

# NUMERICAL TEST RIG FOR LARGE-SCALE AND INTERCONNECTED DYNAMICAL SYSTEMS

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## **Abstract**

The goal of this project was to develop a test rig for large-scale and interconnected dynamical systems. The result is MTIDS or Matlab Toolbox for Interconnected Dynamical Systems, which is a mash-up that wraps different toolboxes used for graph analysis and dynamic systems simulation together. MTIDS allows the definition and analysis of graphs, where each node has a specific dynamic assign to it. The template based design of nodes' dynamics allows great flexibility for the creation of complex interconnected dynamical systems with the possibility of implementing clusters/layers. MTIDS is an open-source project under the GNU GPL v2 license. This document presents a general description of MTIDS and instructions for its use.



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# Chapter 1

## Introduction

In this first Chapter the motivation behind the MTIDS project is explained and the project's goal and framework is presented.

### 1.1 Motivation

Large-scale interconnected dynamical systems are everywhere: biological systems, power and water systems, the brain neurons, social interaction networks, economic markets, etc. In a canonical form all of these systems can be thought of as a bunch of nodes with local dynamics that interact with each other, e.g. a graph. Different topologies of the graph, may lead to different behavior. An example of various large scale interconnected systems can be seen in Figure 1.1.

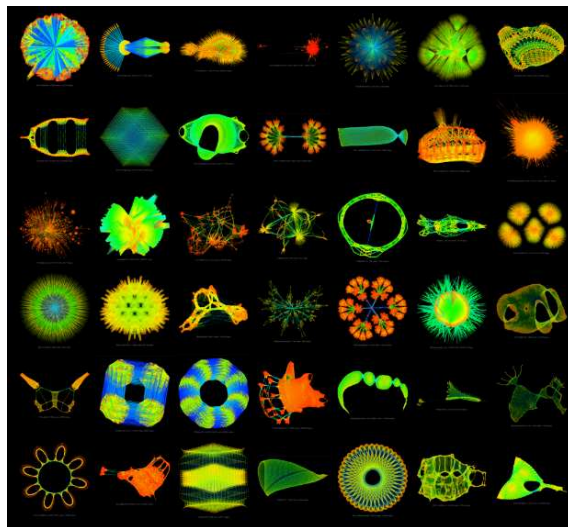


Figure 1.1: Visualization of various large scale systems using the sfdp algorithm © Dr. Yifan Hu of AT&T Labs

There are many tools available for the analysis of interconnected dynamical systems,

for example in power systems you have PSSE and Power Factory. However, this simulation programs are normally very system specific and in most cases it takes a long time to learn how to use them correctly. The difficulties are specially noticed while testing control concepts, where small changes on the topology of the grid or control concept could lead to a painful redesign of your simulation set up. You may actually end up spending the most of your time in the implementation of a simulation. A more general and easy to use solution for the simulation of interconnected dynamical systems is needed.

## 1.2 Idea and Goal

**MTIDS** (Matlab Toolbox for Interconnected Dynamical Systems) is a project that aims to design an easy to use and flexible toolbox to make the simulation of large scale dynamical systems easier for students and researchers. The **goal** is to produce a mash-up that wraps different toolboxes used for graph analysis and dynamic systems simulation together into a framework.

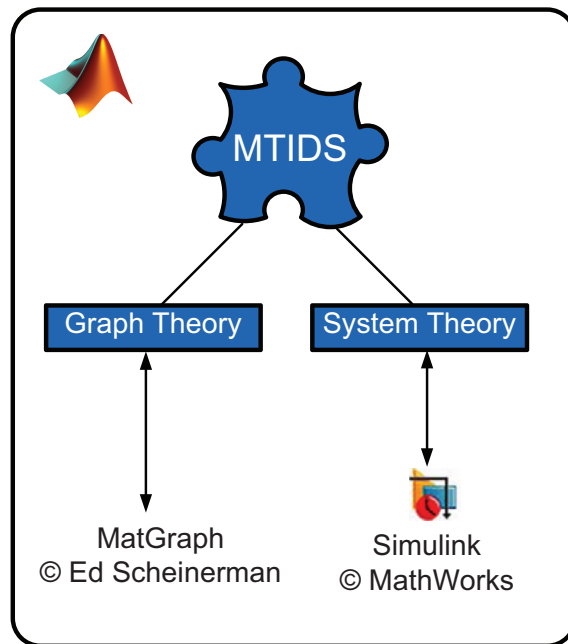


Figure 1.2: MTIDS: Matlab Toolbox for Interconnected Dynamical Systems

As we can see in Figure 1.2 MTIDS runs in the MATLAB environment and is basically a GUI that allows the interaction of tools used in graph theory and control theory. For graph theory we use Matgraph a toolbox design by Prof. Scheinerman of the John Hopkins University [Sch06] and for dynamical simulations we use Simulink[Mat11].



## 1.3 Framework

The current framework of MTID is made out of three basic components. A GUI (**mtids.m**) an export to simulink function (**exportSimulink.m**) and an import from Simulink function (**importSimulink.m**).

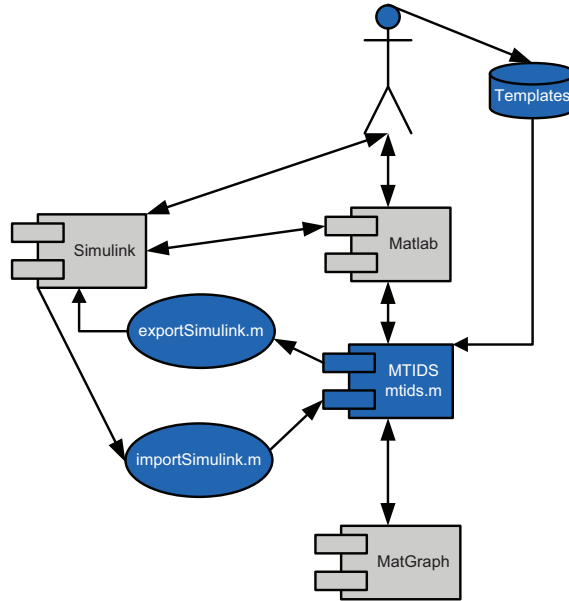


Figure 1.3: MTIDS: Components diagram

In Figure 1.3 we can see that the most important component is the user, specially its head. The better you are at producing templates and interacting with matlab and simulation the more functional MTIDS is going to be for you. In a nutshell MTIDS works as follows:

- GUI (mtids.m) runs inside Matlab
- GUI interacts with Matgraph: create, modify and visualize graphs
- System Inteconnector (SI): exportSimulink.m and importSimulink.m called from GUI to interact with Simulink
- Templates done by User in Matlab/Simulink.
- Simulations done in Simulink



# Chapter 2

## Graph Theory

Graphs are commonly used to represent networked structures. A graph consists of:

1. **Vertices:** Represent nodes, dynamical subsystems and/or agents.
2. **Edges:** Represent connections, links or couplings between vertices.

In this project, we consider only simple, undirected and unweighted graphs.

### 2.1 Algebraic Graph Theory

Algebraic graph theory describes graph properties using numbers (like invariants) and equations. It is important first, to convert the graphical representation of a graph into a mathematically sound description like matrices. Once a the corresponding matrices (like the Laplacian or adjacency matrices) have been derived, we can calculate it's properties [HE11]

The use of linear algebraic tools like rank, eigenvalue and eigenvector extraction of graph matrices is called *Spectral Graph Theory*

#### Degree of a vertex and degree vector

The degree of a vertex is the number of edges that are connected to it. The vector whose i-th component is the degree of the i-th vertex is the degree vector  $\vec{d}$ . The degree vector can analysed using basic statistical tools for for mean, variance, min, max, span, etc.

#### Graph heterogeneity

Graph heterogeneity is the quotient between the standard deviation of the degree vector  $\vec{d}$  and the mean of the degree vector.

$$H = \frac{\sqrt{\text{var}(\vec{d})}}{\vec{d}} \quad (2.1)$$

It describes the heterogeneity between the connections to the nodes.

### Maximal number of edges and graph density

A complete graph is a graph where every vertex is connected to every other vertex. The number of vertices inside a complete graph is:

$$N_{e_{MAX}} = \frac{1}{2} N_v (N_v - 1) \quad (2.2)$$

Alternatively:

$$N_{e_{MAX}} = \frac{1}{2} (N_v^2 - N_v) \quad (2.3)$$

Graph density is a number which describes the *completeness* of a graph. It is defined as the quotient between the actual number of edges  $N_e$  and number of edges of a complete graph  $N_{e_{MAX}}$  with the same number of vertices:

$$D = \frac{N_e}{N_{e_{MAX}}} \quad (2.4)$$

$$D = 2 \frac{N_e}{N_v^2 - N_v} \quad (2.5)$$

## 2.1.1 Graph matrices

### Adjacency Matrix

The adjacency matrix is defined as a  $N_v \times N_v$  matrix whose  $(A)_{ij}$  component is equal to one if there is a connection between vertex  $i$  and vertex  $j$  or zero if not.

### Degree Matrix

A degree matrix is a diagonal matrix whose diagonal  $(D)_{ii}$  components are equal to the degree of the  $i$ -th vertex. All other components for  $(D)_{ij}$   $i \neq j$  are zero.

$$(D)_{ij} = \begin{cases} 0 & \text{if } i \neq j \\ N_v(i) & \text{if } i = j \end{cases} \quad (2.6)$$

### Laplacian Matrix

The Laplacian matrix is defined as the degree matrix  $D$  minus the adjacency matrix  $A$ :

$$L = D - A \quad (2.7)$$

The Laplacian matrix is used to characterize the algebraic connectivity of a graph.

## 2.1.2 Algebraic connectivity and Fiedler vector

### Algebraic connectivity

For sorted the sorted eigenvalues of the Laplacian matrix  $\lambda_1 \leq \lambda_2 \leq \dots \leq \lambda_{N_v}$  we define the algebraic connectivity as the first nonzero eigenvalue. It's corresponding eigenvector is the Fiedler vector. The algebraic connectivity is a measure of how connected a system is. For example, in the consensus problem, the algebraic connectivity describes the rate of convergence of the system to it's final state.

### Number of connected subgraphs

The multiplicity of the zero eigenvalue of the Laplacian matrix is the number of connected subgraphs inside the system. This is also the rank of the nullspace of the Laplacian matrix  $\text{Rank}(\text{Null}(L))$ . From the rank-nullity theorem of linear algebra we know that the rank of a matrix and the rank of it's nullspace add up to the number of columns. Therefore for a square matrix, the rank of the nullspace can be calculated using:

$$\text{Rank}(\text{Null}(L)) = \text{Rank}(L) - N_v \quad (2.8)$$

## 2.1.3 Estrada Index

The Estrada index of a vertex  $i$  is [EH10]

$$E(i) = (e^A)_{ii} \quad (2.9)$$

The Estrada index of an adjacency matrix is:

$$E(A) = \text{tr}(e^A) \quad (2.10)$$

## 2.2 Creating and visualizing systems in MTIDS

### 2.2.1 MTIDS GUI Overview

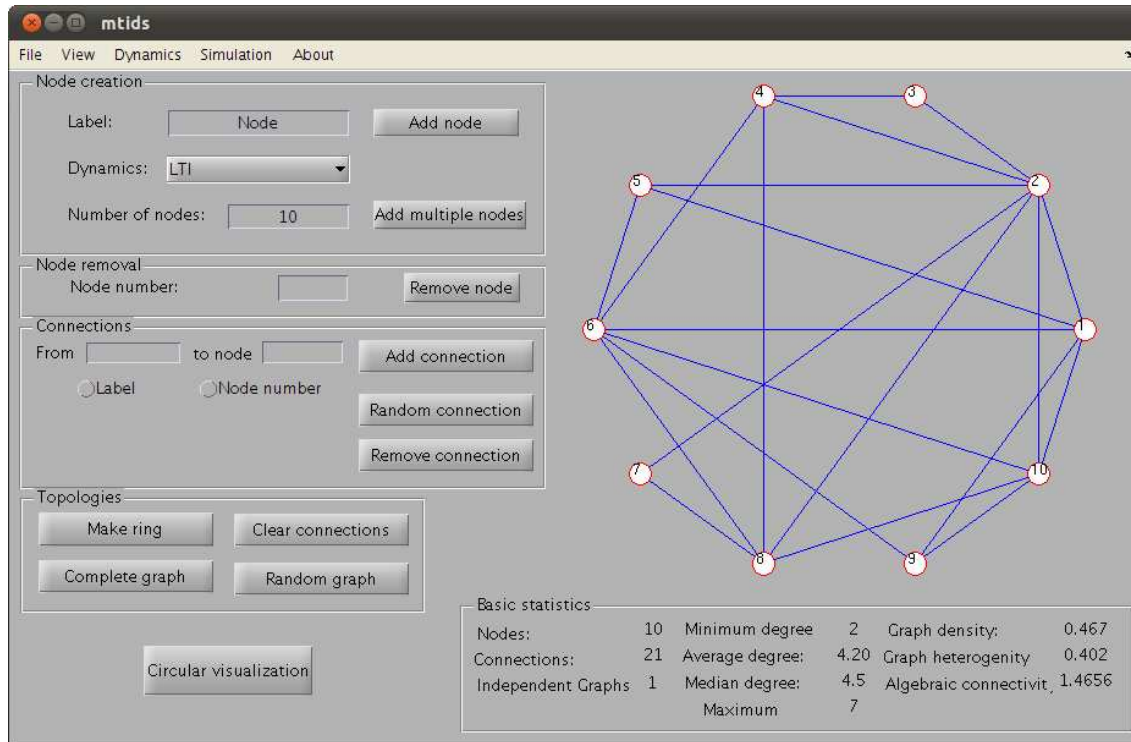


Figure 2.1: The MTIDS Graphical User Interface

### 2.2.2 Building a interconnected system in MTIDS

#### Adding nodes

A node needs to have: A unique label, an assigned dynamic/template Nodes added by using the mouse (<shift>-<left-click>) are given the last selected node dynamics and node label.

#### Adding multiple nodes

Adding multiple nodes at the same time is possible by introducing the number of nodes to be added and by clicking the “Add multiple nodes” button. These nodes start all with the same name (eg. node1, node2,...) and share the same dynamics.

#### Creating and removing connections

Connections can be added or removed using:

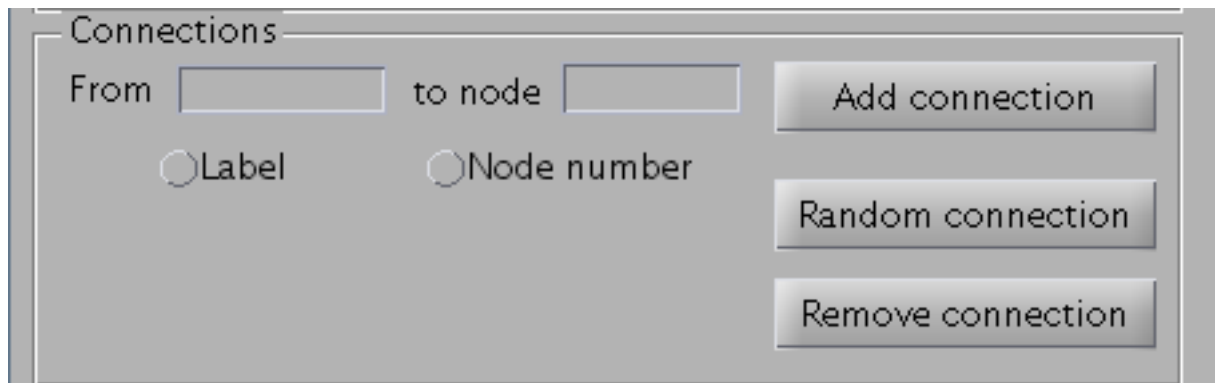


Figure 2.2: Connection options

- **Mouse:** By <Ctrl>-<Left click> on both nodes. If no connection exists, it will create one, otherwise it will delete this connection.
- **Connection subwindow:** Connections to be added or removed can be specified by using node label or node number.
- “Edit node” dialog

#### Default topologies

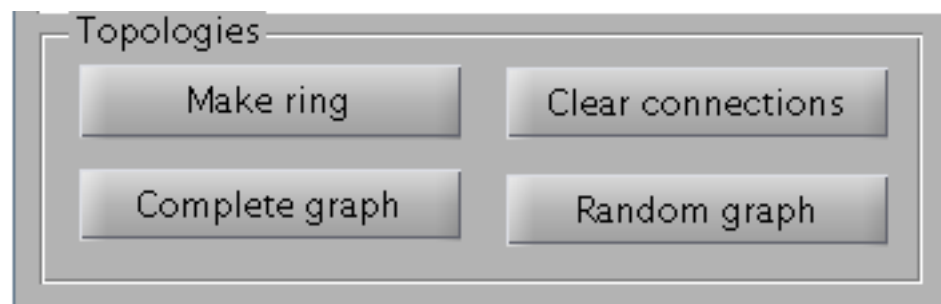


Figure 2.3: The default topologies

- **Complete graph:** Makes the graph into a complete graph.
- **Remove connections:** Removes all edges inside the graph.
- **Make ring:** Connects all nodes into a ring.
- **Random graph:** Uses the random graph function from Matgraph. It adds random connections between nodes up to a density of ca. 0.5.

### 2.2.3 Node properties

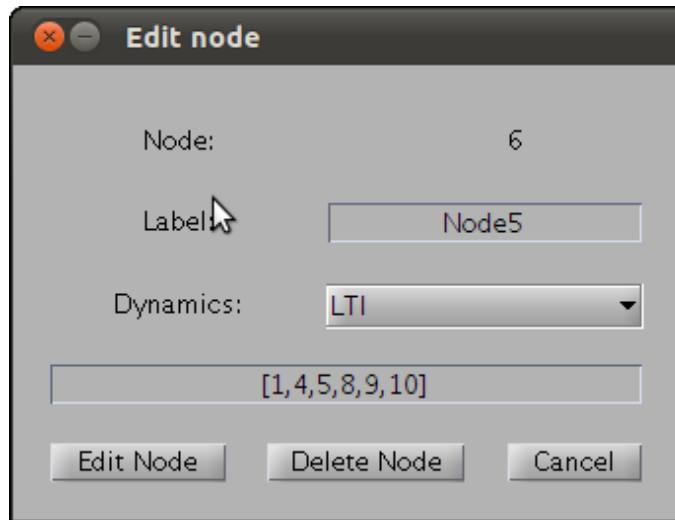


Figure 2.4: The node properties window

Node properties can be edited by double-clicking a node in the graph window. Following node properties can be changed: Node label, node dynamics (from list) and the connection list in Matlab format.

### 2.2.4 Load and Save

A system can be saved by selecting **File** → **Save As...** This saves the graph properties (adjacency matrix), node labels, assigned node dynamics and template list into a binary .mat file. Loading an already saved system for modification is possible by selecting **File** → **Load...** This loads the selected .mat file which contains the system properties.

Remember that a saved system file contains the template names previously imported so reimporting dynamics is not necessary. If a template .mdl file is missing or was deleted, the exporting to Simulink functionality will not work correctly.

### 2.2.5 Exporting matrices to Matlab

Select the corresponding workplace inside Matlab, variable name and matrix type to export. Supported matrices are Laplacian matrix, adjacency matrix and edge list.

### 2.2.6 Importing graph matrices into MTIDS



# Chapter 3

## System Theory

In this Chapter we explain the design and simulation capabilities that MTIDS offers for interconnected dynamical systems.

### 3.1 MTIDS Concepts for Simulink Models

#### 3.1.1 Nodes and connections

**Node:**

Each node in MTIDS is a subsystem block in Simulink. Each node must have a unique label. Each node has an in-port for every node in the graph and an out-port.

**Connections:**

Any connection made inside MTIDS is bidirectional and unweighted. As Simulink connections are directed, each MTIDS bidirectional connection is represented with two directed connections between nodes. To implement weighted graphs, weights on branches have to be realized in the node's dynamic model, e.g inside the subsystem. Another option is to define junction nodes.

### 3.2 Export to Simulink

In order to export the model created in the MTIDS GUI to simulink: **Simulation** → **Export to Simulink...** (see Figure 3.2)

The MTIDS GUI then calls the function `exportability.m` which builds a Simulink model with the following information: model name, list of nodes' dynamics templates, list of templates that are available in `mtids`, adjacency matrix, position of the nodes and nodes' names. The result is a Simulink model in the MTIDS format.

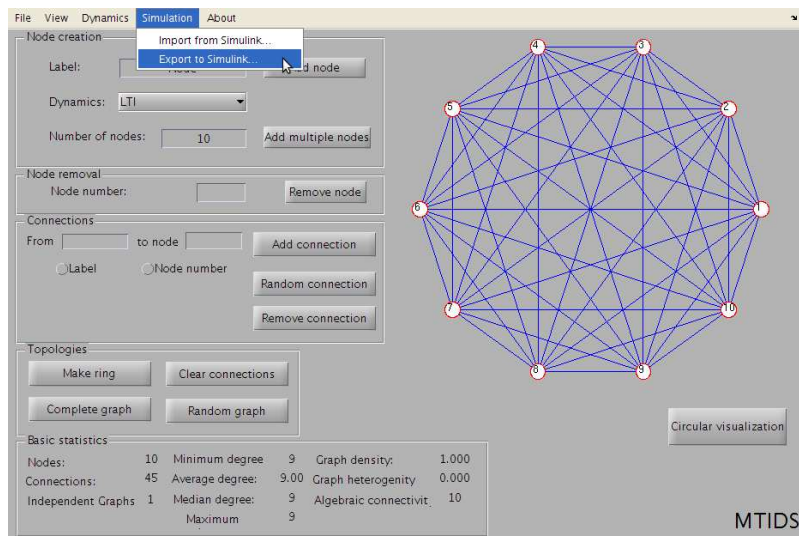


Figure 3.1: MTIDS: export model to Simulink. Example is a complete graph with 10 LTI nodes.

To adjust the size of the model to the Simulink window size: **View → Fit System To View**

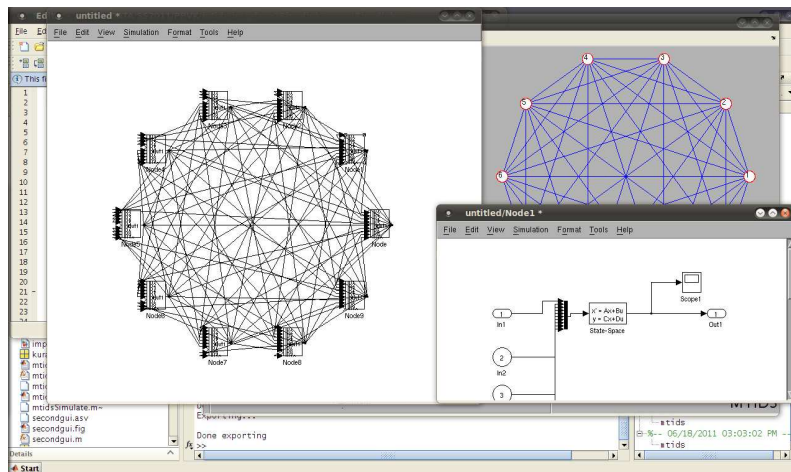


Figure 3.2: Interconnected system Simulink Model. Example is a complete graph with 10 LTI nodes.

In Figure 3.2, the nodes are ordered in a circle, the topology of the system defined in MTIDS remains. The circle arrangement is a design decision, made, in order to allow a better access to the nodes. Each one of the nodes is a subsystem block. The dynamic of the nodes is defined inside the subsystem block. Moreover, each node has a single out-port and  $N$  in-ports, where  $N$  is the number of nodes the whole system has. Each node on the system has its own in-port on each node, compare

with a zoom on the first node of our example in Figure 3.3.

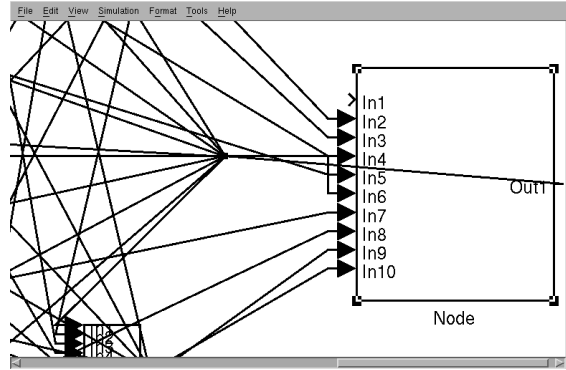


Figure 3.3: Node inputs and output: Each node has an in-port for every node in the model and an out-port. Example is the first node of a complete graph with 10 LTI nodes.

Notice that the port corresponding to the nodes number should always be free, e.g. the first node has an unconnected in-port 1, the second node an unconnected in-port 2, etc. In case that a loop of a node with itself is required we recommend doing this inside the subsystem/node. Another important aspect to point out is that when simulating the system, Simulink will issue a warning for unconnected in-ports and set their input to the subsystem to 0, this means that an **unconnected port enters the subsystem (local dynamics of the node) with a value of zero** during simulations. This can be exploited to make the parametrization of the nodes' dynamics easier.

### 3.3 Nodes' Dynamics

As mentioned in the past section 3.2 each node defined in MTIDS is exported to Simulink as a subsystem. The `exportSimulink.m` function uses predefined dynamic templates, which are modified according to the, in MTIDS, defined topology. Next, we explain how to define your own templates and show how to use 2 preloaded templates: the LTI template and the kuramoto template.

#### 3.3.1 Build your own Template

The real power of MTIDS depends on your ability to build templates.

In Figure 3.4 we can see the components that each template should have: an in-port connected to a mux and an out-port. Between the mux and the out-port you can design your own custom dynamics. The input to the system comes from mux as



Figure 3.4: Scratch template for node's dynamics.

vector, which is composed by the values entering the node/subsystem. The output of your system should also be aggregated to a vector and routed to the out-port. The separation of the different inputs and outputs is left to the system designer. With a well thought architecture complex systems are very easy to achieve, please refer to the LTI and kuramoto template examples.

The dynamic of a node can be as simple as a junction that only reroutes the incoming signals or more complicated to include controllers and systems inside of it. It is this feature that allows the implementation of clusters or layered systems, see subsection 3.4.

### 3.3.2 The LTI template

The LTI template is an example that defines a linear time invariant dynamic for nodes. The mathematical model of a simple interconnected LTI system is written as:

$$\begin{pmatrix} \dot{x}_1 \\ \vdots \\ \dot{x}_N \end{pmatrix} = \begin{pmatrix} A_{11} & \cdots & A_{1N} \\ \vdots & \ddots & \vdots \\ A_{N1} & \cdots & A_{NN} \end{pmatrix} \begin{pmatrix} x_1 \\ \vdots \\ x_N \end{pmatrix} + \begin{pmatrix} B_1 & \cdots & B_N \end{pmatrix} \begin{pmatrix} u_1 \\ \vdots \\ u_N \end{pmatrix} \quad (3.1)$$

or

$$\dot{x} = Ax + Bu \quad (3.2)$$

The local view of a single subsystem/node (here for the first node) is:

$$\dot{x}_1 = \begin{pmatrix} A_{11} & A_{12} & \cdots & A_{1N} & B_1 & \cdots & B_N \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_N \\ u_1 \\ \vdots \\ u_N \end{pmatrix} \quad (3.3)$$

this can be reformulated as

$$\dot{x}_1 = A_{11}x_1 + \begin{pmatrix} A_{11} & A_{12} & \cdots & A_{1N} & B_1 & \cdots & B_N \end{pmatrix} \begin{pmatrix} 0 \\ x_2 \\ \vdots \\ x_N \\ u_1 \\ \vdots \\ u_N \end{pmatrix} \quad (3.4)$$

In order to keep things simple, we define the local output of each node:

$$y_i = x_i, \quad i = 1, \dots, N. \quad (3.5)$$

To implement this dynamic as a template we make use of the State-Space block.

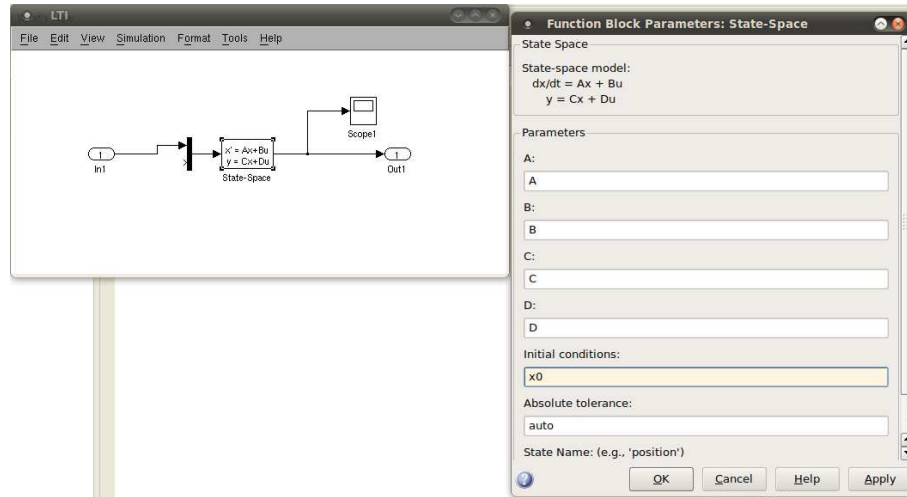


Figure 3.5: LTI template

This template shown in 3.5 can be used in MTIDS to create interconnected LTI systems with different topologies. One way to avoid the work of parameterizing the A,B,C and D matrix of every node separately is to define the same matrix for all subsystems. One can use the formula 3.4 and define the same A, B, C, and D matrix for every node. An example of this is

$$\begin{aligned} A &= 1 \\ B &= [-1 \dots -1]^{1 \times N} \\ C &= 1 \\ D &= [0 \dots 0]^{1 \times N} \end{aligned}$$

As the in-port corresponding to the node itself is automatically set to zero by Simulink during the simulation, we can define the same matrices for all nodes without getting any errors.

For more complicated LTI models we recommend creating many different LTI templates.

### 3.3.3 The Kuramoto Template

The kuramoto template is an example of a non-linear dynamic for a node. The kuramoto model is used to model the behavior of coupled oscillators. One of the interesting behaviors that may occur in this type of systems is synchronization. The mathematical equation of  $N$  coupled oscillators is written for each oscillator  $i$  as

$$\dot{\theta}_i = \omega_i + \frac{K}{N} \sum_{j=1}^N \sin(\theta_j - \theta_i). \quad (3.6)$$

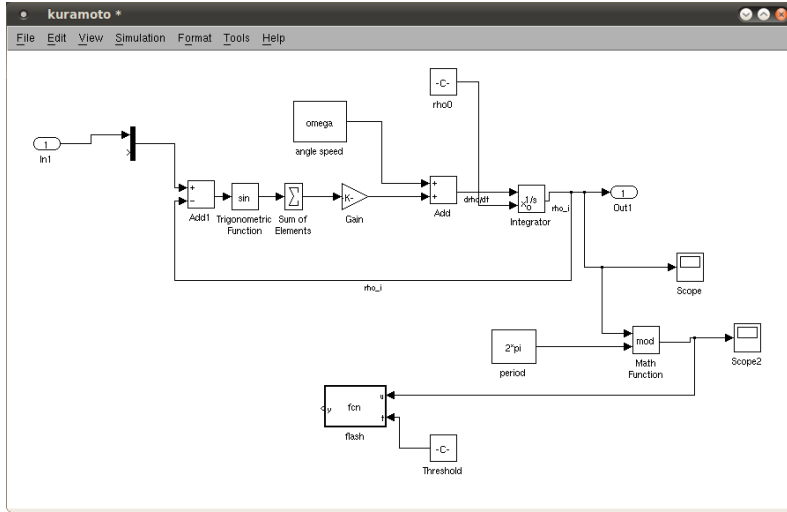


Figure 3.6: Kuramoto template for fireflies synchronization

In Figure 3.6 we see the MTIDS's kuramoto template after formula 3.6. The goal was to produce fireflies synchronization, thus the model has an embedded function that changes the color of the parent block for a defined threshold, this mimics the flashing of a firefly. With the right parameters one can build a synchronizing firefly colony using MTIDS. Remember that the kuramoto.mdl template needs to be added in MTIDS: Dynamics  $\rightarrow$  Add mdl template. You also need to set up the right parameters for synchronization, an example can be seen in Figure 3.7. In order to see the blinking in the correct time scale, you need to set up the simulation with a fixed step size in Simulink, more on this in section 3.5.

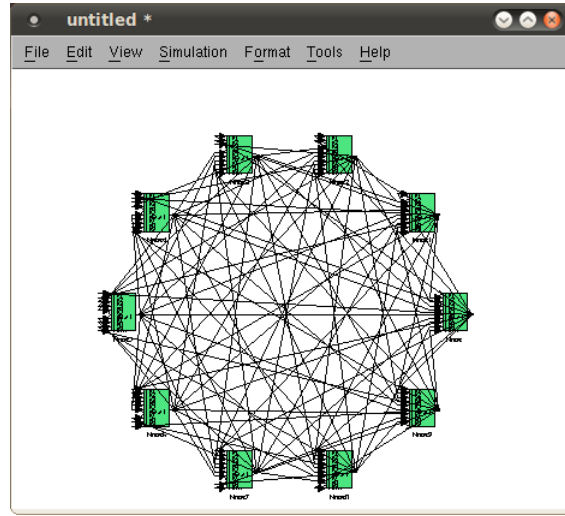


Figure 3.7: Simulation of 10 fireflies synchronizing. Parameters:  $K=2$ ,  $N=10$ ,  $\omega = 0.314$ ,  $\theta_0 = 1$ ,  $\text{var}=100$  (variation of starting point),  $\text{threshold} = 3/4 * 2\pi$

## 3.4 Layering/Clustering Nodes

The **key** to implement layering and clustering in MTIDS is the **interface node**. On clustered/layered interconnected systems there is always an interface that regulates the data communication of one layer/cluster to other layers/clusters. The interface has access to all nodes in the current cluster/layer and on most cases does some information processing (compression, principal component extraction, etc). This processed information is used to interact with other clusters/layers. Inside the cluster/layer the interface node acts like a normal node.

### 3.4.1 Crate a layer/cluster

In order to create a layer/cluster in MTIDS you need to export your system as a layer: **File** → **Export as a layer**. MTIDS will ask you to select a template for the interface node. You may select a customize interface node created by you or select the MTIDS provided interface node : **layerInterface.mdl**.

The result is a Simulink model that differs from the one that MTIDS normally produces, as it includes an extra node, the interface node. If we look more closely in Figure 3.8, we notice that this model also fulfills the requirements needed to build a standard node template, see subsection 3.3.1. By saving this model and using it as a node template in MTIDS we build many of this interconnected systems which interact with each other through their interface nodes, see Figure 3.9.

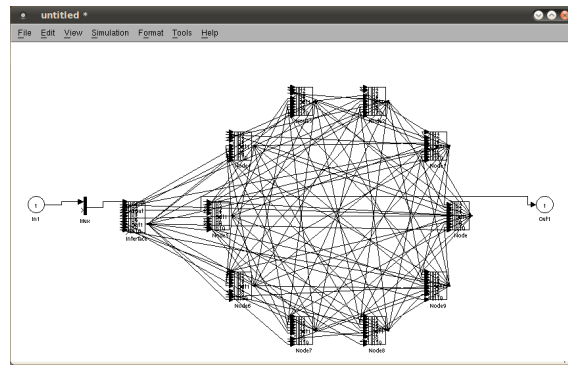


Figure 3.8: Resulting layer/cluster when exporting in MTIDS as layer. Example is a complete graph with 10 LTI nodes.

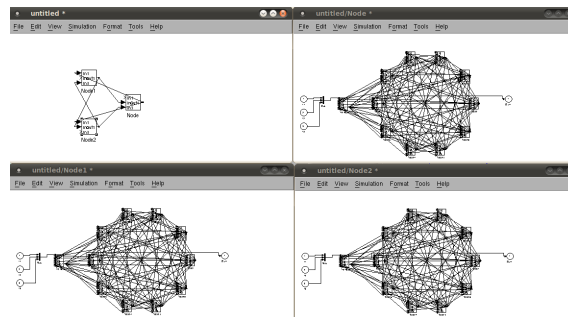


Figure 3.9: Resulting model of layered/clustered interconnected systems. Example uses a complete graph of 3 nodes where each node is an interface/cluster of a complete graph with 10 LTI nodes plus 1 interface node.

### 3.4.2 Build your own Interface Node

The user may define their own interface node behavior using the interface node template (**interfaceTemplate.mdl**).

As we see in Figure 3.10 the interface node requires a layer in and out port numbered as 1, which interacts with other layers/clusters. Moreover it requires the basic components of a node template (an in-port connected to a mux and an out-port) in order to interact with the nodes in the cluster/layer. MTIDS also comes preloaded with a simple aggregating interface template called **layerInterface.mdl**.

## 3.5 Working in Simulink

Here we review a couple of basic concepts which you will need to run and analyze the simulation of the interconnected dynamic systems produced by MTIDS. This is only a refresh, for more detail please go to : Mathworks Simulink Tutorial.



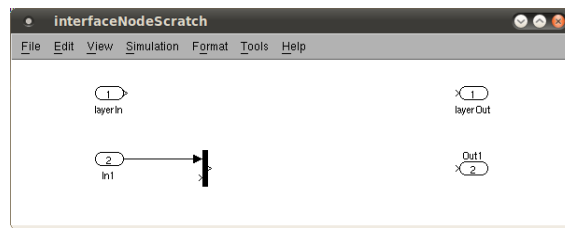


Figure 3.10: Interface node template model : **interfaceTemplate.mdl**.

### 3.5.1 Simulation Parameters

The parameters of your model can be defined in Simulink by hand. However, a better way is to define the parameters in the Simulink model as variables and give a value to this variables in the Matlab workspace. This also allows you to save this parameters by saving the workspace as a mat file with the command: `>> save name.mat`

### 3.5.2 Solver

Before running a simulation you need to define the simulation runtime and the numerical solver that Simulink will use to simulate your model. In Simulink: Simulation → Configure Parameters, and then going to the solver tab, you may define different types of solver, see Figure 3.11.

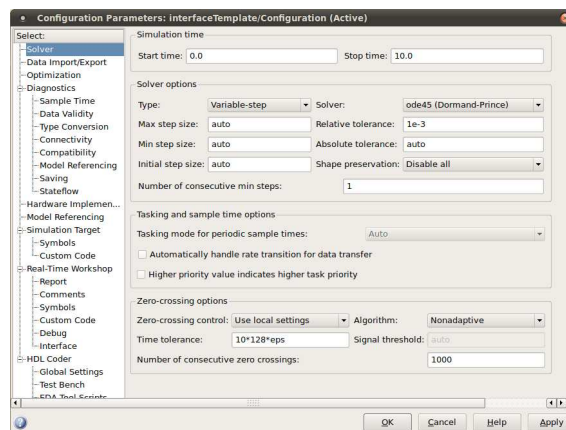


Figure 3.11: Simulink define solver

It is important to notice that if you want a correct time scale during simulation runtime, you need to define a fixed step size. This is used for example in the fireflies synchronization demo.

### 3.5.3 Visualize Simulation Data

The easiest way to visualize data during simulations in Simulink is to use scope blocks. The data can then be seen in real-time during simulation. Another way to do this in real-time is to use the 'To File' block or the 'To Workspace' block which allow a direct interaction with Matlab. Plotting functions can be defined in Matlab to interact with the simulation and show the progress in real time.

The other option is to visualize the result at the end of the simulation. For this you can define in Simulink which data should be send to the workspace under: Simulation → Configure Parameters at the tab of Import/Export, see Figure 3.12. Here it is useful to export the states, which Simulink defines as the values coming out of integrator blocks, but it is also possible to define them by hand.

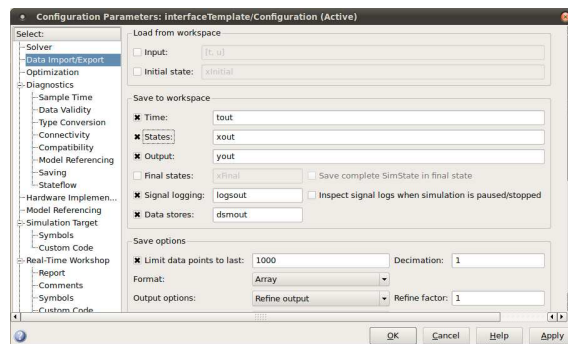


Figure 3.12: Simulink define import/export data

### 3.5.4 Working with a closed Model

Simulations can also be run from Matlab without the need to open the Simulink model. This is particularly useful for large Simulink models, like models of over 100 nodes that one may produce with MTIDS. One can write a Matlab script to parametrize and run the simulation. **Examples** can be found on the **help for the sim command**.

## 3.6 Import from Simulink

MTIDS also offers the possibility of importing Simulink models which were produced by MTIDS or are constructed following the MTIDS format, see section 3.2.

Notice that the dynamics of the imported will be the one that you have select in the MTIDS gui.

Node labels, position and topology is imported from Simulink to MTIDS. To do this in MTIDS: **Simulation** → **Import from Simulink** , see Figure 3.13. Finally, select the model you wish to import.

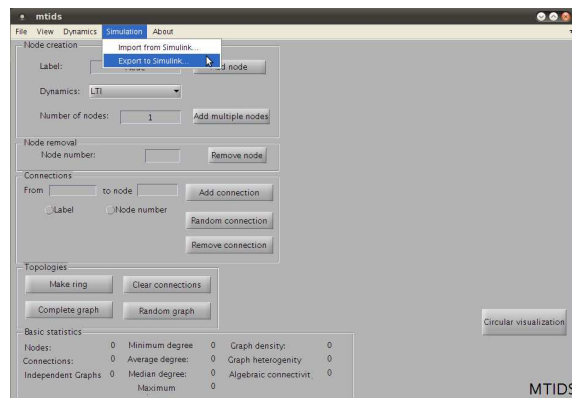


Figure 3.13: MTIDS import form Simulink



## Chapter 4

# Conclusion and Future Development

### 4.1 Conclusion

In this project a toolbox for the simulation of interconnected dynamical systems was developed. MTIDS (Matlab Toolbox of Interconnected Dynamical Systems) is a wrapper that combines tools used for graph theory analysis (Matgraph) and the simulation of interconnected systems (Simulink) were combine to create a flexible and extensible framework to make the simulation of interconnected dynamical systems easier for students and researchers.

MTIDS offers the following **features**:

- Futures

MTIDS is a toolbox aimed for students and researchers working in large-scale and interconnected dynamical systems. We would like to coform a community around this toolbox that helps push the research on this field forward.

There are still many issues and functions to improve in MTIDS:

- Issues.....



## Chapter 5

### MTIDS shortcuts





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