



Thursday office hours moved to Section B ZOOM Midterm Review Thursday 7:30 PM – 8:30 PM (My office hours zoom #) (see canvas for number)

Accessing members of a struct

```
High address
   struct date {      // defining struct type
                                                                            day
                                                                                   10
       int month; // member month
       int day; // member date
                                                                           month
                                                                 quarter[4]
   };
                                                                            day
                                                                                   8
                                                                                   7
                                                                           month
                                                                 quarter[3]
                                                                            dav
                                                                                   6

    You can create an array of structs and initialize them

                                                                 quarter[2]
                                                                           month
  struct date quarter[] =
                                                                            day
                                                                                   4
                 \{ \{1,2\}, \{3,4\}, \{5,6\}, \{7,8\}, \{9,10\} \};
                                                                           month
                                                                 quarter[1]
  int cnt = sizeof(quarter)/sizeof(*quarter); // = 5
                                                                            day
                                                                                   2
  quarter[0].month = 1;
                                                                           month
                                                                 quarter[0]
  quarter[0].day = 2;
                                                                          Low address
```

Accessing members of a struct

```
day
                                                         quarter[2] month
                                                  ptr
                                                                   day
                                                                         21
                                                                  month
                                                         quarter[1]
                                                                   day
struct date quarter[3];
struct date *ptr;
                                                                  month
                                                         quarter[0]
ptr = quarter + 1;  // array name = address
ptr->month = 2;
ptr->day = 21; // or (*ptr).day = 21;
(ptr-1)->month = 1; // or (*(ptr-1)).month = 4;
(ptr-1)->day = 7;
(++ptr)->month = 3;
ptr->day = 5;
```

Typedef usage with Struct – Another Style Conflict

- Typedef is a way to create an alias for another data type (not limited to just structs)
 typedef <data type> <alias>;
 - After typedef, the alias can be used interchangeably with the original data type
 - e.g., typedef unsigned long int size_t;
- Some claim typedefs are easier to understand than tagged struct variables, others not
 - typedef with structs are not allowed in the cse30 style guidelines (Linux kernel standards)

```
struct nm {
   /* fields */
};
typedef struct nm item;

item n1;
struct nm n2;
item *ptr;
struct nm *ptr2;
```

```
typedef struct name2_s {
    int a;
    int b;
} name2_s;

name2_s var2;
name2_s *ptr2;
```

```
typedef struct {
    int a;
    int b;
} pair;

pair var3;
pair *ptr3;
```

Assigning Structs in an expression

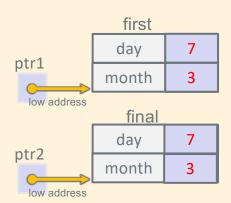
- You can assign (copy) each member value of a struct from a struct of the same type
 Performance Caution: this copies the contents of each struct member during execution
- Individual members can also be copied

```
struct date first = {1, 1};
struct date final = {.day= 31, .month= 12};

struct date *pt1 = &first;
struct date *pt2 = &final;

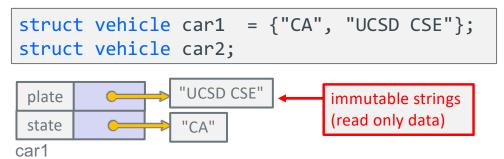
final.day = first.day; // both day are 1
final = first; // copies whole struct

pt2->month = 3;
*pt1 = *pt2; // copies whole struct
pt2->day = 7;
pt1->day = pt2->day; // both days are now 7
```

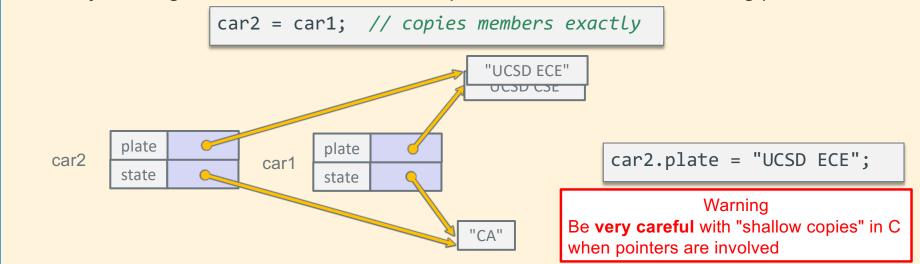


Caution: Assignment is a Shallow Copy of struct members

```
struct vehicle {
  char *state;
  char *plate;
};
```



• When you assign one struct to another, it copies member contents including pointer values!



Struct: Copy and Member Pointers --- "Deep Copy"

```
struct vehicle {
                                struct vehicle car1 = {"CA", "UCSD CSE"};
         char *state;
                                struct vehicle car2;
        char *plate;
      };
                                  mutable strings (heap memory)

    Use strdup() to copy the strings

                                                                immutable strings (read-only data)
                                             "UCS
                                                  "UCSD ECE"
                           "UCSD CSE"
                                                         car2.plate = strdup(car1.plate);
       plate
                            plate
                                                        car2.state = strdup(car1.state);
                      car1
car2
       state
                            state
                                                        car1.plate = "UCSD ECE";
                                            "CA"
                         "CA"
```

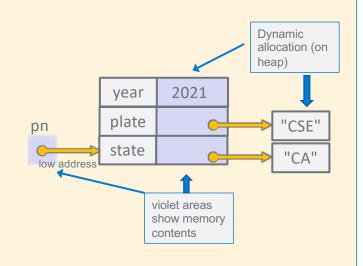
Deep Copies of Structs

• Must first allocate space to be pointed at by member pointers independently (they are not part of the struct, only the pointers are) then copy what they point at

```
struct vehicle {
  char *state;
  char *plate;
  int year;
};
struct vehicle car1 = {"CA", "CSE", 2021};

struct vehicle *pn = malloc(sizeof(*pn));
// check if malloc() failed not shown
```

```
pn->state = strdup(car1.state);
pn->plate = strdup(car1.plate);
pn->year = car1.year;
```



Nested Structs

• Structs like any other variable can be a member of a struct, this is called a nested struct

```
struct date {
                                                                day
                                                                      24
                      struct person {
                                                         bday
    int month;
                          char *name;
                                                              month
                                                                       1
    int day;
                          struct date bday;
                                                                              "Joe"
                                                        name
};
                     };
       struct person first;
       struct person *ptr;
       ptr = &first;
      first.name = "Sam";  // immutable string
       first.name = (char []) {"Joe"}; // mutable string, lost address to Sam
       first.bday.month = 1;
       first.bday.day = 24;
       // below is the same as above
       ptr->bday.month = 1;
       ptr->bday.day = 24;
```

Comparing Two Structs

 You cannot compare entire structs, you must compare them one member at a time struct vehicle { doors doors 2

```
char *state;
                       plate
                                                 plate
                                       "UCSD"
                                                                   "abc"
  char *plate;
                       state
                                                 state
  int doors;
                                       "CA"
                                                                  "NY"
                     car1
                                                car2
};
    struct vehicle car1 = {"CA", "UCSD", 4};
    struct vehicle car2 = { (char []) {"NY"}, (char []) {"abc"}, 2};
          if ((strcmp(car1.state, car2.state) == 0) &&
              (strcmp(car1.plate, car2.plate) == 0) &&
              (car1.doors == car2.doors)) {
              printf("Same\n");
          } else {
              printf("Different\n");
```

Struct Arrays: Dynamic Allocation

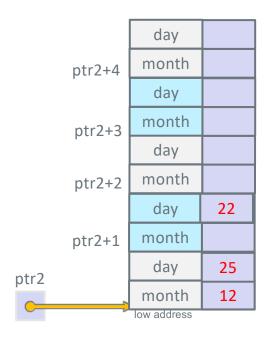
```
#define HOLIDAY 5
struct date *pt1 = malloc(sizeof(*pt1));
struct date *pt2 = malloc(sizeof(*pt2) * HOLIDAY);
```

```
ptr1 day 21 month 2
```

```
(*pt1).month = 2;
(*pt1).day = 21;

pt2->month = 12;
pt2->day = 25;
(pt2+1)->day = 22; //or (*(pt2+1)).month

free(pt1);
pt1 = NULL;
free(pt2);
pt2 = NULL;
```

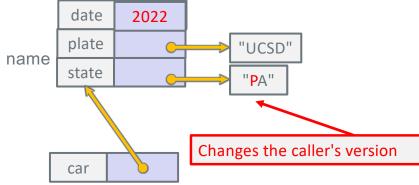


Formal Parameter structs: contents set with shallow copies!

- WARNING: When you pass a struct, you pass a copy of all the struct members
 - This is a shallow copy (shallow copy so if you have members that are pointers watch out)
- More often code will pass the pointer to a struct to avoid the copy costs
 - Be careful and not modify what the pointer points to (unless it is an output parameter)
- Tradeoffs:
 - Passing a pointer is cheaper and takes less space unless struct is small
 - Member access cost: indirect accesses through pointers to a struct member may be a bit more expensive and might be harder for compiler to optimize
 - For small structs like a struct date passing a copy is fine
 - For large structs always use pointers (arrays of struct, pass a pointer)
- For me, I always pass pointers to structs as parameters regardless of size

Struct Function Parameters – Be Careful it is not like arrays

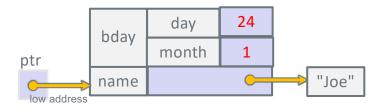
```
void change1(struct vehicle car)
                                               date
                                                      2021
                                               plate
                                                                 "UCSD"
                                        name
    car.date = 2022;  //w oops!
                                               state
                                                                 "PA"
   *(car.state) = "P";
                                                      2022
                                               date
                                               plate
change1(name);
                                        car
                                               state
                Changes the parameter copy
void change2(struct vehicle *car)
                                              date
                                                     2022
                                              plate
                                                                "UCSD"
    car->date = 2022;
                                        name
   *(car->state) = "P";
                                              state
```



Struct as an Output Parameter: Deep Copy Example

```
struct date {
    int month;
    int day;
};
```

```
struct person {
    char *name;
    struct date bday;
};
```



```
int fill(struct person *ptr, char *name, int month, int day)
{
   ptr->bday.month = month;
   ptr->bday.day = day;
   if ((ptr->name = strdup(name)) == NULL)
        return -1;
   return 0;
}
...----calling function ------
   struct person first;
   if (fill(&first, "Joe", 1, 24) == 0)
        printf("%s %d %d\n", first.name, first.bday.month, first.bday.day);
...
```

Review: Singly Linked Linked List - 1



- Is a **linear collection of nodes** whose order is not specified by their relative location in memory, like an array
- Each node consists of a payload and a pointer to the next node in the list
 - The pointer in the last node in the list is NULL (or 0)
 - The head pointer points at the first node in the list (the head is not part of the list)
- Nodes are easy to insert and delete from any position without having to re-organize the entire data structure
- Advantages of a linked list:
 - Length can easily be changed (expand and contract) at execution time
 - Length does not need to be known in advance (like at compile time)
 - List can continue to expand while there is memory available

Review: Singly Linked Linked List - 2



- Memory for each node is typically allocated dynamically at execution time (i.e., using heap memory – malloc() etc.) when a new node is added to the list
- Memory for each node may be freed at execution time, using free() when a node is removed from the list
- Unlike arrays, linked list nodes are usually not arranged (located) sequentially in adjacent memory locations
- No fast and convenient way to "jump" to any specific node.
- Usually the list must be traversed (walked) from the head to locate if a specific payload is stored in any node
- Obviously, the cost in traversing a linked list is O(n)

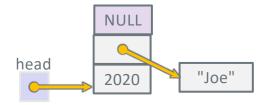
Linked List Using Self-Referential Structs

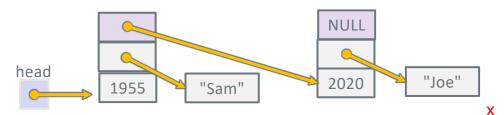
 A self-referential struct is a struct that has one or more members that are pointers to a struct variable of the same type struct node { next O int date; Self-referential member date ⇒struct node *next; | }; points to same type – itself Example: struct node2 { int month; int day; x.month = 1;next struct node2 *next; x.day = 31;day 31 x.next = NULL; month struct node2 x; x low memory struct node2 *head head = &x;

Creating a Node & Inserting it at the Front of the List

```
// create node; insert at front when passed head
                                                                 struct node {
struct node *
                                                                    int vear;
creatNode(int year, char *name, struct node *link)
                                                                   char *name;
{
                                                                    struct node *next;
    struct node *ptr = malloc(sizeof(*ptr));
    if (ptr != NULL) {
        if ((ptr->name = strdup(name)) == NULL) {
            free(ptr);
                                                 // calling function body
           return NULL;
                                                 struct node *head = NULL; // insert at front
                                                 struct node *ptr;
        ptr->year = year;
                                                 if ((ptr = creatNode(2020, "Joe", head)) != NULL) {
        ptr->next = link;
                                                      head = ptr; // error handling not shown
    return ptr;
                    Never use head here!
                                                 if ((ptr = creatNode(1955, "Sam", head)) != NULL) {
                    you can lose your linked list
                                                      head = ptr; // error handling not shown
                    if creatNode() fails!
                                                 }
```







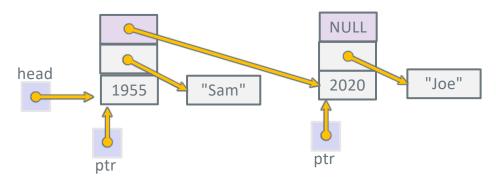
Creating a Node & Inserting it at the End of the List

```
head
// create a node and insert at the end of the list
                                                                     NULL
struct node *
insertEnd(int year, char *name, struct node *head)
{
                                                                     NULL
    struct node *ptr = head;
    struct node *prev = NULL; // base case
                                                            head
                                                                               "Joe"
                                                                     2020
    struct node *new;
    if ((new = creatNode(year, name, NULL)) == NULL)
         return NULL;
                                                                                 NULL
    while (ptr != NULL) {
         prev = ptr;
                                                                                           "Sam"
                                                                                 1955
         ptr = ptr->next;
                                                           lhead
                                                                               "Joe"
                                                                     2020
    if (prev == NULL)
         return new;
                                   struct node *head = NULL; // insert at end
    prev->next = new;
                                   struct node *ptr;
    return head;
                                   if ((ptr = insertEnd(2020, "Joe", head)) != NULL)
}
                                       head = ptr;
                                   if ((ptr = insertEnd(1955, "Sam", head)) != NULL)
                                       head = ptr;
20
```

"Dumping" the Linked List

"walk the list from head to tail"

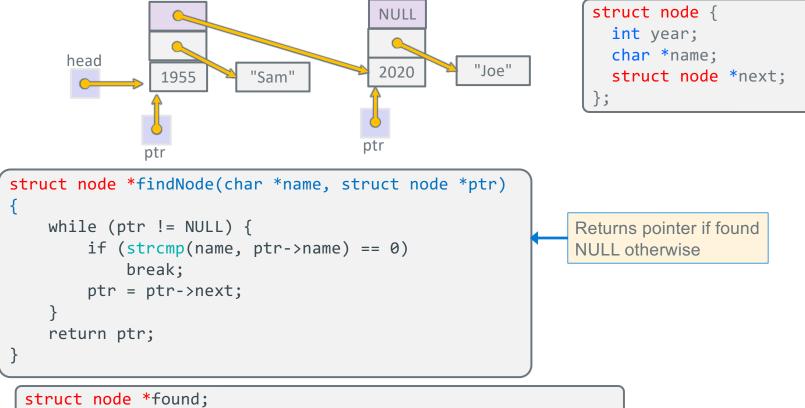
```
struct node {
  int year;
  char *name;
  struct node *next;
};
```





```
struct node *head;
struct node *ptr;
...
printf("\nDumping All Data\n");
ptr = head;
while (ptr != NULL) {
   printf("year: %d name: %s\n", ptr->year, ptr->name);
   ptr = ptr->next;
}
Dumping All Data
   year: 1955 name: Sam
   year: 2020 name: Joe
```

Finding A Node Containing a Specific Payload Value



```
struct node *found;
if ((found = findNode("Joe", head)) != NULL)
    printf("year: %d name: %s\n", found->year, found->name);
```

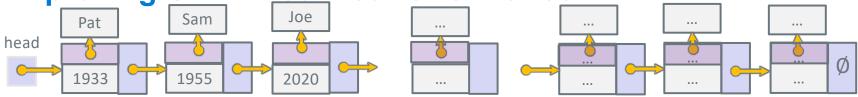
Deleting a Node in a Linked List

```
// returns head pointer; may have changed...
struct node *deleteNode(int name, struct node *head)
   struct node *ptr = head;
   struct node *prev = NULL;
   while (ptr != NULL) {
        if (strcmp(name, ptr->name) == 0)
            break;
        prev = ptr;
        ptr = ptr->next;
   if (ptr == NULL) // not found return head
        return head;
   if (ptr == head) // remove first node new head
        head = ptr->next;
   else
        prev->next = ptr->next; // remove not head
   free(ptr->name); // free strdup() space
   free(ptr);
   return head;
```

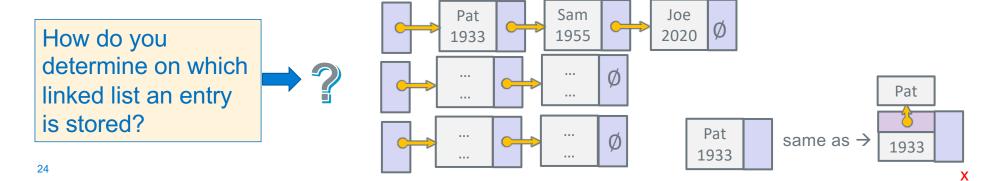
```
NULL
head
                                              "Joe"
                                    2020
           1955
                     "Sam"
          NULL
head
                    "Sam"
           1955
lhead
 NULL
    struct node *head = NULL;
```

```
struct node *head = NULL;
head = deleteNode("Joe", head);
head = deleteNode("Sam", head);
```

Improving On Linked List Performance

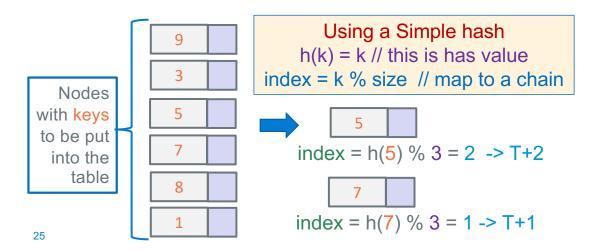


- When linked lists get long, the cost of finding an entry continues to increase O(n)
- How to improve search time?
- Break the single linked list into multiple shorter length linked lists
 - Shorter lists are faster to search
- Requires a function that takes a lookup key and selects just one of the shortened lists

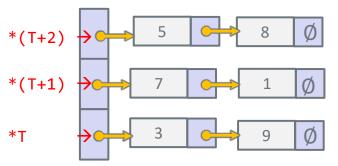


Hashing

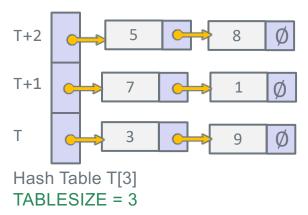
- Hash table is an array of pointers to the head of different linked lists (called hash chains)
- Each data item must have a unique key that identifies it (e.g., auto license plate)
 - h(k) is the hash value of key k to encode the key k into an integer
- Use the Hash value to map to one entry in the hash table T[] of size TABLESIZE
 - Index = h(k) % TABLESIZE (mod operator % maps a keys hash value to table index)
- Keys that hash to the same array index (collide) are put on a linked list
- After hashing a key, you then traverse the selected linked list to find the entry



Hash Table T[3] of linked list head pointers TABLESIZE = 3



Hash Table With Collision Chaining (multiple linked lists)



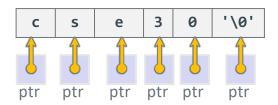
- Make TABLESIZE prime as keys are typically not randomly distributed, and have a pattern
 - Mostly even, mostly multiples of 10, etc.
 - In general: mostly multiples of some k
- If k is a factor of TABLESIZE, then only (TABLESIZE/k) slots will ever be used!
- 1. Calculate index i = hash(key) % TABLESIZE
- 2. Go to array element i, i.e., T+i that contains the head pointer for collision chain
- 3. Walk the linked list for element, add element, remove element, etc. from the linked list
- 4. New items added to the hash table are typically added at the front or at the end of the *collision* chain linked list (when multiple keys hash to same index .. they collide)
- Hash arrays need an index number to select a chain, so if we have a string, we must first convert to a number

Simple 32-bit String Hash Function in C (djb2)

```
uint32_t hash(char *str)
{
    uint32_t hash = 0U;
    uint32_t c;

    while ((c = (unsigned char)*str++) != '\0')
        hash = c + (hash << 6) + (hash << 16) - hash;
    return hash;
}</pre>
```

Signed Data types	Unsigned Data types	Exact Size
int32_t	uint32_t	32 bits (4 bytes)

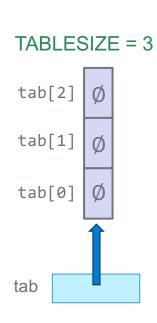


- Many different algorithms for string hash function (Dan Berman's djb2 above)
 - << is the left bit shift operator (later in course)</p>
- Fast to compute, has a reasonable key distribution for short 8-bit ASCII strings into 32-bit unsigned ints

Allocating the Hash Table (collision chain head pointers) Good use for calloc()

```
#define TBSZ 3
int main(void)
{
    struct node *ptr;
    struct node **tab; // pointer to hashtable
    uint32_t index;

    if ((tab = calloc(TBSZ, sizeof(*tab))) == NULL) {
        fprintf(stderr,"Cannot allocate hash
    table\n");
        return EXIT_FAILURE;
    }
// continued on next slide
```

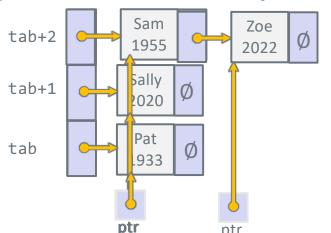


Inserting Nodes into the Hash Table (at the end)

```
struct node {
#define TBSZ 3
                                                                        int year;
unit32 t index;
                                                                        char *name;
                                                                        struct node *next;
index = hash("Pat") % TBSZ;
                                                                     };
if ((ptr = insertEnd(1933, "Pat", *(tab + index))) != NULL)
    *(tab + index) = ptr;
                                                                              Sam
                                                                                          Zoe
                                                                 tab+2
index = hash("Sam") % TBSZ;
                                                                              1955
                                                                                          2022
if ((ptr = insertEnd(1955, "Sam", *(tab + index))) != NULL)
    *(tab + index) = ptr;
                                                                              Sally
                                                                 tab+1
                                                                              2020
index = hash("Sally") % TBSZ;
if ((ptr = insertEnd(2020, "Sally", *(tab + index))) != NULL)
                                                                              Pat
                                                                 tab
                                                                             1933
    *(tab + index) = ptr;
index = hash("Zoe") % TBSZ;
if ((ptr = insertEnd(2022, "Zoe", *(tab + index))) != NULL)
    *(tab + index) = ptr;
                                                                        Notice
```

Substitute **createNode()** for **insertEnd()** to insert nodes at the **front** of the collision chain **instead** of at the **end** of the collision chain

"Dumping" the Hash Table (traversing all Nodes)

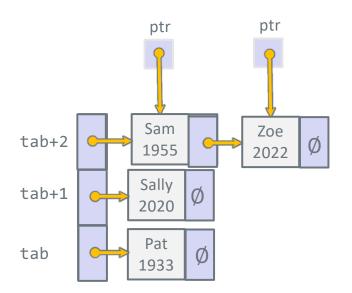


```
Dumping All Data chain: 0
Year: 1933 Name: Pat chain: 1
Year: 2020 Name: Sally chain: 2
Year: 1955 Name: Sam
Year: 2022 Name: Zoe
```

```
printf("\nDumping All Data\n");
for (index = 0U; index < TBSZ; index++) {
   ptr = *(tab + index);
   printf("chain: %d\n", index);

   while (ptr != NULL) {
      printf("Year: %d Name: %s\n", ptr->year, ptr->name);
      ptr = ptr->next;
   }
}
```

Finding a Node with a Specific Payload Value



```
// same routine as shown in a previous slide
struct node *findNode(char *name, struct node *ptr)
{
    while (ptr != NULL) {
        if (strcmp(name, ptr->name) == 0)
            break;
        ptr = ptr->next;
    }
    return ptr;
}
```

```
index = hash("Zoe") % TBSZ;
if ((ptr = findNode("Zoe", *(tab + index))) != NULL)
    printf("Found Year: %d name: %s\n", ptr->year, ptr->name);
else
    printf("Not Found Zoe\n");
```

Positive Number (unsigned) in 4 bits

- Real hardware has a fixed number of bits to store numbers (pi-cluster is 32 bits)
- There are only 2ⁿ distinct values in n bits
- This limits the range of positive number to be 0 (unsigned min) to 2^n 1 (unsigned max)

Hex digit	0x0	0x1	0x2	0x3	0x4	0x5	0x6	0x7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0b0000	0b0001	<mark>0</mark> b0010	0b0011	<mark>0</mark> b0100	0b0101	0b0110	0b0111

umin

Hex digit	0x8	0x9	0xa	0xb	0хс	0xd	0xe	0xf
Decimal value	8	9	10	11	12	13	14	15
Binary value	0b1000	0b1001	0b1010	0b1011	0b1100	0b1101	0b1110	0b1111

umax

Unsigned Integers (positive numbers) with Fixed # of Bits

- 4 bits is 2⁴ = ONLY 16 distinct values
- Modular (C operator: %) or clock math
 - Numbers start at 0 and "wrap around" after 15 and go back to 0
- Keep adding 1

wraps (clockwise)

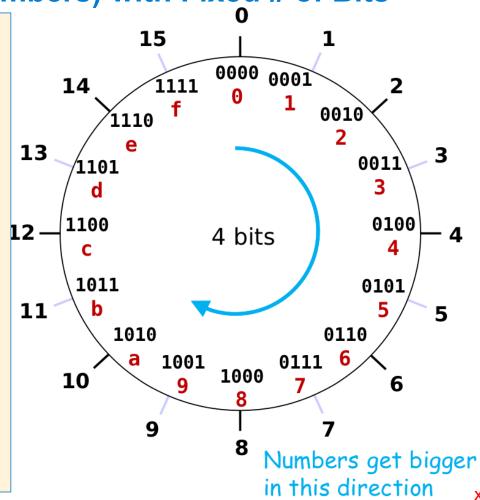
0000 -> 0001 ... -> 1111 -> 0000

Keep subtracting 1

wraps (counter-clockwise)

1111 -> 1110 ... -> 0000 -> 1111

 Addition and subtraction use normal "carry" and "borrow" rules, just operate in binary



Unsigned Binary Number: Addition in 4 bits

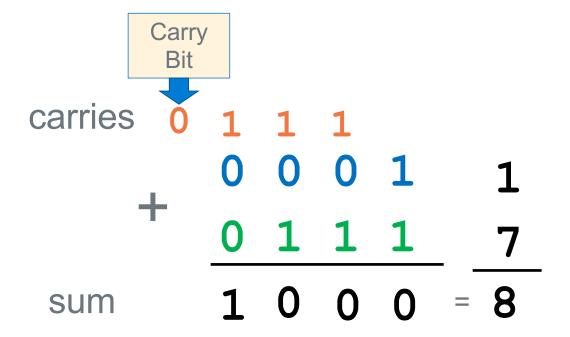
Be Aware in Binary

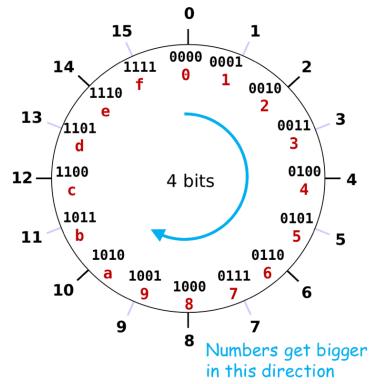
$$1 + 1 = 10$$

 $1 + 1 + 1 = 11$

base 10:
$$(1 + 1 = 2)$$

base 10: $(1 + 1 + 1 = 3)$





Unsigned Binary Number: Subtraction in 4 bits

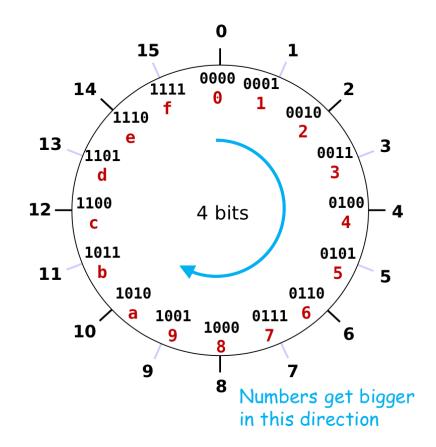
Be Aware in Binary

$$1 - 1 = 0$$

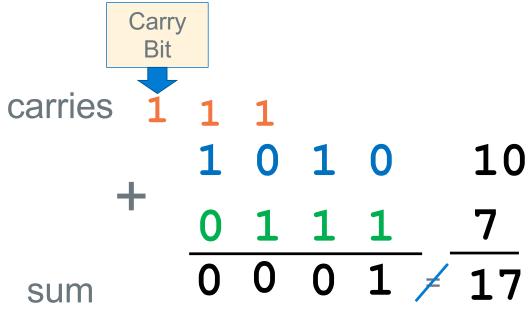
 $10 - 1 = 1$

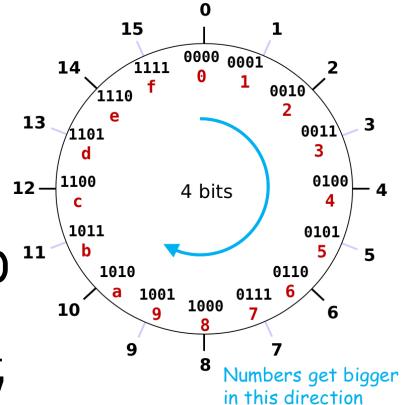
base 10: (1 - 1 = 0)base 10: (2 - 1 = 1)

Borrows



Unsigned Binary Number: Addition in 4 bits – Overflow!





Unsigned Binary Number: Subtraction in 4 bits – Overflow!

Be Aware in Binary

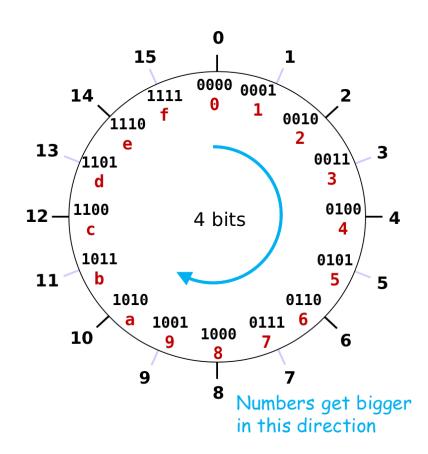
$$1 - 1 = 0$$

 $10 - 1 = 1$

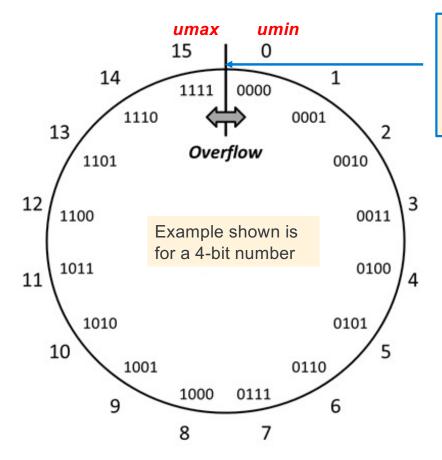
base 10:
$$(1 - 1 = 0)$$

base 10: $(2 - 1 = 1)$

Borrows



Overflow: Going Past the Boundary Between umax and umin



Overflow with unsigned numbers:

Occurs when an arithmetic result (from addition or subtraction for example) is is more than **min** or **max** limits

C (and Java) ignore overflow exceptions

 You end up with a bad value in your program and absolutely no warning or indication... happy debugging!....

Problem: How to Encode **Both Positive and Negative Integers**

- How do we represent the negative numbers within a fixed number of bits?
 - Allocate some bit patterns to negative and others to positive numbers (and zero)
- 2ⁿ distinct bit patterns to encode positive and negative values
- Unsigned values: $0 \dots 2^n 1 \leftarrow$ -1 comes from counting 0 as a "positive" number
- Signed values: $-2^{n-1} \dots 2^{n-1}-1$ (dividing the range in ~ half including 0)
- On a number line (below): 8-bit integers signed and unsigned (e.g., char in C)



Same "width" (same number of encodings), just shifted in value

Negative Integer Numbers: Sign + Magnitude Method

sign bit Remaining bits

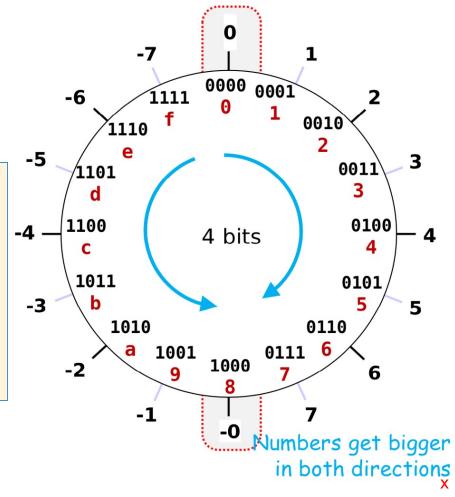
MSB

these numbers show bit position boundaries

0

Note: The second of the

- Use the Most Significant Bit as a sign bit
 - 0 as the MSB represents positive numbers
 - 1 as the MSB represents negative numbers
- Two (oops) representations for zero: 0000, 1000
- Tricky Math (must handle sign bit independently)
 - Positive and Negatives "increment" (+1) in the opposite directions!

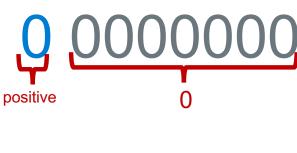


Signed Magnitude Examples (Sign bit is always MSB)





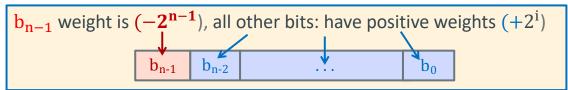
Examples (4 bits):				
1 000 = -0	0000 = 0			
1 001 = -1	0 001 = 1			
1 010 = -2	0010 = 2			
1 011 = -3	0 011 = 3			
1 100 = -4	0100 = 4			
1 101 = -5	0 101 = 5			
1 110 = -6	0 110 = 6			
1 111 = -7	0 111 = 7			



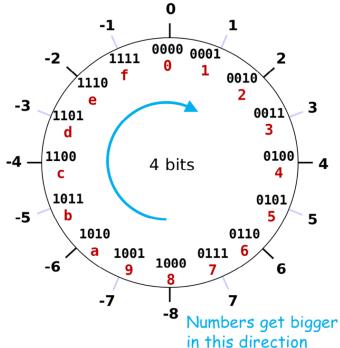


Two's Complement: The MSB Has a Negative Weight

$$2's\ Comp = -b_{n-1}2^{n-1} + b_{n-2}2^{n-2} + ... + b_12^1 + b_02^0$$



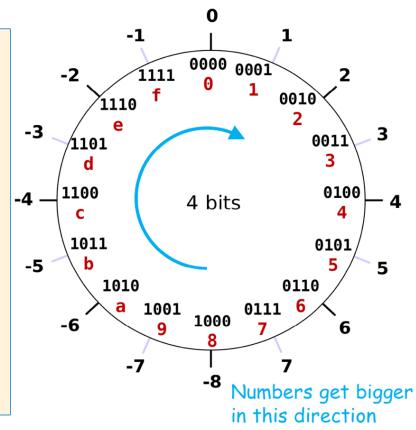
- 4-bit (w = 4) weight = $-2^{4-1} = -2^3 = -8$
 - 1010_2 unsigned: $1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = 10$
 - 1010_2 two's complement: $-1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = -8 + 2 = -6$
 - -8 in two's complement: $1000_2 = -2^3 + 0 = -8$
 - -1 in two's complement: $1111_2 = -2^3 + (2^3 - 1) = -8 + 7 = -1$



2's Complement Signed Integer Method

- Positive numbers encoded same as unsigned numbers
- All negative values have a one in the leftmost bit
- All positive values have a zero in the leftmost bit
 - This implies that 0 is a positive value
- Only one zero
- For n bits, Number range is $-(2^{n-1})$ to $+(2^{n-1}-1)$
 - Negative values "go 1 further" than the positive values
- Example: the range for 8 bits:

- Example the range for 32 bits:
 - **-2147483648** .. 0, .. **+2147483647**
- Arithmetic is the same as with unsigned binary!



Summary: Min, Max Values: Unsigned and Two's Complement

Two's Complement → Unsigned for n bits

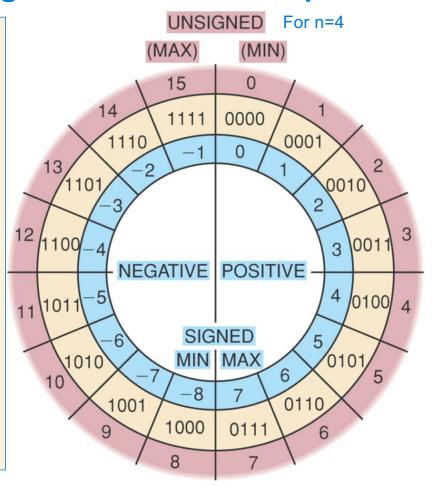
Unsigned Value Range

 $= 2^n - 1$

Two's Complement Range

SMin =
$$0b10...00$$
 = -2^{n-1}

 $= 2^{n-1} - 1$



Negation Of a Two's Complement Number (Method 1)

$$7 = 0111$$
 $-7 = + 1001$
(discard carry) 0000

 $-x == \sim x + 1;$

Negation of a Two's Complement Number (Method 2)

- 1. copy unchanged right most bit containing a 1 and all the 0's to its right
- 2. Invert all the bits to the left of the right-most 1

