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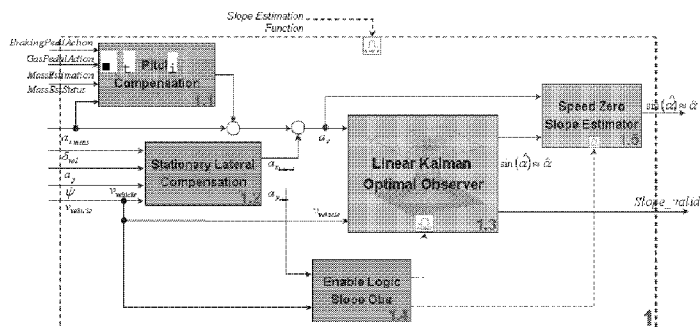
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**(54) Title:** ROAD SLOPE AND VEHICLE MASS ESTIMATION



**Fig. 1**

**(57) Abstract:** Automotive electronic control unit programmed to realtime estimate either or both of vehicle mass and road slope, wherein; a. road slope, is estimated; a1. when vehicle is considered stopped based on an accelerometer signal indicative of vehicle acceleration, wherein the vehicle is considered stopped in the presence of substantially zero values of a speed signal indicative of vehicle speed, and a2. when vehicle is in rectilinear and curvilinear motion by implementing a road slope observer based on a linear Kalman filter, which is designed to: a21. operate based on signals indicative of vehicle speed and acceleration, and a22. compensate for accelerometric disturbances due to; a221. vehicle static pitch resulting from vehicle load distribution, and a222. vehicle dynamic pitch due to acceleration to which vehicle is subjected during motion, and a223. accelerometric disturbance components due to vehicle lateral dynamics; b. vehicle mass is estimated: b1. when vehicle is in motion, and b2. based on a recursive least square algorithm with forgetting factor, and b3. based on an accelerometric signal indicative of vehicle acceleration, on a vehicle speed signal, and other signals representing a vehicle propulsive/resistive torque, and b4. at different low gears, to provide a mass estimation and an associated variance for each gear, and b5. based on mass estimations and corresponding variances for each gear, and b6. compensating for accelerometer disturbances due to: b61, vehicle dynamic pitch; and b62. accelerometric disturbance components due to vehicle lateral dynamics; and b7. minimizing uncertainties on propulsive/resistive torque due to gear efficiency and roiling resistance.

## ROAD SLOPE AND VEHICLE MASS ESTIMATION

TECHNICAL FIELD OF THE INVENTION

The present invention relates in general to real-time vehicle mass and road slope estimation. In particular, the present invention relates to the application of Kalman filter theory and recursive least squares algorithm with forgetting factor on real time vehicle mass and road grade **estimation**.

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BACKGROUND ART

In a continuous effort to improve control of longitudinal vehicle motion in very different terms it is essential to have to access on-line estimates of parameters as vehicle mass and road slope. **Then**, vehicle **parameters variation** plays an even larger role in automated control of vehicles (cars but especially light/heavy commercial vehicles, trucks, tractor & trailers, buses and so on), i.e. light **commercial** vehicles generally exhibit larger variations in parameters such as vehicle mass (**up** to 100% differences between loaded and unloaded configurations). Furthermore all main proposed fuel saving evaluation techniques are dependent on the knowledge of how the road ahead will behave, e.g. modest road grades may prove to be quite a challenge for vehicles with low **power-to-weight** ratio such as commercial vehicles, and how vehicle mass changes real-time and influences CO<sub>2</sub> emissions. These facts highlight the need for estimation of road slope and vehicle mass on a motor vehicle, in particular on Light Commercial Vehicle,

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In literature, proposed mass and slope **estimation**

approaches are model-based approaches, and this is mainly due to need to scale studied algorithms on different production vehicles with a modular re-design,

A vehicle longitudinal dynamics equation will now be formulated in general form to understand plant non-linearity and/or time variance complexity.

The equation of motion at front wheels when the driveline is fully engaged and all mechanical power from engine is passed to the wheels, has the general form:

10

$$m_{at} \cdot \ddot{x} = m \cdot g \cdot \sin(\alpha) + F_p - F_R$$

$$m_{at} = m + \frac{J_{wheels}}{R^2} + \frac{\eta \cdot J_{motor}}{R^2 \cdot \tau_i^2 \cdot \tau_d^2} \quad (1)$$

where  $m$  is total vehicle mass,  $F_p$  is propulsion force and  $F_R$  is resistance force,  $g$  is gravitational acceleration,  $\alpha$  is slope angle,  $R$  wheel is radius and  $\frac{1}{2} m_t$  is equivalent mass at propulsion wheels, so total mass with in addition inertial effects of wheels ( $J_{wheels}$ ) and motor ( $J_{motor}$ ) through gearbox and differential.

In the equation, unknowns are vehicle mass ( $m$ ) and road slope ( $\sin(\alpha)$ ), where vehicle mass, in practice a model parameter, has very slow dynamics while road slope is a 'true' real-time physical quantity with a medium slow dynamics. Seen differential equation {1} is a classic non-linear, time-variant equation. The simultaneous estimation problem requires an Extended Kalman Filter (EKF) design, but the invention's goal is to realize an integrated estimator which is simplest, enough accurate, quite robust and inexpensive under computational complexity and hardware point of view.

The **literature** presents many **algorithms** for online **estimation** of mass and slope.

**Historically**, there have been proposed estimation algorithms for either mass or slope estimation only; for example, for vehicle **mass**, algorithms linked to sharp longitudinal accelerations and decelerations which excite vehicle's mass **significantly**, thereby making this mass easier to estimate.

**For** example., US 5,482,353 proposes using sharp controlled accelerations and decelerations as part of an event-seeking mass estimation method. Similarly, US 4,548,079 proposes estimating vehicle mass specifically during the sharp accelerations and decelerations introduced by gear shifting. US 4,941,365 proposes a similar mass estimator that explicitly compensates for wheel inertia. Further extensions of the same approach are **proposed** in US 5,490,063, US 6,167,357, US 6,438,510, US 6,567,734 and US 2007/0038357, In particular, US 6,438,510 discloses estimating vehicle mass and aerodynamic drag coefficient by recursive least squares (RLS}, wherein samples of the signals of interest are buffered and their validity is assessed.

On the other hand, there have been proposed algorithms for estimation of the road slope independently from vehicle mass based on longitudinal acceleration model, for example in WO 03/40652, or based on Kalman filtering applied to same longitudinal model, for example in WO 03/016837, and further extensions of same approach for example in US 7,263,494 inferring also vehicle speed sign.

As far as simultaneous estimation of mass and slope, **Bae**, H. S., Ryu, J., and Gerdes, J, C., 2001,

"Road Grade and Vehicle Parameter Estimation for Longitudinal Control Using GPS", **Proceedings** of the IEEE **Intelligent** Transportation Systems Conference, for instance, propose a **recursive** least squares **estimator** that utilizes longitudinal force, acceleration, and **GPS-based** road grade **measurements** to **determine** vehicle mass and aerodynamic drag.

In WO 03/016837 and in Lingnan, A., and Schmidtfoauer, B., 2002, "Road **slope** and Vehicle Mass Estimation Using **Kalman** Filtering", Vehicle System Dynamics, 37, pp. 12-23, Lingman and Schmidtfoauer investigate the possibility by **Kalman** filtering to estimate slope and mass using available information on propulsion and brake system characteristics, a vehicle speed measurement and the possible improvement through the addition of a longitudinal accelerometer.

US 6,980,900 proposes again a recursive **least** squares estimator in **which** aerodynamic drag forces are simulated online and subtracted from force measurements, rather than estimated.

In Vahidi, A., Druzhinina, M., Stefanopoulou, A., and Peng, H., 2003, "Simultaneous **Mass** and Time-Varying Grade **Estimation** for **Heavy-Duty** Vehicles", Proceedings of the American Control Conference, Denver, CO, in Vahidi, A., Stefanopoulou, A., and Peng, H., 2003, "Experiments for Online Estimation of Heavy Vehicle's Mass and Time-Varying Road Grade", Proceedings of the 2003 ASME International Mechanical Engineering Congress and Exposition, and in Vahidi, A., Stefanopoulou, A., and Peng, H., 2005, "Recursive Least Squares with Forgetting for Online Estimation of Vehicle Mass and Road Grade: Theory and Experiments", Vehicle System

**Dynamics**, 41(1), pp. 31-55, **Vahidi et al.** propose a similar estimator that does not require road grade **measurements** and estimates vehicle mass, drag, and road grade simultaneously using minimal instruments. The  
 5 algorithm accomraodates the time-varying nature of aerodynamic drag and road **grade** through multi-rate forgetting .

Winstead, **V.**, and **Kolmanovsky, I.**, 2005, "Estimation of Road Grade and vehicle Mass via Model  
 10 Predictive Control", Proceedings of the IEEE Conference on Control Applications, propose an extended **Kaltnan** filter that estimates both longitudinal vehicle states and parameters (including mass) for adaptive cruise control ,

15 EP 1935733 proposes a combined estimation in two steps: road slope estimation based on vehicle speed and longitudinal acceleration., and then on this base and drive train signals vehicle mass inference.

DE 10 2005 008658 discloses estimating vehicle mass  
 20 based on engine torque and on vehicle speed and acceleration. In particular, vehicle mass is estimated based on the comparison of two different computation performed in different ways. Road slope is instead estimated based on the teaching in the above-referenced  
 25 article of **Lingman, A.** and **Schraidtbauer, B.**

**Finally**, WO 03/023334 A1 discloses simultaneously estimating vehicle mass and road slope either recursively or using an extended **Kaltnan** filter or based on an RLS approach.

30

#### OBJECT AND SUMMARY OF THE INVENTION

The Applicant has appreciated that there are

important practical needs that a real-time estimator should meet to be viable, especially for economy-priced vehicles. In particular, the Applicant has found that it should be:

- 5       \* Simple enough to run in real time despite onboard processing limitations; designed algorithms have to be implemented at the first in post-processing then in real-time environment with low memory allocation and computational complexity;
- 10       \* Accurate enough to estimate desired vehicle state/parameter in defined conditions
  - Fast enough to detect changes in a vehicle's states/parameters shortly after it is started and driven onto the road. Estimation needs to be available in
  - 15 according with the activation windows and usability range of estimated information;
  - Robust enough to operate successfully despite real signals disturbances and model plant **uncertainties**; and especially,
- 20       \* Inexpensive enough to penetrate the economy-priced vehicle market, This often translates into a minimal instrumentation requirement and no additional sensors.

With this clear point of view, the Applicant has

25 investigated the possibility of estimating road slope and vehicle mass by using vehicle information on propulsion system state, as motor torque and driveline signal states, together with ESP (Electronic Stability Program) system measures as wheel speed measurements and

30 longitudinal accelerometer available on vehicle CAN network,

The objective of present invention is therefore to

provide a real-time estimator that meets the  
aforementioned requirements .

This objective is achieved by the present invention  
in that it **relates** to a **real-time** vehicle **mass** and road  
5 slope estimator , as defined in the appended claims.

Compared to the solution disclosed in WO 03/016  
837,. where **different** estimation approaches are proposed  
to estimate road slope and vehicle **mass** in vehicle  
dynamic conditions, and where a more complete solution  
10 is disclosed, which is based on an extended, **namely** non-  
linear and **time-variant, Kalman filter**, which **is used to**  
**estimate either vehicle mass only or vehicle mass and**  
**road slope simultaneously**, in the present invention road  
slope is estimated in vehicle static and dynamic  
15 conditions and, in particular, in dynamic conditions,  
and based on a linear and time-invariant Kalman filter,  
**while** vehicle mass is estimated based on a recursive  
algorithm applied **to** a linear and time-variant model,

Compared to the **solution** disclosed US 6,438,510,. in  
20 the present invention no buffering and validity  
assessment of samples for **subsequent** processing is  
provided, rather data are directly selected and then  
only those that are believed to be valid for the  
estimate are considered. In addition, no aerodynamic  
25 drag coefficient is considered in the present invention,  
and the **RLS algorithm is applied** to engine **torque and**  
vehicle acceleration, rather than engine torque and  
vehicle speed.

Compared to the solution disclosed in DE 10 2005  
30 0086 58, in the present **invention** vehicle **mass** is  
estimated in a completely different **way, while road**  
slope is estimated based on the teaching in the above-



referenced article of **Lingman**, A, and **Schmidtbauer**, B,, but it fails to cover all **the** static and dynamic conditions **that** are instead covered by the present **invention** .

5 In the end, compared to **the** solution disclosed in WO 03/023 334, **where** simultaneously vehicle mass and slope estimation using an RL8 approach is technically unpracticable due to the difficulty in estimating quantities with so different dynamics, in the present  
10 invention the RLS algorithm is used to estimate vehicle mass only, which is estimated based also on road slope, while a linear and time-invariant **kalman** filter is used to estimate road slope.

#### 15 BRIEF DESCRIPTION OF THE DRAWINGS

\* Figure 1 depicts a block diagram representing the functional architecture of a road slope estimator according to **the** present **invention**;

» Figure 2 depicts quantities involved in the road  
20 **slope** estimation carried out by a comprises a Linear Kalman Observer; and

\* Figure 3 depicts a **block** diagram representing the functional architecture of a vehicle mass estimator according to the present **invention** .

25

#### BRIEF DESCRIPTION OF PREFERRED EMBODIMENTS OF THE INVENTION

The following description is **provided** to enable a  
30 person skilled in the art to make and use the invention. Various modifications to the **embodiments** will be readily-apparent to **those** skilled in the **art**, without departing

from the scope of the **present** invention as **claimed**.  
Thus, the present invention is not intended to be  
limited to the embodiments shown, but is to be accorded  
the widest scope consistent with the principles and  
5 features disclosed herein and defined in the appended  
claims .

In coherence with explained simplicity and  
**sustainability** of estimations, it has been found that  
the possibility to obtain the estimations **with** a single  
10 extended states estimator, with its relative problems  
about convergence, different represented dynamics and  
non-linearity , is to be put aside.

Instead., it has been found suitable to simplify and  
reduce to the most basic form the problem with a **top-**  
15 down approach. In practice, road slope and vehicle mass  
are **estimates** separately by using different model  
references and real vehicle measurements., in order to  
obtain two independent estimations, and then estimations  
are integrated in order to improve estimation  
20 performance in a model based framework. With this  
theoretical base, selected algorithm for implementation  
of slope observer is a linear Kalman filter based on  
vehicle longitudinal acceleration model and for mass  
estimation has been chosen Recursive Least Square with  
25 forgetting factor applied to equation (1) .

**Estimation** functions have been developed to be  
robust to reciprocal disturbance, in practice slope  
disturbance **hasn't** influence on **mass** estimation by using  
suitably dynamic pitch-compensated longitudinal  
30 acceleration measure instead of vehicle wheels speed,  
while slope estimation is based on longitudinal  
acceleration sensor model, so., it guarantees robustness

to powertrain uncertainties and mass varying by avoiding vehicle motion equation use. Otherwise mass varying disturbance is not fully rejected, there is a not erasable disturbance on longitudinal acceleration  
5 measure, static pitch acceleration offset due to vehicle mass distribution. If a vehicle running on a slope with constant speed or still on flat road is considered, there is a static offset on longitudinal acceleration sensor measure, this error is due to load distribution  
10 on vehicle, and its entity is linked to vehicle suspension stiffness. This last disturbance on slope estimation may be reduced by integrating slope and mass estimations. So, knowing vehicle load attitude diagrams and using mass estimation function is possible to  
15 recognize particular conditions of vehicle load distribution and to correct longitudinal acceleration measure in order to limit this inerascable error on slope estimation improving further estimation precision.

Figure 1 depicts a block diagram representing the  
20 functional architecture of a road slope estimator according to the present invention, and where all the input and output quantities based on which estimator operates are indicated.

The road slope estimator is designed to cover the  
25 greatest number of static and dynamic conditions in which the vehicle may operate, namely stationary or in motion, and, when in motion, in longitudinal motion or in a curve, with the possibility to be customized based on the application in which this information is  
30 required. In addition, the road slope estimator is model-based in order for it to be portable and tunable

on different vehicles to reduce the **development** time and cost.

In particular, the road slope estimator comprises a Pitch Compensation Block., which corrects the longitudinal acceleration to limit the effect of pitch disturbance on the measurement of the longitudinal **acceleration made** by an **accelerometric** sensor, when the vehicle is stationary (static), is braking and is accelerating {**dynamic**}. In essence, the **accelerometric** sensor measures all the main effects involved in the rigid body mechanics on an object with firm suspension when it is **stationary** or moving longitudinally or even when cornering. Among the different overlapping **effects** that are to be purged there is pitching. **The** pitching **phenomenon is both** a static and a dynamic phenomenon: in practice, the static **part is** related to how the vehicle settles down on the suspension based on the load distribution on the floor when the vehicle is stationary, while the dynamic part is an effect that is closely related to braking and accelerating, but extinguishes in a fast transient. The static pitch, which represents a large part of the pitching disturbance, is managed **according** to two different logics, wherein the first logic considers a load mass evenly distributed on the floor, and then, based on the vehicle **suspension structure diagram** (target), a static acceleration correction is **computed**, while the second logic is based, **in** addition to the previous correction, on information from a vehicle mass estimator.

The road slope estimator further comprises a Stationary Lateral **Compensation** Block, **which** makes a correction to limit the effect of the vehicle .lateral

dynamics that, in bend, introduces an additional term to the longitudinal acceleration, hence a new error to the signal. The block is based on a bike model and on target parameters of the vehicle on which the estimator is  
5 implemented.

The road slope estimator further comprises a Linear Kalman Observer designed to estimate the road slope. In order to define the Observer, it is fundamental to describe plant with a detailed model useful to quantify  
10 entity of different terms in play. In particular, longitudinal acceleration measured by sensor is expressed in canonical form in order to understand disturbances and system states for estimation.

With reference to Figure 2, according to rigid body  
15 dynamics, sensor position and direction can be described in fixed inertial reference axis always parallel to road  $R_0$  as:

$$\begin{pmatrix} x_{sens} \\ y_{sens} \\ z_{sens} \end{pmatrix}^{R_0} = \vec{r}_{sens} = \vec{r}_{OG} + R_{body}^O \cdot \vec{r}_{st} \quad (2)$$

20

where  $R_{body}$  is a reference axis fixed with vehicle which rotates on vehicle center of gravity CoG of pitch angle.

Deriving equation (2), it results in:

25

$$\vec{v}_{sens} = \vec{v}_{OG} + \dot{R}_{body}^O \cdot \vec{r}_{st} + R_{body}^O \cdot \dot{\vec{r}}_{st} \quad (3)$$

and again;

$$\vec{a}_{sens} = \vec{a}_{OG} + \hat{R}_{body}^O \cdot \vec{r}_{st} + 2 \cdot \hat{R}_{body}^O \cdot \dot{\vec{r}}_{st} + \hat{R}_{body}^O \cdot \ddot{\vec{r}}_{st} + \vec{g} \quad (4)$$

$$\begin{pmatrix} \ddot{x}_{sens} \\ \ddot{y}_{sens} \\ \ddot{z}_{sens} \end{pmatrix}^{R_0} = \vec{a}_{sens}^{R_0} = \vec{a}_{OG} + \hat{R}_{body}^O \cdot \vec{r}_{st} + \dot{\omega} \times \left( \hat{R}_{body}^O \cdot \vec{r}_{st} \right) + \dots \quad (5)$$

$$\dots + \omega \times \left( \omega \times \left( \hat{R}_{body}^O \cdot \vec{r}_{st} \right) \right) + 2 \cdot \omega \times \left( \hat{R}_{body}^O \cdot \dot{\vec{r}}_{st} \right) + \vec{g}$$

5 Three axis accelerations of sensor body in  $R_0$  are so obtained.

Then in body:

$$\vec{a}_{sens}^{R_{body}} = \mathbf{R}_{\phi}^{body} \cdot \vec{a}_{sens}^{R_0}$$

10

only about longitudinal axis:

$$\begin{aligned} a_{x_{sens}}^{R_{body}} &= \ddot{x}_G \cdot \cos \phi - \ddot{z}_G \cdot \sin \phi + \ddot{\phi} \cdot z_{sens} + \dots \\ &\dots - \dot{\phi}^2 \cdot x_{sens} + g \cdot \sin \Phi \end{aligned} \quad (6)$$

15 Then,, if the road slope angle  $\alpha$  is considered;

$$\begin{aligned} a_{x_{sens}}^{R_{body}} &= \ddot{x}_G \cdot \cos \phi - \ddot{z}_G \cdot \sin \phi + \ddot{\phi} \cdot z_{sens} + \dots \\ &\dots - \dot{\phi}^2 \cdot x_{sens} + g \cdot \sin (\phi + \alpha) \end{aligned} \quad (7)$$

This equation is a non-linear, but time-invariant and can be approximated with a general already known linear, time-invariant relation:

$$5 \quad a_{x_{Meas}} = a_x + a_{disturb} + g \cdot \sin \alpha \quad (8)$$

This equation is useful to estimate road slope independently from vehicle mass using only the longitudinal acceleration model and linear Kalman  
10 filtering theory. Term  $a_{disturb}$  is the part of the vehicle's acceleration caused by disturbances not described by the model for the longitudinal dynamics. It should cover all the model errors found in this section. So, given a good description on how the state  $a_{disturb}$  is  
15 changing, a Kalman filter can be used to estimate system states and to filter this disturbance.

The Kalman filter is then designed using:

$$x = \begin{bmatrix} v_{vehicle} \\ \sin \alpha \end{bmatrix}; u = a_{x_{Meas}} - v_{vehicle}$$

20 so that ;

$$\dot{v}_{vehicle} = a_x = -g \cdot \sin \alpha + a_{x_{Meas}} - a_{disturb} \Rightarrow \dot{x}_1 = -g \cdot x_2 + u + v \quad (9)$$

All the process state variables are considered  
25 Gaussian stochastic ones, so the assumed noise covariance matrix has been defined in coherence with physical characteristics of stochastic variables, and then tuned in order to get the best estimation possible. In this estimation framework, term  $a_{disturb}$  may be modeled  
30 as a simple process noise  $v$  over slope state.

About slope state, it has been modeled **according** to two different approaches., the **first** time under the assumption that the state  $x_2$  undergoes slight changes each sampling period, so its first derivative is equal  
5 to Gaussian noise;

$$\dot{x}_2 \approx \omega \quad (10)$$

and a second method according to a first-order **Gauss - Markov** process:

10

$$\dot{x}_2 = \frac{1}{\tau} x_2 + \zeta \quad (11)$$

where  $\tau$  is a tuned parameter according to **slowest** slope which is to be observed.

This last approach is useful especially to filter  
15 desired slope dynamics from pitch disturbance, so give the possibility to eliminate pitch disturbance leaving only slope information, while there is the need to **pre-**filter longitudinal acceleration from pitch dynamics also partially. Both approaches are valid and give us  
20 interesting estimation results. The latter is preferred, so using a partially pitch corrected longitudinal acceleration as input for explained observer,

The road slope estimator **further** comprises an Enable Logic Block, which is designed to enable and  
25 disable **road** slope estimation in certain situations in which this estimate is unreliable. In fact, the road slope estimator is always active, or rather is active in as many situations of the vehicle as possible. The basic idea of the road slope estimator is to obtain an  
30 estimate as much as possible available, The only



limitation is when road slope estimation when the vehicle in dynamic cornering when the lateral acceleration is above a certain threshold. In these cases, the longitudinal acceleration is too soiled by the effect of the lateral acceleration and hence it is preferred to disable the estimation and indicate this situation in a status signal that accompanies the estimate. The disabling threshold changes from vehicle to vehicle based on design specifications from the dynamic standpoint (e.g., understeer gradient. and gradient balance) . Estimation is disabled when the threshold is reached, and is then re-enabled when a different lower threshold is reached, so as to avoid spurious effects of activation/deactivation on the algorithms downstream of the enablement .

The road slope estimator further comprises a Speed Zero Slope Estimator which is activated when the Linear Kalman Observer is switched off by the Enable Logic Block, during wheel speed measurements blind windows , and smoothly joins dynamic slope estimation to static slope estimation based on the only acceleration measure from inertial sensor avoiding final braking pitch and other noisy effects.

Figure 3 depicts a block diagram representing the functional architecture of a vehicle mass estimator- according to the present invention, and where all the input and output quantities based on which estimator operates are indicated.

The vehicle mass estimator comprises three Real Time Identification Algorithm & Model Matching Blocks associated with lower powertrain gears, one for 1<sup>st</sup> gear, one for the 2<sup>nd</sup> gear and. one. for the 3<sup>rd</sup> gear,

which are activated where longitudinal acceleration entity and powertrain "torque estimated measure" are significant .

Each one of the three blocks implements an estimation **algorithm** which is based on **longitudinal** motion in a condition that a vehicle accelerates with clutch engaged and without turning or turning with a limited lateral acceleration, with the following additional hypotheses :

- \* nominal known drag and rolling resistances; and
- \* no limitation about available surface adhesion.

Mechanical equilibrium equation at front wheels is;

$$\eta \cdot C_{traction} \cdot \tau_{diff} \cdot \tau_{gear} = \left( M \cdot R + \frac{\eta \cdot J_{mot} \cdot \tau_{diff}^2 \cdot \tau_{gear}^2}{R} + \frac{J_{wheels}}{R} \right) \cdot \ddot{x} \quad (12)$$

where  $\tau_{diff}$  and  $\tau_{gear}$  are respectively differential and gearbox ratio and  $C_{traction}$  is traction torque, so applied motor torque at wheels minus frictions torque from powertrain estimations.

In discrete version with sampling time  $T$ :

$$\int_{(k-1)T}^{kT} C_{traction} dt = \dots$$

$$\left( \frac{M \cdot R}{\eta \cdot \tau_{diff} \cdot \tau_{gear}} + \frac{J_{mot} \cdot \tau_{diff}^2 \cdot \tau_{gear}^2}{R} + \frac{J_{wheels}}{R \cdot \eta \cdot \tau_{diff} \cdot \tau_{gear}} \right) \cdot \ddot{x} \quad (13)$$

$$\left( \dot{x}(kT) - \dot{x}((k-1)T) \right)$$

Approximating the first term of equation with 'Bilinear Transformation Method' :

$$\int_{(k-1)T}^{kT} C_{traction} dt = [(1 - \alpha) \cdot C_m((k-1)T) + \alpha \cdot C_m(kT)] \cdot T \quad \text{with } 0 \leq \alpha \leq 1$$

with  $\alpha \approx 1$  (Backward Euler Discretisation) :

5

$$C_{traction}(k) = \left( \frac{M \cdot R}{\eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T} + \frac{J_{mot} \cdot \tau_{diff} \cdot \tau_{gear}}{R \cdot T} + \frac{J_{wheels}}{R \cdot \eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T} \right) \cdot \left( \dot{x}(k) - \dot{x}((k-1)T) \right) \quad (14)$$

In order to be robust to slope disturbance we can pass to consider in place of vehicle speed difference, measured longitudinal acceleration multiplied to sampling time:

10

$$C_{traction}(k) = \left( \frac{M \cdot R}{\eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T} + \frac{J_{mot} \cdot \tau_{diff} \cdot \tau_{gear}}{R \cdot T} + \frac{J_{wheels}}{R \cdot \eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T} \right) \cdot (\ddot{x}(k) \cdot T) \quad (15)$$

This longitudinal equation (15) can be rewritten in following regression form:

15

$$y(k) = \varphi^T(k) \cdot \theta(k) + \xi(k) \quad (16)$$

with ;

20

$$y(k) = C_{traction}(k)$$

$$\phi^T(k) = \dot{x}(k) \cdot T$$

$$\theta(k) = \frac{M \cdot R}{\eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T} + \frac{J_{mot} \cdot \tau_{diff} \cdot \tau_{gear}}{R \cdot T} + \frac{J_{wheels}}{R \cdot \eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T}$$

5 From  $\theta(k)$ , vehicle mass  $M$  is:

$$M = \frac{\theta(k) \cdot \eta \cdot \tau_{diff} \cdot \tau_{gear} \cdot T}{R} - \frac{\eta \cdot J_{mot} \cdot \tau_{diff}^2 \cdot \tau_{gear}^2}{R^2} - \frac{J_{wheels}}{R^2} \quad (17)$$

where identified  $\theta(k)$  is the parameter vector and  $\xi(k)$  denotes lumped disturbance which can degrade the estimation performance of vehicle mass and which must be minimised. In order to overcome this degradation has been used RLS algorithm with forgetting factor ( $\mu$ ) which minimizes prediction error according to quadratic principle, and reduces RLS problem about progressive decay of algorithm reactivity with sampling aging:

$$\begin{aligned} \theta(k) &= \theta(k-1) + K(k) \cdot \varepsilon(k) \\ K(k) &= Vff(k) \cdot \phi(k) \\ \varepsilon(k) &= y(k) - \phi^T(k) \cdot \theta(k-1) \\ Vff(k) &= (1/\mu) \cdot (Vff(k-1) - \beta_{k-1}^{-1} \cdot Vff(k-1) \cdot \phi(k) \cdot \phi^T(k) \cdot Vff(k-1)) \\ \beta_{k-1} &= \mu + \phi^T(k) \cdot Vff(k-1) \cdot \phi(k) \end{aligned} \quad (18)$$

Where  $Vff(k)$  is not so different from estimation variance for every sampling period and forgetting factor  $\mu$  has been managed in a typical mode for estimation of constant parameters :

- 20 -

$$\begin{aligned}
 \mu(k) &= \rho \cdot \mu(k-1) + (1-\rho) \\
 \mu(0) &= \mu_0 \\
 \text{with } \rho &\in (0; 1) \text{ and } \mu_0 \in (0; 1)
 \end{aligned}
 \tag{19}$$

The vehicle mass estimator further comprises a Merge by Variance Weighted Average Block, where mixed mass estimation from different gears is obtained by-  
 5 using a weighted mean where performed choice about weights is:

$$\omega_i = \frac{1}{\sigma_i^2}$$

10 The weighted mean in this case is:

$$\bar{M} = \frac{\sum_i \left( \frac{M_i}{\sigma_i^2} \right)}{\sum_i \left( \frac{1}{\sigma_i^2} \right)}$$

and the variance of the weighted mean is:

15

$$\sigma_M^2 = \frac{1}{\sum_i \left( \frac{1}{\sigma_i^2} \right)}$$

The significance of formulation "'Merge by Variance Weighted Average'" is that this weighted mean is the maximum likelihood estimator of the mean of the probability distributions under the assumption that they  
 20 are independent and normally distributed with the same mean.

The vehicle mass estimator further comprises a pitch compensation block, which performs the **same** compensation as that performed by the pitch compensation block of the road slope estimator. In practice, the same  
5 corrections as those performed to the input signals in the road slope estimation are replicated. The **only** difference is the lack of additional **correction** due to the mass estimation. In this block, in fact, in the absence of knowledge of the vehicle mass., a uniform  
10 distribution of the vehicle mass of the entire vehicle floor is assumed, thus admitting an indelible downstream computation error due to vehicle balance. It is to be noted that in this case this effect is acceptable because it is completely hidden inside of the error committed by  
15 using the engine **torque** signal (signal not measured but in **turn** estimated by the engine control unit).

The vehicle mass estimator further comprises a stationary lateral compensation block, which makes a correction to limit the effect of the vehicle lateral  
20 dynamics, which in bend introduces an additional term to the longitudinal acceleration, hence a new error to the **signal**. The block is **based** on a bike model and on target parameters of the vehicle on which the estimator is implemented.

25 The vehicle mass estimator further comprises a manual gear estimator block, which, in the absence of an automatic transmission, estimates the gear selected by the driver and indicates when engagement of the powertrain system is successfully completed. In  
30 practice, based on vehicle speed, engine speed, clutch pedal **position**, etc., it recognizes synchronization of a gear shift to enable recursive identification algorithms

in the right time, i.e., when the real system is as similar as possible to the mathematical model implemented in the real-time identification Algorithm & model matching blocks.

5        In the end, the vehicle mass estimator further comprises an enable mass & gear block, which manages activation of three different estimators (one for a corresponding gear) and enable them only when the real system is more likely modelable in accordance with the  
10        equations set. It is carried out in first, second and third gear, where vehicle acceleration and engine torque gradients occur such as to better highlight the differences of mass loaded on the vehicle, Activations are based on calibratable thresholds in turn based on  
15        various signals coming mainly from the powertrain and on internal estimates and are intended to minimize uncertainties deriving mainly from powertrain signals that are partly estimated (engine torque/fiction) and partly measured (engine speed, accelerator pedal ,  
20        etc..).

## CLAIMS

1. Automotive electronic control unit (ECU) programmed to real-time estimate either or both of vehicle mass and road slope, wherein;

5 a. road slope is estimated;

a1, when vehicle is considered stopped based on an **accelerometer** signal indicative of vehicle acceleration., **wherein** the vehicle is considered stopped in the presence of substantially zero  
10 **values** of a. speed signal indicative of vehicle speed, and

a2. when **vehicle** is in rectilinear and curvilinear motion by implementing a road slope observer based on a linear Kalman filter, which is  
15 designed to:

**&21.** operate based on signals indicative of vehicle speed and acceleration., and

a22. **compensate** for accelerometric disturbances due to:

20 a221. vehicle static pitch resulting from vehicle load distribution, and

a222. vehicle dynamic pitch due to acceleration to which vehicle is subjected during motion, and

25 a223, accelerometric disturbance components due to vehicle **lateral dynamics**;

b. vehicle mass is estimated;

**hi.** when vehicle is in motion, and

30 b2. based on a recursive least square algorithm with forgetting factor., and

**b3.** based on an accelerometric **signal indicative** of vehicle acceleration, on a **vehicle** speed signal,



and other signals representing a vehicle propulsive/resistive torque, and

b4. at different low gears, to estimate vehicle mass and associated variance for each gear, and

5        b5. based on vehicle mass estimations and corresponding variances for each gear, and

b6. compensating for accelerometer disturbances due to:

b61. vehicle dynamic pitch; and

10        b62. accelerometric disturbance components due to vehicle lateral dynamics ; and

b7. minimizing uncertainties on propulsive/resistive torque due. to gear efficiency and rolling resistance.

15        2. The automotive electronic control unit (ECU) according to claim 1, further programmed to:

c. link road slope estimation carried out when vehicle is considered stopped and in motion;

20        c1, starting road slope estimation when vehicle is stopped based on the latest road slope estimations when vehicle was in motion, and  
c2, starting road slope estimation when vehicle is in motion based on the latest road slope estimations when vehicle was stopped.

25        3, The automotive electronic control unit (ECU) according to any preceding claims, further programmed to, when both road slope and vehicle mass are estimated:

d. either estimate road slope and vehicle mass independently, or

30        e, estimate road slope based on vehicle mass estimation .

4, The automotive electronic control unit (ECU)

according to any preceding **claims**, further programmed to estimate road slope;

**a3.** when vehicle is in curvilinear motion, for vehicle lateral acceleration values comprised in a predetermined range, using the road slope observer as per point a2 and having compensated upstream accelerometric disturbances due to vehicle lateral acceleration .

5, The automotive electronic control unit (ECU) **according** to any preceding claims, further programmed to compensate for **accelerometric** disturbances due to vehicle static and dynamic pitches;

a.2231. estimating vehicle static pitch resulting from the vehicle load distribution based on estimated vehicle mass and attitudes diagram, and

a.2241. estimate vehicle dynamic pitch based on an accelerometer signal indicative of vehicle acceleration during motion.

6. The **automotive** electronic control unit (ECU) according to any preceding claims, further programmed to estimate vehicle mass:

**b8.** limiting dynamic pitch effects and accelerometer disturbances effects due to vehicle **lateral** acceleration on vehicle mass estimation.

7, The automotive electronic control unit (ECU) according to any preceding claims, wherein vehicle mass estimation **is** carried **out** as a weighted average of individual mass estimations at different speeds, and wherein **to** estimated vehicle mass is associated an overall variance computed as a.n **average** of individual **variances** associated with individual mass estimations,

8. The automotive electronic control unit. (ECO)

according to any preceding claims, wherein vehicle mass is estimated when vehicle is in motion and only when propulsive/ resistive torque is considered reliable, and wherein vehicle mass estimation is considered to be  
5 reliable when overall variance of estimated vehicle mass is lower than a threshold value .

9. The automotive electronic control unit (ECU) according to any preceding claims, wherein vehicle mass is estimated when vehicle is in motion and is considered  
10 to be reliable even when vehicle successively stops.

10. The automotive electronic control unit (ECU) according to any preceding claims, wherein vehicle mass is estimated every time that predetermined events occur that make unreliable the previous vehicle mass  
15 estimation.

11. A vehicle comprising an automotive electronic control unit (ECU) according to any preceding claims.

12. A software loadable into an automotive electronic control unit (ECU) and designed to cause,  
20 when executed, the automotive electronic control unit to become programmed as claimed in any preceding claims.

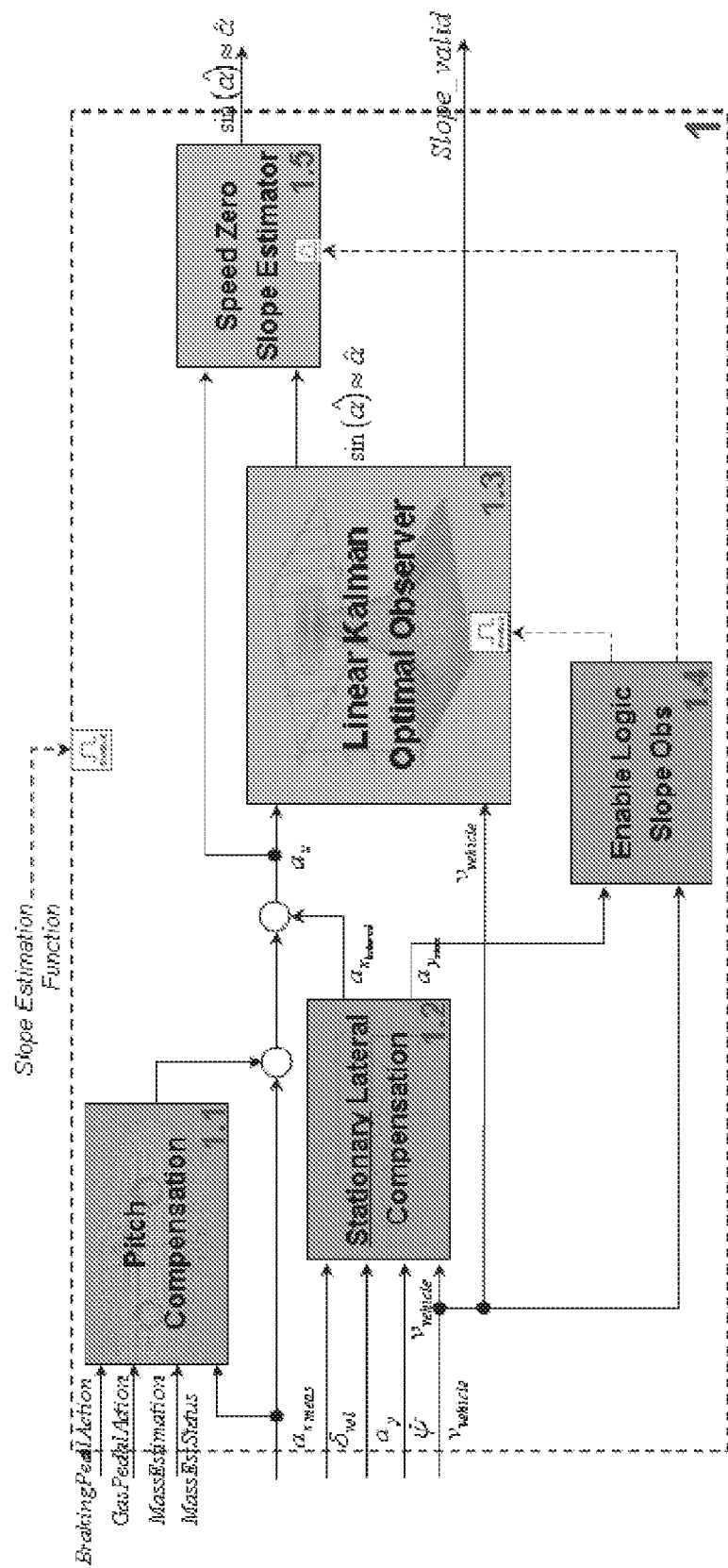


Fig. 1

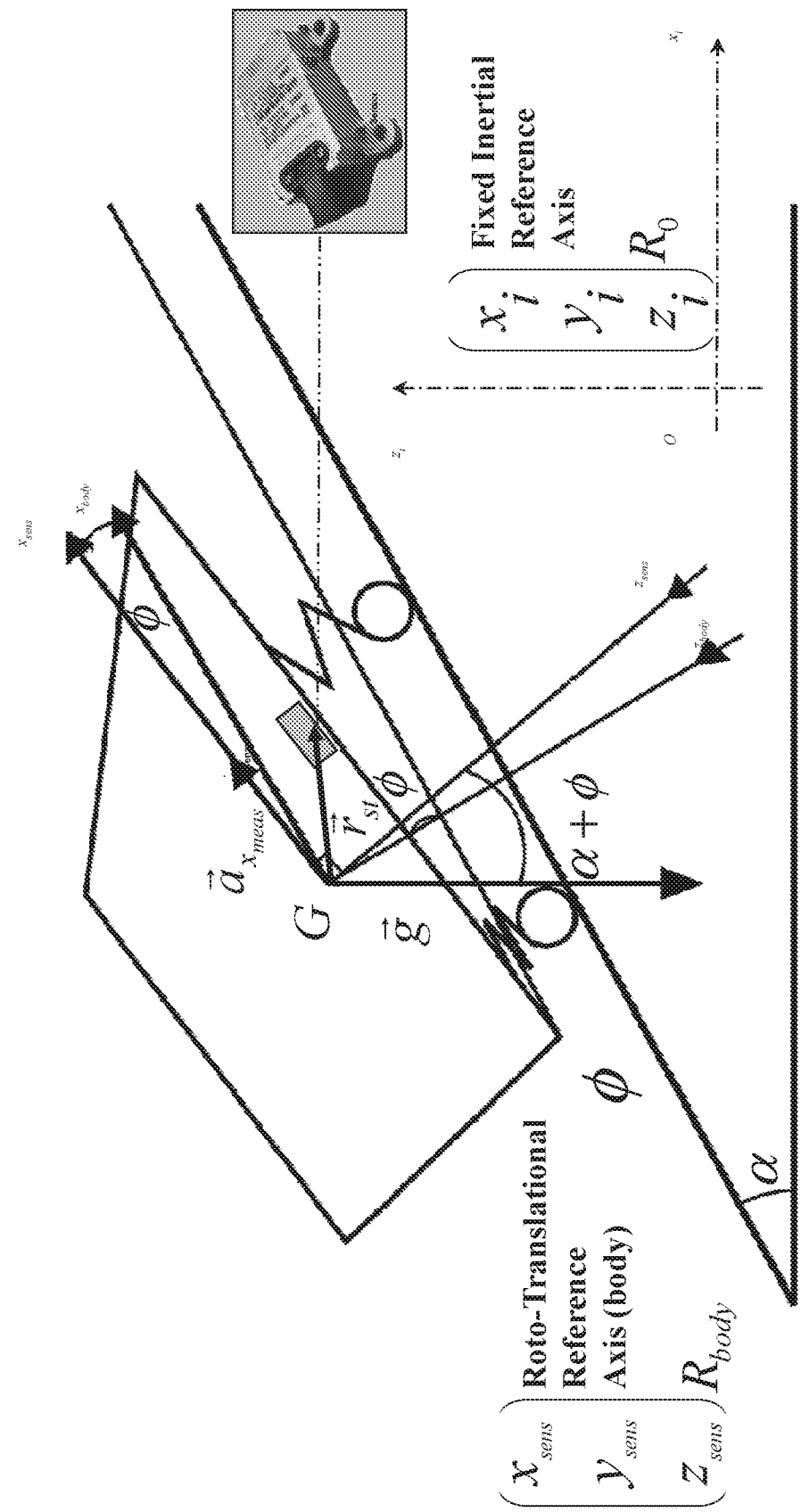


Fig. 2

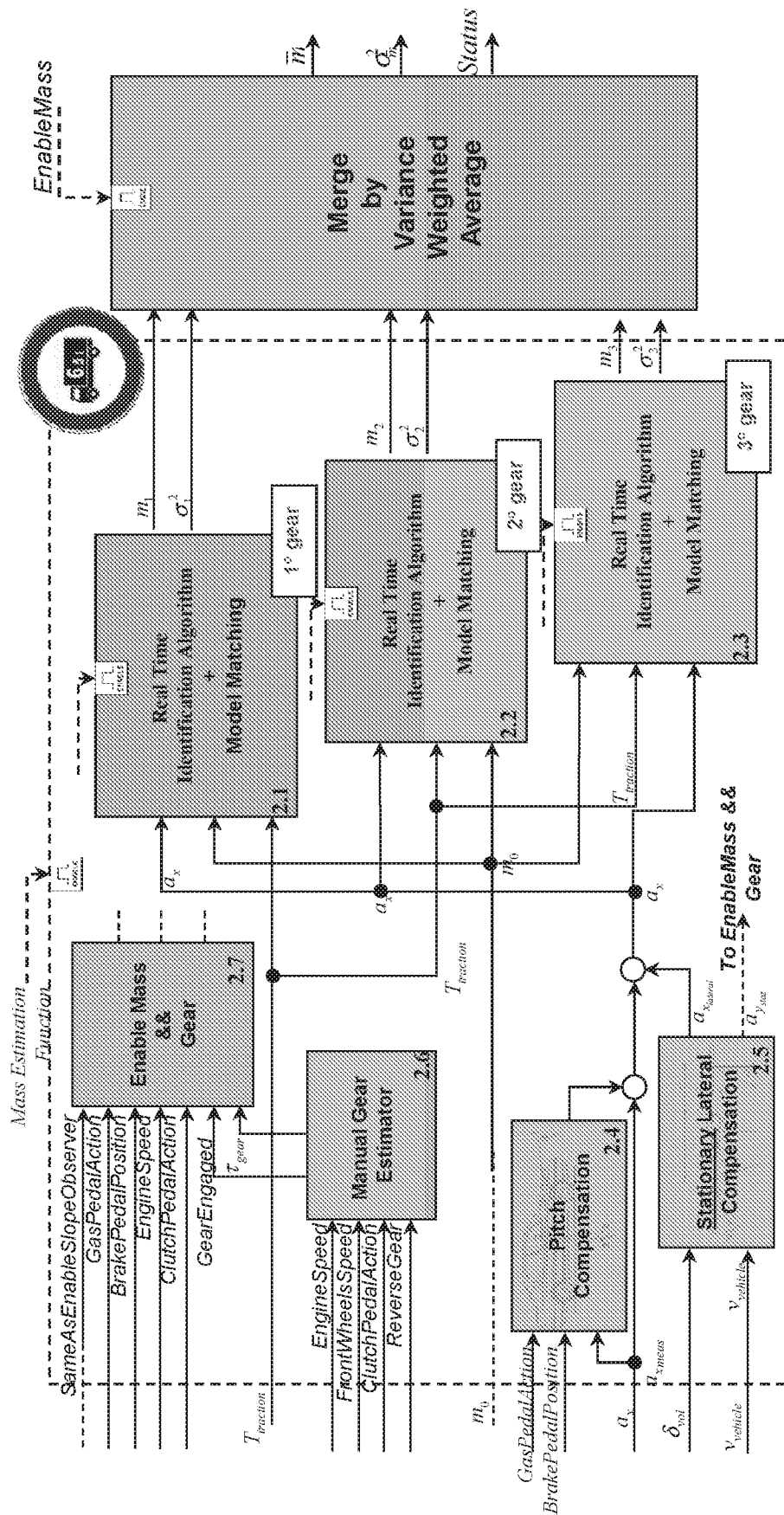


Fig. 3