

$e$	$:=$	$n \mid \text{true} \mid \text{false}$	$n$	$:=$	number literals
		$\mid (\text{let } (x \ e) \ e)$	$x$	$:=$	variable names
		$\mid (+ \ e \ e) \mid (< \ e \ e)$	$\tau$	$:=$	$\text{Num} \mid \text{Bool}$
		$\mid (\text{if } e \ e \ e)$	$\Gamma$	$:=$	$\{x : \tau, \dots\}$

TR-NUM      $n : \text{Num}$ TR-TRUE      $\text{true} : \text{Bool}$ TR-FALSE      $\text{true} : \text{Bool}$ 

TR-PLUS

 $(+ \ e_1 \ e_2) :$ 

TR-LESS

 $(< \ e_1 \ e_2) :$

$$\text{TR-ID} \frac{\boxed{\phantom{\Gamma \vdash x : \tau}}}{\Gamma \vdash x : \boxed{\phantom{\tau}}}$$

$$\text{TR-LET} \frac{\boxed{\phantom{\Gamma \vdash (\text{let } (x \ e_1) \ e_2) : \tau}}}{\Gamma \vdash (\text{let } (x \ e_1) \ e_2) : \boxed{\phantom{\tau}}}$$

$$\text{TR-IFA} \frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \Gamma \vdash e_3 : \tau_3}{\Gamma \vdash (\text{if } e_1 \ e_2 \ e_3) : \tau_1}$$

$$\text{TR-IFB} \frac{\Gamma \vdash e_1 : \text{Bool} \quad \Gamma \vdash e_2 : \tau_2 \quad \Gamma \vdash e_3 : \tau_3}{\Gamma \vdash (\text{if } e_1 \ e_2 \ e_3) : \tau_2}$$

$$\text{TR-IFC} \frac{\Gamma \vdash e_1 : \text{Bool} \quad \Gamma \vdash e_2 : \tau_2 \quad \Gamma \vdash e_3 : \tau_3}{\Gamma \vdash (\text{if } e_1 \ e_2 \ e_3) : \tau_3}$$

$$\text{TR-IFD} \frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \Gamma \vdash e_3 : \tau_3}{\Gamma \vdash (\text{if } e_1 \ e_2 \ e_3) : \tau_2}$$

TR-IFE: None of the above

$$\text{TR-SET} \frac{\Gamma \vdash e : \tau_1 \quad \Gamma[x] = \tau_2}{\Gamma \vdash (\mathbf{set} \ x \ e) : \tau_2}$$