

# Writing Assignment 5

Clark Saben  
Foundations of Mathematics

March 6, 2023

**Theorem 3.10.** Suppose that  $A, B$  and  $C$  are sets. If  $A \subseteq B$  and  $B \subseteq C$  then  $A \subseteq C$ .

*Proof.* Let  $A, B$ , and  $C$  be sets. Let  $x \in A$ . Since  $A \subseteq B$  and  $x \in A$ ,  $x \in B$ . Similarly,  $B \subseteq C$  so  $x \in C$ . Therefore if  $(A \subseteq B) \cap (B \subseteq C)$  then  $A \subseteq C$ .  $\square$

---

**Theorem 3.21b.** If  $A$  and  $B$  are sets, then  $(A \cap B)^c = A^c \cup B^c$ .

*Proof.* Let  $A$  and  $B$  be sets. To show  $(A \cap B)^c = A^c \cup B^c$ , we must show that  $(A \cap B)^c \subseteq A^c \cup B^c$  and  $A^c \cup B^c \subseteq (A \cap B)^c$ . Firstly, Let  $x \in (A \cap B)^c$ . It follows that  $x \in A^c \cup B^c$  by definition 3.14. Secondly, let  $x \in A^c \cup B^c$ . It follows that  $x \in (A \cap B)^c$  by definition 3.14.  $\square$

*clearly my 3.21 edits are lacking a connection between "firstly" and "it follows" so ask jeba after class*