PH-105 Assignment Sheet - 1

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11.08.2012

5. An observer is sitting in a train (call it frame S' and assume that the observer is sitting at the origin). The train moves with a constant speed of 0.6c relative to ground (assume ground to be the inertial frame S). Another observer is sitting at the origin of S. The two observers set the watches to zero time at the instance they cross each other. At time $t' = 2 \times 10^{-6}$ s, the observer in the train finds himself passing a building "A" on the ground. Also in the train frame at time $t' = 2 \times 10^{-6}$ s, lighning strikes the ground at a place where the origin of S is situated. Find the distance of train from origin when lightning struck, according to the observer on ground. Also find the distance of the building "A" from origin in S and the time the train would reach building "A", in S frame?

Solution:

Relative speed, v=0.6c. Hence γ =1.25.

The following events can be identified in the above problem :

E1: Train passing the building A.

E2: Striking of the lightning.

Let (x_1, t_1) and (x_2, t_2) be the coordinates of the two events in A's frame. Similarly, let (x'_1, t'_1) and (x'_2, t'_2) be the corresponding coordinates in B's frame.

Known values are:

$$\begin{array}{c} t_1'=t_2'=t'=2\times 10^{-6}\mathrm{s} \\ x_1'=0 \\ x_2=0 \end{array}$$
 (from the given data) (building is at train's origin when E1 occurs)

When **E2** occurs, the separation between the origins of two frames as seen by the train observer will be:

$$x_2' = -vt_2' = -0.6c \times 2 \times 10^{-6}s = -360m$$

From inverse Lorentz transformation, we get:

$$t_2 = \gamma \left(t_2' + \frac{vx_2'}{c^2} \right) = 1.6 \times 10^{-6} \text{s}$$

Distance of train from origin when lightning struck, according to the observer on ground

$$= vt_2 = 0.6c \times 1.6 \times 10^{-6}s = 288m$$

Since E1 occurs at the position of building, distance of building from origin in frame S equals

$$x_1 = \gamma(x_1' + vt_1') = \gamma vt_1' = 1.25 \times 0.6c \times 2 \times 10^{-6}s = 450m$$

Time difference between the crossing of origins and E1 is proper in the train frame. Hence time taken by train to reach building in S frame

= time difference between crossing of origins and **E1** in S frame
$$= \gamma t_1' = 2.5 \times 10^{-6} s$$

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