

## DAVP Week 7

*Designed by: Pranjal Khare & Aditya Nambiar*

Ques1: Given a sequence of  $n$  numbers  $a_1, a_2, \dots, a_n$  :

1> Given a pair  $(i, j)$ , return the number of distinct elements in the subsequence  $a_i, a_{i+1}, \dots, a_j$ .

2> Given a triplet  $(i, j, k)$ , return the number of elements greater than  $k$  in the subsequence  $a_i, a_{i+1}, \dots, a_j$ .

3> If sequence is in non-decreasing order, given a pair  $(i, j)$ , determine the most frequent value among the integers  $a_i, \dots, a_j$ .

4> Given a pair  $(x, y)$ , return  $\text{Max} \{ a[i] + a[i+1] + \dots + a[j] ; x \leq i \leq j \leq y \}$ .

Ques2:

A computer processor is given  $N$  tasks to perform ( $1 \leq N \leq 50,000$ ). The  $i$ -th task requires  $T_i$  seconds of processing time ( $1 \leq T_i \leq 1,000,000,000$ ). The processor runs the tasks as follows: each task is run in order, from 1 to  $N$ , for 1 second, and then the processor repeats this again starting from task 1. Once a task has been completed, it will not be run in later iterations. Determine, for each task, the total running time elapsed once the task has been completed.

Ques3:

An  $n$ -element permutation is an  $n$ -element sequence of distinct numbers from the set  $\{1, 2, \dots, n\}$ . For example the sequence 2,1,4,5,3 is a 5-element permutation. We are interested in the longest increasing subsequences in a permutation. In this exemplary permutation they are of length 3 and there are exactly 2 such subsequences: 2,4,5 and 1,4,5. We will call a number belonging to any of the longest increasing subsequences a supernumber. In the permutation 2,1,4,5,3 the supernumbers are 1,2,4,5 and 3 is not a supernumber. Your task is to find all supernumbers for a given permutation.

Ques4:

Given a sequence of  $N$  ( $1 \leq N \leq 10,000$ ) integers  $S_1, \dots, S_N$  ( $0 \leq S_i < 100,000$ ), compute the number of increasing subsequences of  $S$  with length  $K$  ( $1 \leq K \leq 50$  and  $K \leq N$ ); that is, the number of  $K$ -tuples  $i_1, \dots, i_K$  such that  $1 \leq i_1 < \dots < i_K \leq N$  and  $S_{i_1} < \dots < S_{i_K}$ .

Ques5:

Let  $A[0 \dots n - 1]$  be an array of  $n$  distinct positive integers. If  $i < j$  and  $A[i] > A[j]$  then the pair  $(i, j)$  is called an inversion of  $A$ . Given  $n$  and an array  $A$  your task is to find the number of inversions of  $A$ .

Ques6:

You have  $k$  lists of sorted integers. Find the smallest range that includes at least one number from each of the  $k$  lists. DAVP Week 7

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Ques6:

You have  $k$  lists of sorted integers. Find the smallest range that includes at least one number from each of the  $k$  lists.

For example,

List 1: [4, 10, 15, 24, 26]

List 2: [0, 9, 12, 20]

List 3: [5, 18, 22, 30]

The smallest range here would be [20, 24] as it contains 24 from list 1, 20 from list 2, and 22 from list 3.

<http://www.careercup.com/question?id=16759664>

Q7)

Given an unsorted array of integers, you need to return maximum possible  $n$  such that the array consists at least  $n$  values greater than or equals to  $n$ . Array can contain duplicate values.

Sample input : [1, 2, 3, 4] -- output : 2

Sample input : [900, 2, 901, 3, 1000] -- output: 3

<http://www.careercup.com/question?id=5094709806497792>

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