- 1) To model the problem input, I will use a Directed graph. I will construct this graph by using an adjacency list. My vertices will be the buckets and all the possible combinations that I can have for these. For example, if I have the two buckets, one of size 5 and one of size 3, I will have 24 vertices (6\*4, since we start counting at 0) and they will be (0,0)(0,1)(0,2)(0,3)(1,0)(1,1) so on and so forth. My edges will be the possible moves I can make at a certain vertex. Let's say for example that I am at vertex (0,0) the only moves I can make is to fill either one of these buckets, so my edges for this Vertex will be (5,0) and (0,3). My graph will be directed, unweighted, and vertex-labelled.
- 2) I will use Bread-First search as my graph algorithm

```
BFS(vector<Vertex>)
{
    Initialize sum to 0
    Initialize count to 0

    Initialize a map of integers to all 0's
    Initialize vector called moves to all 0's

For my vector of vertex's, mark all the vertices as not visited

Initialize a queue of vertices
    Mark the first vertex in my vector to visited and level to 0

Push back the first vertex into my queue

While Queue not empty
{
```

Create a new vertex called current vertex Assign queue.front to current vertex Queue.pop\_front

For int I to currents vertex size

Sum all the integers in my vertex //if I have (5,0) sum would be 5

If moves at sum is equal to the current vertexs level do nothing Else moves at sum is equal to current vertexs level

Map the index to the level

```
For int I to my currents vertexs neighbors size
{

If my neighbor has not been visited
{

My neighbors level will be its parents level+1

Mark the neighbor as visited

Push the neighbor into the queue
}

}
```

Convert the vector moves to a max heap and extract the first element

Return a vector that contains the number of moves and the amount of water that required that many moves

}