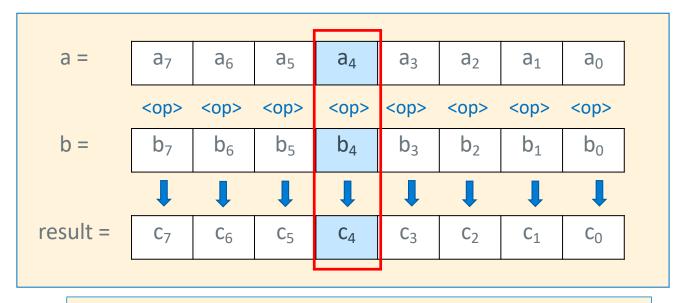


What is a Bitwise Operation?



- Bitwise operators are applied independently to each of the <u>corresponding</u> bit positions in each variable
- Each bit position of the result depends <u>only</u> on bits in the <u>same bit position</u> within the operands

Bitwise (Bit to Bit) Operators in C

output = ∼a;

a	~a
0	1
1	0

а	b	a & b
0	0	0
0	1	0
1	0	0
1	1	1

& with 1 to let a bit through & with 0 to set a bit to 0

output = a & b; output = a | b;

a	b	a b
0	0	0
0	1	1
1	0	1
1	1	1

with 1 to set a bit to 1 I with 0 to let a bit through output = a ^ b; //EOR

а	b	a ^ b
0	0	0
0	1	1
1	0	1
1	1	0

- ^ with 1 will flip the bit
- ^ with 0 to let a bit through

Bitwise NOT



Bitwise **AND**

&	0110 1100
	0100
	0100

Bitwise



Bitwise

EOR 0110 ^ 1100 1010

Bitwise Not (vs Boolean Not)

in C
int output = ~a;

a	~a
0	1
1	0

Bitwise NOT ~ 1100 ---0011

	Bitwise Not							
number	0101	1010	0101	1010	1111	0000	1001	0110
~number	1010	0101	1010	0101	0000	1111	0110	1001

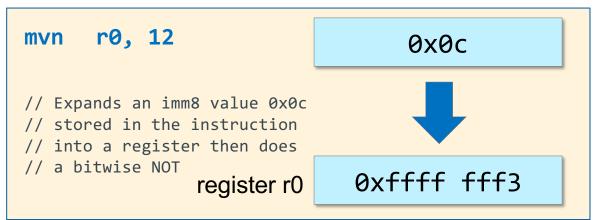
Meaning	Operator	Operator	Meaning
Boolean NOT	!b	~b	Bitwise NOT

Boolean operators act on the entire value not the individual bits

Туре	Operation	result							
bitwise	~0x01	1111	1111	1111	1111	1111	1111	1111	1110
Boolean	!0x01	0000	0000	0000	0000	0000	0000	0000	0000

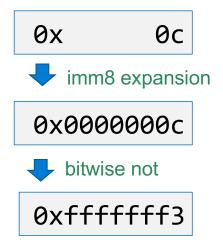
MVN (not)





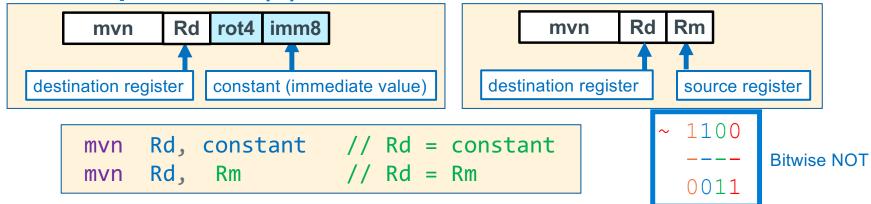


• A **bitwise NOT** operation



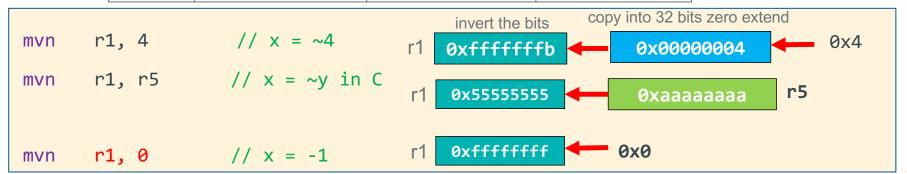
_

mvn – Copies NOT (~)

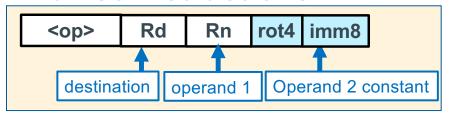


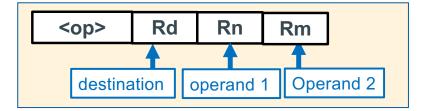
bitwise NOT operation. Immediate (constant) version copies to 32-bit register, then does a bitwise NOT

imm8	extended imm8	inverted imm8	signed base 10
0x00	0x00 00 00 00	0xff ff ff ff	-1
0xff	0x00 00 00 ff	0xff ff ff 00	-256



Bitwise Instructions





Bitwise <op> description</op>	C Syntax	Arm <op> Syntax Op2: either register or constant value</op>	Operation
Bitwise AND	a & b	and R _d , R _n , Op2	$R_d = R_n \& Op2$
Bitwise OR	a b	orr R _d , R _n , Op2	$R_d = R_n \mid Op2$
Exclusive OR	a ^ b	eor R _d , R _n , Op2	$R_d = R_n ^ Op2$
Bitwise NOT	a = ~b	mvn R _d , R _n	$R_d = \sim R_n$

7

Bitwise versus C Boolean Operators

Boolean Operators

Bitwise Operators

Meaning	Operator	Operator	Meaning
Boolean AND	a && b	a & b	Bitwise AND
Boolean OR	a b	a b	Bitwise OR
Boolean NOT	!b	~b	Bitwise NOT

Boolean operators act on the entire value not the individual bits

```
bitwise & versus Boolean &&

0x10 & 0x01 = 0x00 (bitwise)

0x10 && 0x01 = 0x01 (Boolean)

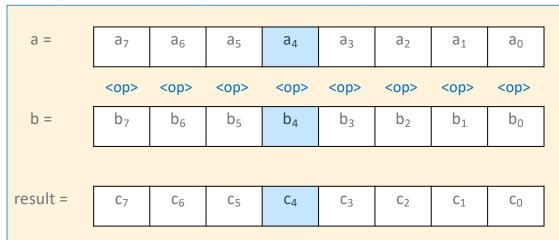
bitwise ~ versus Boolean !

~0x01 = 0xffffffffe (bitwise)

!0x01 = 0x0 (Boolean)

!0xff = 0x0 (Boolean)
```

The act (operation) of *Masking*



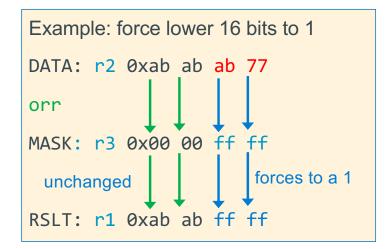
- Bit masks access/modify specific bits in memory
- Masking act of applying a mask to a value with a specific op:
- orr: 0 passes bit unchanged, 1 sets bit to 1 (a = b | c; // in C)
- eor: 0 passes bit unchanged, 1 inverts the bit (a = b ^ c; // in C)
- and: 0 clears the bit, 1 passes bit unchanged (a = b & c; // in C)

Mask on

force bits to 1 "mask on" operation

- 1 to set a bit to 1
- 0 to let a bit through unchanged

```
orr r1, r2, r3
r1 = r2 | r3; // in C
```



```
Example: force lower 8 bits to 1

DATA: r2 0xab ab ab 77

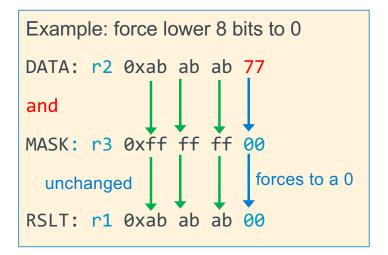
orr r1 r2, 0xff

r1 = r2 | 0xff; // in C

RSLT: r1 0xab ab ab ff
```

Mask off

```
force bits to 0 "mask off" operation
0 to set a bit to 0 ("clears the bit")
1 to let a bit through unchanged
and r1, r2, r3
r1 = r2 & r3; // in C
```



```
Example: force lower 8 bits to 0

DATA: r2 0xab ab ab 77

and r1 r2, 0xffffff00

r1 = r2 & 0xffffff00; // in C

RSLT: r1 0xab ab ab 00
```

Extracting (Isolate) a Field of Bits with a mask

extract top 8 bits of r2 into r1

- 0 to set a bit to 0 ("clears the bit")
- 1 to let a bit through unchanged

```
and r1, r2, r3
```

```
DATA: r2 0xab ab ab 77
and
MASK: r3 0xff 00 00 00
unchanged forces to a 0
RSLT: r1 0xab 00 00 00
```

```
extract top 8 bits of r2 into r1

DATA: r2 0xab ab ab 77

and r1, r2, 0xff000000

RSLT: r1 0xab 00 00 00

r1 = r2 & 0xff000000; // in C
```

Finding if a bit is set

```
query the status of a bit "bit status" operation
  • 0 to set a bit to 0 ("clears the bit")
  • 1 to let a bit through unchanged
        and r1, r2, 0x02
        cmp r1, 0
        beq .Lendif
        // code for is set
.Lendif:
```

```
unsigned int r1, r2;
// code
r1 = r2 & 0x02
if (r1 != 0) {
    // code for is set
}
```

```
unsigned int r2;
// code
if ((r2 & 0x02) != 0) {
      // code for is set
}
```

Even/Odd

```
Even or odd, check LSB (same as mod %2)

check LSB (bit 0) if set then odd, else even

and r1, r2, 0x01

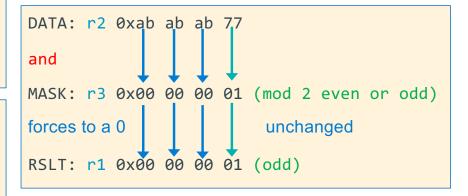
cmp r1, 0x01

bne .Lendif

// code for handling odd numbers

.Lendif:
```

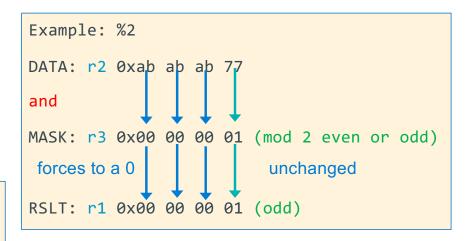
```
unsigned int r2;
// code
if ((r2 & 0x01) != 0) {
    // code for handling odd numbers
}
```

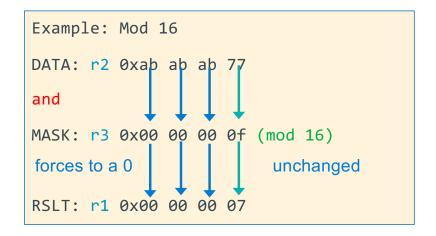


14

MOD %<power of 2>

remainder (mod): num % d where num ≥ 0 and $d = 2^k$ mask = 2^k -1 so for mod 16, mask = 16 -1 = 15 and r1, r2, r3





Flipping bits: bit toggle Used in PA7/PA8

invert (flip) bits "bit toggle" operation

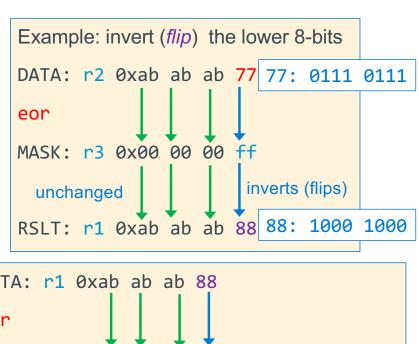
- 1 will flip the bit
- 0 to let a bit through

```
eor r1, r2, r3
```

- Observation: When applied twice, it returns the original value (symmetric encoding)
- With a mask of all 1's is a 1's compliment

```
Example: flip the lower 8-bits eor r1, r2, 0xff
```

```
unsigned int r1, r2;
r1 = r2 ^ 0xff;
```



```
DATA: r1 0xab ab ab 88

eor

MASK: r3 0x00 00 00 ff apply a 2<sup>nd</sup> time
inverts (flips)

RSLT: r1 0xab ab ab 77 original value!
```

16

Unsigned Integers (positive numbers) with Fixed # of Bits

- 4 bits is 2⁴ = ONLY 16 distinct values
- Modular (C operator: %) or clock math
 - Numbers start at 0 and "wrap around" after 15 and go back to 0
- Keep adding 1

wraps (clockwise)

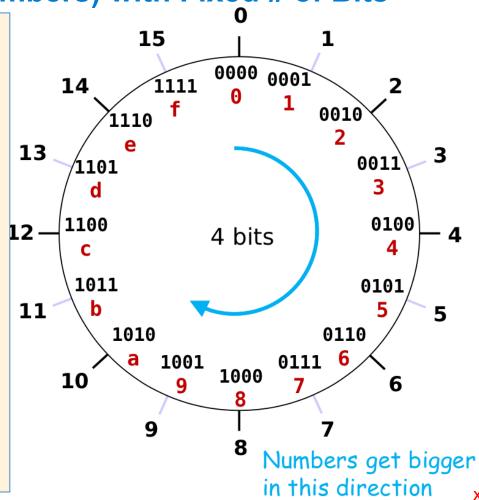
0000 -> 0001 ... -> 1111 -> 0000

Keep subtracting 1

wraps (counter-clockwise)

1111 -> 1110 ... -> 0000 -> 1111

 Addition and subtraction use normal "carry" and "borrow" rules, just operate in binary



Problem: How to Encode **Both Positive and Negative Integers**

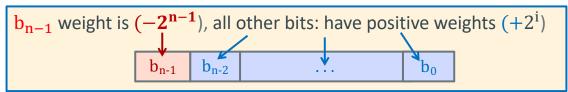
- How do we represent the negative numbers within a fixed number of bits?
 - Allocate some bit patterns to negative and others to positive numbers (and zero)
- 2ⁿ distinct bit patterns to encode positive and negative values
- Unsigned values: $0 \dots 2^n 1 \leftarrow$ -1 comes from counting 0 as a "positive" number
- Signed values: $-2^{n-1} \dots 2^{n-1}-1$ (dividing the range in ~ half including 0)
- On a number line (below): 8-bit integers signed and unsigned (e.g., char in C)



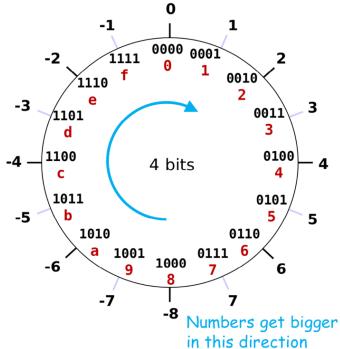
Same "width" (same number of encodings), just shifted in value

Two's Complement: The MSB Has a Negative Weight

$$2's\ Comp = -b_{n-1}2^{n-1} + b_{n-2}2^{n-2} + ... + b_12^1 + b_02^0$$



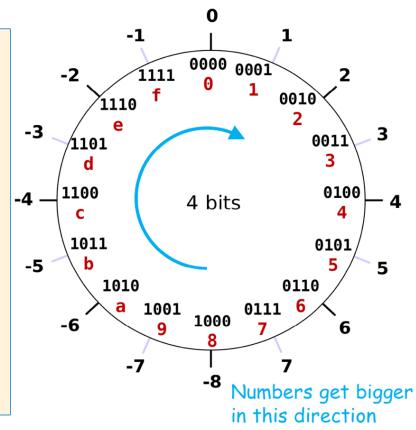
- 4-bit (w = 4) weight = $-2^{4-1} = -2^3 = -8$
 - 1010_2 unsigned: $1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = 10$
 - 1010_2 two's complement: $-1x2^3 + 0x2^2 + 1x2^1 + 0x2^0 = -8 + 2 = -6$
 - -8 in two's complement: $1000_2 = -2^3 + 0 = -8$
 - -1 in two's complement: $1111_2 = -2^3 + (2^3 - 1) = -8 + 7 = -1$



2's Complement Signed Integer Method

- Positive numbers encoded same as unsigned numbers
- All negative values have a one in the leftmost bit
- All positive values have a zero in the leftmost bit
 - This implies that 0 is a positive value
- Only one zero
- For n bits, Number range is $-(2^{n-1})$ to $+(2^{n-1}-1)$
 - Negative values "go 1 further" than the positive values
- Example: the range for 8 bits:

- Example the range for 32 bits:
 - **-2147483648** .. 0, .. **+2147483647**
- Arithmetic is the same as with unsigned binary!



20

Sign Extension (how type promotion works)

• Sometimes you need to work with integers encoded with different number of bits

8 bits (char) -> (16 bits) short -> (32 bits) int

• Sign extension increases the number of bits: n-bit wide signed integer X, EXPANDS to a wider

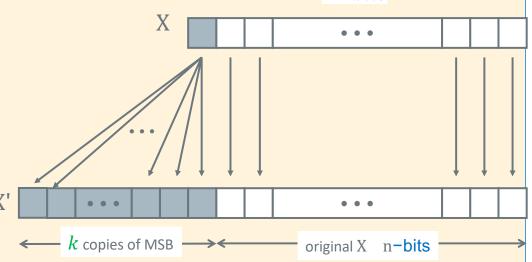
n-bit + k-bit signed integer X' where both have the same value

Unsigned

Just add leading zeroes to the left side

Two's Complement Signed:

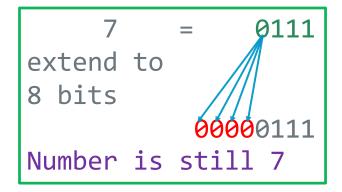
- If positive, add leading zeroes on the left
 - Observe: Positive stay positive
- If negative, add leading ones on the left
 - Observe: Negative stays negative

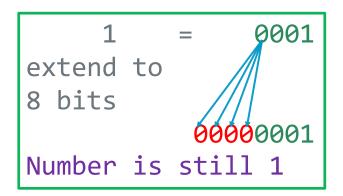


n-bits

Example: Two's Complement Sign or bit Extension - 1

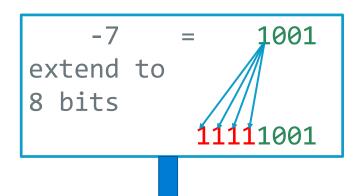
• Adding 0's in front of a positive numbers does not change its value





Example: Two's Complement Sign or bit Extension -2

• Adding 1's if front of a negative number does not change its value

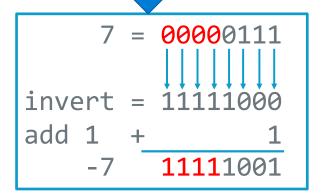


```
1001 = -8 + 1 = -7

11111001 =

(-128 + 64 + 32 + 16 + 8) + 1

= -8 + 1 = -7
```



Sign Extension in C: Type casts

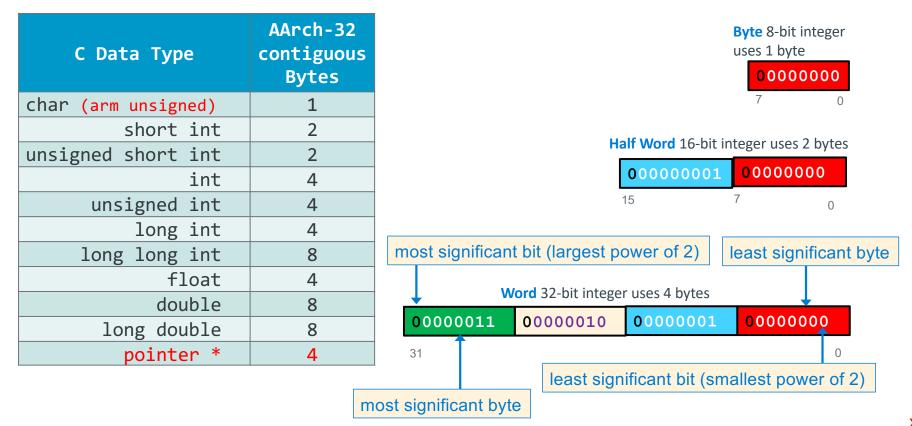
- Convert from smaller to larger integral data types
- C and Java automatically performs sign extension
- Example (on pi-cluster with 32-bit int)

```
#include <stdlib.h>
#include <stdio.h>
int main(void)
    signed char c = -1;
    signed int i = c;
    unsigned char d = 1;
    unsigned int j = d;
    printf("c decimal = %hd\n", c);
    printf("c = 0x\%hhx\n", c);
    printf("i decimal = %d\n", i);
    printf("i = 0x%x \n", i);
    printf("\nd decimal = %hd\n", d);
    printf("d = 0x%hhx\n", d);
    printf("j decimal = %d\n", j);
    printf("j = 0x%x \n", j);
    return EXIT SUCCESS;
```

```
%./a.out
c decimal = -1
c = 0xff
i decimal = -1
i = 0xffffffff

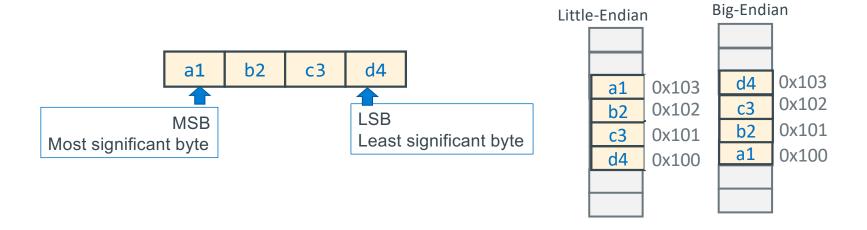
d decimal = 1
d = 0x1
j decimal = 1
j = 0x1
```

Different Type of Numbers each have a Fixed # of Bits Spanning one or more contiguous bytes of memory



Byte Ordering of Numbers In Memory: Endianness

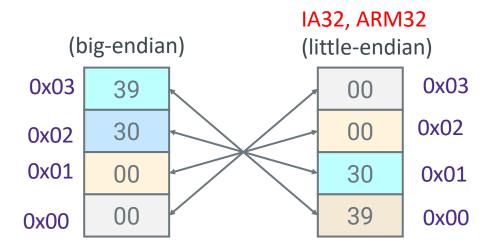
- Two different ways to place multi-byte integers in a byte addressable memory
- Big-endian: Most Significant Byte ("big end") starts at the *lowest (starting)* address
- Little-endian: Least Significant Byte ("little end") starts at the *lowest (starting)* address
- Example: 32-bit integer with 4-byte data



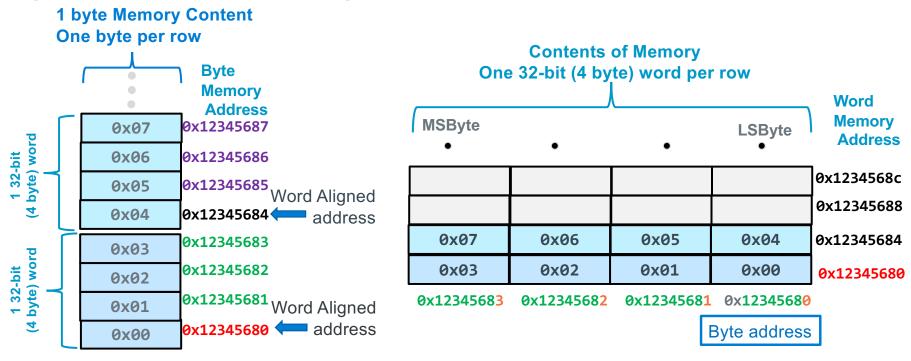
Byte Ordering Example

```
Decimal: 12345
Binary: 0011 0000 0011 1001
Hex: 3 0 3 9
```

```
int x = 12345;
// or x = 0x00003039; // show all 32 bits
```

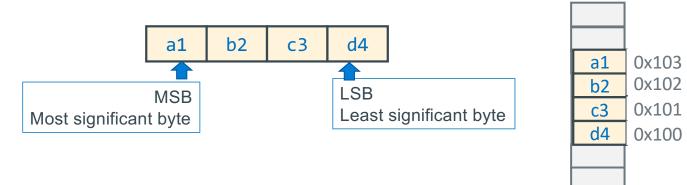


Byte Addressable Memory Shown as 32-bit words



Observation
32-bit aligned addresses
rightmost 2 bits of the address are always 0

Using pointers to examine byte order (on pi-cluster)



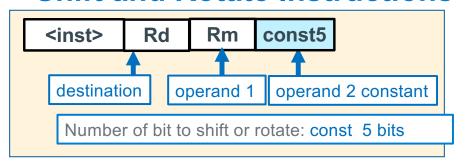
```
#include <stdio.h>
#include <stdlib.h>
#define SZ 2
int main()
{
    unsigned int foo[SZ] = {0x11223344, 0xaabbccdd};
    unsigned char *chptr = (unsigned char *)foo;

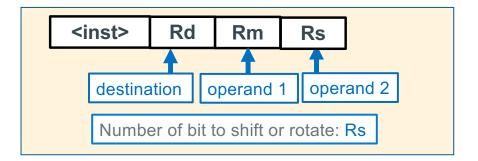
    // print from MSB to LSB - high to Low memory)
    for (int i = sizeof(foo)-1; i >= 0; i--)
        printf("byte %d: %x\n", i, *(chptr + i));

    return EXIT_SUCCESS;
}
```

	_
0xaa	0x12345687
0xbb	0x12345686
0хсс	0x12345685
0xdd	0x12345684
0x11	0x12345683
0x22	0x12345682
0x33	0x12345681
0x44	0x12345680
	0xbb 0xcc 0xdd 0x11 0x22 0x33

Shift and Rotate Instructions





Instruction	Syntax	Operation	Notes	Diagram
Logical Shift Left int x; or unsigned int x x << n;		$\begin{array}{c} R_d \leftarrow R_m & << \textit{const5} \\ R_d \leftarrow R_m & << R_s \end{array}$	Zero fills shift: 0 - 31	C 631 60 0
Logical Shift Right unsigned int x; x >> n;		$\begin{array}{c} R_d \;\leftarrow\; R_m \;\; >> \;\; const5 \\ R_d \;\leftarrow\; R_m \;\; >> \;\; R_s \end{array}$	Zero fills shift: 1 - 32	0
Arithmetic Shift Right int x; x >> n;		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Sign extends shift: 1 - 32	b31 b0 C
<pre>Rotate Right unsigned int x; x = (x>>n) (x<<(32-n));</pre>		$\begin{array}{c} R_d \leftarrow R_m \text{ror} \textit{const5} \\ R_d \leftarrow R_m \text{ror} R_s \end{array}$	right rotate rot: 0 - 31	b31 b0

 x

Shift Operations in C

- n is number of bits to shift a variable x of width w bits
- Shifts by n < 0 or n ≥ w are undefined
- Left shift (x << N) Multiplies by 2^N
 - Shift N bits left, Fill with 0s on right
- In C: behavior of >> is determined by compiler
 - gcc: it depends on data type of x (signed/unsigned)
- Right shift (x >> N) Divides by 2^N
 - Logical shift (for unsigned variables)
 - Shift N bits right, Fill with 0s on left
 - Arithmetic shift (for signed variables) Sign Extension
 - Shift N bits right while <u>Replicating</u> the most significant bit on left
 - Maintains sign of x

31

In Java: logical shift is >>> and arithmetic shift is >>





X

Arithmetic Shift Right Example: Testing Sign

```
asr r2, r0, 31

r0 0xab ab ab 77 // bit 31 is a one
r2 0xff ff ff ff // see the sign extend

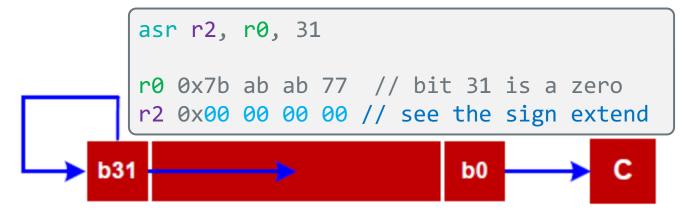
b0 C
```

```
int i;
//code
if ((i>>31) == -1) {
   // code neg #
}
```

```
Test for sign
-1 if r0 negative
```

```
asr r2, r0, 31
cmp r2, -1
bne .Lendif
//code neg #
.Lendif:
```

Arithmetic Shift Right Example: Testing SIgn



```
int i;
//code
if ((i>>31) == 0) {
    // code pos #
}
```

Test for sign 0 if r0 positive

```
asr r2, r0, 31
cmp r2, 0
bne .Lendif
//code positive #
.Lendif:
```

Logical Shift & Rotate Operations

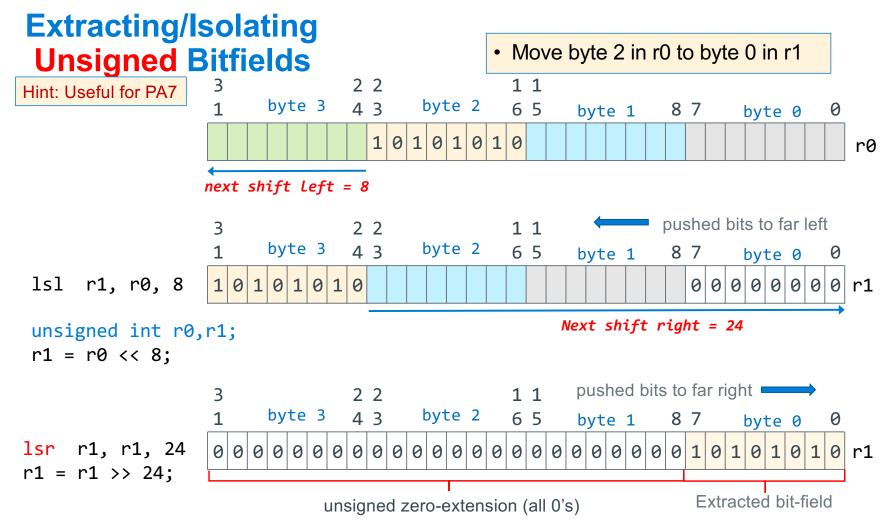


lsr r2, r0, 8
r0 0xab ab ab 77
r2 0x00 ab ab ab

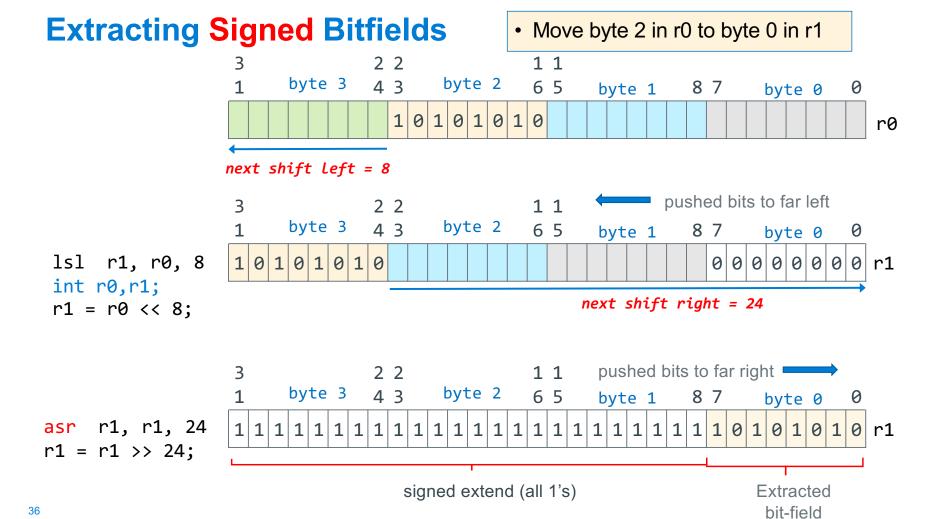


1sl r2, r0, 8 r0 0xab ab ab 77 r2 0xab ab 77 00

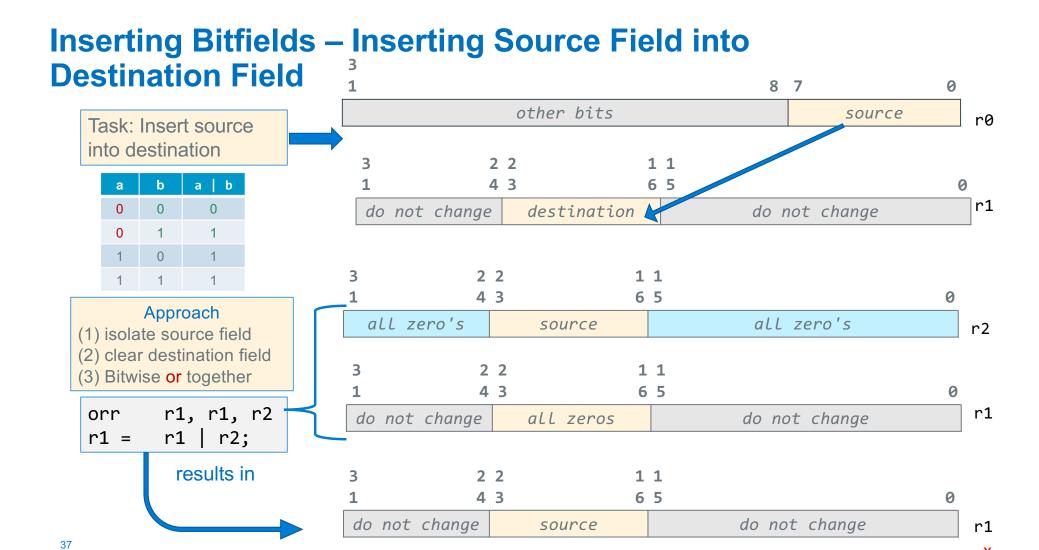




35

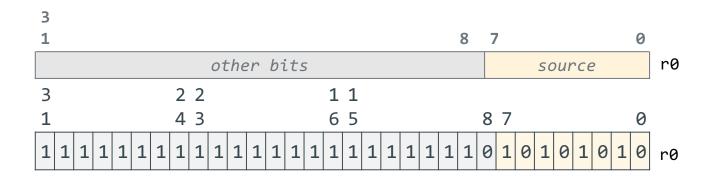


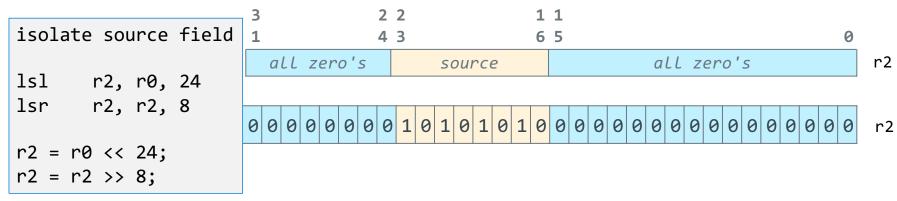
X



X

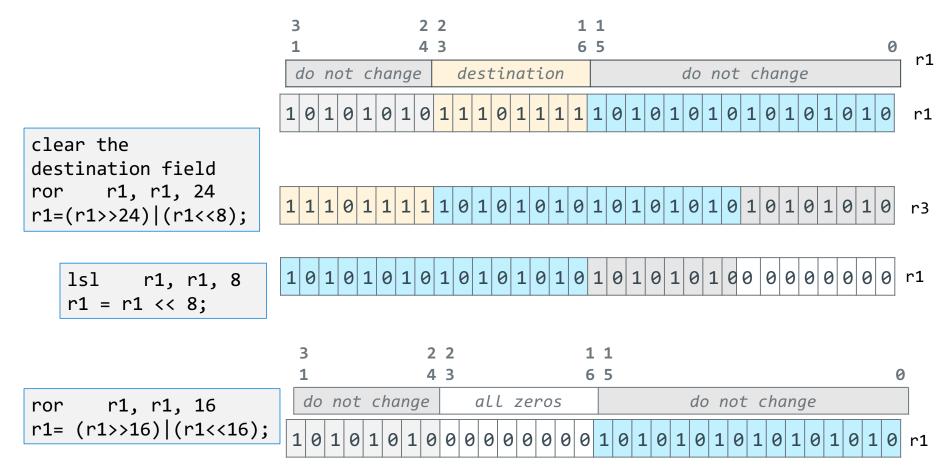
Inserting Bitfields – Isolating the Source Field





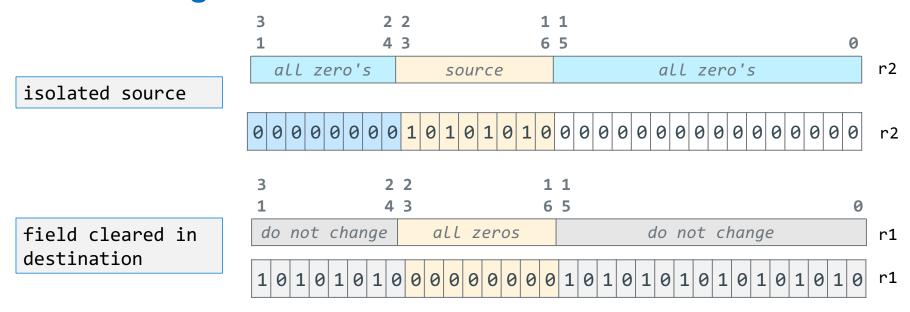
38

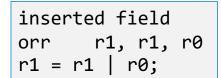
Inserting Bitfields – Clearing the Destination Field

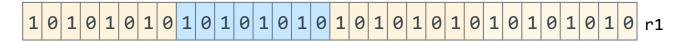


39

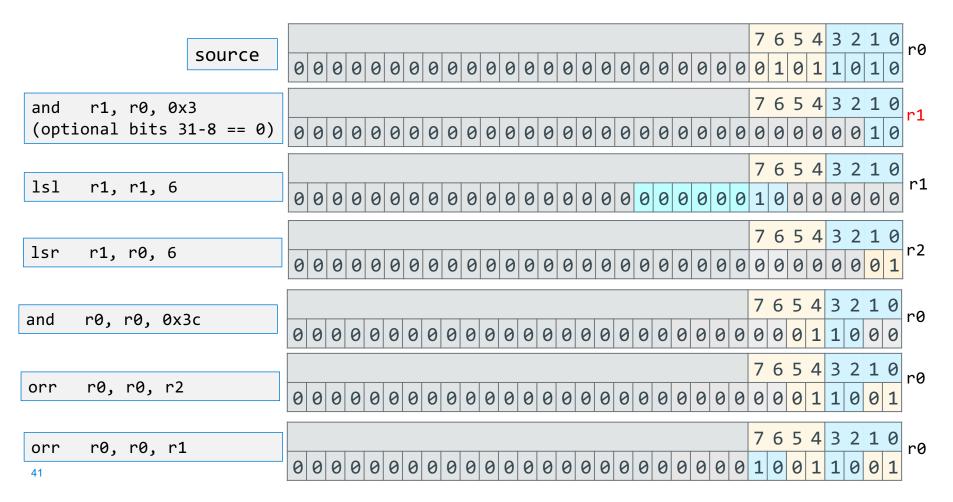
Inserting Bitfields – Combining Isolated Source and Cleared Destination



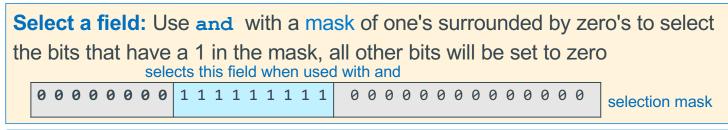




Example: Swapping bits7,6 with bits 1,0



Masking Summary



Clear a field: Use and with a mask of zero's surrounded by one's to select the bits that have a 1 in the mask, all other bits will be set to zero clears this field when used with and

Insert a field: Use orr with fields surrounded by zeros