

CSc 179 – Graph Coverage for Source Code

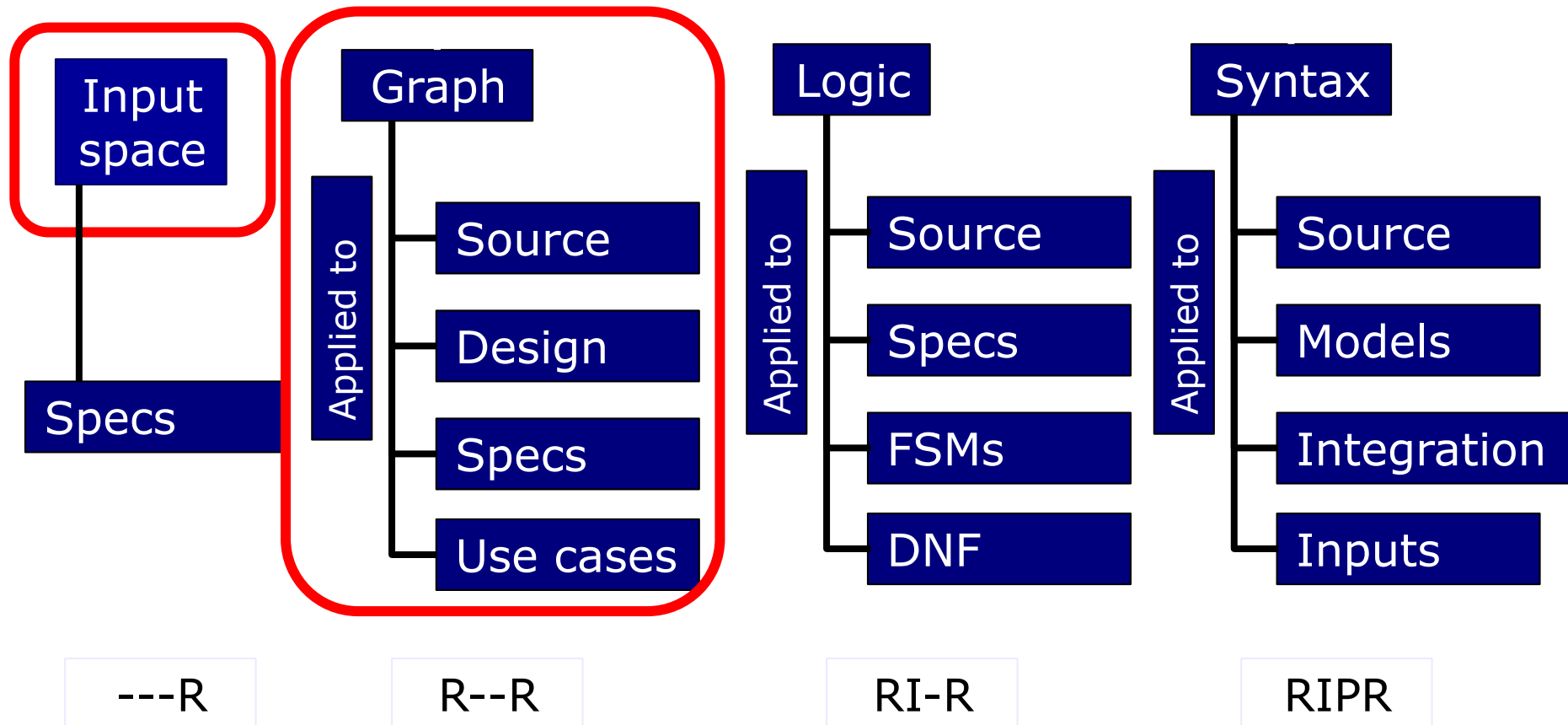
Credits:

AO – Ammann and Offutt, “Introduction to Software Testing,”
Ch. 7

University of Virginia (CS 4501 / 6501)

Structures for Criteria-Based Testing

Four structures for modeling software



Overview

- Graph coverage criteria are widely used on source code
- Define graph, then apply coverage criterion
- **Control flow graph (CFG)**: the most common graph for source code
- Node coverage: execute every statement
- Edge coverage: execute every branch
- Data flow coverage: augment the CFG with
 - defs: statements that assign values to variables
 - uses: statements that use variables

Control Flow Graph (CFG)

- Represent the control flow of a piece of source code
 - **Nodes** represent basic blocks
 - **Basic blocks** represent sequences of instructions / statements that always execute together in sequence
 - **Edges** represent control flow (branch) between basic blocks
 - Transfer of control
 - **Initial nodes** correspond to a method's entry points
 - **Final nodes** correspond to a method's exit points
 - `Return` or `throw` in Java
 - **Decision nodes** represent choices in control flow
 - **`if`** or **`switch-case`** blocks or **`condition for loops`** in Java
- Can be annotated with extra information such as branch predicates, defs, and uses

Example: CFG for *if-else*

```

if (x < y)
{
    y = 0;
    x = x+1;
}
else
{
    x = y;
}

```

- Basic blocks (nodes)

1: if (x < y)
 2: y=0; x = x+1;
 3: x = y;

- Entry node

1

- Decision nodes

1

- Junction nodes

4

- Exit nodes

4

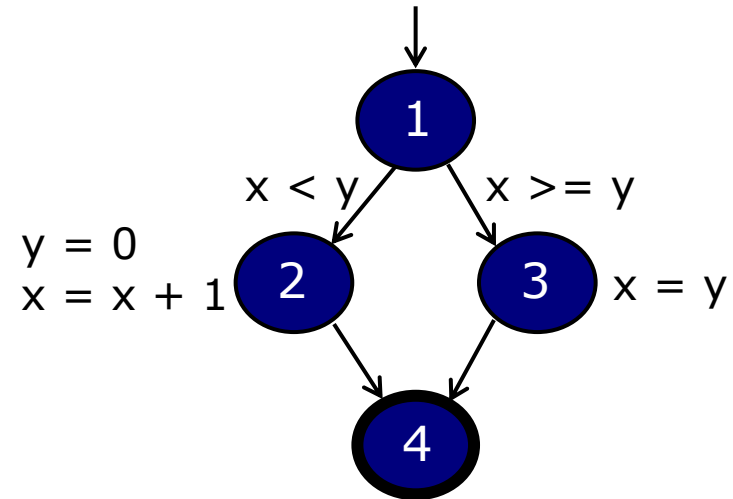
Control flow (edges)

1 → 2

1 → 3

2 → 4

3 → 4



Example: CFG for *If* without *else*

```
if (x < y)
{
  y = 0;
  x = x+1;
}
```

- Basic blocks (nodes)

1: if (x < y)

2: y=0; x = x+1;

- Entry node

1

- Decision nodes

1

- Junction nodes

3

- Exit nodes

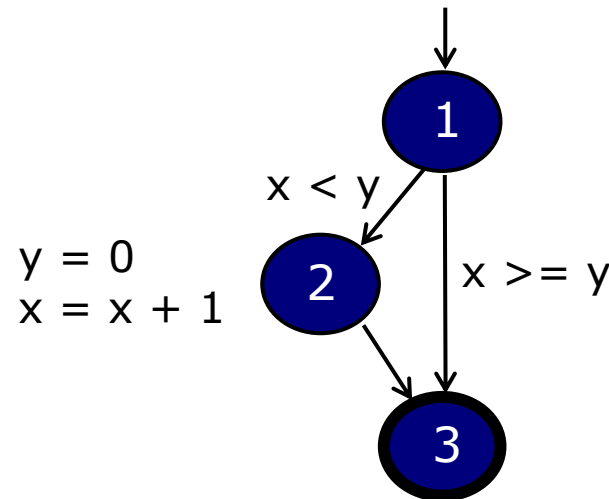
3

Control flow (edges)

1 → 2

1 → 3

2 → 3



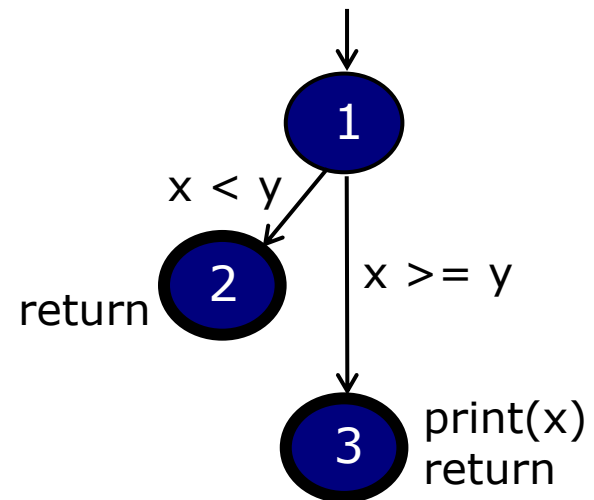
Example: CFG for *If* with *return*

```
if (x < y)
{
    return;
}
print(x);
return;
```

- Basic blocks (nodes)
 - 1: if (x < y)
 - 2: return;
 - 3: print(x); return;
- Entry node
 - 1
- Decision nodes
 - 1
- Junction nodes
 -
- Exit nodes
 - 2, 3

Control flow (edges)

1 → 2
1 → 3



Loops

- Loops require **extra** nodes (“**dummy**” node)
 - Not directly derived from program statements
- Looping structures: *while* loop, *for* loop, *do-while* loop
- Common mistake
 - Try to have the edge go to the entry node

Example: CFG for a *while* loop

```
x = 0;
while (x < y)
{
    y = f(x,y);
    x = x + 1;
}
```

- Basic blocks (nodes)
 - 1: $x = 0$;
 - 2: $\text{while}(x < y)$
 - 3: $y = f(x,y); x = x+1$;

Control flow (edges)

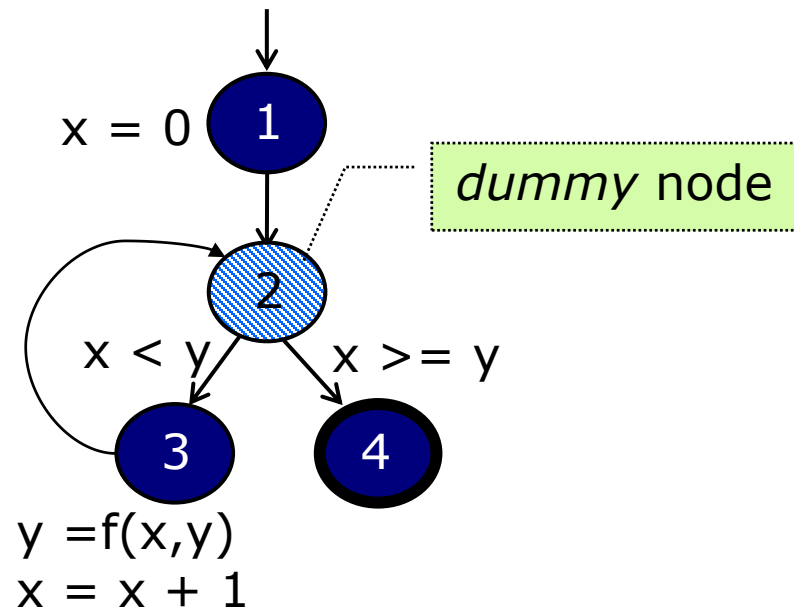
- $1 \rightarrow 2$
- $2 \rightarrow 3$
- $2 \rightarrow 4$
- $3 \rightarrow 2$

Entry node
1

Decision nodes
2

Junction nodes
-

Exit nodes
4



Example: CFG for a *for* loop

```
for (x=0; x<y; x++)
{
    y = f(x,y);
}
```

- Basic blocks (nodes)

1: $x = 0$;
 2: $x < y$
 3: $y = f(x, y)$;
 4: $x++$;

Entry node

1

Decision nodes

2

Junction nodes

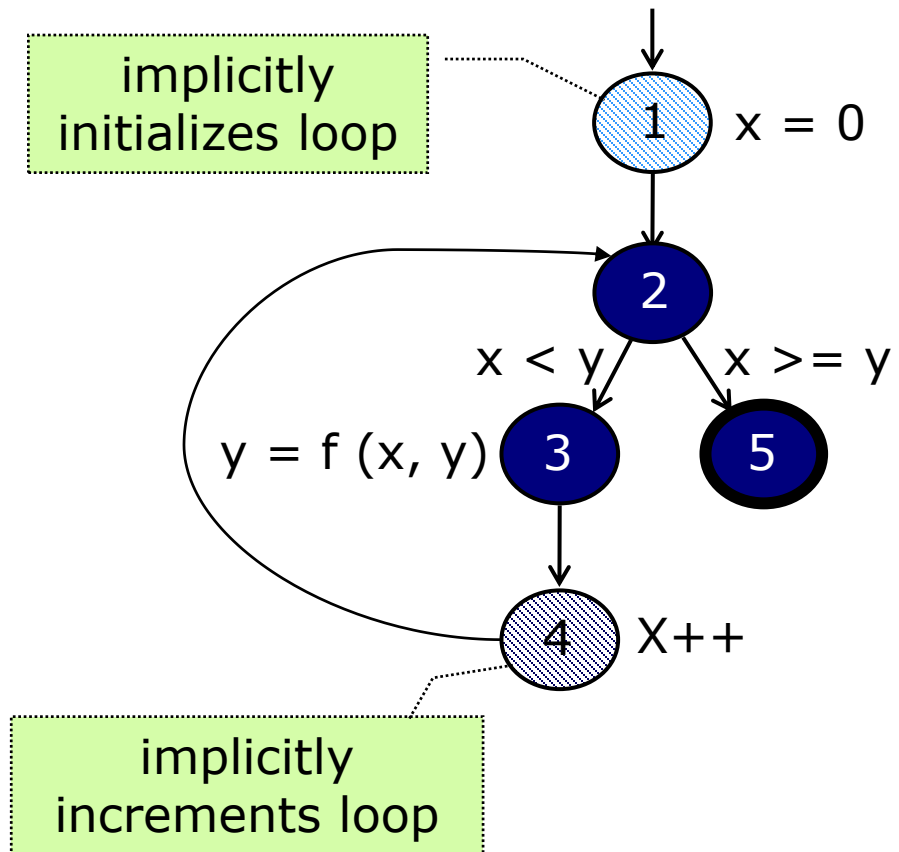
-

Exit nodes

5

Control flow (edges)

$1 \rightarrow 2, 2 \rightarrow 3, 2 \rightarrow 5, 3 \rightarrow 4, 4 \rightarrow 2$



Example: CFG for a *do-while* loop

```
x = 0;
do
{
    y = f(x,y);
    x = x + 1;
} while (x < y)
println(y);
```

- Basic blocks (nodes)
 - 1: `x = 0; do`
 - 2: `y = f(x,y); x = x+1;`
 `while(x < y)`
 - 3: `print(y);`

Control flow (edges)

```
1 → 2
2 → 2
2 → 3
```

Entry node

1

Decision nodes

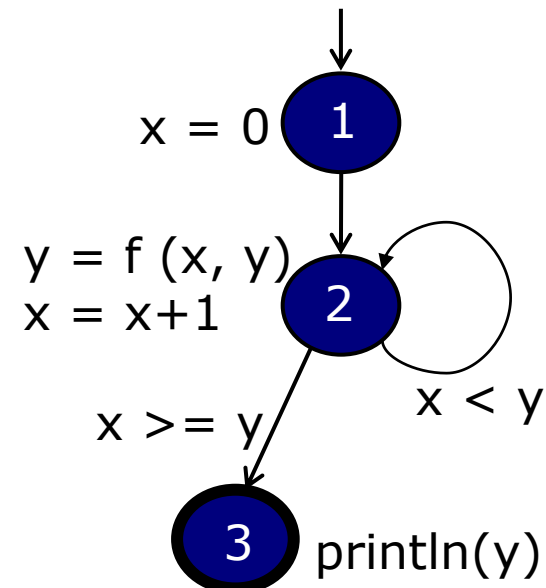
2

Junction nodes

-

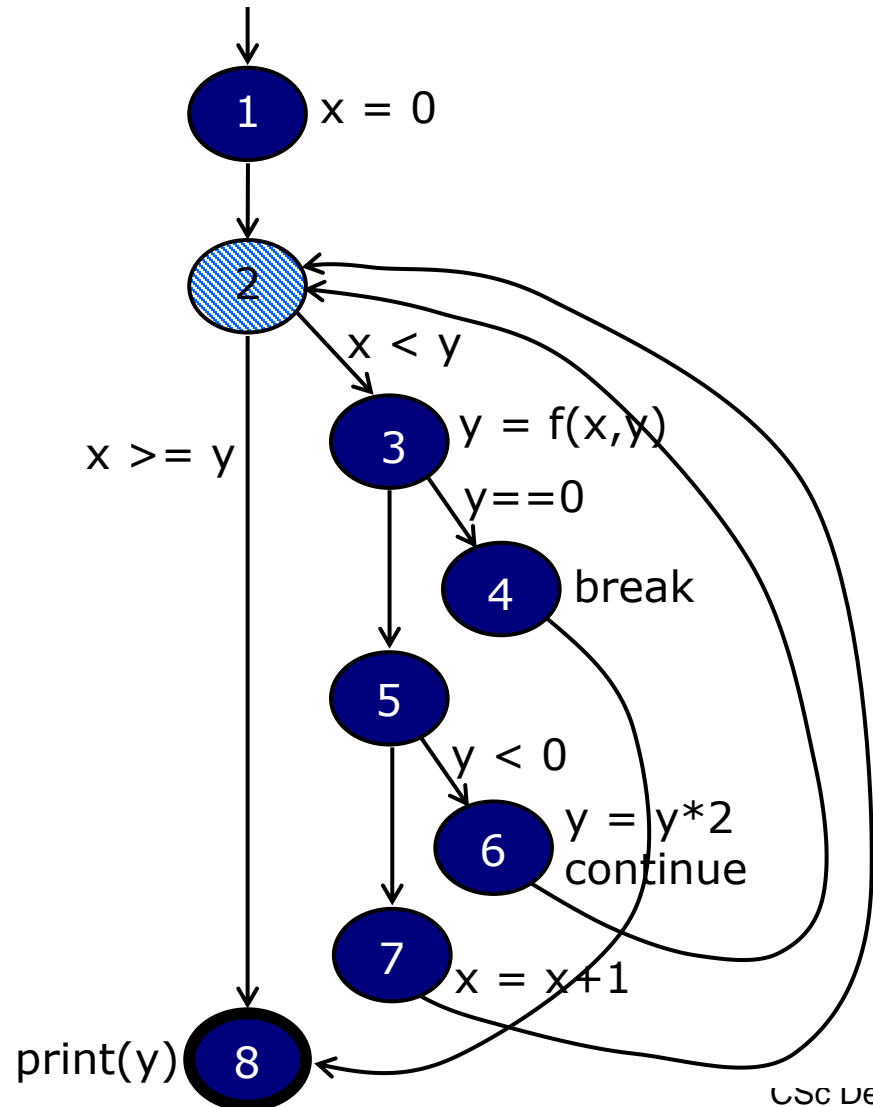
Exit nodes

3



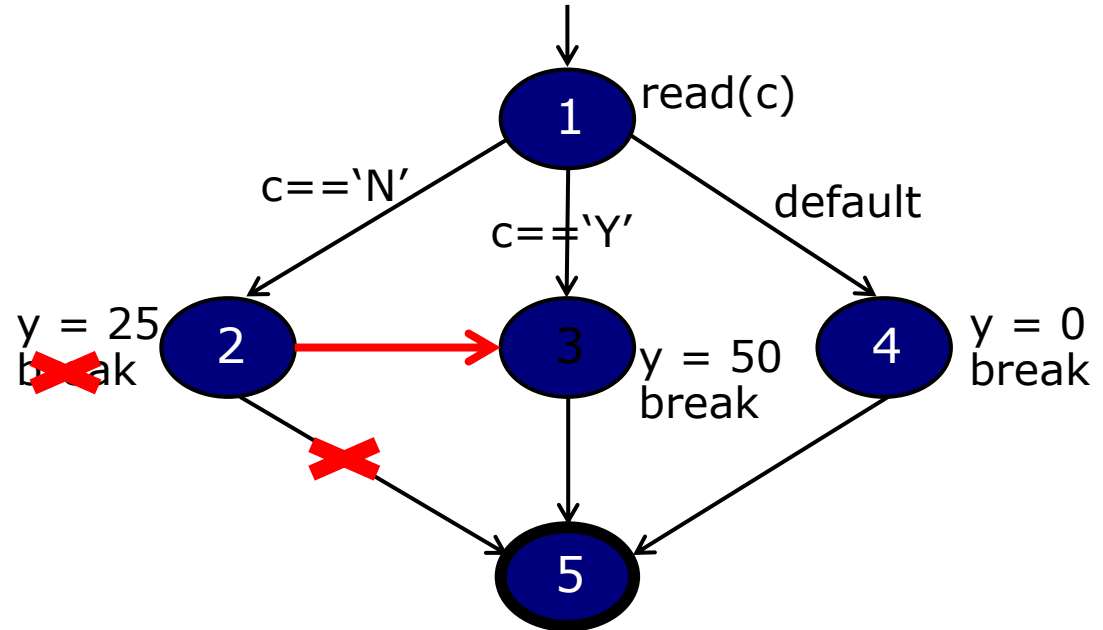
Example: CFG for a loop with *break* and *continue*

```
x = 0;  
while (x < y)  
{  
    y = f(x,y);  
    if (y==0)  
        break;  
    else if (y < 0)  
    {  
        y = y*2;  
        continue;  
    }  
    x = x + 1;  
}  
print(x);
```



Example: CFG for (*switch*) case

```
read(c);  
switch(c)  
{  
  case 'N':  
    y = 25;  
    break;  
  case 'Y':  
    y = 50;  
    break;  
  default:  
    y = 0;  
    break;  
}
```



Cases without break?

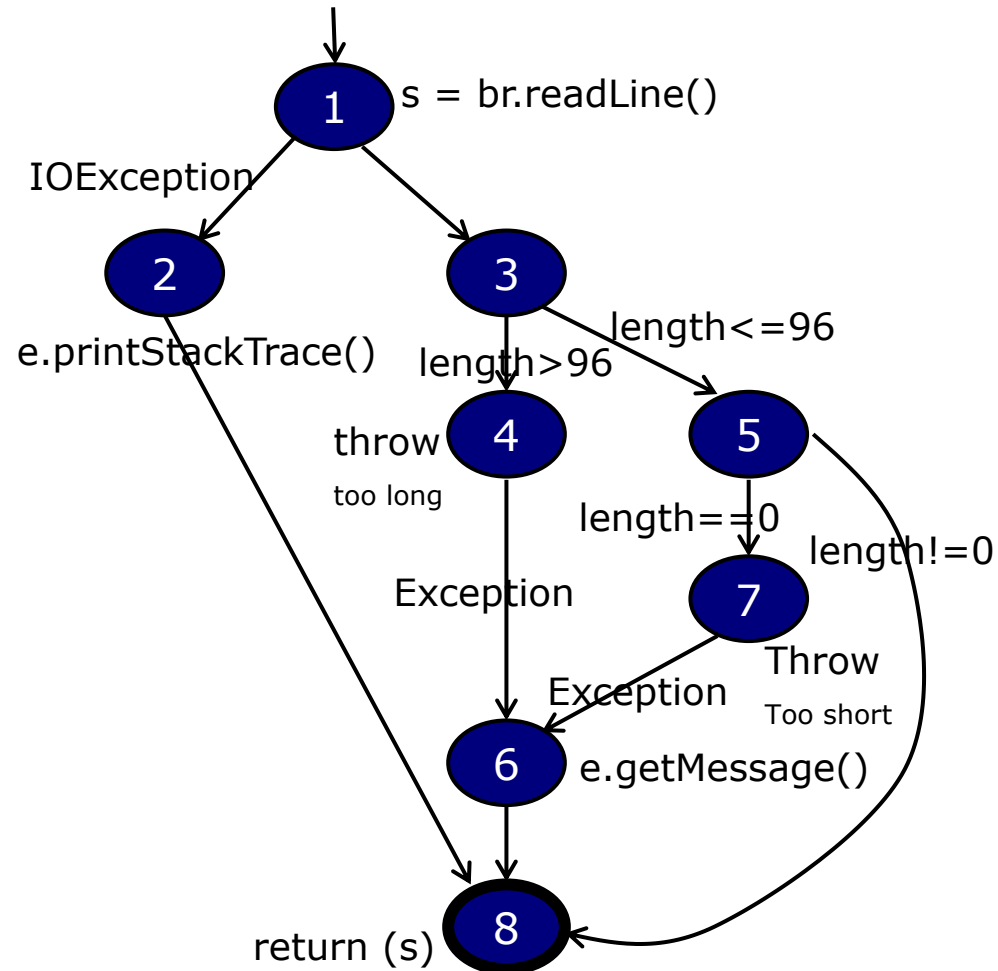
- Fall through to the next case

Example: CFG for Exceptions (*try-catch*)

```

try
{
    s = br.readLine();
    if (s.length() > 96)
        throw new Exception("too long");
    if (s.length() == 0)
        throw new Exception("too short");
} catch (IOException e) {
    e.printStackTrace();
} catch (Exception e) {
    e.getMessage();
}
return(s);

```



Exercise

```
public static int numberOccurrences(char[] v, char c)
{
    if (v == null)
        throw new NullPointerException();
    int n = 0;
    for (int i=0; i<v.length; i++)
    {
        if (v[i] == c)
            n++;
    }
    return n;
}
```

Entry node

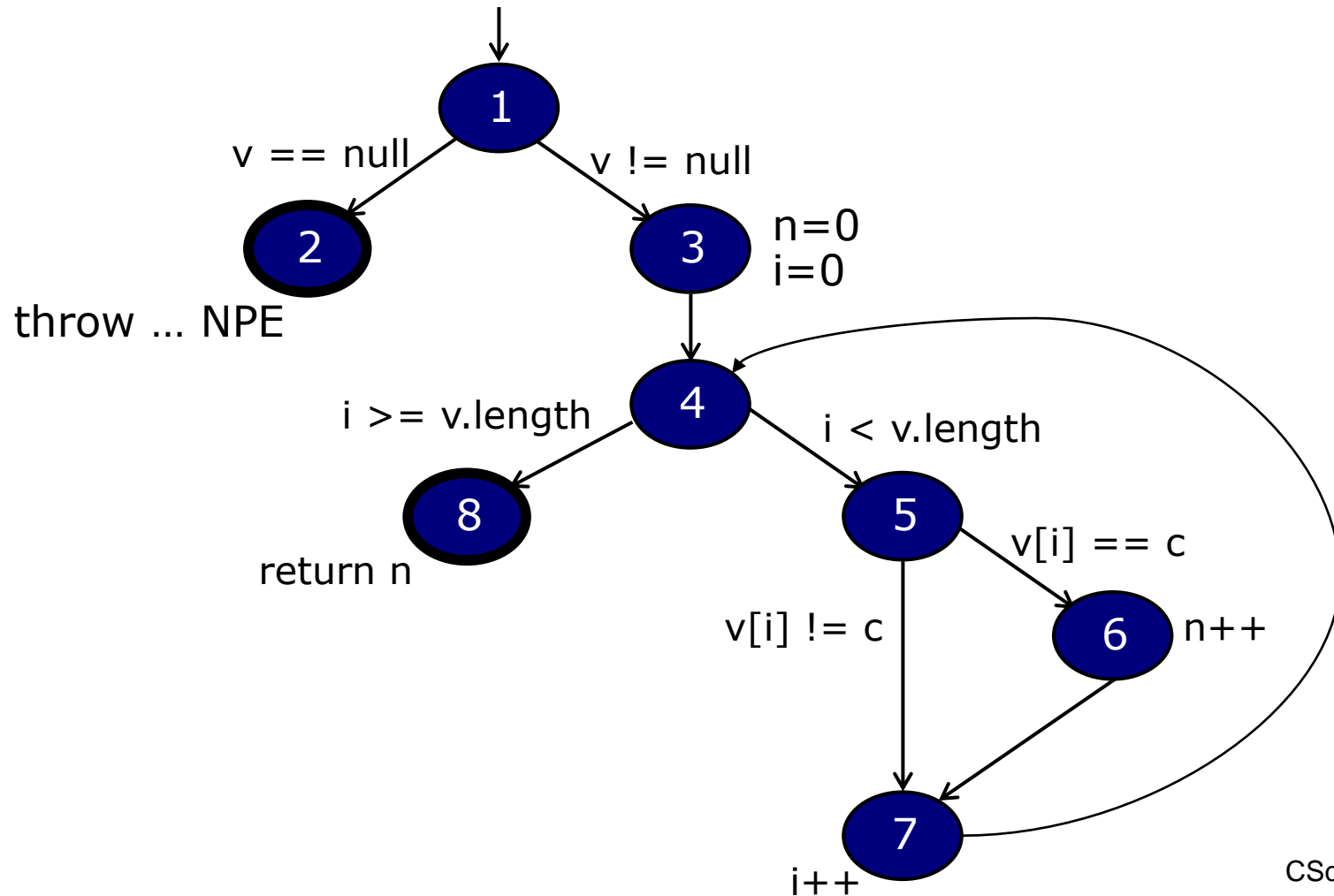
1

Exit nodes

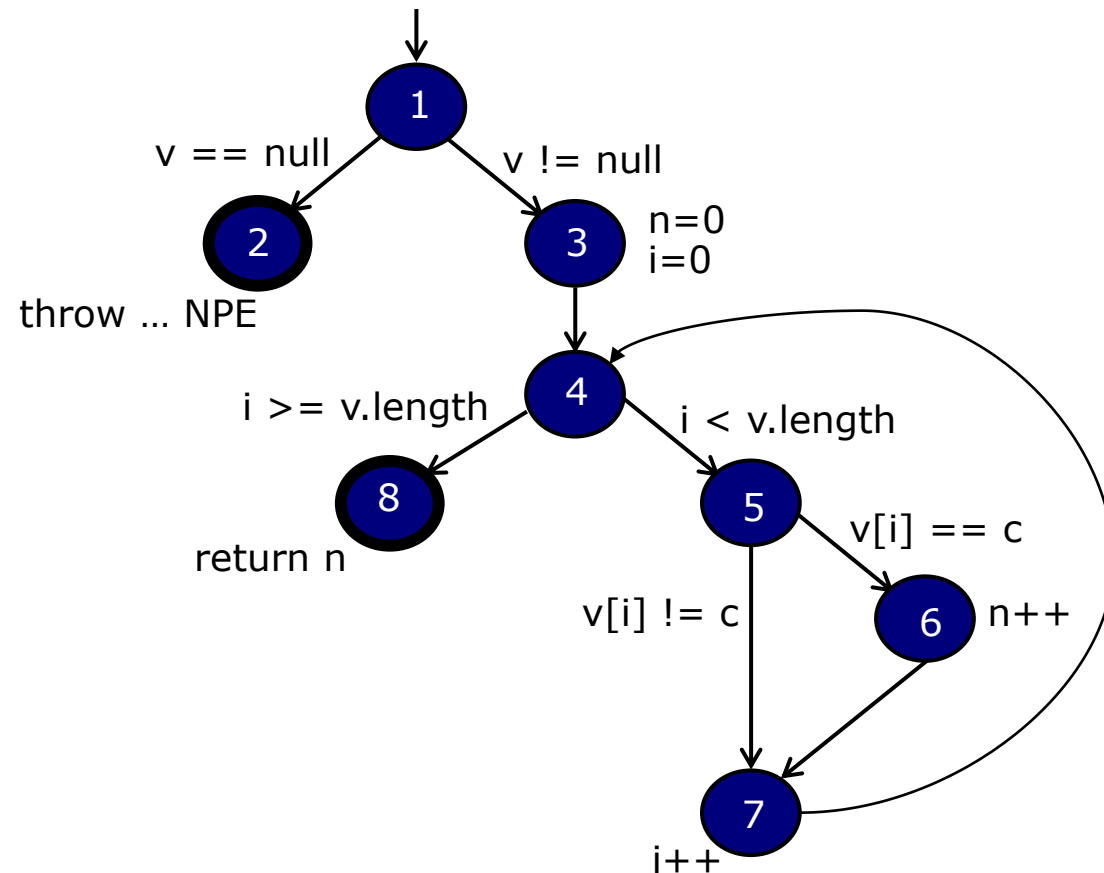
2, 8

- Basic blocks (nodes)
 - 1: if (v == null)
 - 2: throw .. NPE;
 - 3: n=0; i=0;
 - 4: i < v.length;
 - 5: if (v[i] == c)
 - 6: n++;
 - 7: i++;
 - 8: return n;
- Control flow (edges)
 - 1→2, 1→3
 - 3→4
 - 4→5, 4→8
 - 5→6, 5→7
 - 6→7
 - 7→4

CFG for *numberOccurrences()*



Applying Node Coverage (NC)



Test requirements

TR = {1,2,3,4,5,6,7,8}

Test paths

t1 = [1,2]

t2 = [1,3,4,5,6,7,4,8]

NC satisfied by {t1, t2}

Test case values (v,c)

t1 = (null, 'a'), expected NPE

t2 = ({'a'}, 'a'), expected 1

Applying Edge Coverage (EC)

Test requirements

$$TR = \{(1,2), (1,3), (3,4), (4,5), (4,8), (5,6), (5,7), (6,7), (7,4)\}$$

Test paths

$t1 = [1,2]$

$t2 = [1,3,4,5,6,7,4,8]$

$t3 = [1,3,4,5,7,4,8]$

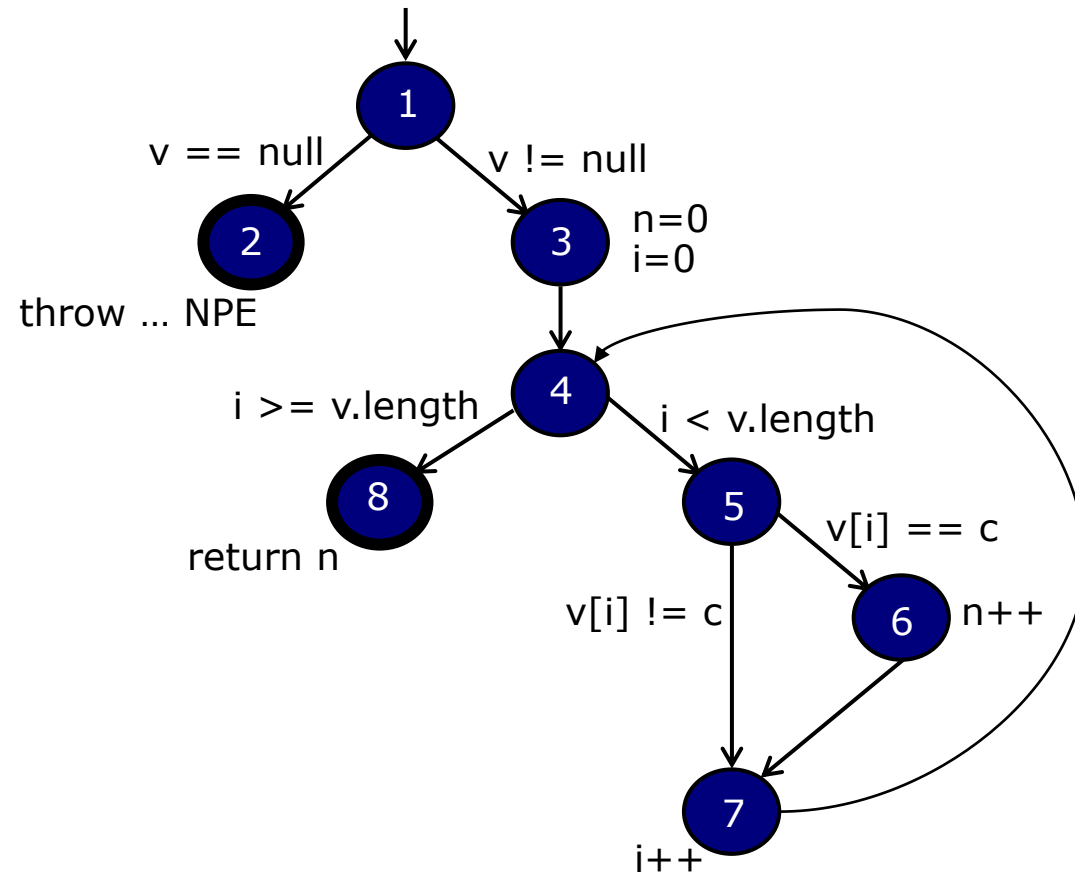
EC satisfied by $\{t1, t2, t3\}$

Test case values (v,c)

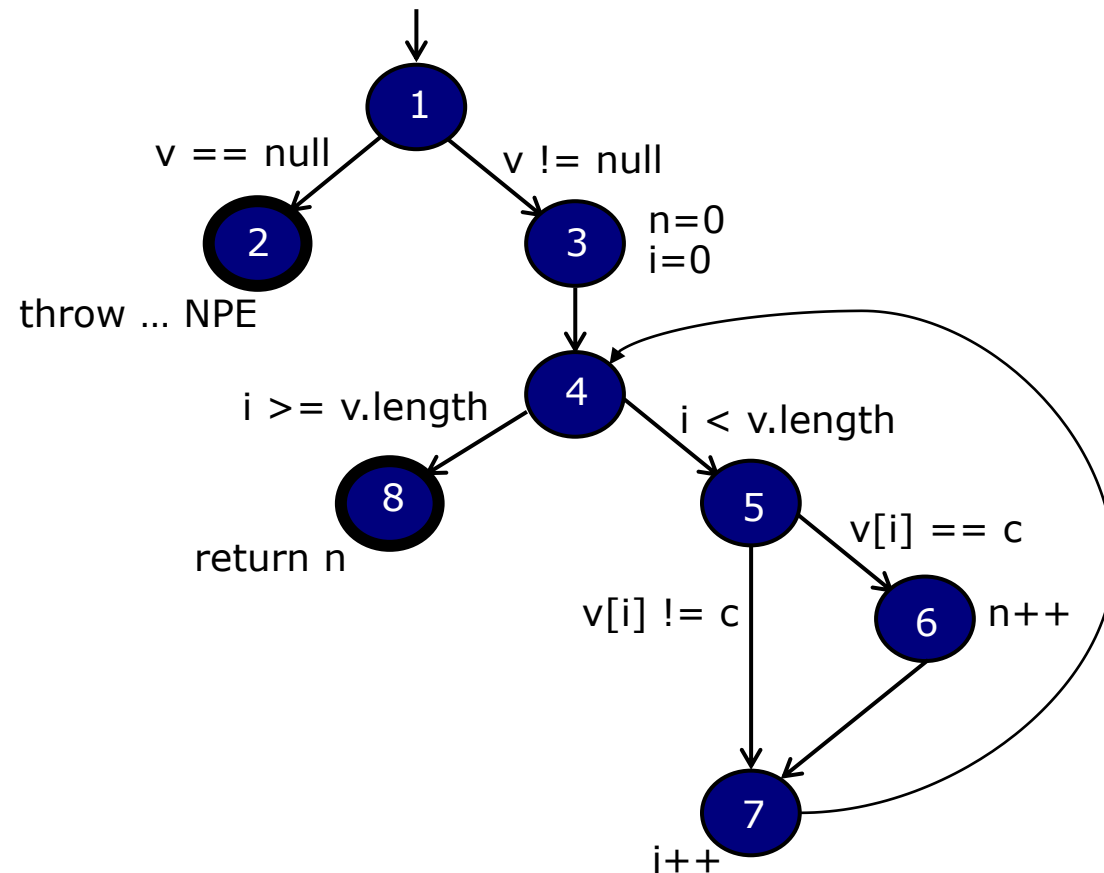
$t1 = (\text{null}, 'a')$, expected NPE

$t2 = (\{'a'\}, 'a')$, expected 1

$t3 = (\{'x'\}, 'a')$, expected 0



Applying Edge-Pair Coverage (EPC)



Test requirements

TR = {(1,2), (1,3,4), (3,4,8),
(3,4,5), (4,5,6), (4,5,7),
(5,6,7), (5,7,4), (6,7,4),
(7,4,5), (7,4,8)}

Test paths

t1 = [1,2]

t2 = [1,3,4,8]

t3 = [1,3,4,5,7,4,5,6,7,4,8]

EPC satisfied by {t1, t2, t3}

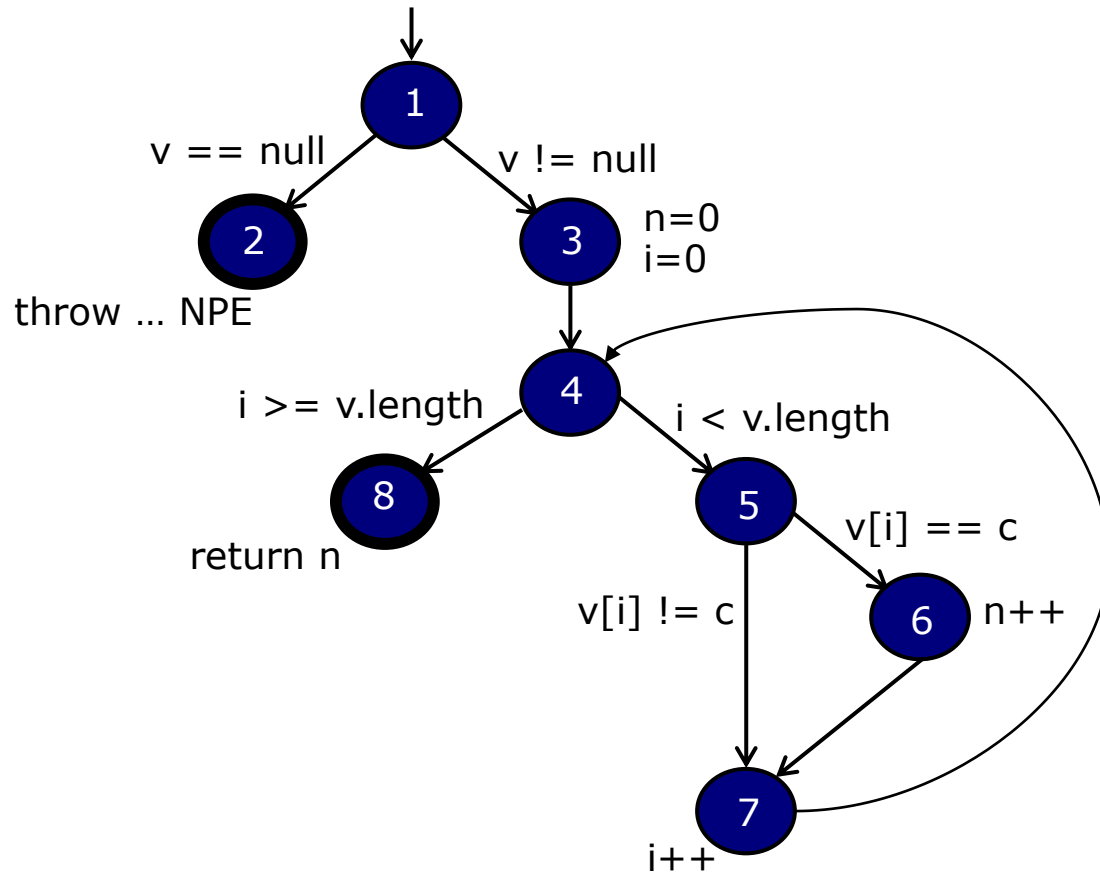
Test case values (v,c)

t1 = (null, 'a'), expected NPE

t2 = ({}, 'a'), expected 0

t3 = ({'x','a'}, 'a'), expected 1

Applying Prime Path Coverage



Deriving prime paths

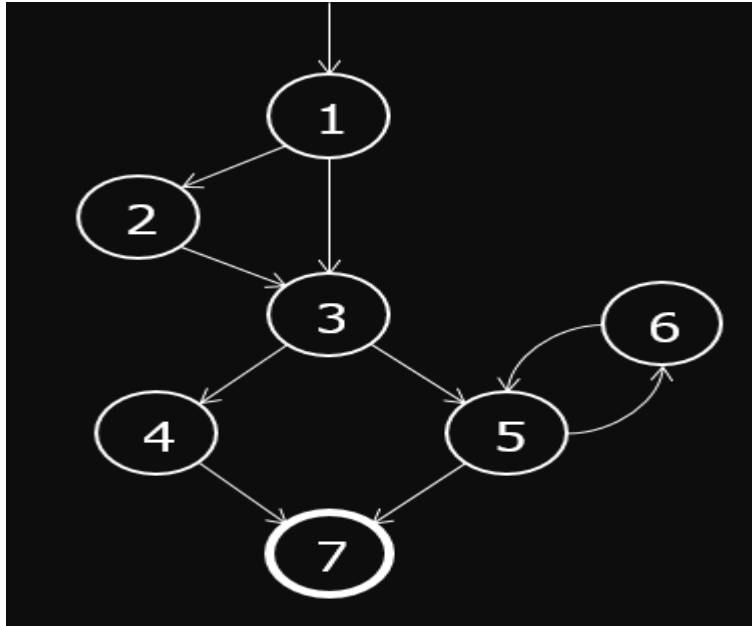
- Enumerate all simple paths of length 0, 1, 2, 3, ... until no more simple paths are found
- Pick the prime paths among all derived simple paths
- Notes: (1) Simple path: Path from node n_i to n_j that is **no internal loops**. (2) Prime Path is simple path that is **not subpath** of any other simple path

Recap: Simple Paths

Path from node n_i to n_j that is **no internal loops**

- A path from n_i to n_j is simple if no node appears more than once in the path (first and last nodes may be identical)
- A loop is a simple path

List simple paths: 31 simple paths



Subpaths of other simple paths → avoid these

[1,2,3,4,7], [1,2,3,5,7], [1,2,3,5,6],

[1,2,3,4], [1,2,3,5],

[1,3,4,7], [1,3,5,7], [1,3,5,6],

[2,3,4,7], [2,3,5,7], [2,3,5,6],

[1,2,3], [1,3,4], [1,3,5],

[2,3,4], [2,3,5],

[3,4,7], [3,5,7], [3,5,6],

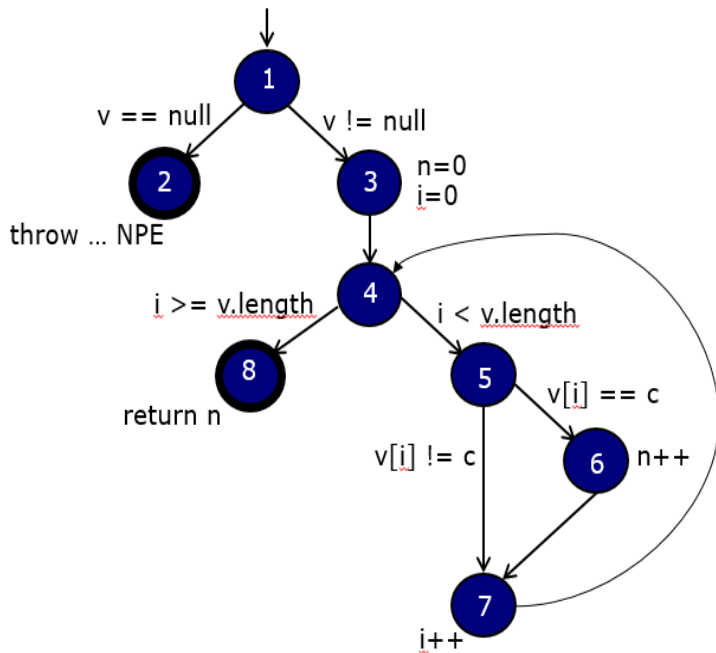
[5,6,5],

[6,5,6], [6,5,7],

[1,2], [1,3], [2,3], [3,4], [3,5],

[4,7], [5,7], [5,6], [6,5]

Applying Prime Path Coverage



! – cannot be extended
* – is a cycle

[1]
[2]!
[3]
[4]
[5]
[6]
[7]
[8]!

[1,2]!
[1,3]
[3,4]
[4,5]
[4,8]!
[5,6]
[5,7]
[6,7]
[7,4]

[1,3,4]
[3,4,5]
[3,4,8]!
[4,5,6]
[4,5,7]
[5,6,7]
[5,7,4]
[6,7,4]
[7,4,5]
[7,4,8]!

[1,3,4,5]
[1,3,4,8]!
[3,4,5,6]
[3,4,5,7]!
[4,5,6,7]
[4,5,7,4]*
[5,6,7,4]
[5,6,7,4]*
[5,7,4,5]*
[5,7,4,8]!
[6,7,4,5]
[6,7,4,8]!
[7,4,5,6]
[7,4,5,7]*

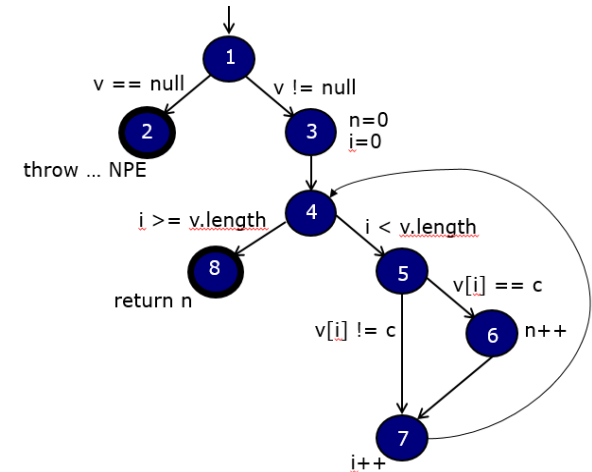
[1,3,4,5,6]
[1,3,4,5,7]!
[3,4,5,6,7]!
[4,5,6,7,4]*
[5,6,7,4,5]*
[5,6,7,4,8]!
[6,7,4,5,6]*
[7,4,5,6,7]*

[1,3,4,5,6,7]!

Applying Prime Path

Coverage

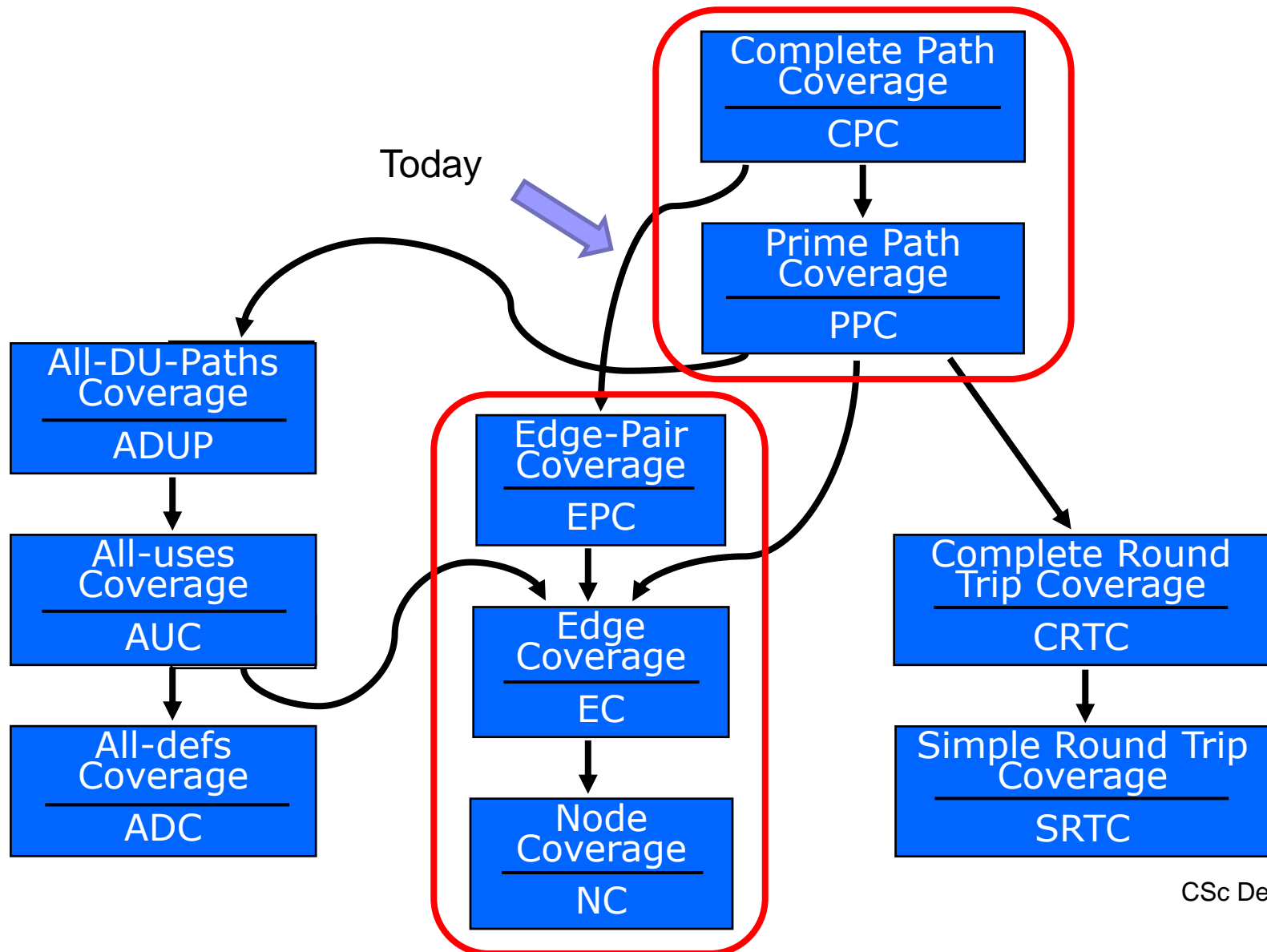
Prime path	Covered by
[1,2]	t1
[1,3,4,8]	t2
[1,3,4,5,6,7]	t4, t5
[1,3,4,5,7]	t3
[4,5,7,4]	t3, t4
[4,5,6,7,4]	t3, t4, t5
[5,7,4,5]	t3
[5,7,4,8]	t4
[5,6,7,4,5]	t4, t5
[5,6,7,4,8]	t3, t5
[6,7,4,5,6]	t5
[7,4,5,7]	t4
[7,4,5,6,7]	t3, t5



	Test paths	Test case values (v,c)	Expected values
t1	[1,2]	(null, 'a')	NPE
t2	[1,3,4,8]	({}, 'a')	0
t3	[1,3,4,5,7,4,5,6,7,4,8]	({'x', 'a'}, 'a')	1
t4	[1,3,4,5,6,7,4,5,7,4,8]	({'a', 'x'}, 'a')	1
t5	[1,3,4,5,6,7,4,5,6,7,4,8]	({'a', 'a'}, 'a')	2

PPC satisfied by {t1, t2, t3, t4, t5}

Recap: Graph Coverage Criteria Subsumption



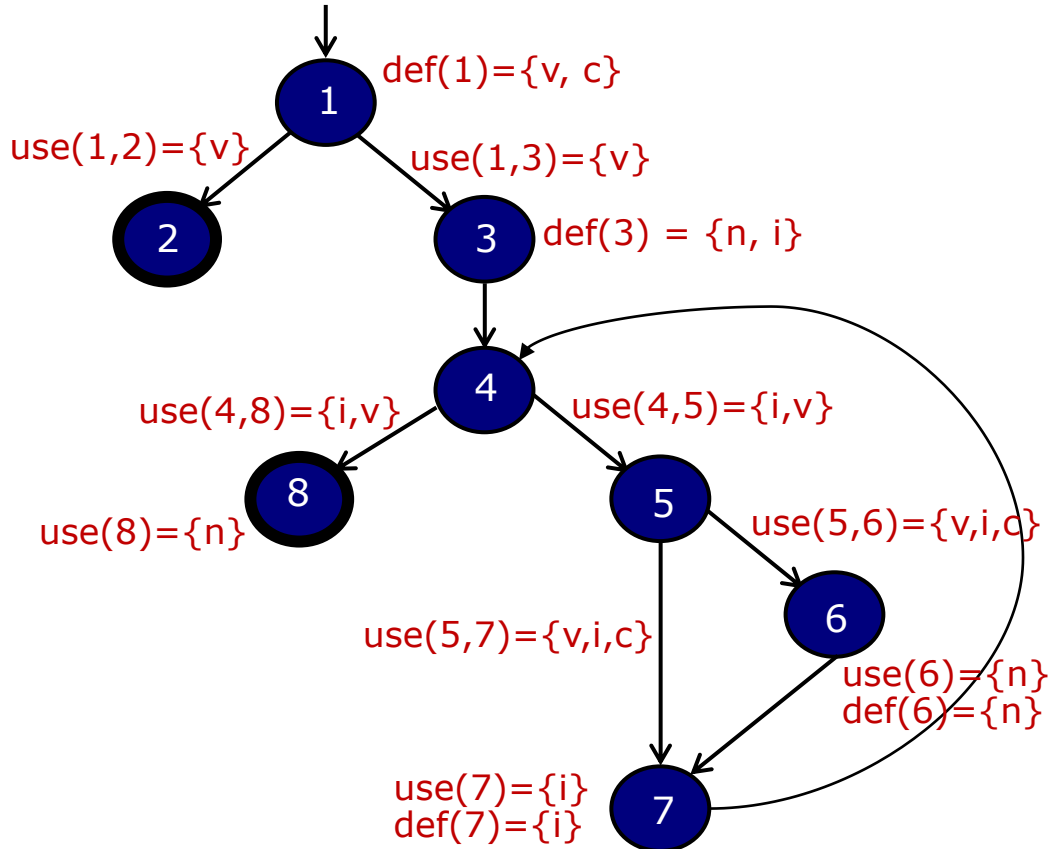
Recap: Handling Loops in Graphs

Attempts to deal with loops:

- 1970s: Execute cycles once ([5, 6, 5] in previous example)
- 1980s: Execute each loop, exactly once
- 1990s: Execute loops 0 times, once, more than once
- 2000s: Prime paths (touring, sidetrips, and detours)

Applying Data Flow Coverage

v and c are forwarded parameters



Deriving test requirements

- List all du-pairs
- Based on du-pairs, derive du-paths
- Must be def-clear paths
- All Defs Coverage (ADC)
 - For each def, at least one use must be reached
- All Uses Coverage (AUC)
 - For each def, all uses must be reached
- All DU-Paths Coverage (ADUPC)
 - For each def-use pair, all paths between defs and uses must be covered

DU-Pairs → DU-Paths

DU Pairs	
[1, (1, 2)]	Variable v
[1, (1, 3)]	
[1, (4, 8)]	
[1, (4, 5)]	
[1, (5, 6)]	
[1, (5, 7)]	
[1, (5, 7)]	Variable c
[1, (5, 6)]	
[3, 8]	Variable n
[3, 6]	
[6, 8]	
[6, 6]	
[3, 7]	Variable i
[7, 7]	
[3, (4, 8)]	
[3, (4, 5)]	
[3, (5, 6)]	
[3, (5, 7)]	
[7, (4, 8)]	
[7, (4, 5)]	
[7, (5, 6)]	
[7, (5, 7)]	

defs after
uses, these are
valid DU pairs

DU Paths	
[1, 3]	Variable v
[1, 2]	
[1, 3, 4, 8]	
[1, 3, 4, 5]	
[1, 3, 4, 5, 7]	
[1, 3, 4, 5, 6]	
[1, 3, 4, 5, 6]	Variable c
[1, 3, 4, 5, 7]	
[3, 4, 8]	Variable n
[3, 4, 5, 6]	
[6, 7, 4, 8]	
[6, 7, 4, 5, 6]	
[3, 4, 5]	Variable i
[3, 4, 8]	
[3, 4, 5, 6]	
[3, 4, 5, 7]	
[3, 4, 5, 6, 7]	
[7, 4, 5]	
[7, 4, 8]	
[7, 4, 5, 6]	
[7, 4, 5, 7]	
[7, 4, 5, 6, 7]	

ADC: DU-Paths → Test Paths

DU Paths

[1,3]	Variable v
[1,2]	
[1,3,4,8]	
[1,3,4,5]	
[1,3,4,5,7]	
[1,3,4,5,6]	Variable c
[1,3,4,5,6]	
[1,3,4,5,7]	Variable n
[3,4,8]	
[3,4,5,6]	
[6,7,4,8]	
[6,7,4,5,6]	Variable i
[3,4,5]	
[3,4,8]	
[3,4,5,6]	
[3,4,5,7]	
[3,4,5,6,7]	
[7,4,5]	
[7,4,8]	
[7,4,5,6]	
[7,4,5,7]	
[7,4,5,6,7]	

Test paths that satisfy All Defs Coverage

Variable	All Def Coverage
v	[1,3,4,8]
c	[1,3,4,5,6,7,4,8]
n	[1,3,4,8] [1,3,4,5,6,7,4,8]
i	[1,3,4,5,7,4,8] [1,3,4,5,7,4,5,7,4,8]

AUC: DU-Paths → Test Paths

DU Paths	
[1,3]	Variable v
[1,2]	
[1,3,4,8]	
[1,3,4,5]	
[1,3,4,5,7]	
[1,3,4,5,6]	Variable c
[1,3,4,5,6]	
[1,3,4,5,7]	Variable n
[3,4,8]	
[3,4,5,6]	
[6,7,4,8]	
[6,7,4,5,6]	Variable i
[3,4,5]	
[3,4,8]	
[3,4,5,6]	
[3,4,5,7]	
[3,4,5,6,7]	
[7,4,5]	
[7,4,8]	
[7,4,5,6]	
[7,4,5,7]	
[7,4,5,6,7]	

Test paths that satisfy All Uses Coverage

Variable	All Use Coverage
v	[1,2]
	[1,3,4,8]
	[1,3,4,5,7,4,8]
	[1,3,4,5,6,7,4,8]
c	[1,3,4,5,7,4,8]
	[1,3,4,5,6,7,4,8]
n	[1,3,4,8]
	[1,3,4,5,6,7,4,8]
	[1,3,4,5,6,7,4,5,6,7,4,8]
i	[1,3,4,5,7,4,8]
	[1,3,4,5,7,4,5,7,4,8]
	[1,3,4,8]
	[1,3,4,5,6,7,4,8]
	[1,3,4,5,7,4,8]
	[1,3,4,5,7,4,5,6,7,4,8]

ADUPC: DU-Paths → Test Paths

DU Paths	
[1,3]	Variable v
[1,2]	
[1,3,4,8]	
[1,3,4,5]	
[1,3,4,5,7]	
[1,3,4,5,6]	
[1,3,4,5,6]	Variable c
[1,3,4,5,7]	
[3,4,8]	Variable n
[3,4,5,6]	
[6,7,4,8]	
[6,7,4,5,6]	
[3,4,5]	Variable i
[3,4,8]	
[3,4,5,6]	
[3,4,5,7]	
[3,4,5,6,7]	
[7,4,5]	
[7,4,8]	
[7,4,5,6]	
[7,4,5,7]	
[7,4,5,6,7]	

Test paths that satisfy All DU-Paths Coverage

Variable	All DU Path Coverage
v	[1,3,4,8] [1,2] [1,3,4,5,7,4,8] [1,3,4,5,6,7,4,8]
c	[1,3,4,5,6,7,4,8] [1,3,4,5,7,4,8]
n	[1,3,4,8] [1,3,4,5,6,7,4,8] [1,3,4,5,6,7,4,5,6,7,4,8]
i	[1,3,4,5,7,4,8] [1,3,4,8] [1,3,4,5,6,7,4,8] [1,3,4,5,7,4,5,7,4,8] [1,3,4,5,7,4,8] [1,3,4,5,7,4,5,6,7,4,8]

Summary

- A common application of graph coverage criteria is to program source – control flow graph (CFG)
- Applying graph coverage criteria to control flow graphs is relatively straightforward
- A few decisions must be made to translate control structures into the graph
- We use basic blocks when assigning program statements to nodes while some tools assign each statement to a unique node.
 - Coverage is the same, although the bookkeeping will differ

McCabe's Cyclomatic Complexity & Code Coverage

McCabe's Cyclomatic Complexity

Cyclomatic complexity is a [software metric](#) used to indicate the complexity of a program. It is a quantitative measure of the number of linearly independent paths through a program's [source code](#).

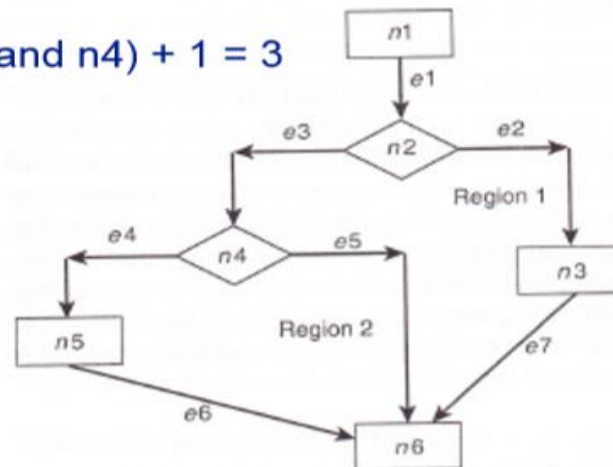
Source: https://en.wikipedia.org/wiki/Cyclomatic_complexity

McCabe's Cyclomatic Complexity

- Basic idea: program quality is directly related to the complexity of the control flow (branching)
- Computed from a control flow diagram
 - Cyclomatic complexity = $E - N + 2p$
 - E = number of edges of the graph
 - N = number of nodes of the graph
 - p = number of connected components (usually 1)
- Alternate computations:
 - number of binary decision + 1
 - number of closed regions + 1

McCabe's Cyclomatic Complexity Example

- Using the different computations:
 - 7 edges - 6 nodes + 2*1 = 3
 - 2 regions + 1 = 3
 - 2 binary decisions (n2 and n4) + 1 = 3



McCabe's Cyclomatic Complexity

- What does the number mean?
- Lower the Program's cyclomatic complexity, lower the risk to modify and easier to understand
- It's the maximum number of linearly independent paths through the flow diagram - used to determine the number of test cases needed to cover each path through the system
- The higher the number, the more risk exists (and more testing is needed)
 - 1-10 is considered low risk
 - greater than 50 is considered high risk

Structural Analysis ... Providing Actionable Metrics

The higher the complexity the more bugs. The more bugs the more security flaws

Cyclomatic Complexity & Reliability Risk

- 1 – 10 Simple procedure, little risk
- 11- 20 More Complex, moderate risk
- 21 – 50 Complex , high risk
- >50 Untestable, VERY HIGH RISK

Cyclomatic Complexity & Bad Fix Probability

- | | |
|-------------------|-----|
| • 1 – 10 | 5% |
| • 20 –30 | 20% |
| • > 50 | 40% |
| • Approaching 100 | 60% |

Essential Complexity (Unstructuredness) & Maintainability (future Reliability) Risk

- 1 – 4 Structured, little risk
- > 4 Unstructured, High Risk



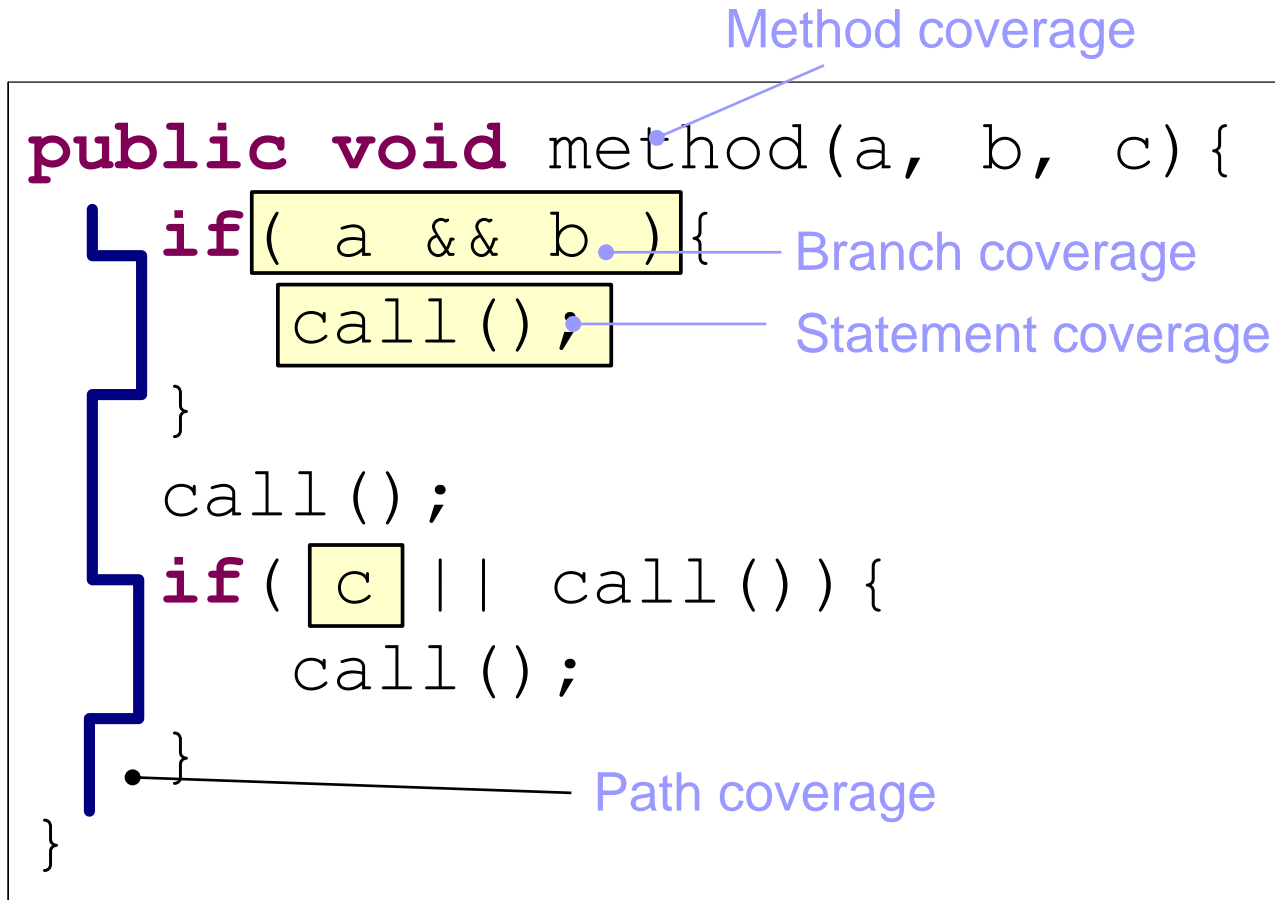
Code Coverage

- Code coverage is a measure to describe the degree to which the source code of a program is executed when a particular test suite runs
- Code Coverage is classified as a White box testing

Benefits

- Identify untested part of codebase
- Identify testing gaps or missing tests
- Identify the redundant/dead Code

Types of Coverage



Code Coverage

- ECLEmma Code Coverage offers covered instruction and missed instructions

Gradle Tasks		Coverage				
Element		Coverage	Covered Instructions	Missed Instructions	Total Instructions	
[-] CSC179A2Test		56.6 %	5,252	4,030	9,282	
[-] src		56.6 %	5,252	4,030	9,282	
[-] (default package)		56.6 %	5,252	4,030	9,282	
[-] Main.java		0.0 %	0	3,115	3,115	
[-] TestTriangleGetPerimeter.java		75.9 %	466	148	614	
[-] TestTriangleGetSideLengths.java		79.1 %	559	148	707	
[-] TestTriangleSetSideLengths.java		80.1 %	595	148	743	
[-] TestTriangleIsScalene.java		79.2 %	506	133	639	
[-] TestTriangleGetArea.java		78.8 %	464	125	589	
[-] TestTriangleIsImpossible.java		90.2 %	495	54	549	
[-] TestTriangleClassify.java		93.8 %	587	39	626	
[-] TestTriangleIsEquilateral.java		93.2 %	535	39	574	
[-] TestTriangleIsIsosceles.java		93.5 %	560	39	599	
[-] TestTriangleIsRightAngled.java		92.6 %	485	39	524	
[-] TriangleTestSuite.java		0.0 %	0	3	3	