# Synchronous Dataflow Programming CS684: Embedded Systems

Topic 2

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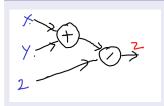
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## Synchronous Dataflow Programs in Lustre/Heptagon

A network of Operators connected by named wires.

#### Example

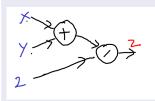


```
node MEAN(X,Y: int)
            returns (Z:int)
let
    Z = (X + Y) / 2;
tel
```

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#### Example



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#### **Semantics**

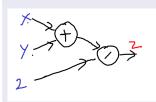
Semantics: X, Y, Z are discrete flows.

- ullet Time is discrete. Given by  $\mathbb{N}$ . (e.g. clock cycles in circuits).
- Flow  $X : \mathbb{N} \to Val_X$ . (almost)
- $\forall t \in \mathbb{N}$ :  $Z_t = (X_t + Y_t)/2$  (pointwise application)

# Synchronous Dataflow Programs in Lustre/Heptagon

A network of Operators connected by named wires.

#### Example



#### Simulation

$$Z_i = (X_i + Y_i)/2, \forall i \in Clock$$

## Set of Equations Defining Variables

#### **Equivalent Programs**

```
node MEAN(X,Y: int)
            returns (Z:int)
let
   Z = (X + Y) / 2;
tel
```

```
node MEAN(X,Y: int)
            returns (Z:int)
var W : int;
let
    Z = W / 2;
    W = X + Y;
tel
```

#### Structure of Lustre Node

- Set of equations, one for each output or local flow (variable).
- Declarative order not important.
- Semantics: Order the equations in data dependancy order and then compute at each reaction.
- All operators are applied pointwise.
- Causality ensures deterministic behaviour unique output for each input.

#### Language Elements

- Primitive Data types bool, int, real
- Expressions and equations
  - constants 2 gives the flow 2,2,2,2
  - combinational operators arithmetic, logical, ... Z = X + Y applied pointwise  $Z_i = X_i + Y_i$ ,  $\forall i$ .
  - if < bexpr> then <expr> else <expr>

# Memory/Delay

#### pre X

X	<i>x</i> <sub>0</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	
pre(X)	nil	<i>x</i> <sub>0</sub>	<i>x</i> <sub>1</sub>	
Clock	0	1	2	
pre(pre(X))	nil	nil	<i>x</i> <sub>0</sub>	

$$(pre(X))_0 = nil$$
  
 $(pre(X))_i = X_{i-1}, \forall i > 0$ 

## Initialization $X-\rangle Y$

X	<i>x</i> <sub>0</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	
Y	<i>y</i> 0	<i>y</i> <sub>1</sub>	<i>y</i> <sub>2</sub>	
X->Y	<i>x</i> <sub>0</sub>	<i>y</i> <sub>1</sub>	<i>y</i> <sub>2</sub>	
Clock	0	1	2	
$X \rightarrow pre(Y)$	<i>x</i> <sub>0</sub>	<i>y</i> <sub>0</sub>	<i>y</i> <sub>1</sub>	

$$(X -> Y)_0 = X_0$$
  
 $(X -> Y)_i = Y_i, \forall i > 0$ 

### **Examples of Equations**

```
    Counter X = 0 -> (pre(X) + 1)
    Fibonnachi Z = 1 -> pre(Z -> (Z + pre(Z)))
    Edge
```

```
node EDGE(X:bool) returns (Y:bool)
let
    Y = false -> X and not pre X;
tel
```

Counter with Reset Counts no of occurrences of X. Resets when R occurs.

## Modularity: Node as Operator

```
node MINMAX(X:int)
            returns (min, max:int)
let
  min = X \rightarrow if (pre(min) < X) then
                   pre(min) else X;
  max = X \rightarrow if (X < pre(max)) then
                (pre max) else X;
tel
node AvgMINMAX(X:int)
               returns (Z:real)
var U,V:int;
let.
   Z = Average(U,V);
   U.V = MINMAX(X):
tel
```

#### Tools

Compilation:

lustre file.lus nodename

Simulation luciole file.lus nodename

### Causality

#### Causally incorrect Programs

- X = X Circular definition.
- X = Y; Y = X Indirect Circular Definition
- X = pre(X) Causality ok but failur of initialization.
- X = 0 -> pre(X) Correct
- Syntactic causality Failure.

```
X = if C then A else Y;
Y = if C then X else B
```

Equivalent causally correct program.

```
X = if C then A else B;
Y = if C then A else B
```

## More Examples

Inverse Z transform? Stopwatch?

#### Heptagon

- Extension of Lustre. Similar to commercial language SCADE.
- New data types: enumeration, structures, array iterators, Generic nodes, Automata.
- Enumeration type Tlight = Red | Yellow | Green
- Structured Records type complex = { re: real; im: real}
- Arrays type Req: bool<sup>5</sup>

See Heptagon Manual for how to read elements of strucutured types and how to modify its value.

### Arrays

- Array type BaseType^Indextype E.g. Req : bool^5
   Static index access Req[0], Req[4].
   Dynamic index access Req.[x] default false.
- Array modification [ Req with [x] = false ].
- Array constructor [1,x,3,y,5]
- Array slice Req[1:3] gives array of size 3.
- Array slice catenation: A1@A2

## Array Slices Example

```
node rotate() returns (y0,y1,y2,y3:int)
var z: int^4;
let
  z = ([5,6,7,8]) fby ([z[3]]@z[0..2]);
  (y0,y1,y2,y3) = (z[0],z[1],z[2],z[3]);
tel
```

## Global Types and Constants

```
const n : int = 3
const v1 : int^n = [2,3,5]
node examplearrayslice() returns (z : int^n)
let
   z = ((v1) \text{ fby } ([z[n-1]]@z[0..n-2]));
tel
node display() returns (y0,y1,y2:int)
var z: int^n;
let
  z = examplearrayslice();
  (y0,y1,y2) = (z[0],z[1],z[2]);
tel
```

#### Parameterized Nodes and Static Genericity

We can pass static (compile time) parameters to nodes.

```
const n : int = 10
const t0 : float^n = 1.0^n
node TRANSVEC<<m:int; t1: int^n>>(a:int^m) = (b:int^m)
let
o = map << m>> (+)(a, t1);
tel
node SHIFT(a:int^n) = (o:int^n)
let.
o = f << n. t0>> (a):
tel
```

#### Array Iterators

Objectives: To manipulate arrays iteratively.

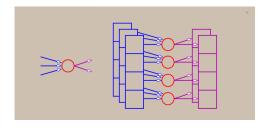
- Given vectors A: int<sup>n</sup> and B: int<sup>n</sup>, add them up to give vector
   C: int<sup>n</sup>. Use map.
- Given array  $A: int^n$ , find sum of its elements. Use fold. We can also compute  $\Sigma(A[i]^2)$  and use this to find standard deviation.
- Mapfold combines the map and the fold.

## Мар

 Example: Adding two 3-dimentional vectors a,b:real^3 to get c:real^3.

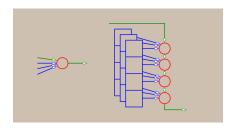
Method: Use + pointwise on every index accumulating the sum.

- c = map << 3>> (+) ([1,3,5],[4,3,-2]) gives [5,6,3]
- In general map<<n>>(F)  $(x_1,...,x_m)$  returns  $(y_1,...,y_k)$ Here  $F:(t_1\times...\times t_m)\to t'_1\times...\times t'_k$ . Also,  $x_i:t_i^n$  for  $1\leq i\leq m$  and  $y_j:t'_j^n$  for  $1\leq j\leq k$ .



#### Fold

- Example: Finding sum of array of 4 elements a:int^4 to get c:int.
   Method: Use + pointwise on every index accumulating the sum.
- c = fold << 4>> (+) ([1,3,5,7],0) gives 16
- In general fold<<n>>(F)  $(x_1, ..., x_m, z)$  returns y Here  $F: (t_1 \times ... \times t_m \times t) \rightarrow t$ . Also,  $x_i: t_i \hat{\ } n$  for  $1 \le i \le m$  and z, y: t.



### Mapfold

- Example: Adding two 3-dimentional vectors a,b:real^3 AND getting their dot-product c:real^3; dot:real
- node F(a,b,c:real) returns (d,e:real) let d=a+b; e=c + (
- c = mapfold<<3>>(F) ([1,3,5],[4,3,-2],0) gives [5,6,3], 3
- In general map<<n>>(F)  $(x_1,...,x_m)$  returns  $(y_1,...,y_k)$ Here  $F:(t_1\times...\times t_m)\to t'_1\times...\times t'_k$ . Also,  $x_i:t_i\hat{\ }n$  for  $1\leq i\leq m$  and  $y_j:t'_j\hat{\ }n$  for  $1\leq j\leq k$ .

