

# A Framework for Formal Verification to Correct Actions in Reinforcement Learning

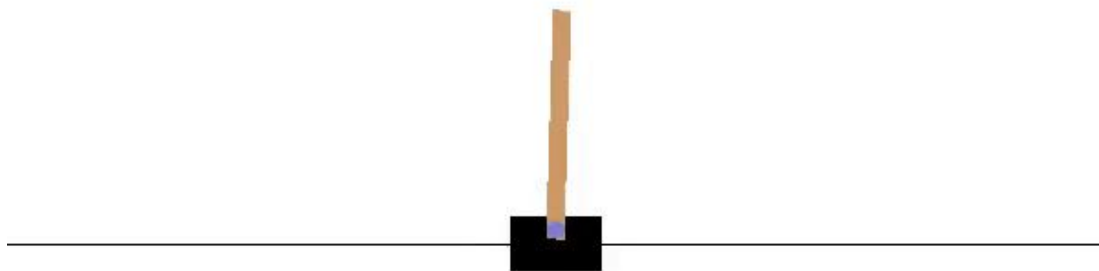
Ethan Hobbs and Vikas Nataraja

# Outline

- Reinforcement Learning Background
- Motivation
- Our Approach
- Algorithm
- Implementation
- Results
- Conclusion and Future Work

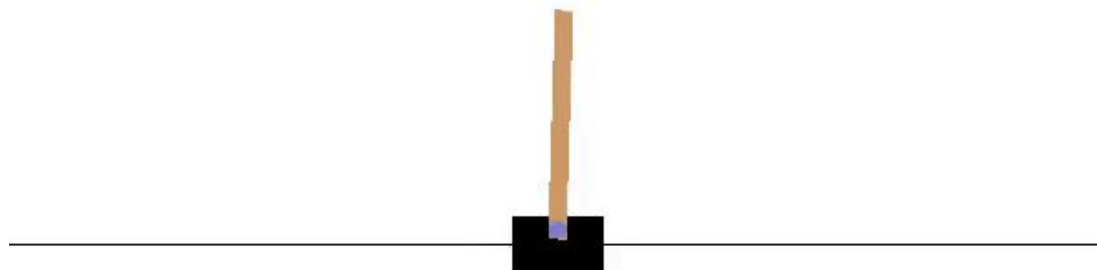
# Reinforcement Learning Background

- Cartpole
- Maximize a reward in a given situation.
- +1: every timestep it stays upright
- -1: every time it falls.



# Reinforcement Learning Background

- RL agent has to take the “correct” actions at the “correct” states.
- policy  $\pi$ : how the agent knows what action ‘a’ to take at a state ‘s’.
- States - Safe vs Unsafe



State Verification is Hard



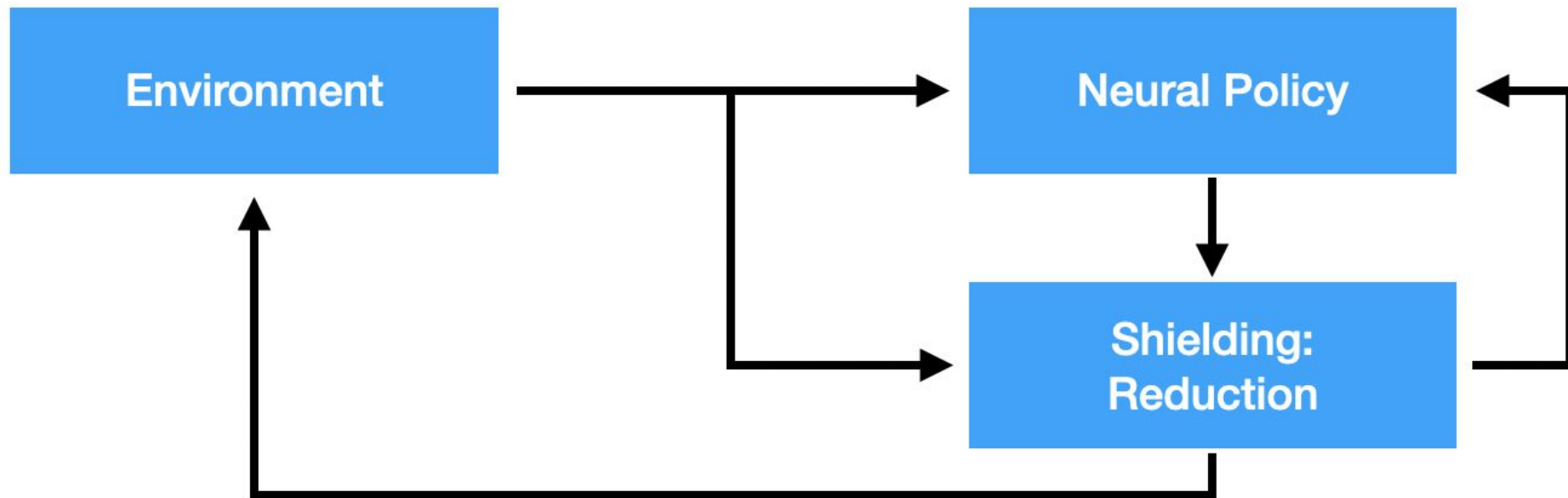
Reachability Analysis or

Markov Decision Process

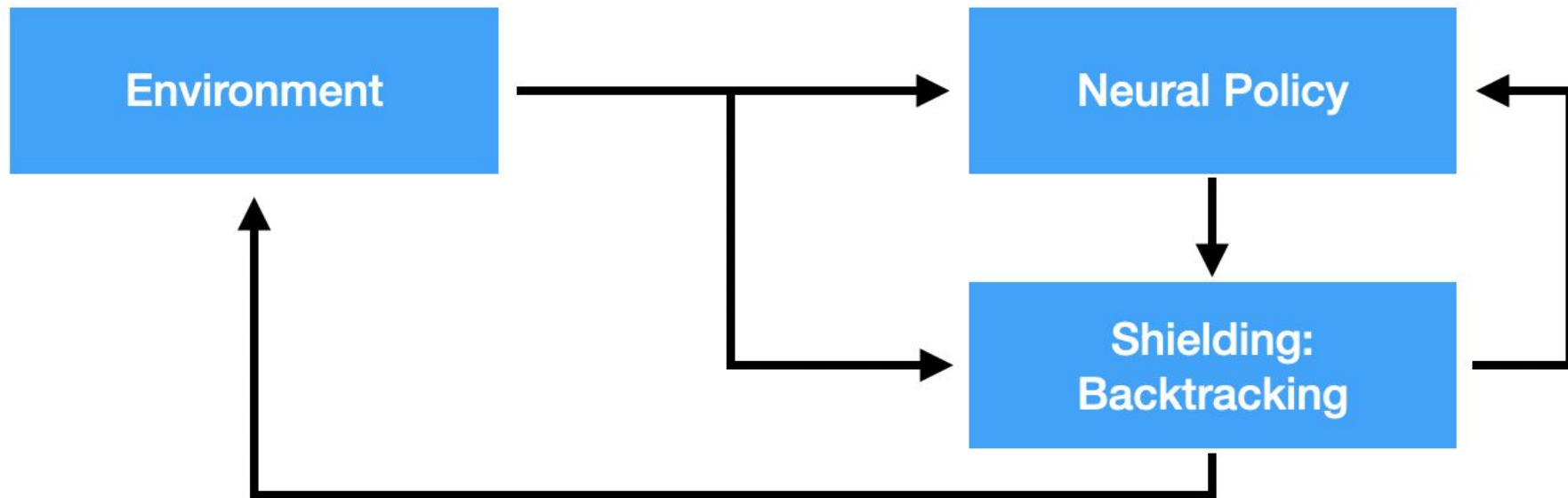


Shielding Methods

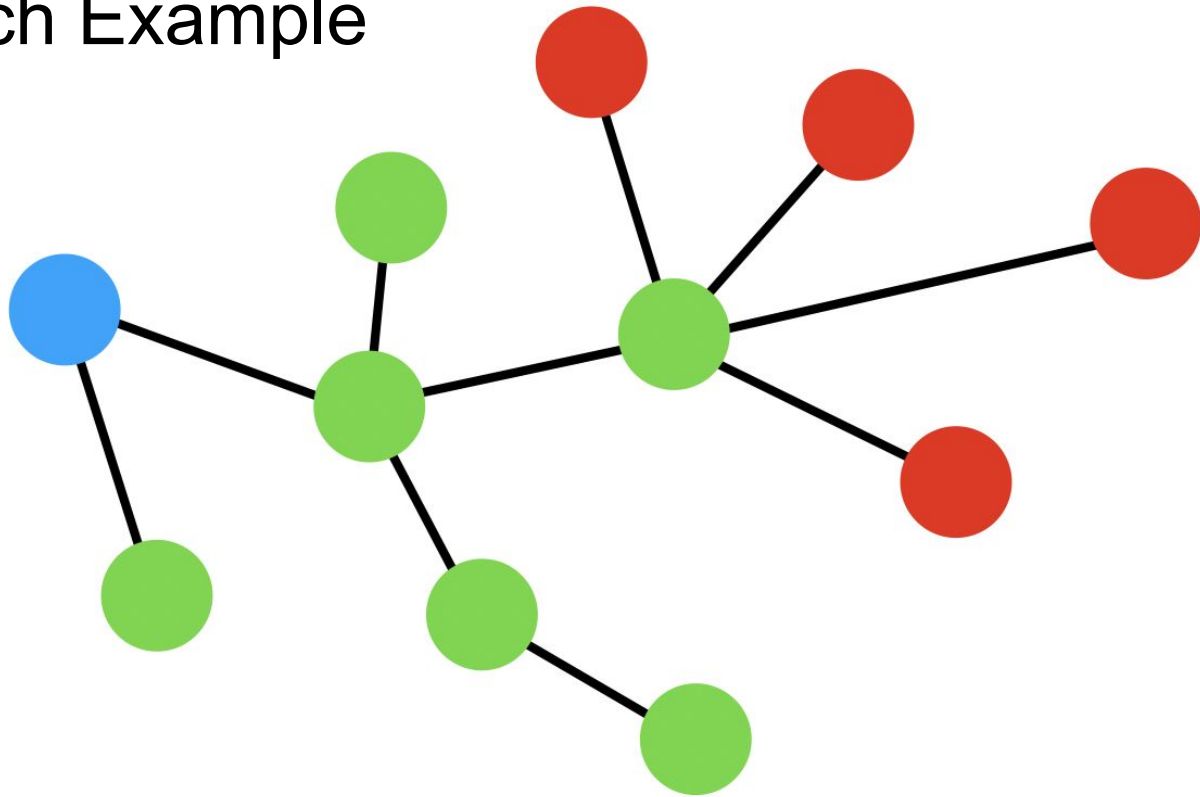
# Our Approach



# Our Approach

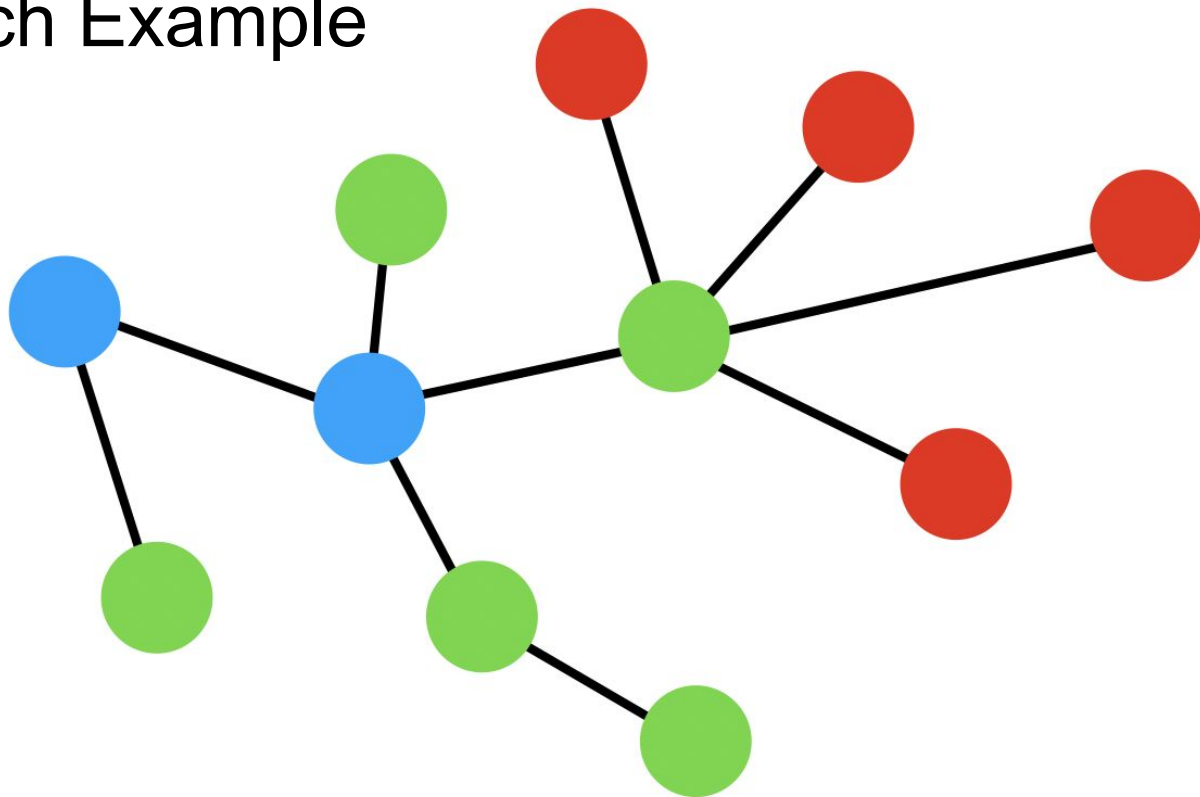


## Approach Example

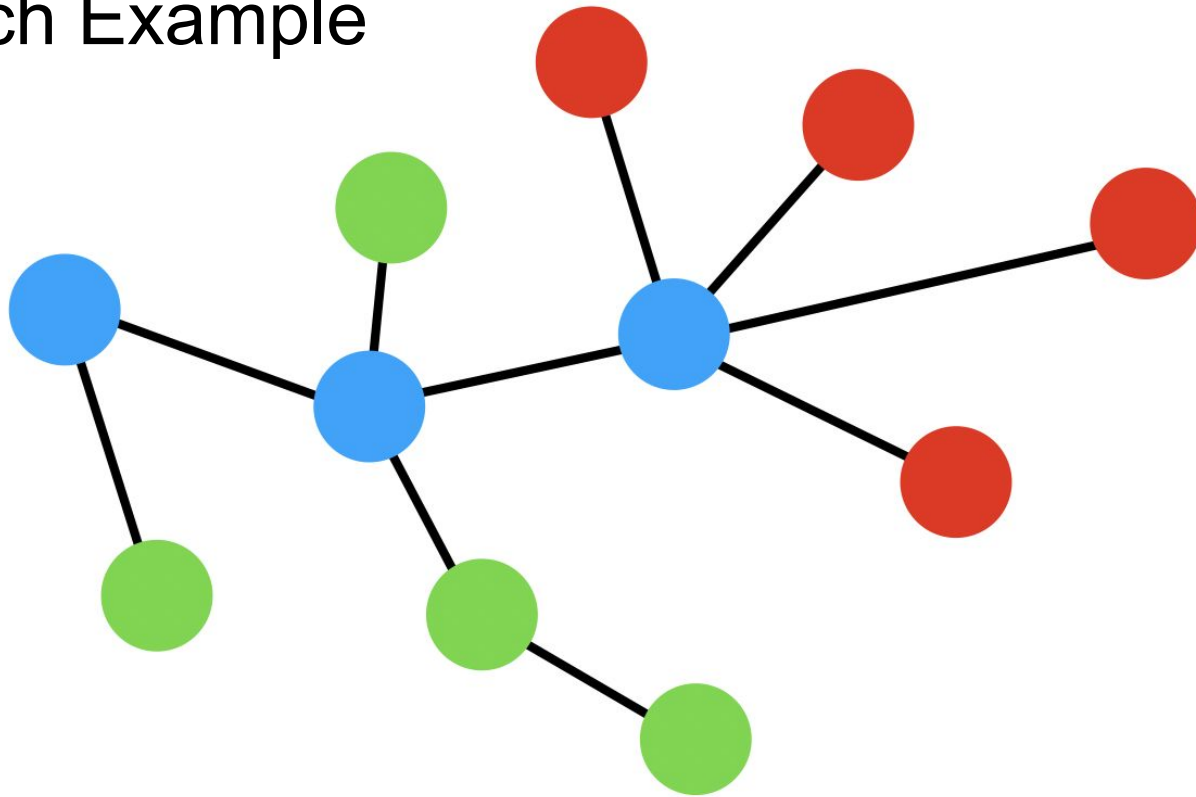




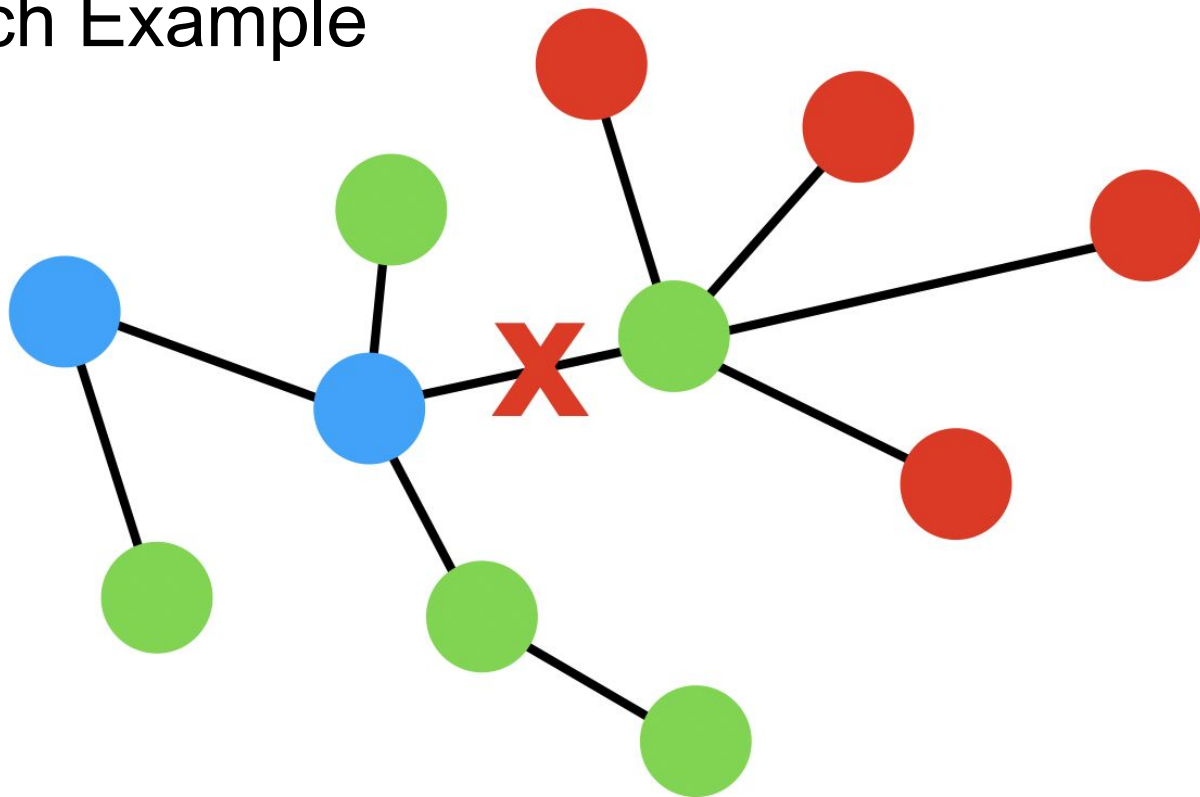
## Approach Example



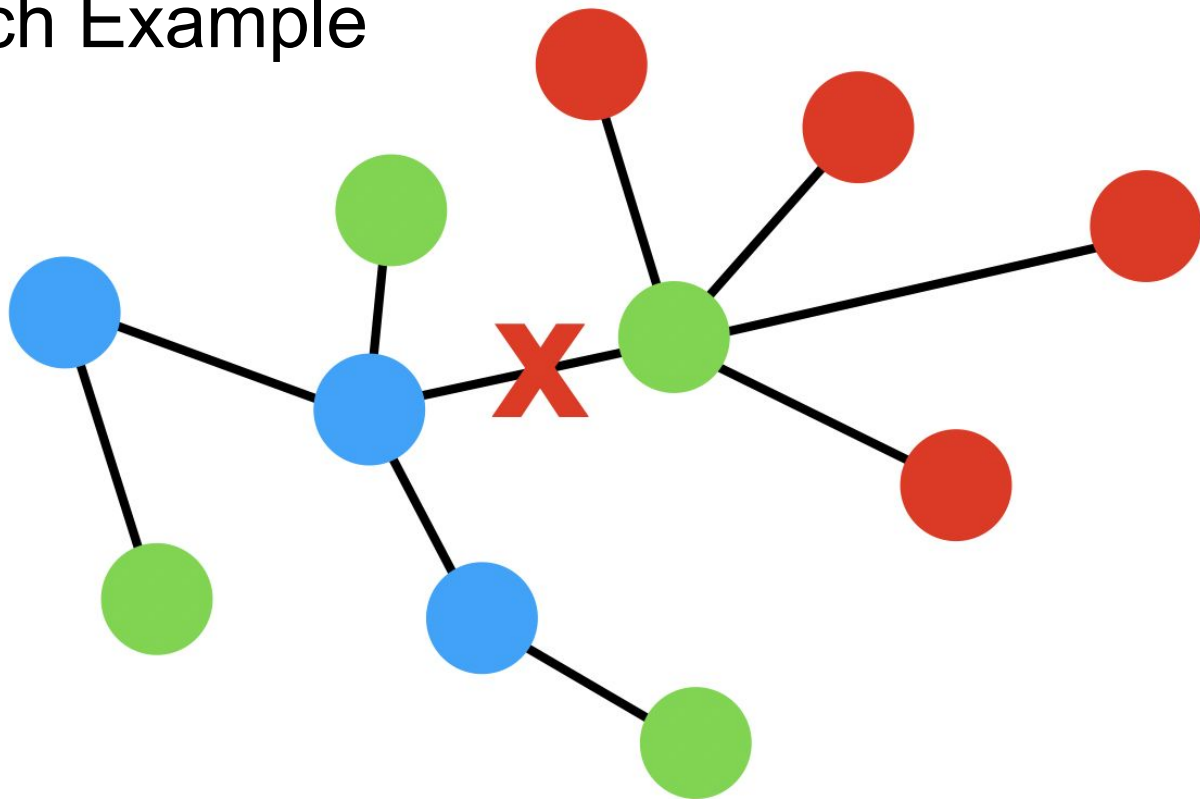
## Approach Example



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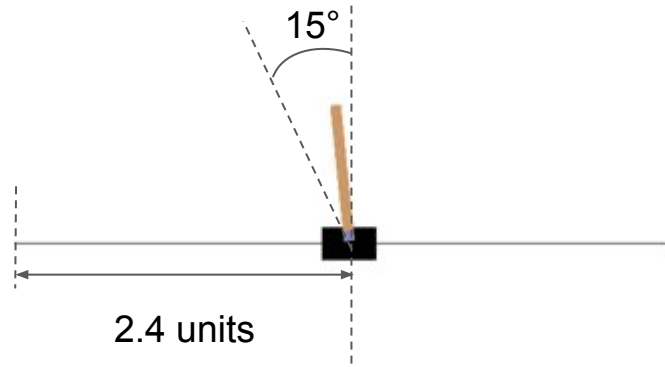


## Approach Example

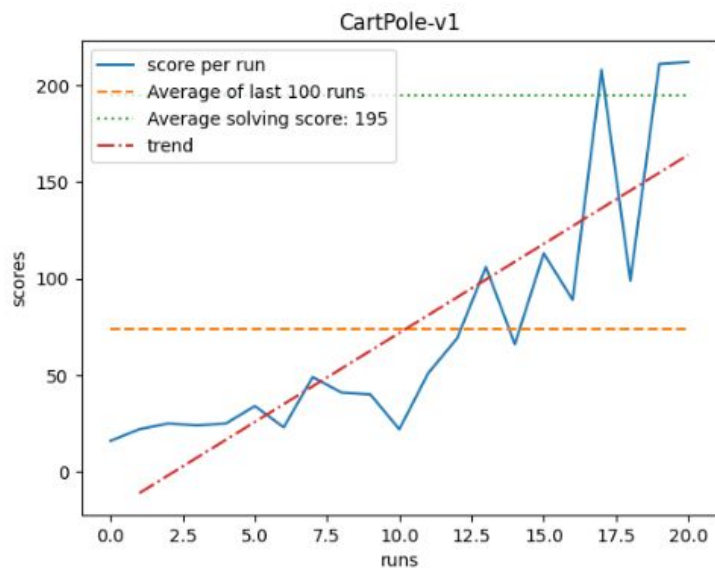


# Implementation

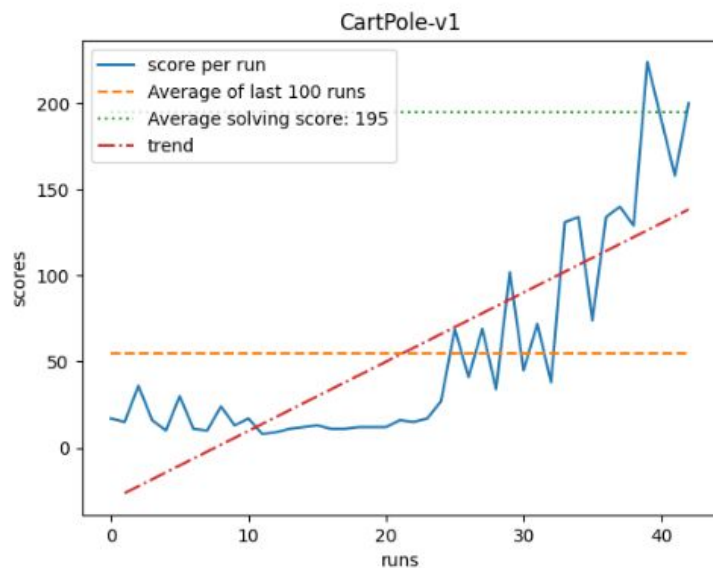
- Used OpenAI gym CartPole scenario
- A pole is attached by an un-actuated joint to a cart, which moves along a frictionless track.
- The system is controlled by applying a discrete force measure to the cart. The pendulum starts upright, and the goal is to prevent it from falling over.
- Reward of +1 for every time step that the cart doesn't fall over.
- Episode ends when the pole moves more than  $15^\circ$  from the vertical or when the cart moves 2.4 units from the center.



# Results - All valid states

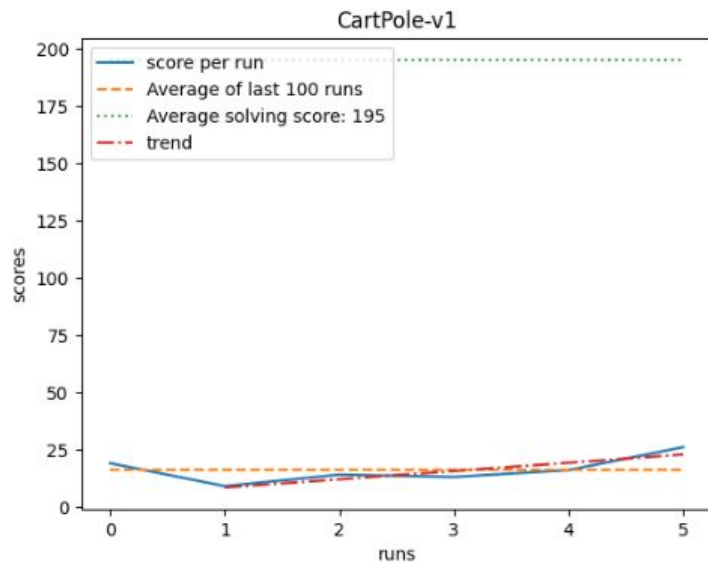


(a) Baseline model evaluated under all valid states

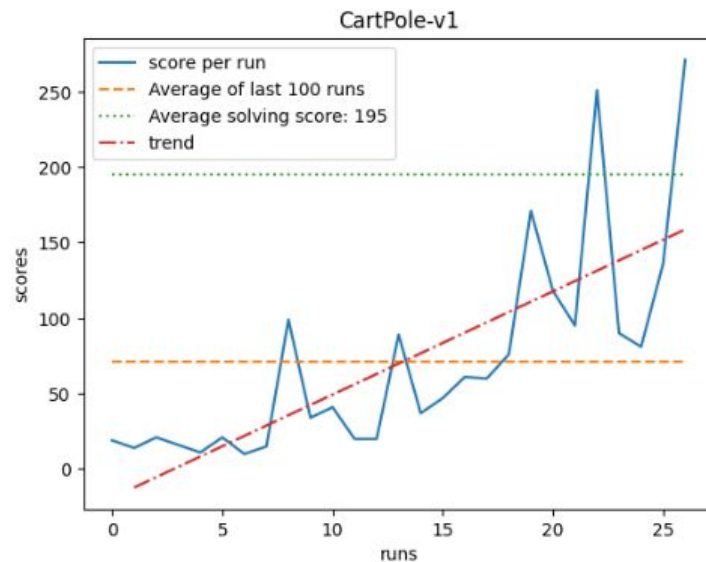


(b) Proposed model evaluated under all valid states

# Results - One invalid state

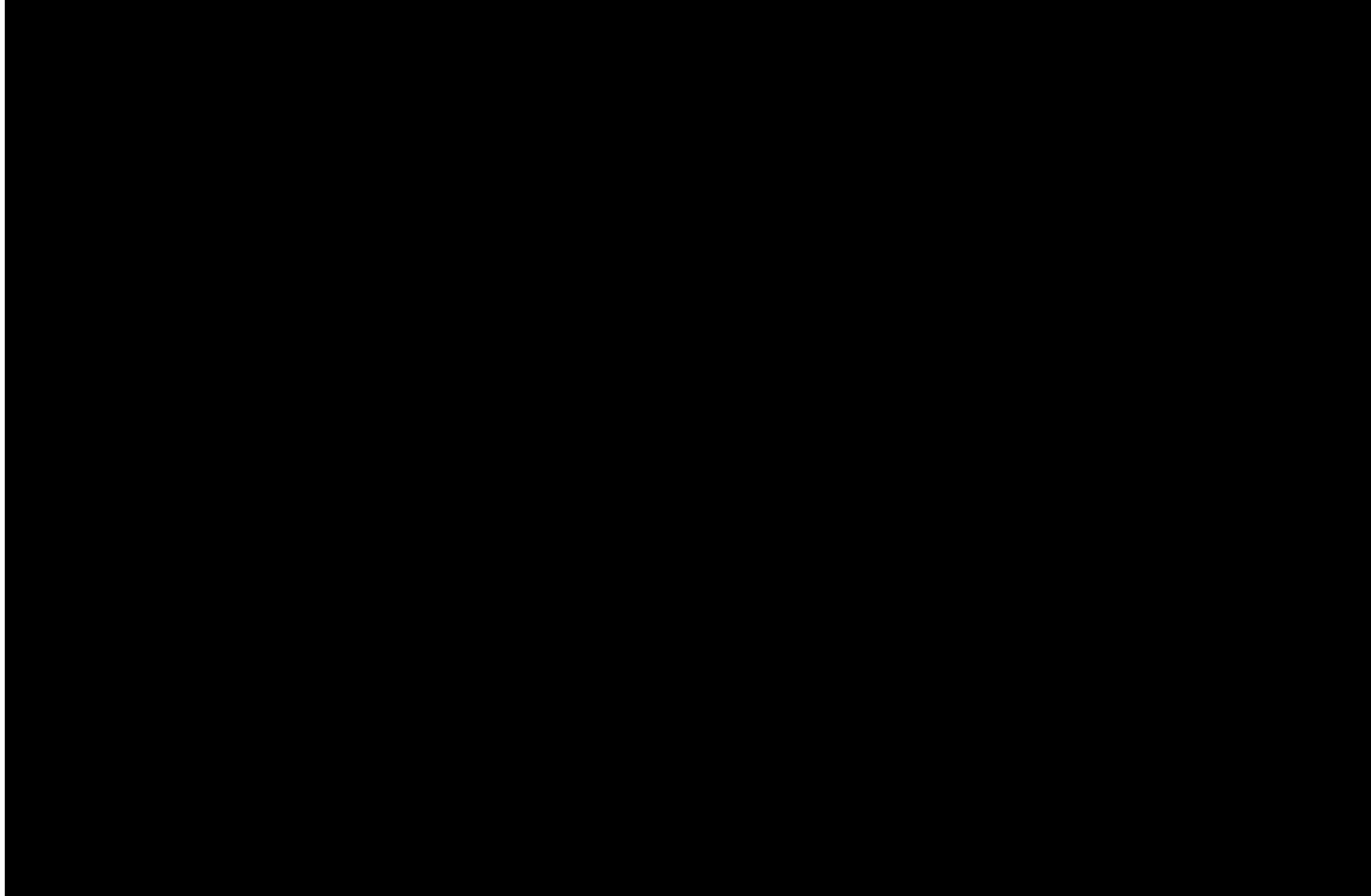


(a) Baseline model evaluated under one invalid state



(b) Proposed model evaluated under one invalid state

# Video Demonstration





# Conclusion and Future Work

- We propose an alternative approach to verifying validity of states and actions in reinforcement learning.
- Instead of reverting to one of initial states or reducing the state space, we propose using “backtracking” where we use the agent’s history of states and actions to switch to a safe state.
- Our approach although results in a temporary sub-optimal policy guarantees safe state transitions.
- To expand on our approach, we intend to test on other scenarios and dynamics where the environment’s observation space is more complex.
- We also would like to work on making the model perform faster because currently the model gets slower as the look-ahead factor increases

# Thank you!





# Reinforcement Learning Background

- To maximize the reward, the RL agent has to take the “correct” actions at the “correct” states.
  - This is called a *policy*  $\pi$  which is how the agent knows what action ‘a’ to take at a state ‘s’.
  - To do this, a Q-function is used:

$$Q^\pi(s, a) = \mathbb{E}_\pi[R_t | S_t = s, A_t = a]$$

- After an action is taken, the outcome is observed and the Q value is updated:

$$\underbrace{\text{New } Q^\pi(s, a)}_{\text{New Q-Value}} = Q^\pi(s, a) + \underbrace{\alpha}_{\text{Learning Rate}} \left[ \underbrace{R(s, a)}_{\text{Reward}} + \underbrace{\gamma \max_{a'} Q'(s', a')}_{\substack{\text{Maximum predicted reward, given} \\ \text{new state and all possible actions}}} - Q(s, a) \right]$$

Discount factor

# Algorithm

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**Algorithm 1:** Verification Algorithm

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- 1 Synthesize the deterministic program
  - 2 Project forward  $n$ -steps
  - 3 Set threshold for backtracking timestep  $thresh$
  - 4 Check the validity of possible future states dependent on  $\gamma$
  - 5 **if**  $valid\ states \geq 1$  **then**
    - 6      $Q^\pi(s, a) = \mathbb{E}_\pi[R_t | S_t = s, A_t = a]$
    - 7      $NewQ^\pi(s, a) = Q^\pi(s, a) + \alpha[R(s, a) + \gamma \cdot \max Q'(s', a') - Q(s, a)]$
  - 8 **else**
    - 9     search replay buffer history and choose random state with  $k > thresh$
    - 10     $s = s_k, a = a_k$
    - 11     $Q^\pi(s, a) = \mathbb{E}_\pi[R_t | S_t = s, A_t = a]$
    - 12     $NewQ^\pi(s, a) = Q^\pi(s, a) + \alpha[R(s, a) + \gamma \cdot \max Q'(s', a') - Q(s, a)]$
  - 13 **end**
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