CS 61A

Structure and Interpretation of Computer Programs

Spring 2023 MIDTERM 2

INSTRUCTIONS

You have 1 hour and 50 minutes to complete the exam.

- The exam is closed book, closed notes, closed computer, closed calculator, except two $8.5" \times 11"$ pages of your own creation and the provided midterm 1 and midterm 2 study guides.
- Mark your answers on the exam itself in the spaces provided. We will not grade answers written on scratch paper or outside the designated answer spaces.
- If you need to use the restroom, bring your phone and exam to the front of the room.
- You may use built-in Python functions that do not require import, such as pow, len, abs, bool, int, float, str, round, max, min, list, tuple, sum, all, any, map, filter, zip, sorted, and reversed.
- You may not use example functions defined on your study guide unless a problem clearly states you can.
- Unless otherwise specified, you are allowed to reference functions defined in previous parts of the same question.
- You may not use; to place two statements on the same line.
- You may use the Tree and Link classes defined on the midterm 2 study guide.

You can complete and submit these questions before the exam starts.

Preliminaries

(a)	What is your full name?	
(b)	What is your student ID number?	
(c)	What is your @berkeley.edu email address?	
(d)	Sign (or type) your name to confirm that all work on this exam will be your own. The penalty misconduct on an exam is an F in the course.	for academic

1. (6.0 points) What Would Python Display?

Assume the following code has been executed.

```
def chain(s):
    return [s[0], s[1:]]

silver = [2, chain([3, 4, 5])]
gold = [silver[0], silver[1].pop()]
silver[0] = 1
platinum = chain(chain([6, 7, 8]))
```

Write the output displayed by the interactive Python interpreter when each expression below is evaluated.

Hint: Try drawing an environment diagram!

Reminder: s.pop() removes and returns the last item in list s.

(a) (2.0 pt) silver

```
[1, [3]]
```

(b) (2.0 pt) gold

```
[2, [4, 5]]
```

(c) (2.0 pt) platinum

```
[6, [[7, 8]]]
```

2. (10.0 points) Letter Grade

(a) (4.0 points)

Implement the Letter class. A Letter has two instance attributes: contents (a str) and sent (a bool). Each Letter can only be sent once. The send method prints whether the letter was sent, and if it was, returns the reply, which is a new Letter instance with the same contents, but in all caps. *Hint*: 'hi'.upper() evaluates to 'HI'.

```
class Letter:
```

```
"""A letter receives an all-caps reply when sent successfully.
```

```
>>> hi = Letter('Hello, World!')
>>> hi.send()
Hello, World! has been sent.
HELLO, WORLD!
>>> hi.send()
Hello, World! was already sent.
>>> Letter('Hey').send().send()
Hey has been sent.
HEY has been sent.
HEY
11 11 11
def __init__(self, contents):
    self.contents = contents
       (a)
def send(self):
    if self.sent:
        print(self, 'was already sent.')
    else:
        print(self, 'has been sent.')
           (b)
        return _____
                  (c)
def __repr__(self):
    # Note: since no __str__ method is defined, the repr and str strings are the same.
    return self.contents
```

i. (1.0 pt) Fill in blank (a).

```
self.sent = False
```

ii. (1.0 pt) Fill in blank (b)

```
self.sent = True
```

iii. (2.0 pt) Fill in blank (c)

```
Letter(self.contents.upper())
```

(b) (6.0 points)

Implement the Numbered class. A Numbered letter has a number attribute equal to how many numbered letters have previously been constructed. This number appears in its repr string. Assume Letter is implemented correctly.

```
class Numbered(Letter):
```

```
"""A numbered letter has a different repr method that shows its number.
```

```
>>> hey = Numbered('Hello, World!')
>>> hey.send()
#0 has been sent.
HELLO, WORLD!
>>> Numbered('Hi!').send()
#1 has been sent.
HI!
>>> hey
#0
11 11 11
number = 0
def __init__(self, contents):
    super().__init__(contents)
       (d)
       (e)
def __repr__(self):
    return '#' + _____
```

- i. (2.0 pt) Fill in blank (d).
 - Numbered.number = 0
 - Numbered.number = number
 - Numbered.number = self.number
 - self.number = 0
 - self.number = number
 - self.number = Numbered.number
- ii. (2.0 pt) Fill in blank (e).

```
Numbered.number += 1
```

iii. (2.0 pt) Fill in blank (f).

```
str(self.number)
```

3. (9.0 points) Prefixes

Definition. A prefix sum of a sequence of numbers is the sum of the first n elements for some positive length n.

(a) (4.0 points)

Implement prefix, which takes a list of numbers s and returns a list of the prefix sums of s in increasing order of the length of the prefix.

i. (2.0 pt) Fill in blank (a).

```
sum(s[:k+1])
```

- ii. (1.0 pt) Fill in blank (b).
 - () s
 - (s)
 - Os[1:]
 - range(s)
 - range(len(s))
- iii. (1.0 pt) What is the order of growth of the time to run this alternate implentation in terms of the length of s?

 Assume that the append method of a list takes just 1 step (constant time).

- Logarithmic
- Linear
- O Quadratic
- Exponential

(b) (5.0 points)

Implement tens, which takes a **non-empty** linked list of numbers s represented as a Link instance. It prints all of the prefix sums of s that are multiples of 10 in increasing order of the length of the prefix.

The Link class appears on the midterm 2 study guide.

```
def tens(s):
    """Print all prefix sums of Link s that are multiples of ten.
    >>> tens(Link(3, Link(9, Link(8, Link(10, Link(0, Link(14, Link(6))))))))
    20
    30
    30
    50
    11 11 11
    def f(suffix, total):
        if total % 10 == 0:
            print(total)
        if ____:
              (d)
               (e)
       (f)
 i. (1.0 pt) Fill in blank (d).
   s is not Link.empty
       s.rest is not Link.empty
       s.rest.rest is not Link.empty
   suffix is not Link.empty
   O suffix.rest is not Link.empty
   Suffix.rest.rest is not Link.empty
ii. (2.0 pt) Fill in blank (e).
      f(suffix.rest, total + suffix.first)
iii. (2.0 pt) Fill in blank (f).
      f(s.rest, s.first)
```

4. (10.0 points) Tree Trimming

(a) (7.0 points)

Implement exclude, which takes a Tree instance t and a value x. It returns a Tree containing the root node of t as well as each non-root node of t with a label not equal to x. The parent of a node in the result is its nearest ancestor node that is not excluded. The input t must not be modified.

The Tree class appears on the midterm 2 study guide.

```
def exclude(t, x):
    """Return a Tree with the non-root nodes of t whose labels are not equal to x.
    >>> t = Tree(1, [Tree(2, [Tree(2), Tree(3)]), Tree(4, [Tree(1)])])
    >>> exclude(t, 2)
    Tree(1, [Tree(3), Tree(4, [Tree(1)])])
    >>> t
                       # t is not changed
   Tree(1, [Tree(2, [Tree(2), Tree(3)]), Tree(4, [Tree(1)])])
    >>> exclude(t, 1) # The root node cannot be excluded
    Tree(1, [Tree(2, [Tree(2), Tree(3)]), Tree(4)])
    filtered_branches = map(lambda y: _____, t.branches)
                                         (a)
   bs = []
    for b in filtered_branches:
        if ____:
              (b)
            bs.____(___)
        else:
            bs.append(b)
    return Tree(t.label, bs)
 i. (2.0 pt) Fill in blank (a).
      exclude(y, x)
ii. (2.0 pt) Fill in blank (b).
      b.label == x
```

iii. (1.0 pt) Fill in blank (c).
○ remove
O рор
<pre>append</pre>
<pre>extend</pre>
iv. (2.0 pt) Fill in blank (d).
○ b
<pre>b.branches</pre>
<pre>O exclude(b, x)</pre>
<pre>Tree(b.label, [exclude(y, x) for y in b.branches])</pre>

(b) (3.0 points)

Implement remove, which takes a Tree instance t and a value x. It removes all non-root nodes from t that have a label equal to x, then returns t. The parent of a node in t is its nearest ancestor that is not removed. Assume that exclude is implemented correctly.

```
def remove(t, x):
    """Remove all non-root nodes labeled x from t and return t.

>>> t = Tree(1, [Tree(2, [Tree(2), Tree(3)]), Tree(4)])
>>> remove(t, 2)
Tree(1, [Tree(3), Tree(4)])
>>> remove(t, 3) # t was changed, so both 2 and 3 are now removed.
Tree(1, [Tree(4)])
    """

------
    (e)

return t

i. (3.0 pt) Fill in blank (e).

t.branches = exclude(t, x).branches
```

5. (10.0 points) Parking

Definition. When parking vehicles in a row, a *motorcycle* takes up 1 parking spot and a *car* takes up 2 adjacent parking spots. A string of length n can represent n adjacent parking spots using % for a motorcycle, <> for a car, and . for an empty spot. For example '.%%.<>>' represents an empty spot, then two spots containing motorcycles, then another empty spot, then four spots containing two cars.

Thanks to the Berkeley Math Circle for introducing this question.

(a) (4.0 points)

Implement count_park, which returns the number of ways that vehicles can be parked in n adjacent parking spots for positive integer n. Some or all spots can be empty.

```
def count_park(n):
    """Count the ways to park cars and motorcycles in n adjacent spots.
    >>> count_park(1) # '.' or '%'
    >>> count_park(2) # '..', '.%', '%.', '%%', or '<>'
    >>> count_park(4) # some examples: '<><>', '.\%\.', '\%<>\'', '\%.<>'
    29
    11 11 11
    if n < 0:
        return 0
    if n == 0:
        return ____
                   (a)
    return _____
              (b)
 i. (1.0 pt) Fill in blank (a).
      1
```

ii. (3.0 pt) Fill in blank (b).

```
2 * count_park(n-1) + count_park(n-2)
```

(b) (6.0 points)

Implement park, a generator function that takes a non-negative integer n. It yields (in any order) all possible strings representing n adjacent parking spots.

```
def park(n):
```

"""Yield the ways to park cars and motorcycles in n adjacent spots.

```
>>> sorted(park(1))
['%', '.']
>>> sorted(park(2))
['\\\', '\\.', '.\\', '...', '<>']
>>> sorted(park(3))
['%%%', '%%.', '%.%', '%..', '%<>', '.%%', '.%.', '..%', '...', '...', '.<>', '<>.']
>>> len(list(park(4)))
29
11 11 11
if n == 0:
    yield ''
elif n > 0:
    for s in park(n-1):
        -----
           (c)
           (d)
    for s in _____:
                (e)
           (f)
```

i. (3.0 pt) Fill in blanks (c) and (d) with two lines of code. You may not use yield from.

```
yield s + '.'
yield s + '%'
```

ii. (1.0 pt) Fill in blank (e).

```
park(n-2)
```

iii. (2.0 pt) Fill in blank (f).

```
yield s + '<>'
```

(c) This A+ question is not worth any points. It can only affect your course grade if you have a high A and might receive an A+. Finish the rest of the exam first!

Implement pack, a generator function that takes a non-negative integer n. It yields (in any order) all possible strings representing n adjacent parking spots in which an equal number of cars and motorcycles are parked, no motorcycle is adjacent to a car, and no empty spot is adjacent to another empty spot.

```
def pack(n):
   """Yield the ways to park an equal number of cars and motorcycles
   in n adjacent spots with no motorcycle adjacent to a car and no
   empty spot adjacent to another empty spot.
   >>> sorted(pack(4))
   ['%.<>', '<>.%']
   >>> sorted(pack(7))
   ['%%.<><>', '<><>.%%']
   >>> sorted(pack(8))
   '.<><>.\%', '<>.\%', '<>.\%', '<>.\%', '<><>.\%'
   def f(n, k):
       if n == 0 and k == 0:
          yield ''
       elif n > 0:
          yield from g(n-1, k-1, '<', '%')
          yield from g(n-1, k, '.', '.')
          yield from g(n-2, k+1, '%', '<>')
   def g(n, k, no, yes):
       yield from _____
   yield from f(n, 0)
```

i. Fill in the blank.

```
[yes + s for s in f(n, k) if not s or s[0] != no]
(Omitting the surrounding [] is ok and in fact more efficient.)
```