

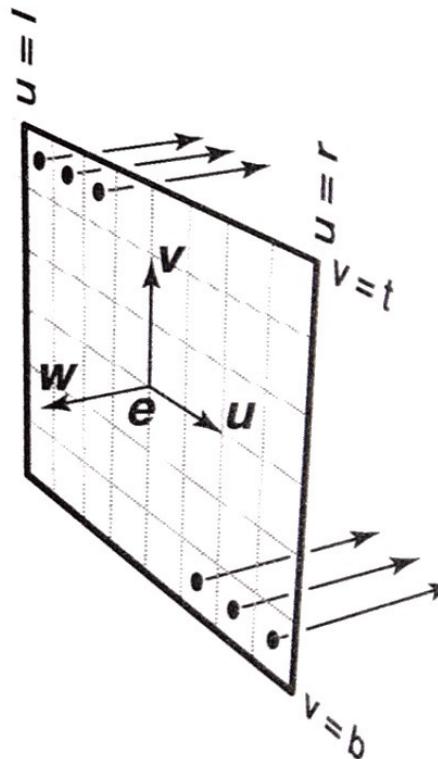
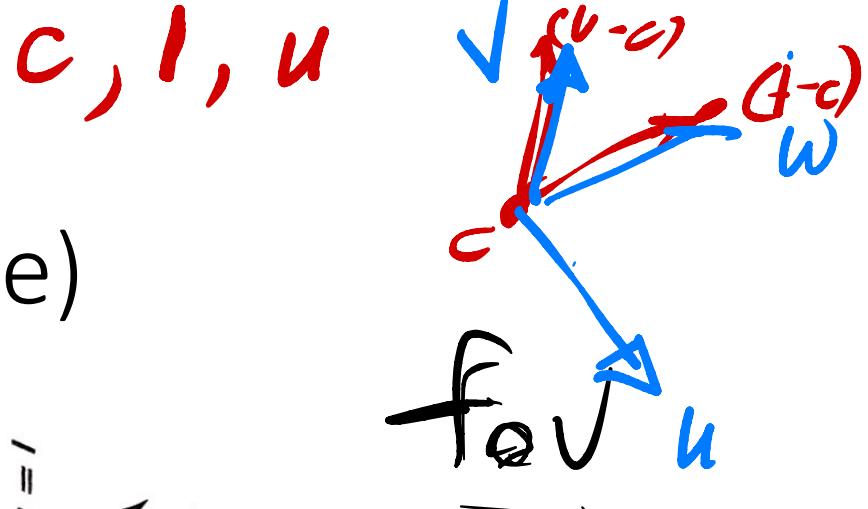
16 – more texture

Bump Mapping and Environment Mapping

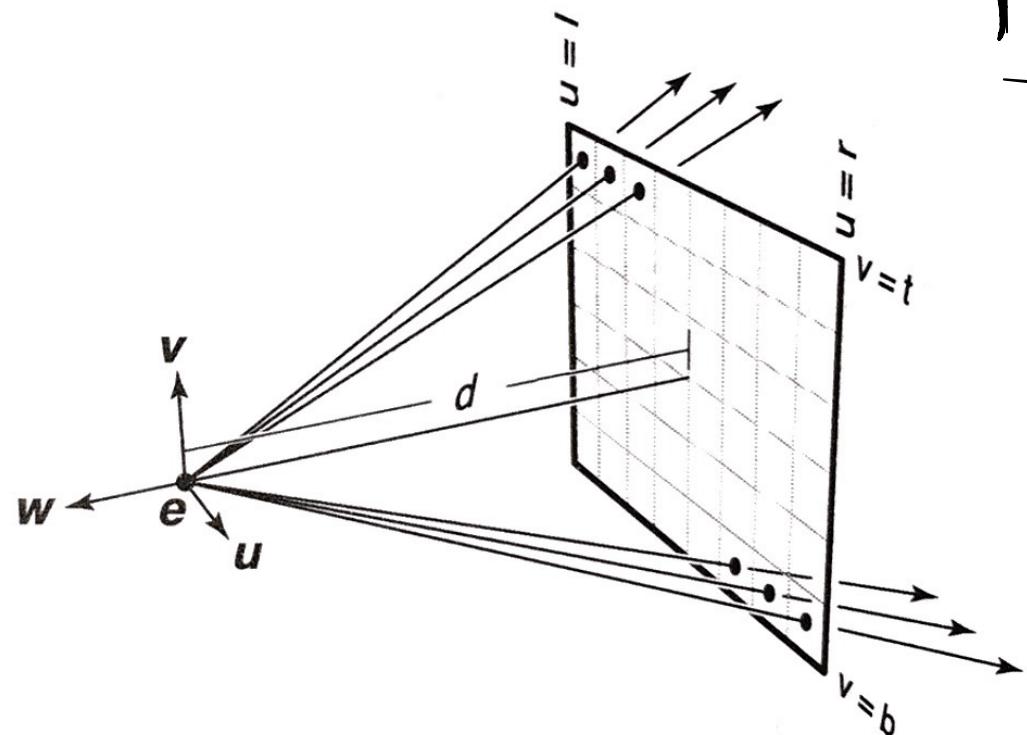
Basic Algorithm

```
for each pixel  $(x_s, y_s)$ 
    create a ray  $R$  from eye through  $(x_s, y_s)$ 
    for each object  $Q_i$  in scene
        if  $R$  intersects  $Q_i$  & it's the closest
            so far
            record this intersection
    shade pixel based on nearest intersection
        (recursively for ref & transmission)
```

Eye Rays: Depends on Projection (Orthographic, Perspective, Oblique)



Parallel projection
same direction, different origins

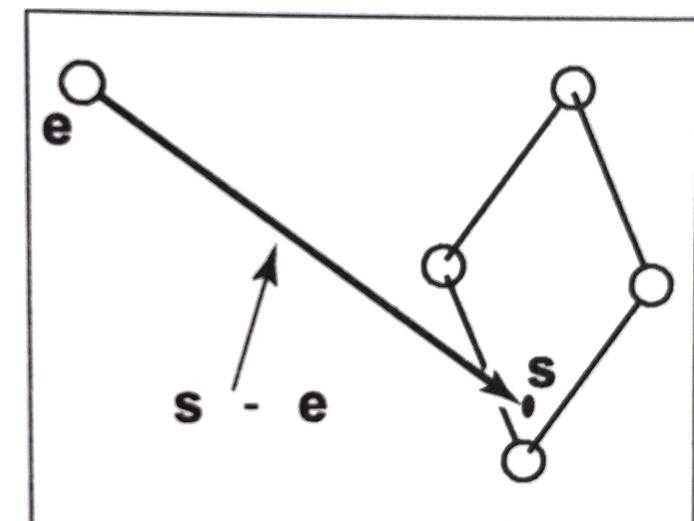
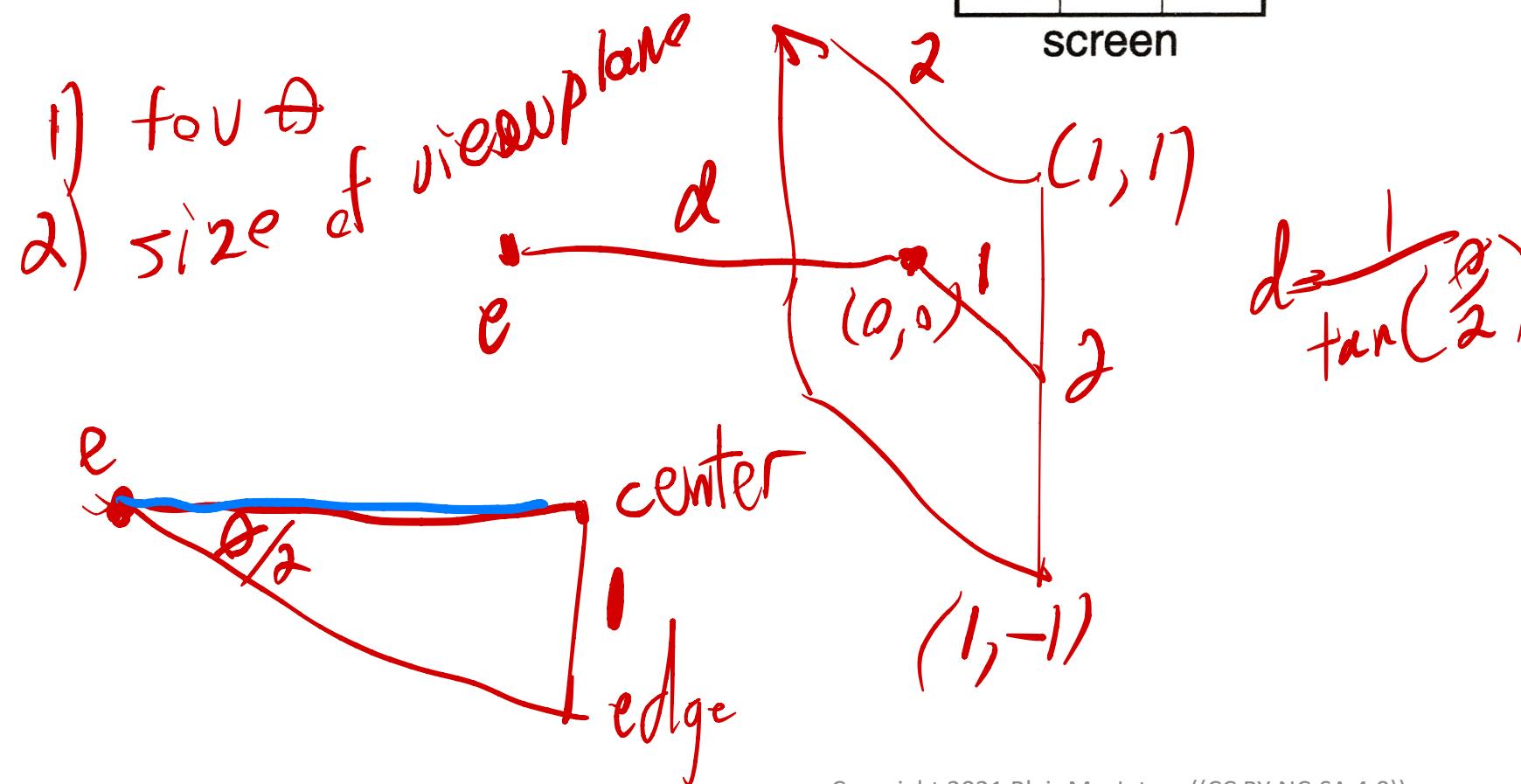
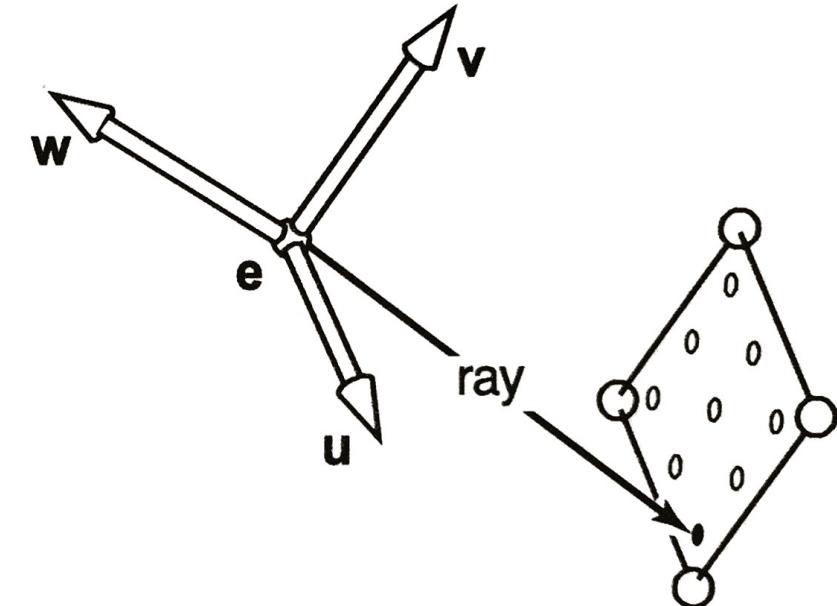
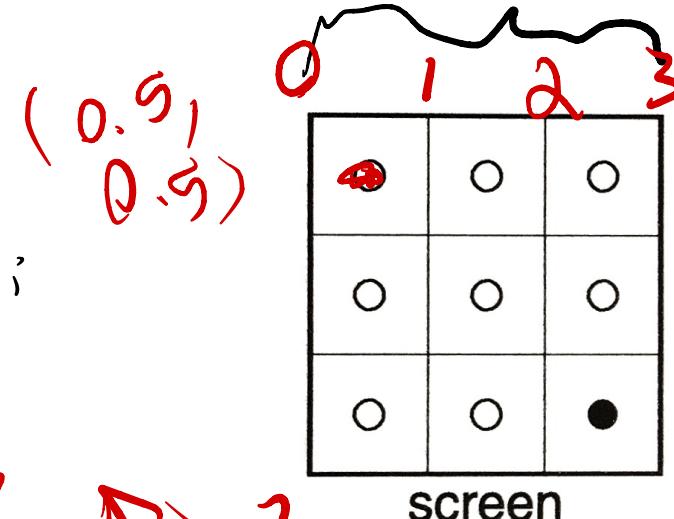


Perspective projection
same origin, different directions

$$\text{fov} = \text{fov}'$$

parametric eq'n:

$$p(t) = e + t(s - e)$$

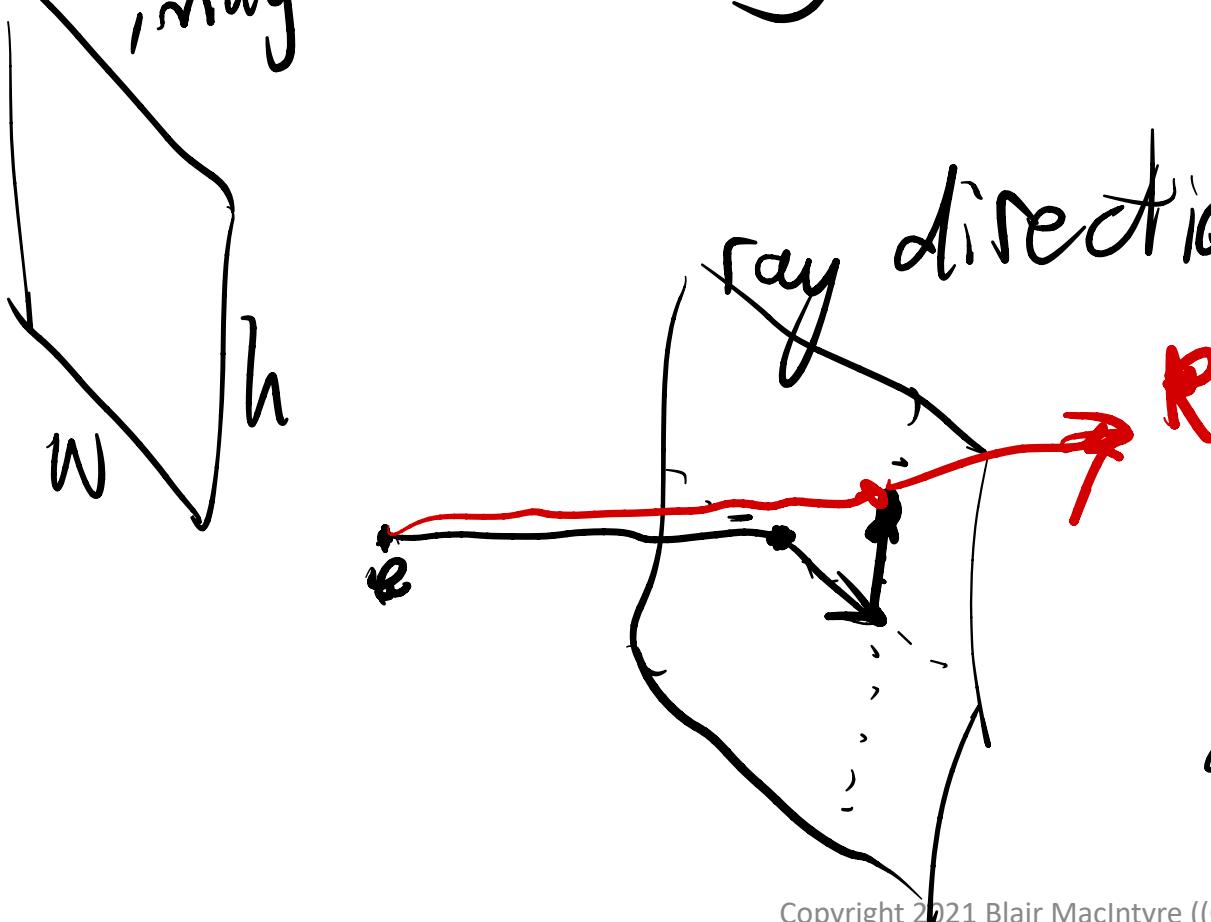


$$u_s = -l + \frac{a_i^w}{h}$$

$$v_s = -l + \frac{a_i^h}{h}$$

for u & v
 $-l \dots i$ range
 u
 v
 w

image



ray direction = $\frac{s - e}{|s - e|}$

= $-dw + u_s u + v_s v$

origin = e

Bump Mapping

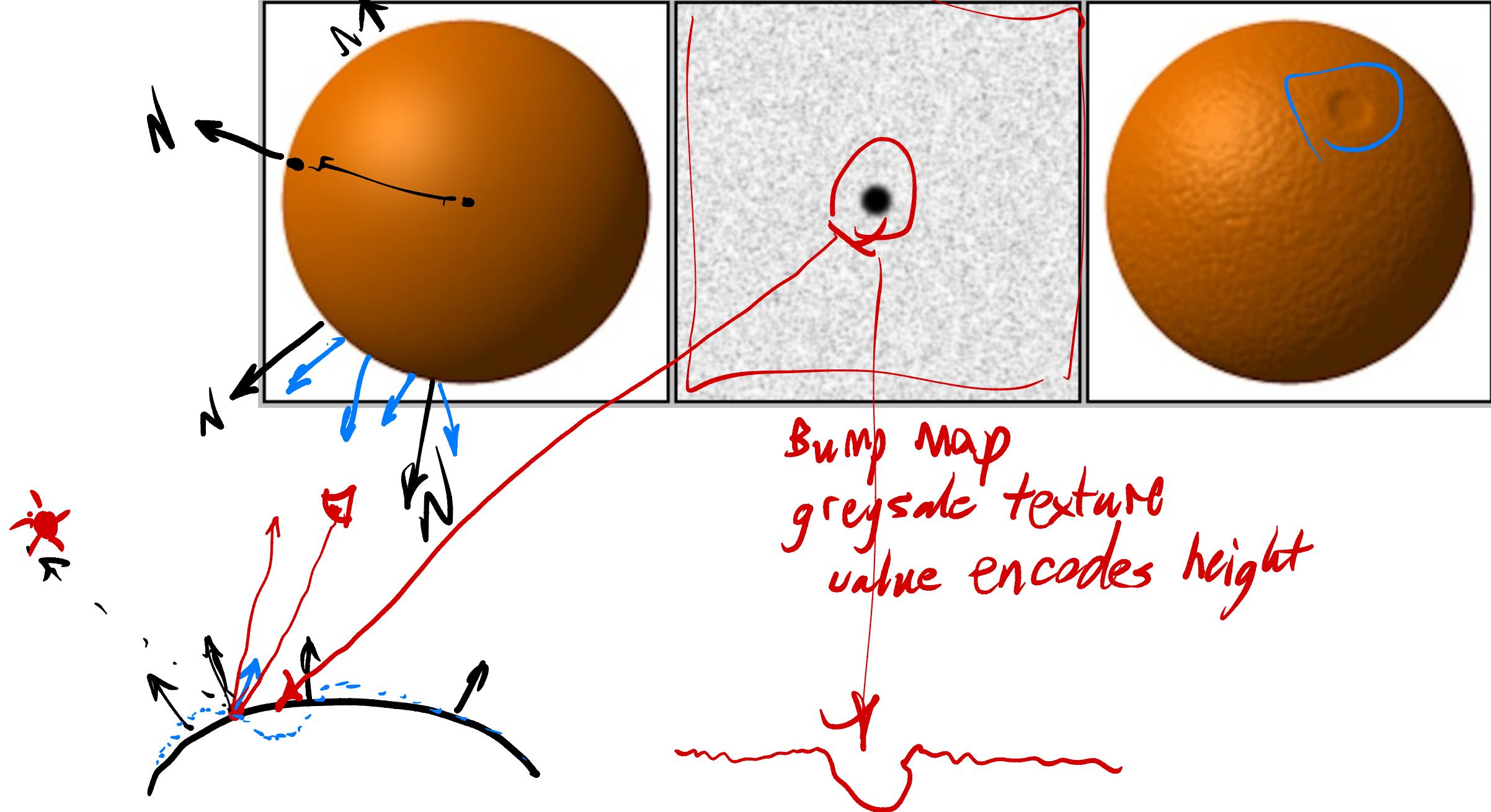


From this

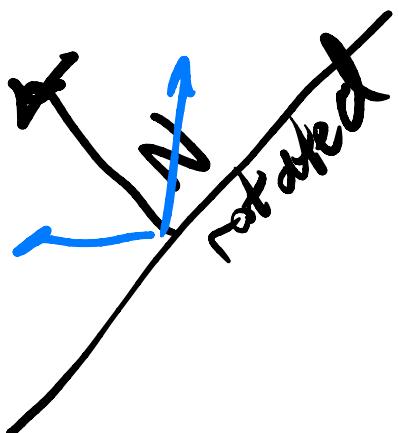
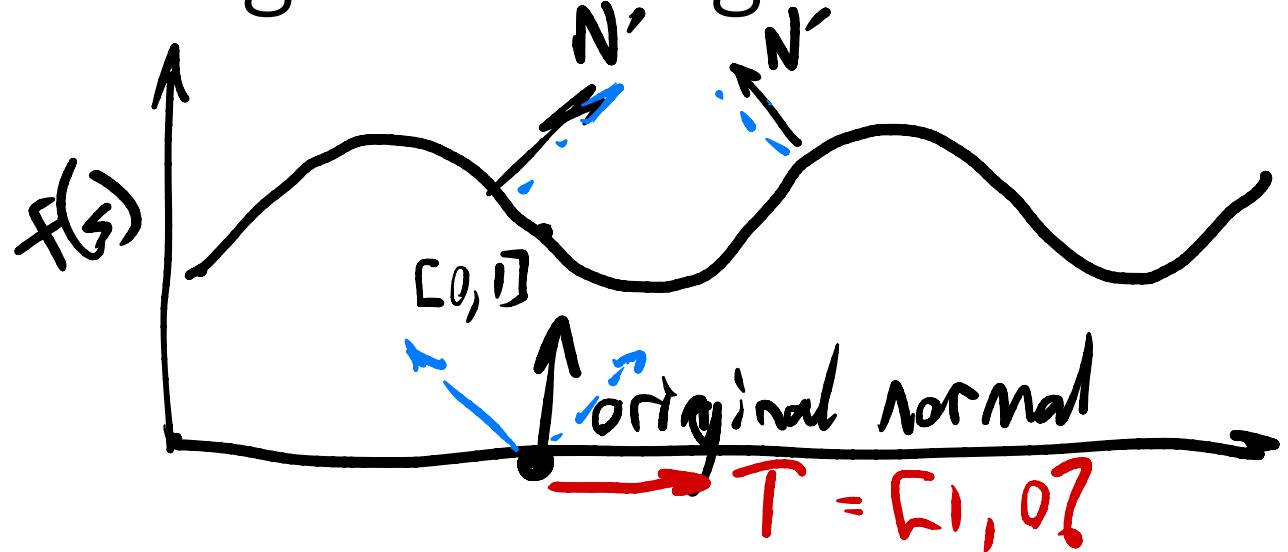


to this





High level algorithm

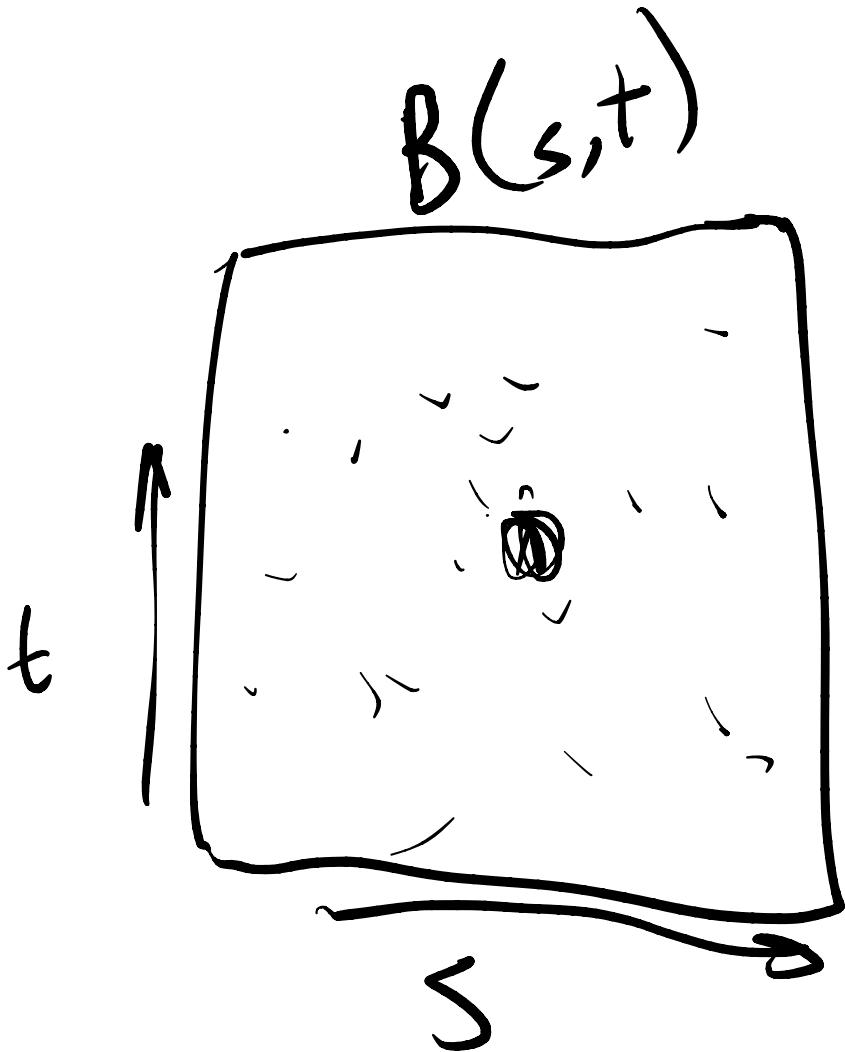


$$N = N - f(s) [1, 0]$$

\dagger

$$f(s) = [1 \dots 1]$$
$$0 \dots 255 \rightarrow -1 \dots 1$$

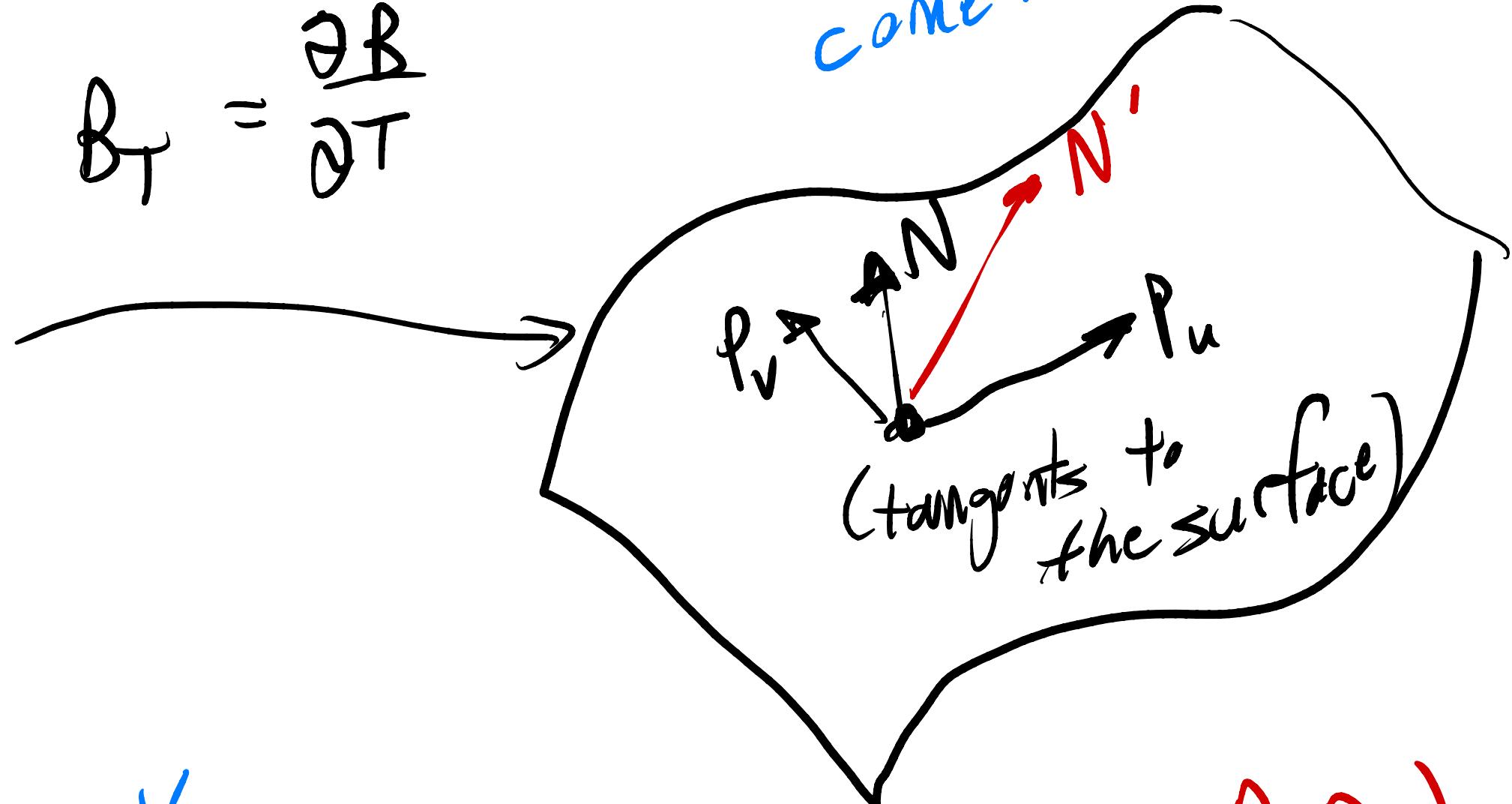
texture does not encode slope



$$B_s = \frac{\partial B}{\partial s}$$

$$B_t = \frac{\partial B}{\partial t}$$

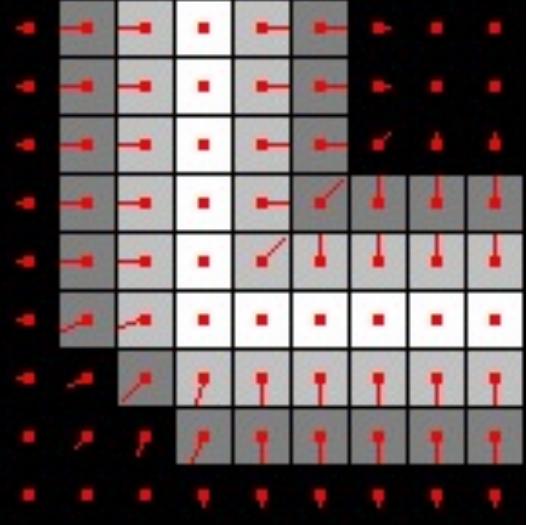
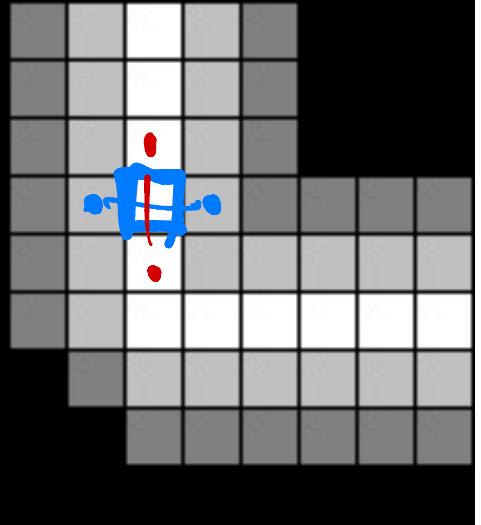
where do
 P_V & P_u ... ?
come from



$$N = N - (B_s P_u + B_t P_v)$$

(-1...)

slopes



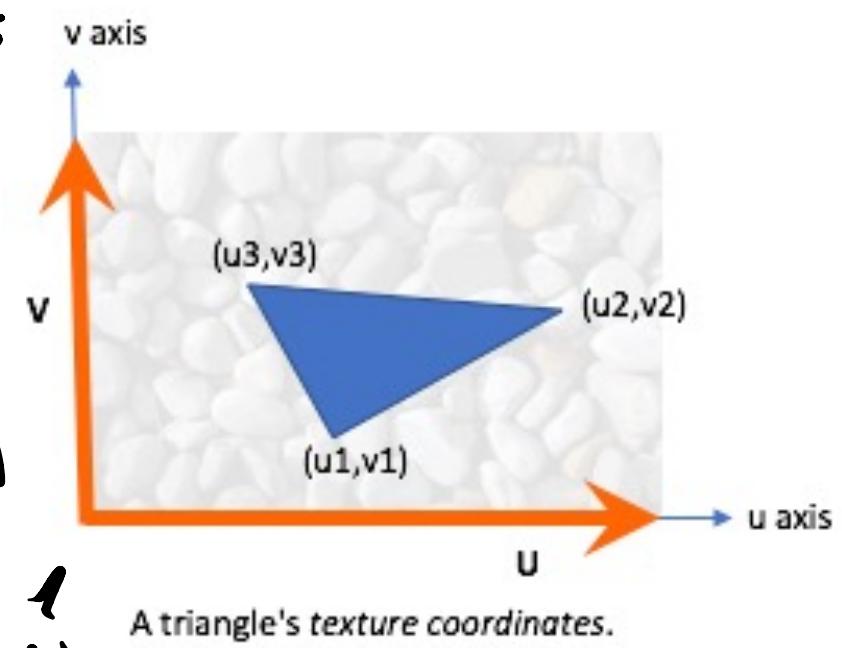
x_gradient = pixel(x-1, y) - pixel(x+1, y)
y_gradient = pixel(x, y-1) - pixel(x, y+1)

where do we
get B_s & B_t ?

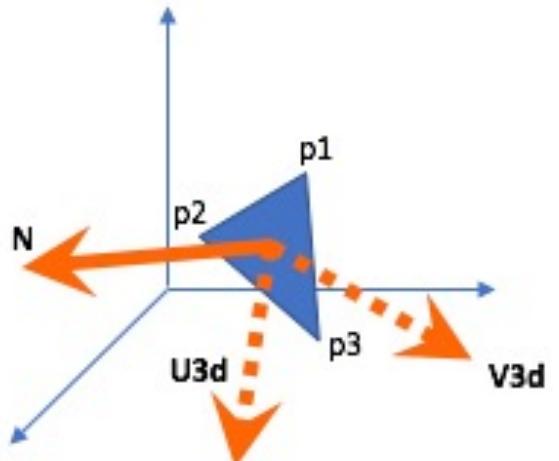
For Triangles

where
do
 $P_u \times P_v$
come
from?

want a basis
vectors that
align with
 u & v in the
texture



A triangle's texture coordinates.



3D object space.

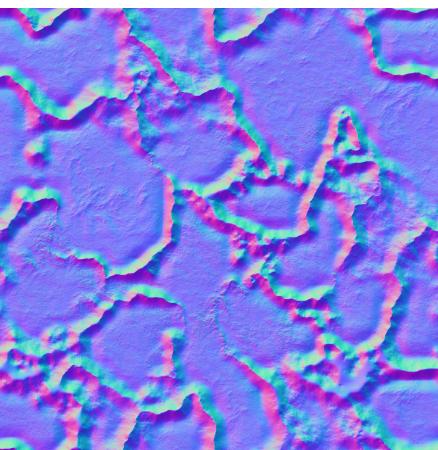
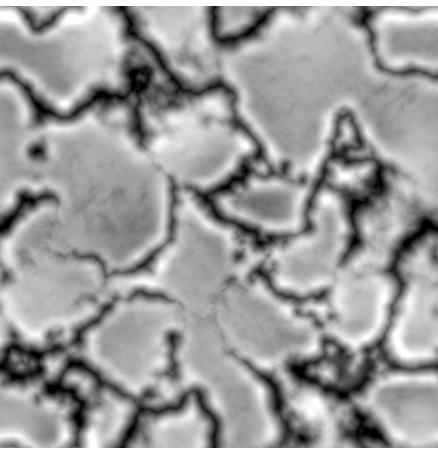
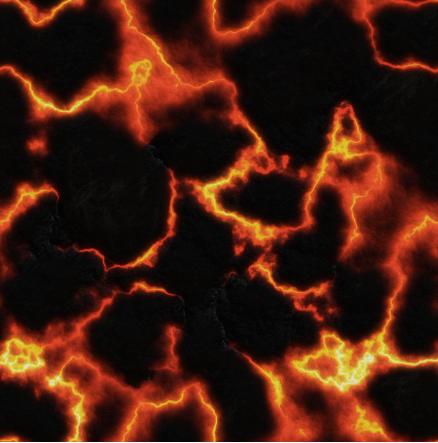
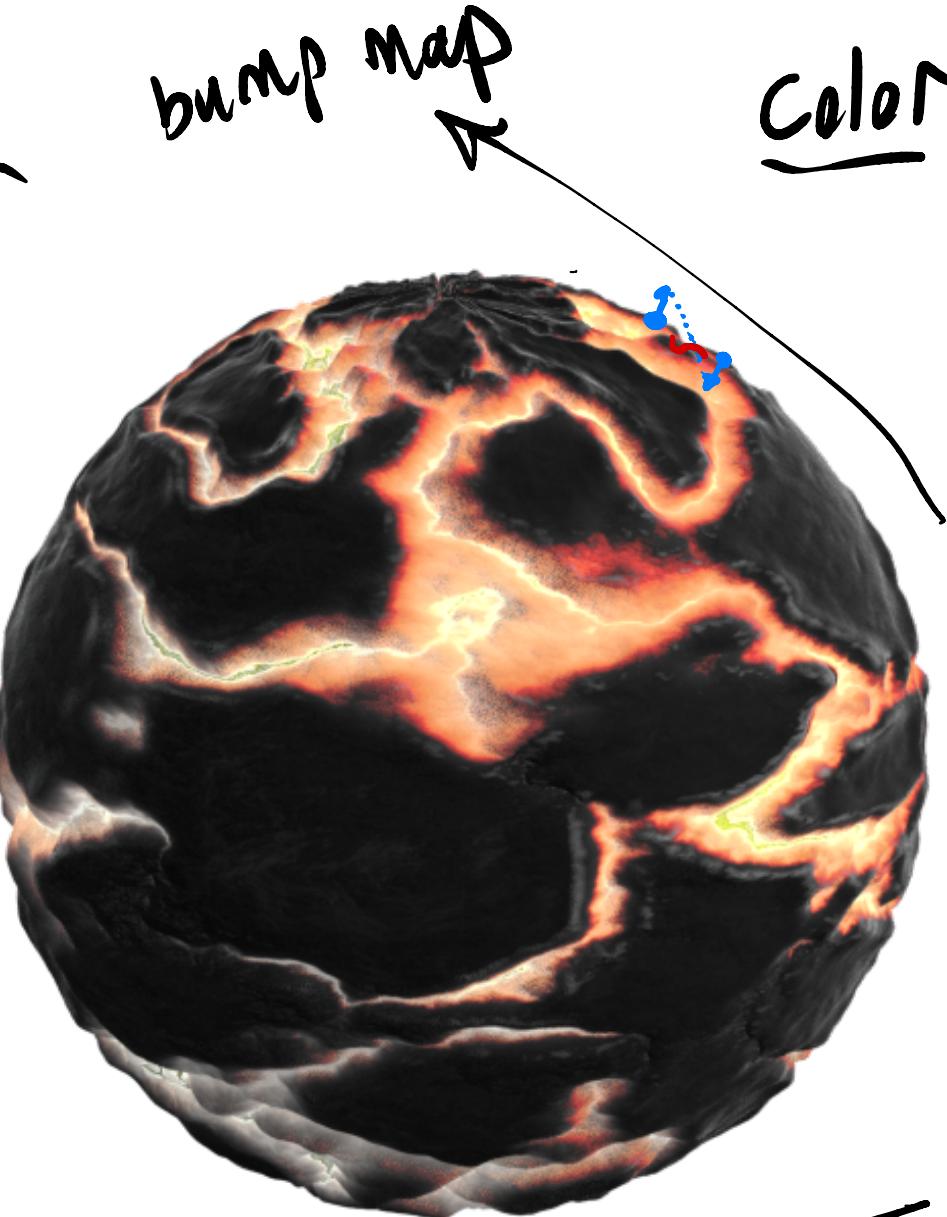
https://csawesome.runestone.academy/runestone/books/published/learnwebgl2/11_surface_properties/10_bump_maps.html

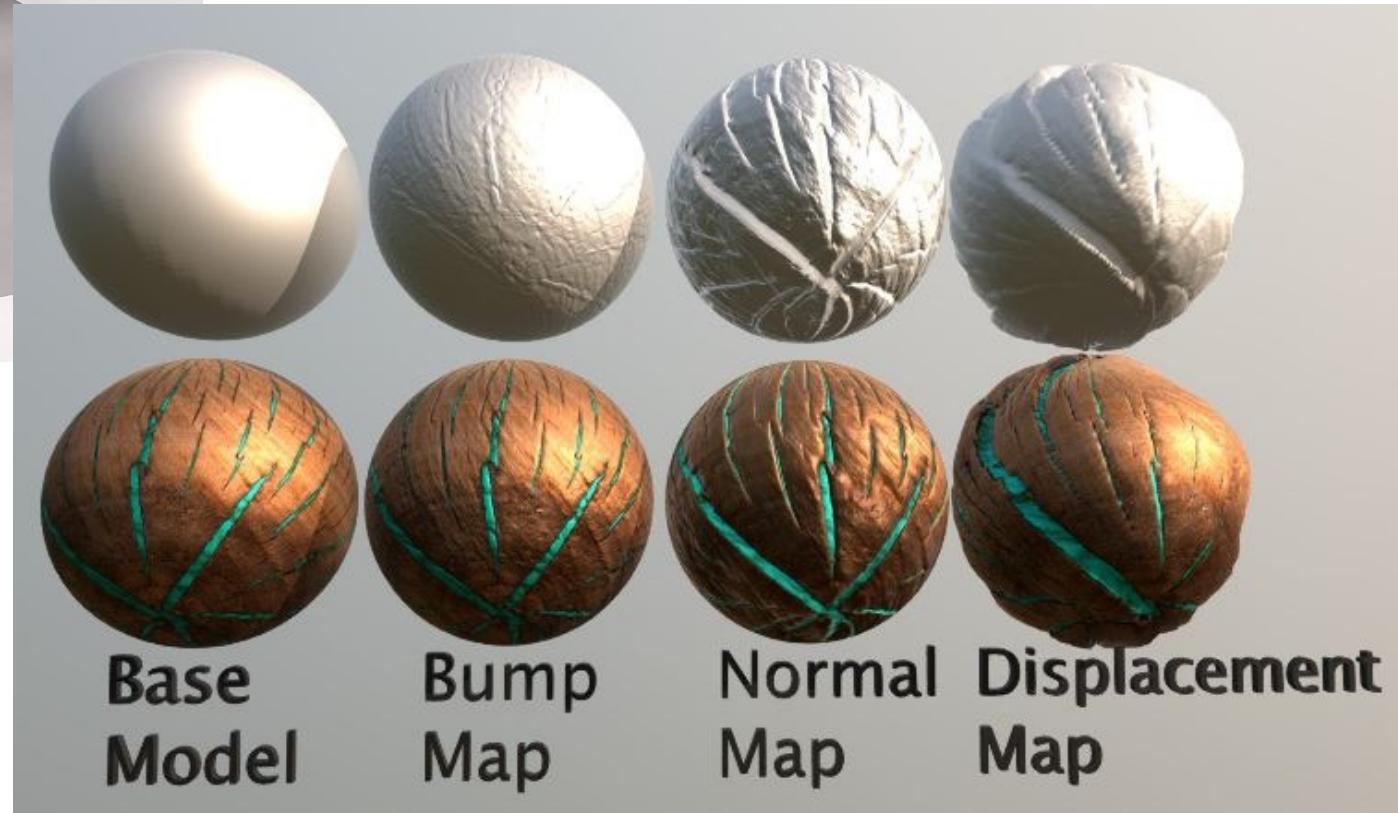
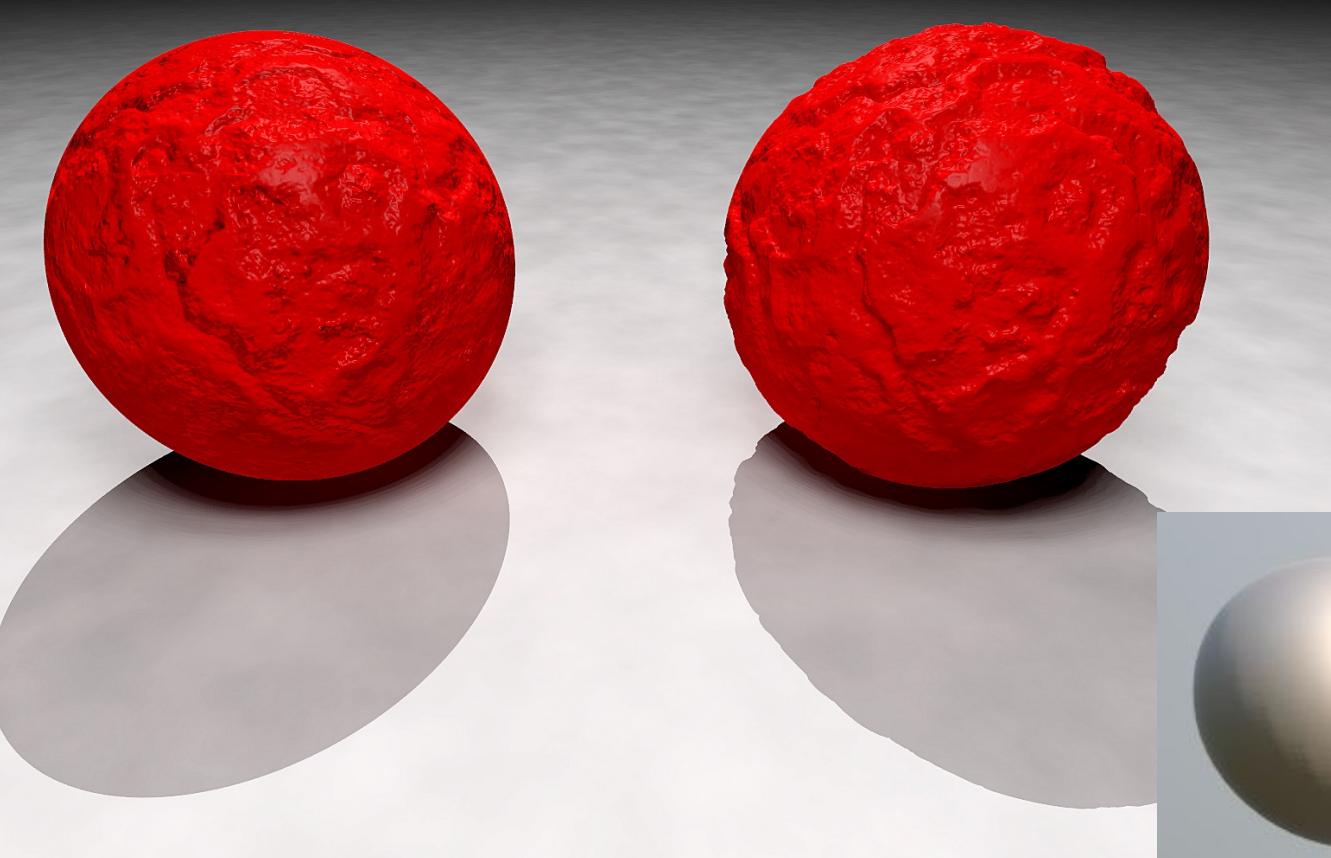
also use Norm Map
in vertex shader



$Q \dots 255$
 $P -1 \dots 1$ for x, y

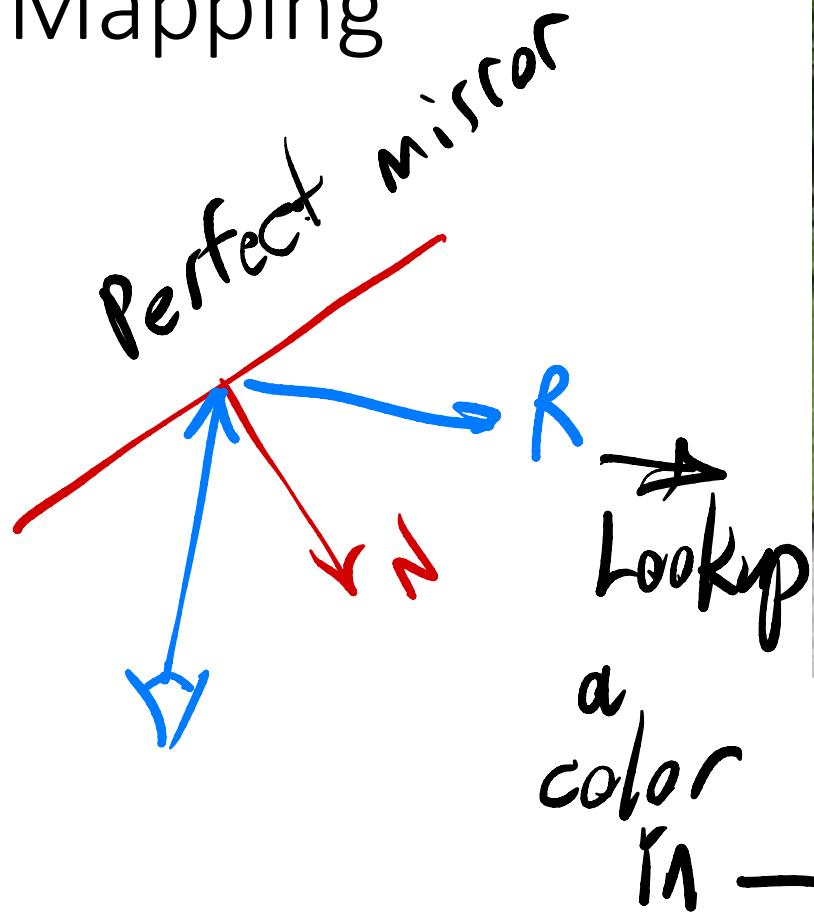
RGB of the normal
is the normal
 $(x, y, 1) \rightarrow (x, y, z)$





<https://spiderlili.com/2020/03/01/tech-art-tips-tricks-all-about-displacement-normal-bump-maps/>

Environment Mapping



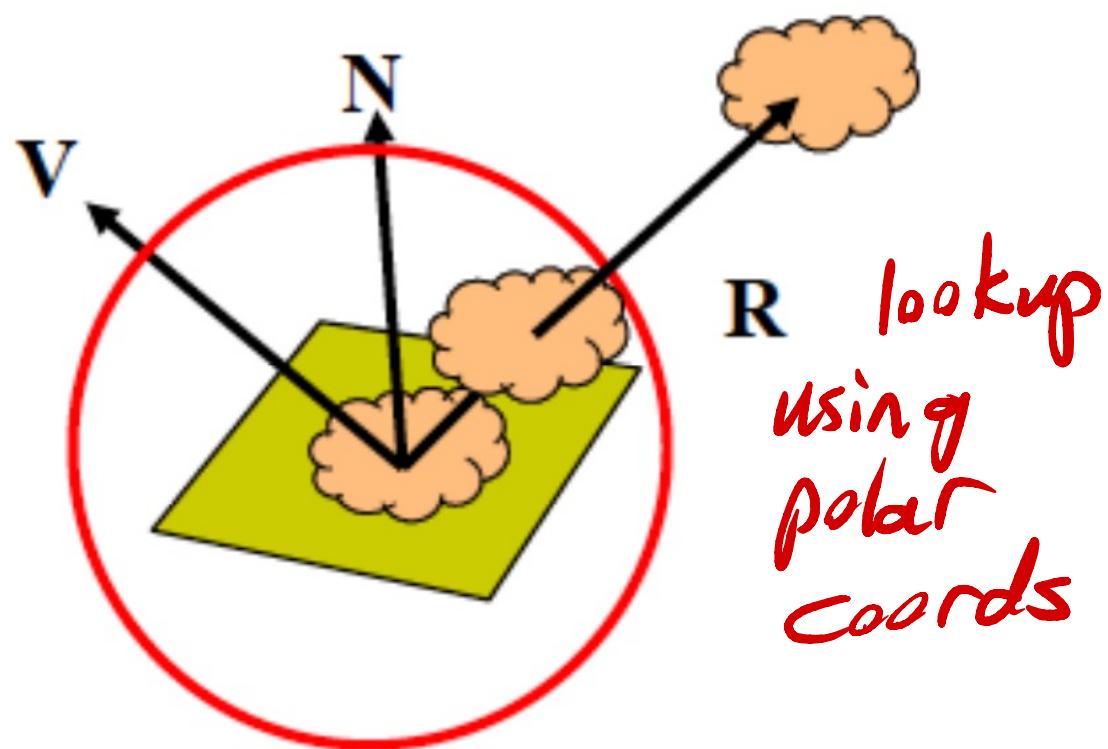
<https://www.youtube.com/watch?app=desktop&v=xLPRHNIxE6w>

Algorithm

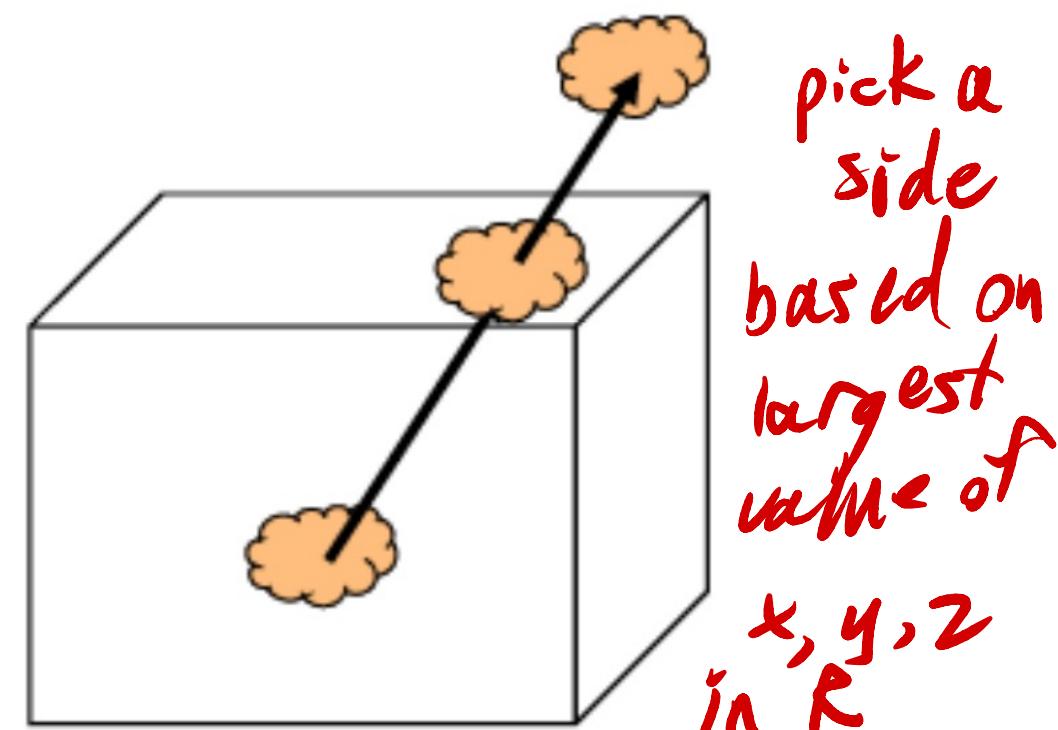
- 1) calculate R (vector) from NAV
 - 2) Use R to look up color in env map.
Texture lookup
- what are (u, v) \leftarrow texture coordinates

Two kinds of environment maps

a) Sphere around object (sphere map)



b) Cube around object (cube map)



<https://courses.engr.illinois.edu/cs418/fa2017/418-Lecture%2027-%20Environment%20Mapping.pdf>

Sphere maps

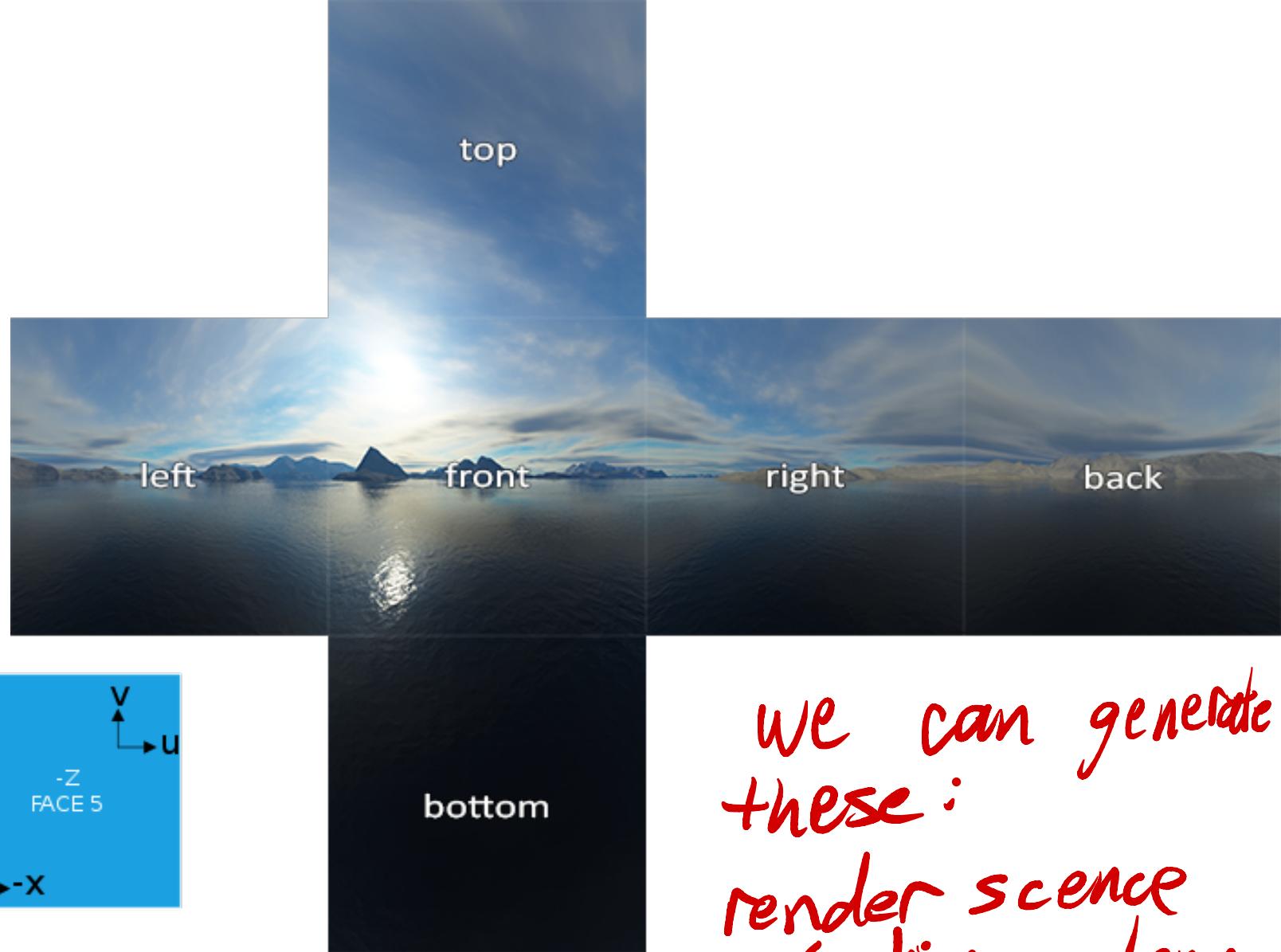
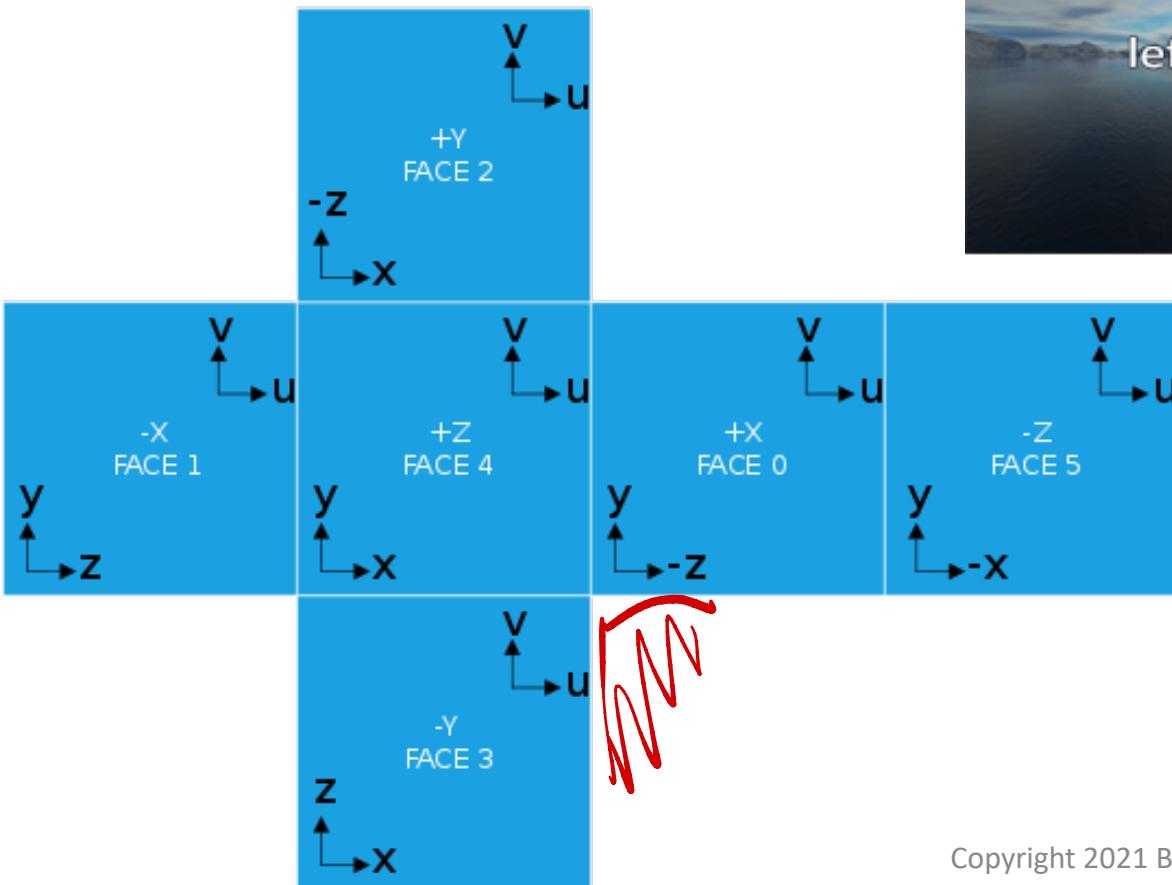
top & bottom are a single point



<https://aerotwist.com/tutorials/create-your-own-environment-maps/>

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Cube Map



We can generate these:
render scene 6 times along each \pm axis

