

7)

Assume a free electron absorbs a photon,

Energy conservation gives

$$hc/\lambda + mc^2 = \gamma mc^2 \text{ ---(1)}$$

Momentum conservation gives

$$h/\lambda = \gamma mv \text{ ---(2)}$$

Substitute (2) in (1)

$$\gamma mvc + mc^2 = \gamma mc^2$$

$$\gamma vc + c^2 = \gamma c^2$$

$$\gamma(c-v) = c$$

On solving,

$$(c-v)(c+v) - (c-v)^2 = 0$$

i.e. $v=c$ or $v=0$

If $v=0$ momentum is not conserved

And if $v=c$, Energy is not conserved.

Hence a free electron cannot absorb a photon.

In case of Compton effect, there-radiated photon conserves momentum and energy.