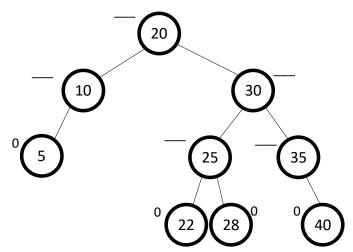
CS104: Data Structures & Object-Oriented Programming Summer 2021 - Final Exam Sample Problems

1. **(12 pts.) AVL trees:** Consider the AVL tree shown below.



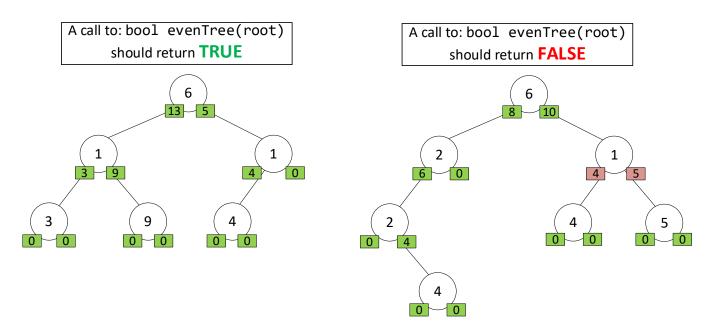
- 1.1. Choose the correct balance for the node with key 10? [-2 / -1 / 0 / +1 / +2].
- 1.2. Choose the correct balance for the node with key 20? [-2/-1/0/+1/+2].
- 1.3. Choose the correct balance for the node with key 25? [-2/-1/0/+1/+2].
- 1.4. Choose the correct balance for the node with key 30? [-2/-1/0/+1/+2].
- 1.5. Choose the correct balance for the node with key 35? [-2/-1/0/+1/+2].
- 1.6. Which node, if any, when removed would necessitate a rotation(s)? [List the node's key or type "none" if none exists].
- 1.7. Show the process for insert(29) including where it is added, updates of any balance values, and the result of any necessary rotations. You can draw the tree at a few points in time during the insert process and need only draw the relevant parts of the tree (though you must show the relevant parts). Upload a PDF or image of your work.

- 2. **(10 pts.) Counting**: For all 3 problems below, Julia has <u>EXACTLY 6 hours</u> to bingewatch some episodes for various shows. You must show work that supports your final answer to get any credit. You can either upload your work as a scan/picture OR just type it in using a text-based approach (i.e. nCk for n Choose k, nPr for n Permute r, 3^2 for 3 squared, etc.)
 - 2.1. Assuming that for a given show she always watches episodes in sequential order (never out of order), how many orderings exist for her to watch <u>8 half-hour</u> episodes from show A and <u>2 one-hour</u> long episodes from show B (assuming she can switch back and forth between shows as she pleases).
 - 2.2. Now assume she (strangely!) is willing to watch the episodes of the same show in ANY order (not sequentially). How many orderings exist of the ten total episodes described in the previous part of the problem.
 - 2.3. Assume she again watches episodes in (sequential) order. There are two unique shows (C and D...forget about A and B for this question) where one has at least <u>12</u> <u>half-hour</u> long episodes and the other has at least <u>3 two-hour</u> long episodes which she can watch in any (mixed) order. How many orderings exist of the episodes that she will watch?

- **3. (10 pts.) Number Theory** Show your work in the same manner and with the same requirements as the previous problem.
 - **3.1.** Find the **gcd(396,168)** using Euclid's algorithm (showing your work and demonstrating your understanding of the algorithm.

3.2. Find the smallest two integer such that 396x + 168y = gcd(396,168) demonstrating you understand the method taught in class.

4. (10 pts.) Trees and Recursion. Given a binary tree of non-negative integers, write a recursive function that returns TRUE if the sum of all nodes in the left and right subtree of EACH node is an even number. If the sum of nodes in the left and right subtree of even 1 node is odd, return false. Non-existent nodes have an implicit value of 0. Also, an empty tree should return `true`. No loops are allowed so you must use recursion.



Complete your code in the linked <u>eventree.cpp</u> and submit that file. A portion is reproduced below.

5. Hashing (10 pts.)

Consider a hash table that uses **open-addressing** (some form of probing) and the same table structure (vector of HashItem pointers) from homework 6 as well as a similar HashItem structure (reproduced below for your benefit). Now write a function that will **compute how many buckets** of the hash table would be **empty** if **chaining / closed-addressing** had been used instead (for the same table size).

You do not necessarily need to convert the table to use chaining, simply calculate how many locations / buckets would be **empty**. Your function must run in **Theta(m)** time where `m` is the table size. You may declare other arrays / data structures as needed.

Complete your code in the linked **chains.cpp** and submit that file. A portion is reproduced below.

```
// HashItem definition used by the hash table
template <typename KeyType, typename ValueType>
struct HashItem {
   typedef std::pair<KeyType, ValueType> ItemType;
   ItemType item;
   bool deleted;
};
* @brief FUNCTION YOU NEED TO WRITE
* Computes the number of empty buckets that would exist if
* the hash table used chaining rather than open-addressing (probing).
* @param [in] table Hash table of pointers to HashItems. An entry
* is occupied if the pointer is non-NULL
* @param [in] h Hash function that supports operator()(Key) and returns
    an unsigned integer of arbitrary size
* @return the number of buckets/chains that would be empty had chaining
    been used rather than open-addressing
*/
template<typename HashItem, typename Hash>
size t numEmptyIfChaining(const std::vector< HashItem* >& table, Hash h);
```

Intentionally blank for scratch work.	Please turn it in with your exam:
Name:	Section time: