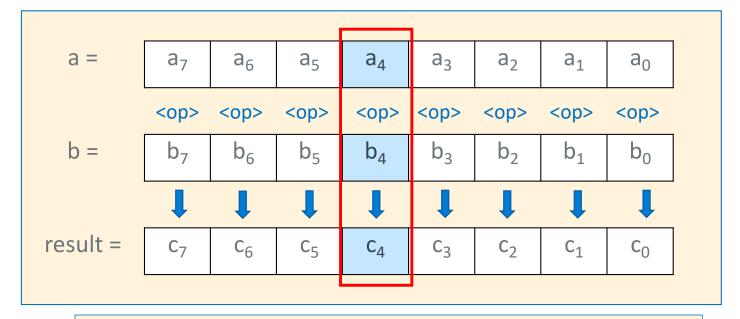


What is a Bitwise Operation?



- Bitwise operators are applied independently to each of the <u>corresponding</u> bit positions in each variable
- Each bit position of the result depends <u>only</u> on bits in the <u>same</u> bit position within the operands

Bitwise (Bit to Bit) Operators in C

output = ~a;

a	~a
0	1
1	0

output = a & b;

а	b	a & b
0	0	0
0	1	0
1	0	0
1	1	1

& with 1 to let a bit through

& with 0 to set a bit to 0

output	=	a	b;
--------	---	---	----

а	b	a b
0	0	0
0	1	1
1	0	1
1	1	1

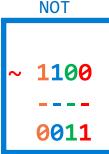
with 1 to set a bit to 1 with 0 to let a bit through

а	b	a ^ b
0	0	0
0	1	1
1	0	1
1	1	0

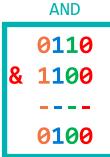
^ with 1 will flip the bit

^ with 0 to let a bit through

Bitwise NOT



Bitwise



Bitwise



Bitwise

DICWISC
EOR
0110
1100
1010

Bitwise Not (vs Boolean Not)

in C
int output = ~a;

a	~a
0	1
1	0

~ 1100 ----0011

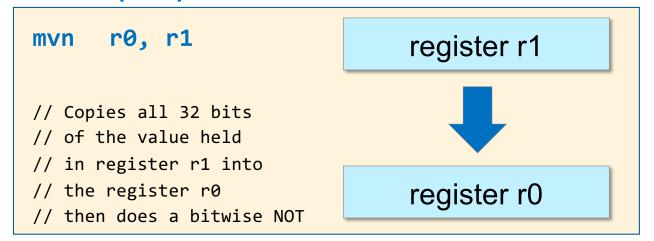
	Bitwise Not							
number	0101	1010	0101	1010	1111	0000	1001	0110
~number	1010	0101	1010	0101	0000	1111	0110	1001

Meaning	Operator	Operator	Meaning
Boolean NOT	!b	~b	Bitwise NOT

Boolean operators act on the entire value not the individual bits

Туре	Operation	result							
bitwise	~0x01	1111	1111	1111	1111	1111	1111	1111	1110
Boolean	!0x01	0000	0000	0000	0000	0000	0000	0000	0000

MVN (not)





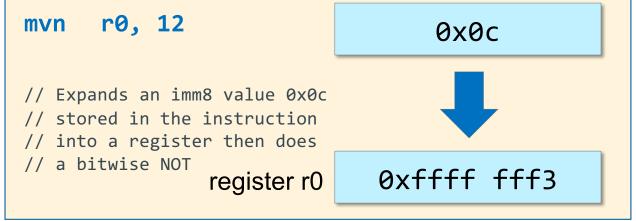
A bitwise NOT operationØxØc

imm8 expansion

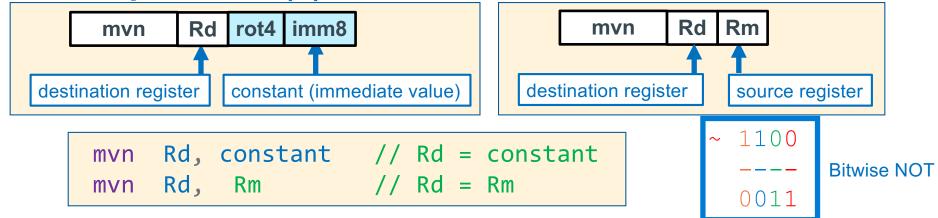
0x0000000c

bitwise not

0xfffffff3

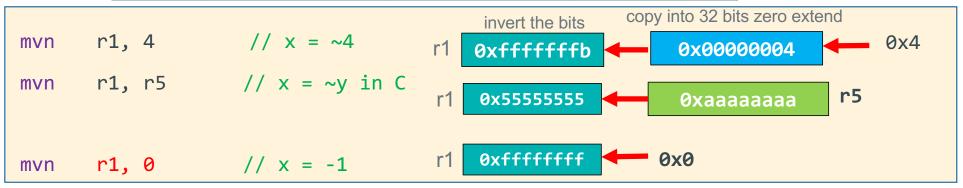


mvn – Copies NOT (~)

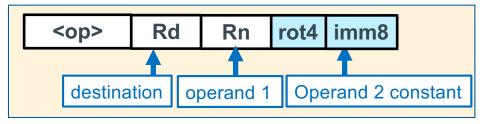


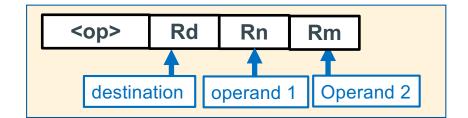
bitwise NOT operation. Immediate (constant) version copies to 32-bit register, then does a bitwise NOT

imm8	extended imm8	inverted imm8	signed base 10
0x00	0x00 00 00 00	0xff ff ff ff	-1
0xff	0x00 00 00 ff	0xff ff ff 00	-256



Bitwise Instructions





Bitwise <op> description</op>	C Syntax	Arm <op> Syntax Op2: either register or constant value</op>	Operation
Bitwise AND	a & b	and R _d , R _n , Op2	$R_d = R_n \& Op2$
Bitwise OR	a b	orr R _d , R _n , Op2	$R_d = R_n \mid Op2$
Exclusive OR	a ^ b	eor R _d , R _n , Op2	$R_d = R_n ^ Op2$
Bitwise NOT	a = ~b	mvn R _d , R _n	$R_d = \sim R_n$

Bitwise versus C Boolean Operators

Boolean Operators

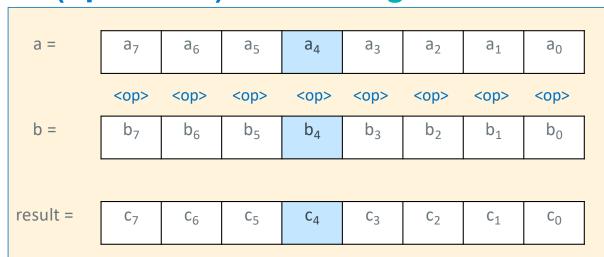
Bitwise Operators

Meaning	Operator	Operator	Meaning
Boolean AND	a && b	a & b	Bitwise AND
Boolean OR	a b	a b	Bitwise OR
Boolean NOT	!b	~b	Bitwise NOT

Boolean operators act on the entire value not the individual bits

```
bitwise & versus Boolean &&
0x10 \& 0x01 = 0x00 \text{ (bitwise)}
0x10 \&\& 0x01 = 0x01 \text{ (Boolean)}
bitwise ~ versus Boolean !
\sim 0x01 = 0xfffffffe \text{ (bitwise)}
!0x01 = 0x0 \text{ (Boolean)}
!0xff = 0x0 \text{ (Boolean)}
```

The act (operation) of *Masking*



- Bit masks access/modify specific bits in memory
- Masking act of applying a mask to a value with a specific op:
- orr: 0 passes bit unchanged, 1 sets bit to 1 (a = b | c; // in C)
- eor: 0 passes bit unchanged, 1 inverts the bit (a = b ^ c; // in C)
- and: 0 clears the bit, 1 passes bit unchanged (a = b & c; // in C)

Mask on

force bits to 1 "mask on" operation

- 1 to set a bit to 1
- 0 to let a bit through unchanged

```
Example: force lower 16 bits to 1

DATA: r2 0xab ab ab 77

orr

MASK: r3 0x00 00 ff ff

unchanged forces to a 1

RSLT: r1 0xab ab ff ff
```

```
Example: force lower 8 bits to 1

DATA: r2 0xab ab ab 77

orr r1 r2, 0xff

r1 = r2 | 0xff; // in C

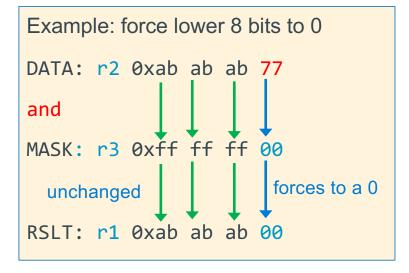
RSLT: r1 0xab ab ab ff
```

Mask off

force bits to 0 "mask off" operation

- 0 to **set a bit to 0** ("clears the bit")
- 1 to let a bit through unchanged

```
and r1, r2, r3
r1 = r2 & r3; // in C
```



```
Example: force lower 8 bits to 0

DATA: r2 0xab ab ab 77

and r1 r2, 0xffffff00

r1 = r2 & 0xffffff00; // in C

RSLT: r1 0xab ab ab 00
```

Extracting (Isolate) a Field of Bits with a mask

```
extract top 8 bits of r2 into r1
0 to set a bit to 0 ("clears the bit")
1 to let a bit through unchanged
and r1, r2, r3
```

```
DATA: r2 0xab ab ab 77
and
MASK: r3 0xff 00 00 00
unchanged forces to a 0
RSLT: r1 0xab 00 00 00
```

```
extract top 8 bits of r2 into r1

DATA: r2 0xab ab ab 77

and r1, r2, 0xff000000

RSLT: r1 0xab 00 00 00

r1 = r2 & 0xff000000; // in C
```

Finding if a bit is set

```
query the status of a bit "bit status" operation
  • 0 to set a bit to 0 ("clears the bit")
  • 1 to let a bit through unchanged
        and r1, r2, 0x02
        cmp r1, 0
        beq .Lendif
        // code for is set
.Lendif:
```

```
unsigned int r1, r2;
// code
r1 = r2 & 0x02
if (r1 != 0) {
    // code for is set
}
```

```
Example is bit 1 set

DATA: r2 0xab ab ab 77

and

MASK: 0x00 00 00 02 is bit 1 set?

forces to a 0 unchanged

RSLT: r1 0x00 00 00 02 != 0 if set
```

```
unsigned int r2;
// code
if ((r2 & 0x02) != 0) {
     // code for is set
}
```

Even/Odd

```
Even or odd, check LSB (same as mod %2)

check LSB (bit 0) if set then odd, else even

and r1, r2, 0x01

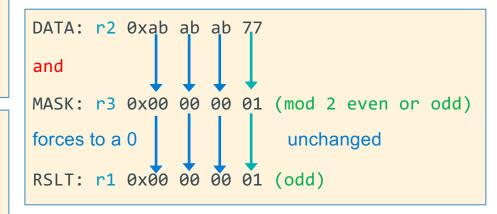
cmp r1, 0x01

bne .Lendif

// code for handling odd numbers

.Lendif:
```

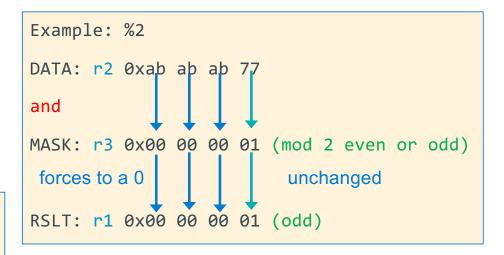
```
unsigned int r2;
// code
if ((r2 & 0x01) != 0) {
    // code for handling odd numbers
}
```

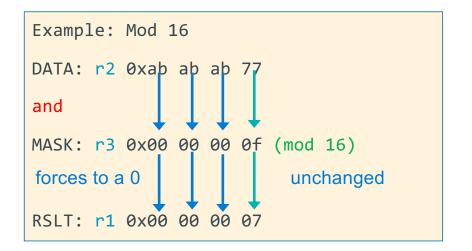


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MOD %<power of 2>

remainder (mod): num % d where num ≥ 0 and d = 2^k mask = 2^k -1 so for mod 16, mask = 16 -1 = 15 and r1, r2, r3





Flipping bits: bit toggle Used in PA7/PA8

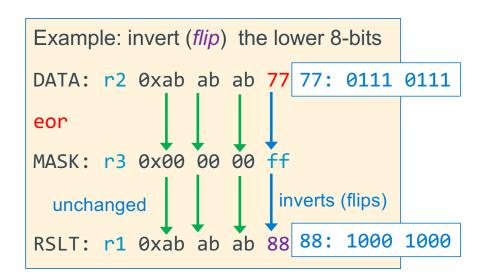
invert (flip) bits "bit toggle" operation

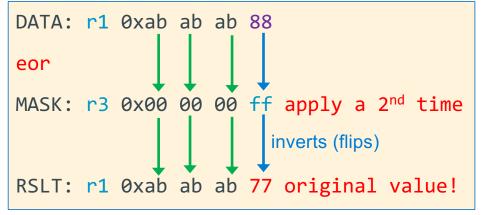
- 1 will flip the bit
- 0 to let a bit through

- Observation: When applied twice, it returns the original value (symmetric encoding)
- With a mask of all 1's is a 1's compliment

```
Example: flip the lower 8-bits eor r1, r2, 0xff
```

```
unsigned int r1, r2;
r1 = r2 ^ 0xff;
```





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Unsigned Integers (positive numbers) with Fixed # of Bits

- 4 bits is 2⁴ = ONLY 16 distinct values
- Modular (C operator: %) or clock math
 - Numbers start at 0 and "wrap around" after 15 and go back to 0
- Keep adding 1

wraps (clockwise)

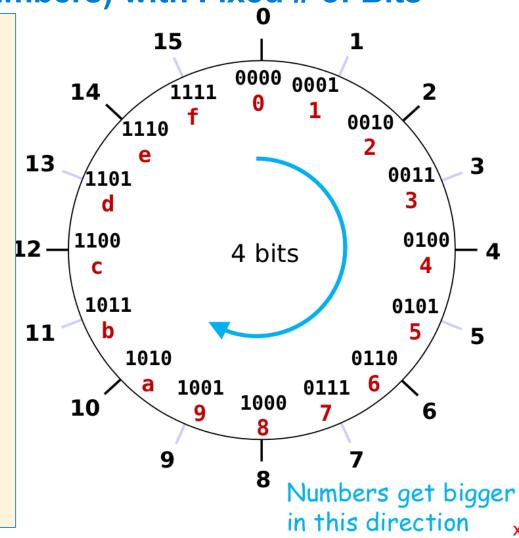
0000 -> 0001 ... -> 1111 -> 0000

Keep subtracting 1

wraps (counter-clockwise)

1111 -> 1110 ... -> 0000 -> 1111

 Addition and subtraction use normal "carry" and "borrow" rules, just operate in binary



Problem: How to Encode **Both** Positive and Negative Integers

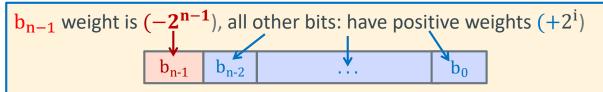
- How do we represent the negative numbers within a fixed number of bits?
 - Allocate some bit patterns to negative and others to positive numbers (and zero)
- 2ⁿ distinct bit patterns to encode positive and negative values
- Unsigned values: $0 \dots 2^n 1 \leftarrow$ -1 comes from counting 0 as a "positive" number
- Signed values: $-2^{n-1} \dots 2^{n-1}-1$ (dividing the range in ~ half including 0)
- On a number line (below): 8-bit integers signed and unsigned (e.g., char in C)



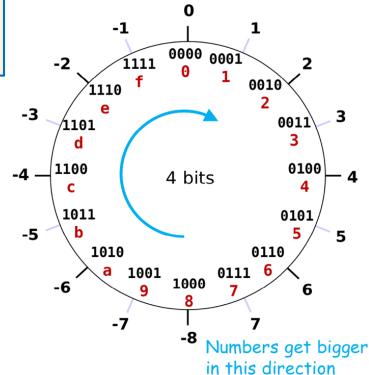
Same "width" (same number of encodings), just shifted in value

Two's Complement: The MSB Has a Negative Weight

$$2's\ Comp = -b_{n-1}2^{n-1} + b_{n-2}2^{n-2} + ... + b_12^1 + b_02^0$$



- 4-bit (w = 4) weight = $-2^{4-1} = -2^3 = -8$
 - 1010_2 unsigned: $1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = 10$
 - 1010_2 two's complement: $-1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = -8 + 2 = -6$
 - -8 in two's complement: $1000_2 = -2^3 + 0 = -8$
 - -1 in two's complement: $1111_2 = -2^3 + (2^3 - 1) = -8 + 7 = -1$

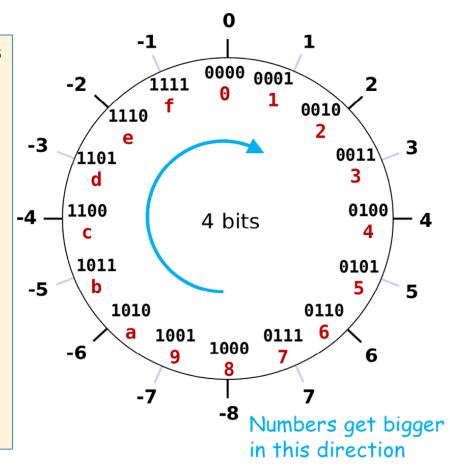


2's Complement Signed Integer Method

- Positive numbers encoded same as unsigned numbers
- All negative values have a one in the leftmost bit
- All positive values have a zero in the leftmost bit
 - This implies that 0 is a positive value
- Only one zero
- For n bits, Number range is $-(2^{n-1})$ to $+(2^{n-1}-1)$
 - Negative values "go 1 further" than the positive values
- Example: the range for 8 bits:

• Example the range for 32 bits:

Arithmetic is the same as with unsigned binary!



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Sign Extension (how type promotion works)

Sometimes you need to work with integers encoded with different number of bits

8 bits (char) -> (16 bits) **short** -> (32 bits) **int**

• Sign extension increases the number of bits: n-bit wide signed integer X, EXPANDS to a wider

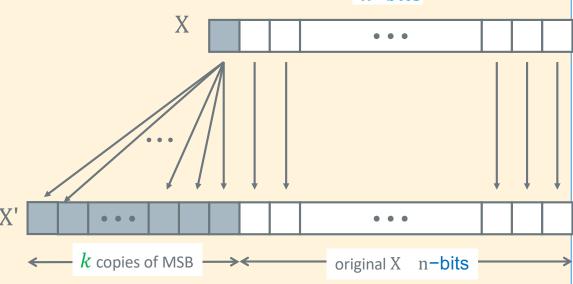
n-bit + k-bit signed integer X' where both have the same value \leftarrow n-bits

Unsigned

Just add leading zeroes to the left side

Two's Complement Signed:

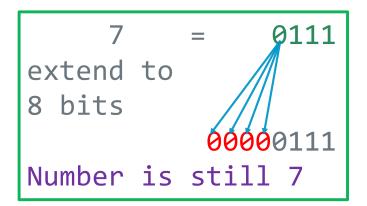
- If positive, add leading zeroes on the left
 - Observe: Positive stay positive
- If negative, add leading ones on the left
 - Observe: Negative stays negative

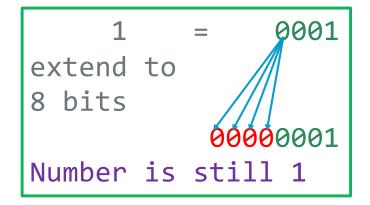


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Example: Two's Complement Sign or bit Extension - 1

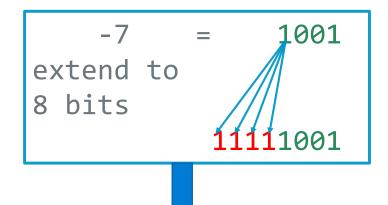
Adding 0's in front of a positive numbers does not change its value





Example: Two's Complement Sign or bit Extension -2

• Adding 1's if front of a negative number does not change its value



```
1001 = -8 + 1 = -7

11111001 =

(-128 + 64 + 32 + 16 + 8) + 1

= -8 + 1 = -7
```

```
7 = 00000111
||||||||
invert = 11111000
add 1 + 1
-7 11111001
```

Sign Extension in C: Type casts

- Convert from smaller to larger integral data types
- C and Java automatically performs sign extension
- Example (on pi-cluster with 32-bit int)

```
#include <stdlib.h>
#include <stdio.h>
int main(void)
{
    signed char c = -1;
    signed int i = c;
    unsigned char d = 1;
    unsigned int j = d;
    printf("c decimal = %hd\n", c);
    printf("c = 0x\%hhx\n", c);
    printf("i decimal = %d\n", i);
    printf("i = 0x%x \n", i);
    printf("\nd decimal = %hd\n", d);
    printf("d = 0x\%hhx\n", d);
    printf("j decimal = %d\n", j);
    printf("j = 0x%x n", j);
    return EXIT_SUCCESS;
```

```
%./a.out
c decimal = -1
c = 0xff
i decimal = -1
i = 0xffffffff

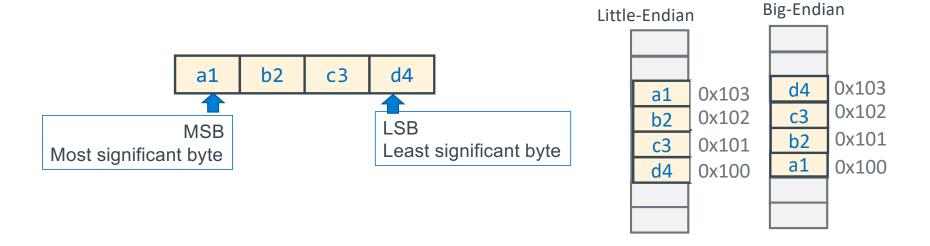
d decimal = 1
d = 0x1
j decimal = 1
j = 0x1
```

Different Type of Numbers each have a Fixed # of Bits Spanning one or more contiguous bytes of memory

C Data Type	AArch-32 contiguous Bytes	Byte 8-bit integer uses 1 byte
char (arm unsigned)	1	7 0
short int	2	Halfantand 4.6 hit into annuar 2 hatas
unsigned short int	2	Half Word 16-bit integer uses 2 bytes
int	4	00000001 0000000
unsigned int	4	15 7 0
long int	4	
long long int	8	most significant bit (largest power of 2) least significant byte
float	4	Wand 22 bit into an anal 4 batas
double	8	Word 32-bit integer uses 4 bytes
long double	8	00000011 00000010 00000001 00000000
pointer *	4	31 0
-		least significant bit (smallest power of 2)
	m	ost significant byte

Byte Ordering of Numbers In Memory: Endianness

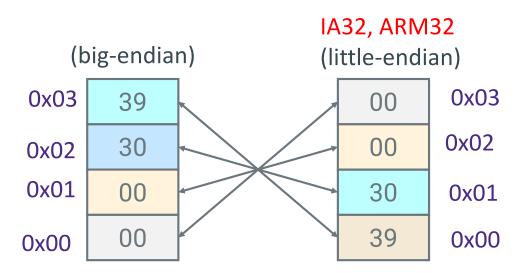
- Two different ways to place multi-byte integers in a byte addressable memory
- Big-endian: Most Significant Byte ("big end") starts at the *lowest (starting)* address
- Little-endian: Least Significant Byte ("little end") starts at the *lowest (starting)* address
- Example: 32-bit integer with 4-byte data



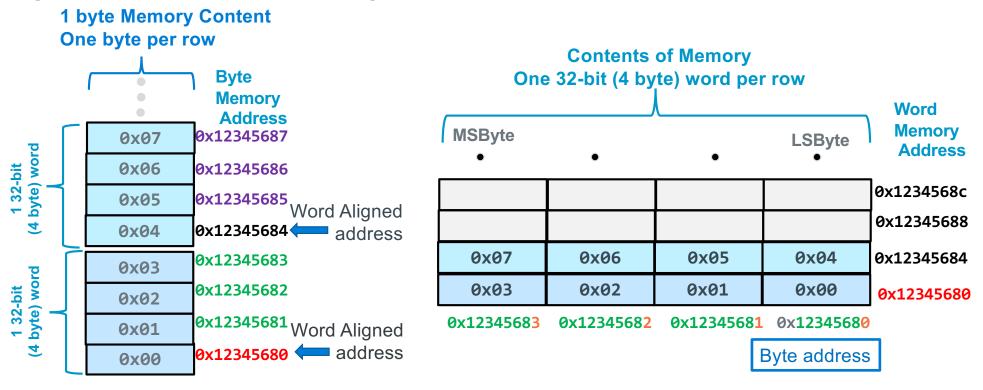
Byte Ordering Example

```
Decimal: 12345
Binary: 0011 0000 0011 1001
Hex: 3 0 3 9
```

```
int x = 12345;
// or x = 0x00003039; // show all 32 bits
```

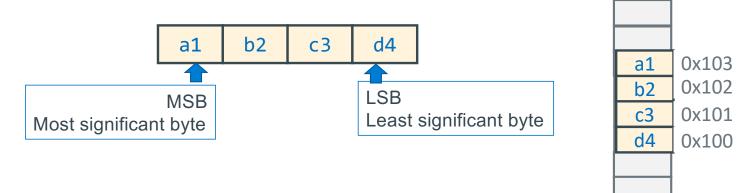


Byte Addressable Memory Shown as 32-bit words



Observation
32-bit aligned addresses
rightmost 2 bits of the address are always 0

Using pointers to examine byte order (on pi-cluster)_{Little-Endian}



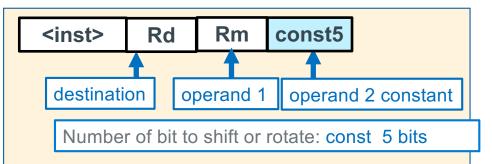
```
#include <stdio.h>
#include <stdlib.h>
#define SZ 2
int main()
{
    unsigned int foo[SZ] = {0x11223344, 0xaabbccdd};
    unsigned char *chptr = (unsigned char *)foo;

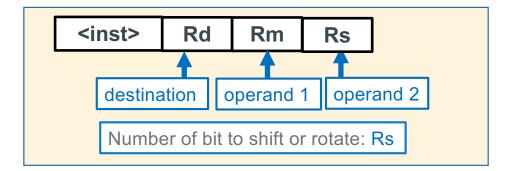
    // print from MSB to LSB - high to low memory)
    for (int i = sizeof(foo)-1; i >= 0; i--)
        printf("byte %d: %x\n", i, *(chptr + i));

    return EXIT_SUCCESS;
}
```

\$./a.out		-
byte 7: aa	0xaa	0x12345687
byte 6: bb	0xbb	0x12345686
byte 5: cc	0хсс	0x12345685
byte 4: dd	0xdd	0x12345684
byte 3: 11	0x11	0x12345683
byte 2: 22	0x22	0x12345682
byte 1: 33	0x33	0x12345681
byte 0: 44	0x44	0x12345680

Shift and Rotate Instructions





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Instruction	Syntax	Operation	Notes	Diagram
Logical Shift Left int x; or unsigned int x x << n;		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Zero fills shift: 0 - 31	C b31 b0 0
Logical Shift Right unsigned int x; x >> n;	- "	$\begin{array}{c} R_d \; \leftarrow \; R_m \; \; >> \; \; const5 \\ R_d \; \leftarrow \; R_m \; \; >> \; \; R_s \end{array}$	Zero fills shift: 1 - 32	0
Arithmetic Shift Right int x; x >> n;	asr R_d , R_m , const5 asr R_d , R_m , R_s	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Sign extends shift: 1 - 32	b31
Rotate Right unsigned int x; x = (x>>n) (x<<(32-n));		$\begin{array}{c} R_d \leftarrow R_m \text{ror} \textit{const5} \\ R_d \leftarrow R_m \text{ror} R_s \end{array}$	right rotate rot: 0 - 31	b31 b0

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Shift Operations in C

- n is number of bits to shift a variable x of width w bits
- Shifts by n < 0 or $n \ge w$ are undefined
- Left shift (x << N) Multiplies by 2^N
 - Shift N bits left, Fill with 0s on right
- In C: behavior of >> is determined by compiler
 - gcc: it depends on data type of x (signed/unsigned)
- Right shift (x >> N) Divides by 2^N
 - Logical shift (for unsigned variables)
 - Shift N bits right, Fill with 0s on left
 - Arithmetic shift (for signed variables) Sign Extension
 - Shift N bits right while <u>Replicating</u> the most significant bit on left
 - Maintains sign of x
- In Java: logical shift is >>> and arithmetic shift is >>>







X

Arithmetic Shift Right Example: Testing Sign

```
asr r2, r0, 31

r0 0xab ab ab 77 // bit 31 is a one
r2 0xff ff ff ff // see the sign extend

b0 C
```

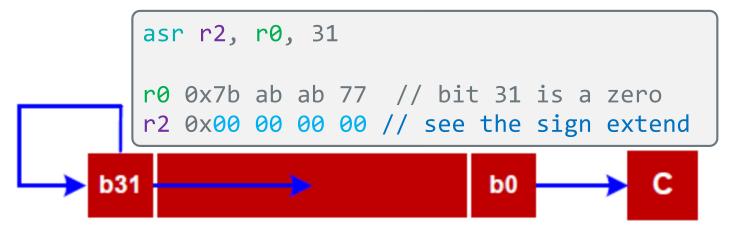
```
int i;
//code
if ((i>>31) == -1) {
   // code neg #
}
```

```
-1 if r0 negative

asr r2, r0, 31
cmp r2, -1
bne .Lendif
//code neg #
.Lendif:
```

Test for sign

Arithmetic Shift Right Example: Testing Slgn



```
int i;
//code
if ((i>>31) == 0) {
    // code pos #
}
```

Test for sign 0 if r0 positive

```
asr r2, r0, 31
cmp r2, 0
bne .Lendif
//code positive #
.Lendif:
```

Logical Shift & Rotate Operations



lsr r2, r0, 8
r0 0xab ab ab 77
r2 0x00 ab ab ab

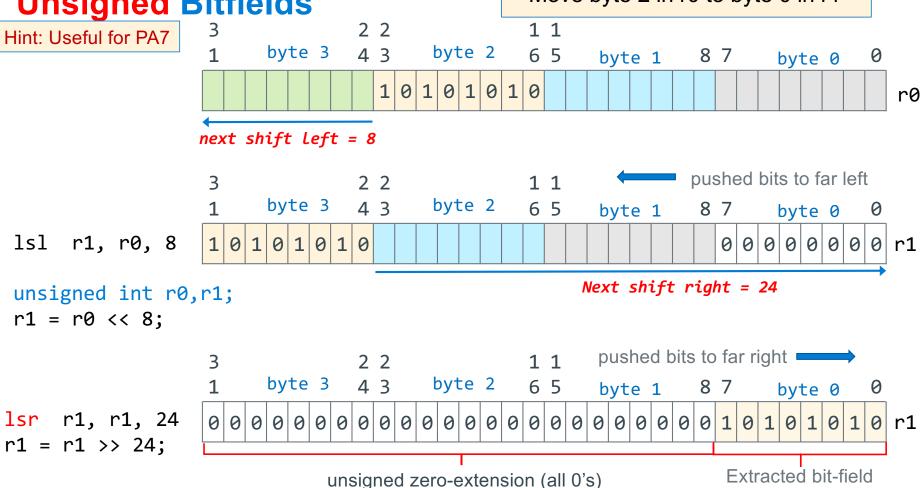


```
1sl r2, r0, 8
r0 0xab ab ab 77
r2 0xab ab 77 00
```

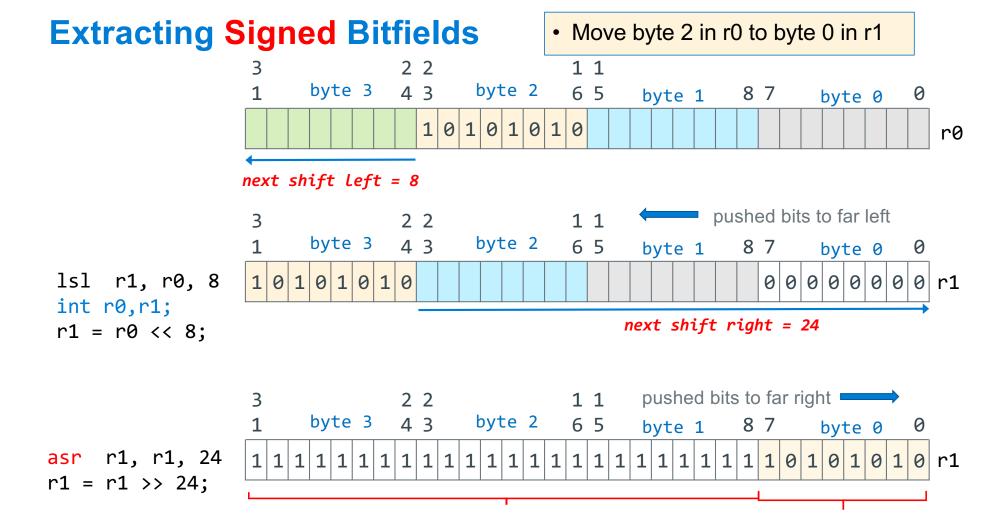


Extracting/Isolating Unsigned BitfieldsHint: Useful for PA7

• Move byte 2 in r0 to byte 0 in r1



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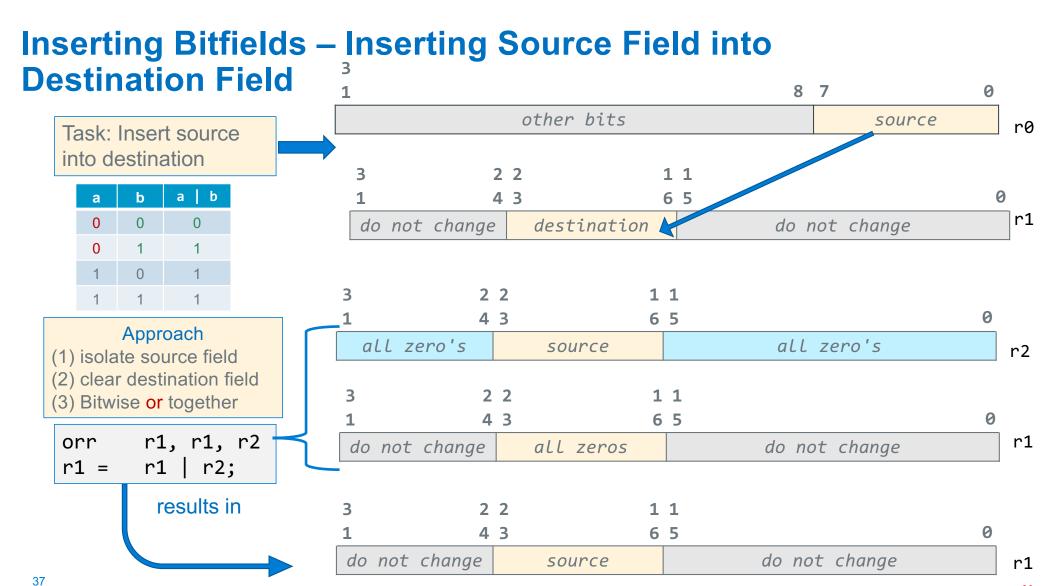


signed extend (all 1's)

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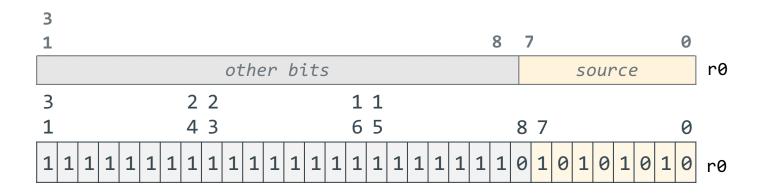
Extracted

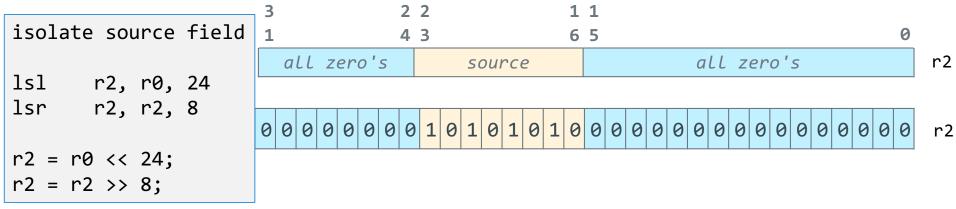
bit-field



X

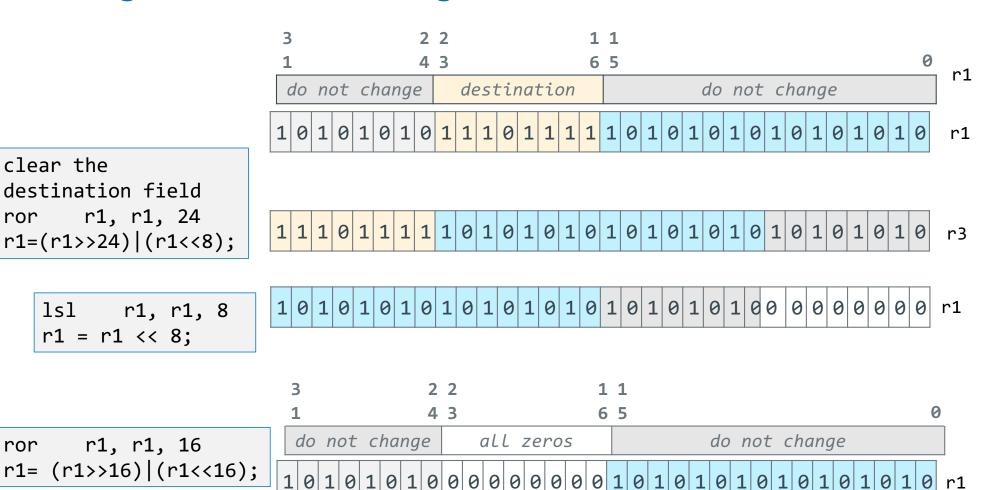
Inserting Bitfields – Isolating the Source Field





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Inserting Bitfields – Clearing the Destination Field



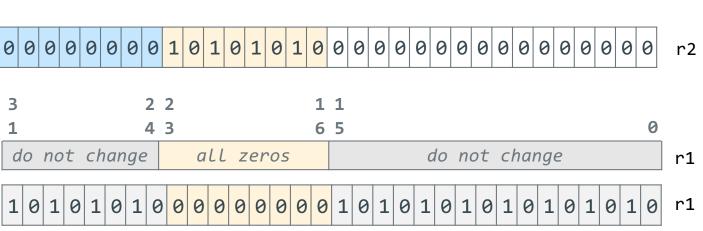
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Inserting Bitfields – Combining Isolated Source and Cleared Destination

isolated source

3 2 2 1 1 1 4 3 6 5 0 all zero's source all zero's

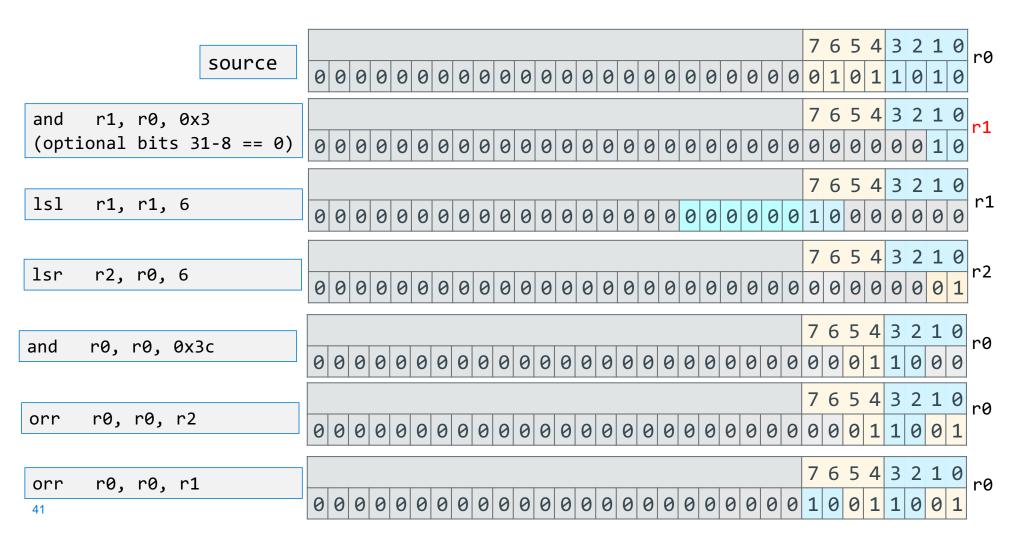
field cleared in destination



inserted field
orr r1, r1, r0
r1 = r1 | r0;

r2

Example: Swapping bits7,6 with bits 1,0



Masking Summary

Select a field: Use and with a mask of one's surrounded by zero's to select the bits that have a 1 in the mask, all other bits will be set to zero selects this field when used with and

0 0 0 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 selection mask

Clear a field: Use and with a mask of zero's surrounded by one's to select the bits that have a 1 in the mask, all other bits will be set to zero clears this field when used with and

Isolate a field: Use lsr, lsl, rot to get a field surrounded by zeros

Insert a field: Use orr with fields surrounded by zeros

0 0 0 0 0 0 0	source	0 0 0 0 0 0 0 0 0 0 0 0 0 0
Keep these bits	00000000	Keep these bits