

Solution for tutorial 5

1)

a) At resonant frequency $Z = R = 10\text{ohm}$

$$\text{resonant frequency } f_r = 1/(2\pi \sqrt{LC}) = 5.03\text{KHz}$$

b) At $f = 4.03\text{KHz}$

$$X_C = 3.95\text{Kohm}$$

$$X_L = 2.53\text{Kohm}$$

$$Z = 1.42\text{Kohm}$$

c) At $f = 6.03\text{KHz}$

$$X_C = 2.64\text{Kohm}$$

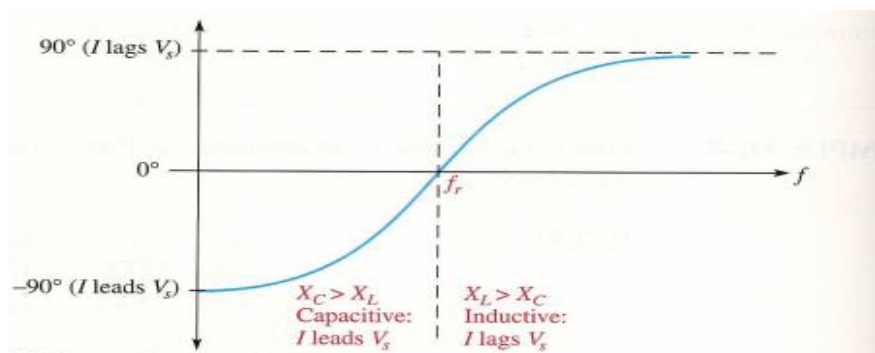
$$X_L = 3.79\text{Kohm}$$

$$Z = 1.15\text{Kohm}$$

2) For low frequencies C is open hence impedance is high and falls as inversely proportional to omega . Minimum resistance R at resonance. At high frequency L is open and impedance again increases proportional to frequency. From problem 1 minimum value is 10 ohm at 5.03KHz, 1.42Kohm at 4.03KHz and 1.15Kohm at 6.03KHz

Current magnitude plot can be obtained from impedance magnitude plot by dividing voltage with impedance.

At frequencies below resonance, $X_C > X_L$, and the current leads the source voltage. The phase angle decreases as the frequency approaches the resonant value and is 0 at resonance. At frequencies above resonance, $X_L > X_C$, and the current lags the source voltage, as indicated in part (c). As the frequency goes higher, the phase angle approaches 90.



3) Find the total impedance and equate imaginary term to zero at resonance

$$L=2\text{mH}, C=0.5\text{mF}, R= 1 \text{ ohm}$$

$$\text{a) Resonant frequency } \omega_r = \sqrt{((1/LC)-(R/L)^2)}$$

$$= 866.05 \text{ rad/sec}$$

b) Resonant frequency $\omega_r = \sqrt{1/LC}$
 $= 316.2 \text{ rad/sec}$

4)

a) Resonant frequency = 1.59MHz

$$Q = X_L / R = 200$$

$$BW = 7.95 \text{ KHz}$$

b) Resonant frequency = 22.5MHz

$$Q = X_L / R = 14.1$$

$$BW = 1.6 \text{ KHz}$$