

1. Write a set of inference rules that allow us to work through a simple addition example.

DoPlus Example:

$$4 + 2 = 6$$

DoPlus Example:

$$5 + 6 = 11$$

SearchPlus Example:

$$5 + (4 + 2) \quad (\text{use SearchPlus to step on } e2)$$

$$5 + 6 \quad (\text{use DoPlus})$$

$$11$$

SearchPlus2 Example:

$$(2 + 3) + (4 + 2) \quad (\text{use SearchPlus 2 to step on } e1)$$

$$5 + (4 + 2) \quad (\text{use SearchPlus to step on } e2)$$

$$5 + 6 \quad (\text{use DoPlus})$$

$$11$$

2. Write a set of inference rules such that the evaluation of $e1 / e2$ short-circuits if $e2$ is zero.

Definition: Short-circuiting is when we return out of an evaluation early. Here, we know that anything divided by zero is undefined - it doesn't matter what the numerator is. So if the denominator is ever zero, we can return undefined without looking at $e1$ (the numerator) at all.

Short-Circuit Example:

$$((6/2)/3)/0 \rightarrow \text{undefined}$$

DoMinus Example

$$3 - 3 = 0$$

DoMinus Example

$$4 - 1 = 3$$

DoDiv1 Example:

$$81 / 3 = 27$$

DoDiv1 Example:

$$27 / 3 = 9$$

DoDiv2 Example:

$$((6/2)/3) / 0 \rightarrow \text{undefined}$$

DoDiv2 Example:

$(81/3) / 0 = \text{undefined}$

SearchDiv1 Example:

$(81/3) / (3-3)$ (use SearchDiv1/DoMinus to step on e2)

$(81/3) / 0$ (use DoDiv2 to short-circuit)

undefined

SearchDiv2 Example:

$(81/3) / (4-1)$ (use SearchDiv1/DoMinus to step on e2)

$(81/3) / 3$ (use SearchDiv2 to step on e1)

$27 / 3$ (use DoDiv1)

9