

Practice Assignment

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$$\begin{array}{cccccc}
 (\log n + 1)^3 & 7^{2n} & n^{\log_7 2} & 2^n & 1000(\log n)^2 \\
 = (\log n)^3 & 49^n & \sqrt{n} & 128^n & (\log n)^3 \\
 \textcircled{1} & \textcircled{2} & \textcircled{3} & \textcircled{4} & \textcircled{5} \\
 2^{\log_2 n} & n \log n & 5^{\log_5 n} & 0 & \textcircled{6} \\
 n & n \log n & \textcircled{7} & & \textcircled{8} \\
 \textcircled{9} & \textcircled{10} & & &
 \end{array}$$

1) $2^{2n} 7^{2n} 5^{\log_5 n} \approx n \log_2 2^{2n} n^{\log_5 2} \approx (\log n + 1)^3 = 1000(\log n)^2$

2) a) $\lim_{n \rightarrow \infty} \frac{3n+6}{10000n-500} = \frac{3}{10000} f = \Theta(g)$

b) $\lim_{n \rightarrow \infty} \frac{n^2}{n^{2/3}} = \frac{1}{n^{1/3}} = \frac{1}{\infty} = 0 f = O(g)$

c) $\lim_{n \rightarrow \infty} \frac{\log(7n)}{\log(n)} = 1 f = \Theta(g)$

d) $\lim_{n \rightarrow \infty} \frac{n^{2/3}}{n \log n} \geq \lim_{n \rightarrow \infty} \frac{n^{2/3}}{n \log n} = \infty f = \Omega(g)$

e) $\lim_{n \rightarrow \infty} \frac{\sqrt{n}}{(\log n)^3} = \infty f = \Omega(g) \quad (\text{from } \#1)$

f) $\lim_{n \rightarrow \infty} \frac{n^{2/3}}{3^n} = 0 f = O(g)$