$\begin{array}{c} \mathrm{DATA} \ \mathrm{C88C} \\ \mathrm{Spring} \ 2025 \end{array}$

Final Review

Discussion 12: April 29, 2025

HOF_s

Q1: Make Repeater

Implement the function make_repeater so that make_repeater(f, n)(x) returns f(f(...f(x)...)), where f is applied n times. That is, make_repeater(f, n) returns another function that can then be applied to another argument. For example, make_repeater(square, 3)(42) evaluates to square(square(square(42))).

```
def make_repeater(f, n):
   """Returns the function that computes the nth application of f.
   >>> add_three = make_repeater(increment, 3)
   >>> add_three(5)
   8
   >>> make_repeater(triple, 5)(1) # 3 * 3 * 3 * 3 * 3 * 1
   >>> make_repeater(square, 2)(5) # square(square(5))
   >>> make_repeater(square, 4)(5) # square(square(square(5))))
   152587890625
   >>> make_repeater(square, 0)(5) # Yes, it makes sense to apply the function zero
   times!
   0.000
   "*** YOUR CODE HERE ***"
def composer(func1, func2):
   """Returns a function f, such that f(x) = func1(func2(x))."""
   def f(x):
       return func1(func2(x))
   return f
```

Recursion

Q2: Subsequences

A subsequence of a sequence S is a subset of elements from S, in the same order they appear in S. Consider the list [1, 2, 3]. Here are a few of its subsequences [], [1, 3], [2], and [1, 2, 3].

Write a function that takes in a list and returns all possible subsequences of that list. The subsequences should be returned as a list of lists, where each nested list is a subsequence of the original input.

In order to accomplish this, you might first want to write a function insert_into_all that takes an item and a list of lists, adds the item to the beginning of each nested list, and returns the resulting list.

```
def insert_into_all(item, nested_list):
    """Return a new list consisting of all the lists in nested_list,
   but with item added to the front of each. You can assume that
   nested list is a list of lists.
   >>> nl = [[], [1, 2], [3]]
   >>> insert_into_all(0, nl)
    [[0], [0, 1, 2], [0, 3]]
   "*** YOUR CODE HERE ***"
def subseqs(s):
   """Return a nested list (a list of lists) of all subsequences of S.
   The subsequences can appear in any order. You can assume S is a list.
   >>> seqs = subseqs([1, 2, 3])
   >>> sorted(seqs)
    [[], [1], [1, 2], [1, 2, 3], [1, 3], [2], [2, 3], [3]]
   >>> subseqs([])
   [[]]
    ....
   if ____:
       _____
   else:
       _____
```

OOP

Q3: Bear

Implement the SleepyBear, and WinkingBear classes so that calling their print method matches the doctests. Use as little code as possible and try not to repeat any logic from Eye or Bear. Each blank can be filled with just two short lines.

Discussion Time: Before writing code, talk about what is different about a **SleepyBear** and a **Bear**. When using inheritance, you only need to implement the differences between the base class and subclass. Then, talk about what is different about a **WinkingBear** and a **Bear**. Can you think of a way to make the bear wink without a new implementation of **print**?

class Eye: """An eye.

```
>>> Eye().draw()
    101
    >>> print(Eye(False).draw(), Eye(True).draw())
    0 -
    def __init__(self, closed=False):
        self.closed = closed
    def draw(self):
        if self.closed:
            return '-'
        else:
            return '0'
class Bear:
    """A bear.
    >>> Bear().print()
    ? 000?
    0.00
    def __init__(self):
        self.nose_and_mouth = 'o'
    def next_eye(self):
        return Eye()
    def print(self):
        left, right = self.next_eye(), self.next_eye()
        print('? ' + left.draw() + self.nose_and_mouth + right.draw() + '?')
```

```
class SleepyBear(Bear):
   """A bear with closed eyes.
   >>> SleepyBear().print()
   ? -0-?
   0.00
   "*** YOUR CODE HERE ***"
class WinkingBear(Bear):
   """A bear whose left eye is different from its right eye.
   >>> WinkingBear().print()
   ? -00?
   def __init__(self):
        "*** YOUR CODE HERE ***"
   def next_eye(self):
        "*** YOUR CODE HERE ***"
```

Linked Lists

A linked list is a Link object or Link.empty.

You can mutate a Link object s in two ways: - Change the first element with s.first = ... - Change the rest of the elements with s.rest = ...

You can make a new Link object by calling Link: - Link(4) makes a linked list of length 1 containing 4. - Link(4, s) makes a linked list that starts with 4 followed by the elements of linked list s.

```
class Link:
   """A linked list is either a Link object or Link.empty
   >>> s = Link(3, Link(4, Link(5)))
   >>> s.rest
   Link(4, Link(5))
   >>> s.rest.rest.rest is Link.empty
   >>> s.rest.first * 2
   >>> print(s)
   <3 4 5>
   0.00
   empty = ()
   def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest
   def __repr__(self):
        if self.rest:
            rest_repr = ', ' + repr(self.rest)
        else:
            rest_repr = ''
        return 'Link(' + repr(self.first) + rest_repr + ')'
   def __str__(self):
        string = '<'
       while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'
```

Q4: Linear Sublists

Definition: A *sublist* of linked list **s** is a linked list of some of the elements of **s** in order. For example, <3 6 2 5 1 7> has sublists <3 2 1> and <6 2 7> but not <5 6 7>.

Definition: A *linear sublist* of a linked list of numbers s is a sublist in which the difference between adjacent numbers is always the same. For example <2 4 6 8> is a linear sublist of <1 2 3 4 6 9 1 8 5> because the difference between each pair of adjacent elements is 2.

Implement linear which takes a linked list of numbers s (either a Link instance or Link.empty). It returns the longest linear sublist of s. If two linear sublists are tied for the longest, return either one.

```
def linear(s):
   """Return the longest linear sublist of a linked list s.
   >>> s = Link(9, Link(4, Link(6, Link(7, Link(8, Link(10))))))
   >>> linear(s)
   Link(4, Link(6, Link(8, Link(10))))
   >>> linear(Link(4, Link(5, s)))
   Link(4, Link(5, Link(6, Link(7, Link(8)))))
   >>> linear(Link(4, Link(5, Link(4, Link(7, Link(3, Link(2, Link(8))))))))
   Link(5, Link(4, Link(3, Link(2))))
   def complete(first, rest):
        "The longest linear sublist of Link(first, rest) with difference d."
        if rest is Link.empty:
            return ____
        elif ____ == d:
            return Link(____, complete(____, ___))
        else:
            return complete(first, rest.rest)
   if s is Link.empty:
        return s
   longest = Link(s.first) # The longest linear sublist found so far
   while s is not Link.empty:
        t = s.rest
        while t is not Link.empty:
            d = t.first - s.first
            candidate = ____
            if length(candidate) > length(longest):
                longest = candidate
            t = t.rest
        s = s.rest
   return longest
def length(s):
   if s is Link.empty:
        return 0
   else:
        return 1 + length(s.rest)
```

There are three cases: - If rest is empty, return a one-element list containing just first. - If rest.first is in the linear sublist that starts with first, then build a list that contains first, and rest.first. - Otherwise, complete(first, rest.rest).

This while loop is creating a candidate linear sublist for every two possible starting values: s.first and t.first. The rest of the linear sublist must be in t.rest.

Q5: Repeated

Implement repeated, which takes in an iterator t and an integer k greater than 1. It returns the first value in t that appears k times in a row.

Important: Call **next** on t only the minimum number of times required. Assume that there is an element of t repeated at least k times in a row.

Hint: If you are receiving a StopIteration exception, your repeated function is calling next too many times.

```
def repeated(t, k):
    """Return the first value in iterator t that appears k times in a row,
   calling next on t as few times as possible.
   >>> s = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(s, 2)
   >>> t = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(t, 3)
   >>> u = iter([3, 2, 2, 2, 1, 2, 1, 4, 4, 5, 5, 5])
   >>> repeated(u, 3)
   2
   >>> repeated(u, 3)
   >>> v = iter([4, 1, 6, 6, 7, 7, 8, 8, 2, 2, 2, 5])
   >>> repeated(v, 3)
   2
   assert k > 1
    "*** YOUR CODE HERE ***"
```

Trees

Q6: Long Paths

Implement long_paths, which returns a list of all *paths* in a tree with length at least n. A path in a tree is a list of node labels that starts with the root and ends at a leaf. Each subsequent element must be from a label of a branch of the previous value's node. The *length* of a path is the number of edges in the path (i.e. one less than the number of nodes in the path). Paths are ordered in the output list from left to right in the tree. See the doctests for some examples.

```
def long_paths(t, n):
    """Return a list of all paths in t with length at least n.
    >>> long_paths(Tree(1), 0)
    [[1]]
    >>> long_paths(Tree(1), 1)
    >>> t = Tree(3, [Tree(4), Tree(4), Tree(5)])
    >>> left = Tree(1, [Tree(2), t])
    >>> mid = Tree(6, [Tree(7, [Tree(8)]), Tree(9)])
    >>> right = Tree(11, [Tree(12, [Tree(13, [Tree(14)])])])
    >>> whole = Tree(0, [left, Tree(13), mid, right])
    >>> print(whole)
    0
      1
        2
        3
          4
           4
           5
      13
      6
        7
          8
        9
      11
        12
           13
    >>> for path in long_paths(whole, 2):
             print(path)
    . . .
    [0, 1, 2]
    [0, 1, 3, 4]
    [0, 1, 3, 4]
    [0, 1, 3, 5]
    [0, 6, 7, 8]
    [0, 6, 9]
    [0, 11, 12, 13, 14]
    >>> for path in long_paths(whole, 3):
            print(path)
    . . .
    [0, 1, 3, 4]
    [0, 1, 3, 4]
    [0, 1, 3, 5]
    [0, 6, 7, 8]
    [0, 11, 12, 13, 14]
    >>> long_paths(whole, 4)
Note: This worksheet is a problem table most TAs will not cover all the problems in discussion section.
    "*** YOUR CODE HERE ***"
```

Document the Occasion

Please all fill out the attendance form (one submission per person per week).