

CSc 179 – Input Space Modeling Criteria

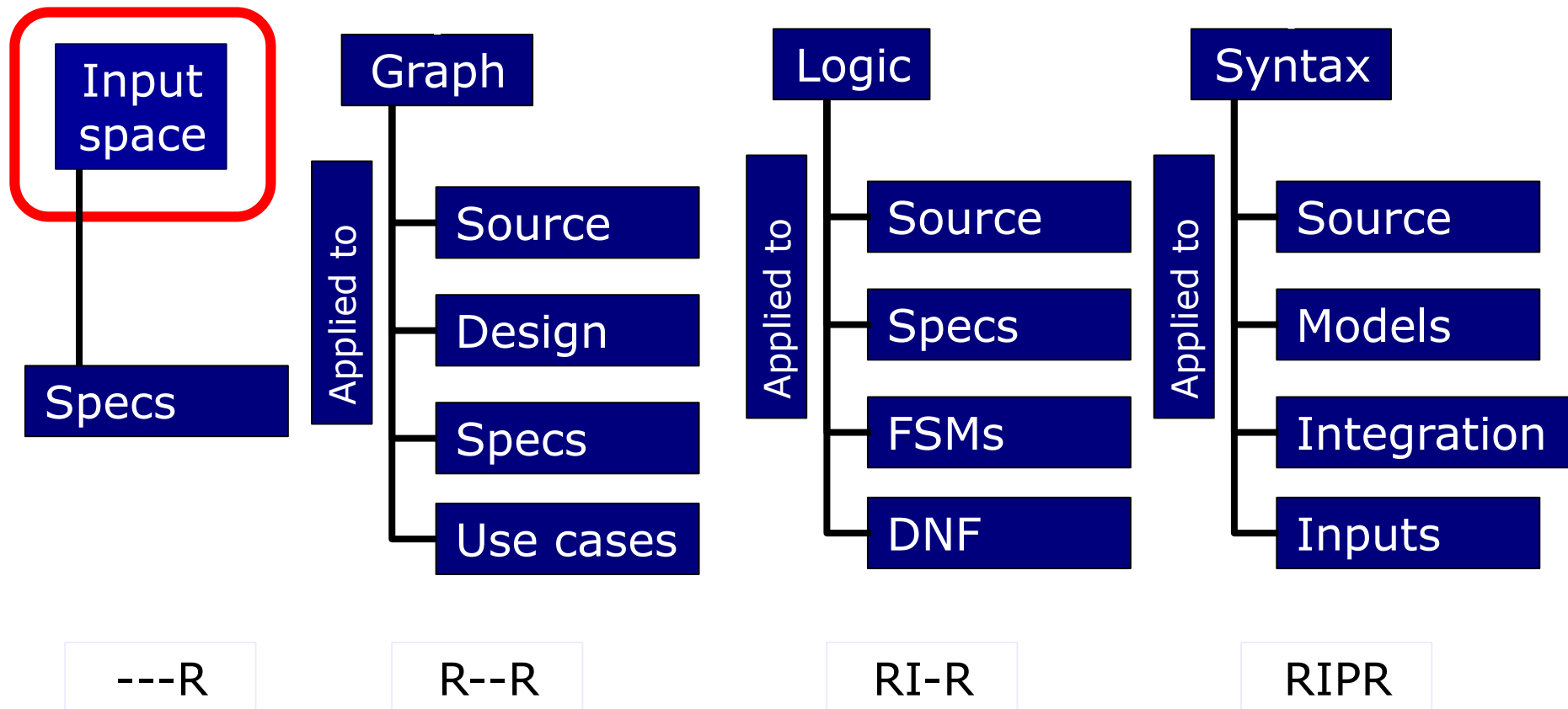
Credits:

AO – Ammann and Offutt, “Introduction to Software Testing,”
Ch. 6

University of Virginia (CS 4501 / 6501)

Structures for Criteria-Based Testing

Four structures for modeling software



Today's Objectives

- How should we consider multiple partitions or IDMs at the same time?
- What combinations of blocks should we choose values from?
- How many tests should we expect?

Applying ISP

Identify testable functions



Identify parameters, return types,
return values, exceptional behavior



Model the input domain



Input Domain Model (IDMs)

Apply a test criterion to choose
combinations of blocks



Test requirements (TRs)

Derive test values



Test cases

Task I: Model
input domain

The most creative
design step in using ISP

Task II: Choose
combinations
of values

Modeling the Input Domain

- The domain is scoped by the parameters
- Characteristics define the structure of the input domain
 - Characteristics should be based on the input domain – not program source

Two Approaches

Interface-based (simpler)

Develop characteristics from individual parameters

Functionality-based (harder))

Develop characteristics from a behavior view

Design characteristics



Partition each characteristic into blocks



Identify values of each block

Using Multiple Partitions or IDMs

- Some programs may have many parameters
- It is typical to create **several** small IDMs
 - Using a divide-and-conquer approach
- Some parameters may appear in more than one IDM
 - Leading to **overlap** IDMs
- Some IDMs may include specific constraints (such as invalid values)
- Multiple partitions or IDMs can be combined to create tests

How should we consider multiple partitions or IDMs at the same time?

Applying ISP

Identify testable functions



Identify parameters, return types,
return values, exceptional behavior



Model the input domain

Task I: Model
input domain

The most creative
design step in using ISP

Input Domain Model (IDMs)

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Test requirements (TRs)

Derive test values



Test cases

Task II: Choose
combinations
of values

Today's focus

Running Example: triang()

- Partition characteristics

Characteristic	b1	b2	b3	b4
C1) = length of Side1	greater than 1	equal to 1	equal to 0	less than 0
C2) = length of Side2	greater than 1	equal to 1	equal to 0	less than 0
C3) = length of Side3	greater than 1	equal to 1	equal to 0	less than 0

- For convenience, let's relabel the blocks

Characteristic	b1	b2	b3	b4
A = length of Side1	A1	A2	A3	A4
B = length of Side2	B1	B2	B3	B4
C = length of Side3	C1	C2	C3	C4

- Possible values

Characteristic	b1	b2	b3	b4
A = length of Side1	2	1	0	-1
B = length of Side2	2	1	0	-1
C = length of Side3	2	1	0	-1

Choosing Combinations of Values

- Once characteristics and partitions are defined, the next step is to choose which combinations of values to test
- Approaches to choose values
 - Select values randomly
 - Quality of tests depends on experience and expertise
 - Use coverage **criteria** – to choose **effective** subsets
 - Quality of tests depends on the strength of the criteria
- ISP Coverage criteria
 - All Combinations Coverage (ACoC)
 - Each Choice Coverage (EEC)
 - Pair-Wise Coverage (PWC)
 - Base Choice Coverage (BCC)
 - Multiple Base Choice Coverage (MBCC)

All Combinations (ACoC)

All combinations of blocks from all characteristics must be used

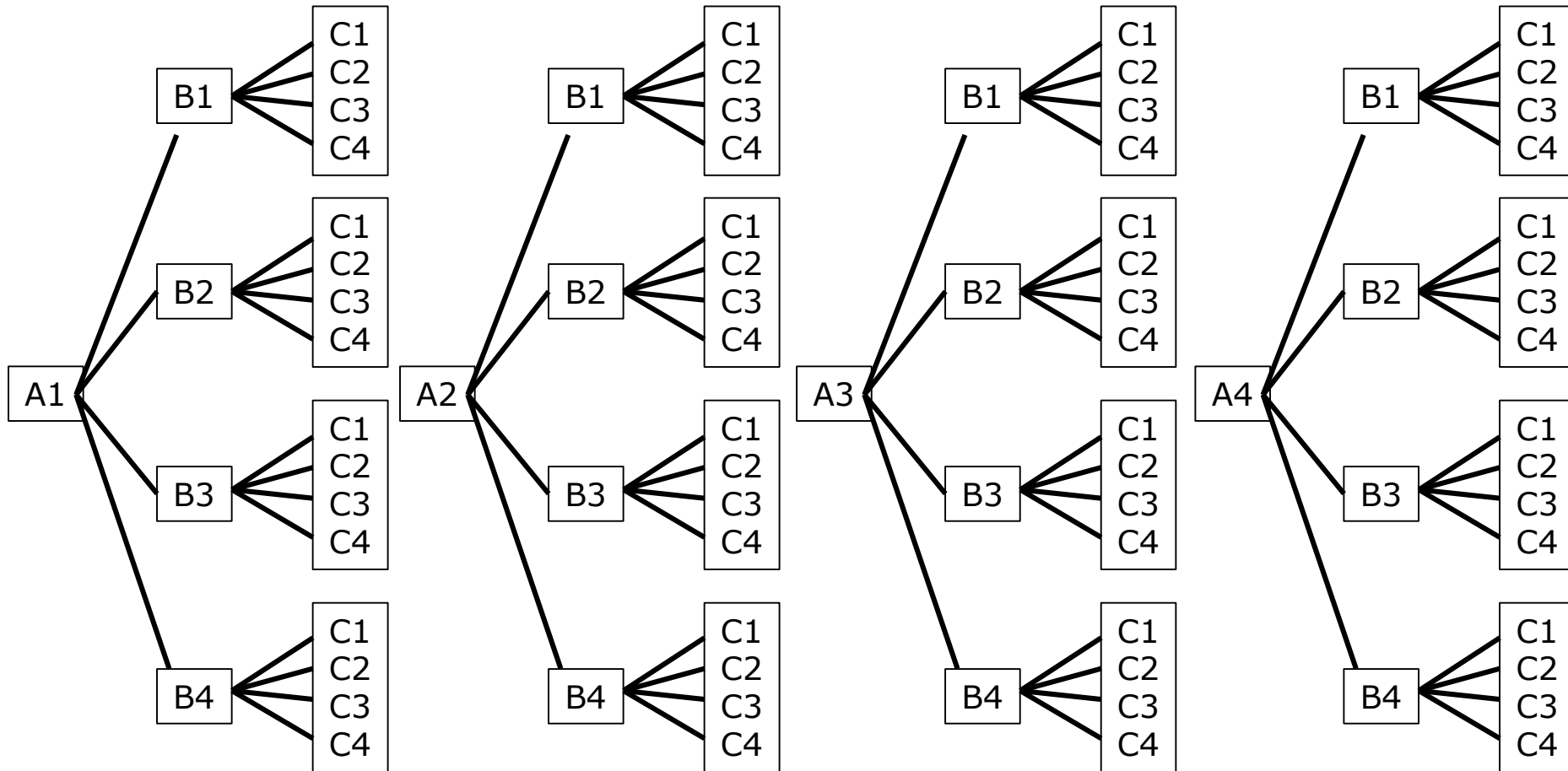
- Number of tests = $\prod_{i=1}^Q (B_i)$

Q = number partitions (or characteristics), B = number blocks

- More tests \rightarrow likely to find more faults
- More tests than necessary
- Impractical when more than two or three partitions are defined

ACoC - Example

- Applying ACoC to derive test requirements



ACoC – Example (cont)

- Test requirements: $4*4*4 = 64$ tests

(A1, B1, C1)	(A2, B1, C1)	(A3, B1, C1)	(A4, B1, C1)
(A1, B1, C2)	(A2, B1, C2)	(A3, B1, C2)	(A4, B1, C2)
(A1, B1, C3)	(A2, B1, C3)	(A3, B1, C3)	(A4, B1, C3)
(A1, B1, C4)	(A2, B1, C4)	(A3, B1, C4)	(A4, B1, C4)

(A1, B2, C1)	(A2, B2, C1)	(A3, B2, C1)	(A4, B2, C1)
(A1, B2, C2)	(A2, B2, C2)	(A3, B2, C2)	(A4, B2, C2)
(A1, B2, C3)	(A2, B2, C3)	(A3, B2, C3)	(A4, B2, C3)
(A1, B2, C4)	(A2, B2, C4)	(A3, B2, C4)	(A4, B2, C4)

(A1, B3, C1)	(A2, B3, C1)	(A3, B3, C1)	(A4, B3, C1)
(A1, B3, C2)	(A2, B3, C2)	(A3, B3, C2)	(A4, B3, C2)
(A1, B3, C3)	(A2, B3, C3)	(A3, B3, C3)	(A4, B3, C3)
(A1, B3, C4)	(A2, B3, C4)	(A3, B3, C4)	(A4, B3, C4)

(A1, B4, C1)	(A2, B4, C1)	(A3, B4, C1)	(A4, B4, C1)
(A1, B4, C2)	(A2, B4, C2)	(A3, B4, C2)	(A4, B4, C2)
(A1, B4, C3)	(A2, B4, C3)	(A3, B4, C3)	(A4, B4, C3)
(A1, B4, C4)	(A2, B4, C4)	(A3, B4, C4)	(A4, B4, C4)

This is almost certainly more than we need

Only 8 are valid
(all sides greater than zero)

ACoC – Example (cont)

Substituting test values

(2, 2, 2)	(1, 2, 2)	(0, 2, 2)	(-1, 2, 2)
(2, 2, 1)	(1, 2, 1)	(0, 2, 1)	(-1, 2, 1)
(2, 2, 0)	(1, 2, 0)	(0, 2, 0)	(-1, 2, 0)
(2, 2, -1)	(1, 2, -1)	(0, 2, -1)	(-1, 2, -1)

(2, 1, 2)	(1, 1, 2)	(0, 1, 2)	(-1, 1, 2)
(2, 1, 1)	(1, 1, 1)	(0, 1, 1)	(-1, 1, 1)
(2, 1, 0)	(1, 1, 0)	(0, 1, 0)	(-1, 1, 0)
(2, 1, -1)	(1, 1, -1)	(0, 1, -1)	(-1, 1, -1)

(2, 0, 2)	(1, 0, 2)	(0, 0, 2)	(-1, 0, 2)
(2, 0, 1)	(1, 0, 1)	(0, 0, 1)	(-1, 0, 1)
(2, 0, 0)	(1, 0, 0)	(0, 0, 0)	(-1, 0, 0)
(2, 0, -1)	(1, 0, -1)	(0, 0, -1)	(-1, 0, -1)

(2, -1, 2)	(1, -1, 2)	(0, -1, 2)	(-1, -1, 2)
(2, -1, 1)	(1, -1, 1)	(0, -1, 1)	(-1, -1, 1)
(2, -1, 0)	(1, -1, 0)	(0, -1, 0)	(-1, -1, 0)
(2, -1, -1)	(1, -1, -1)	(0, -1, -1)	(-1, -1, -1)

Substituting values
before refining TRs
→ Useless tests

Refining TRs by
eliminating
redundant and
infeasible tests

Always refine TRs
before deriving test
values

Different choices of values from the same block are equivalent from a testing perspective. Thus, we need only one value from each block

Each Choice (ECC)

One value from each block for each characteristic must be used in at least one test case

- Number of tests = $\text{Max}_{i=1}^Q (B_i)$

Q = number partitions (or characteristics), B = number blocks

- Flexibility in terms of how to combine the test values
- Fewer tests \rightarrow cheap but may be ineffective
- Not require values to be combined with other values
 \rightarrow weak criterion

ECC – Example

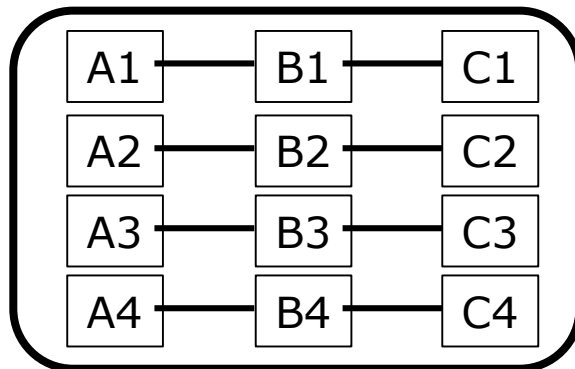
- Applying ECC to derive test requirements

Partitions for characteristic A = {A1, A2, A3, A4}

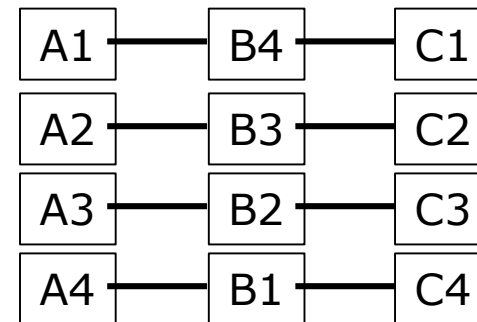
Partitions for characteristic B = {B1, B2, B3, B4}

Partitions for characteristic C = {C1, C2, C3, C4}

Possible combination



Another possible combination



ECC – Example (cont)

- Test requirements: Max number of blocks = 4

(A1, B1, C1)

(A2, B2, C2)

(A3, B3, C3)

(A4, B4, C4)

- Substituting values – test cases

(2, 2, 2)

(1, 1, 1)

(0, 0, 0)

(-1, -1, -1)

What are missing?

Testers sometimes recognize that certain values are important. To strengthen ECC, domain knowledge of the program must be incorporated

– *What is the most important block for each partition?*

Pair-Wise (PWC)

A value from each block for each characteristic must be combined with a value from every block for each other characteristic

- Number of tests = $(\text{Max}_{i=1}^Q (B_i)) * (\text{Max}_{j=1, j \neq i}^Q (B_j))$

Q = number partitions (or characteristics), B = number blocks

- Allow the same test case to cover more than one unique pair of values

PWC – Example 1: triang()

- Applying PWC to derive test requirements

Partitions for characteristic A = {A1, A2, A3, A4}

Partitions for characteristic B = {B1, B2, B3, B4}

Partitions for characteristic C = {C1, C2, C3, C4}

- Number of tests = $4 * 4 = 16$
- Test requirements
 - It is simpler to list the combinations in a table (see next slide)

Pair-Wise – Example 1

TR	A	B	C
1	A1	B1	C1
2	A1	B2	C2
3	A1	B3	C3
4	A1	B4	C4
5	A2	B1	C2
6	A2	B2	C3
7	A2	B3	C4
8	A2	B4	C1
9	A3	B1	C3
10	A3	B2	C4
11	A3	B3	C1
12	A3	B4	C2
13	A4	B1	C4
14	A4	B2	C1
15	A4	B3	C2
16	A4	B4	C3

Order characteristics in columns,
from max number of blocks

Fill the first column, repeat as
many times as the number of the
next max blocks

Fill the second column

Ensure each block of A pairs with
all possible blocks of B. Swap as
needed

Fill the third column

Ensure each block of B pairs with
all possible of blocks of C. Swap
as needed

Ensure each block of A pairs with
all possible blocks of C. Swap as
needed

Pair-Wise – Example 1

Substituting values – test cases

TC	A	B	C
1	2	2	2
2	2	1	1
3	2	0	0
4	2	-1	-1
5	1	2	1
6	1	1	0
7	1	0	-1
8	1	-1	2
9	0	2	0
10	0	1	-1
11	0	0	2
12	0	-1	1
13	-1	2	-1
14	-1	1	2
15	-1	0	1
16	-1	-1	0

TC = Test case

Base Choice (BCC)

A base choice block is chosen for each characteristic.

A base test is formed by using the base choice for each characteristic.

Subsequent tests are chosen by holding all but one base choice constant and using each non-base choice in each other characteristic.

- Number of tests = $1 + \sum_{i=1}^Q (B_i - 1)$

Q = number partitions (or characteristics), B = number blocks

- Use domain knowledge of the program
 - *What is the most important block for each partition?*
- Pick the base choice test, then add additional tests
- Test quality depends on the selection of the base choice

BCC – Example

- Applying BCC to derive test requirements

Partitions for characteristic A = {A1, A2, A3, A4}

Partitions for characteristic B = {B1, B2, B3, B4}

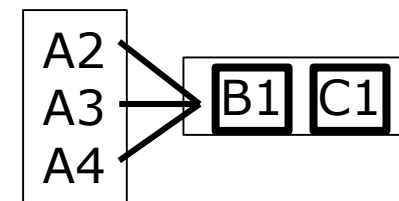
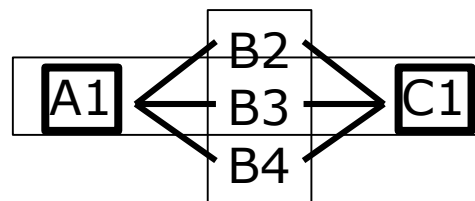
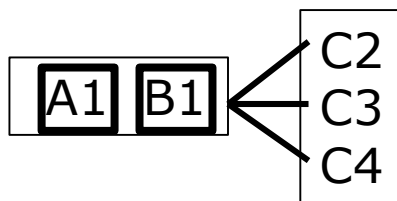
Partitions for characteristic C = {C1, C2, C3, C4}

Suppose **base choice blocks** are A1, B1, and C1

Then the **base choice test** is (A1, B1, C1)

Hold all but one base choice constant, use each non-base choice in each other characteristic

A1, B1, C1



BCC – Example (cont)

- Test requirements: $1 + 3 + 3 + 3 = 10$

(A1, B1, C1)	(A1, B1, C2)	(A1, B2, C1)	(A2, B1, C1)
Base	(A1, B1, C3)	(A1, B3, C1)	(A3, B1, C1)
	(A1, B1, C4)	(A1, B4, C1)	(A4, B1, C1)

- Substituting test values

(2, 2, 2)	(2, 2, 1)	(2, 1, 2)	(1, 2, 2)
Base	(2, 2, 0)	(2, 0, 2)	(0, 2, 2)
	(2, 2, -1)	(2, -1, 2)	(-1, 2, 2)

BCC – Notes

- The base test must be **feasible**
- Base choices can be
 - From an end-user point of view
 - Simplest
 - Smallest
 - First in some order
 - **Happy path** test
- The base choice is a crucial design decision as it affects the quality of testing
 - Test designers should always document why the choices were made

Testers sometimes have multiple logical base choices

Multiple Base Choice (MBCC)

At least one, and possible more, base choice blocks are chosen from each characteristic.

Base tests are formed by using each base choice for each characteristic at least once.

Subsequent tests are chosen by holding all but one base choice constant for each base test and using each non-base choice in each other characteristic.

- Number of tests = $M + \sum_{i=1}^Q (M * (B_i - m_i))$

M = number base tests

m_i = number base choices for each characteristic

Q = number partitions (or characteristics)

B = number blocks

MBCC – Example

- Applying MBCC to derive test requirements

Partitions for characteristic A = {A1, A2, A3, A4}

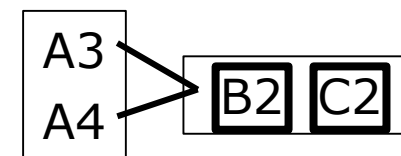
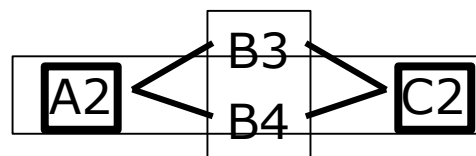
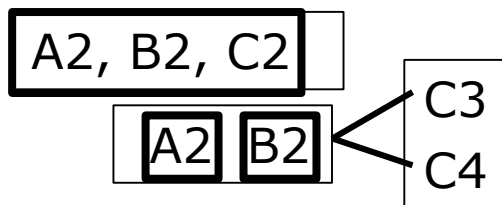
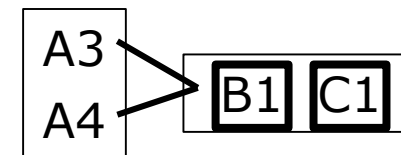
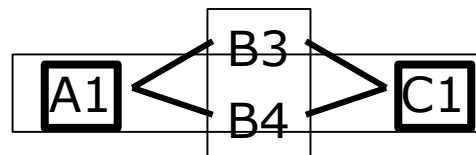
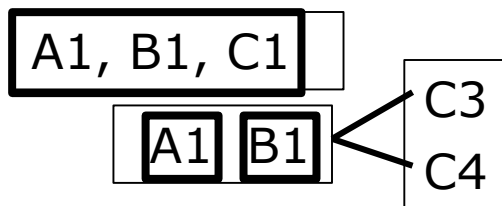
Partitions for characteristic B = {B1, B2, B3, B4}

Partitions for characteristic C = {C1, C2, C3, C4}

Suppose **base choice blocks** are A1, B1, C1 and A2, B2, C2

Then the **base choice tests** are (A1, B1, C1) and (A2, B2, C2)

Hold all but one base choice constant for each base test, use each non-base choice in each other characteristic



MBCC – Example (cont)

- Test requirements: $2 + (2 * (4 - 2)) + (2 * (4 - 2)) + (2 * (4 - 2)) = 14$

(A1, B1, C1)

Base

(A1, B1, C3)

(A1, B1, C4)

(A1, B3, C1)

(A1, B4, C1)

(A3, B1, C1)

(A4, B1, C1)

(A2, B2, C2)

Base

(A2, B2, C3)

(A2, B2, C4)

(A2, B3, C2)

(A2, B4, C2)

(A3, B2, C2)

(A4, B2, C2)

- Substituting test values

(2, 2, 2)

Base

(2, 2, 0)

(2, 2, -1)

(2, 0, 2)

(2, -1, 2)

(0, 2, 2)

(-1, 2, 2)

(1, 1, 1)

Base

(1, 1, 0)

(1, 1, -1)

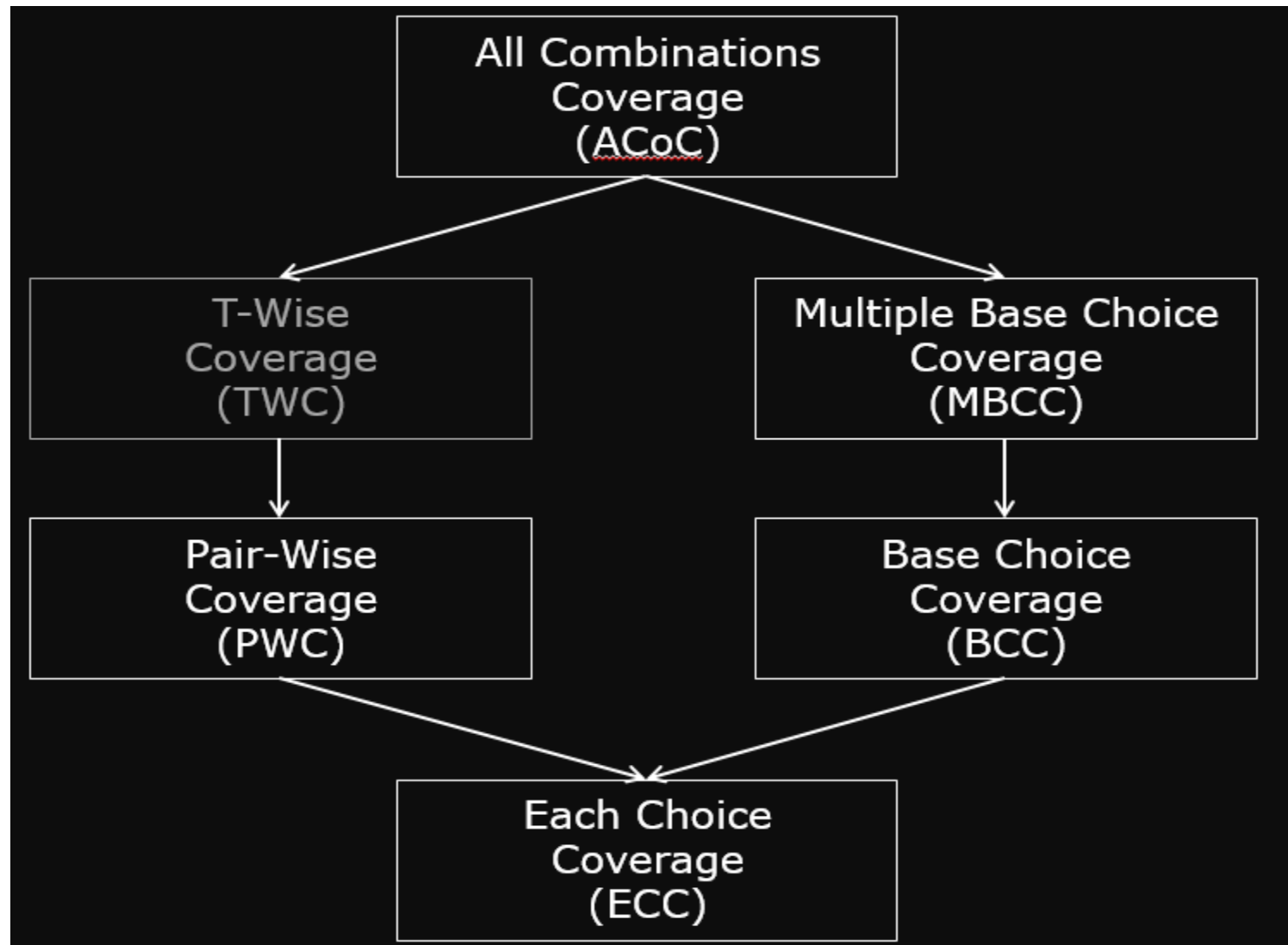
(1, 0, 1)

(1, -1, 1)

(0, 1, 1)

(-1, 1, 1)

ISP Coverage Criteria Subsumption



Constraints Among Characteristics

- Some combinations of blocks are **infeasible**
 - A triangle cannot be “less than 0” and “scalene” at the same time
- These are represented as **constraints** among blocks
- Two kinds of constraints
 - A block from one characteristic **cannot be** combined with a block from another characteristic
 - A block from one characteristic must be combined with a **specific** block from another characteristic
- Handling constraints depends on the criterion used
 - **ACoC** – drop the infeasible pairs
 - **ECC** – change a value to find a feasible combination
 - **BCC, MBCC** – change a value to another non-base choice to find a feasible combination

Handling Constraints - Example

```
# Return index of the first occurrence of a letter in string,  
# Otherwise, return -1
```

```
def get_index_of(string, letter):
```

Characteristic	b1	b2	b3
C1 = number of occurrence of letter in string	0	1	> 1
C2 = letter occurs first in string	True	False	
Invalid combinations: (C1b1)			

If a letter cannot be found in string,
it cannot appear first in string

Summary

- Sometimes testers decide to use more than one IDM
- Once characteristics and partitions are defined, criteria are used to choose the combinations of test values
- Different criteria provide different coverage and result in different number of test requirements (and hence testing effort)
- ACoC may not be practical
- ECC may be too simplistic and ineffective
- BCC and MBCC pick meaningful blocks → "*do smarter*"

ISP testing is simple, straightforward, effective,
and widely used