

Step	Algorithm: $C = AB^T + BA^T + C$
1a	$\{C = \hat{C}$
4	$A \rightarrow \left( \begin{array}{c c} A_T & \\ \hline A_B & \end{array} \right), B \rightarrow \left( \begin{array}{c c} B_T & \\ \hline B_B & \end{array} \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$ where $A_T$ has 0 rows, $B_T$ has 0 rows, $C_{TL}$ is $0 \times 0$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
3	while $m(C_{TL}) < m(C)$ do
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge m(C_{TL}) < m(C) \right\}$
5a	Determine block size $b$ $\left( \begin{array}{c c} A_T & \\ \hline A_B & \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ \hline A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c c} B_T & \\ \hline B_B & \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ \hline B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$ where $A_1$ has $b$ rows, $B_1$ has $b$ rows, $C_{11}$ is $b \times b$
6	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ A_1 B_0^T + \hat{C}_{10} & \hat{C}_{11} & * \\ A_2 B_0^T + \hat{C}_{20} & \hat{C}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
8	$C_{11} := A_1 B_1^T + B_1 A_1^T + C_{11}$ $C_{10} := B_1 A_0^T + C_{10}$ $C_{21} := A_2 B_1^T + C_{21}$
7	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ A_1 B_0^T + B_1 A_0^T + \hat{C}_{10} & A_1 (B_1^T) + B_1 (A_1^T) + \hat{C}_{11} & * \\ A_2 B_0^T + \hat{C}_{20} & A_2 (B_1^T) + \hat{C}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
5b	$\left( \begin{array}{c c} A_T & \\ \hline A_B & \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ \hline A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c c} B_T & \\ \hline B_B & \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ \hline B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge \neg(m(C_{TL}) < m(C)) \right\}$
1b	$\{C = AB^T + BA^T + \hat{C}$

Step	Algorithm: $C = AB^T + BA^T + C$
1a	{
4	
	where
2	{
3	while do
2,3	{
	Determine block size $b$
5a	
	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{
1b	{

Step	Algorithm: $C = AB^T + BA^T + C$
1a	{ $C = \hat{C}$ }
4	where
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2,3	{ $\wedge$ }
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6	{
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7	{
5b	
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	endwhile
2,3	{ $\wedge \neg($ ) }
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2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_TB_T^T + B_TA_T^T + \widehat{C}_{TL} & * \\ \hline A_BB_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
3	while do
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	where
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2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_TB_T^T + B_TA_T^T + \widehat{C}_{TL} & * \\ \hline A_BB_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
	endwhile
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2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_TB_T^T + B_TA_T^T + \hat{C}_{TL} & * \\ \hline A_BB_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
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5b	$\left( \begin{array}{c c} A_T & \\ \hline A_B & \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ \hline A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c c} B_T & \\ \hline B_B & \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ \hline B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$
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2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline A_B B_T^T + \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge \neg(m(C_{TL}) < m(C)) \right\}$
1b	$\{C = AB^T + BA^T + \hat{C}$

Step	Algorithm: $C = AB^T + BA^T + C$
1a	$\{C = \widehat{C}$
4	$A \rightarrow \left( \begin{array}{c} A_T \\ A_B \end{array} \right), B \rightarrow \left( \begin{array}{c} B_T \\ B_B \end{array} \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$ where $A_T$ has 0 rows, $B_T$ has 0 rows, $C_{TL}$ is $0 \times 0$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \widehat{C}_{TL} & * \\ \hline A_B B_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
3	while $m(C_{TL}) < m(C)$ do
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \widehat{C}_{TL} & * \\ \hline A_B B_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \wedge m(C_{TL}) < m(C) \right\}$
5a	Determine block size $b$ $\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$ where $A_1$ has $b$ rows, $B_1$ has $b$ rows, $C_{11}$ is $b \times b$
6	$\left\{ \begin{pmatrix} C_{00} & * & * \\ C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{pmatrix} = \begin{pmatrix} A_0 B_0^T + B_0 A_0^T + \widehat{C}_{00} & * & * \\ A_1 B_0^T + \widehat{C}_{10} & \widehat{C}_{11} & * \\ A_2 B_0^T + \widehat{C}_{20} & \widehat{C}_{21} & \widehat{C}_{22} \end{pmatrix} \right\}$
8	$C_{11} := A_1 B_1^T + B_1 A_1^T + C_{11}$ $C_{10} := B_1 A_0^T + C_{10}$ $C_{21} := A_2 B_1^T + C_{21}$
7	$\left\{ \begin{pmatrix} C_{00} & * & * \\ C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{pmatrix} = \begin{pmatrix} A_0 B_0^T + B_0 A_0^T + \widehat{C}_{00} & * & * \\ A_1 B_0^T + B_1 A_0^T + \widehat{C}_{10} & A_1 (B_1^T) + B_1 (A_1^T) + \widehat{C}_{11} & * \\ A_2 B_0^T + \widehat{C}_{20} & A_2 (B_1^T) + \widehat{C}_{21} & \widehat{C}_{22} \end{pmatrix} \right\}$
5b	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \widehat{C}_{TL} & * \\ \hline A_B B_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \widehat{C}_{TL} & * \\ \hline A_B B_T^T + \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \wedge \neg(m(C_{TL}) < m(C)) \right\}$
1b	$\{C = AB^T + BA^T + \widehat{C}$

	Algorithm: $C = AB^T + BA^T + C$
	$A \rightarrow \left( \begin{array}{c} A_T \\ A_B \end{array} \right), B \rightarrow \left( \begin{array}{c} B_T \\ B_B \end{array} \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$ <p>where <math>A_T</math> has 0 rows, <math>B_T</math> has 0 rows, <math>C_{TL}</math> is <math>0 \times 0</math></p>
	while $m(C_{TL}) < m(C)$ do
	<p><b>Determine block size <math>b</math></b></p> $\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$ <p>where <math>A_1</math> has <math>b</math> rows, <math>B_1</math> has <math>b</math> rows, <math>C_{11}</math> is <math>b \times b</math></p>
	$C_{11} := A_1 B_1^T + B_1 A_1^T + C_{11}$ $C_{10} := B_1 A_0^T + C_{10}$ $C_{21} := A_2 B_1^T + C_{21}$
	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ A_1 \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ B_1 \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$
	endwhile

**Algorithm:**  $C = AB^T + BA^T + C$

$$A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}, B \rightarrow \begin{pmatrix} B_T \\ B_B \end{pmatrix}, C \rightarrow \left( \begin{array}{c|c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$$

**where**  $A_T$  has 0 rows,  $B_T$  has 0 rows,  $C_{TL}$  is  $0 \times 0$

**while**  $m(C_{TL}) < m(C)$  **do**

**Determine block size**  $b$

$$\begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ A_1 \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \rightarrow \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix}, \left( \begin{array}{c|c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|cc} C_{00} & * & * \\ \hline C_{10} & C_{11} & * \\ C_{20} & C_{21} & C_{22} \end{array} \right)$$

**where**  $A_1$  has  $b$  rows,  $B_1$  has  $b$  rows,  $C_{11}$  is  $b \times b$

$$C_{11} := A_1 B_1^T + B_1 A_1^T + C_{11}$$

$$C_{10} := B_1 A_0^T + C_{10}$$

$$C_{21} := A_2 B_1^T + C_{21}$$

$$\begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ A_1 \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix}, \left( \begin{array}{c|c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{cc|c} C_{00} & * & * \\ C_{10} & C_{11} & * \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$$

**endwhile**