

# Discovery of Parkinson's disease states using machine learning and longitudinal data

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September 27, 2021

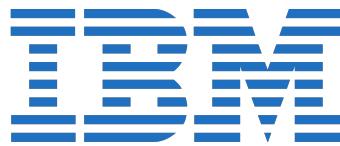
1. IBM Research, Center for Computational Health
2. University of Pittsburgh, Department of Neurology
3. Michael J. Fox Foundation

# Why Machine Learning?

- Key challenges in PD
  - Incomplete biological understanding
  - Heterogeneity in symptom presentation and progression
  - Desire for personalized patient management and prognostication
  - Noisy, varied, and possibly qualitative measurements
- Key advantages of machine learning
  - Ability to discover complex patterns
  - Opportunity to incorporate prior knowledge
  - Power to synthesize large amounts of data
  - Possibility to incorporate uncertainty estimates

# Disease progression modeling

IBM, Machine Learning



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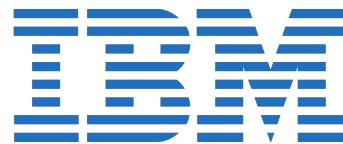
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# Disease progression modeling

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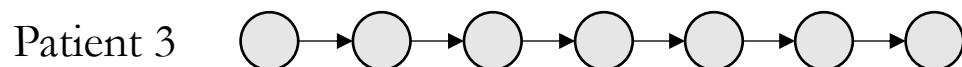
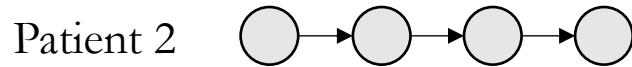
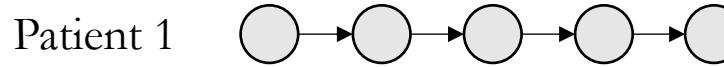
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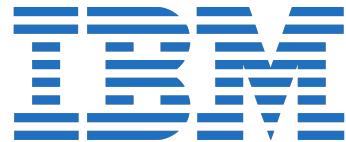
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Time →

# Disease progression modeling

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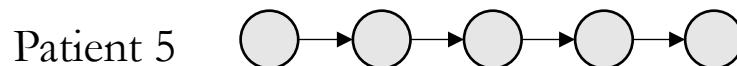
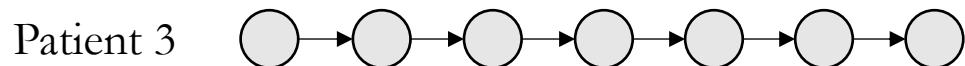
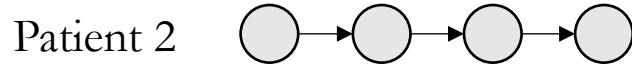
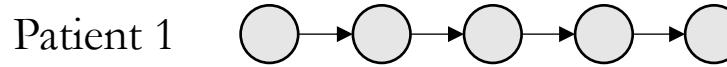
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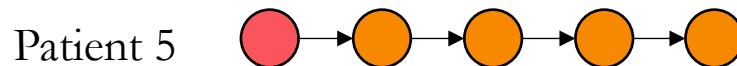
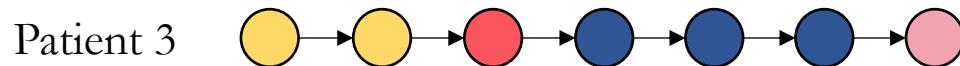
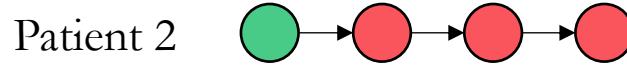
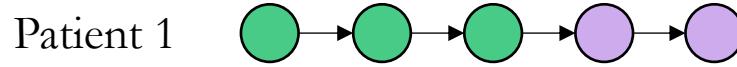
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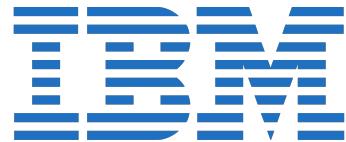
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Time →

# Disease progression modeling

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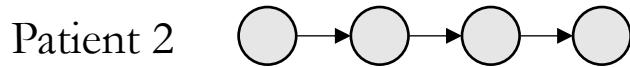
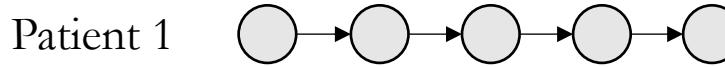
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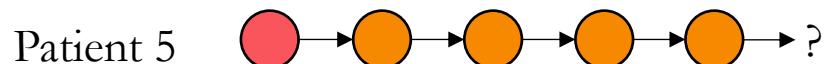
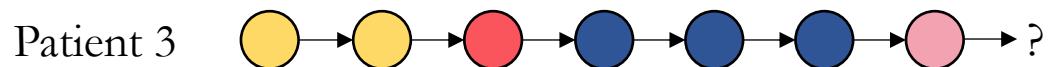
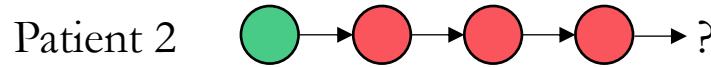
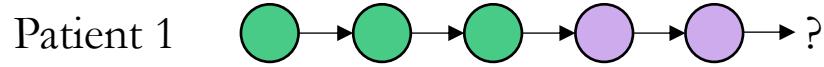
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Time →

# Disease progression modeling

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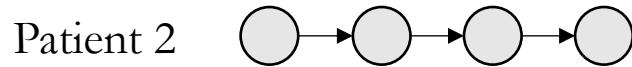
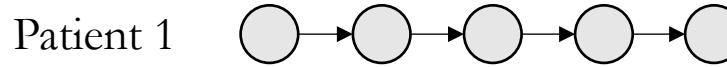
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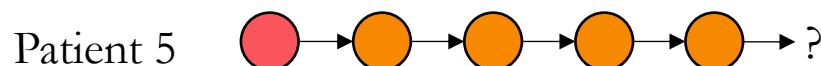
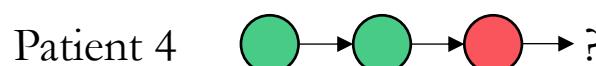
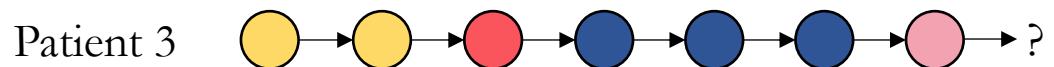
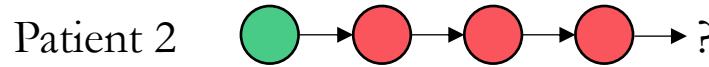
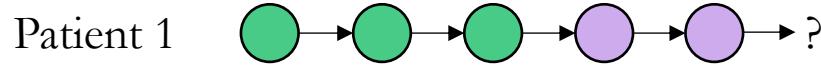
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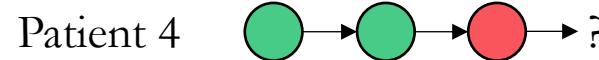
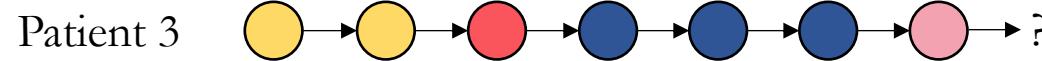
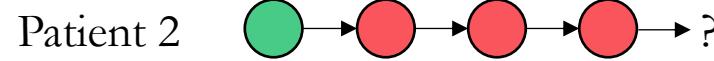
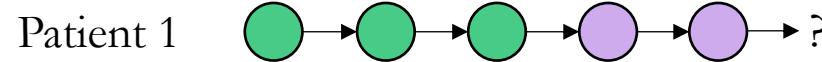
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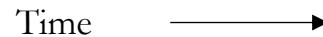
Patient \* A question mark enclosed in a circle, indicating an unknown or predicted state for Patient \*.

Time →

# Disease progression modeling



Patient \*   

Time   

## Patient management

Answer questions such as:

- How quickly will disease progress?
- What types of therapies will be most useful for me?
- When should I schedule my next visit?

## Clinical trial design

Patient 1   

Patient 2   

Patient 4   

# Past work

## Expert opinion

Three subtypes:

- Postural instability and gait dominant
- Tremor dominant
- Indeterminant

**3.10 GAIT**

Instructions to examiner: Testing gait is best performed by having the patient walking away from and towards the examiner so that both right and left sides of the body can be easily observed.

**3.11 FREEZING OF GAIT**

Instructions to examiner: While assessing gait, also assess for the presence of any gait freezing episodes.

**3.12 POSTURAL STABILITY**

Instructions to examiner: The test examines the response to sudden body displacement produced by a quick, forceful pull on the shoulders while the patient is standing erect with eyes open and feet shoulder width apart and parallel to each other. Test retropulsion. Stand behind the patient and instruct the patient on what is about to happen. Explain that s/he is allowed to take a step backwards to avoid falling. There should be a solid wall behind the examiner, at least 1-2 meters away to allow for the observation of the number of retropulsive steps. The first pull is an instructional demonstration and is purposely milder and not rated. The second time the shoulders are pulled briskly and forcefully towards the back. The examiner should observe the number of steps the patient takes to recover from a fall or fall backwards. The examiner needs to be ready to catch the patient, but must stand sufficiently back so as to allow enough room for the patient to take several steps to recover independently. Do not allow the patient to flex the body abnormally forward in anticipation of the pull. Observe for the number of steps backwards or falling. Up to and including two steps for recovery is considered normal, so abnormal ratings begin with three steps. If the patient fails to understand the test, the examiner can repeat the instructions so that the rating is based on an assessment that the examiner fully respects the patient's limitations rather than misunderstanding or lack of preparedness. Observe standing posture for item 3.13.

0: Normal:	No problems. Recovers with one or two steps.
1: Slight:	3-5 steps, but subject recovers unaided.
2: Mild:	More than 5 steps, but subject recovers unaided.
3: Moderate:	Stands safely, but with absence of postural response; falls if not caught by examiner.
4: Severe:	Very unstable, tends to lose balance spontaneously or with just a gentle pull on the shoulders.

**3.13 RETROPROLIFATION**

Instructions to examiner: This item receives one rating for all rest tremor and focuses on the constancy of rest tremor during the examination period when different body parts are variously at rest. It is rated purposefully at the end of the examination.

**3.14 CONSTANCY OF REST TREMOR**

Instructions to examiner: This item receives one rating for all rest tremor and focuses on the constancy of rest tremor during the examination period when different body parts are variously at rest. It is rated purposefully at the end of the examination.

**3.15 POSTURAL TREMOR OF THE HANDS**

Instructions to examiner: All tremor, including re-emergent rest tremor, that is present in this posture is rated.

**3.16 KINETIC TREMOR OF THE HANDS**

Instructions to examiner: This is tested by the finger-to-nose maneuver. With the arm starting from the shoulder, the patient is instructed to reach outstretched to touch the examiner's nose with the tip of the index finger. The examiner observes the rate and rhythm of tremor in the patient's hand as it reaches the nose. The patient should then return the hand to the shoulder.

**3.17 REST TREMOR AMPLITUDE**

Instructions to examiner: This and the next item have been placed purposefully at the end of the examination to follow the rate and rhythm observations on rest tremor that may occur at any time during the exam, including when quietly sitting, during walking, and during activities when some body parts are moving but others are at rest. Score the maximum amplitude that is seen at any time as the final score. Rate only the amplitude and not persistence or the intermittency of the tremor.

As part of this testing, the patient should sit quietly in a chair with the hands placed on the arms of the chair (not in the lap) and the feet comfortably spread on the floor for 10 seconds with no other movement. Rest tremor is assessed separately for all four limbs and also for the lip/jaw. Rate only the maximum amplitude that is seen at any time as the final rating.

Extremity ratings:

0: Normal:	No tremor.
1: Slight:	< 1 cm in maximal amplitude.
2: Mild:	≥ 1 cm but < 3 cm in maximal amplitude.
3: Moderate:	≥ 3 cm but < 10 cm in maximal amplitude.
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# Past work

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Instructions to examiner: This item receives one rating for all rest tremor and focuses on the constancy of rest tremor during the examination period when different body parts are variously at rest. It is rated purposefully at the end of the rating.

**3.15 POSTURAL TREMOR OF THE HANDS**  
Instructions to examiner: All tremor, including re-emergent rest tremor, that is present in this posture is rated.

0: Patient is able to reach outstretched arms to the side and behind the head.	1: Patient is able to reach outstretched arms to the side and behind the head.
2: Patient is able to reach outstretched arms to the side and behind the head.	3: Patient is able to reach outstretched arms to the side and behind the head.
4: Patient is able to reach outstretched arms to the side and behind the head.	5: Patient is able to reach outstretched arms to the side and behind the head.

**3.16 KINETIC TREMOR OF THE HANDS**  
Instructions to examiner: This is tested by the finger-to-nose maneuver. With the arm starting from the side, the patient reaches the nose with the index finger. The examiner observes the tremor.

**3.17 REST TREMOR AMPLITUDE**  
Instructions to examiner: This and the next item have been placed purposefully at the end of the examination to follow the rate and the observations on rest tremor that may occur at any time during the exam, including when quietly sitting, during walking, and during activities when some body parts are moving but others are at rest. Score the maximum amplitude that is seen at any time as the final score. Rate only the amplitude and not persistence or the intermittency of the tremor.

As part of this testing, the patient should sit quietly in a chair with the hands placed on the arms of the chair (not in the lap) and the feet comfortably spread on the floor for 10 seconds with no other movement. Rest tremor is assessed separately for all four limbs and also for the l/p/j/w. Rate only the maximum amplitude that is seen at any time as the final rating.

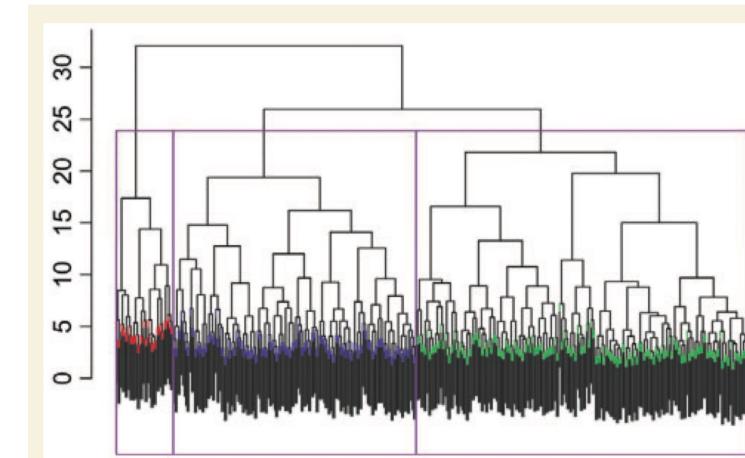
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## Machine-learning based approaches

Three subtypes:

- Mild motor-predominant
- Diffuse malignant
- Intermediate



**Figure 1 Dendrogram of the final hierarchical cluster solution in the PPMI population.** Green = mild motor-predominant; blue = intermediate; red = diffuse malignant.

# Past work

## Expert opinion

Three subtypes:

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- Tremor dominant
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**3.18 CONSTANCY OF REST TREMOR**  
Instructions to examiner: This item receives one rating for all rest tremor and focuses on the constancy of rest tremor during the examination period when different body parts are variously at rest. It is rated purposefully at the end of the rating.

**3.15 POSTURAL TREMOR OF THE HANDS**  
Instructions to examiner: All tremor, including re-emergent rest tremor, that is present in this posture is rated.

0: Patient is able to reach outstretched arms to the side and back without difficulty.
1: Patient is able to reach outstretched arms to the side and back with some difficulty.
2: Patient is able to reach outstretched arms to the side and back with considerable difficulty.
3: Patient is unable to reach outstretched arms to the side and back.

**3.16 KINETIC TREMOR OF THE HANDS**  
Instructions to examiner: This is tested by the finger-to-nose maneuver. With the arm starting from the side, the patient is asked to touch the tip of the nose with the tip of the index finger as rapidly as possible.

**3.17 REST TREMOR AMPLITUDE**  
Instructions to examiner: This and the next item have been placed purposefully at the end of the examination to follow the rate and observations on rest tremor that may occur at any time during the exam, including when quietly sitting, during walking, and during activities when some body parts are moving but others are at rest. Score the maximum amplitude that is seen at any time as the final score. Rate only the amplitude and not persistence or the intermittency of the tremor.

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Extremity ratings

0: Normal: No tremor.
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## Machine-learning based approaches

Four subtypes:

- Fast motor progression (1)
- Mild motor and non-motor disease (2)
- Severe motor disease, poor psychological well-being and sleep (3)
- Slow motor progression (4)

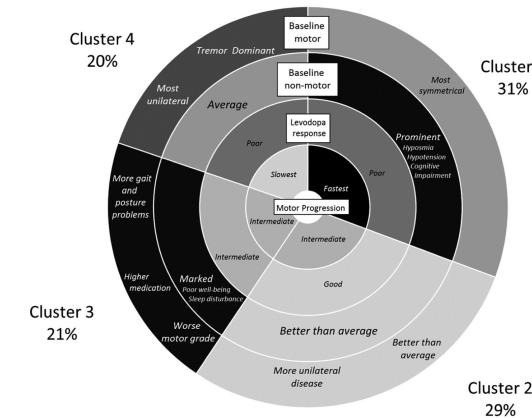


Figure 1 Important salient clinical features of the four clusters across the two cohorts where the percentages within each cluster are from the Tracking Parkinson's cohort.

# Analysis Goals

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- Particularly interested in discovering *disease states*

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Disease state definition: *discrete label* of a patient with two primary characteristics: a transition model which describes the probability of changing states and an observation model which describes the distribution of clinical measures associated with a state

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- Particularly interested in discovering *disease states*
- Account for *medications* which affect clinical presentation but do not affect disease course

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- Particularly interested in discovering *disease states*
- Account for *medications* which affect clinical presentation but do not affect disease course
- Allow for *personalized* deviations in symptom presentation and medication effects

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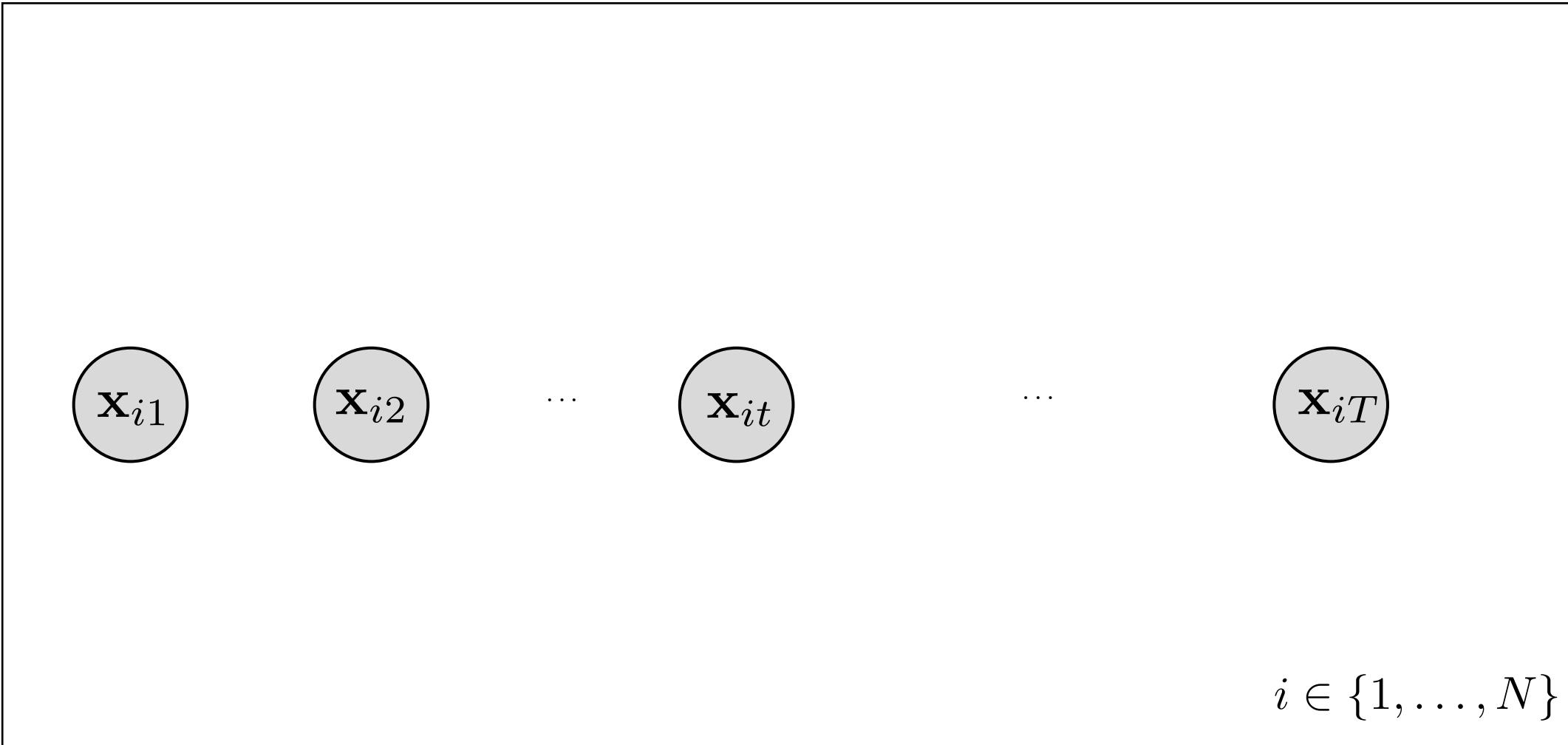
- Pre-process the data using a latent variable model
- Model progression using a Markov model, a specific type of probabilistic model
- Medications effect symptoms but not underlying disease progression

# Key Model Assumptions

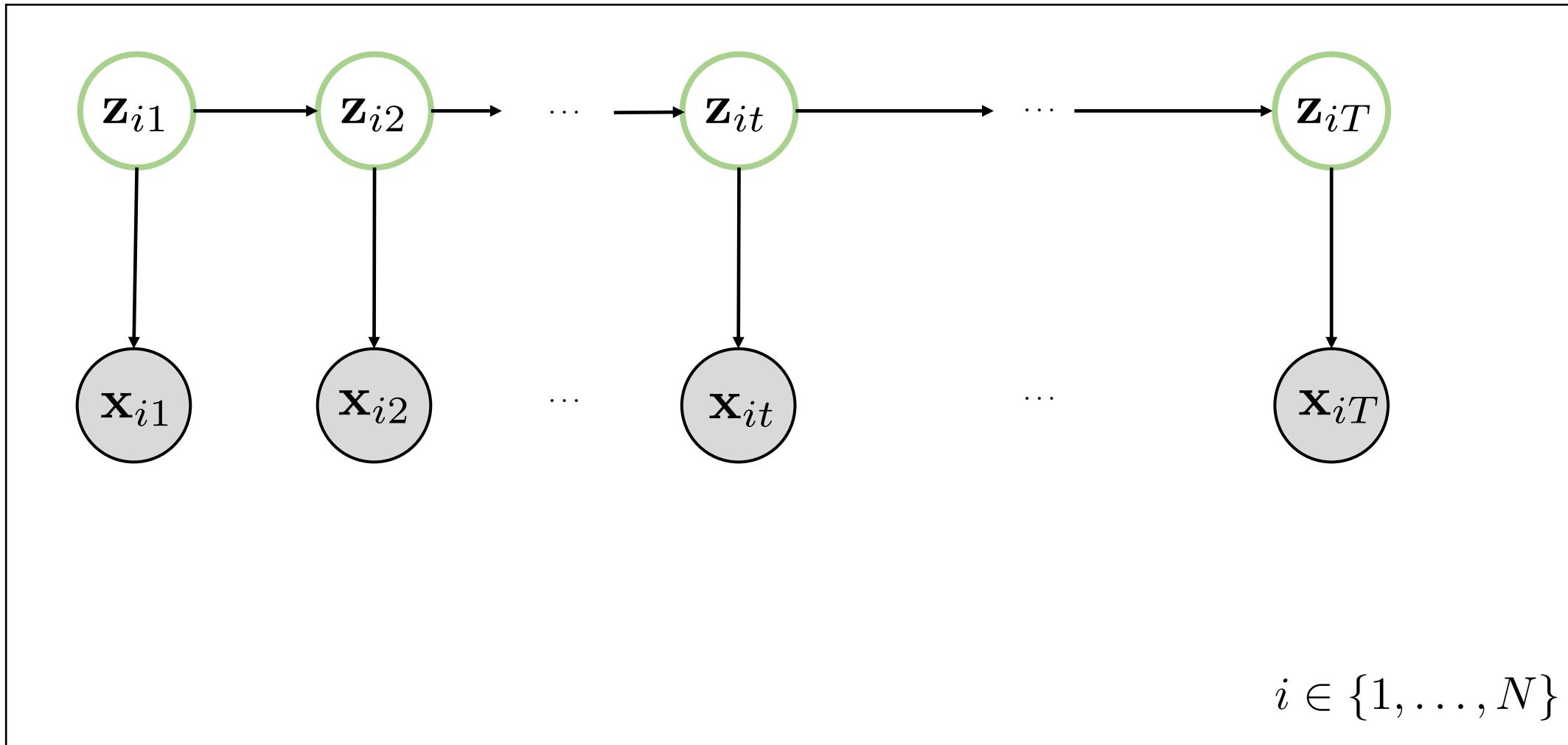
- Pre-process the data using a latent variable model
- Model progression using a Markov model, a specific type of probabilistic model
- Medications effect symptoms but not underlying disease progression
- Patients can only move progressively through states

To	1	2	3	4
From	1			
	2			
	3			
	4			

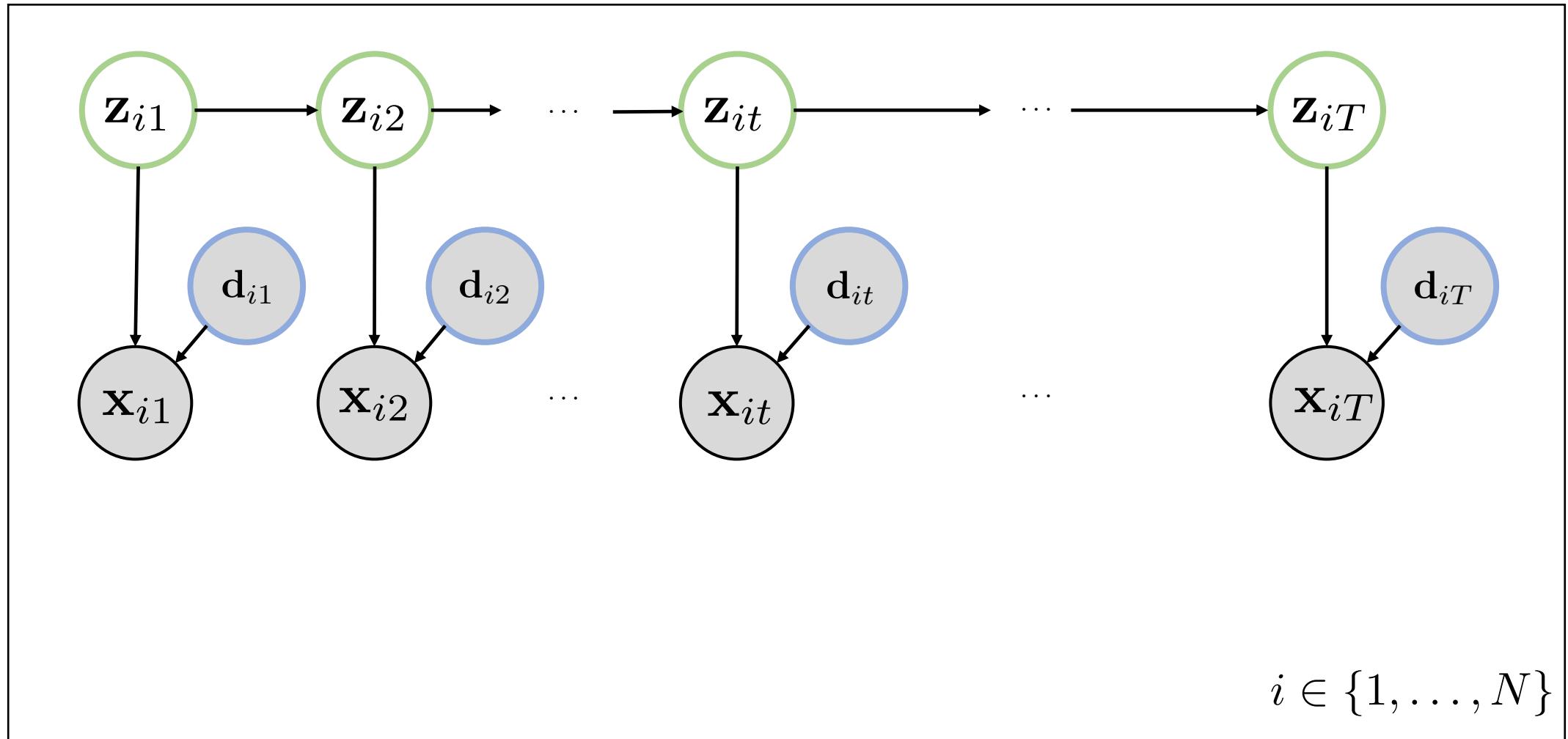
# Personalized input output hidden Markov models



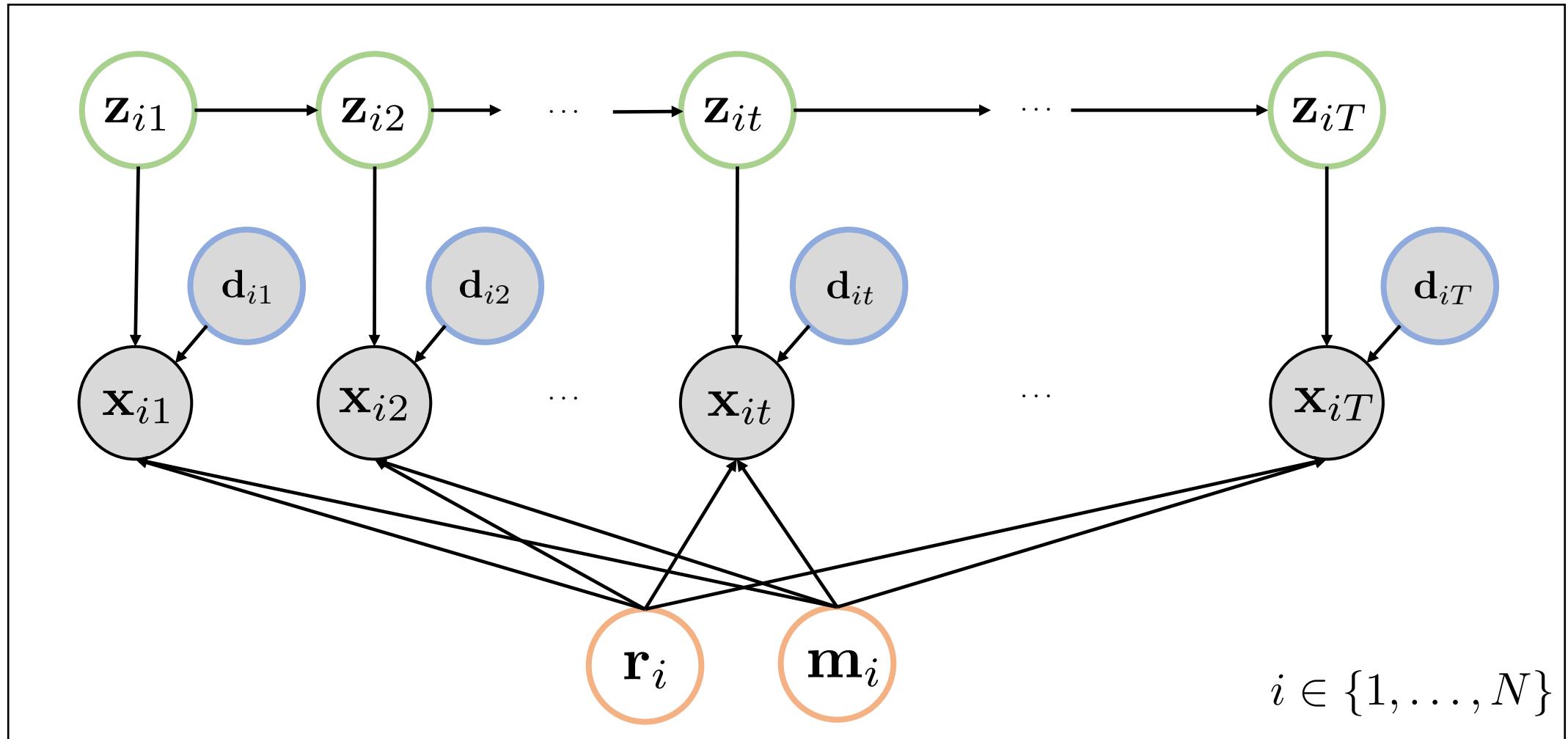
# Personalized input output hidden Markov models



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# Personalized input output hidden Markov models

- The graphical model on the previous slide is specified using the following distributions:

$$z_{i,1} \sim \text{Cat}(\pi), \quad z_{i,t}|z_{i,t-1} = j \sim \text{Cat}(A_j)$$

$$x_{i,t}|z_{i,t} = k, d_{i,t} \sim \mathcal{N}(\mu_k + r_i + (v_k + m_i)d_{i,t}, \Sigma_k)$$

$$m_i \sim \mathcal{N}(0, \sigma_m^2 \mathbf{I}_D), \quad r_i \sim \mathcal{N}(0, \sigma_r^2 \mathbf{I}_D), \quad v_k \sim \mathcal{N}(0, \sigma_v^2, \mathbf{I}_D)$$

# Learning the model

**X:** Observed data  
**Z:** Disease states  
**R:** Personalized state  
**M:** Personalized medication effects

Optimization objective:

$$\mathcal{L}(\theta, \lambda) = \mathbb{E}_{q(\mathbf{Z}, \mathbf{M}, \mathbf{R} | \mathbf{X}, \lambda)} [\log p(\mathbf{X}, \mathbf{Z}, \mathbf{M}, \mathbf{R} | \theta)] + \mathbb{H}[q(\mathbf{Z}, \mathbf{M}, \mathbf{R} | \mathbf{X}, \lambda)]$$

Two remaining pieces to the learning algorithm for PIOHMM:

1. How to choose  $q(\mathbf{Z}, \mathbf{M}, \mathbf{R} | \mathbf{X}, \lambda)$ ?
2. Given the posterior approximation, can we evaluate the required expectations?

# Choosing the variational approximation

**X:** Observed data  
**Z:** Disease states  
**R:** Personalized state  
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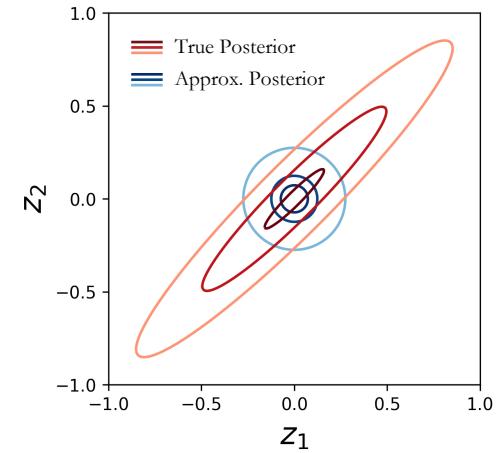


Image based on: Bishop. Pattern Recognition and Machine Learning. 2006.

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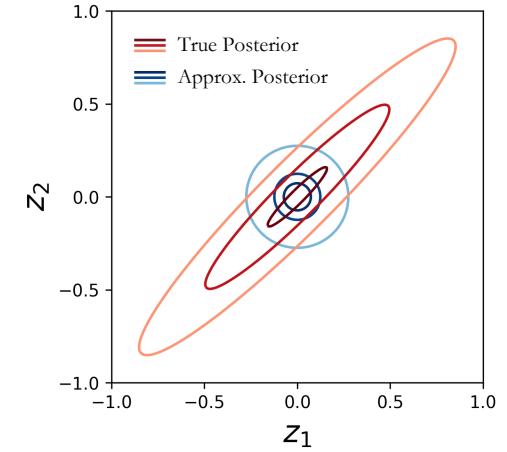


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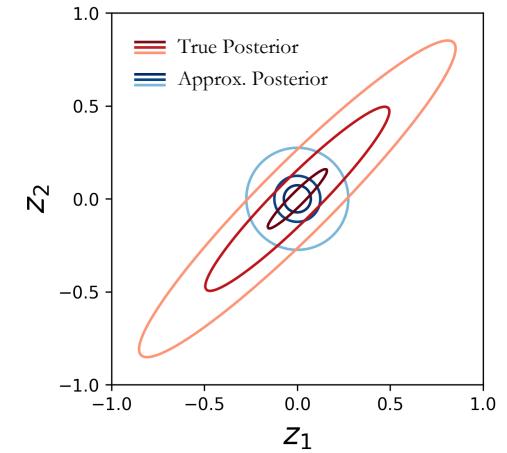


Image based on: Bishop. Pattern Recognition and Machine Learning. 2006.

# Evaluating the expectations

**X:** Observed data  
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Optimization objective:

$$\mathcal{L}(\theta, \lambda) = \mathbb{E}_{q(\mathbf{Z}, \mathbf{M}, \mathbf{R} | \mathbf{X}, \lambda)} [\log p(\mathbf{X}, \mathbf{Z}, \mathbf{M}, \mathbf{R} | \theta)] + \mathbb{H}[q(\mathbf{Z}, \mathbf{M}, \mathbf{R} | \mathbf{X}, \lambda)]$$

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Monte Carlo approximation:

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“Reparameterization trick”:

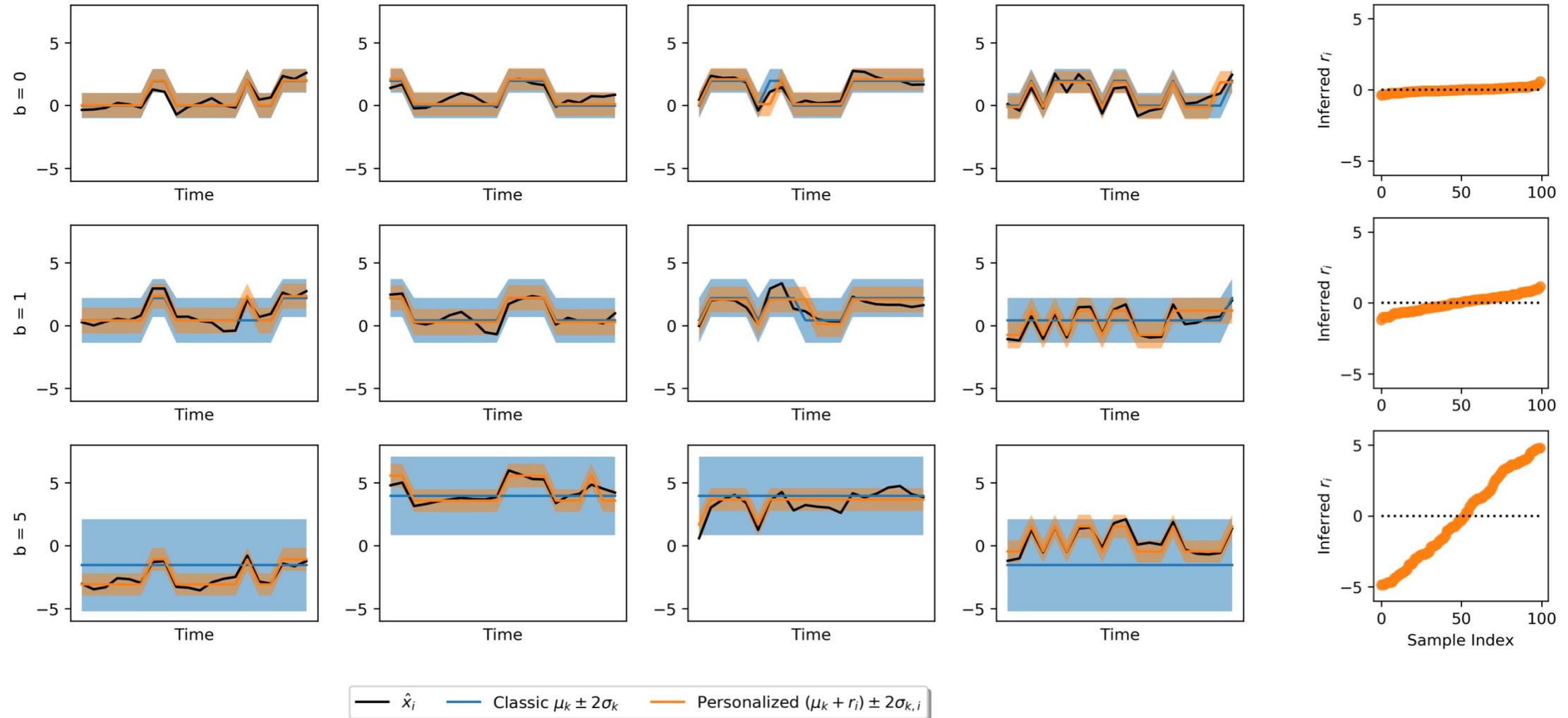
$$\epsilon_{m_i}^s \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

$$m_i^s = \hat{L}_{m_i} \epsilon_{m_i}^s + \hat{\mu}_{m_i}$$

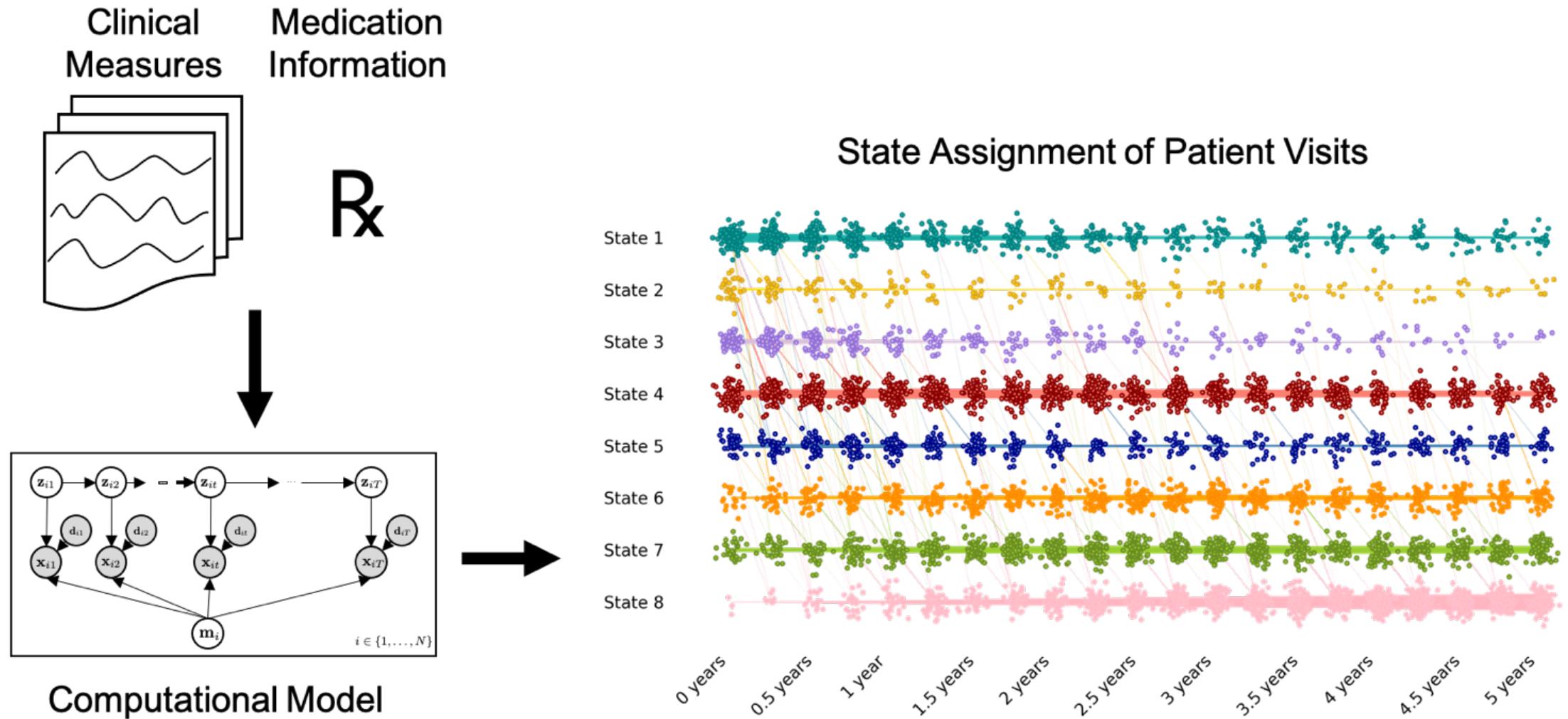
$$\epsilon_{r_i}^s \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

$$r_i^s = \hat{L}_{r_i} \epsilon_{r_i}^s + \hat{\mu}_{r_i}$$

# Synthetic proof of concept

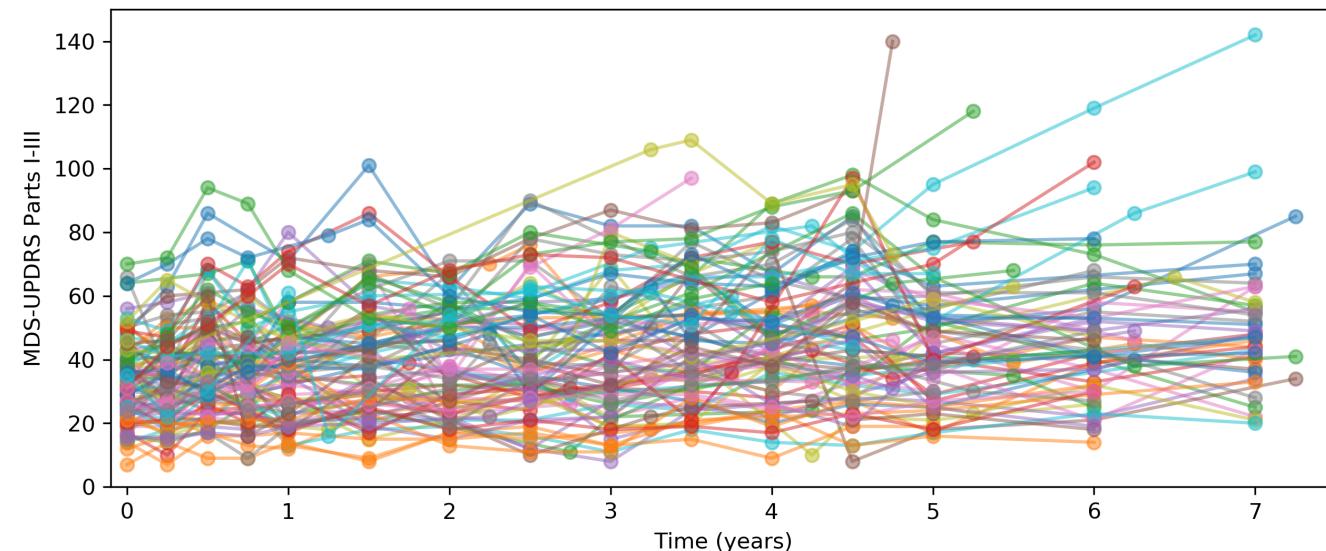


# Summarizing the project

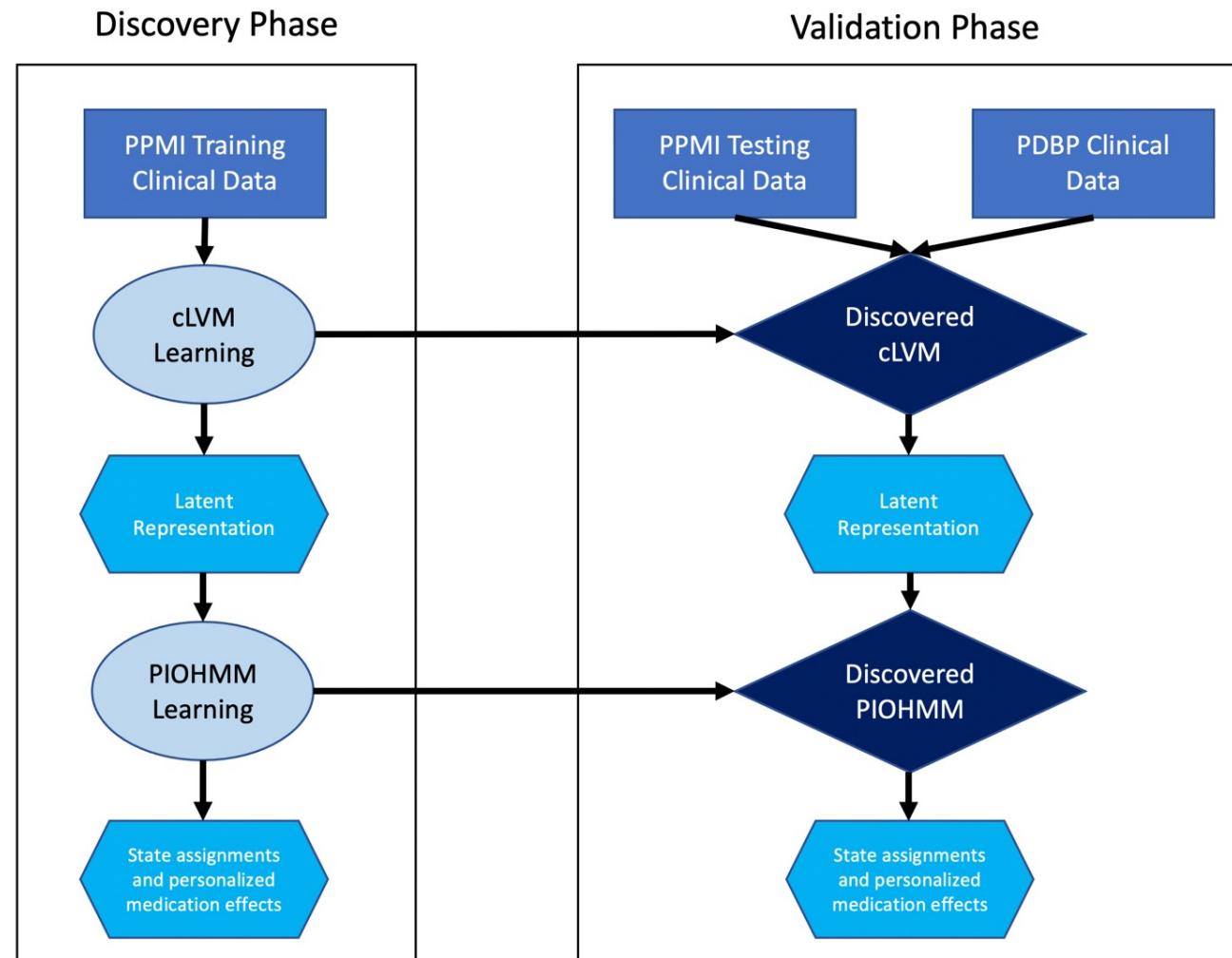


# Dataset for analysis

- Longitudinal data from the Parkinson's Progression Markers Initiative (PPMI) and Parkinson's Disease Biomarker Program (PDBP)
- 82 variables measuring motor and non-motor symptoms over time
- 423 PD patients from PPMI and 610 PD patients from PDBP



# Analysis workflow



# Key take-aways

- The learning procedure resulted in an 8 state model where states are primarily differentiated by functional impairment, tremor, bradykinesia, and neuropsychiatric measures

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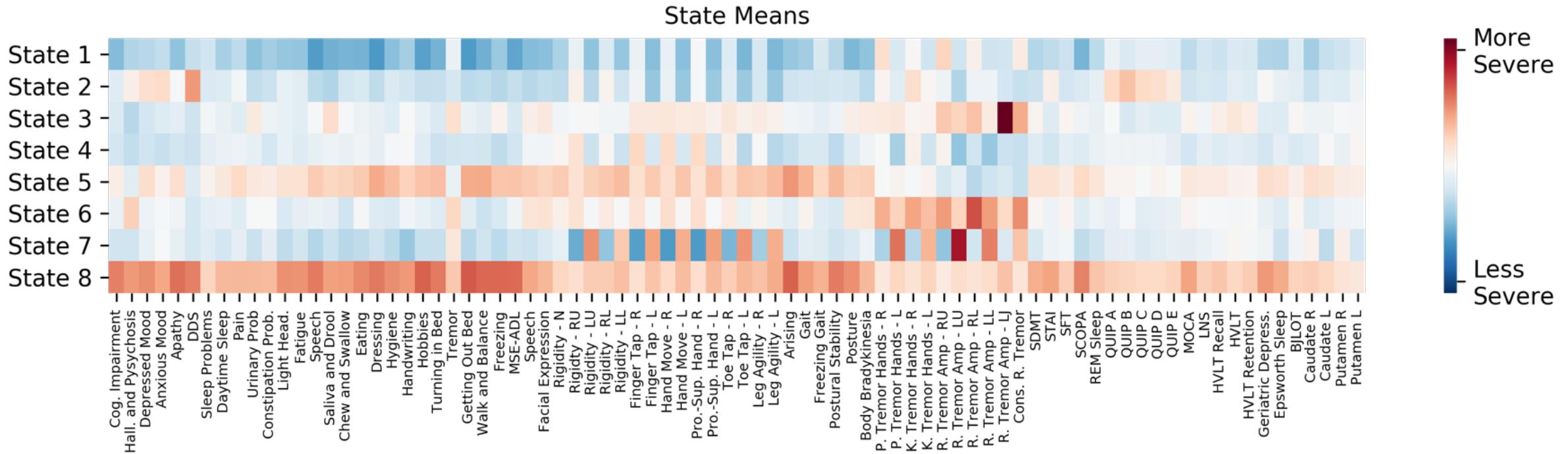
- The learning procedure resulted in an 8 state model where states are primarily differentiated by functional impairment, tremor, bradykinesia, and neuropsychiatric measures
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# Key take-aways

- The learning procedure resulted in an 8 state model where states are primarily differentiated by functional impairment, tremor, bradykinesia, and neuropsychiatric measures
- The predictive model discovers non-sequential overlapping disease progression trajectories
- The addition of personalized medication effects leads to a more descriptive model

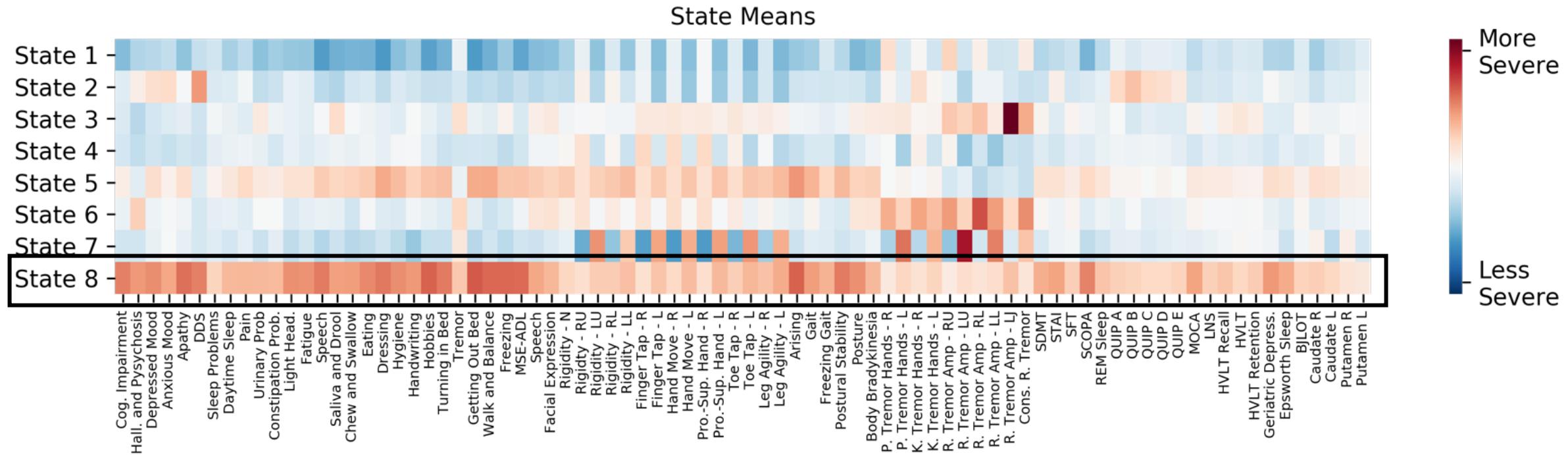
# Model parameters – State means

# How can we interpret the states?



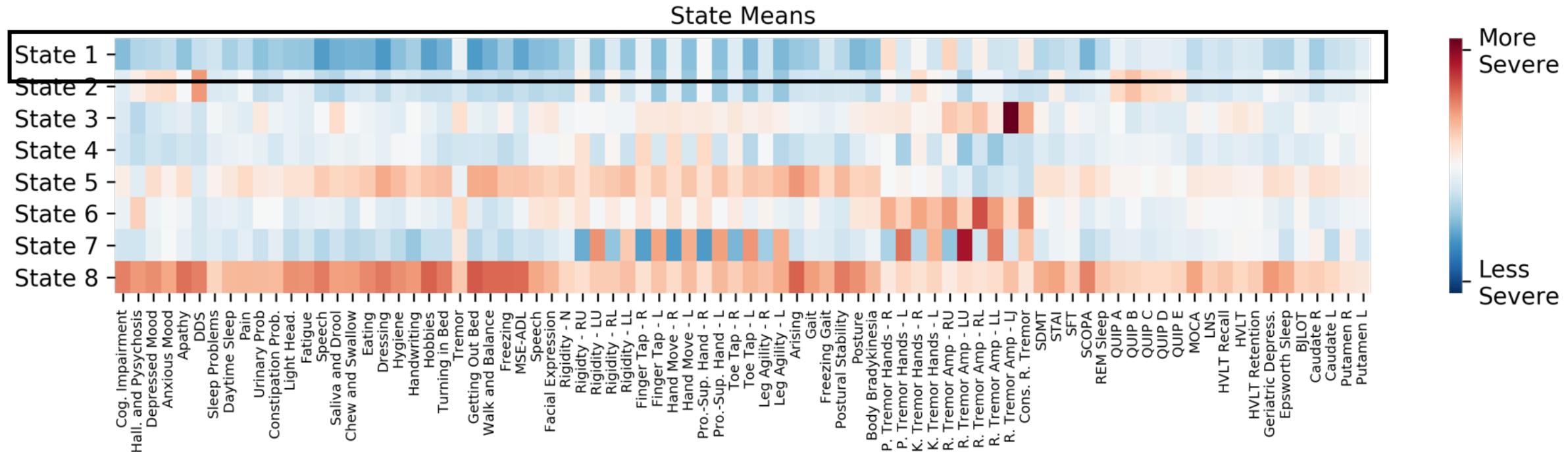
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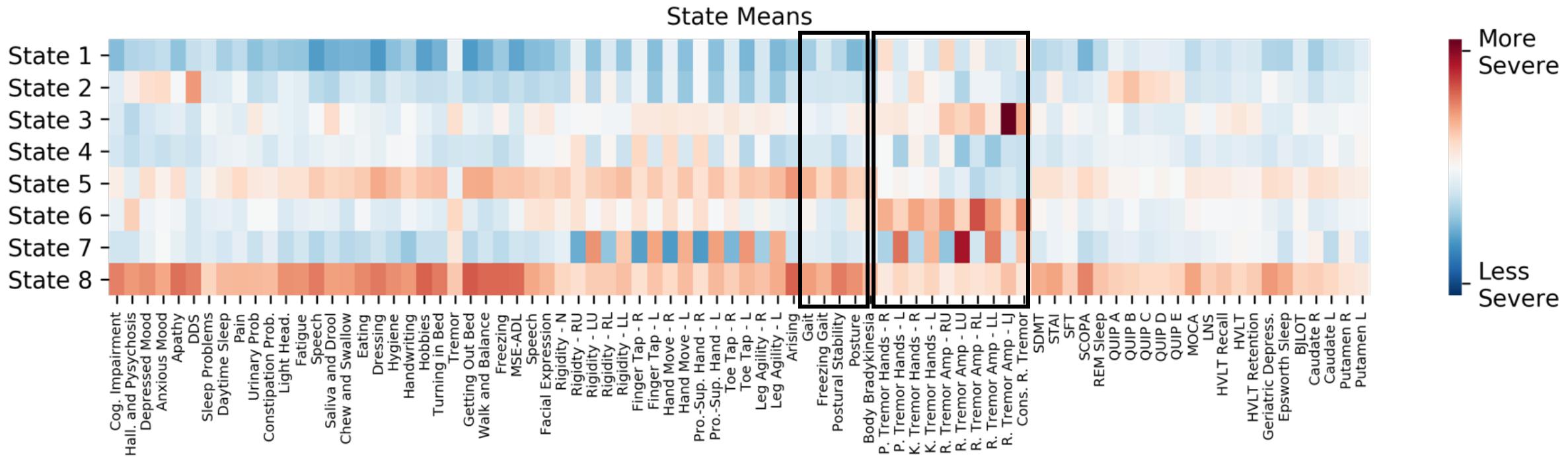
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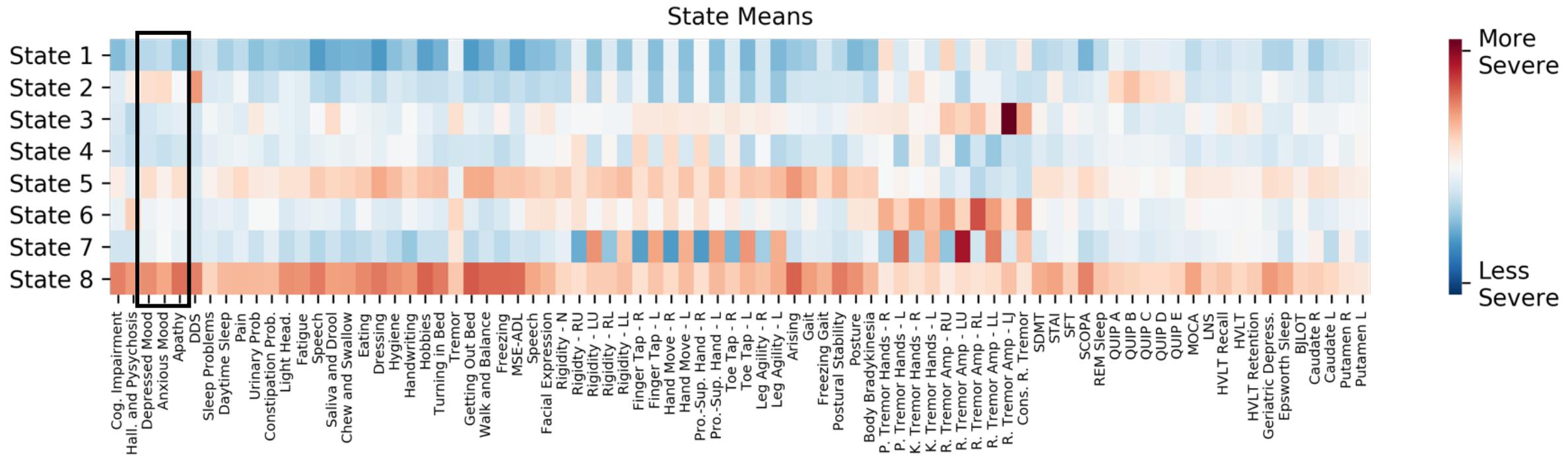
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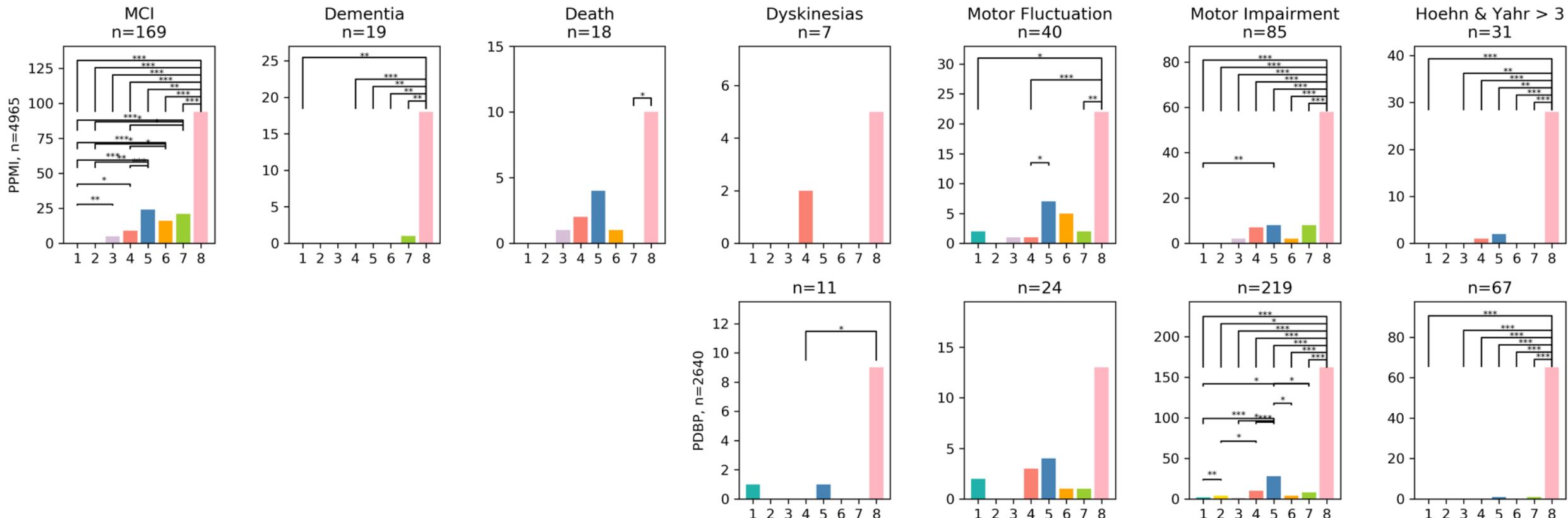
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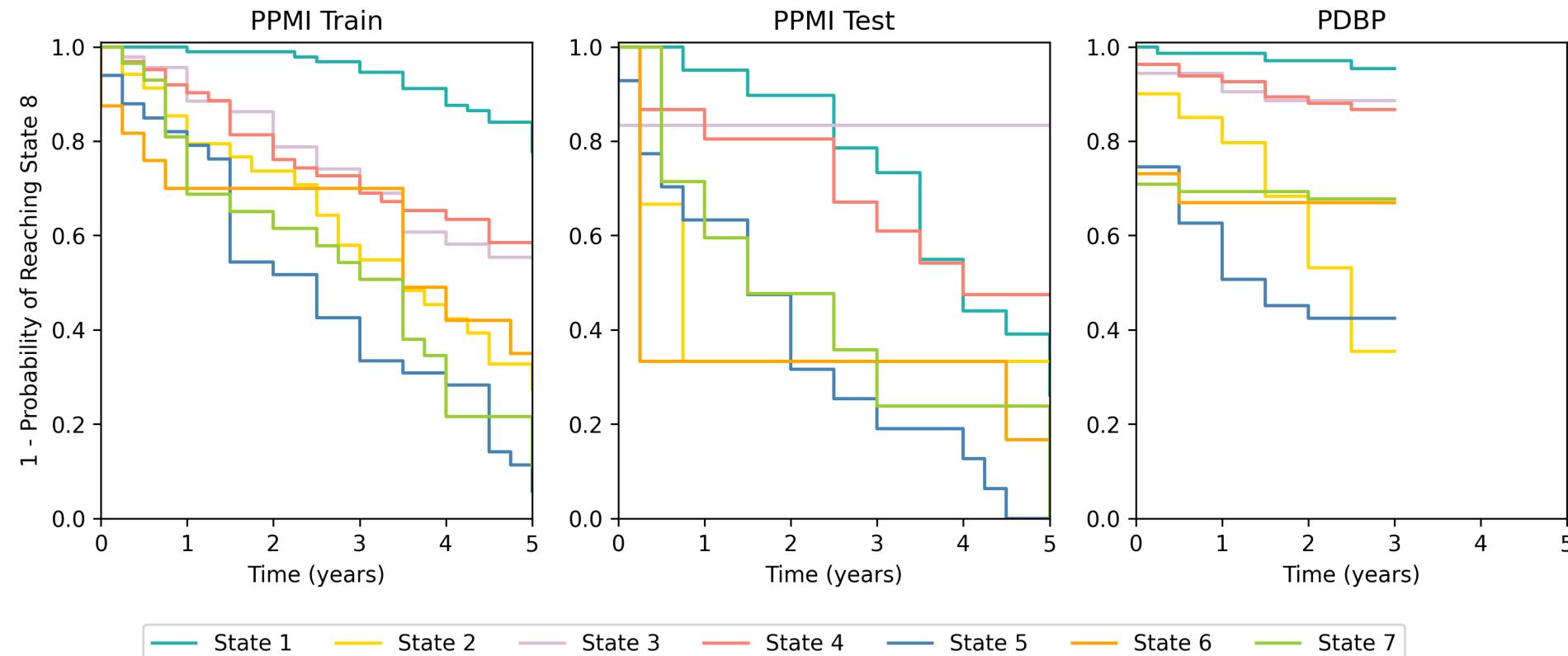
# Outcome measures

What are the clinical implications of the states?



# Progression pathways

What can we say about the progression of the states?



# Predictive capability

- What can we say about the predictive capability of the model?
- Predictive question: how well can we predict disease state at year 2 given data from baseline?
- Prediction in this case is defined as the most probable state assignment

PPMI Testing	Condition Positive	Condition Negative	
Predicted Positive	<b>10</b>	7	Precision = 0.59
Predicted Negative	14	<b>52</b>	NPV = 0.79
	Recall = 0.42	Specificity = 0.88	Accuracy = 0.75 F1 Score = 0.49

PDBP	Condition Positive	Condition Negative	
Predicted Positive	<b>91</b>	62	Precision = 0.59
Predicted Negative	52	<b>405</b>	NPV = 0.87
	Recall = 0.64	Specificity = 0.87	Accuracy = 0.81 F1 Score = 0.61

# Conclusions

- Application of the disease progression resulted in novel Parkinson's disease insights and strong predictive performance
- Disease state was found to vary across motor and non-motor symptoms
- The model discovered non-sequential, overlapping disease progression trajectories, supporting the use of non-deterministic disease progression models

# Acknowledgements

## Project team



Kristen  
Severson



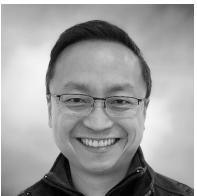
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Hu



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Dhuliawala



Kenney  
Ng

IBM, Machine Learning

University of Pittsburgh, Neurology

Michael J. Fox Foundation, Advisory



Lana  
Chahine



Mark  
Frasier



Luba  
Smolensky

Funding provided by the Michael J. Fox Foundation





# Comparison to a standard hidden Markov model

