

Recursion and Iteration

Many linked list processing functions can be written both iteratively and recursively

Recursive approach:

- What recursive call do you make?
- What does this recursive call do/return?
- How is this result useful in solving the problem?

```
def length(s):
    """The number of elements in s.
    >>> length(Link(3, Link(4, Link(5))))
    3
    """
    if s is Link.empty:
        return 0
    else:
        return 1 + length(s.rest)
```

Iterative approach:

- Describe a process that solves the problem.
- Figure out what additional names you need to carry out this process.
- Implement the process using those names.

```
def length(s):
    """The number of elements in s.

>>> length(Link(3, Link(4, Link(5))))
3
"""

k = 0
while s is not Link.empty:
    s, k = s.rest, k + 1
return k
```

Constructing a Linked List

Build the rest of the linked list, then combine it with the first element.

```
3 4 5
```

```
s = Link.empty
s = Link(5, s)
s = Link(4, s)
s = Link(3, s)
```

```
def range_link(start, end):
    """Return a Link containing consecutive
    integers from start up to end.

>>> range_link(3, 6)
    Link(3, Link(4, Link(5)))
    """

if start >= end:
    return Link.empty

else:
    return _Link(start, range_link(start + 1, end))
```

```
def range_link(start, end):
    """Return a Link containing consecutive
    integers from start to end.

>>> range_link(3, 6)
    Link(3, Link(4, Link(5)))
    """

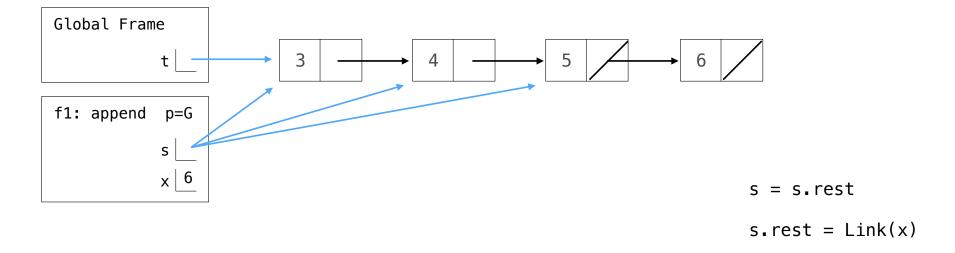
s = Link.empty
    k = end - 1
    while k >= start:
        s = Link(k, s)
        k -= 1
    return s
```

Linked List Mutation

To change the contents of a linked list, assign to first and rest attributes

Example: Append x to the end of non-empty s

```
>>> t = Link(3, Link(4, Link(5)))
>>> append(t, 6)
>>> t
Link(3, Link(4, Link(5, Link(6))))
```



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Recursion and Iteration

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Recursive approach:

- What recursive call do you make?
- What does this recursive call do/return?
- How is this result useful in solving the problem?

```
def append(s, x):
    """Append x to the end of non-empty s.
    >>> append(s, 6) # returns None!
    >>> print(s)
    <3 4 5 6>
    """
    if __s.rest is not Link.empty :
        append(_s.rest_, _x__)
    else:
        s.rest = Link(x)
```

Iterative approach:

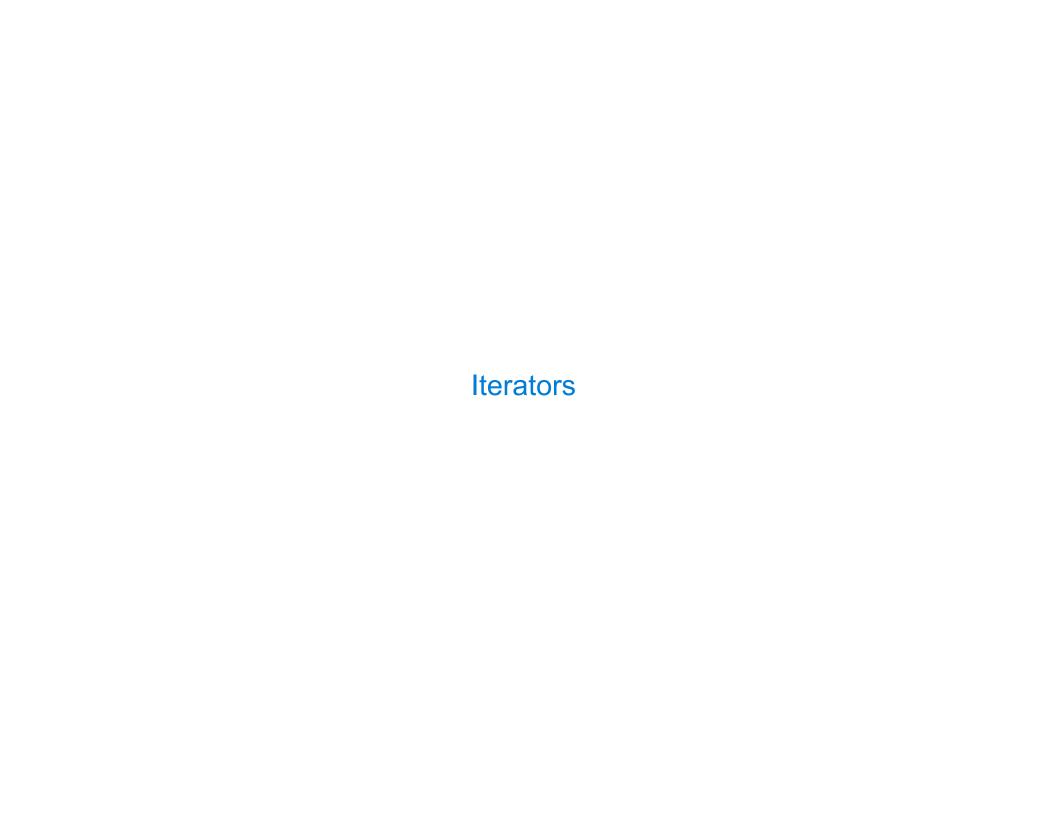
- Describe a process that solves the problem.
- Figure out what additional names you need to carry out this process.
- Implement the process using those names.

Example: Pop

Implement pop, which takes a linked list s and positive integer i. It removes and returns the element at index i of s (assuming s.first has index 0).

```
def pop(s, i):
    """Remove and return element i from linked list s for positive i.
    >>> t = Link(3, Link(4, Link(5, Link(6))))
    >>> pop(t, 2)
    >>> pop(t, 2)
                                          Global Frame
    >>> pop(t, 1)
    4
                                                  t
                                                              3
    >>> t
    Link(3)
                                          f1: pop p=G
    assert i > 0 and i < length(s)
                                                  S
    for x in range(^{i} - ^{1}):
        s = s_rest
                                             result
    result = s.rest.first
    s.rest = s.rest.rest
    return _ result
```

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Iterators

A container can provide an iterator that provides access to its elements in order

```
>>> s = [3, 4, 5
>>> t = iter(s)
>>> next(t)
3
>>> next(t)
4
>>> u = iter(s)
>>> next(u)
3
>>> next(t)
5
>>> next(u)
```

(Demo)

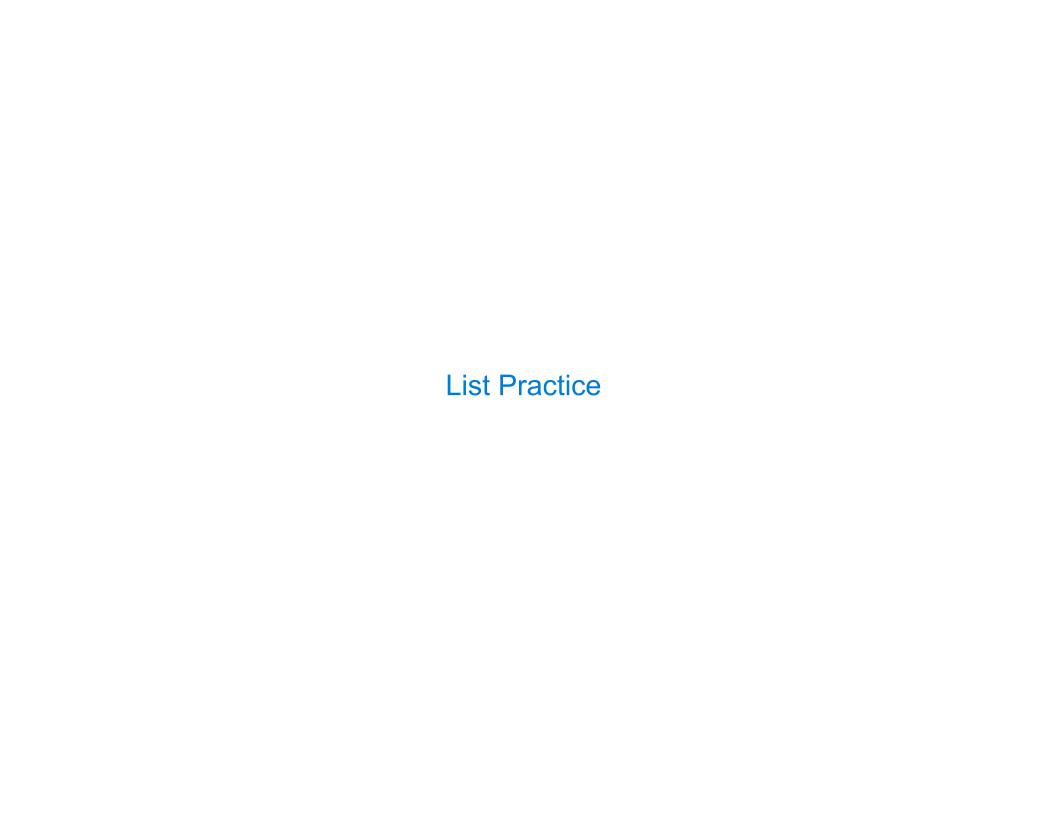
Discussion Question

```
What will be printed?

a = [1, 2, 3]
b = [a, 4]
c = iter(a)
d = c
print(next(c))
print(next(d))
print(b)
```

Map Function

(Demo)



Spring 2023 Midterm 2 Question 1

```
def chain(s):
    return [s[0], s[1:]]
silver = [2, chain([3, 4, 5])]
gold = [silver[0], silver[1].pop()]
silver[0] = 1
platinum = chain(chain([6, 7, 8]))
Reminder: s.pop() removes and
returns the last item in list s.
>>> silver
[1, [3]]
>>> gold
[2, [4, 5]]
>>> platinum
[6, [[7, 8]]]
```

