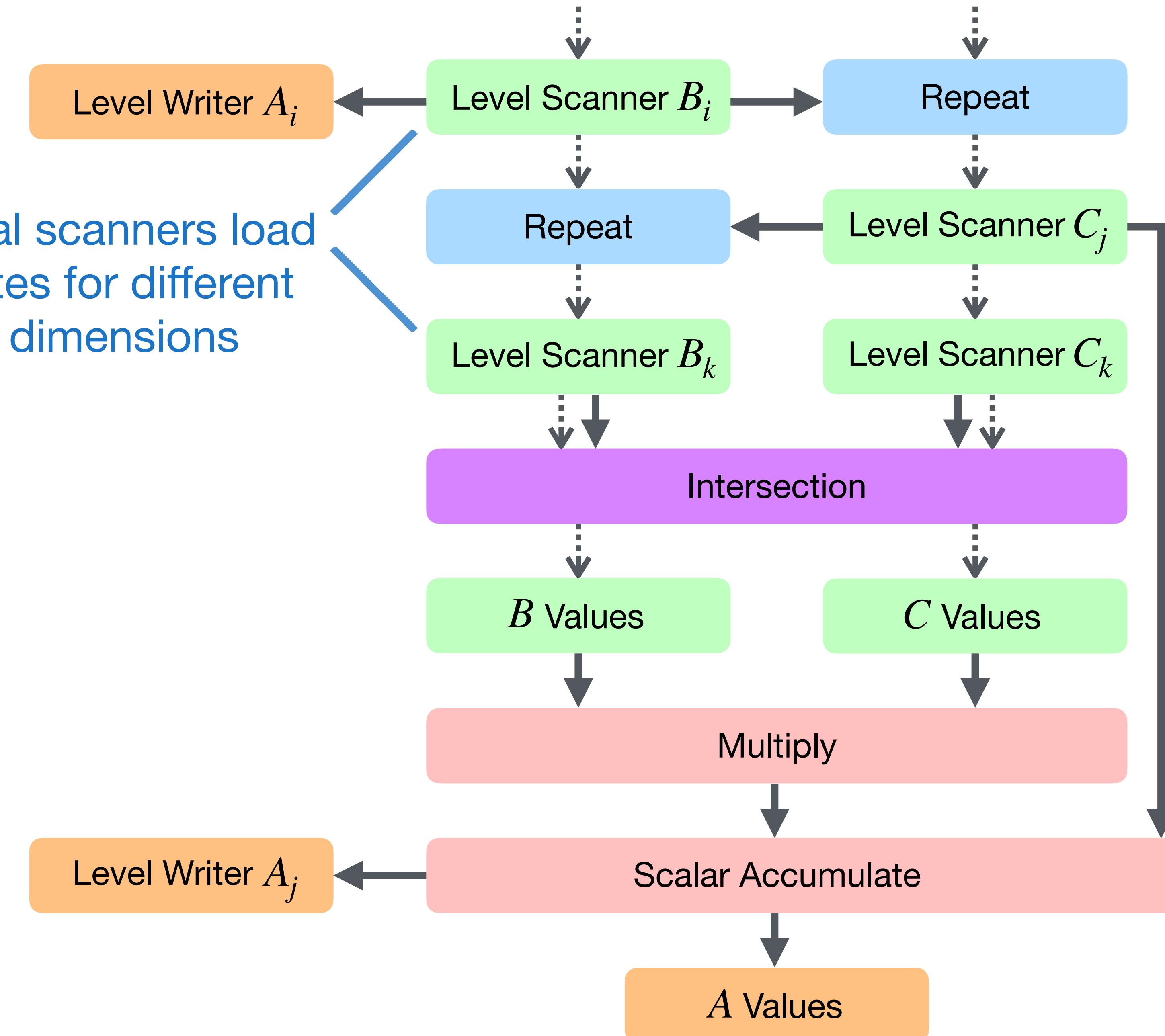
# Compiling to the streaming dataflow abstract machine



# Inner-product sparse matrix multiplication

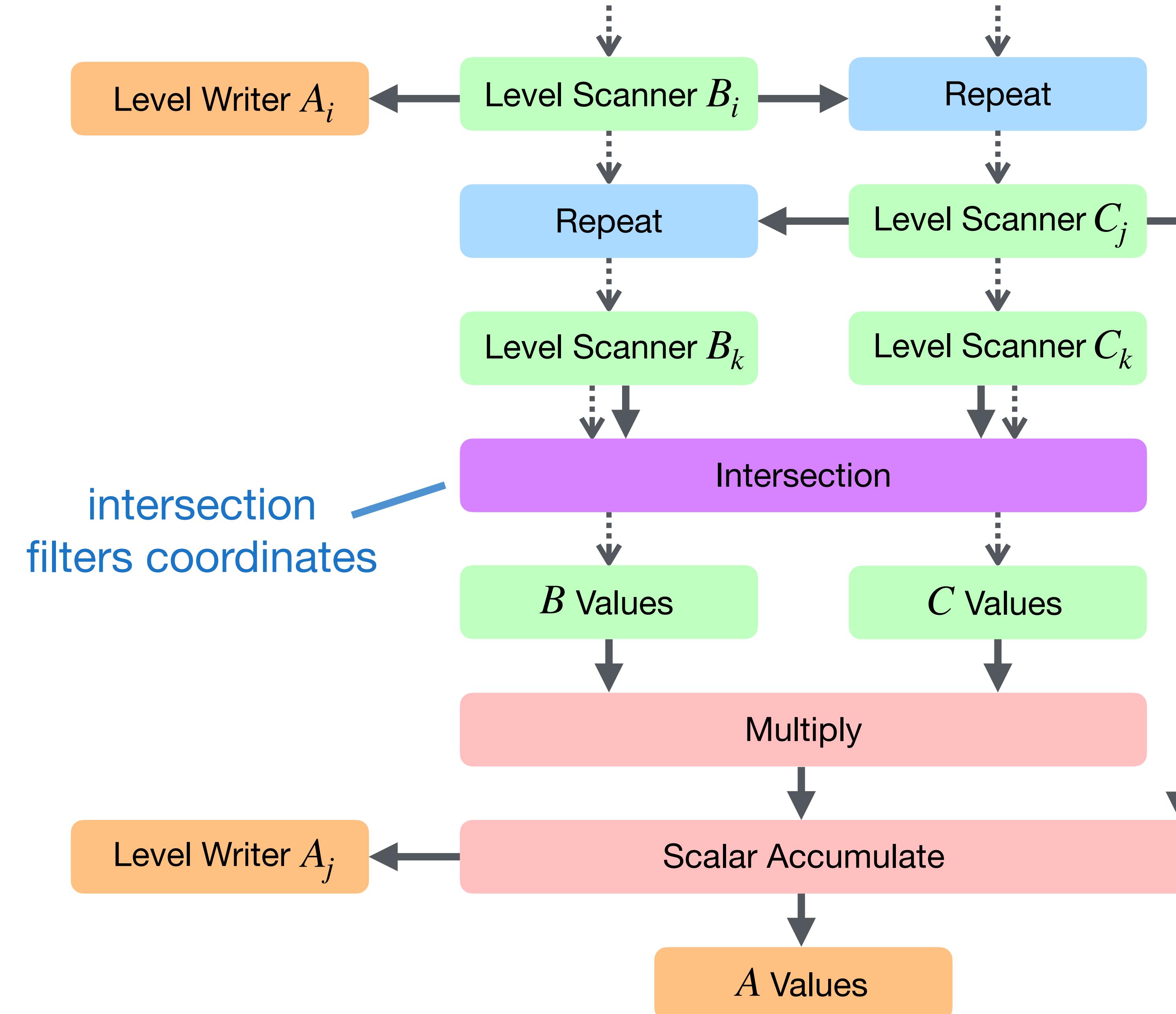
$$A_{ij} = \sum_k B_{ik} C_{kj}$$

hierarchical scanners load  
coordinates for different  
tensor dimensions



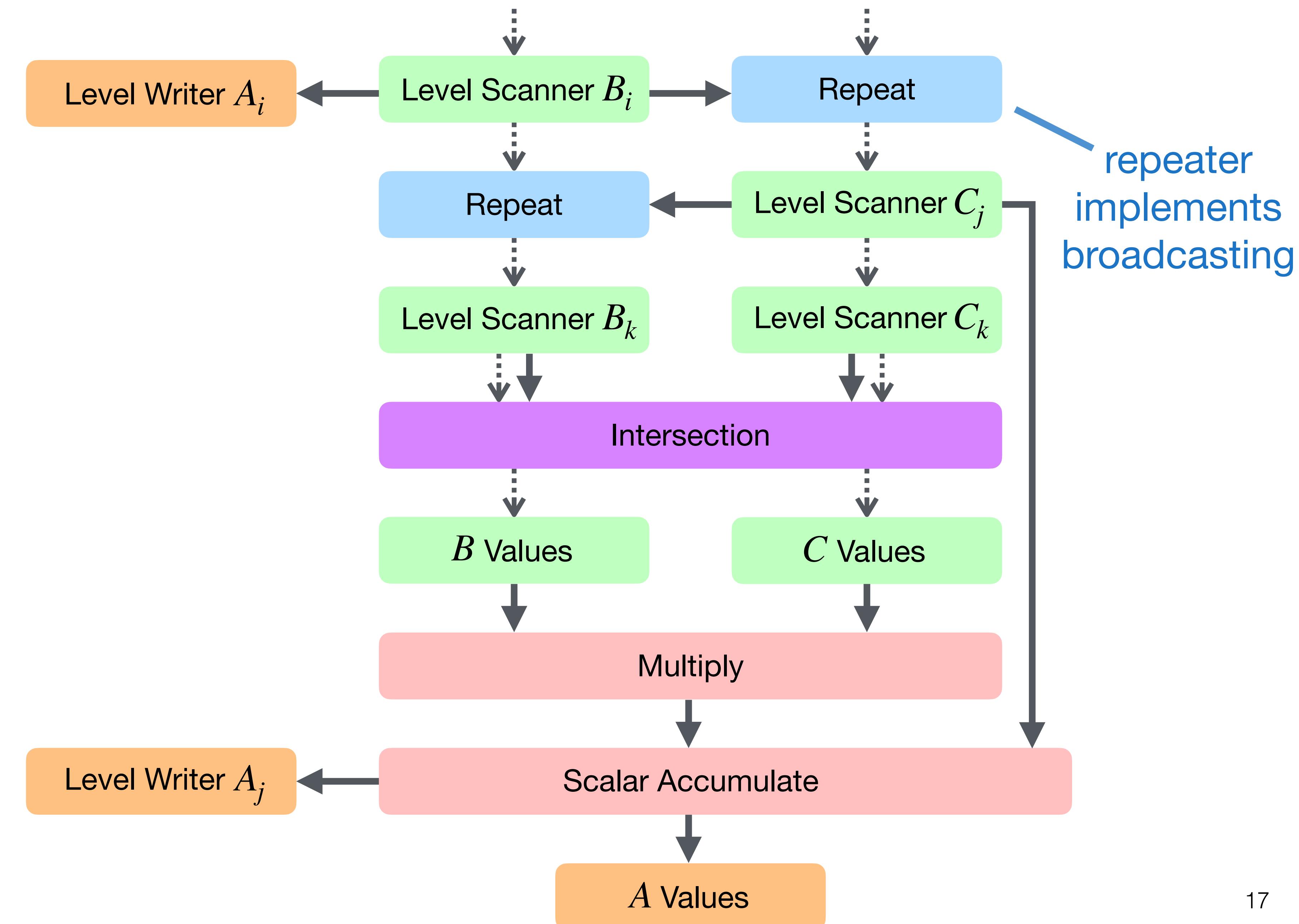
# Inner-product sparse matrix multiplication

$$A_{ij} = \sum_k B_{ik} C_{kj}$$



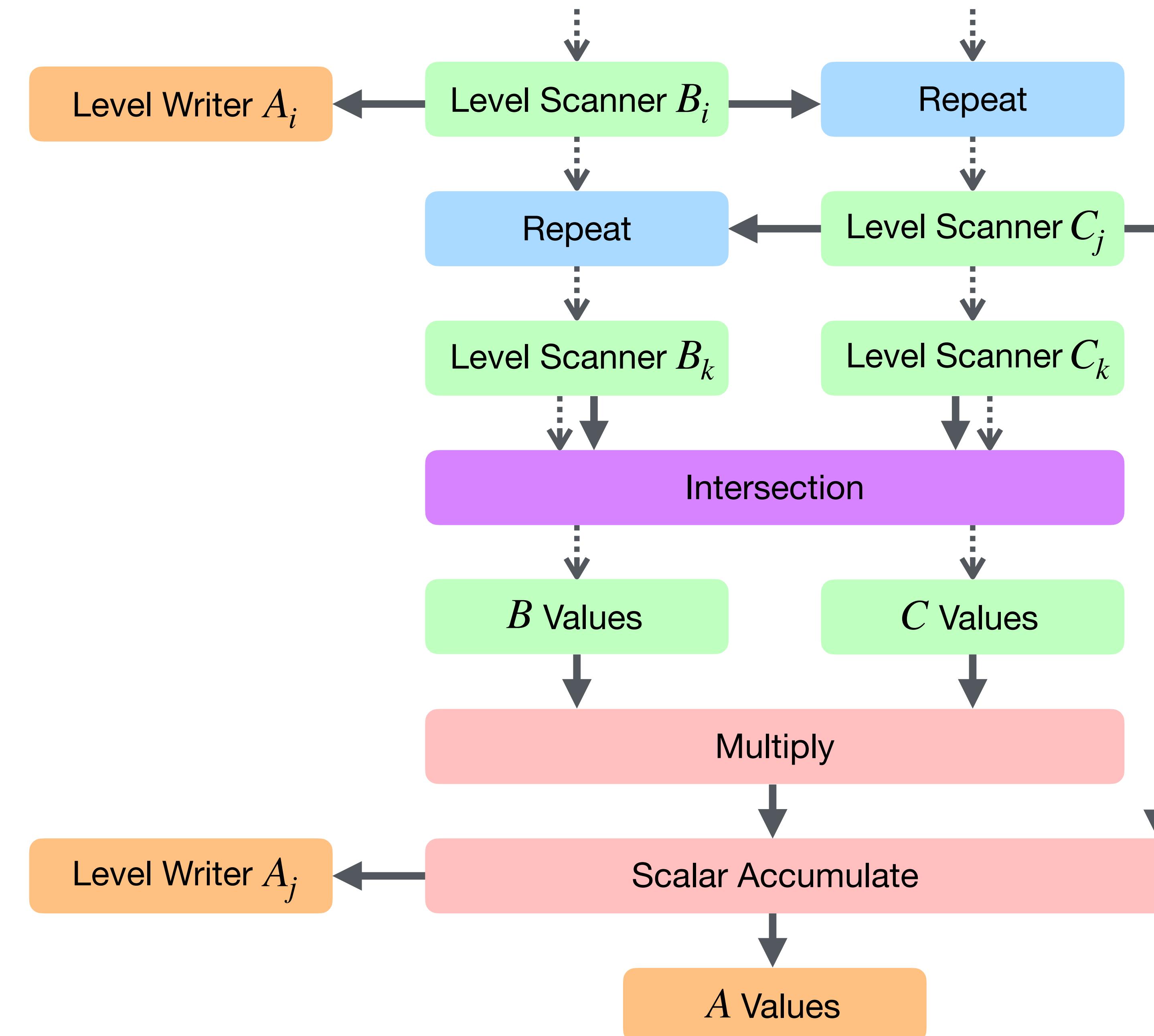
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$$A_{ij} = \sum_k B_{ik} C_{kj}$$



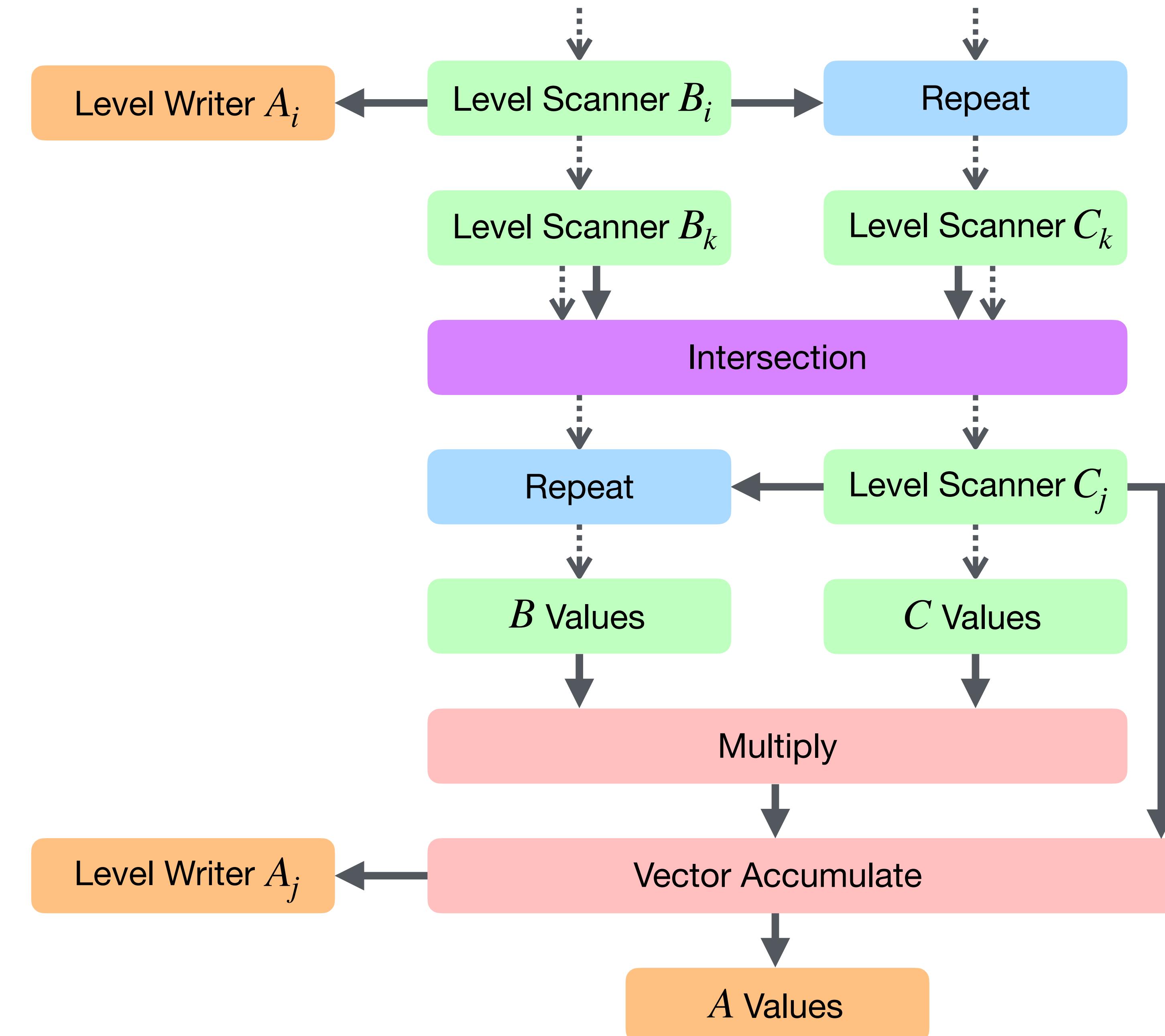
# Inner-product sparse matrix multiplication

$$A_{ij} = \sum_k B_{ik} C_{kj}$$

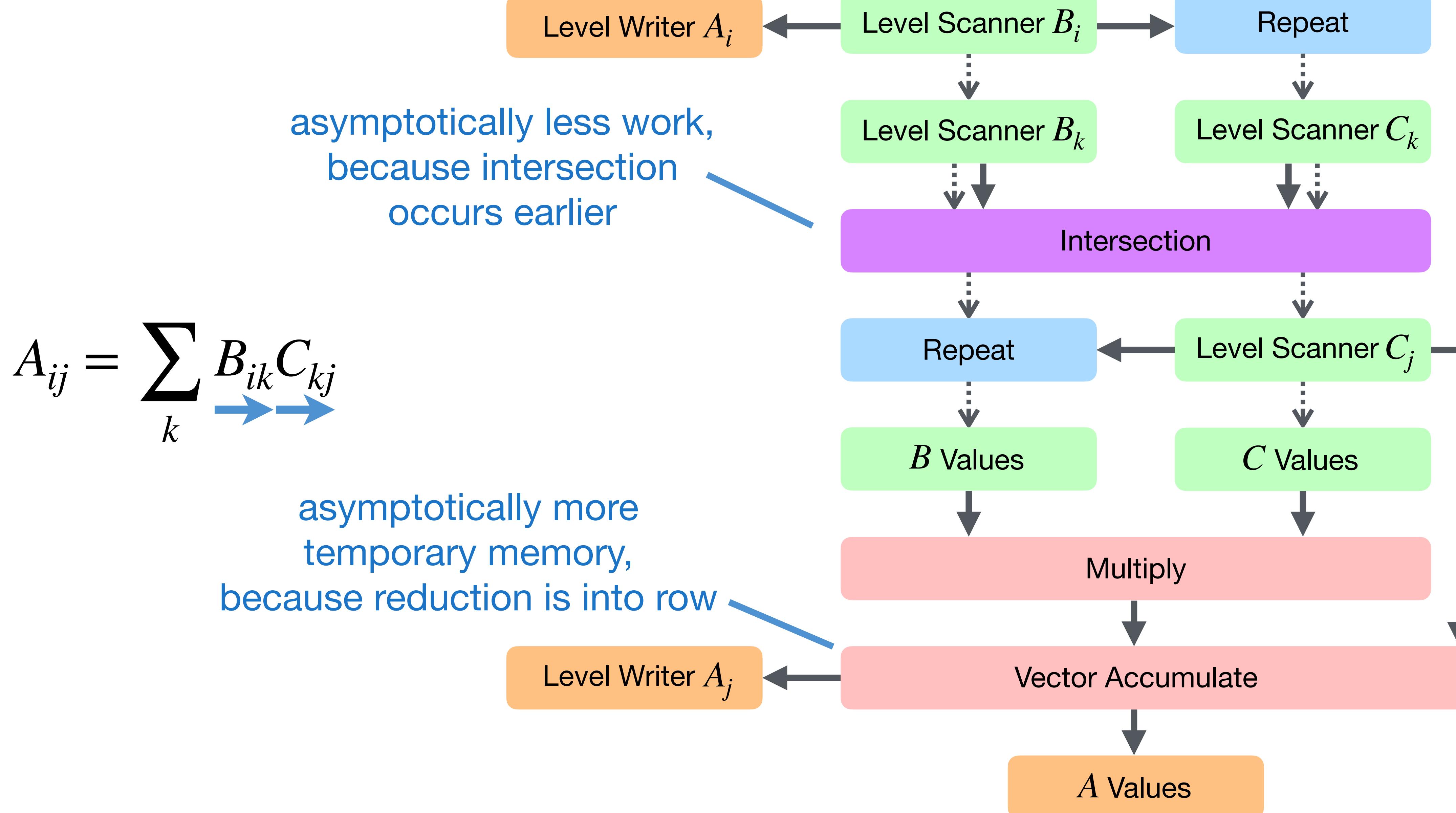


# Gustafson sparse matrix multiplication

$$A_{ij} = \sum_k B_{ik} C_{kj}$$



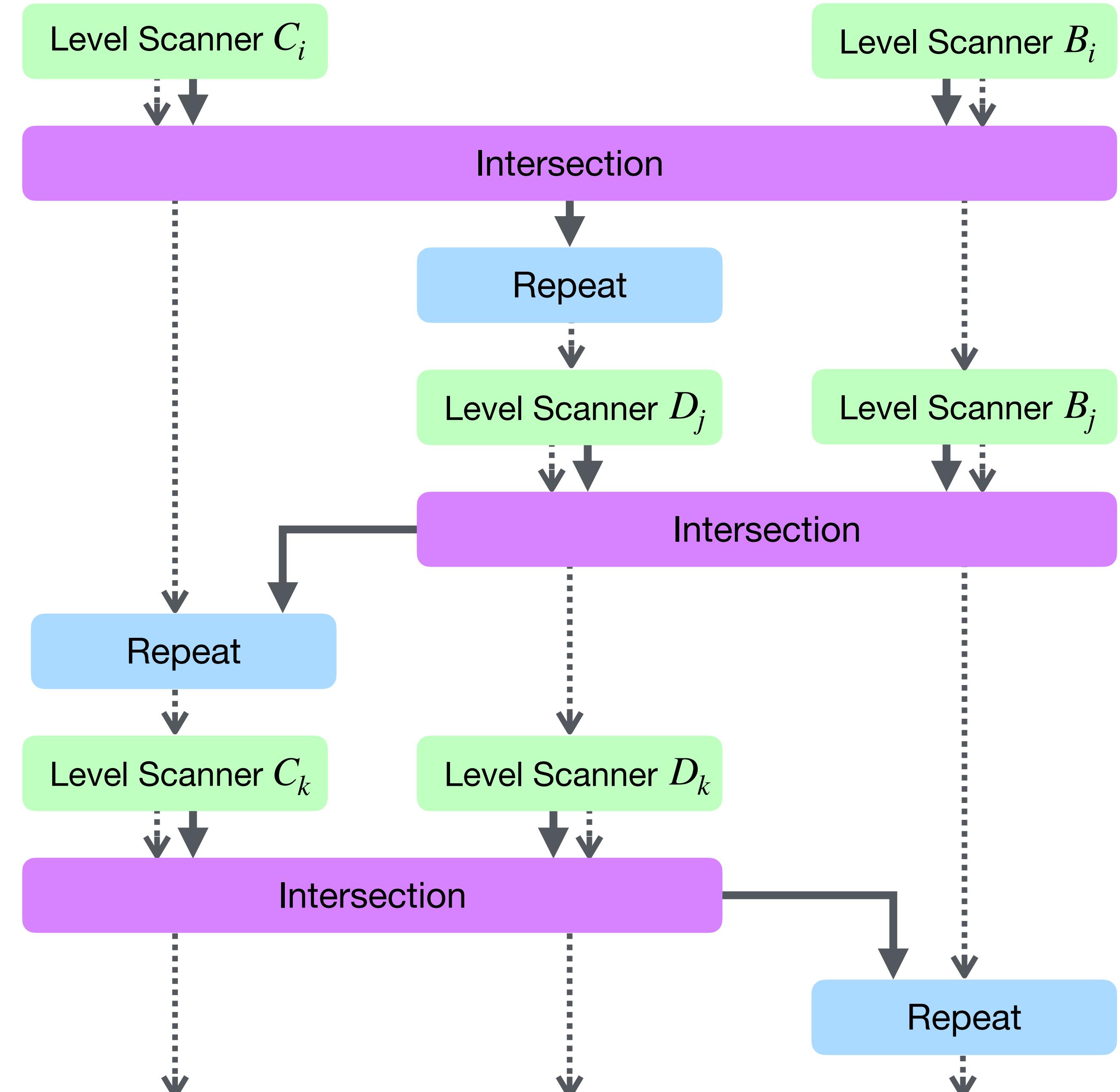
# Gustafson sparse matrix multiplication



# Fused SDDMM

$$A = B \odot (CD)$$

$$O(\text{NNZ}_B \cdot K)$$



# Sparse Dataflow Compiler Overview

