

Step	Algorithm: $C = AB^T + BA^T + \hat{C}$
1a	$\{C = \hat{C}$ }
4	$A \rightarrow \left( \begin{array}{c c} A_T & \\ \hline & A_B \end{array} \right), B \rightarrow \left( \begin{array}{c c} B_T & \\ \hline & B_B \end{array} \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$ where $A_T$ has 0 rows, $B_T$ has 0 rows, $C_{TL}$ is $0 \times 0$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
3	while $m(C_{TL}) < m(C)$ do
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge m(C_{TL}) < m(C) \right\}$
5a	$\left( \begin{array}{c c} A_T & \\ \hline & A_B \end{array} \right) \rightarrow \left( \begin{array}{c c} A_0 & \\ \hline a_1^T & A_2 \end{array} \right), \left( \begin{array}{c c} B_T & \\ \hline & B_B \end{array} \right) \rightarrow \left( \begin{array}{c c} B_0 & \\ \hline b_1^T & B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$ where $a_1$ has 1 row, $b_1$ has 1 row, $\gamma_{11}$ is $1 \times 1$
6	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ \hat{c}_{10}^T & \hat{\gamma}_{11} & * \\ \hat{C}_{20} & \hat{c}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
8	$\gamma_{11} = a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \gamma_{11}$ $c_{10}^T = a_1 B_0^T + b_1^T A_0^T + c_{10}^T$
7	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ a_1 B_0^T + b_1^T A_0^T + \hat{c}_{10}^T & a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \hat{\gamma}_{11} & * \\ \hat{C}_{20} & \hat{c}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
5b	$\left( \begin{array}{c c} A_T & \\ \hline & A_B \end{array} \right) \leftarrow \left( \begin{array}{c c} A_0 & \\ \hline a_1^T & A_2 \end{array} \right), \left( \begin{array}{c c} B_T & \\ \hline & B_B \end{array} \right) \leftarrow \left( \begin{array}{c c} B_0 & \\ \hline b_1^T & B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge \neg(m(C_{TL}) < m(C)) \right\}$
1b	$\{C = AB^T + BA^T + \hat{C}$ }

Step	Algorithm: $C = AB^T + BA^T + \widehat{C}$
1a	{
4	where
2	{
3	while do
2,3	{ $\wedge$ }
5a	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{ $\wedge \neg($ ) }
1b	}

Step	Algorithm: $C = AB^T + BA^T + \widehat{C}$
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	endwhile
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Step	Algorithm: $C = AB^T + BA^T + \hat{C}$
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	where
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_TB_T^T + B_TA_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
3	while do
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_TB_T^T + B_TA_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge \right\}$
5a	
	where
6	$\left\{ \right\}$
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	endwhile
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3	while $m(C_{TL}) < m(C)$ do
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2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
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5a	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$ where $a_1$ has 1 row, $b_1$ has 1 row, $\gamma_{11}$ is $1 \times 1$
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6	$\left\{ \begin{pmatrix} C_{00} & * & * \\ c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{pmatrix} = \begin{pmatrix} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ \hat{c}_{10}^T & \hat{\gamma}_{11} & * \\ \hat{C}_{20} & \hat{c}_{21} & \hat{C}_{22} \end{pmatrix} \right\}$
8	
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5b	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$
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5b	$\begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ b_1^T \\ B_2 \end{pmatrix}, \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$
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3	while $m(C_{TL}) < m(C)$ do
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge m(C_{TL}) < m(C) \right\}$
5a	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$ where $a_1$ has 1 row, $b_1$ has 1 row, $\gamma_{11}$ is $1 \times 1$
6	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ \hat{c}_{10}^T & \hat{\gamma}_{11} & * \\ \hat{C}_{20} & \hat{c}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
8	$\gamma_{11} = a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \gamma_{11}$ $c_{10}^T = a_1 B_0^T + b_1^T A_0^T + c_{10}^T$
7	$\left\{ \left( \begin{array}{ccc} C_{00} & * & * \\ c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right) = \left( \begin{array}{ccc} A_0 B_0^T + B_0 A_0^T + \hat{C}_{00} & * & * \\ a_1 B_0^T + b_1^T A_0^T + \hat{c}_{10}^T & a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \hat{\gamma}_{11} & * \\ \hat{C}_{20} & \hat{c}_{21} & \hat{C}_{22} \end{array} \right) \right\}$
5b	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ C_{20} & c_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} A_T B_T^T + B_T A_T^T + \hat{C}_{TL} & * \\ \hline \hat{C}_{BL} & \hat{C}_{BR} \end{array} \right) \wedge \neg(m(C_{TL}) < m(C)) \right\}$
1b	$\{C = AB^T + BA^T + \hat{C}\}$

	Algorithm: $C = AB^T + BA^T + \hat{C}$
	$A \rightarrow \left( \begin{array}{c} A_T \\ A_B \end{array} \right), B \rightarrow \left( \begin{array}{c} B_T \\ B_B \end{array} \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$ <p>where <math>A_T</math> has 0 rows, <math>B_T</math> has 0 rows, <math>C_{TL}</math> is <math>0 \times 0</math></p>
	while $m(C_{TL}) < m(C)$ do
	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ \hline C_{20} & c_{21} & C_{22} \end{array} \right)$ <p>where <math>a_1</math> has 1 row, <math>b_1</math> has 1 row, <math>\gamma_{11}</math> is <math>1 \times 1</math></p>
	$\gamma_{11} = a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \gamma_{11}$ $c_{10}^T = a_1 B_0^T + b_1^T A_0^T + c_{10}^T$
	$\left( \begin{array}{c} A_T \\ A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ a_1^T \\ A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ b_1^T \\ B_2 \end{array} \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ \hline C_{20} & c_{21} & C_{22} \end{array} \right)$
	endwhile

**Algorithm:**  $C = AB^T + BA^T + \widehat{C}$

$$A \rightarrow \left( \begin{array}{c} A_T \\ \hline A_B \end{array} \right), B \rightarrow \left( \begin{array}{c} B_T \\ \hline B_B \end{array} \right), C \rightarrow \left( \begin{array}{c|c} C_{TL} & * \\ \hline C_{BL} & C_{BR} \end{array} \right)$$

**where**  $A_T$  has 0 rows,  $B_T$  has 0 rows,  $C_{TL}$  is  $0 \times 0$

**while**  $m(C_{TL}) < m(C)$  **do**

$$\left( \begin{array}{c} A_T \\ \hline A_B \end{array} \right) \rightarrow \left( \begin{array}{c} A_0 \\ \hline a_1^T \\ \hline A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left( \begin{array}{c} B_0 \\ \hline b_1^T \\ \hline B_2 \end{array} \right), \left( \begin{array}{c|c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ \hline C_{20} & c_{21} & C_{22} \end{array} \right)$$

**where**  $a_1$  has 1 row,  $b_1$  has 1 row,  $\gamma_{11}$  is  $1 \times 1$

$$\gamma_{11} = a_1^T (b_1^T)^T + b_1^T (a_1^T)^T + \gamma_{11}$$

$$c_{10}^T = a_1 B_0^T + b_1^T A_0^T + c_{10}^T$$

$$\left( \begin{array}{c} A_T \\ \hline A_B \end{array} \right) \leftarrow \left( \begin{array}{c} A_0 \\ \hline a_1^T \\ \hline A_2 \end{array} \right), \left( \begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left( \begin{array}{c} B_0 \\ \hline b_1^T \\ \hline B_2 \end{array} \right), \left( \begin{array}{c|c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|cc} C_{00} & * & * \\ \hline c_{10}^T & \gamma_{11} & * \\ \hline C_{20} & c_{21} & C_{22} \end{array} \right)$$

**endwhile**