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(*
                              CS51 Lab 4
                Error Handling, Options, and Exceptions
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Readings:

    This lab builds on material from Chapter 10 of the textbook
    <http://book.cs51.io>, which should be read before the lab session.

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Part 1: Option types and exceptions

In Lab 2, you implemented a function `max_list` that returns the maximum
element in a non-empty integer list. Here's a possible implementation
for `max_list`:

    let rec max_list (lst : int list) : int =
      match lst with
      | [elt] -> elt
      | head :: tail -> max head (max_list tail) ;;

(This implementation makes use of the polymorphic `max` function from
the `Stdlib` module.)

As written, this function generates a warning that the match is not
exhaustive. Why? What's an example of the missing case? Try entering
the function in `ocaml` or `utop` and see what information you can
glean from the warning message. Go ahead; we'll wait.

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The problem is that *there is no reasonable value for the maximum
element in an empty list*. This is an ideal application for option
types.

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Exercise 1:

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Reimplement `max_list`, but this time, it should return an `int option`
instead of an `int`. Call it `max_list_opt`. The `None` return value
should be used when called on an empty list.

(Using the suffix `_opt` is a standard convention in OCaml for
functions that return an option type for this purpose. See, for
instance, the functions `nth` and `nth_opt` in the `List` module.)
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let max_list_opt (lst : int list) : int option =
  failwith "max_list_opt not implemented" ;;

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Exercise 2: Alternatively, we could have `max_list` raise an exception
upon discovering the error condition. Reimplement `max_list` so that it
does so. What exception should it raise? (See Section 10.3 in the
textbook for some advice.)
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let max_list (lst : int list) : int =
  failwith "max_list not implemented" ;;

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Exercise 3: Write a function `min_option` to return the smaller of its
two `int option` arguments, or `None` if both are `None`. If exactly one
argument is `None`, return the other. The built-in function `min` from
the Stdlib module may be useful. You'll want to make sure that all
possible cases are handled; no nonexhaustive match warnings!
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let min_option (x : int option) (y : int option) : int option =
  failwith "min_option not implemented" ;;

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Exercise 4: Write a function `plus_option` to return the sum of its two
`int option` arguments, or `None` if both are `None`. If exactly one
argument is `None`, return the other.
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let plus_option (x : int option) (y : int option) : int option =
  failwith "plus_option not implemented" ;;

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Part 2: Polymorphism practice

Do you see a pattern in your implementations of
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`min_option` and `plus_option`? How can we factor out similar code?

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Exercise 5: Write a polymorphic higher-order function `lift_option` to
"lift" binary operations to operate on option type values, taking
three arguments in order: the binary operation (a curried function)
and its first and second arguments as option types. If both arguments
are `None`, return `None`.  If one argument is `None`, the function
should return the other argument. If neither argument is `None`, the
binary operation should be applied to the argument values and the
result appropriately returned.

What is the type signature for `lift_option`? (If you're having
trouble figuring that out, call over a staff member, or check our
intended type at <https://url.cs51.io/lab4-1>.)

Now implement `lift_option`.
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let lift_option =
  fun _ -> failwith "lift_option not implemented" ;;

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Exercise 6: Now rewrite `min_option` and `plus_option` using the
higher-order function `lift_option`. Call them `min_option_2` and
`plus_option_2`.

    Note: You might encounter inexplicable "weak type variable"
    warnings. If you do, you should make sure to type the arguments of
    the function. For more information read the detailed explanation
    in the lab's solution comments or Section 9.6 of the textbook.
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let min_option_2 =
  fun _ -> failwith "min_option_2 not implemented" ;;

let plus_option_2 =
  fun _ -> failwith "plus_option_2 not implemented" ;;

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Exercise 7: Now that we have `lift_option`, we can use it in other
ways. Because `lift_option` is polymorphic, it can work on things other
than `int option`s. Define a function `and_option` to return the boolean
AND of two `bool option`s, or `None` if both are `None`. If exactly one
is `None`, return the other.
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137
138 let and_option =
139   fun _ -> failwith "and_option not implemented" ;;
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142 Exercise 8: In Lab 3, you implemented a polymorphic function `zip` that
143 takes two lists and "zips" them together into a list of pairs. Here's
144 a possible implementation of `zip`:
145
146     let rec zip (x : 'a list) (y : 'b list) : ('a * 'b) list =
147       match x, y with
148       | [], [] -> []
149       | xhd :: xtl, yhd :: ytl -> (xhd, yhd) :: (zip xtl ytl) ;;
150
151 A problem with this implementation of `zip` is that, once again, its
152 match is not exhaustive and it raises an exception when given lists of
153 unequal length. How can you use option types to generate an alternate
154 solution without this property?
155
156 Do so below in a new definition of `zip` -- called `zip_opt` to make
157 clear that its signature has changed -- which returns an appropriate
158 option type in case it is called with lists of unequal length. Here
159 are some examples:
160
161     # zip_opt [1; 2] [true; false] ;;
162     - : (int * bool) list option = Some [(1, true); (2, false)]
163     # zip_opt [1; 2] [true; false; true] ;;
164     - : (int * bool) list option = None
165 .....................................................................*)
166
167 let zip_opt =
168   fun _ -> failwith "zip_opt not implemented" ;;
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170 (*======================================================================
171 Part 3: Factoring out None-handling
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173 Recall the definition of `dotprod` from Lab 2. Here it is, adjusted to
174 an option type:
175
176     let dotprod_opt (a : int list) (b : int list) : int option =
177       let pairsopt = zip_opt a b in
178       match pairsopt with
179       | None -> None
180       | Some pairs -> Some (sum (prods pairs)) ;;
181
182 It uses `zip_opt` from Exercise 8, `prods` from Lab 3, and a function
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`sum` to sum up all the integers in a list. The `sum` function is
simply *)

let sum : int list -> int =
  List.fold_left (+) 0 ;;

(* and a version of `prods` is *)

let prods =
  List.map (fun (x, y) -> x * y) ;;

(* Notice how in `dotprod_opt` and other option-manipulating functions
we frequently and annoyingly have to test if a value of option type is
`None`; this requires a separate match, and passing on the `None`
value in the "bad" branch and introducing a `Some` in the "good"
branch. This is something we're likely to be doing a lot of. Let's
factor that out to simplify the implementation.

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Exercise 9: Define a function called `maybe` that takes a first
argument, function of type `'arg -> 'result`, and a second argument,
of type `'arg option`, and "maybe" applies the first (the function) to
the second (the argument), depending on whether its argument is a
`None` or a `Some`. The `maybe` function either passes on the `None`
if its second argument is `None`, or if its second argument is `Some
v`, it applies its first argument to that `v` and returns the result,
appropriately adjusted for the result type.

What should the type of the `maybe` function be?

Now implement the `maybe` function.
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let maybe (f : 'arg -> 'result) (x : 'arg option) : 'result option =
  failwith "maybe not implemented" ;;

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Exercise 10: Now reimplement `dotprod_opt` to use the `maybe`
function. (The previous implementation makes use of functions `sum`
and `prods`, which we've provided for you above.)  Your new solution
for `dotprod` should be much simpler than the version we provided
above at the top of Part 3.
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let dotprod_opt (a : int list) (b : int list) : int option =
  failwith "dotprod_opt not implemented" ;;
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231 Exercise 11: Reimplement `zip_opt` using the `maybe` function, as
232 `zip_opt_2` below.
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234
235 let rec zip_opt_2 (x : 'a list) (y : 'b list) : (('a * 'b) list) option =
236   failwith "zip_opt_2 not implemented" ;;
237
238 (*.....................................................................
239 Exercise 12: [Optional] For the energetic, reimplement `max_list_opt`
240 as `max_list_opt_2` along the same lines. There's likely to be a
241 subtle issue here, since the `maybe` function always passes along the
242 `None`.
243 .....................................................................*)
244
245 let rec max_list_opt_2 (lst : int list) : int option =
246   failwith "max_list_opt_2 not implemented" ;;
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