

# PROGRAMMING IN HASKELL



## Chapter 1 - Introduction

# What is a Functional Language?

Opinions differ, and it is difficult to give a precise definition, but generally speaking:

- z Functional programming is style of programming in which the basic method of computation is the application of functions to arguments;
- z A functional language is one that supports and encourages the functional style.

# Example

Summing the integers 1 to 10 in Java:

```
int total = 0;  
for (int i = 1; i ≤ 10; i++)  
    total = total + i;
```

The computation method is variable assignment.

# Example

Summing the integers 1 to 10 in Haskell:

```
sum [1..10]
```

The computation method is function application.

# A Taste of Haskell

```
f [] = []
```

```
f (x:xs) = f ys ++ [x] ++ f zs
```

```
  where
```

```
    ys = [a | a ← xs, a ≤ x]
```

```
    zs = [b | b ← xs, b > x]
```

?

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## Chapter 2 - First Steps

# Glasgow Haskell Compiler

- z GHC is the leading implementation of Haskell, and comprises a compiler and interpreter;
- z The interactive nature of the interpreter makes it well suited for teaching and prototyping;
- z GHC is freely available from:

[www.haskell.org/platform](http://www.haskell.org/platform)

# Starting GHCi

The interpreter can be started from the terminal command prompt \$ by simply typing ghci:

```
$ ghci
```

```
GHCi, version X: http://www.haskell.org/ghc/ :? for help
```

```
Prelude>
```

The GHCi prompt > means that the interpreter is now ready to evaluate an expression.



For example, it can be used as a desktop calculator to evaluate simple numeric expressions:

```
> 2+3*4
```

```
14
```

```
> (2+3)*4
```

```
20
```

```
> sqrt (3^2 + 4^2)
```

```
5.0
```

# The Standard Prelude

Haskell comes with a large number of standard library functions. In addition to the familiar numeric functions such as  $+$  and  $*$ , the library also provides many useful functions on lists.

z Select the first element of a list:

```
> head [1,2,3,4,5]  
1
```

- z Remove the first element from a list:

```
> tail [1,2,3,4,5]  
[2,3,4,5]
```

- z Select the nth element of a list:

```
> [1,2,3,4,5] !! 2  
3
```

- z Select the first n elements of a list:

```
> take 3 [1,2,3,4,5]  
[1,2,3]
```

z Remove the first n elements from a list:

```
> drop 3 [1,2,3,4,5]  
[4,5]
```

z Calculate the length of a list:

```
> length [1,2,3,4,5]  
5
```

z Calculate the sum of a list of numbers:

```
> sum [1,2,3,4,5]  
15
```

z Calculate the product of a list of numbers:

```
> product [1,2,3,4,5]  
120
```

z Append two lists:

```
> [1,2,3] ++ [4,5]  
[1,2,3,4,5]
```

z Reverse a list:

```
> reverse [1,2,3,4,5]  
[5,4,3,2,1]
```

# Function Application

In mathematics, function application is denoted using parentheses, and multiplication is often denoted using juxtaposition or space.

$$f(a,b) + c d$$

Apply the function  $f$  to  $a$  and  $b$ , and add the result to the product of  $c$  and  $d$ .

In Haskell, function application is denoted using space, and multiplication is denoted using `*`.

```
f a b + c*d
```



As previously, but in Haskell syntax.

Moreover, function application is assumed to have higher priority than all other operators.

$f\ a\ +\ b$

Means  $(f\ a) + b$ , rather than  $f\ (a + b)$ .



# Examples

## Mathematics

$f(x)$

$f(x, y)$

$f(g(x))$

$f(x, g(y))$

$f(x)g(y)$

## Haskell

$f\ x$

$f\ x\ y$

$f\ (g\ x)$

$f\ x\ (g\ y)$

$f\ x\ * \ g\ y$

# Haskell Scripts

- z As well as the functions in the standard library, you can also define your own functions;
- z New functions are defined within a script, a text file comprising a sequence of definitions;
- z By convention, Haskell scripts usually have a .hs suffix on their filename. This is not mandatory, but is useful for identification purposes.

# My First Script

When developing a Haskell script, it is useful to keep two windows open, one running an editor for the script, and the other running GHCi.

Start an editor, type in the following two function definitions, and save the script as test.hs:

```
double x = x + x
```

```
quadruple x = double (double x)
```

Leaving the editor open, in another window start up GHCi with the new script:

```
$ ghci test.hs
```

Now both the standard library and the file test.hs are loaded, and functions from both can be used:

```
> quadruple 10  
40  
  
> take (double 2) [1,2,3,4,5,6]  
[1,2,3,4]
```

Leaving GHCi open, return to the editor, add the following two definitions, and resave:

```
factorial n = product [1..n]  
average ns = sum ns `div` length ns
```

Note:

z `div` is enclosed in back quotes, not forward;

z `x `f` y` is just syntactic sugar for `f x y`.

GHCi does not automatically detect that the script has been changed, so a reload command must be executed before the new definitions can be used:

```
> :reload
Reading file "test.hs"

> factorial 10
3628800

> average [1,2,3,4,5]
3
```

# Useful GHCi Commands

<u>Command</u>	<u>Meaning</u>
<code>:load <i>name</i></code>	load script <i>name</i>
<code>:reload</code>	reload current script
<code>:set editor <i>name</i></code>	set editor to <i>name</i>
<code>:edit <i>name</i></code>	edit script <i>name</i>
<code>:edit</code>	edit current script
<code>:type <i>expr</i></code>	show type of <i>expr</i>
<code>:?</code>	show all commands
<code>:quit</code>	quit GHCi

# Naming Requirements

- z Function and argument names must begin with a lower-case letter. For example:

myFun

fun1

arg\_2

x'

- z By convention, list arguments usually have an s suffix on their name. For example:

xs

ns

nss



# The Layout Rule

In a sequence of definitions, each definition must begin in precisely the same column:

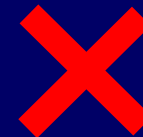
```
a = 10
b = 20
c = 30
```



```
a = 10
  b = 20
c = 30
```

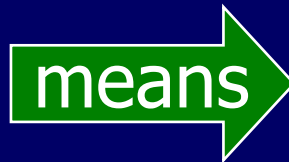


```
  a = 10
b = 20
  c = 30
```



The layout rule avoids the need for explicit syntax to indicate the grouping of definitions.

```
a = b + c
  where
    b = 1
    c = 2
d = a * 2
```



```
a = b + c
  where
    {b = 1;
     c = 2}
d = a * 2
```

implicit grouping

explicit grouping

# Exercises

- (1) Try out slides 2-7 and 13-16 using GHCi.
- (2) Fix the syntax errors in the program below, and test your solution using GHCi.

```
N = a 'div' length xs
  where
    a = 10
    xs = [1,2,3,4,5]
```

- (3) Show how the library function last that selects the last element of a list can be defined using the functions introduced in this lecture.
- (4) Can you think of another possible definition?
- (5) Similarly, show how the library function init that removes the last element from a list can be defined in two different ways.

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## Chapter 3 - Types and Classes

# What is a Type?

A type is a name for a collection of related values.  
For example, in Haskell the basic type

Bool

contains the two logical values:

False

True

# Type Errors

Applying a function to one or more arguments of the wrong type is called a type error.

```
> 1 + False  
error ...
```

1 is a number and False is a logical value, but + requires two numbers.

# Types in Haskell

- z If evaluating an expression  $e$  would produce a value of type  $t$ , then  $e$  has type  $t$ , written

$e :: t$

- z Every well formed expression has a type, which can be automatically calculated at compile time using a process called type inference.



- z All type errors are found at compile time, which makes programs safer and faster by removing the need for type checks at run time.
- z In GHCi, the :type command calculates the type of an expression, without evaluating it:

```
> not False  
True
```

```
> :type not False  
not False :: Bool
```

# Basic Types

Haskell has a number of basic types, including:

`Bool`

- logical values

`Char`

- single characters

`String`

- strings of characters

`Int`

- fixed-precision integers

`Integer`

- arbitrary-precision integers

`Float`

- floating-point numbers

# List Types

A list is sequence of values of the same type:

```
[False,True,False] :: [Bool]
```

```
['a','b','c','d'] :: [Char]
```

In general:

$[t]$  is the type of lists with elements of type  $t$ .

## Note:

- z The type of a list says nothing about its length:

```
[False,True] :: [Bool]
```

```
[False,True,False] :: [Bool]
```

- z The type of the elements is unrestricted. For example, we can have lists of lists:

```
[['a'],['b','c']] :: [[Char]]
```

# Tuple Types

A tuple is a sequence of values of different types:

```
(False,True) :: (Bool,Bool)
```

```
(False,'a',True) :: (Bool,Char,Bool)
```

In general:

$(t_1, t_2, \dots, t_n)$  is the type of  $n$ -tuples whose  $i$ th components have type  $t_i$  for any  $i$  in  $1 \dots n$ .

## Note:

- z The type of a tuple encodes its size:

```
(False, True) :: (Bool, Bool)
```

```
(False, True, False) :: (Bool, Bool, Bool)
```

- z The type of the components is unrestricted:

```
('a', (False, 'b')) :: (Char, (Bool, Char))
```

```
(True, ['a', 'b']) :: (Bool, [Char])
```

# Function Types

A function is a mapping from values of one type to values of another type:

```
not :: Bool → Bool
```

```
even :: Int → Bool
```

In general:

$t_1 \rightarrow t_2$  is the type of functions that map values of type  $t_1$  to values to type  $t_2$ .

## Note:

- z The arrow  $\rightarrow$  is typed at the keyboard as `->`.
- z The argument and result types are unrestricted. For example, functions with multiple arguments or results are possible using lists or tuples:

```
add :: (Int,Int) -> Int  
add (x,y) = x+y
```

```
zeroto :: Int -> [Int]  
zeroto n = [0..n]
```



# Curried Functions

Functions with multiple arguments are also possible by returning functions as results:

```
add' :: Int → (Int → Int)
add' x y = x+y
```

add' takes an integer x and returns a function add' x. In turn, this function takes an integer y and returns the result x+y.

## Note:

- z `add` and `add'` produce the same final result, but `add` takes its two arguments at the same time, whereas `add'` takes them one at a time:

```
add :: (Int,Int) → Int
```

```
add' :: Int → (Int → Int)
```

- z Functions that take their arguments one at a time are called curried functions, celebrating the work of Haskell Curry on such functions.

- z Functions with more than two arguments can be carried by returning nested functions:

```
mult :: Int → (Int → (Int → Int))  
mult x y z = x*y*z
```

mult takes an integer  $x$  and returns a function mult  $x$ , which in turn takes an integer  $y$  and returns a function mult  $x$   $y$ , which finally takes an integer  $z$  and returns the result  $x*y*z$ .

# Why is Currying Useful?

Curried functions are more flexible than functions on tuples, because useful functions can often be made by partially applying a curried function.

For example:

```
add' 1 :: Int → Int
```

```
take 5 :: [Int] → [Int]
```

```
drop 5 :: [Int] → [Int]
```

# Currying Conventions

To avoid excess parentheses when using curried functions, two simple conventions are adopted:

- z The arrow  $\rightarrow$  associates to the right.

$\text{Int} \rightarrow \text{Int} \rightarrow \text{Int} \rightarrow \text{Int}$



Means  $\text{Int} \rightarrow (\text{Int} \rightarrow (\text{Int} \rightarrow \text{Int}))$ .

- z As a consequence, it is then natural for function application to associate to the left.

```
mult x y z
```



Means  $((\text{mult } x) y) z$ .

Unless tupling is explicitly required, all functions in Haskell are normally defined in curried form.

# Polymorphic Functions

A function is called polymorphic (“of many forms”) if its type contains one or more type variables.

```
length :: [a] → Int
```



For any type  $a$ , `length` takes a list of values of type  $a$  and returns an integer.

## Note:

- z Type variables can be instantiated to different types in different circumstances:

```
> length [False,True]  
2
```

a = Bool

```
> length [1,2,3,4]  
4
```

a = Int

- z Type variables must begin with a lower-case letter, and are usually named a, b, c, etc.



- z Many of the functions defined in the standard prelude are polymorphic. For example:

```
fst :: (a,b) → a
```

```
head :: [a] → a
```

```
take :: Int → [a] → [a]
```

```
zip :: [a] → [b] → [(a,b)]
```

```
id :: a → a
```

# Overloaded Functions

A polymorphic function is called overloaded if its type contains one or more class constraints.

```
(+) :: Num a => a -> a -> a
```

For any numeric type  $a$ ,  $(+)$  takes two values of type  $a$  and returns a value of type  $a$ .

## Note:

- z Constrained type variables can be instantiated to any types that satisfy the constraints:

```
> 1 + 2  
3
```

a = Int

```
> 1.0 + 2.0  
3.0
```

a = Float

```
> 'a' + 'b'  
ERROR
```

Char is not a  
numeric type

z Haskell has a number of type classes, including:

**Num** - Numeric types

**Eq** - Equality types

**Ord** - Ordered types

z For example:

```
(+) :: Num a => a -> a -> a
```

```
(==) :: Eq a => a -> a -> Bool
```

```
(<) :: Ord a => a -> a -> Bool
```

# Hints and Tips

- z When defining a new function in Haskell, it is useful to begin by writing down its type;
- z Within a script, it is good practice to state the type of every new function defined;
- z When stating the types of polymorphic functions that use numbers, equality or orderings, take care to include the necessary class constraints.

# Exercises

(1) What are the types of the following values?

```
['a', 'b', 'c']
```

```
('a', 'b', 'c')
```

```
[(False, '0'), (True, '1')]
```

```
[(False, True), ['0', '1']]
```

```
[tail, init, reverse]
```

(2) What are the types of the following functions?

```
second xs = head (tail xs)
```

```
swap (x,y) = (y,x)
```

```
pair x y = (x,y)
```

```
double x = x*2
```

```
palindrome xs = reverse xs == xs
```

```
twice f x = f (f x)
```

(3) Check your answers using GHCi.

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## Chapter 4 - Defining Functions



# Conditional Expressions

As in most programming languages, functions can be defined using conditional expressions.

```
abs :: Int → Int  
abs n = if n ≥ 0 then n else -n
```

abs takes an integer  $n$  and returns  $n$  if it is non-negative and  $-n$  otherwise.

Conditional expressions can be nested:

```
signum :: Int → Int
signum n = if n < 0 then -1 else
            if n == 0 then 0 else 1
```

Note:

- z In Haskell, conditional expressions must always have an else branch, which avoids any possible ambiguity problems with nested conditionals.

# Guarded Equations

As an alternative to conditionals, functions can also be defined using guarded equations.

```
abs n | n ≥ 0      = n  
      | otherwise = -n
```

As previously, but using guarded equations.

Guarded equations can be used to make definitions involving multiple conditions easier to read:

```
signum n | n < 0      = -1  
         | n == 0     = 0  
         | otherwise  = 1
```

Note:

- z The catch all condition otherwise is defined in the prelude by `otherwise = True`.

# Pattern Matching

Many functions have a particularly clear definition using pattern matching on their arguments.

```
not :: Bool → Bool  
not False = True  
not True  = False
```



not maps False to True, and True to False.

Functions can often be defined in many different ways using pattern matching. For example

```
(&&) :: Bool → Bool → Bool
True  && True   = True
True  && False  = False
False && True   = False
False && False  = False
```

can be defined more compactly by

```
True && True = True
_    && _    = False
```

However, the following definition is more efficient, because it avoids evaluating the second argument if the first argument is False:

```
True  && b = b  
False && _ = False
```

Note:

- z The underscore symbol `_` is a wildcard pattern that matches any argument value.

- z Patterns are matched in order. For example, the following definition always returns False:

```
_      && _      = False
True && True = True
```

- z Patterns may not repeat variables. For example, the following definition gives an error:

```
b && b = b
_ && _ = False
```



# List Patterns

Internally, every non-empty list is constructed by repeated use of an operator (`:`) called “cons” that adds an element to the start of a list.

`[1, 2, 3, 4]`

Means `1:(2:(3:(4:[])))`.

Functions on lists can be defined using x:xs patterns.

```
head :: [a] → a  
head (x:_) = x
```

```
tail :: [a] → [a]  
tail (_:xs) = xs
```

head and tail map any non-empty list to its first and remaining elements.

## Note:

- z `x:xs` patterns only match non-empty lists:

```
> head []  
*** Exception: empty list
```

- z `x:xs` patterns must be parenthesised, because application has priority over `(:)`. For example, the following definition gives an error:

```
head x:_ = x
```

# Lambda Expressions

Functions can be constructed without naming the functions by using lambda expressions.

$$\lambda x \rightarrow x + x$$

the nameless function that takes a number  $x$  and returns the result  $x + x$ .

## Note:

- z The symbol  $\lambda$  is the Greek letter lambda, and is typed at the keyboard as a backslash `\`.
- z In mathematics, nameless functions are usually denoted using the  $\mapsto$  symbol, as in  $x \mapsto x + x$ .
- z In Haskell, the use of the  $\lambda$  symbol for nameless functions comes from the lambda calculus, the theory of functions on which Haskell is based.

# Why Are Lambda's Useful?

Lambda expressions can be used to give a formal meaning to functions defined using currying.

For example:

```
add x y = x + y
```

means

```
add =  $\lambda x \rightarrow (\lambda y \rightarrow x + y)$ 
```

Lambda expressions are also useful when defining functions that return functions as results.

For example:

```
const :: a → b → a  
const x _ = x
```

is more naturally defined by

```
const :: a → (b → a)  
const x = λ_ → x
```

Lambda expressions can be used to avoid naming functions that are only referenced once.

For example:

```
odds n = map f [0..n-1]
      where
        f x = x*2 + 1
```

can be simplified to

```
odds n = map ( $\lambda x \rightarrow x*2 + 1$ ) [0..n-1]
```



# Operator Sections

An operator written between its two arguments can be converted into a curried function written before its two arguments by using parentheses.

For example:

```
> 1+2
```

```
3
```

```
> (+) 1 2
```

```
3
```

This convention also allows one of the arguments of the operator to be included in the parentheses.

For example:

> (1+) 2

3

> (+2) 1

3

In general, if  $\oplus$  is an operator then functions of the form  $(\oplus)$ ,  $(x\oplus)$  and  $(\oplus y)$  are called sections.

# Why Are Sections Useful?

Useful functions can sometimes be constructed in a simple way using sections. For example:

$(1+)$  - successor function

$(1/)$  - reciprocation function

$(*2)$  - doubling function

$(/2)$  - halving function

# Exercises

- (1) Consider a function safetail that behaves in the same way as tail, except that safetail maps the empty list to the empty list, whereas tail gives an error in this case. Define safetail using:
- (a) a conditional expression;
  - (b) guarded equations;
  - (c) pattern matching.

Hint: the library function `null :: [a] → Bool` can be used to test if a list is empty.

- (2) Give three possible definitions for the logical or operator (||) using pattern matching.
- (3) Redefine the following version of (&&) using conditionals rather than patterns:

```
True  && True  = True
_     && _     = False
```

- (4) Do the same for the following version:

```
True  && b = b
False && _ = False
```

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## Chapter 5 - List Comprehensions

# Set Comprehensions

In mathematics, the comprehension notation can be used to construct new sets from old sets.

$$\{x^2 \mid x \in \{1\dots 5\}\}$$

The set  $\{1,4,9,16,25\}$  of all numbers  $x^2$  such that  $x$  is an element of the set  $\{1\dots 5\}$ .

# List Comprehensions

In Haskell, a similar comprehension notation can be used to construct new lists from old lists.

```
[x^2 | x ← [1..5]]
```

The list [1,4,9,16,25] of all numbers  $x^2$  such that  $x$  is an element of the list [1..5].



## Note:

- z The expression  $x \leftarrow [1..5]$  is called a generator, as it states how to generate values for  $x$ .
- z Comprehensions can have multiple generators, separated by commas. For example:

```
> [(x,y) | x ← [1,2,3], y ← [4,5]]  
[(1,4), (1,5), (2,4), (2,5), (3,4), (3,5)]
```

- z Changing the order of the generators changes the order of the elements in the final list:

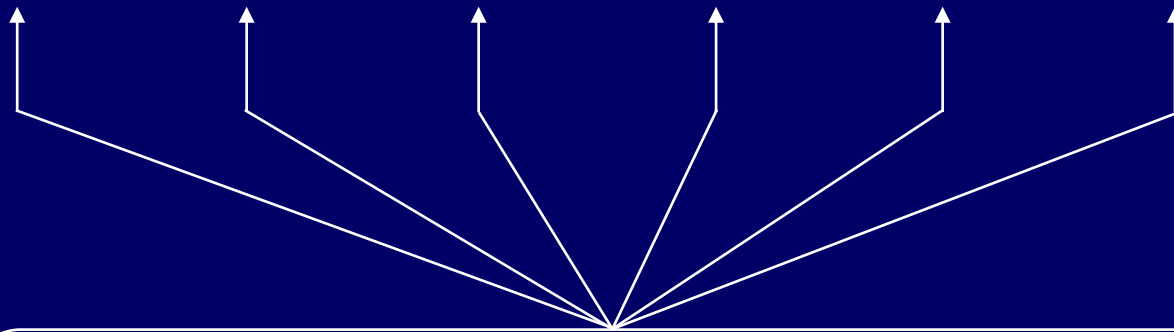
```
> [(x,y) | y ← [4,5], x ← [1,2,3]]  
[(1,4),(2,4),(3,4),(1,5),(2,5),(3,5)]
```

- z Multiple generators are like nested loops, with later generators as more deeply nested loops whose variables change value more frequently.

z For example:

```
> [(x,y) | y ← [4,5], x ← [1,2,3]]
```

```
[(1,4), (2,4), (3,4), (1,5), (2,5), (3,5)]
```



$x \leftarrow [1,2,3]$  is the last generator, so the value of the x component of each pair changes most frequently.

# Dependant Generators

Later generators can depend on the variables that are introduced by earlier generators.

$[(x, y) \mid x \leftarrow [1..3], y \leftarrow [x..3]]$

The list  $[(1,1),(1,2),(1,3),(2,2),(2,3),(3,3)]$  of all pairs of numbers  $(x,y)$  such that  $x,y$  are elements of the list  $[1..3]$  and  $y \geq x$ .

Using a dependant generator we can define the library function that concatenates a list of lists:

```
concat :: [[a]] → [a]
concat xss = [x | xs ← xss, x ← xs]
```

For example:

```
> concat [[1,2,3],[4,5],[6]]
[1,2,3,4,5,6]
```

# Guards

List comprehensions can use guards to restrict the values produced by earlier generators.

```
[x | x ← [1..10], even x]
```

The list [2,4,6,8,10] of all numbers x such that x is an element of the list [1..10] and x is even.

Using a guard we can define a function that maps a positive integer to its list of factors:

```
factors :: Int → [Int]
factors n =
    [x | x ← [1..n], n `mod` x == 0]
```

For example:

```
> factors 15
[1,3,5,15]
```

A positive integer is prime if its only factors are 1 and itself. Hence, using factors we can define a function that decides if a number is prime:

```
prime :: Int → Bool  
prime n = factors n == [1,n]
```

For example:

```
> prime 15  
False  
  
> prime 7  
True
```



Using a guard we can now define a function that returns the list of all primes up to a given limit:

```
primes :: Int → [Int]
primes n = [x | x ← [2..n], prime x]
```

For example:

```
> primes 40
[2,3,5,7,11,13,17,19,23,29,31,37]
```

# The Zip Function

A useful library function is `zip`, which maps two lists to a list of pairs of their corresponding elements.

```
zip :: [a] → [b] → [(a,b)]
```

For example:

```
> zip ['a', 'b', 'c'] [1,2,3,4]  
[('a',1), ('b',2), ('c',3)]
```

Using `zip` we can define a function returns the list of all pairs of adjacent elements from a list:

```
pairs :: [a] → [(a,a)]  
pairs xs = zip xs (tail xs)
```

For example:

```
> pairs [1,2,3,4]  
[(1,2), (2,3), (3,4)]
```

Using pairs we can define a function that decides if the elements in a list are sorted:

```
sorted :: Ord a => [a] -> Bool  
sorted xs = and [x ≤ y | (x,y) ← pairs xs]
```

For example:

```
> sorted [1,2,3,4]  
True  
  
> sorted [1,3,2,4]  
False
```

Using `zip` we can define a function that returns the list of all positions of a value in a list:

```
positions :: Eq a => a -> [a] -> [Int]
positions x xs =
    [i | (x',i) <- zip xs [0..], x == x']
```

For example:

```
> positions 0 [1,0,0,1,0,1,1,0]
[1,2,4,7]
```

# String Comprehensions

A string is a sequence of characters enclosed in double quotes. Internally, however, strings are represented as lists of characters.

```
"abc" :: String
```



Means ['a', 'b', 'c'] :: [Char].

Because strings are just special kinds of lists, any polymorphic function that operates on lists can also be applied to strings. For example:

```
> length "abcde"
```

```
5
```

```
> take 3 "abcde"
```

```
"abc"
```

```
> zip "abc" [1,2,3,4]
```

```
[('a',1),('b',2),('c',3)]
```

Similarly, list comprehensions can also be used to define functions on strings, such counting how many times a character occurs in a string:

```
count :: Char → String → Int  
count x xs = length [x' | x' ← xs, x == x']
```

For example:

```
> count 's' "Mississippi"  
4
```



# Exercises

- (1) A triple  $(x,y,z)$  of positive integers is called pythagorean if  $x^2 + y^2 = z^2$ . Using a list comprehension, define a function

```
pyths :: Int → [(Int,Int,Int)]
```

that maps an integer  $n$  to all such triples with components in  $[1..n]$ . For example:

```
> pyths 5  
[(3,4,5), (4,3,5)]
```

(2) A positive integer is perfect if it equals the sum of all of its factors, excluding the number itself. Using a list comprehension, define a function

```
perfects :: Int → [Int]
```

that returns the list of all perfect numbers up to a given limit. For example:

```
> perfects 500
```

```
[6, 28, 496]
```

- (3) The scalar product of two lists of integers `xs` and `ys` of length `n` is give by the sum of the products of the corresponding integers:

$$\sum_{i=0}^{n-1} (xs_i * ys_i)$$

Using a list comprehension, define a function that returns the scalar product of two lists.

