

1. (1 point) Write the 8-bit sign-magnitude binary number 11110000 in the form of a 16-bit sign-magnitude binary number.

1000 0000 0111 0000

2. (3 points) Write the value 18.125×10^0 in 32-bit IEEE Floating Point format.

$$\begin{aligned}
 18.125 \times 10^0 &= 18.125 \times 2^0 \\
 &= 10010.001 \times 2^0 = 1.0010001 \times 2^4 \\
 \text{Exp} &= 4 + 127 = 131 = 10000011 \\
 \Rightarrow & \quad 0 \quad 10000011 \quad 0010001000 \dots 0
 \end{aligned}$$

3. (2 points) Suppose there was a large floating point representation which used 16 bits for the exponent. If the exponent was represented using a bias, what would you expect the bias to be?

$$\begin{aligned}
 \text{for } 8 \text{ bits Exp } 2^{8/2} - 1 &= 127 \text{ is the bias} \\
 \Rightarrow \text{for } 16 \text{ bit Exp } 2^{16/2} - 1 &= 2^{15} - 1 = \underline{\underline{32767}}
 \end{aligned}$$

4. (2 points) Give the **minimal** sequence of actual MIPS instructions to perform the pseudo instruction

ble \$t5, \$t3, L (branch to label L if \$t5 <= \$t3)

slt \$t0, \$t3, \$t5
 beq \$t0, \$0, L. (\Rightarrow go to L
 if $t3 \neq t5$
 $\Rightarrow t3 \geq t5$
 or $t5 \leq t3$)

5. Consider the following code sequence in MIPS assembly:

```
here: beq $t1, $t2, there
```

```
...
```

```
there: add $t1, $t1, $t1
```

- (a) (2 points) Can you think of a situation where this code sequence might cause issues given the semantics of the (branch) instructions?

of instructions between "here"
to "there" might be more than what
can be represented in the range of
a I type instruction.

- (b) (3 points) Rewrite the code sequence to fix the problem(s).

still need to test $t1 = t2$?

```
here: bne $t1, $t2, closeby
      j     there
closeby: ...
```

```
there: add $t1, $t1, $t1
```

6. (10 points) State whether each of the following are [T]rue or [F]alse next to the statement in the space provided. Each carries 1 point.

- (a) An exclusive-NOR gate output is HIGH when the inputs are unequal. [F]
- (b) A circuit containing only OR and NOT gates must be a combinational circuit. [F]
- (c) For two's complement numbers, the negative of a number can be found by adding one and then inverting the bits. [F]
- (d) The word address 0x01FF044C is word aligned in a 32 bit computer with byte addressed memory. [T]
- (e) Doubling the number of registers of a register file (but leaving everything else the same) will double the number of input lines to the register file. [F]
- (f) To perform the operation $A - B$, where A and B are numbers represented in two's complement, one can build hardware to perform the following steps: flip the bits of A, add B with a carry-in of 1, flip the bits of the result, and then add 1. [T]
- (g) The opcode field of all J-format MIPS instructions is 0. [F]
- (h) Since MIPS provides instructions to access memory directly (such as lw and sw) MIPS is NOT a load-store architecture. [F]
- (i) A CPU with a faster clock frequency always has higher performance than one with a slower clock. [F]
- (j) The instruction pair used for function calls in MIPS are JALR and JR. [F] JAL 2 JR

7. (3 points) State one instruction each of I-type, R-type and J-type that allows us to change control flow in MIPS.

lneq/bneq
jr
jal

8. (4 points) Consider the following program fragment in MIPS32 assembly code:

```
li $s0, -1
srl $v0, $s0, 1
addiu $a0, $v0, 1
```

pseudo instruction = 2
 real instructions
 $\Rightarrow 4$ total inst 040
 = 128 bits

Which of the following statements are correct? Justify.

- (i) The fragment of code will occupy 128 bits in memory
- (ii) Register \$a0 will contain the largest positive representable signed number after executing the fragment
- (iii) Register \$a0 will contain the least negative representable signed number after executing the fragment
- (iv) The fragment will raise an overflow exception
- (v) Register \$v0 will contain -1 after executing the fragment

0 0 0 0 0 0 0 0 0 0 0 1

1 1 1 1 1 1 1 1 1 0

1

0x F F F F F F F F

0111 FFFF : - - f

0 111 1111 1111 1111 1111 1111 1111 1111

1 000 000 000

00


```

# x is the first argument and has been stored in $a0
# y is the second argument and has been stored in $a1
GCD:      subi $sp, $sp, 12    # create stack frame
          sw  $a0, 0($sp)      # save x
          sw  $a1, 4($sp)      # save y
          sw  $ra, 8($sp)      # save return address

          bne $a0, $a1, rec    # if x != y, jump to 'rec'

          # if x == y, return x
          move $v0, $a0
          addi $sp, $sp, 12

```

```

jr $RA    # return

```

```

# The recursion begins
rec:   bgt $a0, $a1, xgty    # if x > y, jump to xgty
xlt:   sub $a1, $a1, $a0     # a1 <- y-x

```

```

jal GCD    # call GCD(x, (y-x))

```

```

# after returning from GCD(x, (y-x))
lw  $a0, 0($sp)    # restore x
lw  $a1, 4($sp)    # restore y
lw  $ra, 8($sp)    # restore return address
addi $sp, $sp, 12  # destroy stack frame

```

```

jr $RA    # return

```

```

xgty:
sub  $a0, $a0, $a1
jal  GCD
lw   $a0, 0($sp)
lw   $a1, 4($sp)
lw   $ra, 8($sp)
addi $sp, $sp, 12
jr   $ra

```