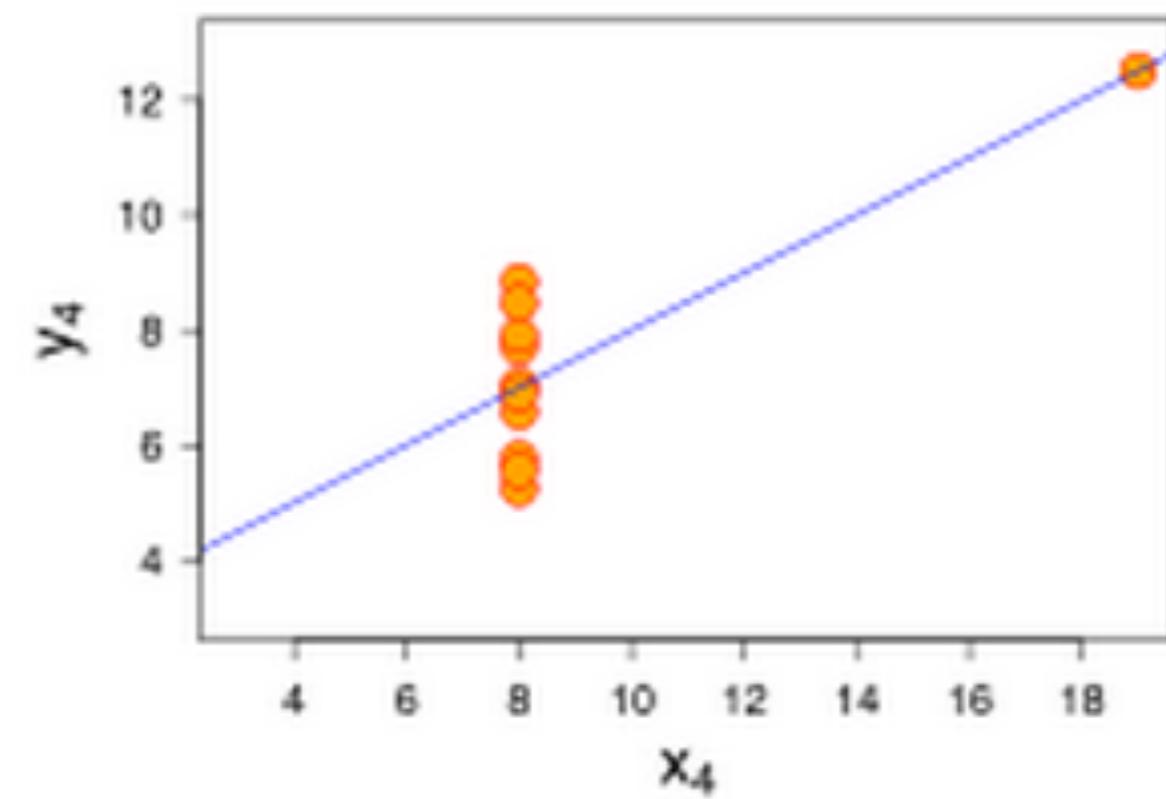
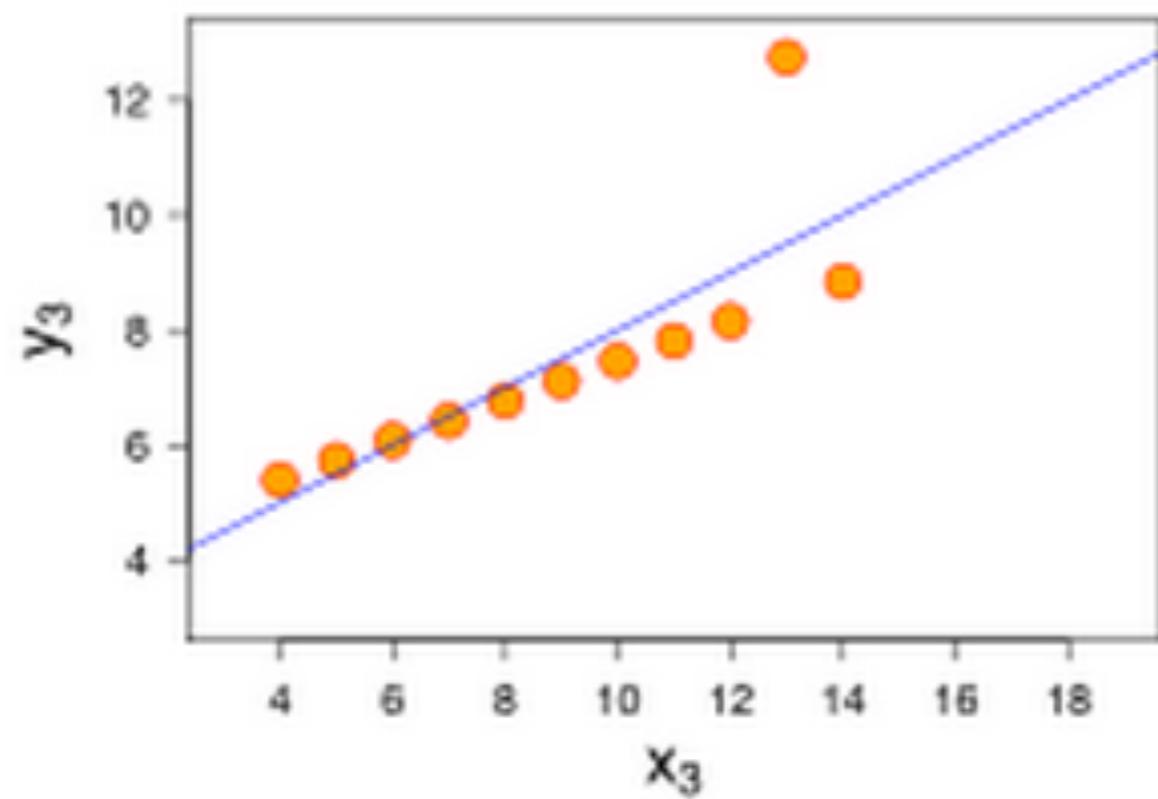
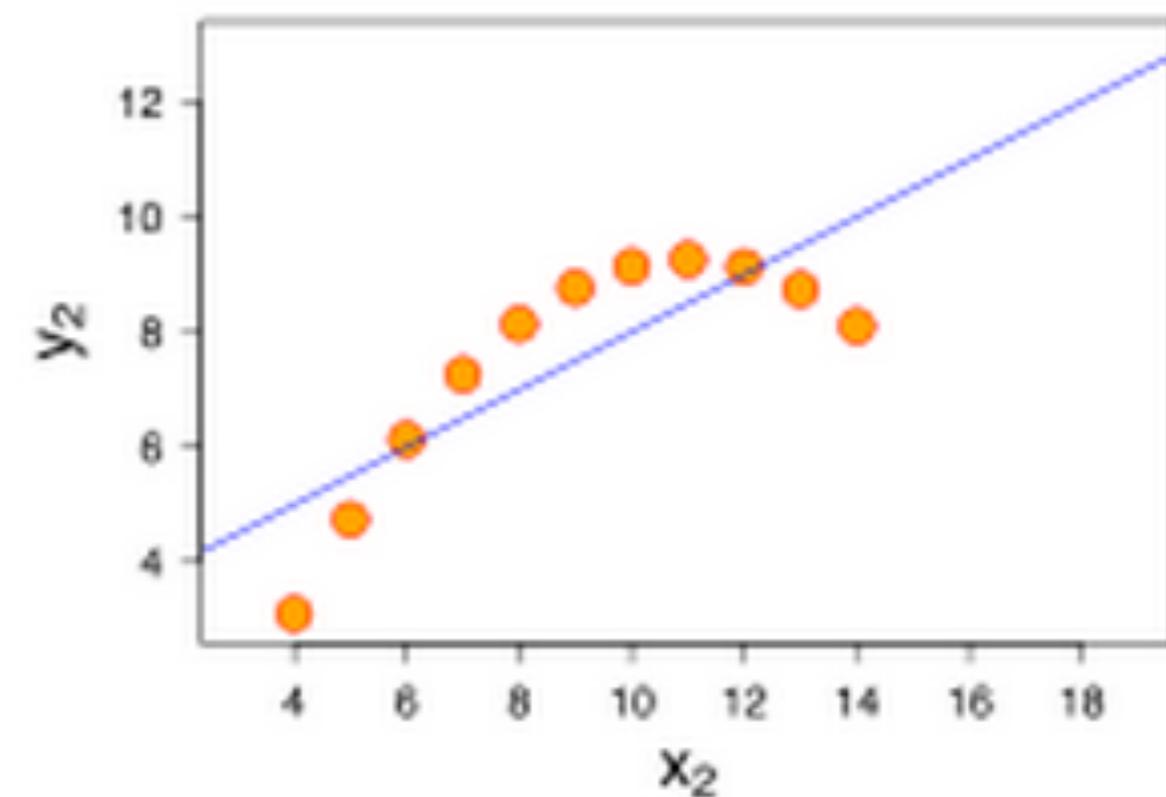
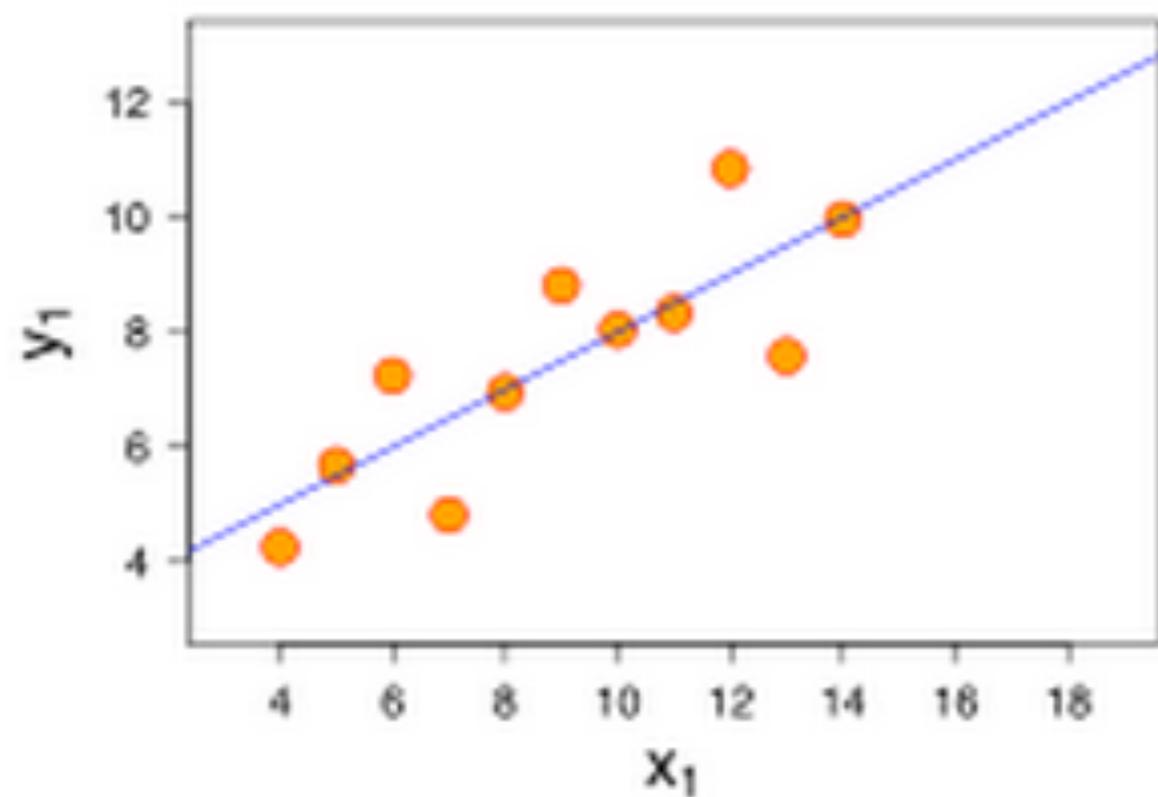


# Retrospective, Wrap-Up, What's Next

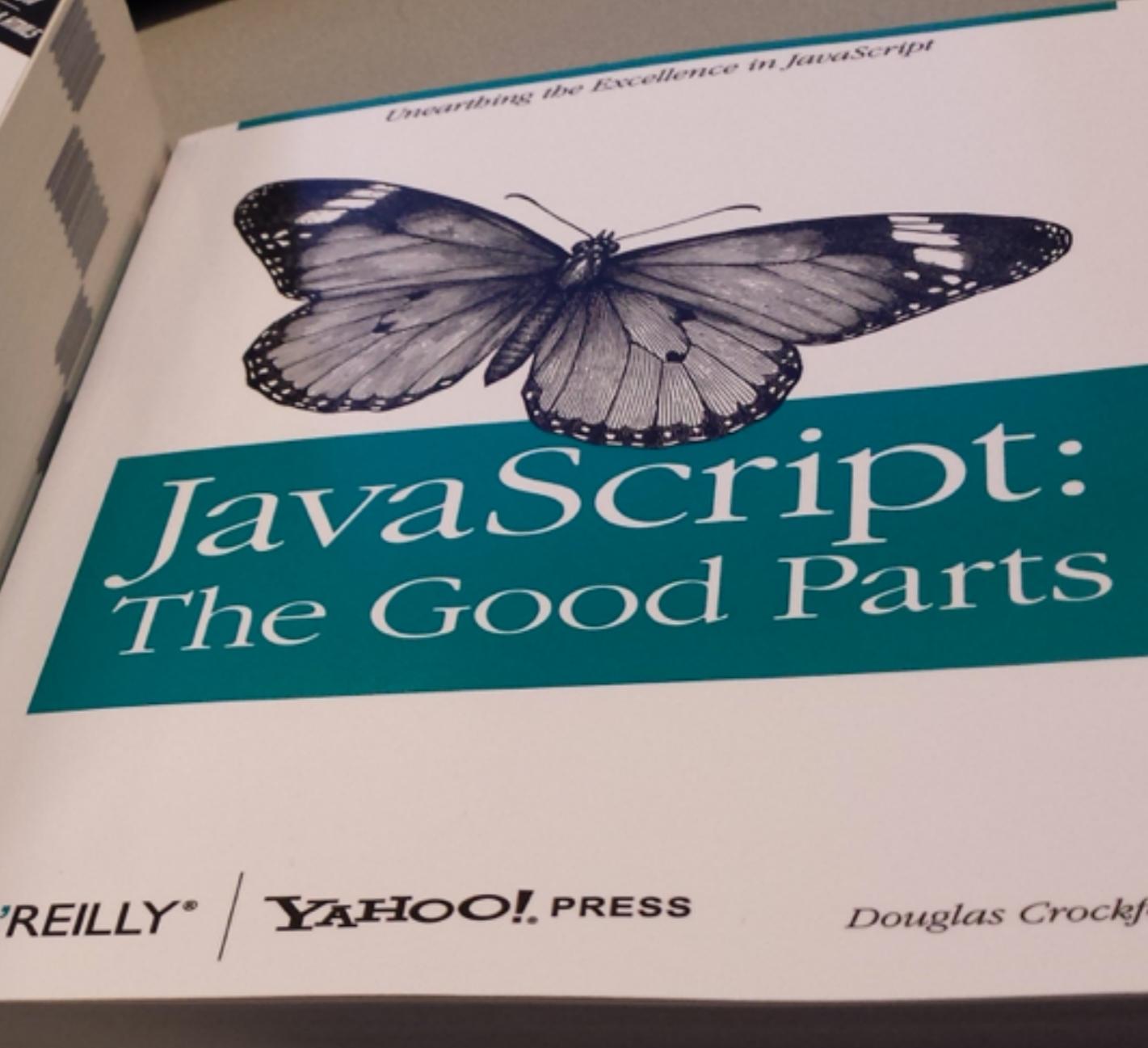
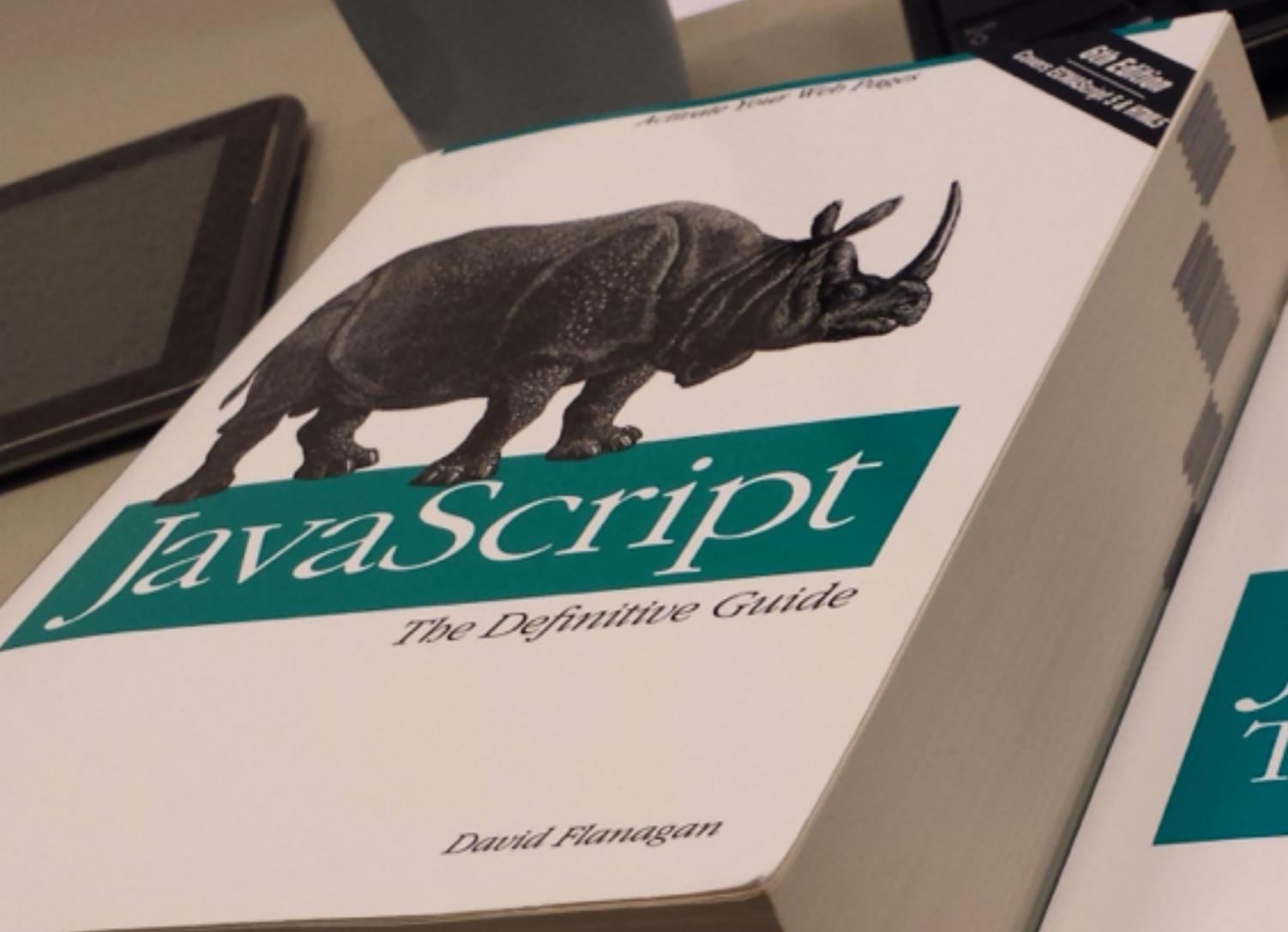
CS444

Property	Value
Mean of $x$ in each case	9 (exact)
Sample variance of $x$ in each case	11 (exact)
Mean of $y$ in each case	7.50 (to 2 decimal places)
Sample variance of $y$ in each case	4.122 or 4.127 (to 3 decimal places)
Correlation between $x$ and $y$ in each case	0.816 (to 3 decimal places)
Linear regression line in each case	$y = 3.00 + 0.500X$ (to 2 and 3 decimal places, respectively)



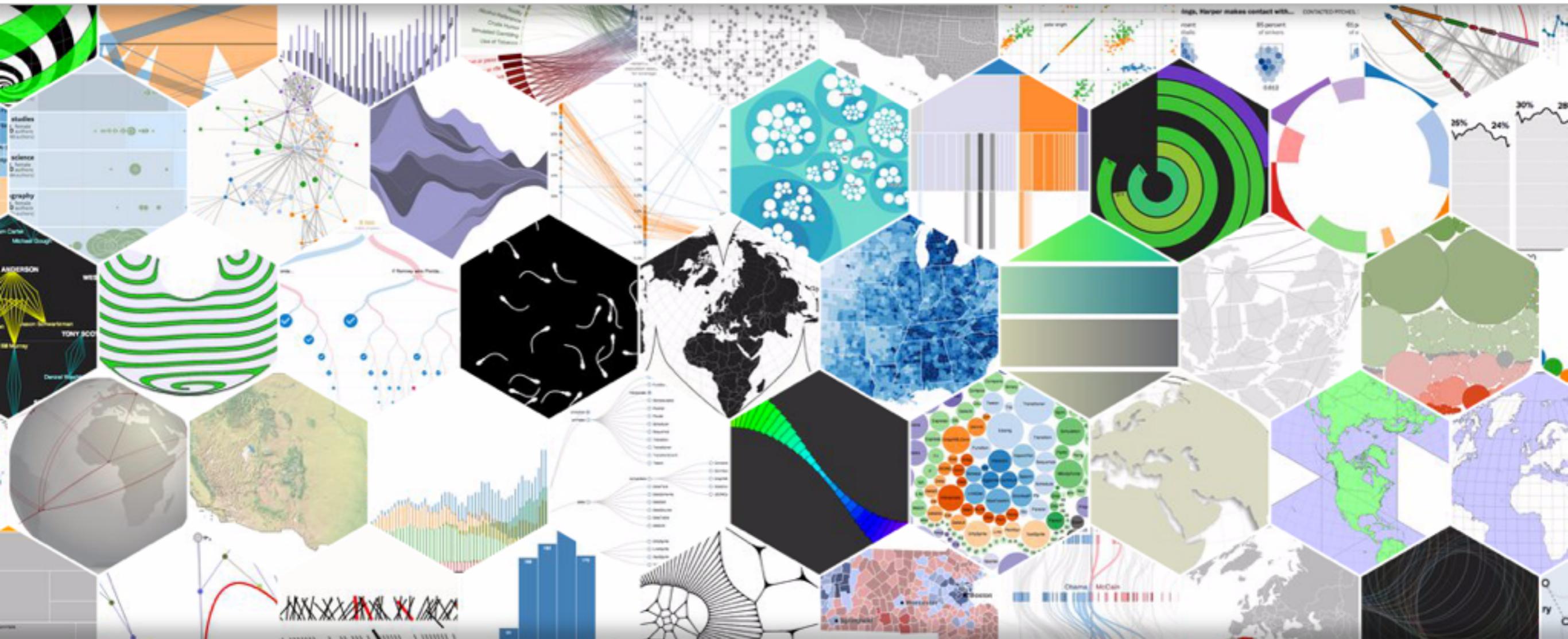
We do visualization not  
because it's pretty  
(although it can  
certainly be!), but  
because **it works**  
**better**

# Mechanics





# Data-Driven Documents



**D3.js** is a JavaScript library for manipulating documents based on data. **D3** helps you bring data to life using HTML, SVG, and CSS. D3's emphasis on web standards gives you the full capabilities of modern browsers without tying yourself to a proprietary framework, combining powerful visualization components and a data-driven approach to DOM manipulation.

[See more examples.](#)

# Why did we bother?

- It's the state of the art
  - (I know, right?! If you care, come help me fix it!)
- It's what actually gets used in the real world

 [mbostock / d3](#)

 Watch ▾ 1,392

 Unstar 37,351

 Fork 9,493

- What you learned in this class is exactly what the New York Times pros use

# Why did we bother?

- It's the state of the art
  - (I know, right?! If you care, come help me fix it!)
- It's what actually gets used in the real world



d3 / d3

Watch ▾

2,855

Unstar

57,638

Fork

15,435

- What you learned in this class is exactly what the New York Times pros use

# What did we leave out?

- We learned how to use d3, and we learned how to write a part of it
- But we didn't go into a lot of detail of how d3 is implemented
  - If we want to improve things, we must first understand them
  - API design for visualization is important!

# What did we leave out?

- Web technologies for more complex graphics
  - Canvas, WebGL
- Non-web technologies
  - Raw OpenGL, for when all else fails

# SVG: ~1K points

```
svg.append("rect")
  .attr("class", "overlay")
  .attr("width", width)
  .attr("height", height);

var circle = svg.selectAll("circle")
  .data(data)
  .enter().append("circle")
  .attr("r", 2.5)
  .attr("transform", transform);

function zoom() {
  circle.attr("transform", transform);
}

function transform(d) {
  return "translate(" + x(d[0]) + "," + y(d[1]))
}
```

<http://bl.ocks.org/mbostock/3680957>

# Canvas: ~50K points

```
function zoom() {
  canvas.clearRect(0, 0, width, height);
  draw();
}

function draw() {
  var i = -1, n = data.length, d, cx, cy;
  canvas.beginPath();
  while (++i < n) {
    d = data[i];
    cx = x(d[0]);
    cy = y(d[1]);
    canvas.moveTo(cx, cy);
    canvas.arc(cx, cy, 2.5, 0, 2 * Math.PI);
  }
  canvas.fill();
```

<http://bl.ocks.org/mbostock/3681006>

# WebGL: ~1M points

```
1  Function WebGLCircleRenderer(glowContext, circleCount, colors, radii, alpha) {
2    this.context = glowContext;
3    this.count = circleCount;
4
5    var vertShader = [
6      "uniform mat4 u_matrix",
7      "attribute float a_x",
8      "attribute float a_y",
9      "attribute float a_radius",
10     "attribute vec3 a_color",
11     "varying vec3 v_color",
12   ];
13
14   "void main() {\n",
15   "  gl_PointSize = a_radius;\n",
16   "  gl_Position = u_matrix * vec4(a_x, a_y, 1.0, 1.0);\n",
17   "  v_color = a_color;\n",
18   }".join("\n");
19
20   var fragShader = [
21     "precision mediump float;",
22     "uniform float u_alpha;",
23     "varying vec3 v_color",
24   ];
25
26   "void main() {\n",
27   "  float centerDist = length(gl_PointCoord - 0.5);\n",
28   "  float radius = 0.5;\n",
29   // works for overlapping circles if blending is enabled
30   "  gl_FragColor = vec4(v_color, u_alpha * step(centerDist, radius));\n",
31   }".join("\n");
32
33   var circleShaderInfo = {
34     vertexShader: vertShader,
35     fragmentShader: fragShader,
36
37     data: {
38       // uniforms
39       // Use a transformation matrix that makes 1 unit 1 pixel.
40       u_matrix: { value: new Float32Array([
41         2 / this.context.width, 0, 0,
42         0, 2 / this.context.height, 0, 0,
43         0, 0, 1, 0,
44         -1, -1, 0, 1
45       ])},
46       u_alpha: { value: new Float32Array([alpha]) },
47
48       // attributes
49       a_color: new Float32Array(colors),
50       a_radius: new Float32Array(radii),
51       a_x: new Float32Array(circleCount),
52       a_y: new Float32Array(circleCount)
53     },
54     primitives: this.context.GL.POINTS,
55
56     interleave: {
57       a_x: false,
58       a_y: false
59     },
60
61     usage: {
62       a_x: this.context.GL.DYNAMIC_DRAW,
63       a_y: this.context.GL.DYNAMIC_DRAW
64     }
65   };
66
67   this.shader = new GLWr.Shader(circleShaderInfo);
68
69   WebGLCircleRenderer.prototype.setPositions = function(xs, ys) {
70     this.shader.attributes.a_x.bufferSubData(xs);
71     this.shader.attributes.a_y.bufferSubData(ys);
72   }
73
74   WebGLCircleRenderer.prototype.draw = function() {
75     this.shader.draw();
76   }
77
78   WebGLCircleRenderer.prototype.dispose = function() {
79     delete this.context;
80     this.shader.dispose();
81     delete this.shader;
82   }
83 }
```

```
19  var context, state, animationID, circleRenderer;
20  function initPage() {
21    var container = document.getElementById("container");
22
23    context = new GLWr.Context({
24      width: container.offsetWidth,
25      height: container.offsetHeight,
26      alpha: true
27    });
28
29    if (null === context.GL) {
30      alert("no WebGL!");
31      return false;
32    }
33
34    container.appendChild(context.domElement);
35    context.setupClear({ red: 0, green: 0, blue: 0.3 });
36    context.GL.enable(context.GL.BLEND);
37    context.GL.blendFunc(context.GL.SRC_ALPHA,
38      context.GL.ONE_MINUS_SRC_ALPHA);
39
40    state = new State();
41    state.addElement();
42    state.addElement.style.position = 'absolute';
43    state.addElement.style.left = '0px';
44    state.addElement.style.top = '0px';
45    document.body.appendChild(state.addElement);
46
47    return true;
48  }
49
50  function initCircle() {
51    if (animationID === undefined) {
52      cancelAnimationFrame(animationID);
53      circleRenderer.dispose();
54    }
55
56    var numPoints = parseInt(document.getElementById("numCircles").value);
57    var minRadius = 5;
58    var maxRadius = parseInt(document.getElementById("maxRadius").value);
59    var alpha = parseFloat(document.getElementById("alpha").value);
60    var maxVelocity = 0.5;
61    var bands = 3;
62    var bandWidth = 0.25;
63    var pointsPerBand = (numPoints / bands) | 0;
64
65    var colors = new Float32Array(numPoints * 3);
66    var xs = new Float32Array(numPoints);
67    var ys = new Float32Array(numPoints);
68    var radii = new Float32Array(numPoints);
69    var phase = new Float32Array(numPoints);
70
71    for (var band = 0; band < bands; band++) {
72      for (var i = 0; i < pointsPerBand; i++) {
73        var point = (band * pointsPerBand) + i;
74        colors[point * 3] = ((band + 0.2) * 10) + 0.8 * (1 / pointsPerBand);
75        colors[point * 3 + 1] = ((band + 0.2) * 10) + 0.8 * (1 / pointsPerBand);
76        colors[point * 3 + 2] = ((band + 0.2) * 10) + 0.8 * (1 / pointsPerBand);
77
78        xs[point] = (1 / pointsPerBand) * context.width;
79        ys[point] = ((band / bands) * context.height) + (Math.random() * ((context.height - bandWidth) / bands));
80        radii[point] = minRadius + (Math.random() * (maxRadius - minRadius));
81        phase[point] = Math.random() * Math.PI * 2;
82      }
83    }
84
85    circleRenderer.setPositions(xs, ys);
86
87    context.cache.clear();
88    context.clear();
89    circleRenderer.draw();
90    animationID = requestAnimationFrame(step);
91
92    state.end();
93  }
94
95  animationID = requestAnimationFrame(step);
96
97  if (initPage()) {
98    var drawButton = document.getElementById("drawButton");
99    drawButton.onclick = initCircle;
100   initCircle();
101 }
```

# CUDA/OpenGL: 32M points



NVIDIA  
GAMEWORLDS

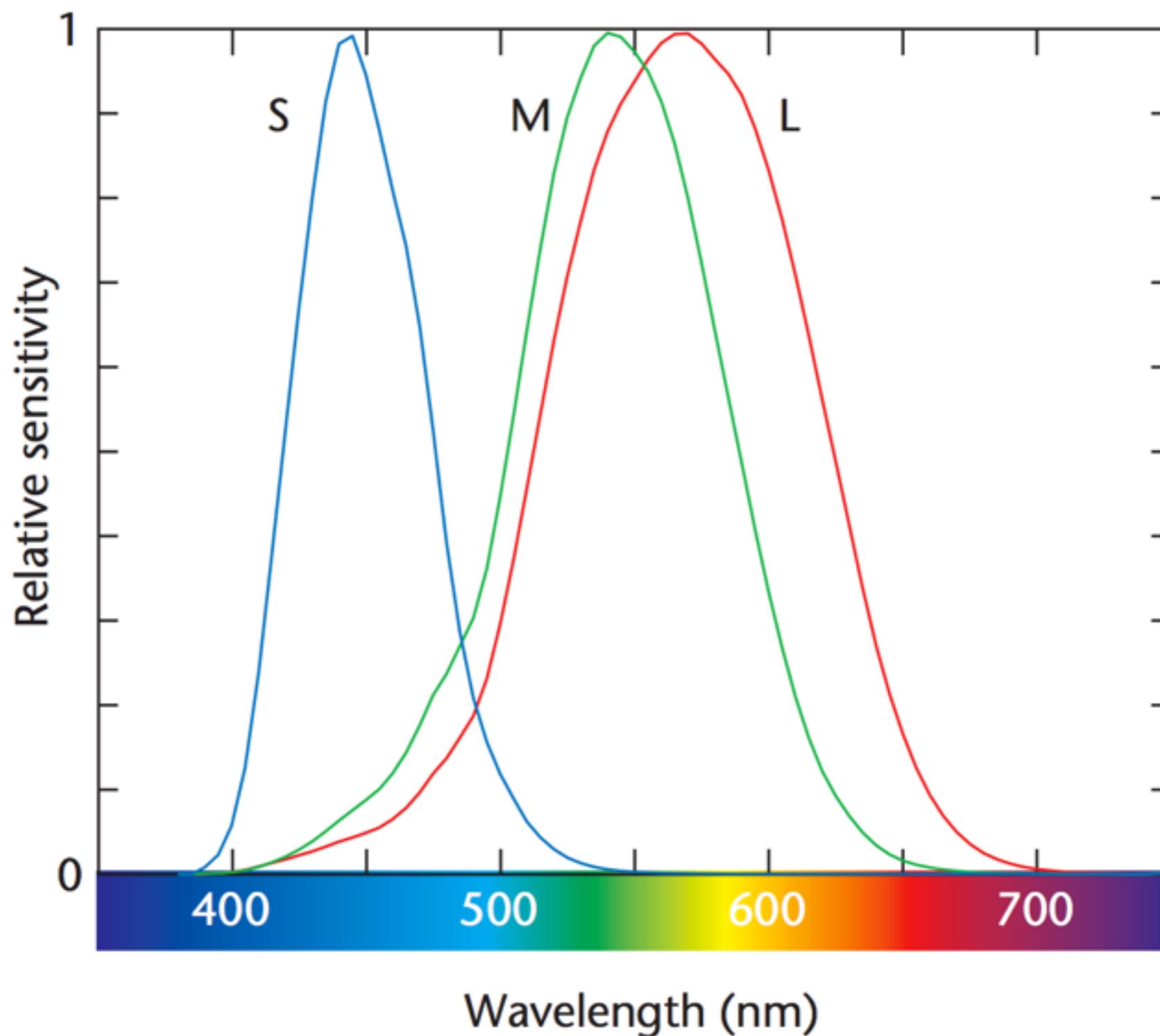
0:09 / 1:25

<https://www.youtube.com/watch?v=NDLPOJsqqoA>

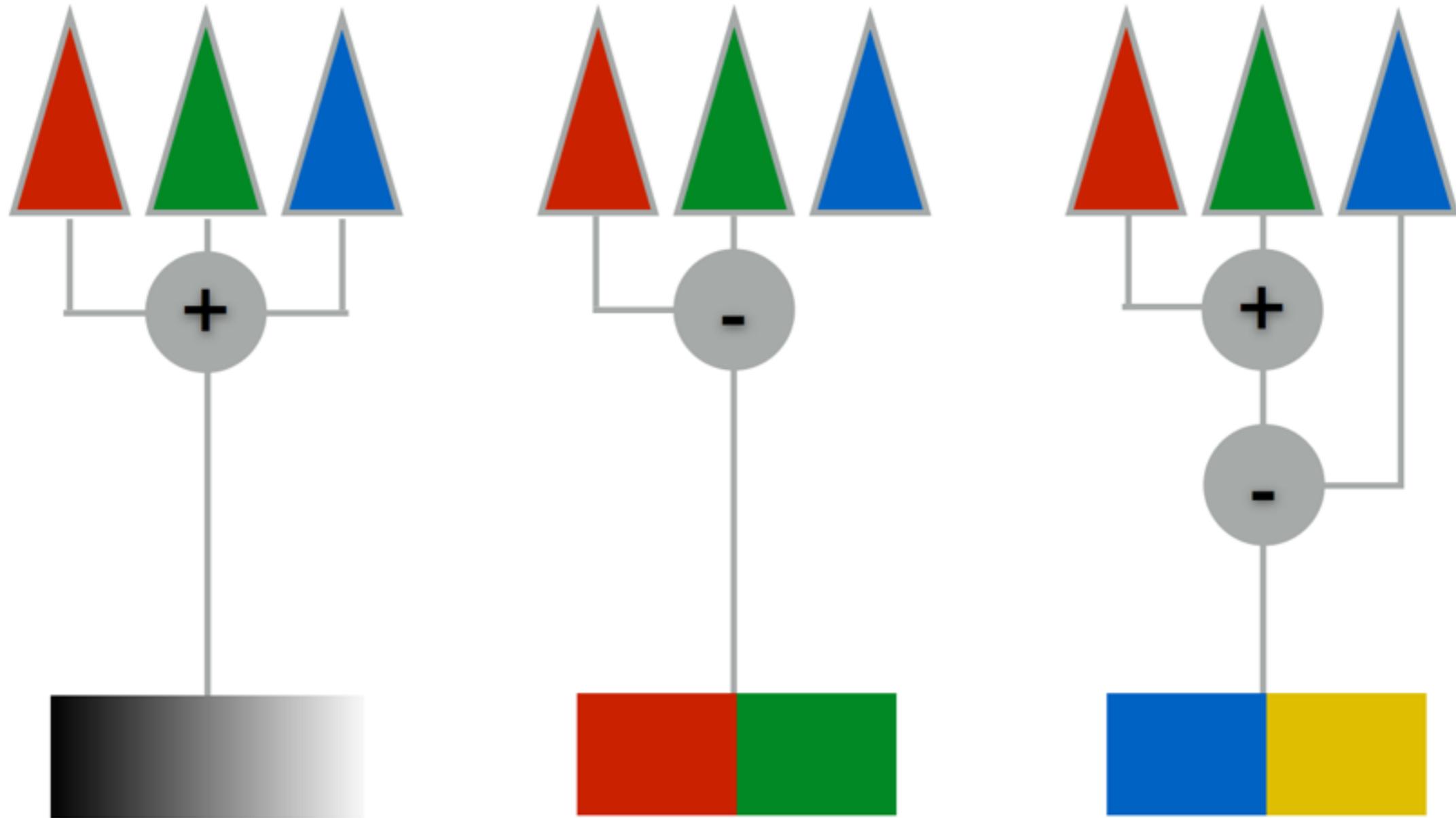
# Principles

# Color Vision

# How does your eye work?

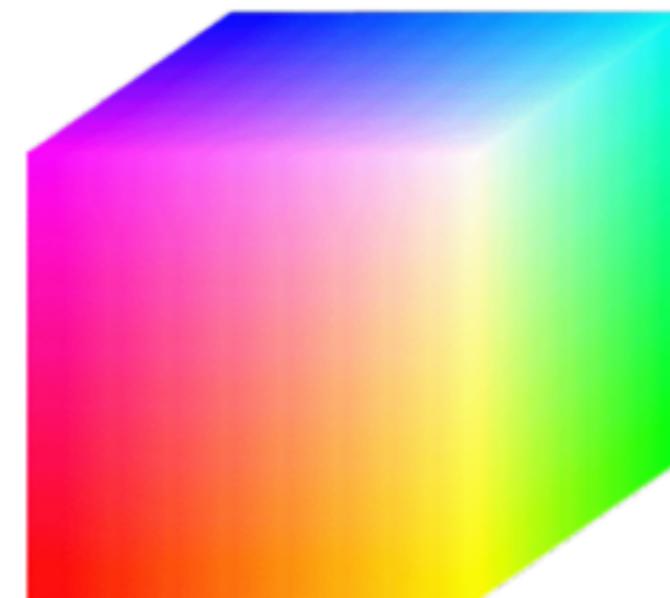
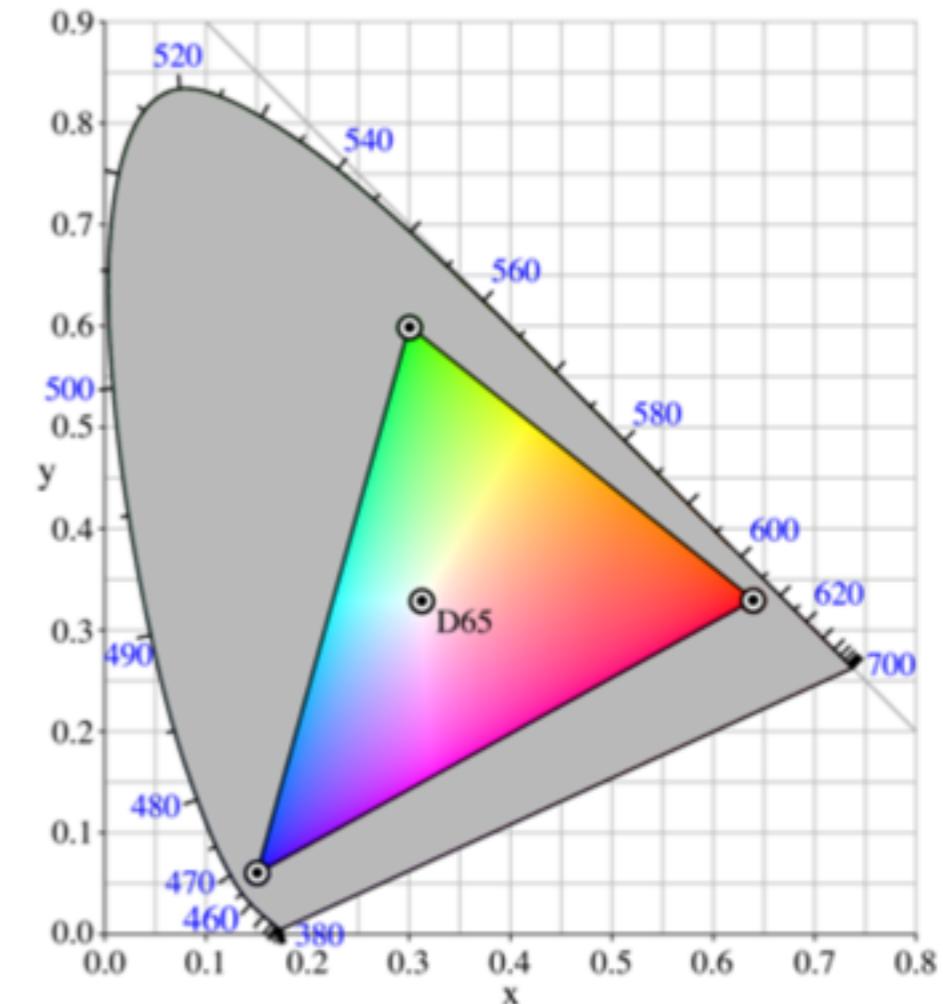
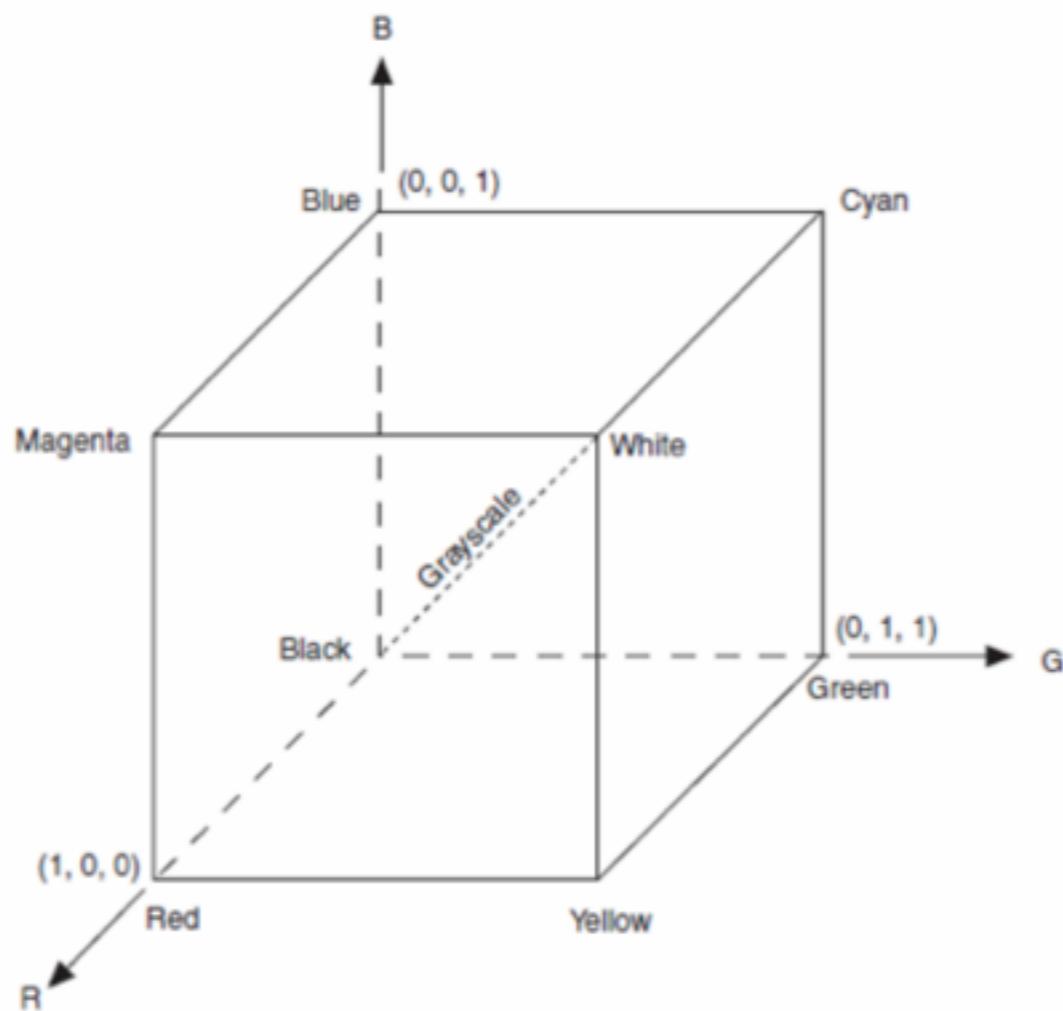


# OPPONENT PROCESS MODEL



# RGB

- Device-centric
- What programs want,  
**not** what humans want



D65: midday sun in Western Europe

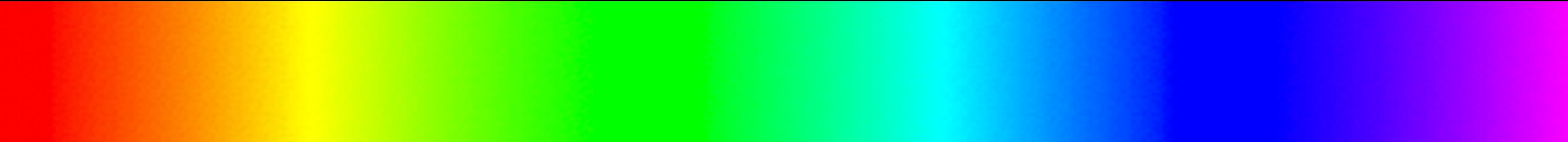
# Polar LUV (or HCL)

- “Perceptually uniform”, like LUV
- Transform UV to polar coordinates: radius is Chroma, Angle is Hue
- **Like HSV, but device-independent. All else being equal, think HCL first**

[http://cscheid.net/static/20120216/hcl\\_frame.html](http://cscheid.net/static/20120216/hcl_frame.html)

If you're going to use the rainbow colormap, use an **isoluminant** version, **quantize** it, or **both**

**Bad**



**Better**



Number of data classes: 3

[how to use](#) | [updates](#) | [downloads](#) | [credits](#)

Nature of your data:

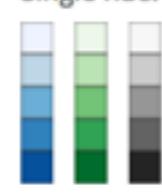
sequential  diverging  qualitative

Pick a color scheme:

Multi-hue:



Single hue:



**COLORBREWER 2.0**

color advice for cartography

Only show:

- colorblind safe
- print friendly
- photocopy safe

Context:

- roads
- cities
- borders

Background:

- solid color
- terrain

color transparency

3-class BuGn



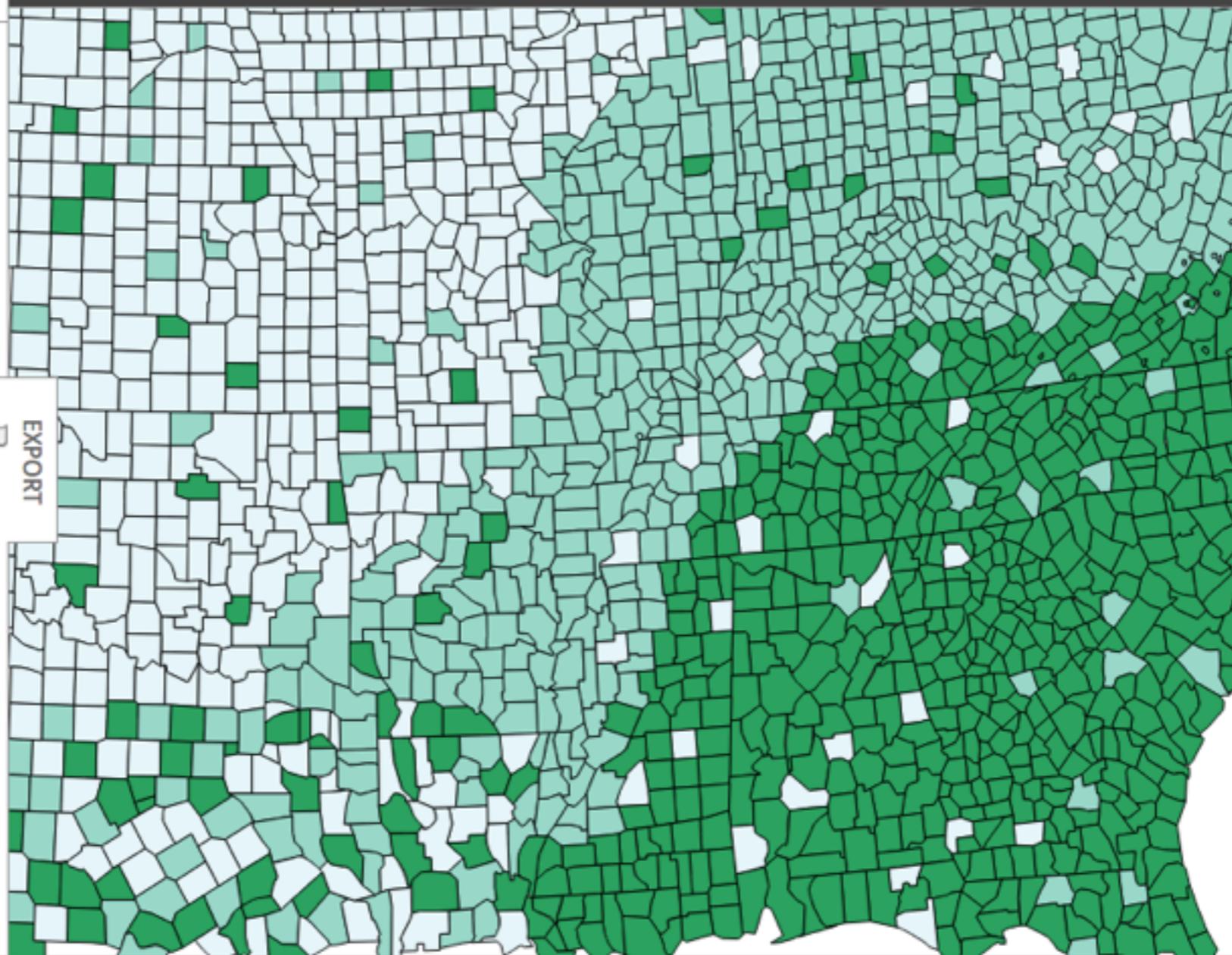
EXPORT

HEX

#e5f5f9

#99d8c9

#2ca25f



© Cynthia Brewer, Mark Harrower and The Pennsylvania State University

Support

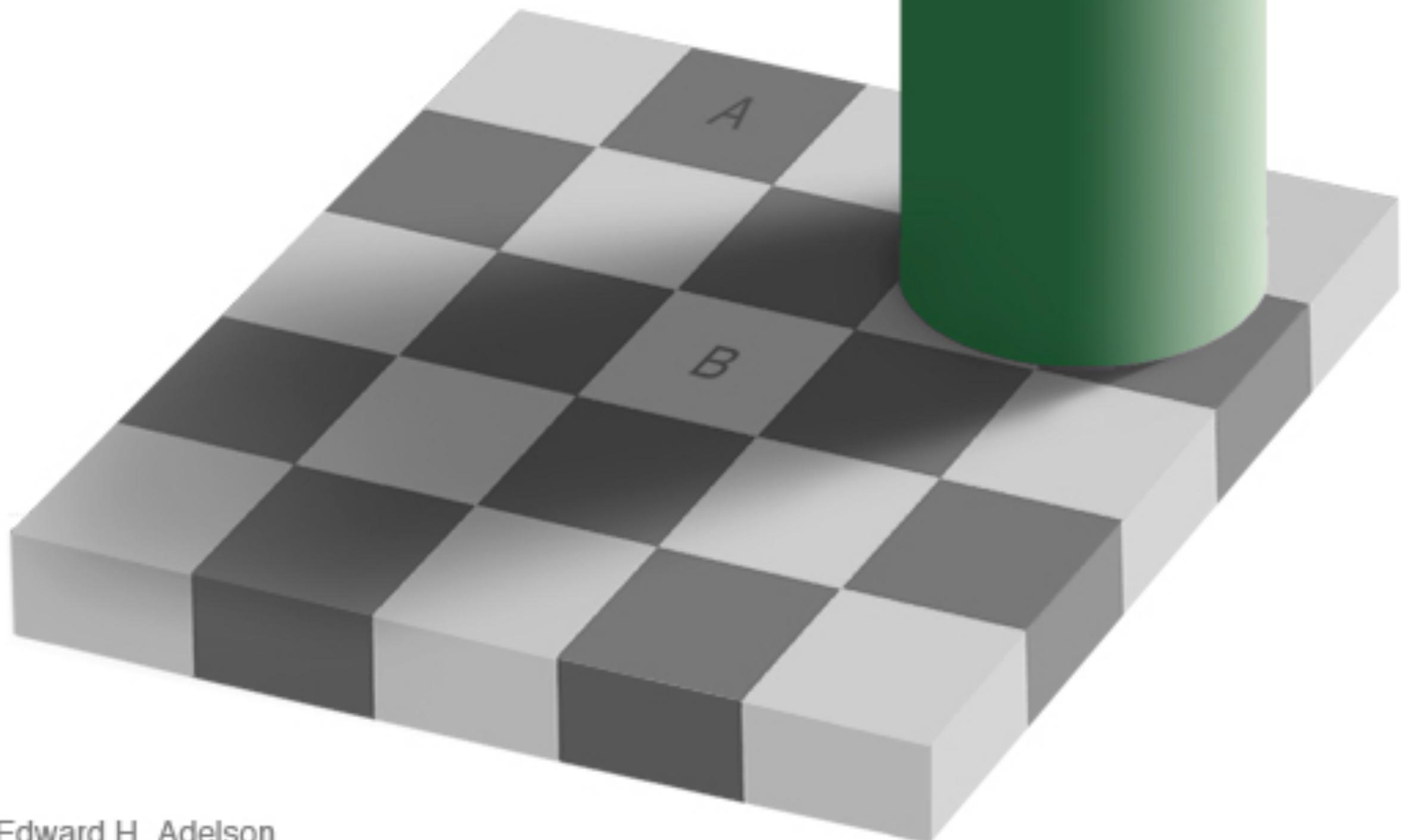
[Back to Flash version](#)

[Back to ColorBrewer 1.0](#)

 axismaps

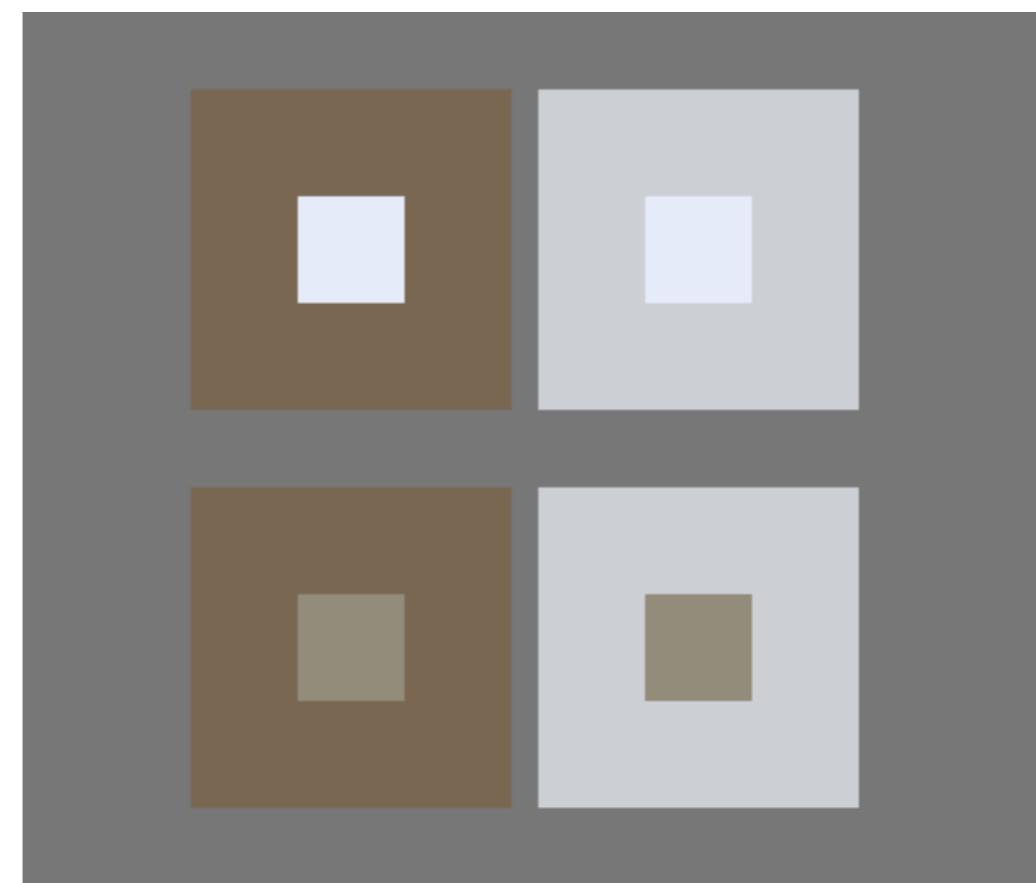
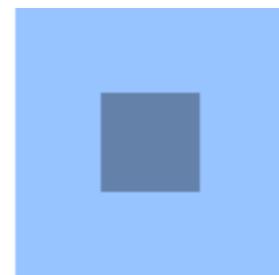
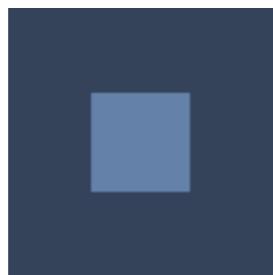
# COLORBREWER

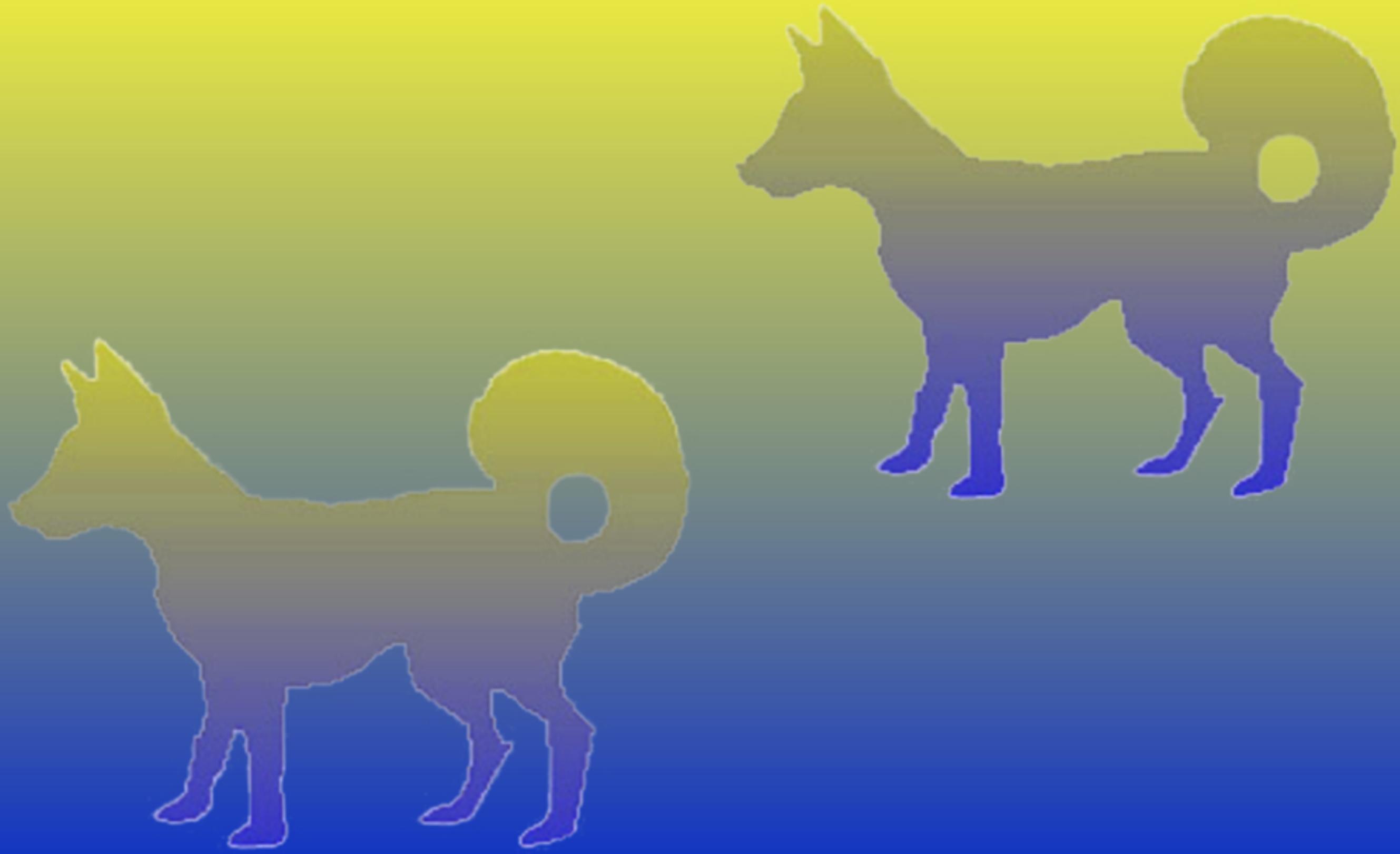
# SIMULTANEOUS CONTRAST



Edward H. Adelson

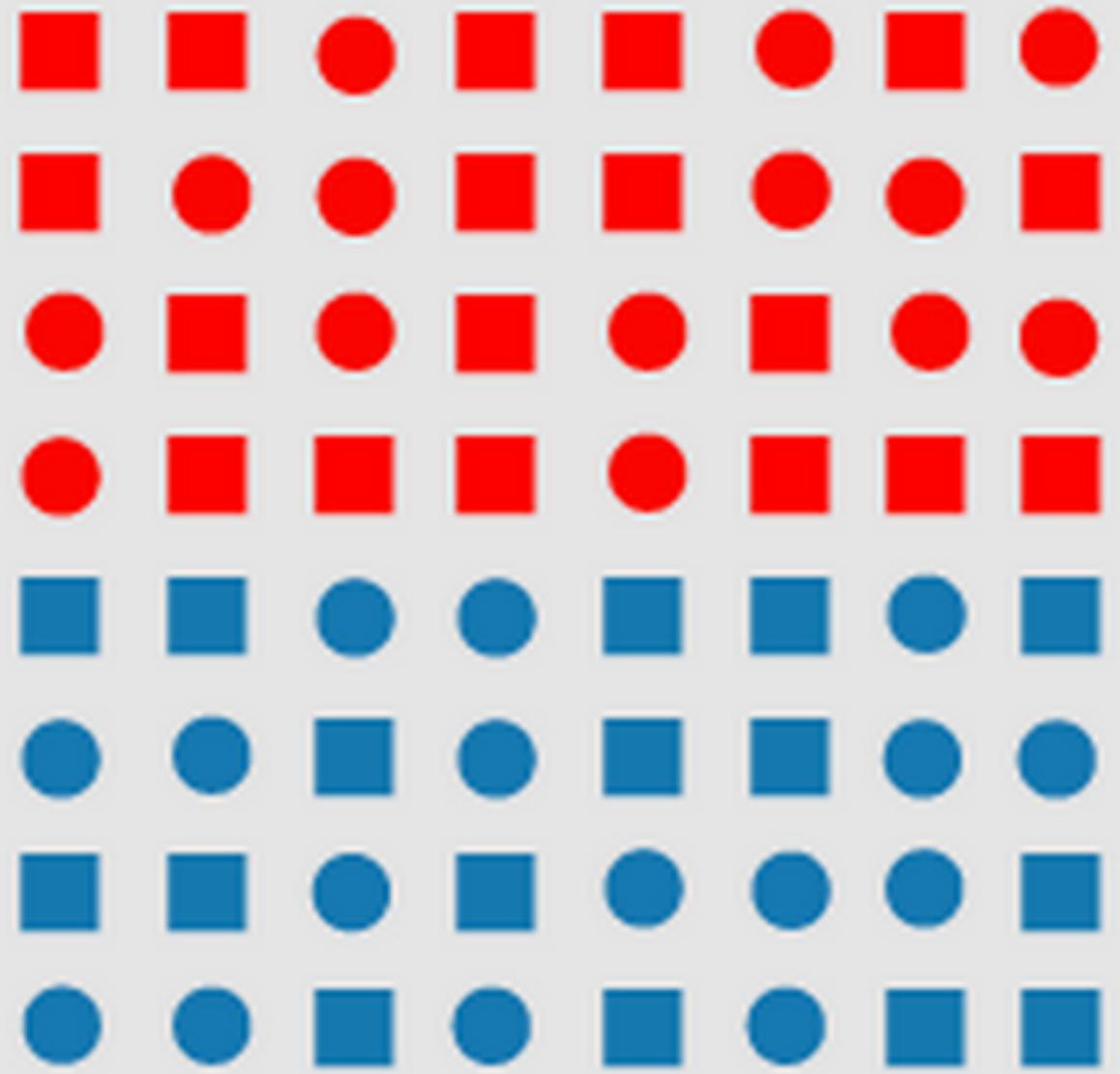
# SIMULTANEOUS CONTRAST



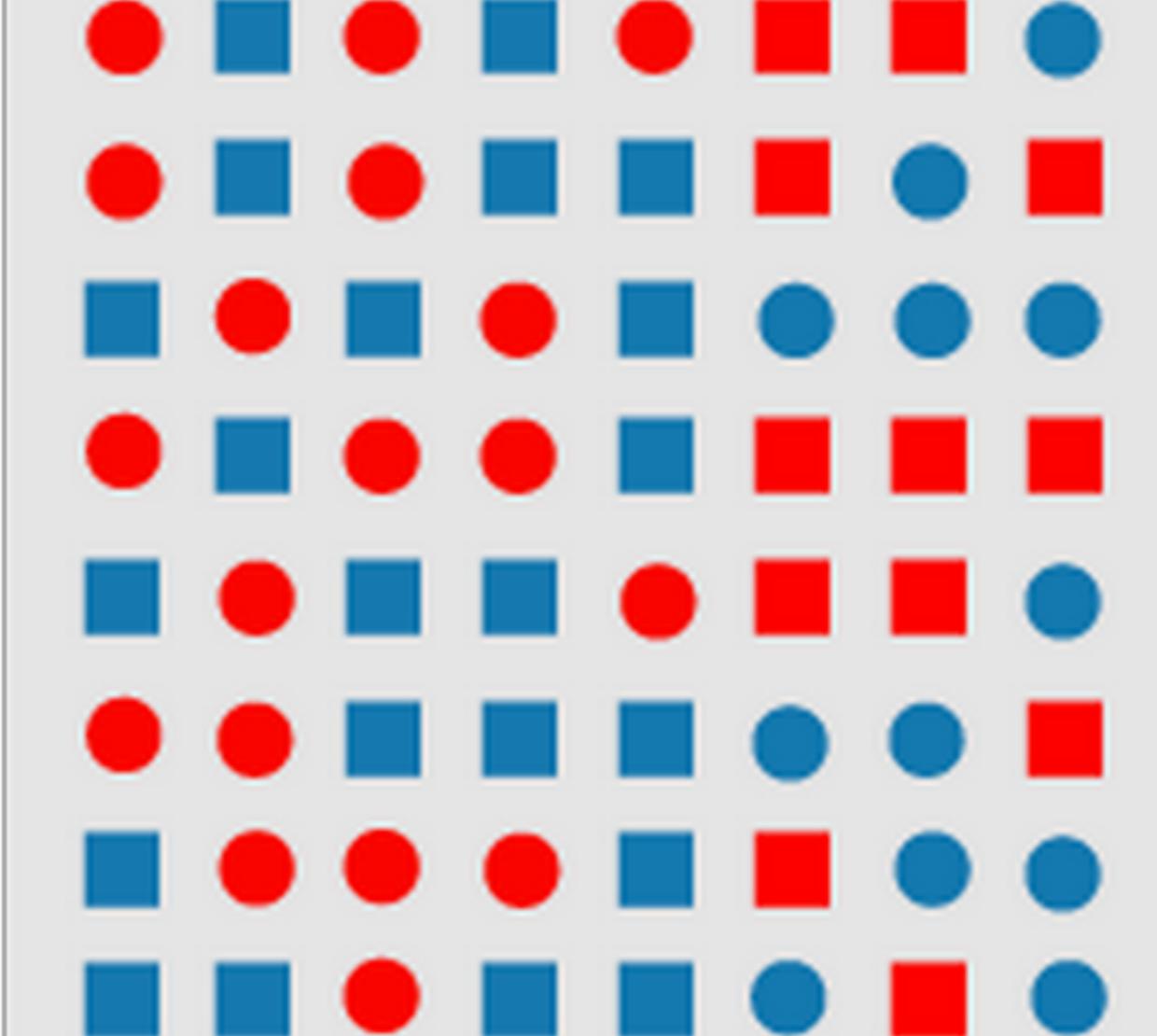




PREATTENTIVENESS,  
OR “VISUAL POP-OUT”

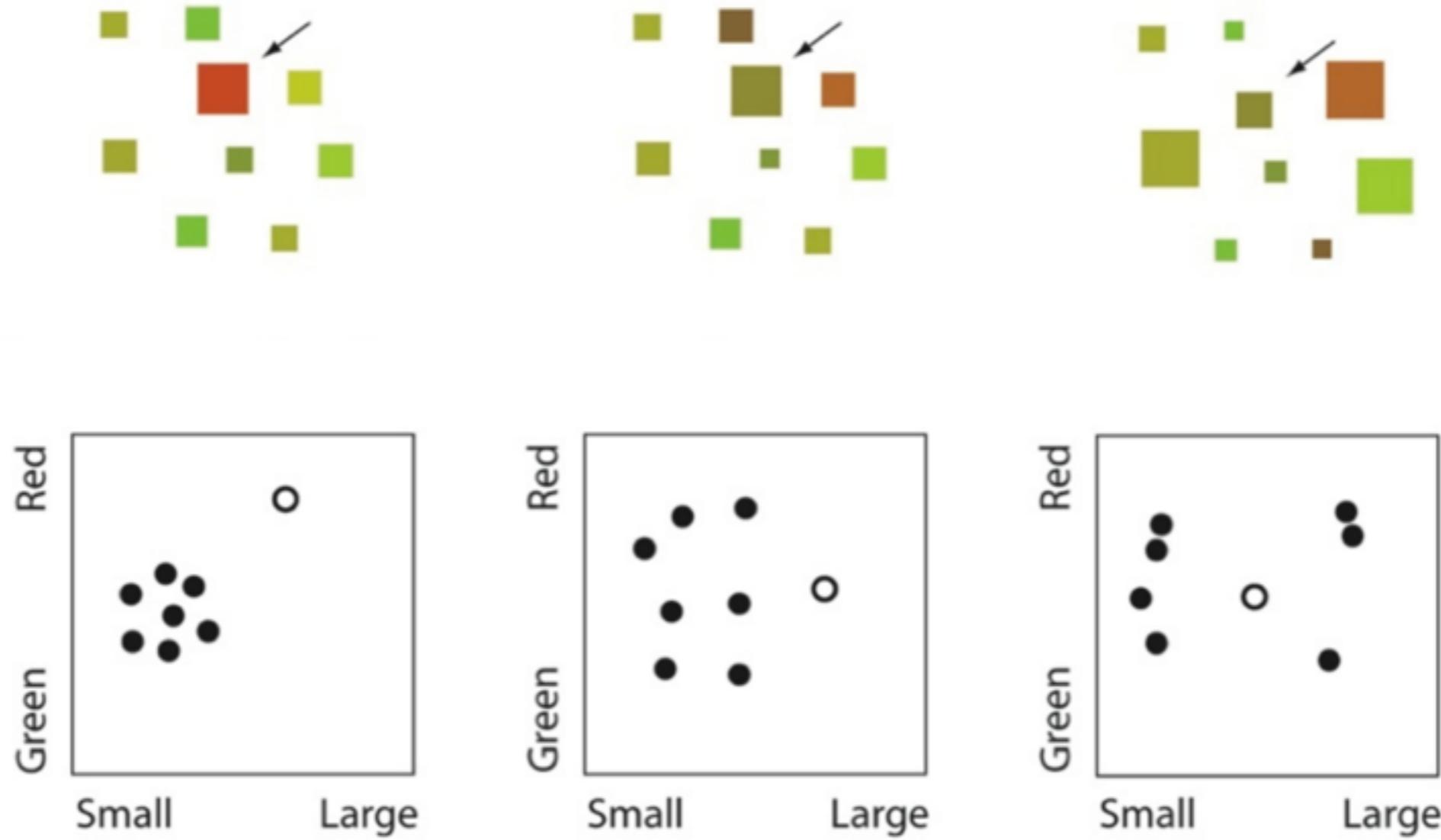


(a)



(b)

# Mixing is not always pre-attentive



Preattentiveness, only  
one-channel-at-a-  
time.

④ Position

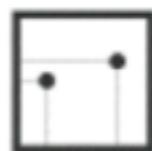
→ Horizontal



→ Vertical



→ Both



④ Color



④ Shape



④ Tilt



④ Size

→ Length



→ Area



→ Volume



# Cleveland/McGill perception papers

## Graphical Perception: Theory, Experimentation, and Application to the Development of Graphical Methods

WILLIAM S. CLEVELAND and ROBERT McGILL\*

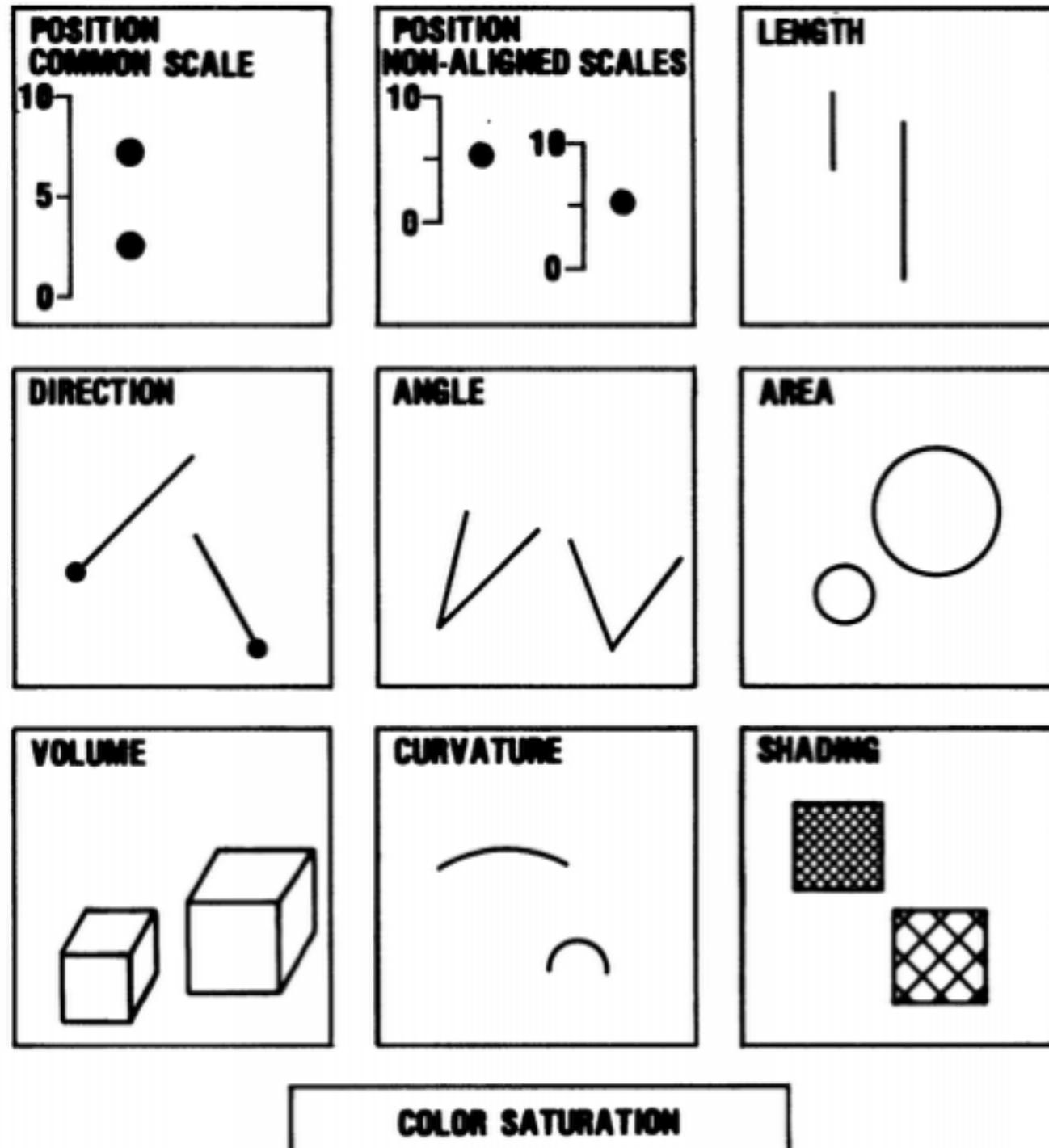
---

The subject of graphical methods for data analysis and for data presentation needs a scientific foundation. In this article we take a few steps in the direction of establishing such a foundation. Our approach is based on *graphical perception*—the visual decoding of information encoded on graphs—and it includes both theory and experimentation to test the theory. The theory deals with a small but important piece of the whole process of graphical perception. The first part is an identification of a set of *elementary perceptual tasks* that are carried out when people extract quantitative information from graphs. The second part is an ordering of the tasks on the basis of how accurately people perform them. Elements of the theory are tested by experimentation in which subjects record their judgments of the quantitative information on graphs. The experiments validate these elements but also suggest that the set of elementary tasks should be expanded. The theory provides a guideline for graph construction: Graphs should employ elementary tasks as high in the ordering as possible. This principle is applied to a variety of graphs, including bar charts, divided bar charts,

largely unscientific. This is why Cox (1978) argued, “There is a major need for a theory of graphical methods” (p. 5), and why Kruskal (1975) stated “in choosing, constructing, and comparing graphical methods we have little to go on but intuition, rule of thumb, and a kind of master-to-apprentice passing along of information. . . . there is neither theory nor systematic body of experiment as a guide” (p. 28–29).

There is, of course, much good common sense about how to make a graph. There are many treatises on graph construction (e.g., Schmid and Schmid 1979), bad practice has been uncovered (e.g., Tufte 1983), graphic designers certainly have shown us how to make a graph appealing to the eye (e.g., Marcus et al. 1980), statisticians have thought intensely about graphical methods for data analysis (e.g., Tukey 1977; Chambers et al. 1983), and cartographers have devoted great energy to the construction of statistical maps (Bertin 1973; Robinson, Sale, and Morrison 1978). The ANSI manual on time series charts (American National Standards Institute 1979) provides guidelines for making graphs, but the manual ad-

# Cleveland/McGill perception papers



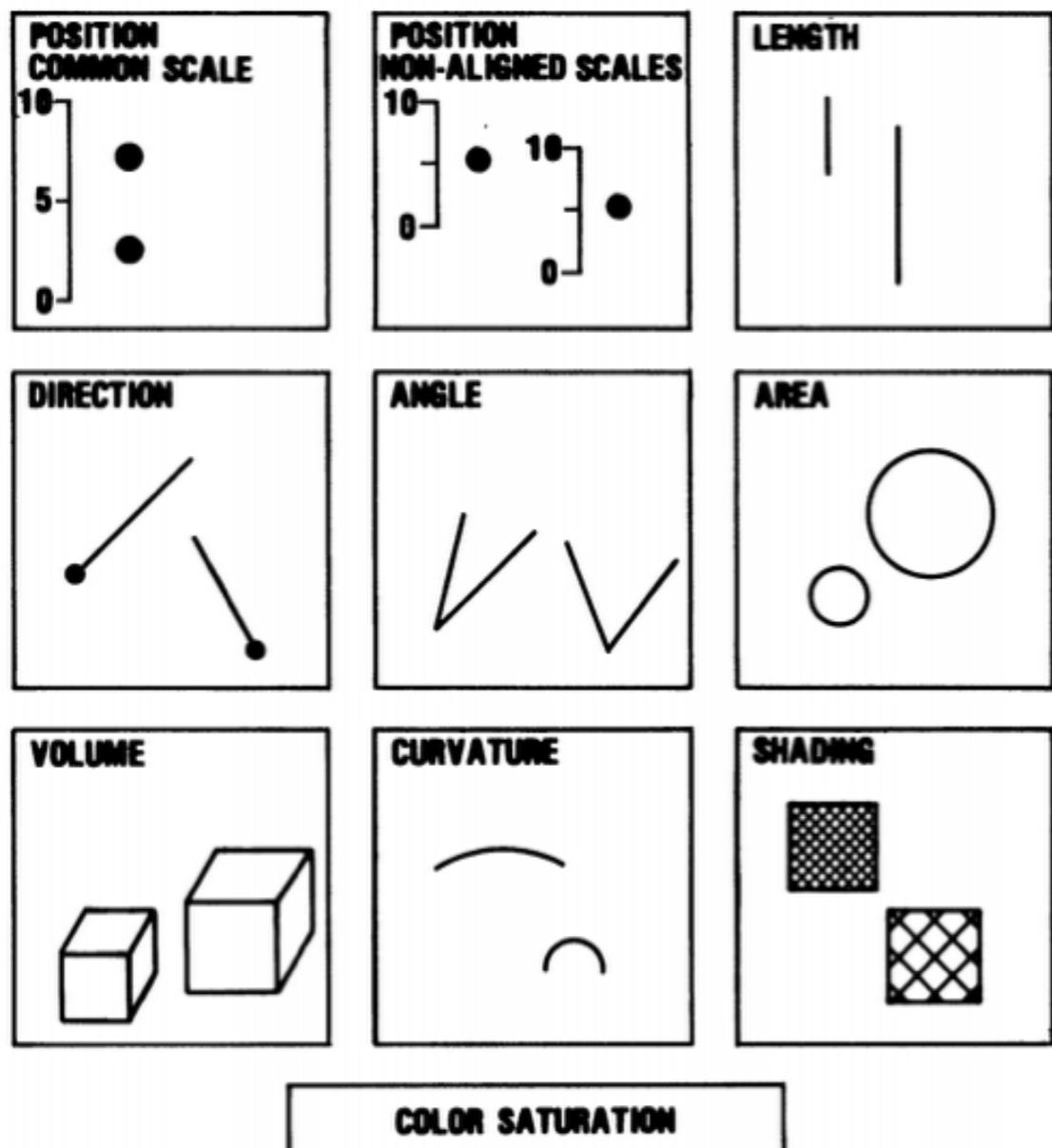
**Better to worse:**

1. Position along a common scale
2. Positions along nonaligned scales
3. Length, direction, angle
4. Area
5. Volume, curvature
6. Shading, color saturation

*Figure 1. Elementary perceptual tasks.*

Pie Chart Bad,  
Scatterplot Good

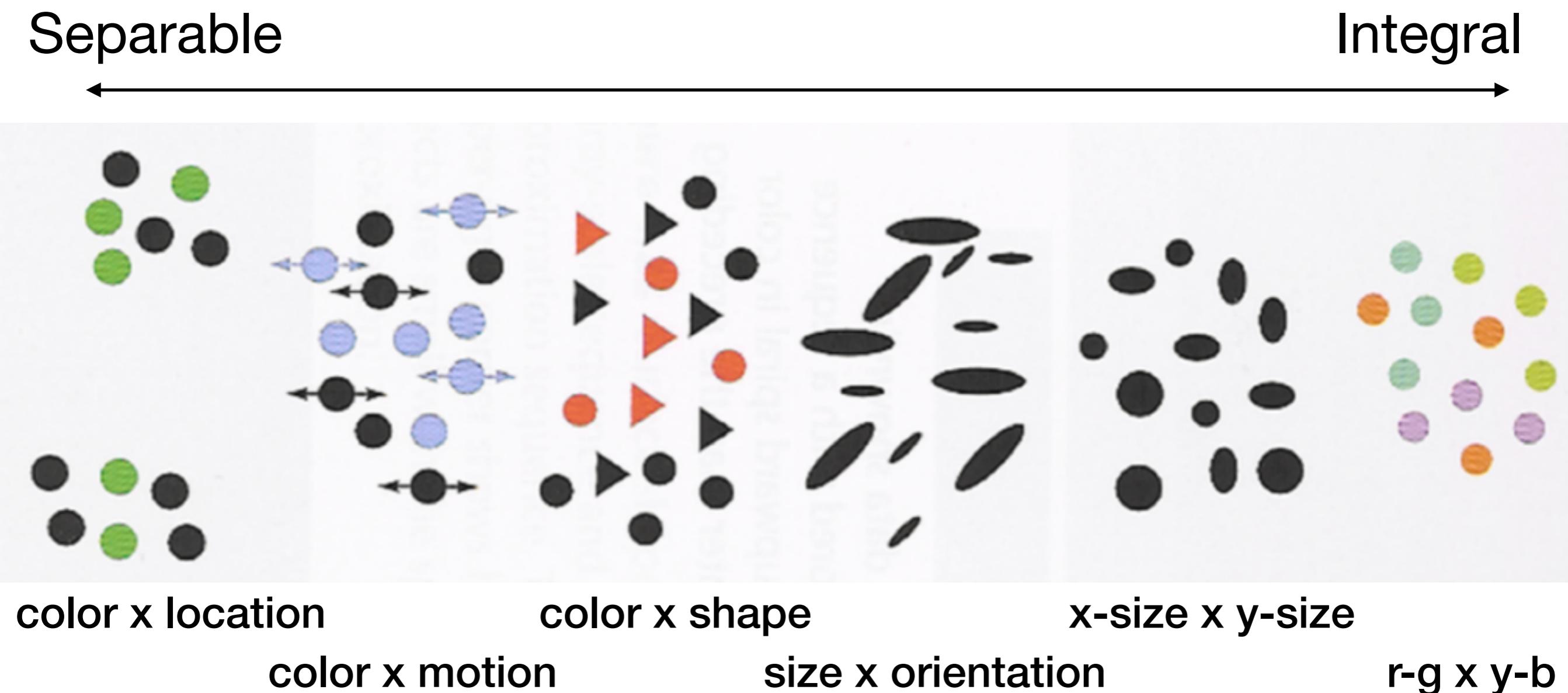
# Cleveland/McGill perception papers



*Figure 1. Elementary perceptual tasks.*

- Notice the “elementary perceptual tasks”
- What about higher-level tasks?

# Integral vs. Separable Channels



# READING, WRITING, AND EARNING MONEY

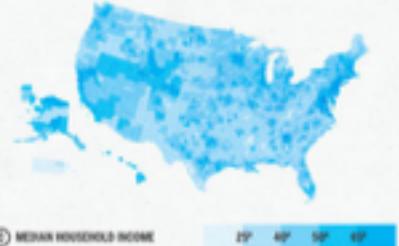
The latest data from the U.S. Census's American Community Survey paints a fascinating picture of the United States at the county level. We've looked at three educational achievement and the median income of the entire nation, to see where people are going to school, where they're earning money, and if there is any correlation.



① HIGH SCHOOL GRADUATES 65% 75% 82% 85%



② COLLEGE GRADUATES 15% 22% 30% 40%

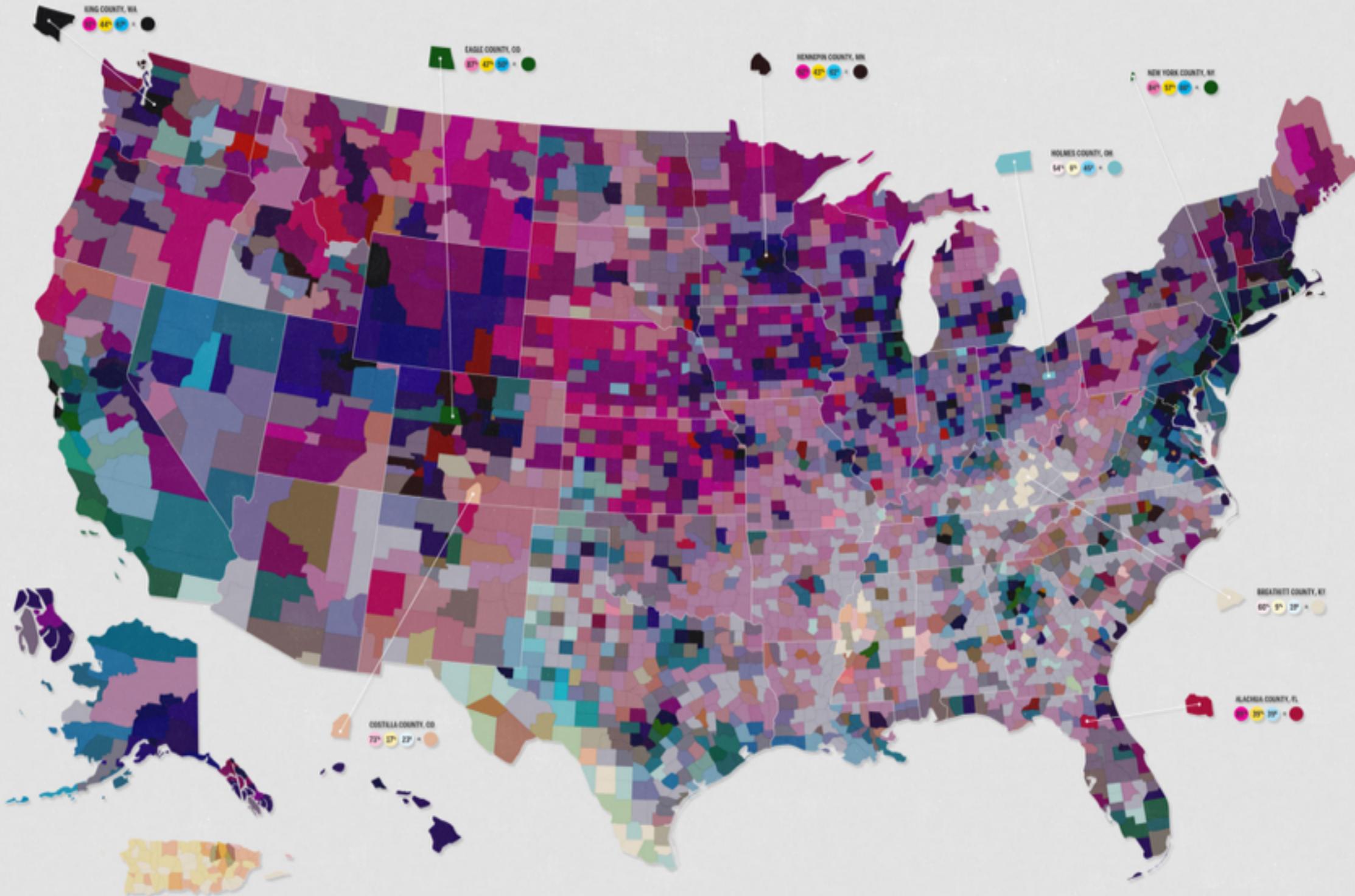


③ MEDIAN HOUSEHOLD INCOME 25k 40k 50k 60k

The map at right is a product of overlaying the three sets of data. The variation in hue and value has been produced from the data shown above in general, darker counties represent a more educated, better paid population while lighter areas represent communities with fewer graduates and lower incomes.



A collaboration between GOOD and Gregory Hulakoff.  
SOURCE: US Census



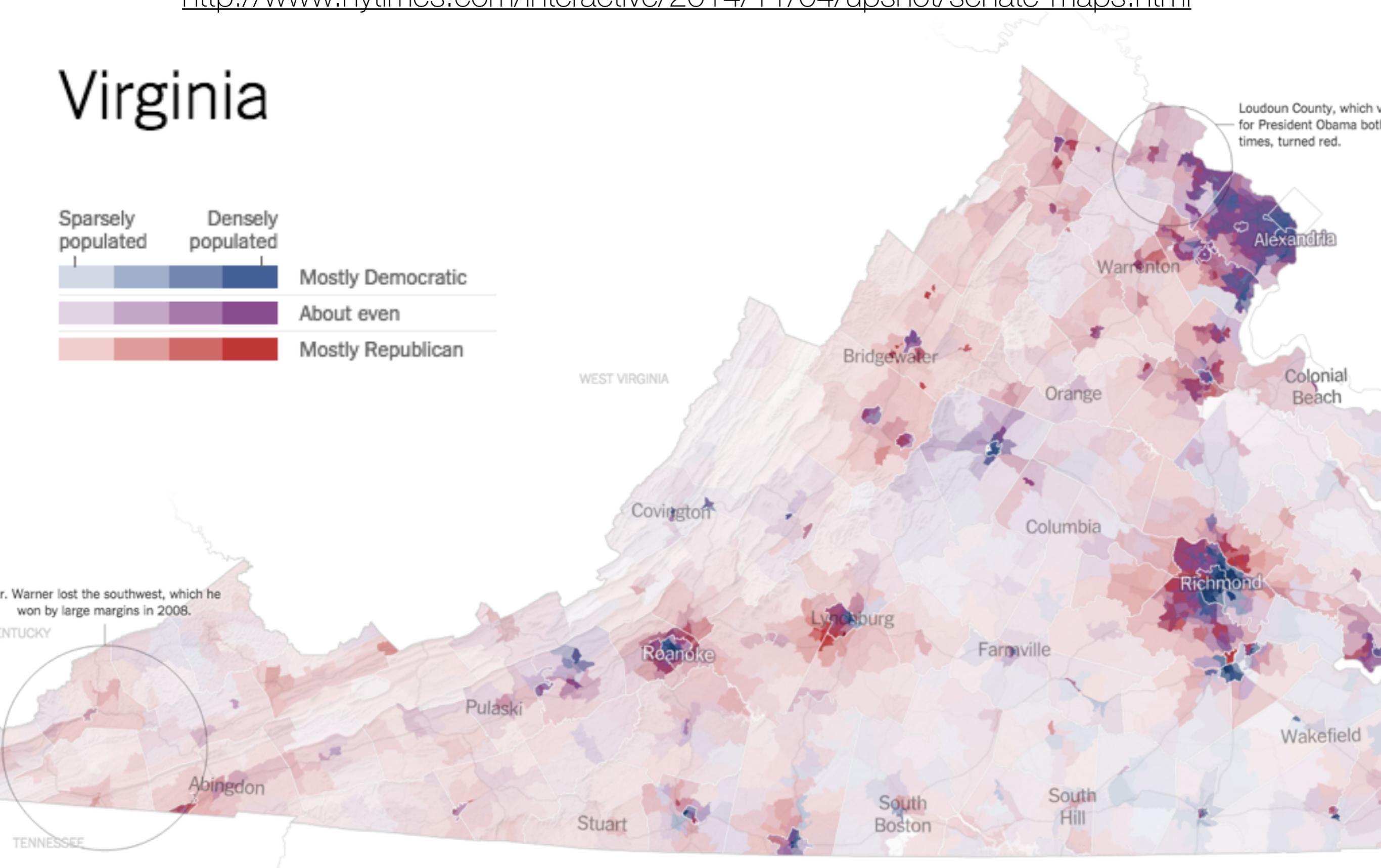
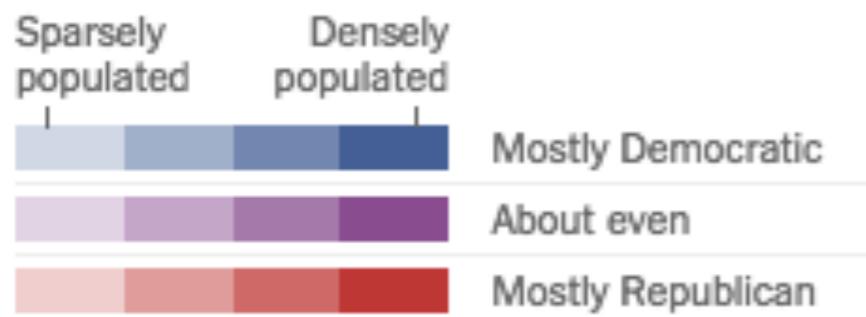
# Trivariate (!) Color Map (terrible, terrible idea)

<http://magazine.good.is/infographics/america-s-richest-counties-and-best-educated-counties#open>

# The best bivariate colormap I know

<http://www.nytimes.com/interactive/2014/11/04/upshot/senate-maps.html>

## Virginia

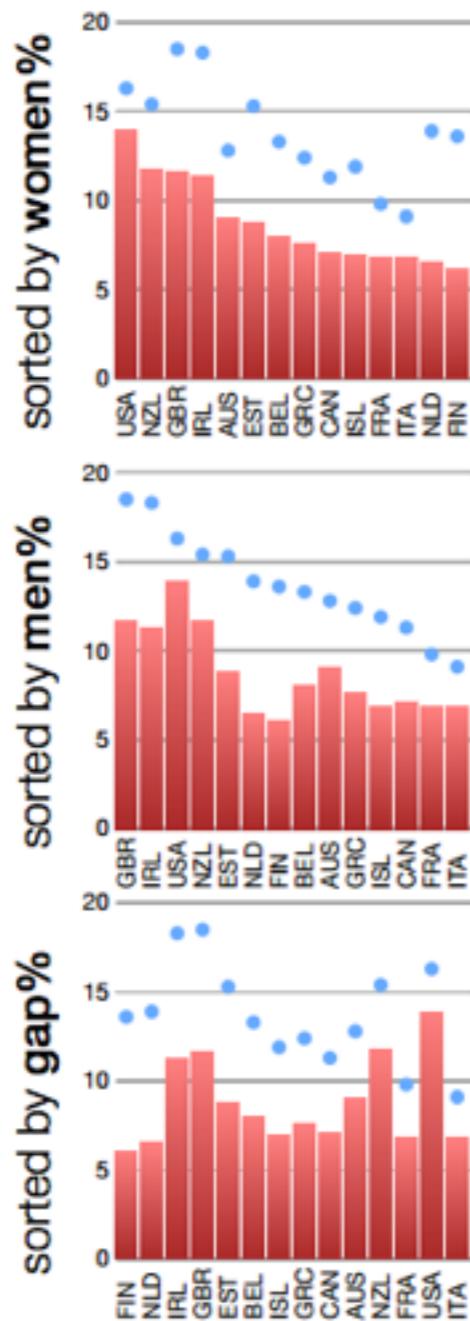


# Bivariate Color Maps are Possible, but Hard

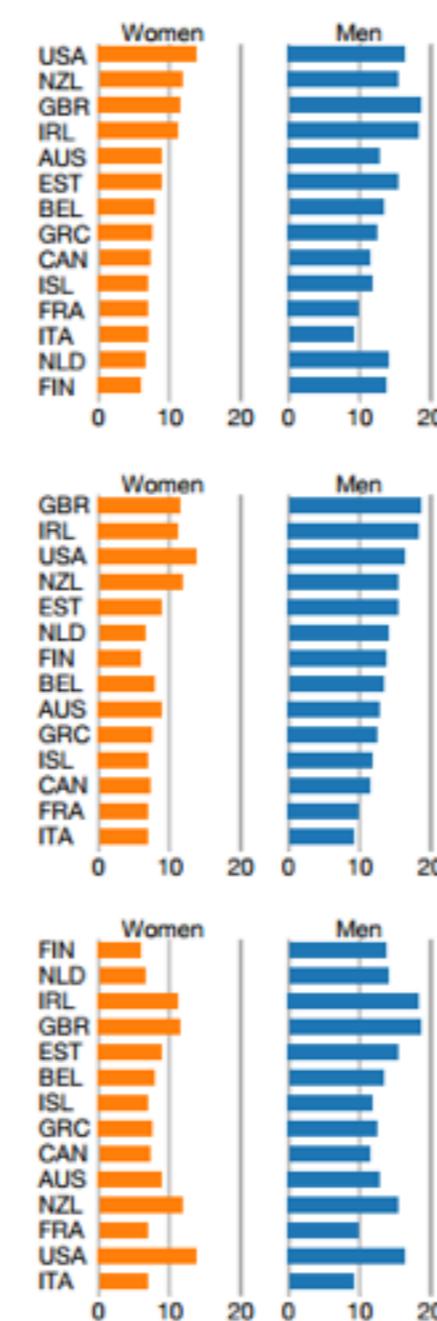
pay attention to the **behavior of the variables** you're mapping from, and the **behavior of the channels** you're mapping to.

# Algebraic Design Process

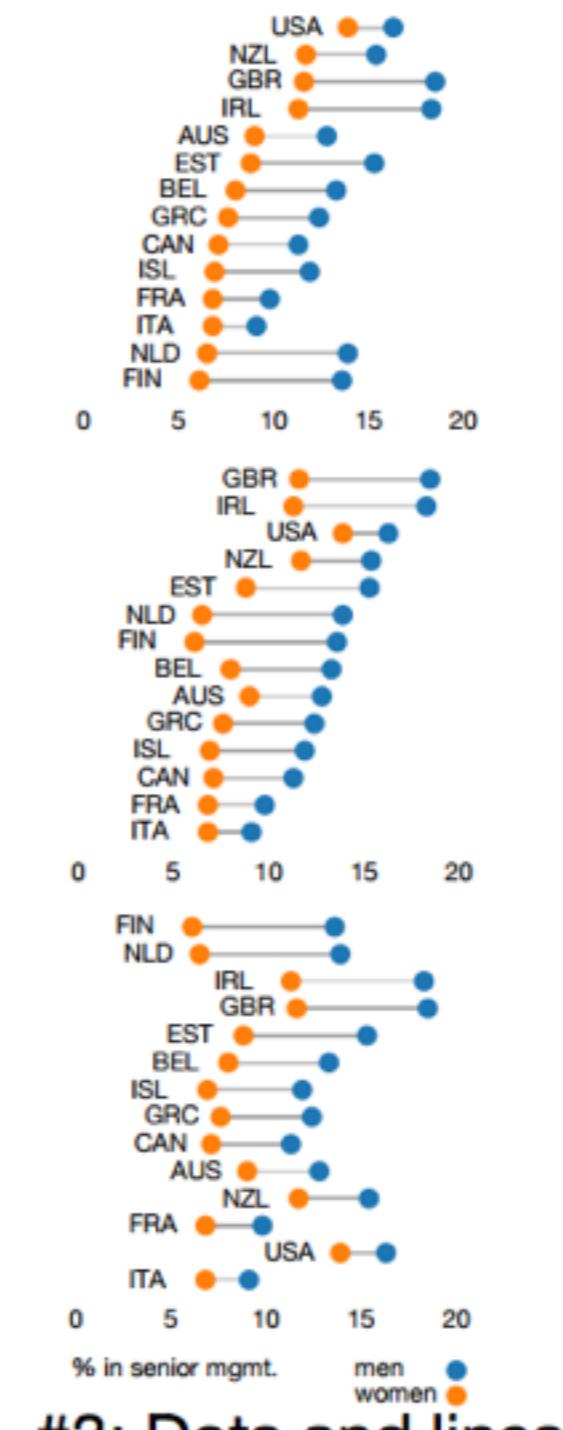
Invariance Principle failures:  
Different permutations  $\Rightarrow$  Different Impressions



#1: Bars and dots

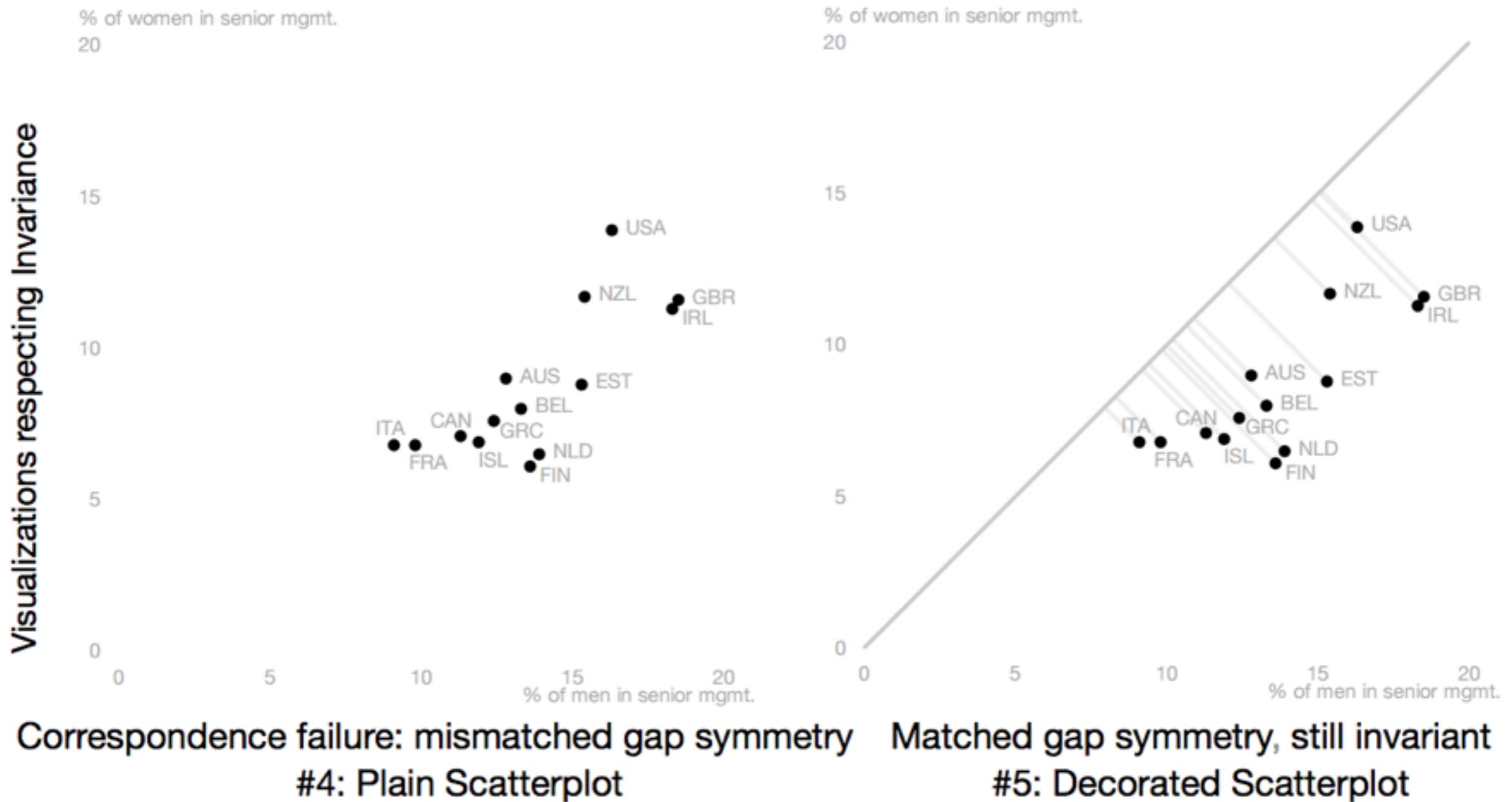


#2: Bars



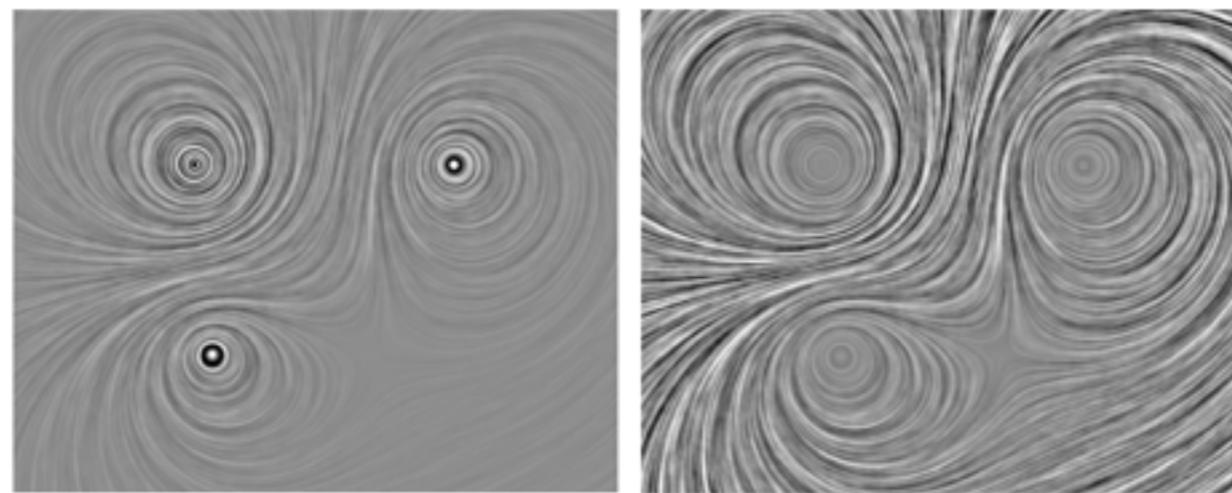
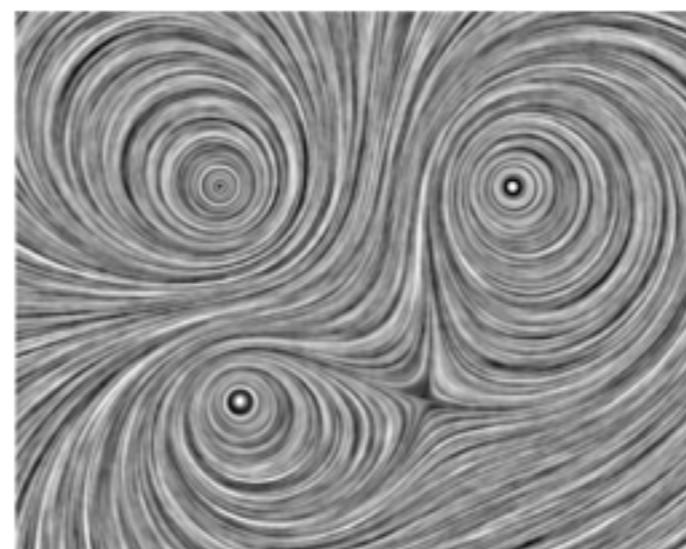
#3: Dots and lines

# Algebraic Design Process



# Algebraic Design Process

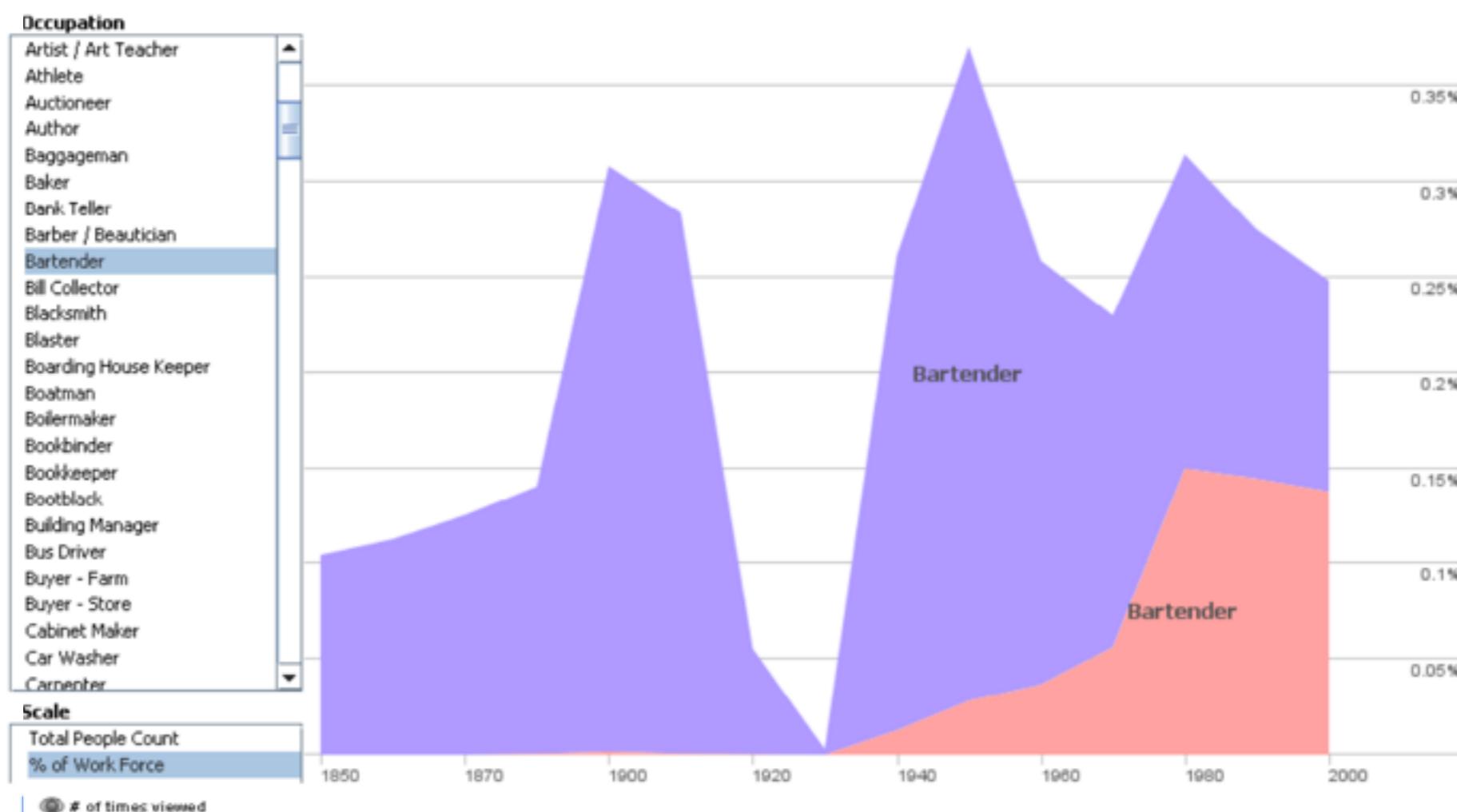
Same streamlines,  
**different flow velocities**



(c) LIC (with contrast modulation)

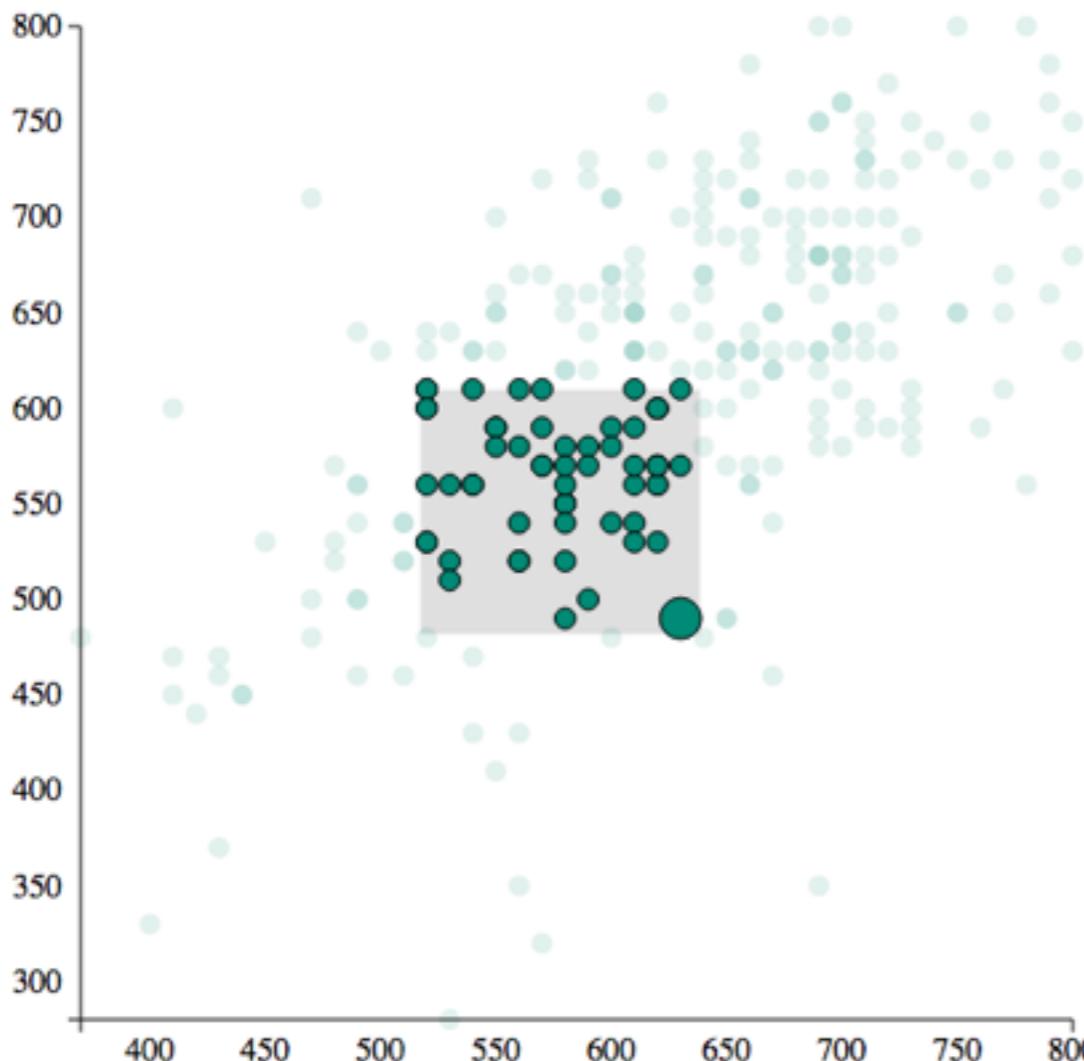
# Interaction

- Interpret the state of elements in the UI as a **clause** in a **query**. As UI changes, update data

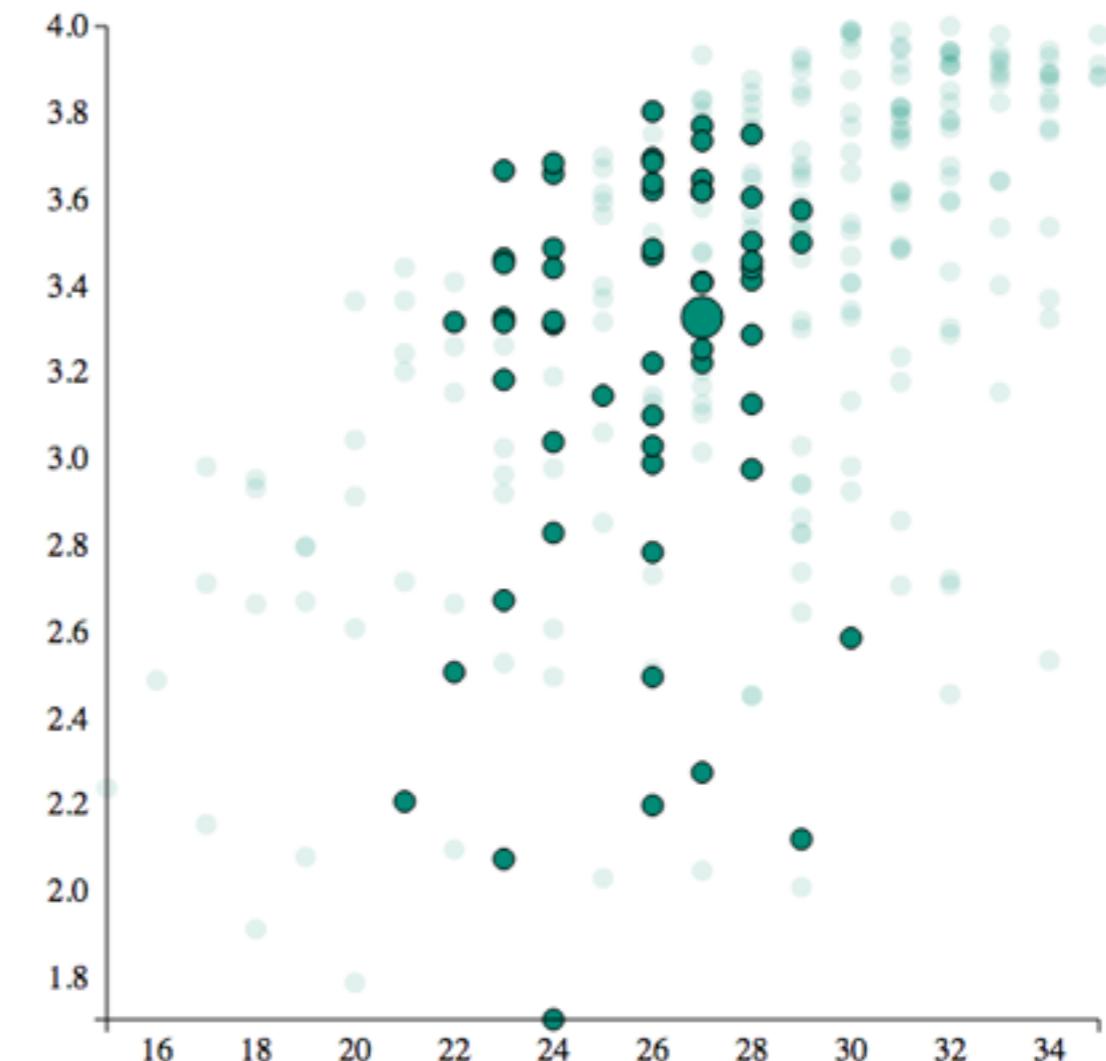


# Linked Brushing

**SATM x SATV**



**ACT x GPA**



# Shneiderman's “Visual information seeking mantra”

**Overview first,  
zoom and filter,  
then details-on-demand**

# Techniques

# Regular Scatterplots

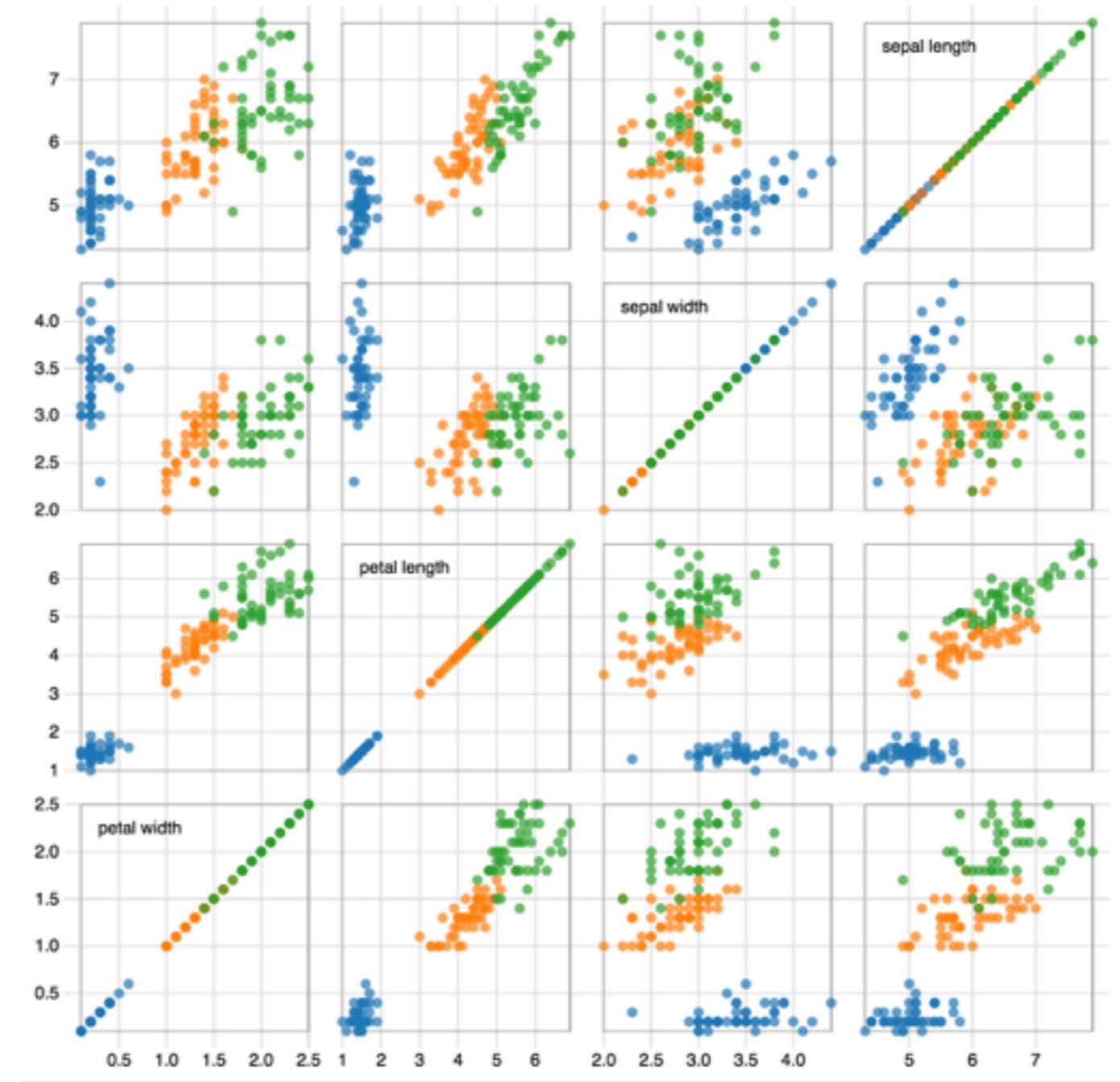
- Every data point is a vector:

$$\begin{bmatrix} v_0 \\ v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

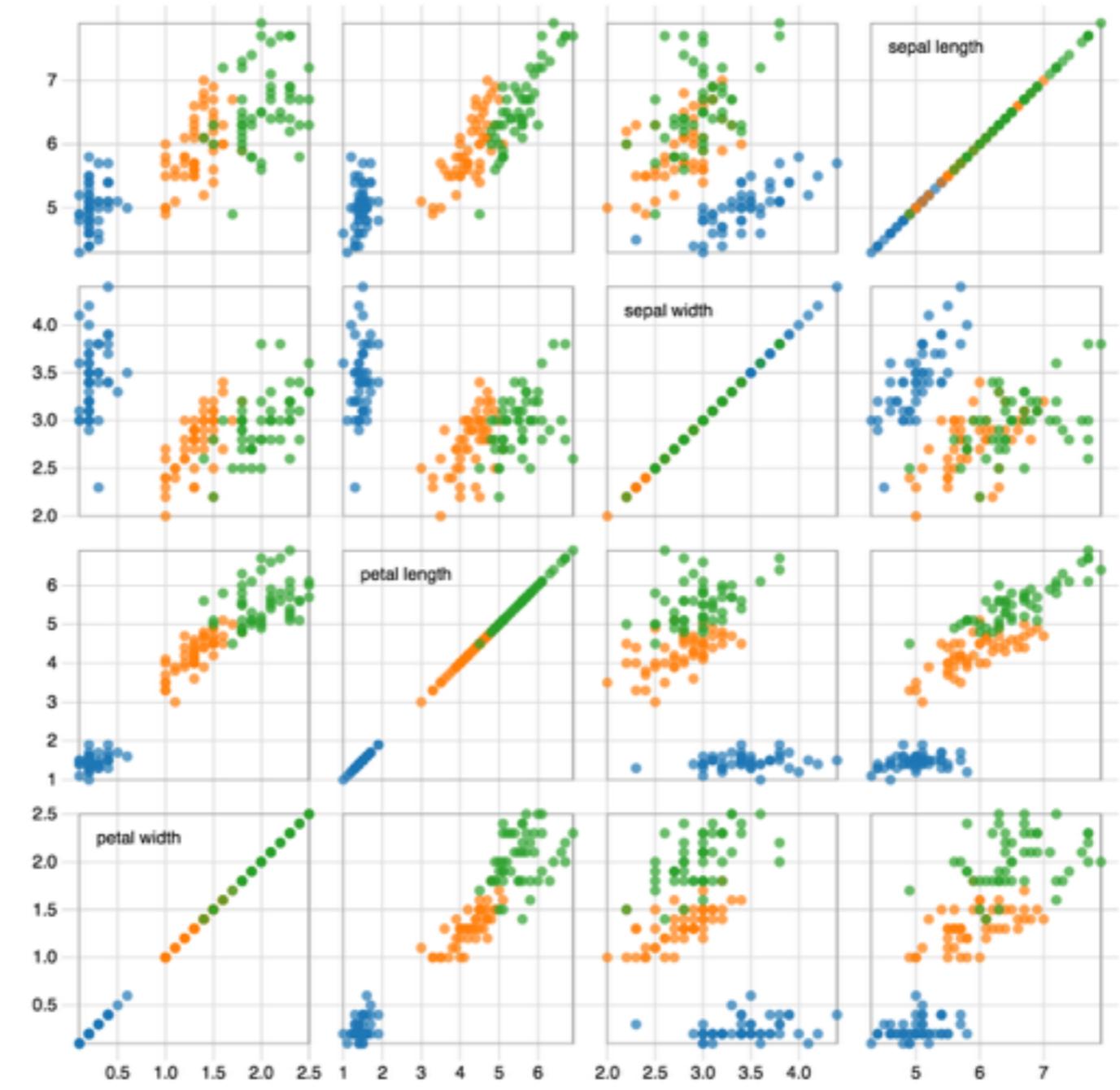
- Every scatterplot is produced by a very simple matrix:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

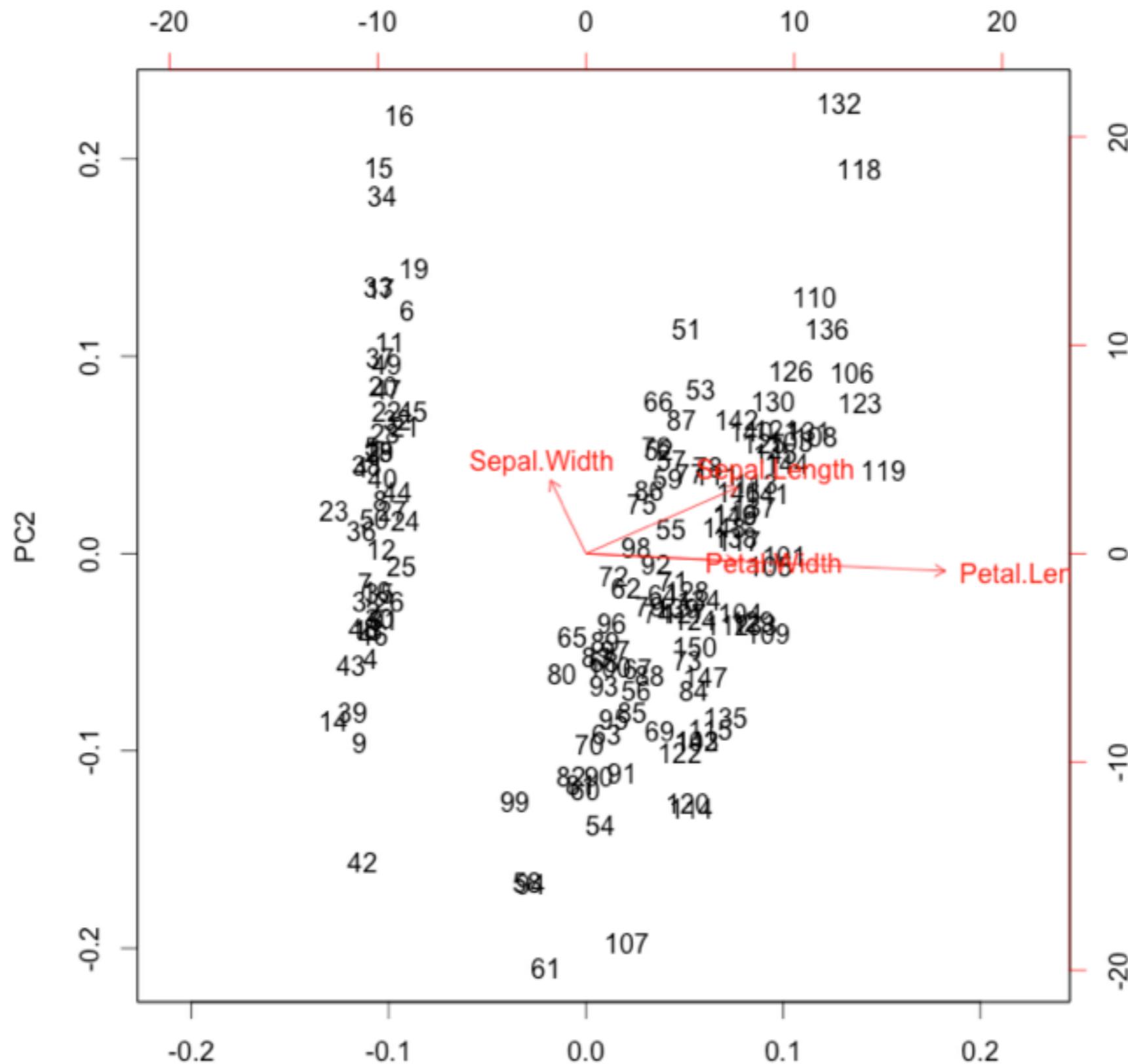


# What about other matrices?

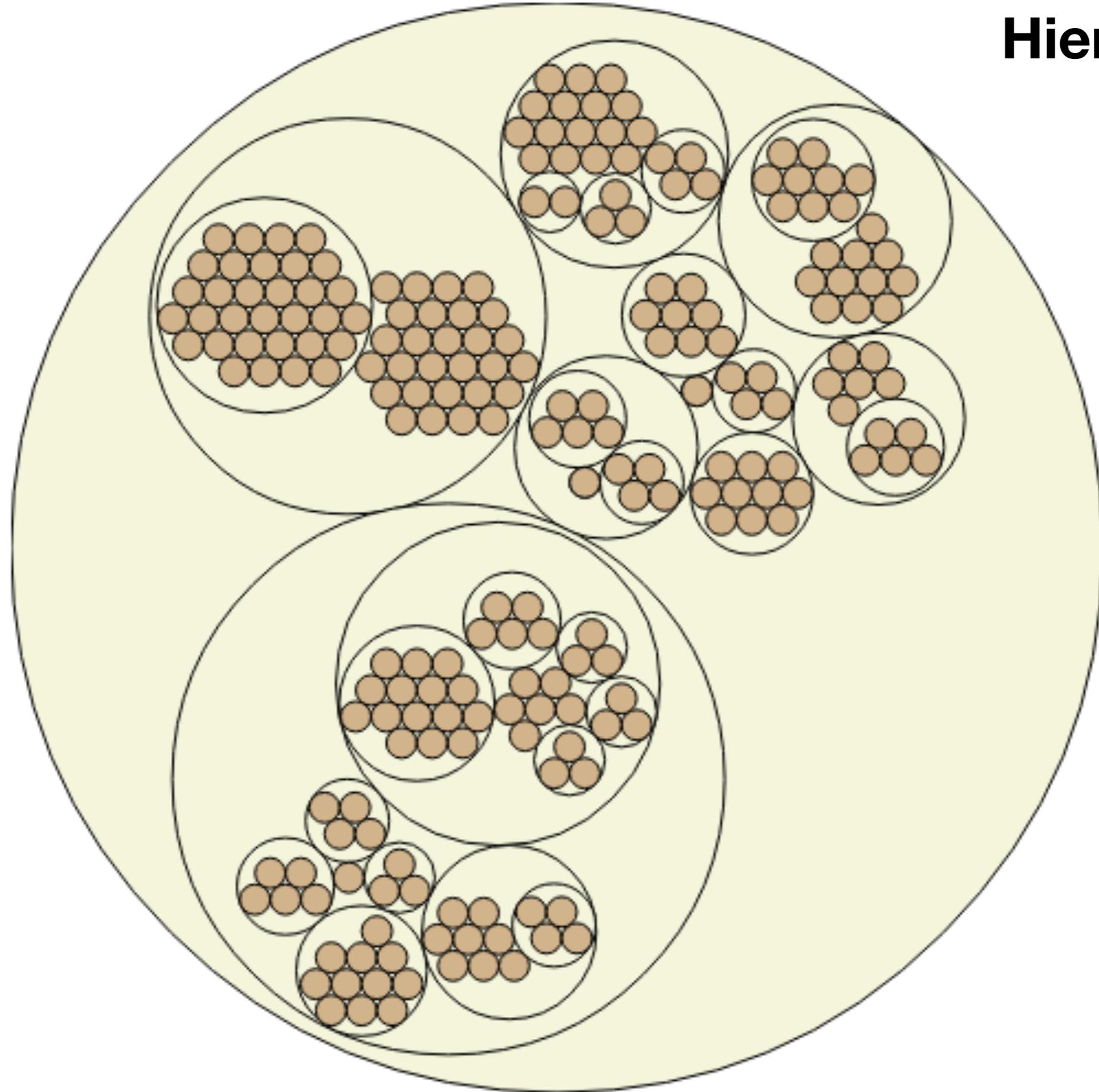


# Dimensionality Reduction

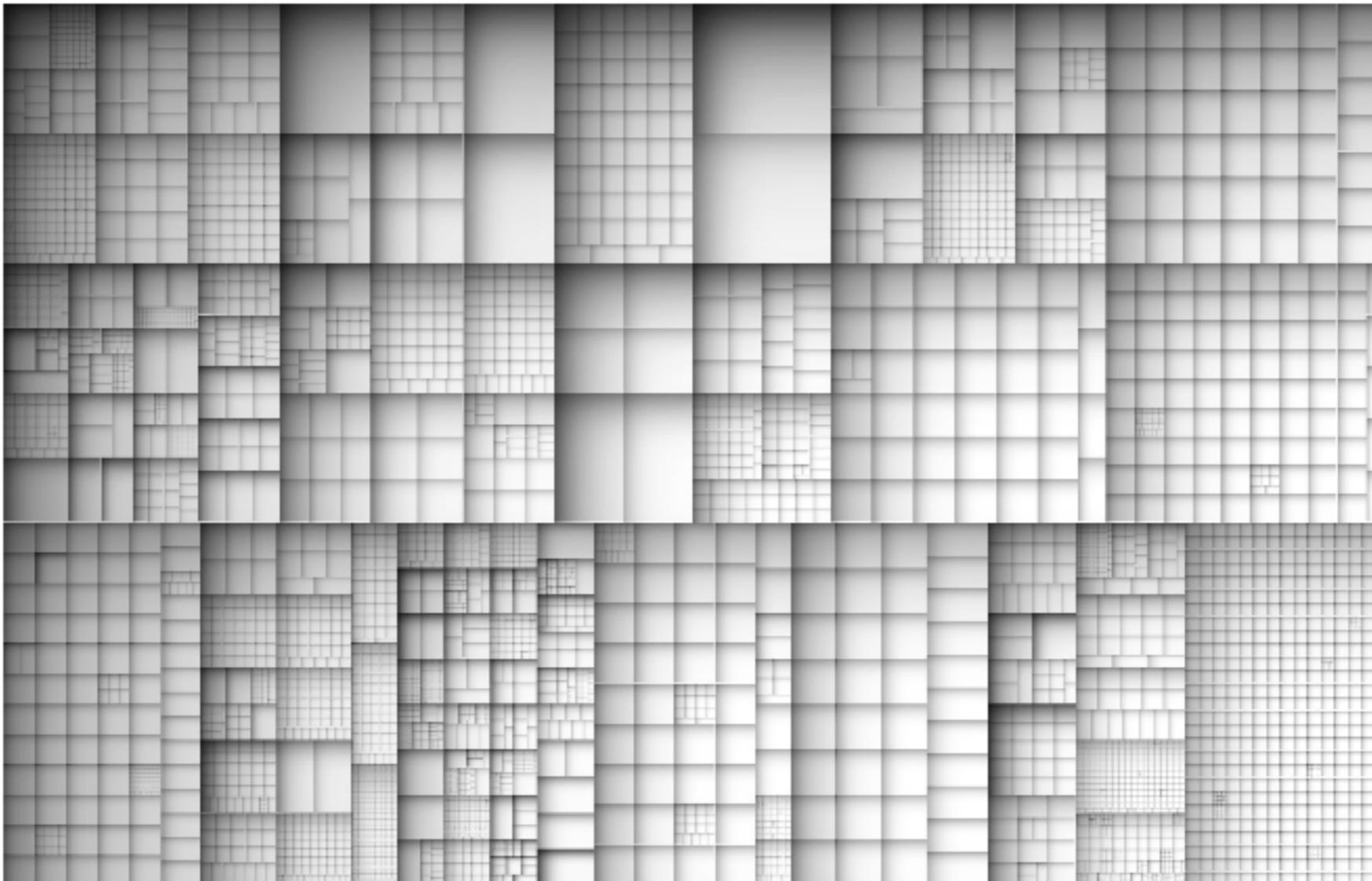
# Principal Component Analysis



# Hierarchies

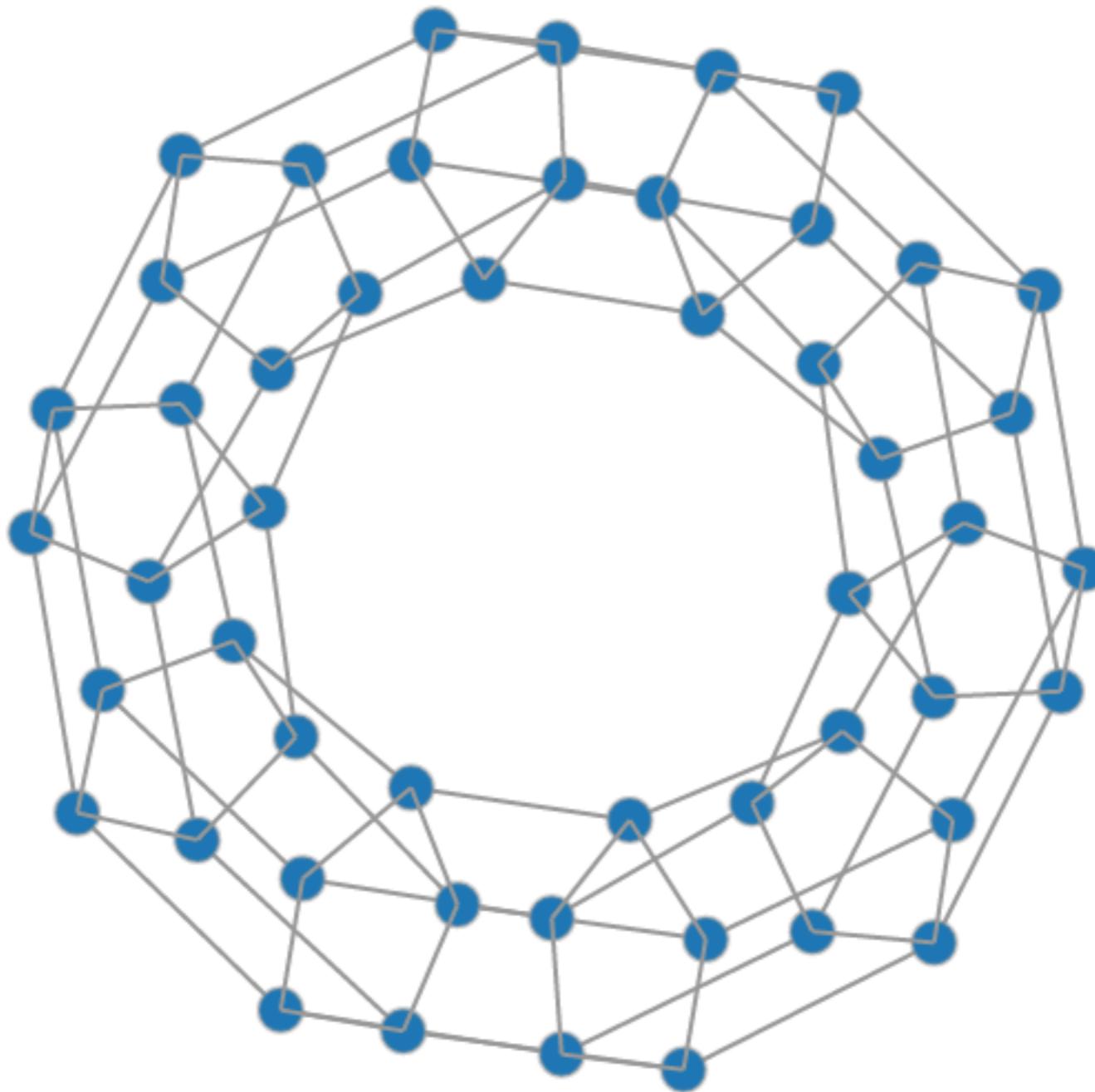


# Hierarchies



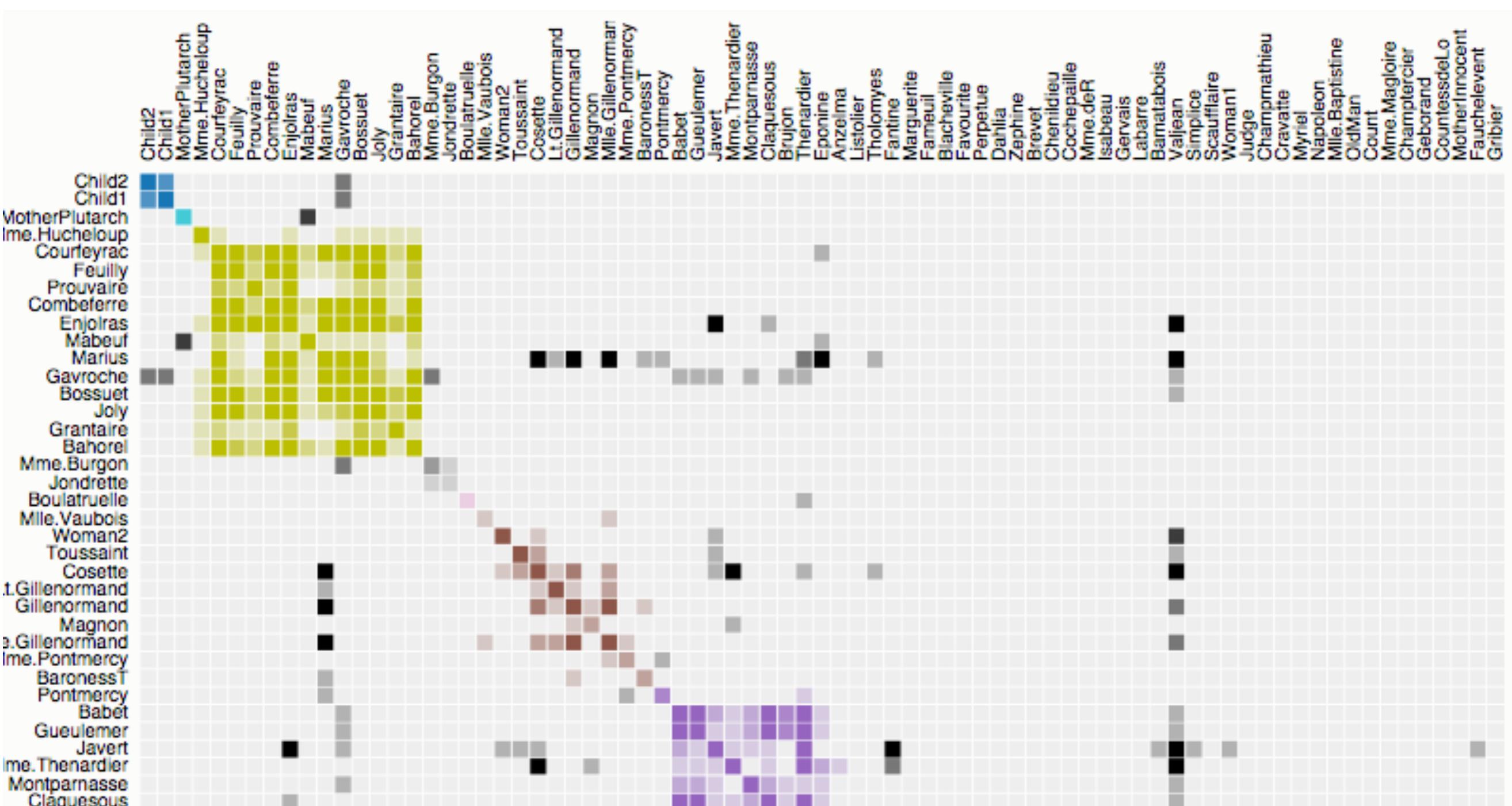
<http://www.cs.rug.nl/svcg/SoftVis/ViewFusion>

# Node-link diagrams

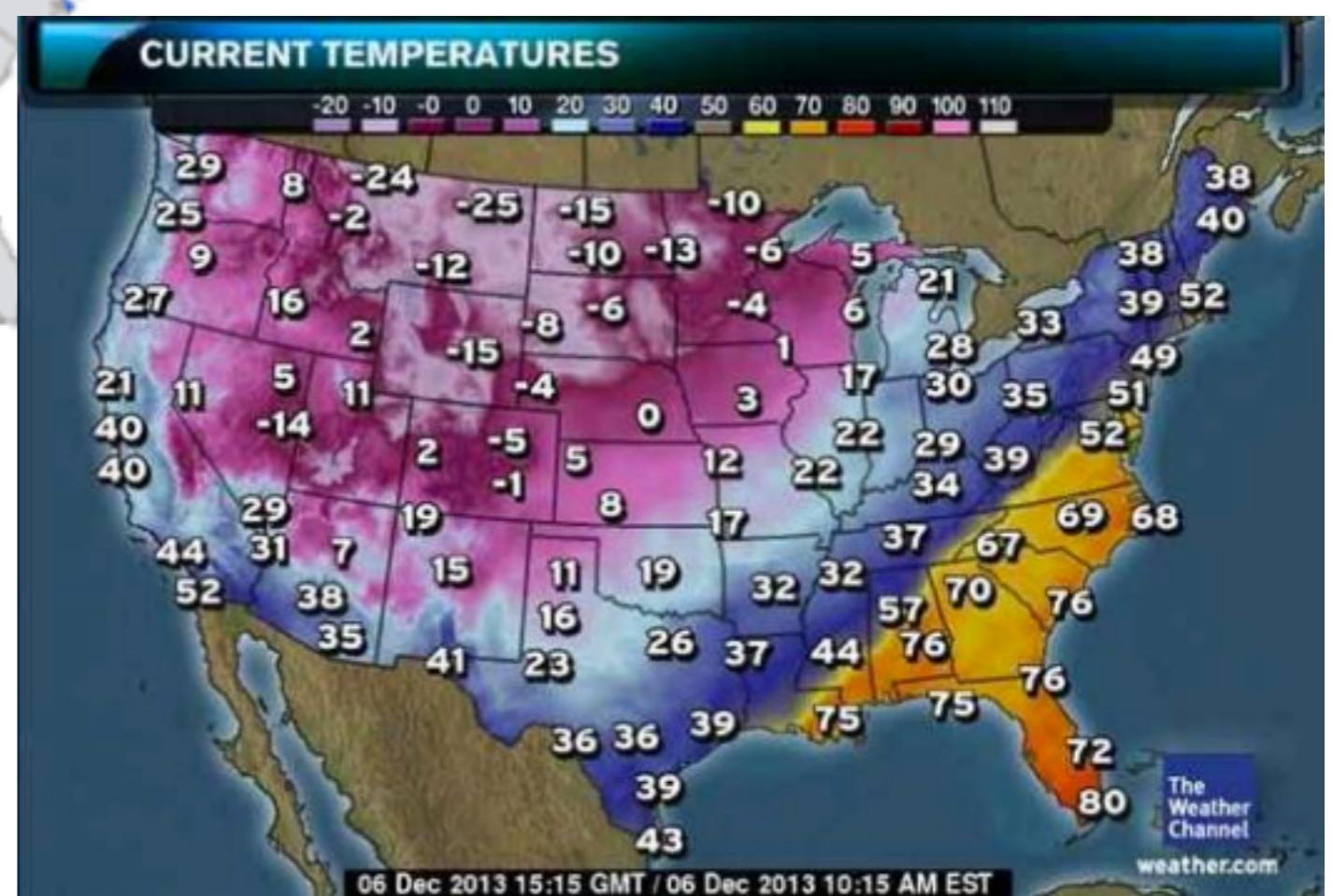
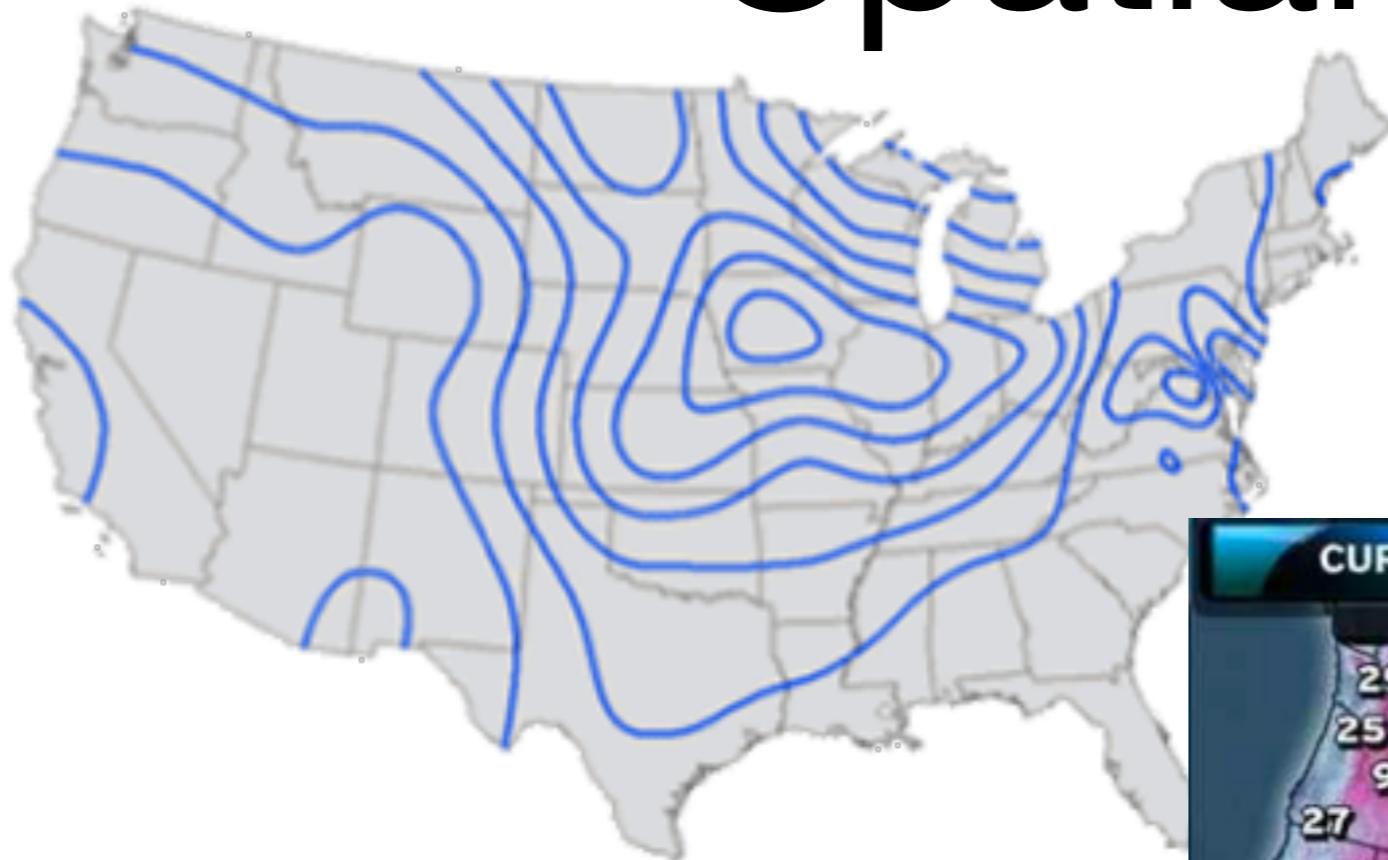


# Matrix Diagrams

<http://bost.ocks.org/mike/miserables/>



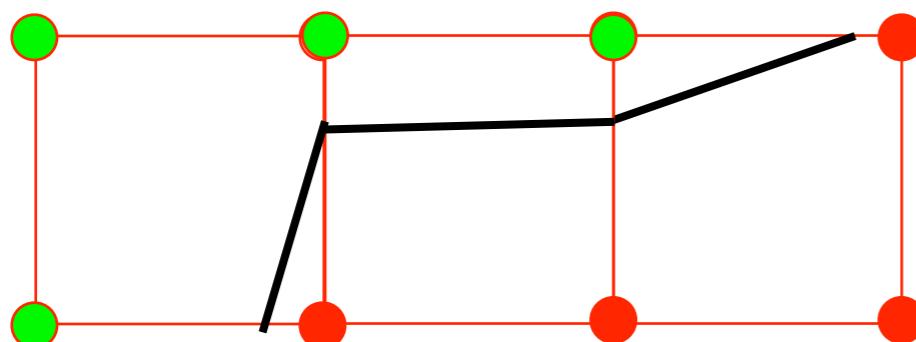
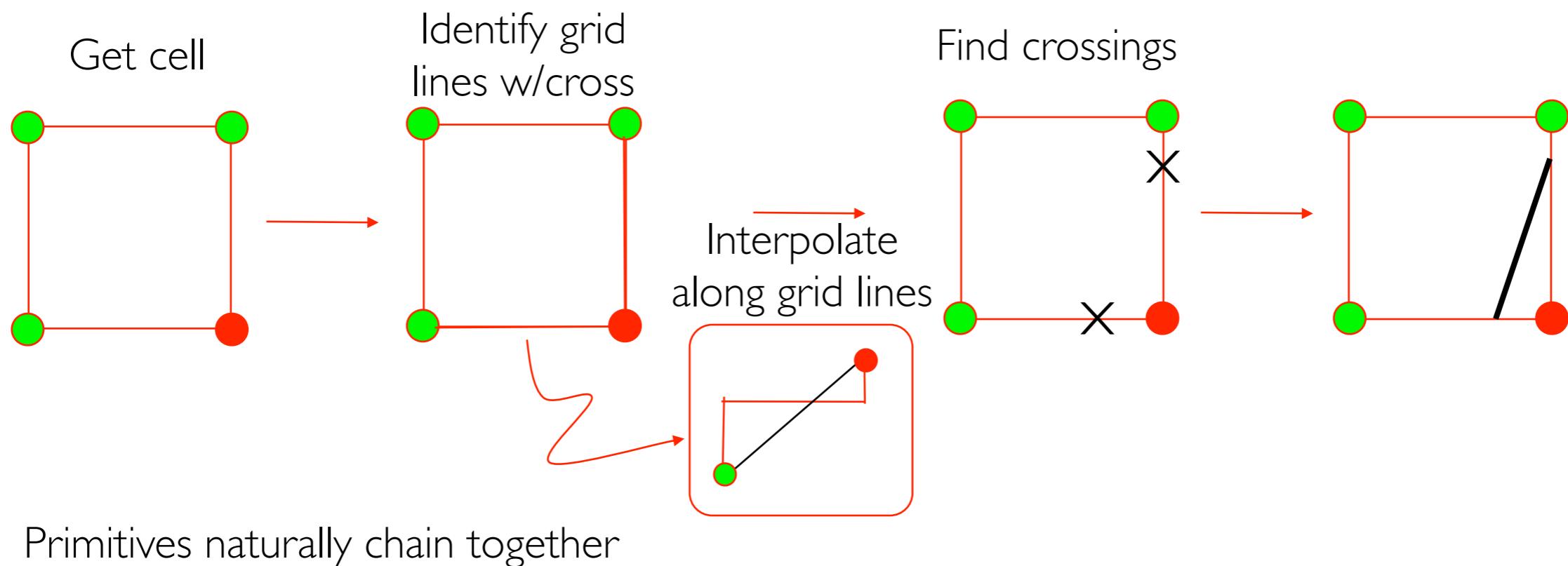
# Spatial Data



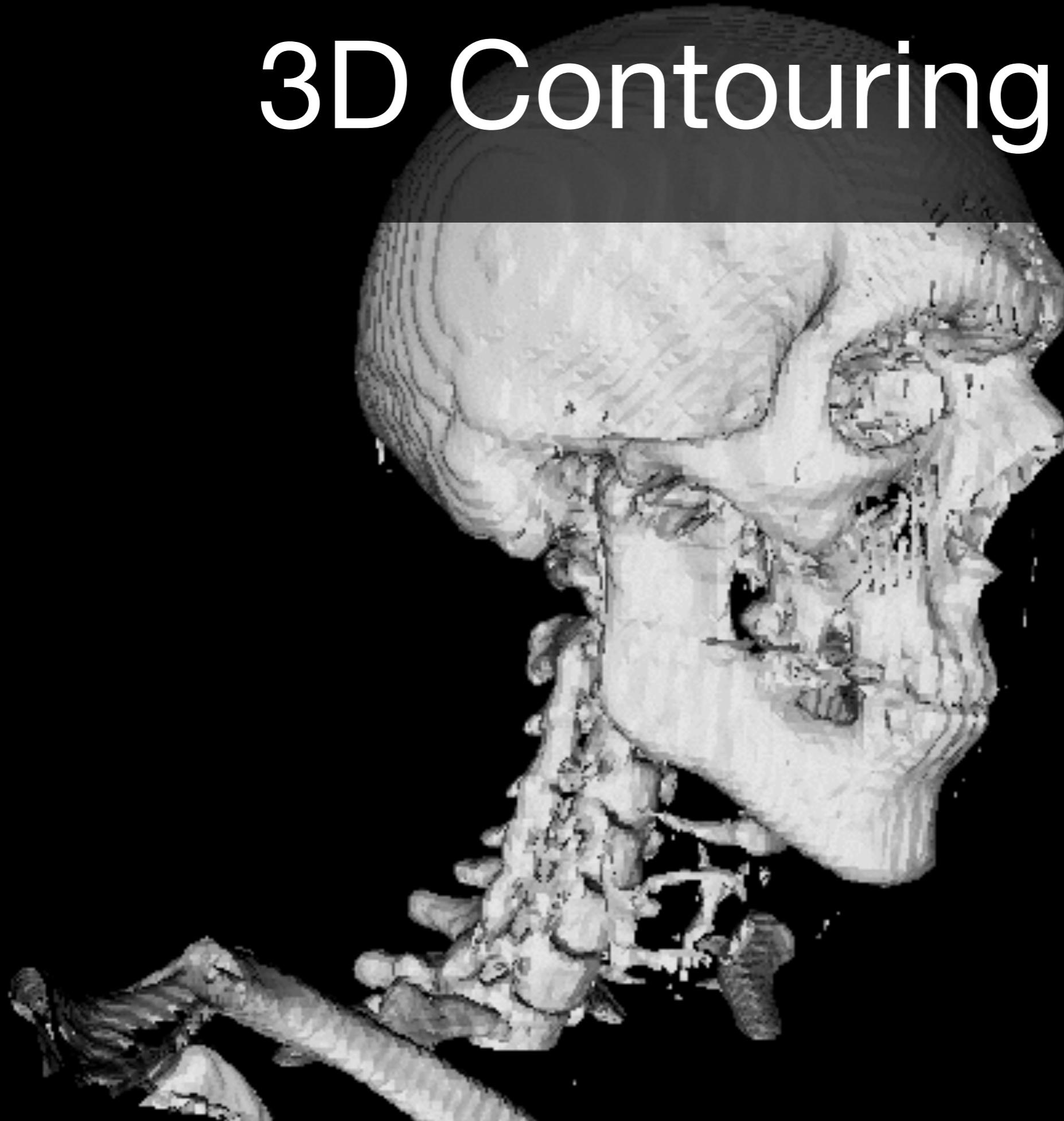
<http://ryanhill1.blogspot.com/2011/07/isoline-map.html>

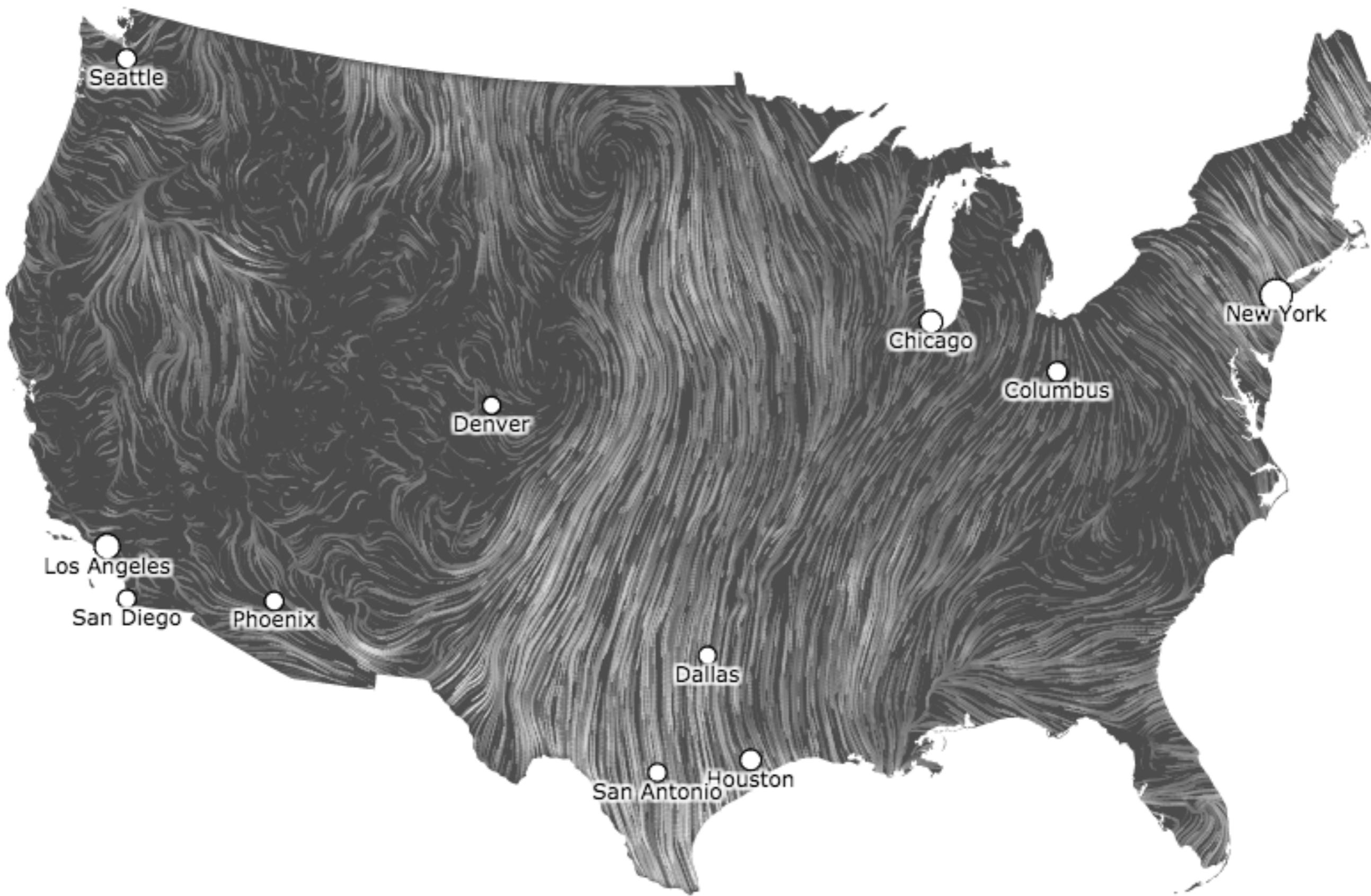
# Approach to Contouring in 2D

- Contour must cross every grid line connecting two grid points of opposite sign



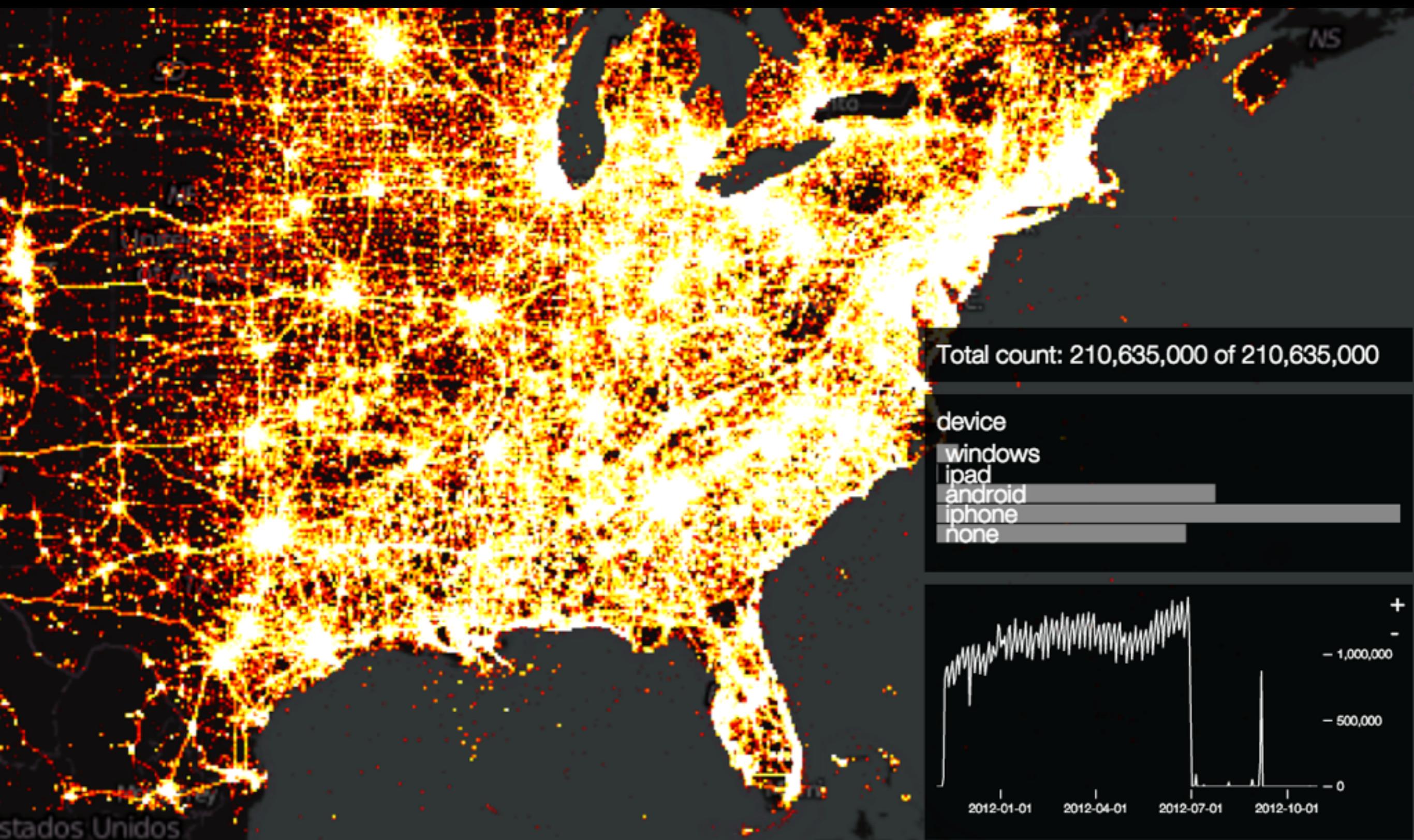
# 3D Contouring





# Spatial Data: Vector Fields

# Large Data



# Large Data: Open Problems

- Can we do exploratory visual analysis, cleaning, etc. on large data?
- What are the necessary data structures?

# CS444: Data Visualization

- Now you know **why, how and how not to** create visualizations for your data!