Recursive Datatypes and Functions – Templates

```
type 'a lst<mark>√</mark>=
                                             type 'a tree_=
  Empty
  | Link of 'a * 'a lst
                                               | Node of 'a * 'a tree * 'a tree
let rec lf (1 : 'a lst) ... : ... =
                                             let rec tf (t : 'a lst) ... : ... =
                                               match t with
  match 1 with
                                                 | Leaf | > ... base case ...
    | Empty\ -> ... base case ...
                                                 | Node(val, left, right) ->
    | Link(fst, rest) ->
                                                   ... fst\...
      ... fst\ ...
      ... (lf rest ...) ...
                                                   ... (tf\ left ...) ...
                                                   ... (tf \right ...) ...
type op = Inc | Dec
                                    let rec expr_to_instrs (e : expr) =
type expr =
                                       match e with
  | ENum of int
                                         | ENum(i) -> [sprintf "mov rax, %d" i]
  | EOp of op * expr
                                         | EOp(op, e) ->
let rec ef (e : expr) ... : ... =
                                           let arg_instrs = expr_to_instrs e in
  match e with
                                           match op with
    \mid ENum(n) -> ... base case ...
                                             | Inc -> arg_instrs @ ["add rax, 1"]
    | EOp1(op, arg) ->
                                             Dec -> arg_instrs @ ["sub rax, 1"]
      ... op \...
      ... (ef arg ...) ...
```

```
module Sexp = Sexplib.Sexp
                                                                let rec expr to instrs (e : expr) : string list =
(*
                                                                  match e with
                                                                    | ENum(i) -> [sprintf "mov rax, %d" i]
expr := <number>
     | (<op> <expr>)
                                                                     | EOp(op, e) ->
     := inc | dec
                                                                      let arg_exprs = expr_to_instrs e in
                                                                      match op with
                                                                        | Inc -> arg exprs @ ["add rax, 1"]
type op =
                                                                         Dec -> arg_exprs @ ["sub rax, 1"]
  Inc
  Dec
                                                                (* Compiles a source program string to an x86 string *)
                                                                let compile (program : string) : string =
                                                                  let ast = parse program in
type expr =
  | ENum of int
                                                                  let instrs = expr_to_instrs ast in
  | EOp of op * expr
                                                                  let instrs_str = (String.concat "\n" instrs) in
                                                                  sprintf "
let rec sexp_to_expr (se : Sexp.t) : expr =
                                                                section .text
                                                                global our_code_starts_here
  match se with
     Atom(s) -> ENum(int of string s)
                                                                our code starts here:
     List(sexps) ->
                                                                  ret\n" instrs_str;;
      match sexps with
        [Atom("inc"); arg] -> EOp(Inc, sexp_to_expr arg)
          [Atom("dec"); arg] -> EOp(Dec, sexp_to_expr arg)
                                                                let () =
        _ -> failwith "Parse error"
                                                                  let input file = (open in (Sys.argv.(1))) in
                                                                  let input_program = (input_line input_file) in
let parse (s : string) : expr =
                                                                  let program = (compile input program) in
                                                                  printf "%s\n" program;;
  sexp_to_expr (Sexp.of_string s)
  "(inc (dec 4))" EOp(Inc, EOp(Dec, ENum(4)))
open Sexplib.Sexp
                                                            (*
module Sexp = Sexplib.Sexp
                                                            expr := <number>
type op =
                                                                  (<op> <expr>)
                                                                    (let (<name> <expr>) <expr>)
   Inc
  Dec
                                                                    <name>
type expr =
                                                                 := inc | dec
                                                            op
   ENum of int
   EOp of op * expr
  (* Add the cases for ELet and EId! *)
                                                            open Printf
                                                            (* FILL the ELet case and anything else for the header! *)
let rec sexp_to_expr (se : Sexp.t) : expr =
                                                            let rec expr_to_instrs
  match se with
    | Atom(s) ->
                                                              match e with
    | List(sexps) ->
      match sexps with
        | [Atom("inc"); arg] -> EOp(Inc, sexp_to_expr arg)
                                                                | ENum(i) -> [sprintf "mov eax, %d" i]
        [Atom("dec"); arg] -> EOp(Dec, sexp_to_expr arg)
                                                                | EOp(op, e) ->
          (* Add the case for ELet! *)
                                                                  let arg_exprs = expr_to_instrs e
                                                                                                                   in
                                                                  match op with
                                                                     | Inc -> arg_exprs @ ["add rax, 1"]
                                                                     Dec -> arg_exprs @ ["sub rax, 1"]
        _ -> failwith "Parse error"
```

open Printf

open Sexplib.Sexp

 What assembly code is generated for this input program (on worksheet)?

```
(inc (dec 4))
```

- A: mov rax, 4 add rax, 1 sub rax, 1
- B: add rax, 1 sub rax, 1 mov rax, 4
- C: mov rax, 4 sub rax, 1 add rax, 1

 Which of these is a good definition for the ELet variant of the expr definition?

```
A: | ELet of expr * expr * expr
B: | ELet of string * expr
C: | ELet of string * expr * expr
D: | ELet of string * int * expr
```

Which of these correctly parses let expressions?

```
• A:
  [Atom("let"); bind; body]->
   match bind with
     [name; e] -> ELet(name, e, body)
• B:
  [Atom("let"); bind; body]->
   match bind with
      | [name; e] ->
       ELet(name, sexp_to_expr e, sexp_to_expr body)
• C:
  [Atom("let"); name; e; body]->
   ELet(name, sexp_to_expr e, sexp_to_expr body)
• D:
  [Atom("let"); Atom(name); bind; body]->
    ELet(name, sexp_to_expr e, sexp_to_expr body)
• E:
  [Atom("let"); List(bind); body]->
   match bind with
      [Atom(name); e] ->
       ELet(name, sexp_to_expr e, sexp_to_expr body)
```

 Which of these matches the grammar extended with let and identifiers?

```
A: (let x 5 x)
B: (let (x 5) x)
C: (let x 10)
D: (let 10 x 10)
E: (let 10 x)
```

• Which of these matches the grammar on the left?

```
A: (+ 1 2)
B: (inc 3 3)
C: (inc (inc 4))
D: (inc dec 3)
E: (inc x)
```