

Definitie O functie $f : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ se numeste izometrie dacă pentru orice $x = (x^1, x^2), y = (y^1, y^2) \in \mathbb{R}^2$

$$d(x, y) = d(f(x), f(y))$$

$$[d((x^1, x^2), (y^1, y^2)) \stackrel{def}{=} \sqrt{(x^1 - y^1)^2 + (x^2 - y^2)^2}]$$

Ex: 1. Functia identică

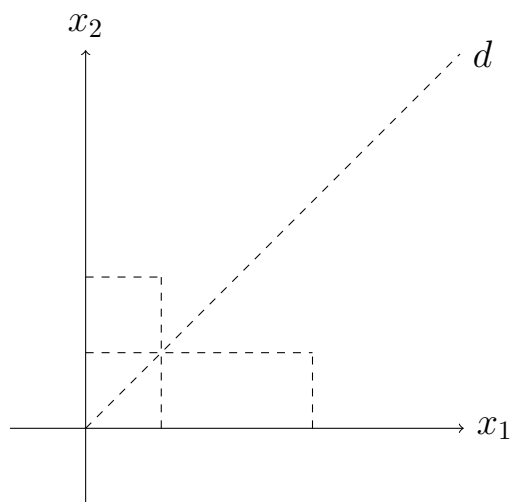
2. Functia $f : \mathbb{R}^2 \rightarrow \mathbb{R}^2, \forall x = (x^1, x^2) \in \mathbb{R}^2$

$$f(x) = (x^2, x^1)$$

Fie $x, y \in \mathbb{R}^2$ unde

$$\begin{aligned} x &= (x^1, y^2) \\ y &= (y^1, x^2) \end{aligned}$$

$$d(f(x), f(y)) = \sqrt{(x^2 - y^2)^2 + (x^1 - y^1)^2}$$



$$d : x^2 - y^1 = 0$$

$$f = \underset{(simetric)}{Sim} d$$

3. Functia $f : \mathbb{R}^2 \rightarrow \mathbb{R}^2$

$$\forall x = (x^1, x^2)$$

$$f(x) = (x^1 + \alpha, x^2 + \beta)$$

$$f = T_{(\alpha, \beta)}$$

$$f(x) = x + (\alpha, \beta)$$

$$\alpha = (1, 1)$$

