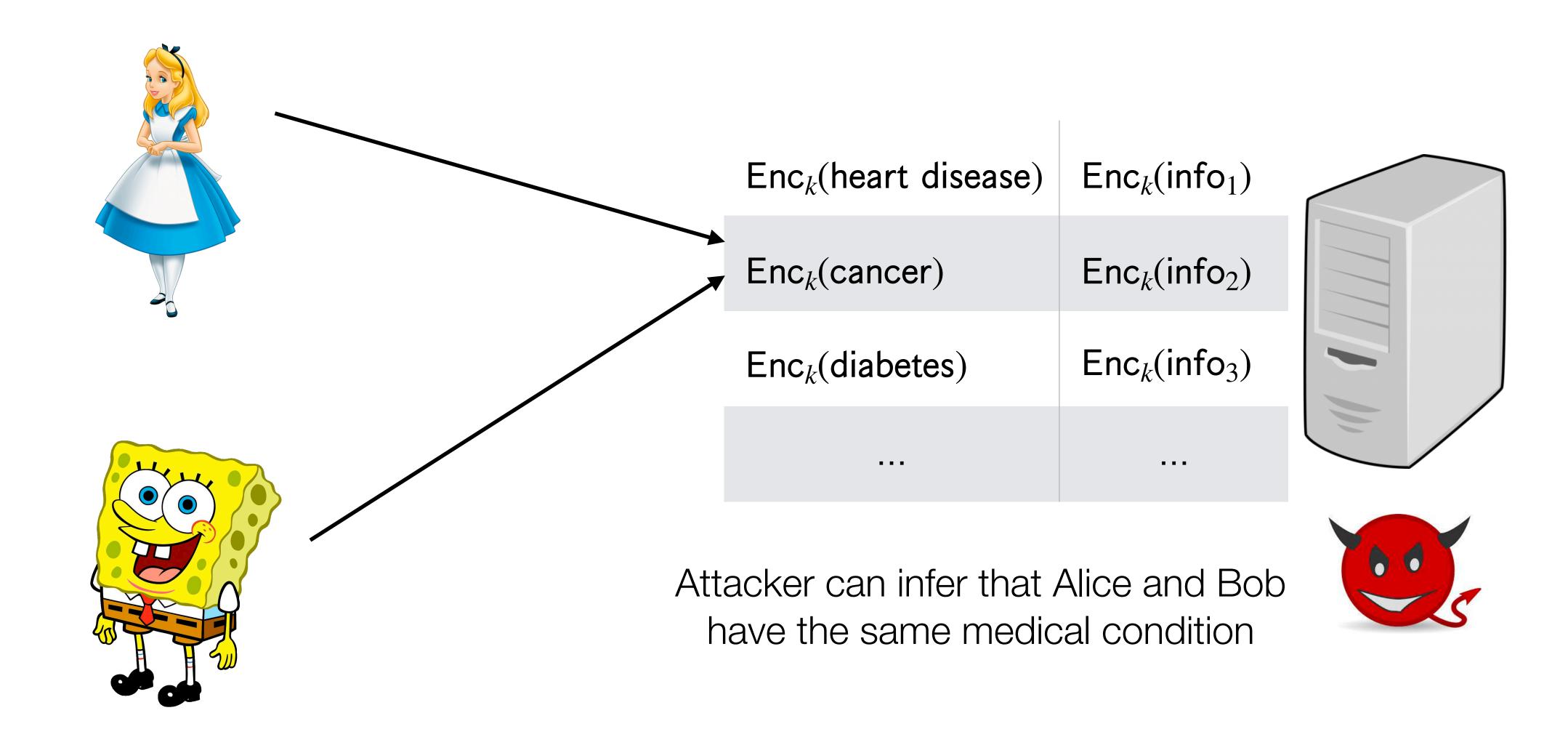
CS 350S: Privacy-Preserving Systems

Oblivious RAM

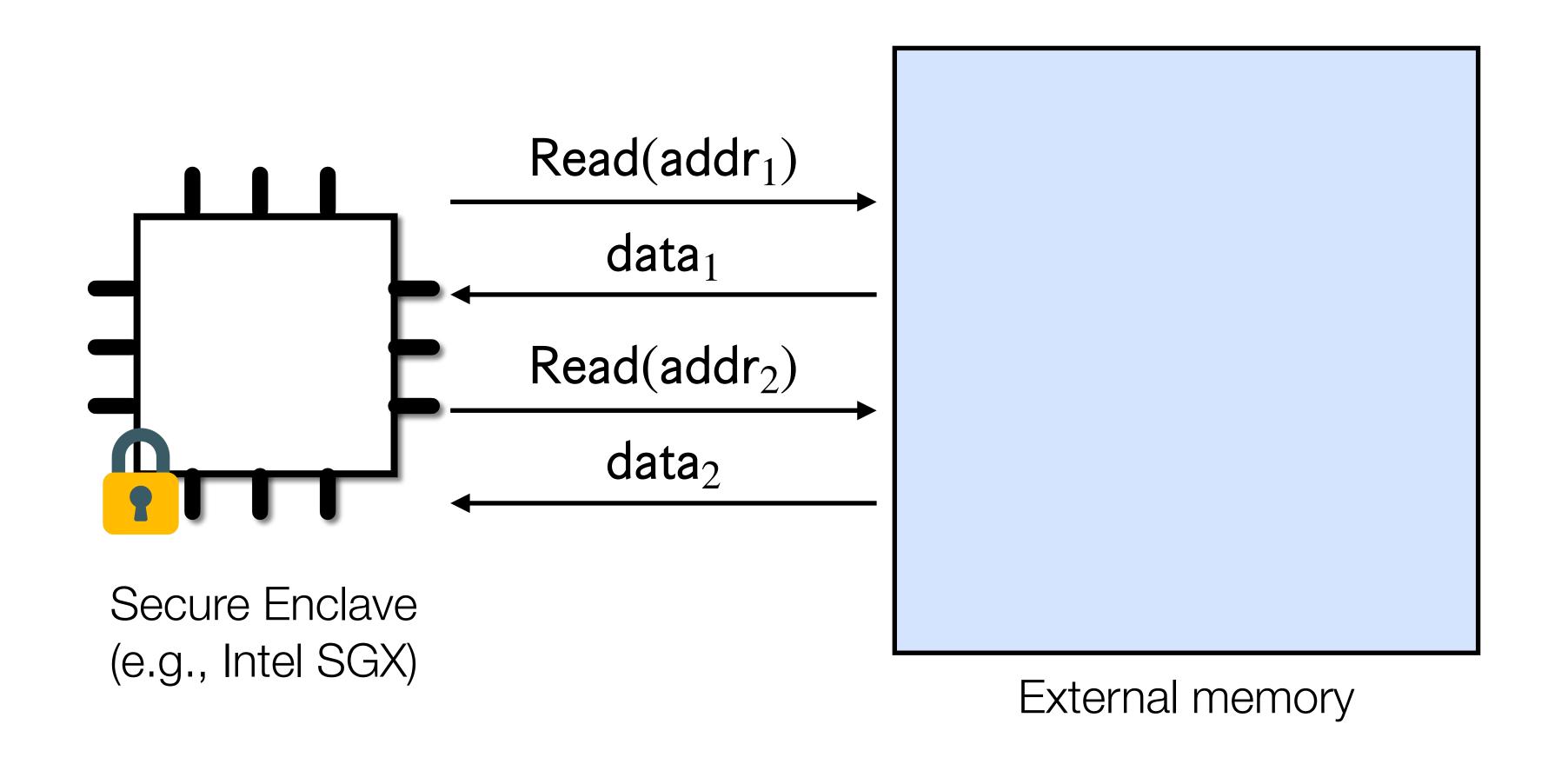
Outline

- 1. Overview
- 2. Square-root construction
- 3. Hierarchical construction
- 4. Limitations
- 5. Student presentation: PathORAM

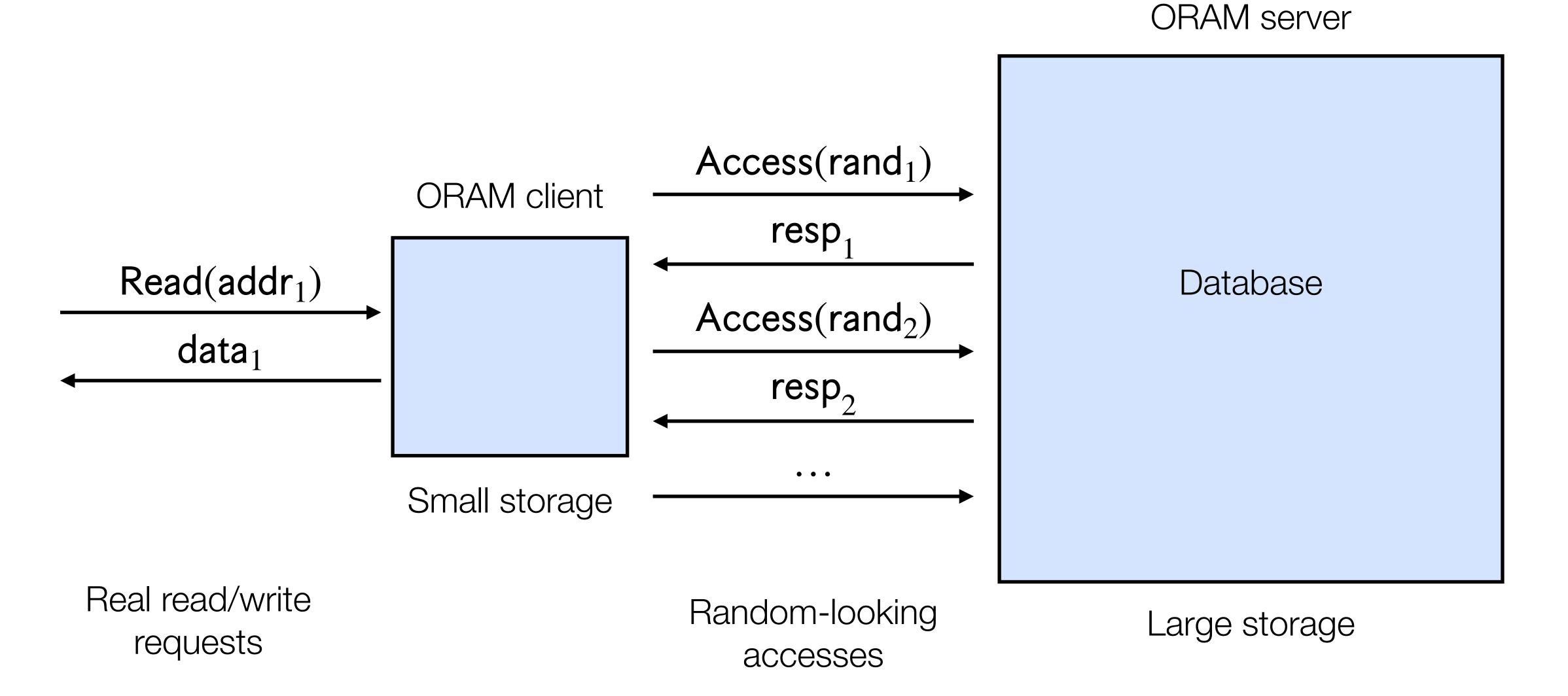
Access patterns can reveal sensitive information



Access patterns can reveal sensitive information

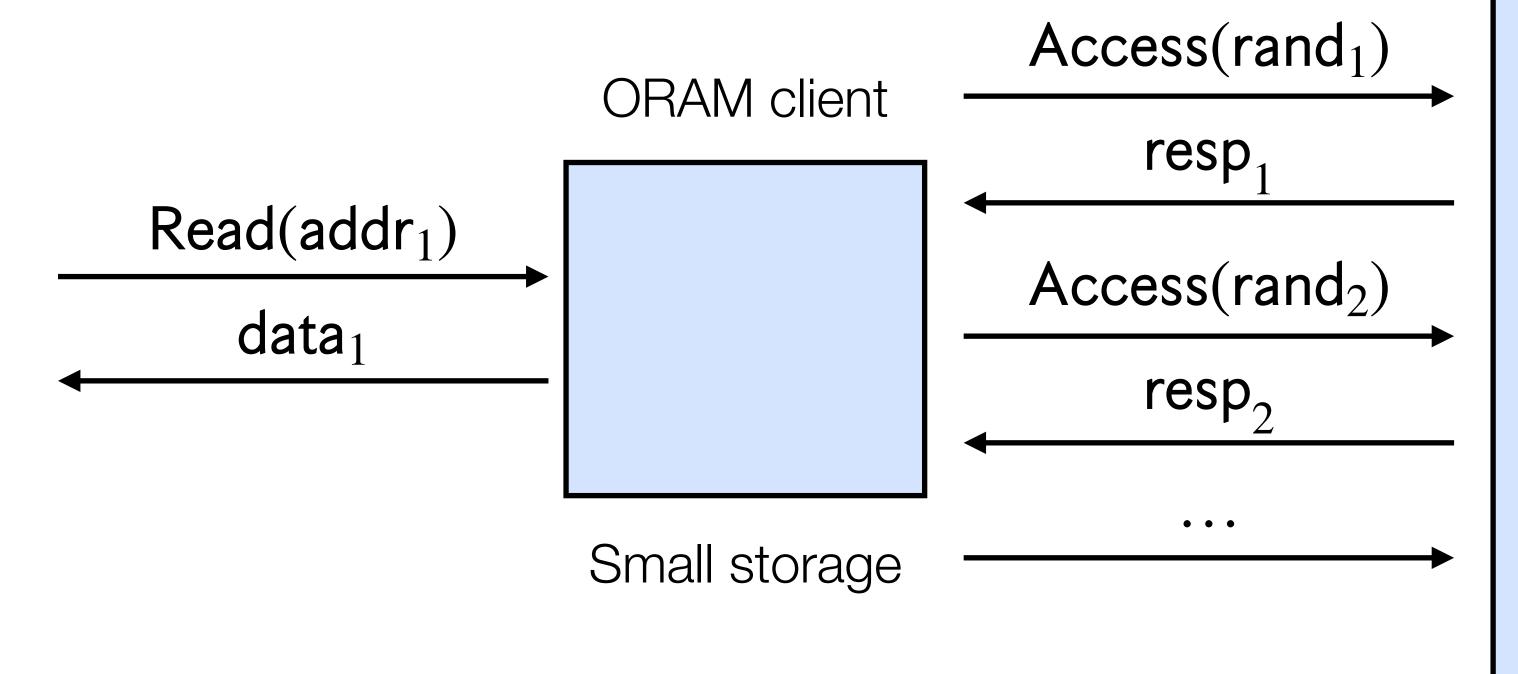


Oblivious RAM



Oblivious RAM

Attacker that observes memory accesses "learns nothing" about the real read/write requests



Database

Real read/write requests

Random-looking accesses

Large storage

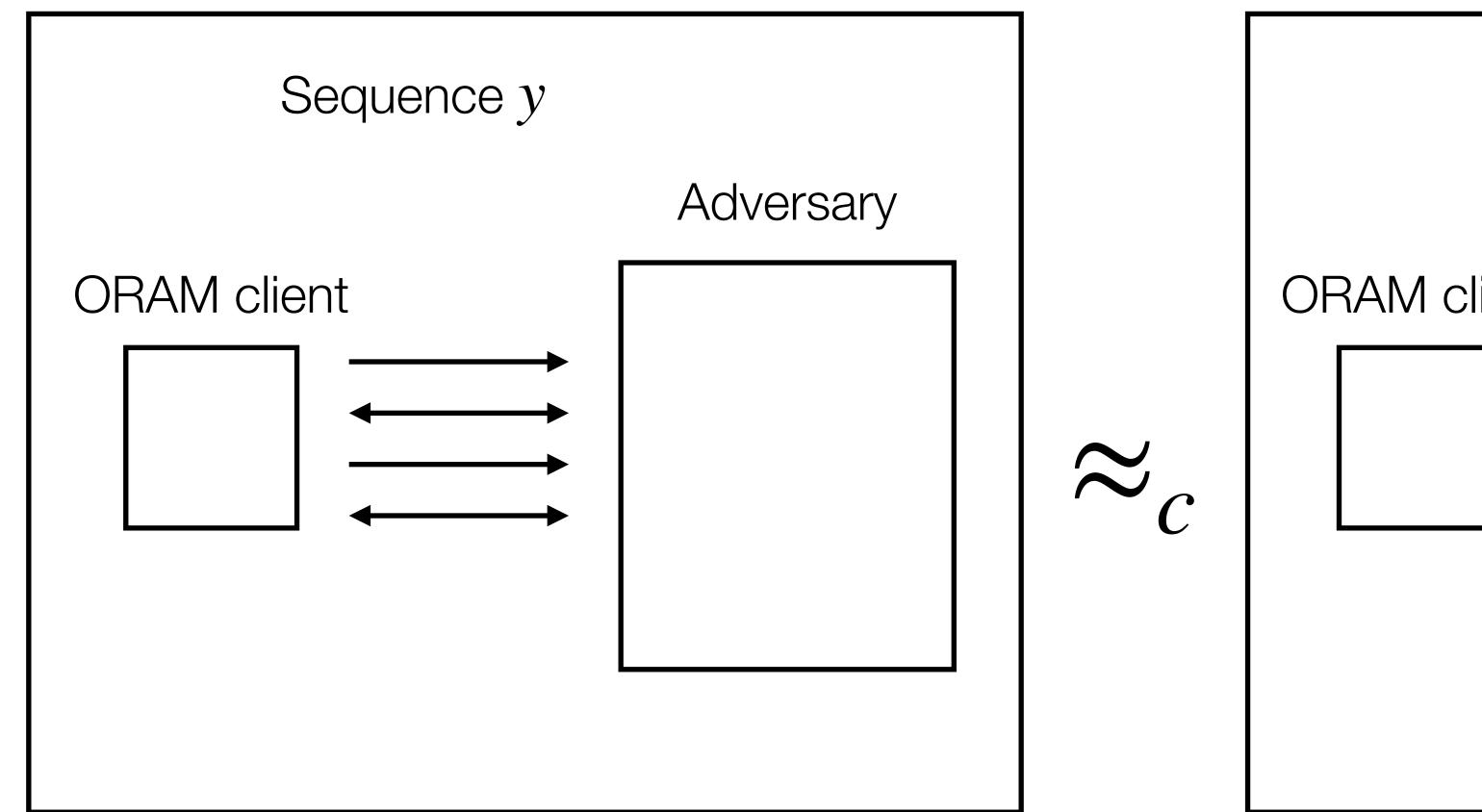
Definitions

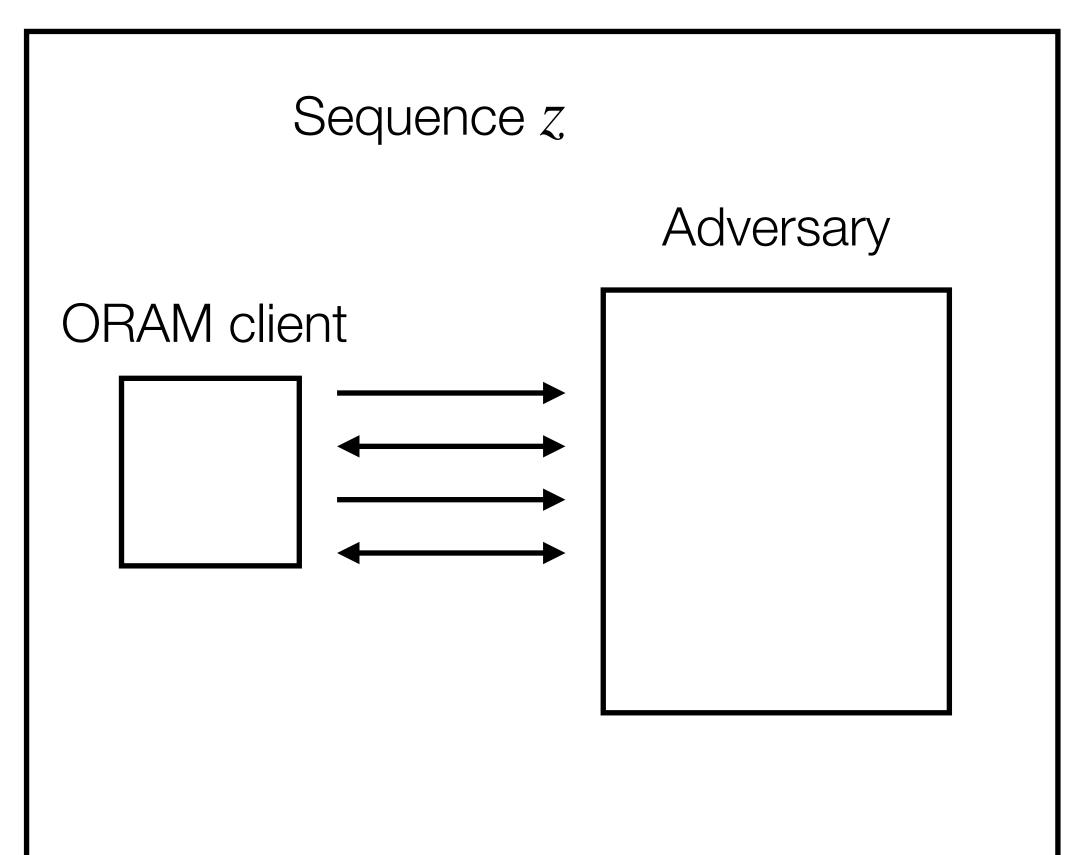
Sequence of operations $y = ((op_1, addr_1, data_1), (op_2, addr_2, data_2), ...)$ where $op \in \{read, write\}$

Correctness: An ORAM construction is correct if the responses from the ORAM for a sequence of operations y matches the responses from a standard RAM (with overwhelming probability).

Security: For any two request sequences y, z of the same length, their access patterns (i.e., interactions between ORAM client and server) are indistinguishable.

Security definition





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A very simple, very expensive construction

ORAM server

ORAM client Scan over every data element Why private? Server touched every element, and so the client could be accessing any element

Square-root ORAM construction

Goldreich and Ostrovsky

- Can we reduce the costs?
- Take advantage of:
 - Randomness
 - Large, mutable server state
 - Small, mutable client state

Setup: Client shuffles server data with permutation π

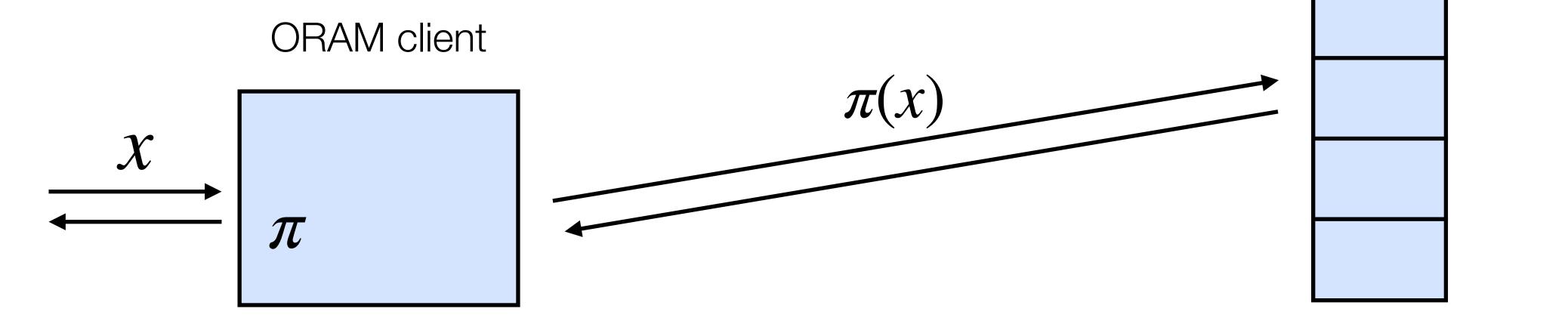
Access(x):

Step 1: Client accesses address x at $\pi(x)$

Problem: Server can tell if the client is accessing the same element twice

Use oblivious sorting algorithm so that access patterns are data-independent (Batcher's sorting)

ORAM server



ORAM server Setup: Client shuffles server data with permutation π Access(x): Step 1: Client accesses address x at $\pi(x)$ or the stash Step 2: Client adds accessed data to the stash ORAM client $\pi(x)$ Stash

Stash stores all elements fetched with π

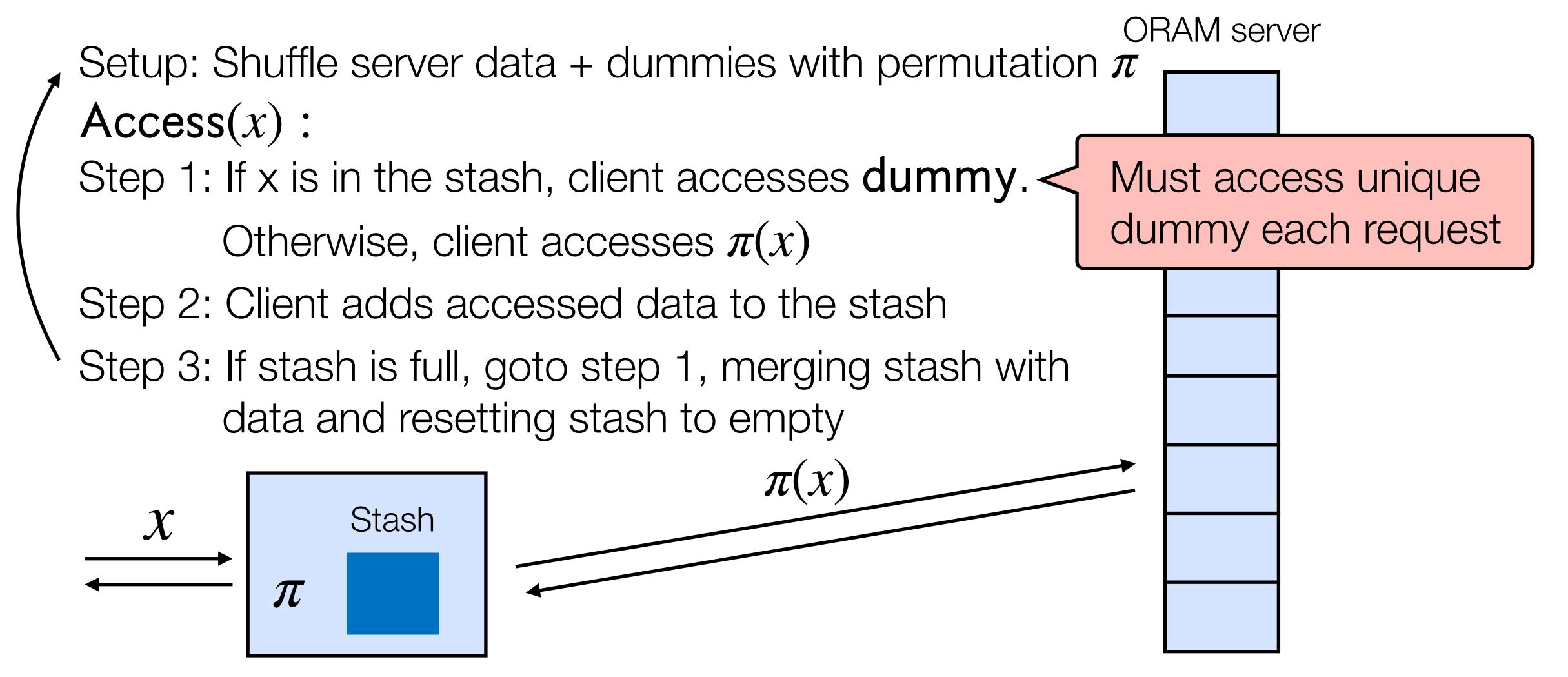
ORAM server Setup: Client shuffles server data with permutation π Access(x): Step 1: Client accesses address x at $\pi(x)$ or the stash Step 2: Client adds accessed data to the stash ORAM client $\pi(x)$ Stash

Problem: How to keep stash from growing indefinitely?

ORAM server Setup: Client shuffles server data with permutation π Access(x): Step 1: Client accesses address x at $\pi(x)$ or the stash Step 2: Client adds accessed data to the stash Step 3: If stash is full, goto step 1, merging stash with data and resetting stash to empty ORAM client Stash

Problem: How to hide if a request is in the stash?

ORAM server Setup: Shuffle server data + dummies with permutation $\tilde{\pi}$ Access(x): Step 1: If x is in the stash, client accesses dummy. Otherwise, client accesses $\pi(x)$ Step 2: Client adds accessed data to the stash Step 3: If stash is full, goto step 1, merging stash with data and resetting stash to empty Stash



Correctness

Setup: Shuffle server data + dummies with permutation π

Access(x):

Step 1: If x is in the stash, client accesses dummy.

Otherwise, client accesses $\pi(x)$

Step 2: Client adds accessed data to the stash

Step 3: If stash is full, goto step 1, merging stash with data and resetting stash to empty

Correctness from:

- Correctness of shuffle
- Correct maintenance of the stash

Security

Setup: Shuffle server data + dummies with permutation π

Access(x):

Step 1: If x is in the stash, client accesses dummy.

Otherwise, client accesses $\pi(x)$

Step 2: Client adds accessed data to the stash

Step 3: If stash is full, goto step 1, merging stash with data and resetting stash to empty

Security from:

- Permutation appears random to the server
- Each request accesses a unique element
- Server cannot distinguish a real request from a dummy request

Parameterizing square-root ORAM

Length n array, stash size s

Add s dummies

Setup: Shuffle server data + dummies with permutation π

 $\begin{cases} O(n \cdot \log^2 n) \\ \text{comparisons} \end{cases}$

Check s elements

Access(x):

Step 1: If x is in the stash, client accesses dummy.

Otherwise, client accesses $\pi(x)$

Step 2: Client adds accessed data to the stash

Step 3: If stash is full, goto step 1, merging stash with data and resetting stash to empty

By setting stash size $s = \sqrt{n}$, amortized overhead is $O(\sqrt{n} \cdot \log^2 n)$

Client storage is $O(\sqrt{n})$

Outline

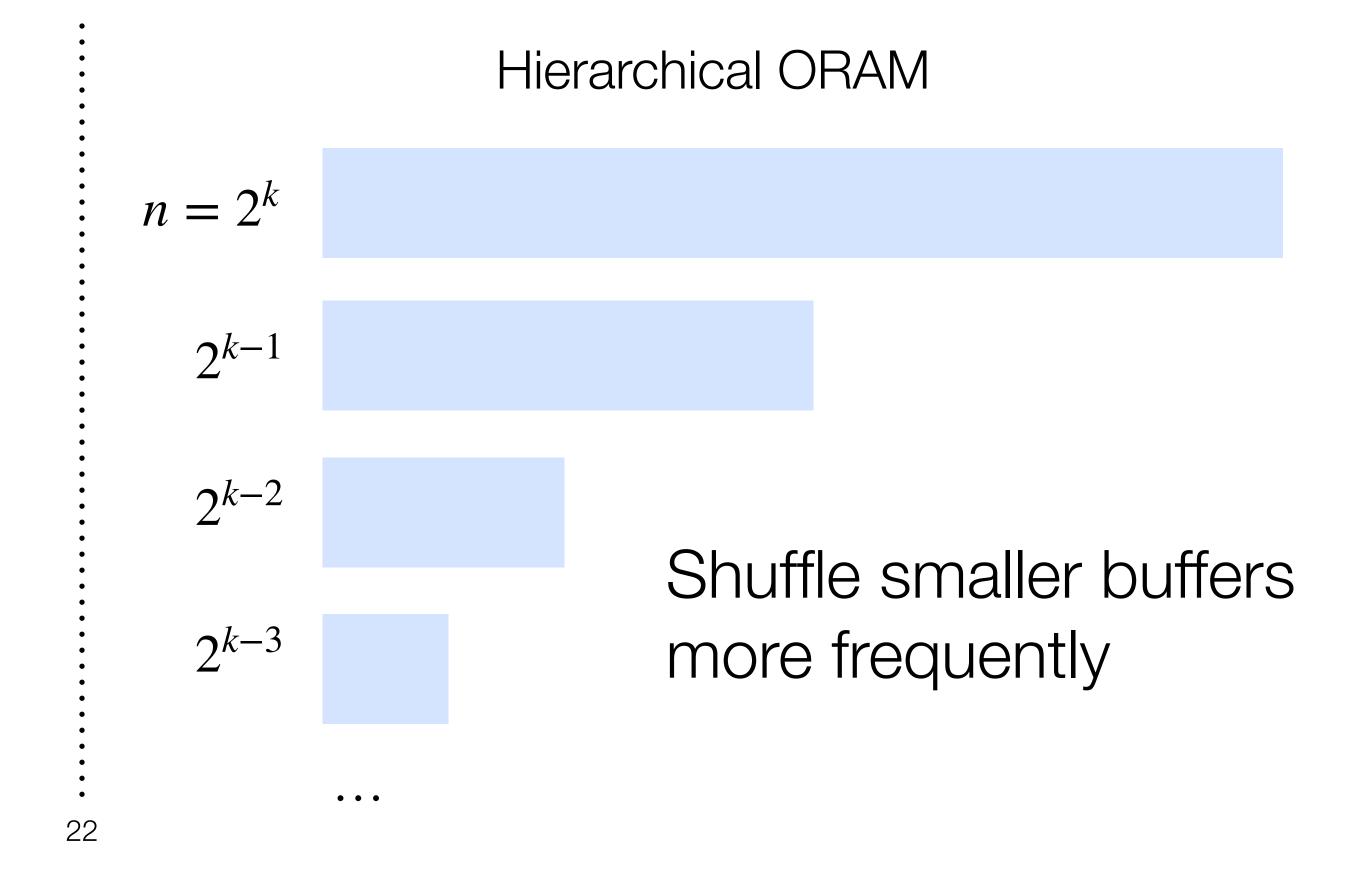
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[Goldreich, Ostrovsky]

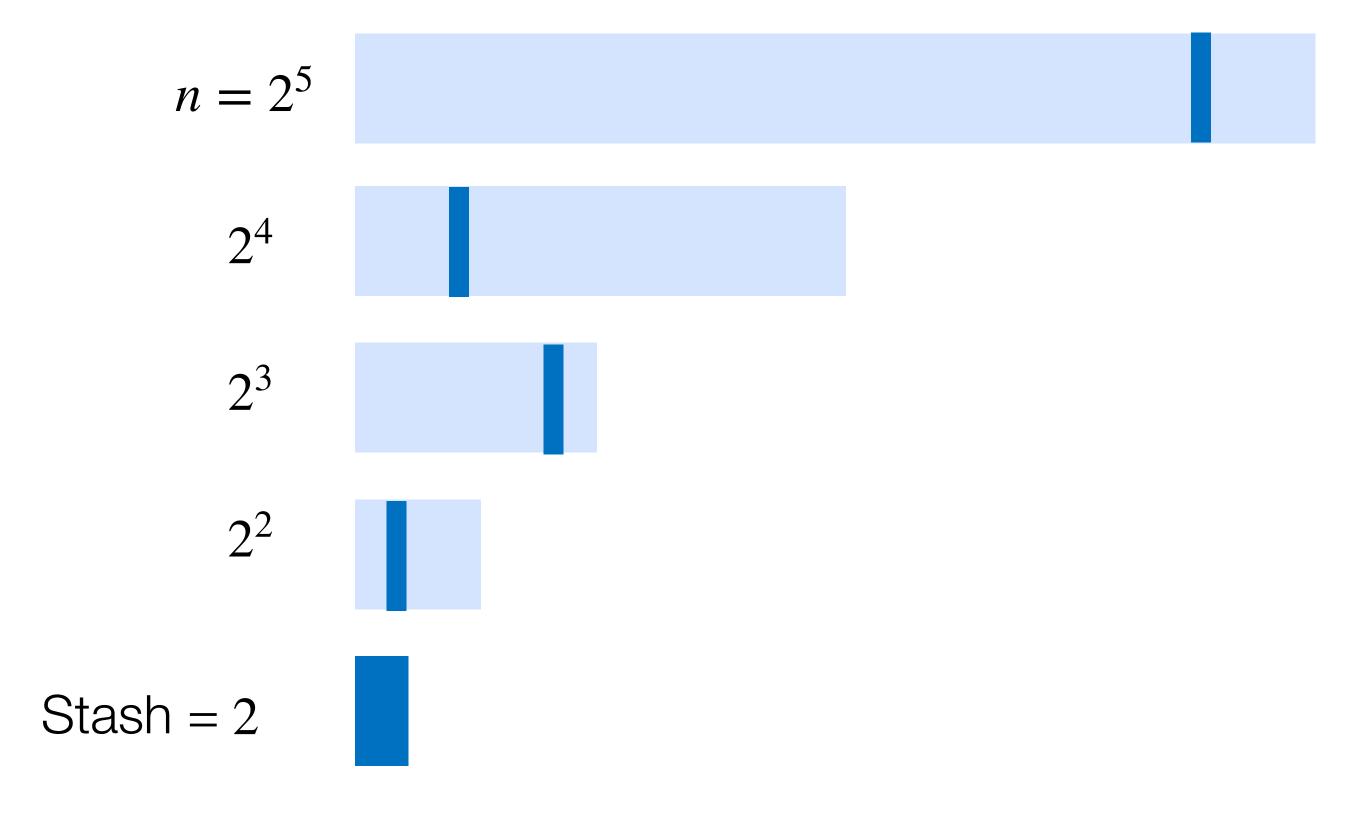
High-level idea: Hierarchy of different-sized buffers to achieve logarithmic overhead

Square-root ORAM

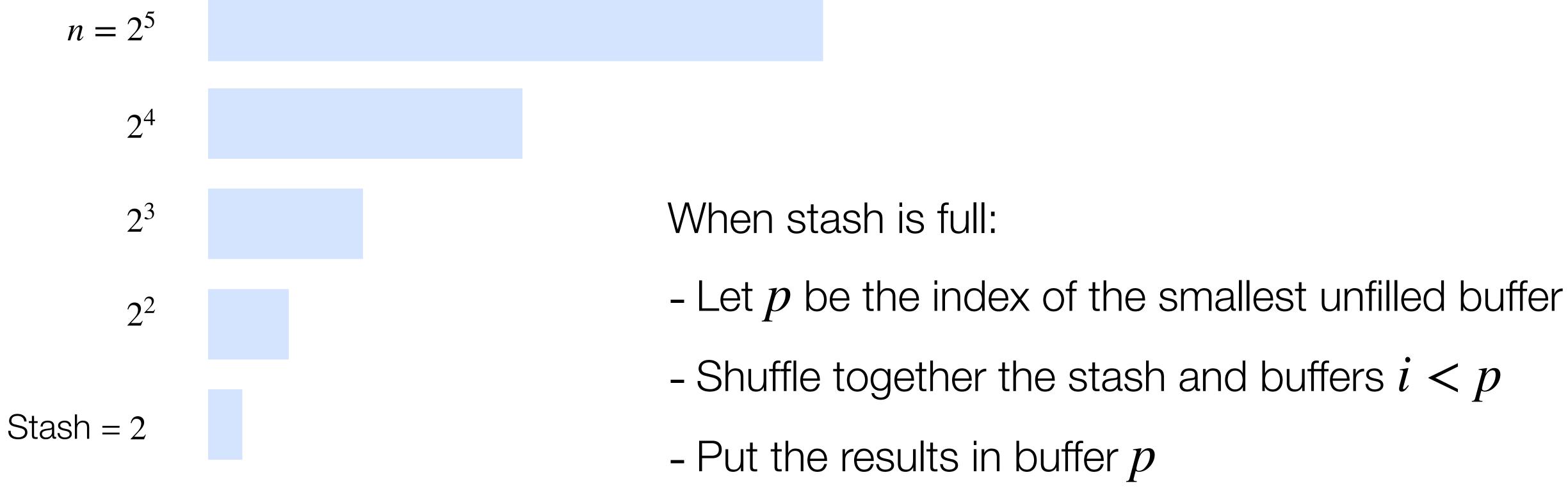
 $n = 2^{k}$



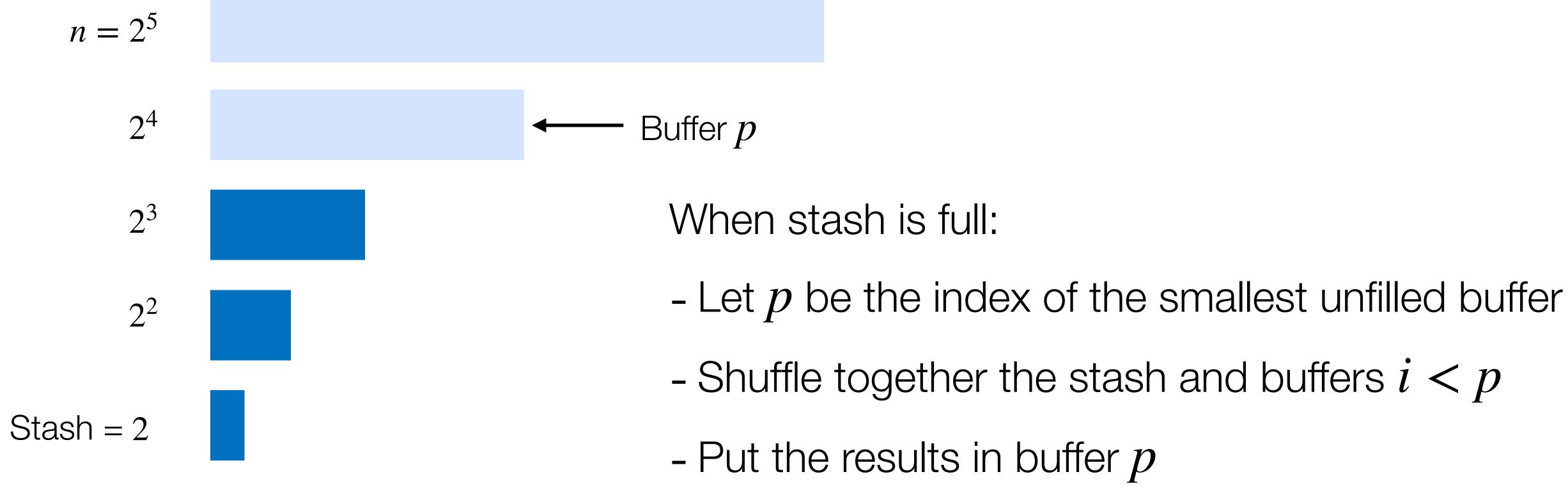
Access requires scanning over the stash and making a lookup in each buffer



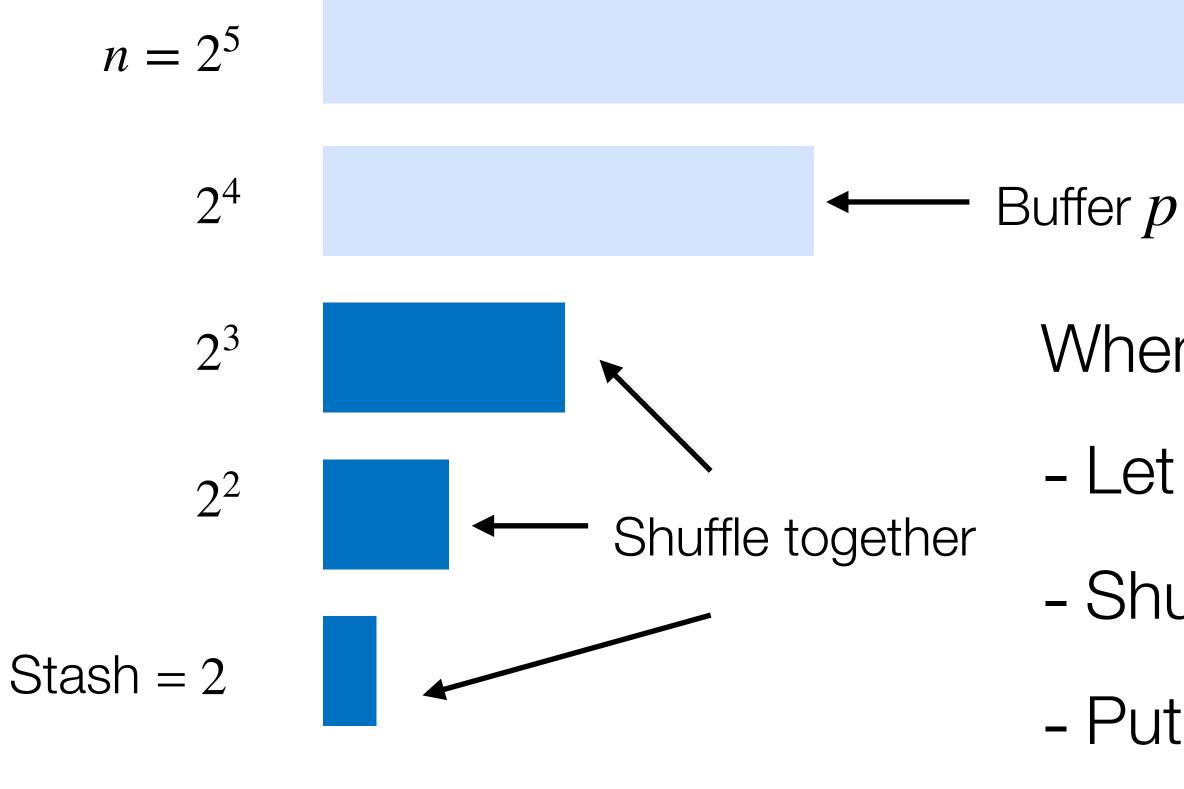
Shuffle smaller buffers more frequently



Shuffle smaller buffers more frequently



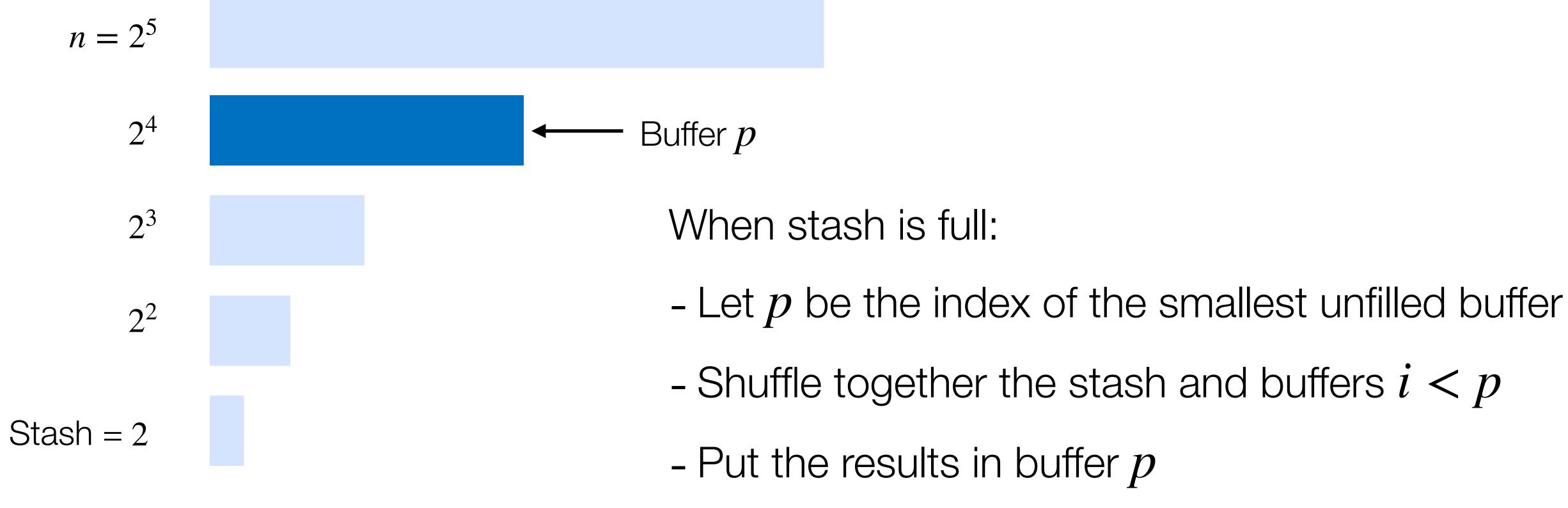
Shuffle smaller buffers more frequently



When stash is full:

- Let p be the index of the smallest unfilled buffer
- Shuffle together the stash and buffers i < p
- Put the results in buffer *p*

Shuffle smaller buffers more frequently



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Limitations of ORAM

- All elements must be the same length
- Increased cost compared to plaintext RAM accesses: lower bound of $O(\log n)$ accesses per operation [Larsen, Nielsen]
- ORAM is designed for a single client; does not directly support multiple clients
- Accesses where shuffling is required take longer than accesses without shuffling (not the case for tree-based ORAMs)
- Elements must be fetched in sequence, not in parallel (addressed in subsequent work, e.g., TaoStore)
- Only supports key-value lookups, but applications need other types of queries

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References

Goldreich, Oded, and Rafail Ostrovsky. "Software protection and simulation on oblivious RAMs." *Journal of the ACM (JACM)* 43.3 (1996): 431-473.

Larsen, Kasper Green, and Jesper Buus Nielsen. "Yes, there is an oblivious RAM lower bound!." *Annual International Cryptology Conference*. Cham: Springer International Publishing, 2018.

Sahin, Cetin, et al. "Taostore: Overcoming asynchronicity in oblivious data storage." 2016 IEEE Symposium on Security and Privacy (SP). IEEE, 2016.

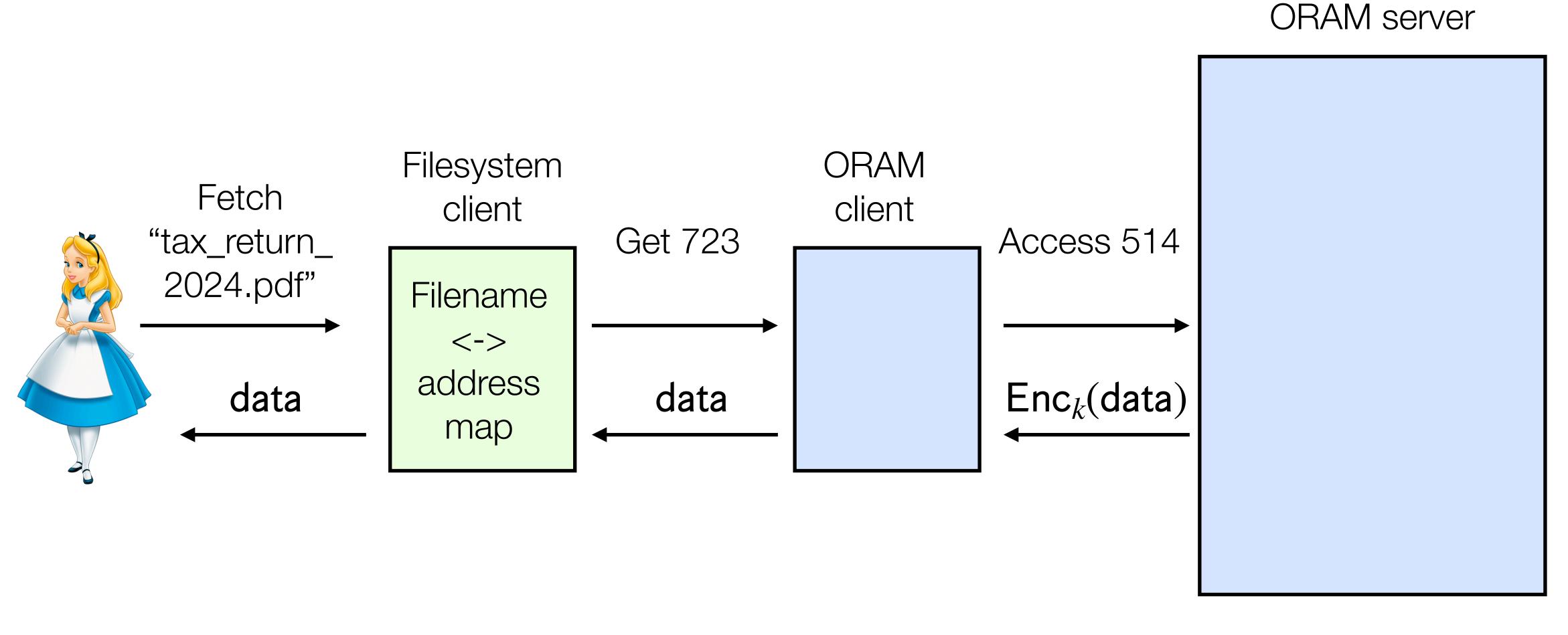
Stefanov, Emil, et al. "Path ORAM: an extremely simple oblivious RAM protocol." *Journal of the ACM (JACM)* 65.4 (2018): 1-26

https://6893.csail.mit.edu/lec7.pdf

Applications

- Oblivious filesystem: hide both the client's documents and the access patterns to these documents
- Oblivious search over files: hide both the client's documents and the client's queries

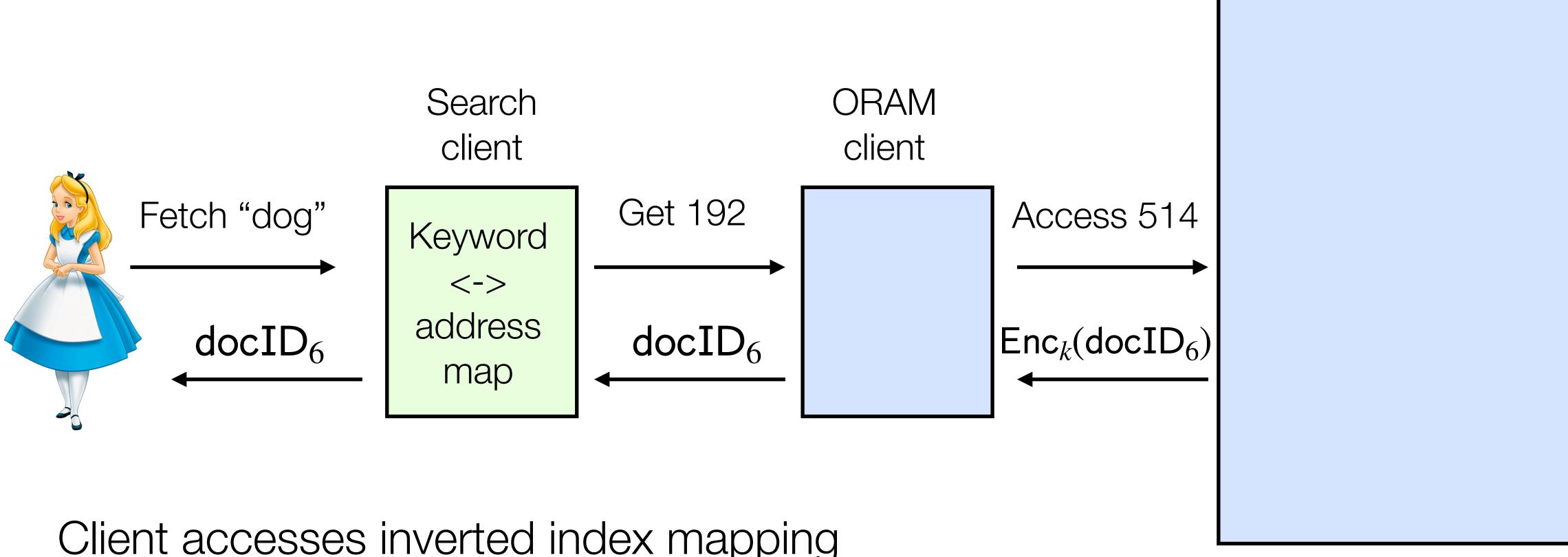
Application: Oblivious filesystem



Stores encrypted, shuffled blocks of user files

Application: Oblivious search over encrypted files

ORAM server



Client accesses inverted index mapping keyword to list of docIDs inside ORAM

Stores encrypted, shuffled list of docIDs containing keywords