

# Digital Image Processing

## Segmentation - Edge Detection

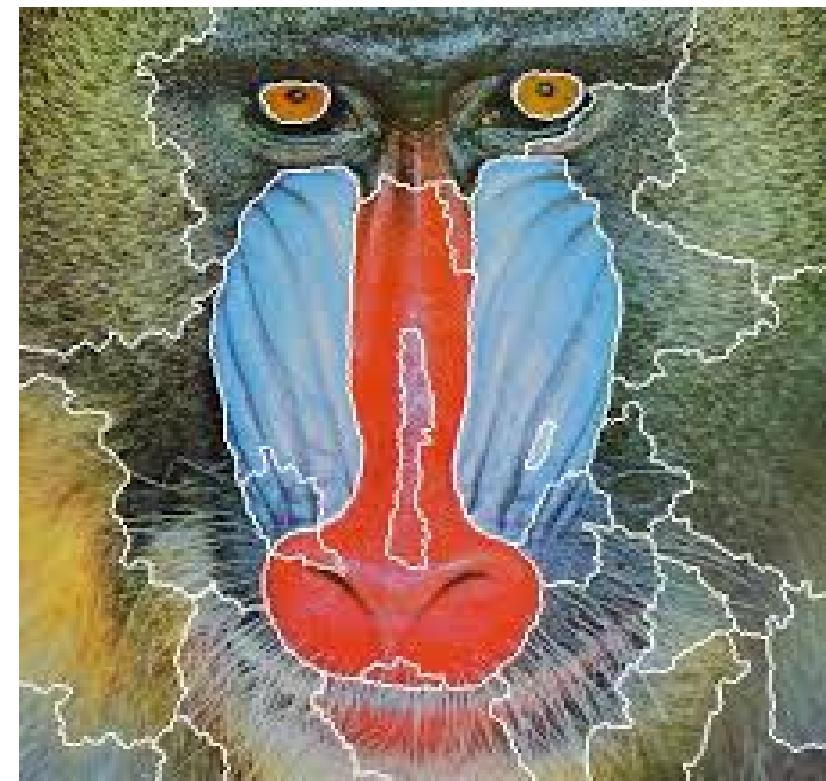
Suyash P. Awate

# Segmentation

- Definition : Process of partitioning an image into parts
  - Parts are called **segments**
- Why ?
  - Simplification of information content
  - Towards higher-level understanding / interpretation
- Segmentation = **labeling**
  - Label = categorical variable
    - {A, B, C}, {1, 2, 3}, etc.
  - Assign a label to each pixel
  - All pixels with same label = one segment
- Typically, 1 segment = 1 (or more) connected regions

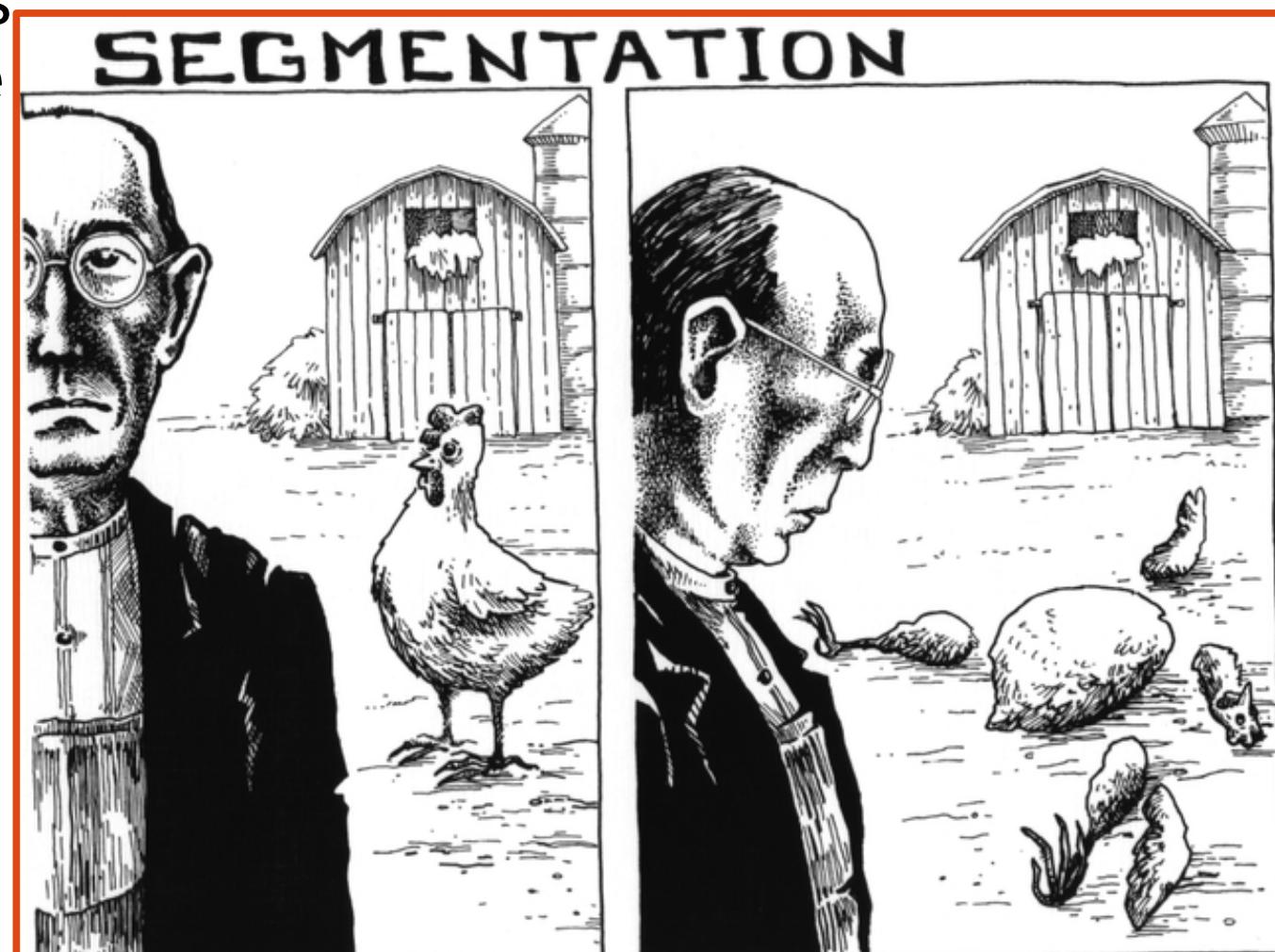
# Segmentation

- Segmentation example



# Segmentation

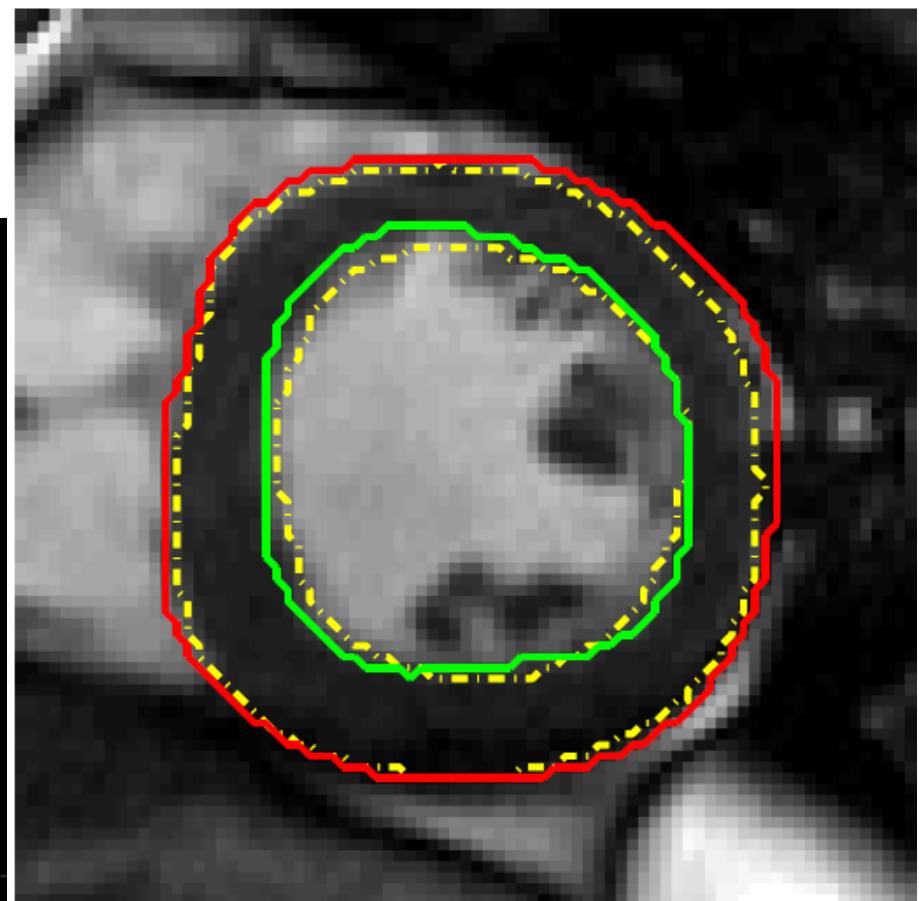
- Human perception
  - Instead of perceiving **indivisible** objects, we perceive objects in terms of their **labeled** or **categorized** parts
  - We break objects into parts that we have learned are relevant or important



# Segmentation

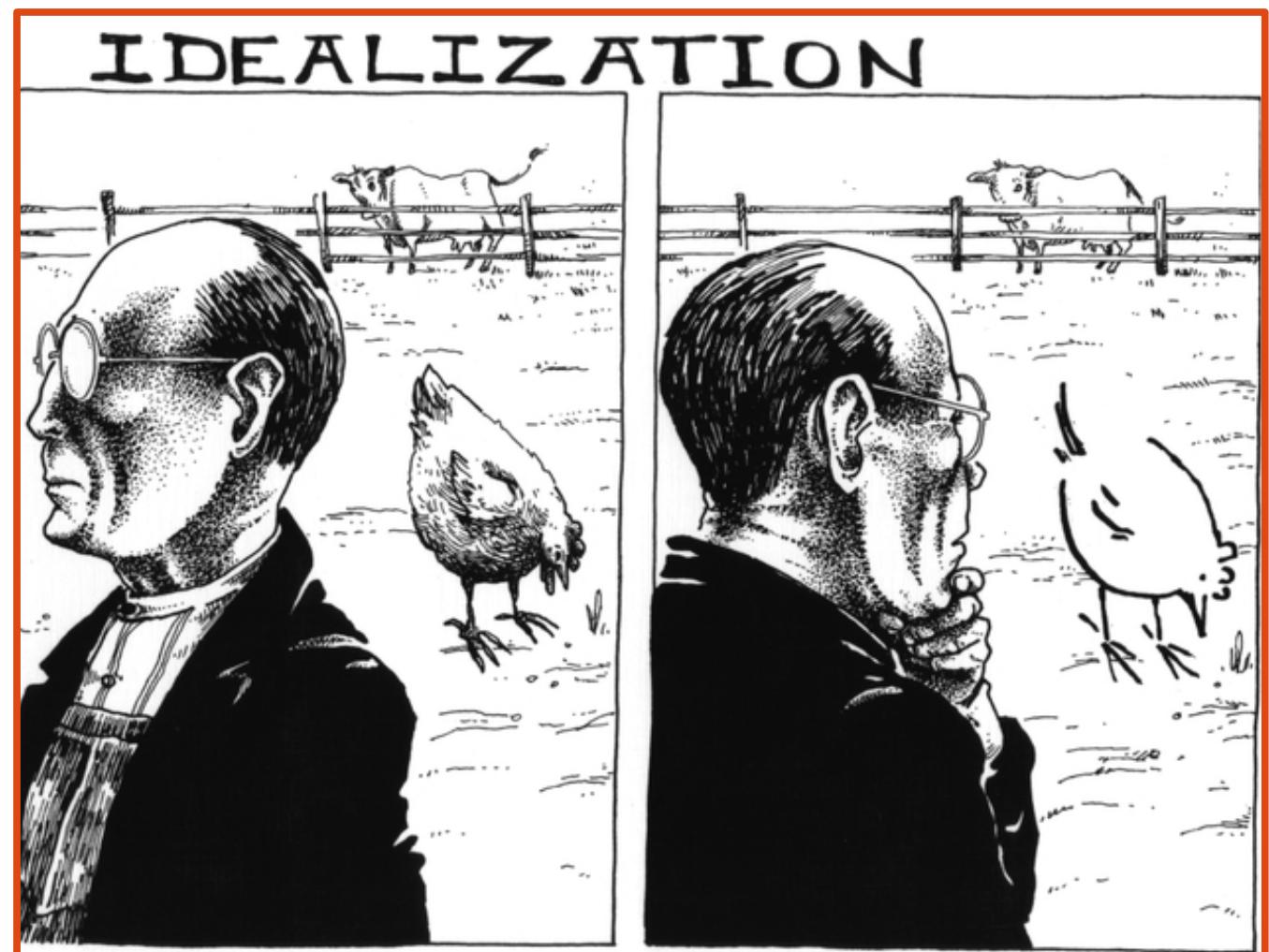
- **Delineation**

- Process of determining the outline of **an object** in image



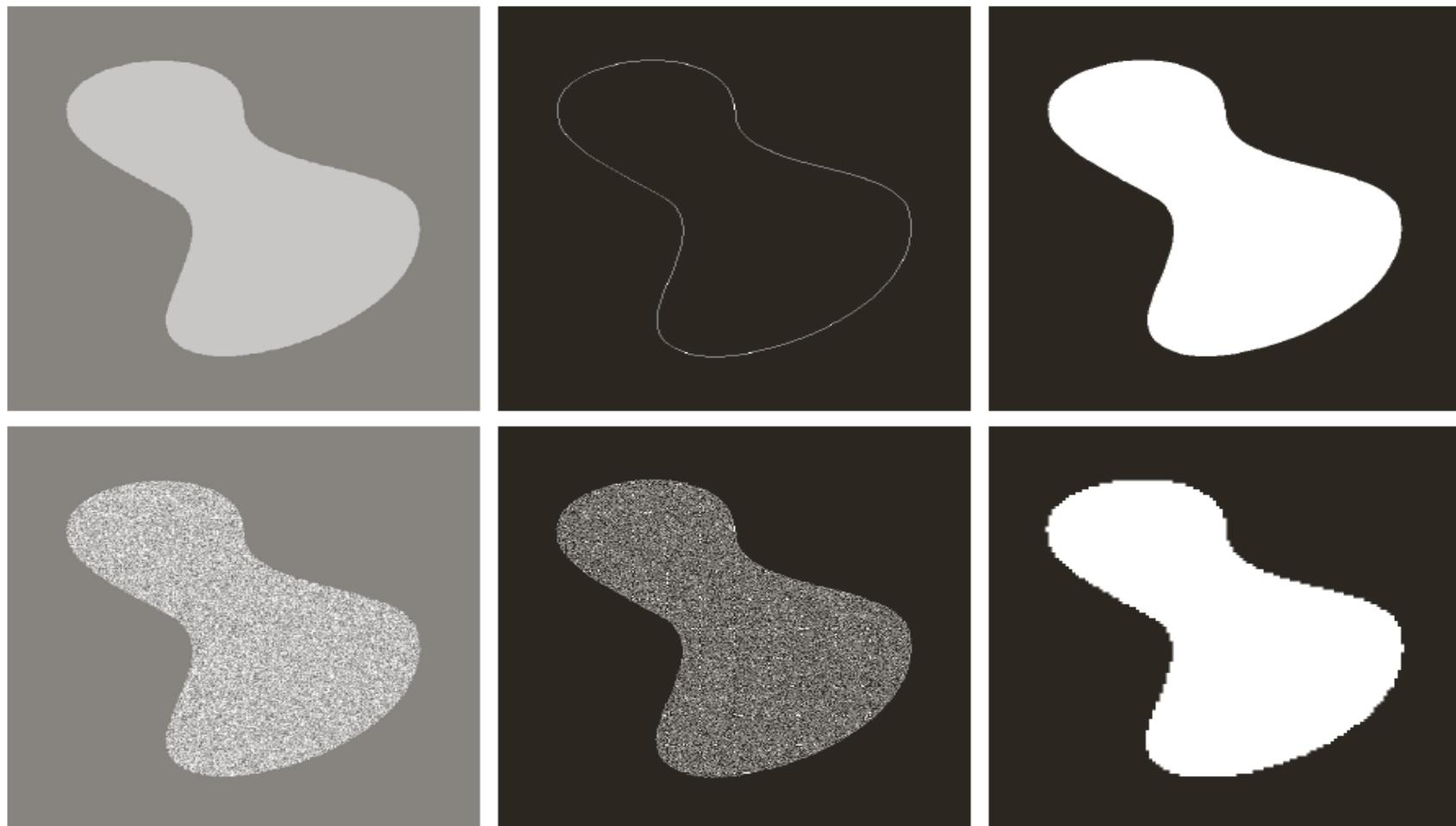
# Segmentation

- Human perception (delineation)
  - Objects are often simplified so as to capture the **basic essence** of the underlying concept



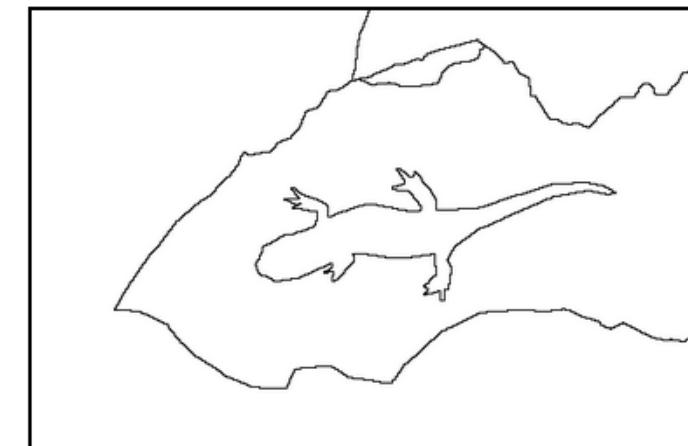
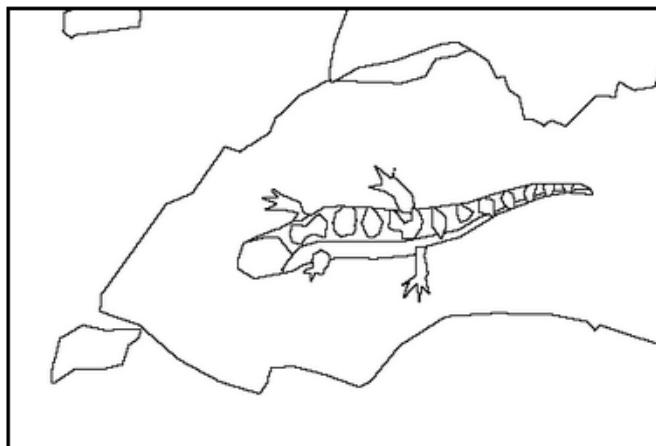
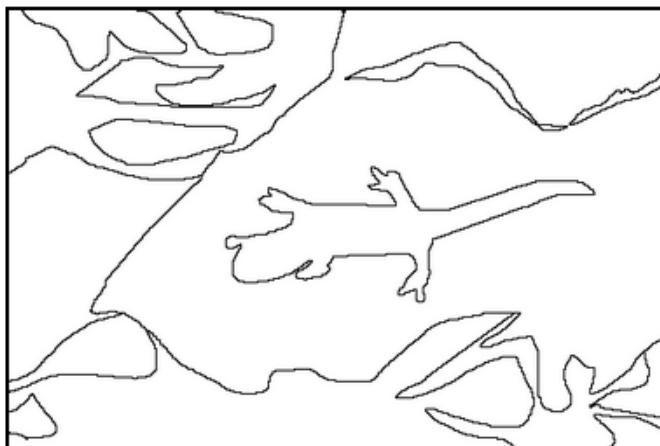
# Segmentation

- Image segmentation
  - Top row: noiseless image, edge detection, segmentation
  - Bottom row: noisy image, edge detection, segmentation



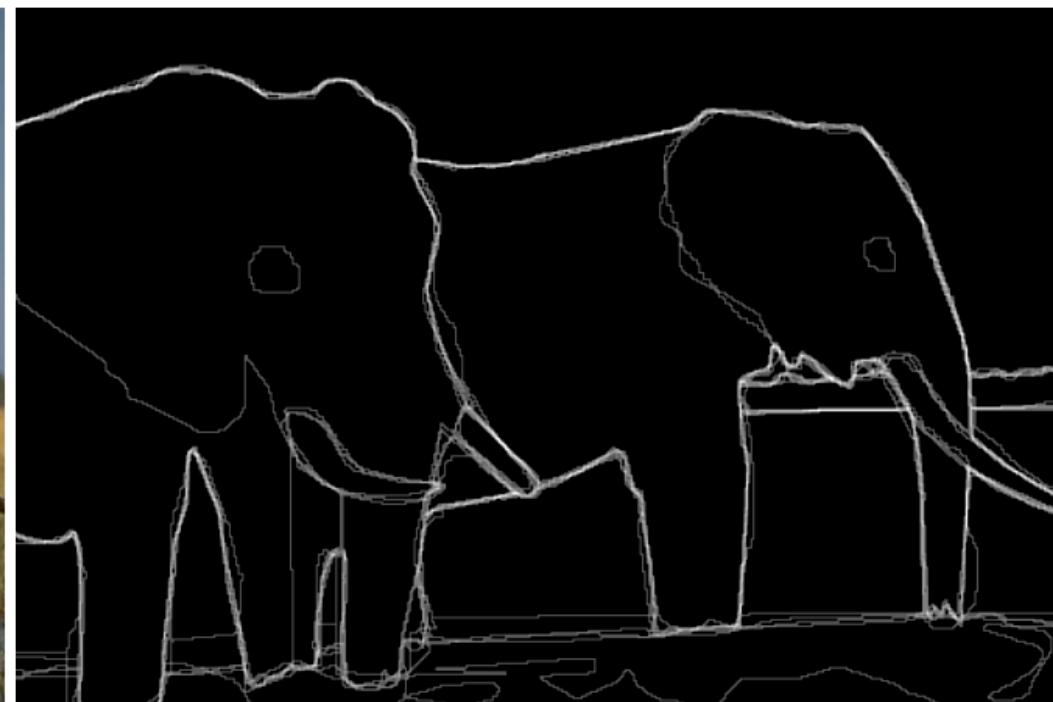
# Segmentation

- Subjective
  - Segmentation is in the eye of the beholder !



# Segmentation

- Subjective
  - Segmentation is in the eye of the beholder !



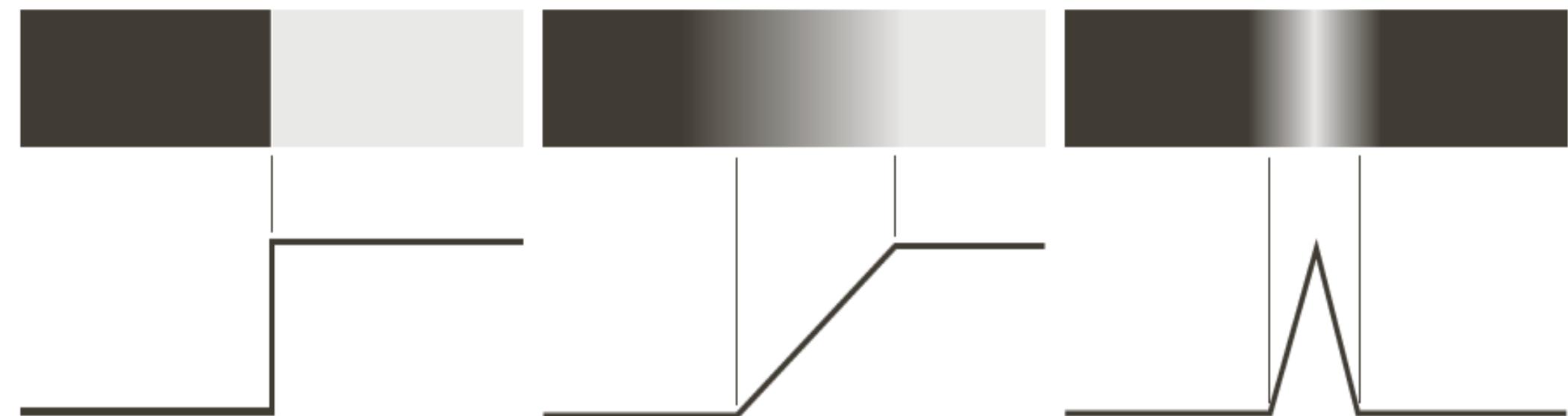
# Edge Detection

- Edge = sharp change in image intensity over space
  - Large magnitude of gradient



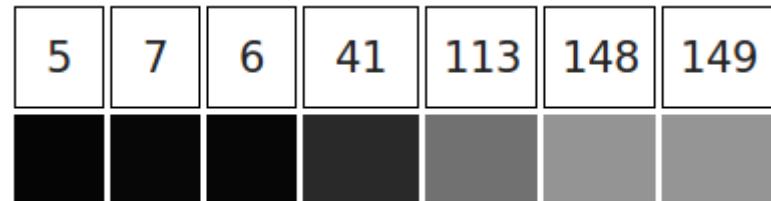
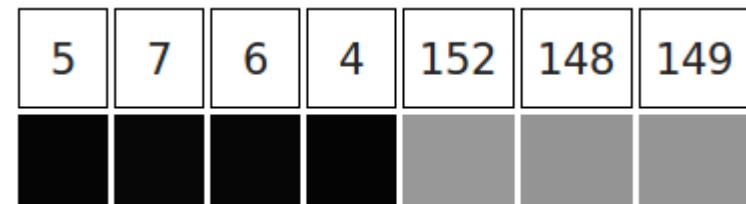
# Edge Detection

- Ideal edges
  - (1) Step edge
  - (2) Ramp edge
  - (3) Double edge / roof edge



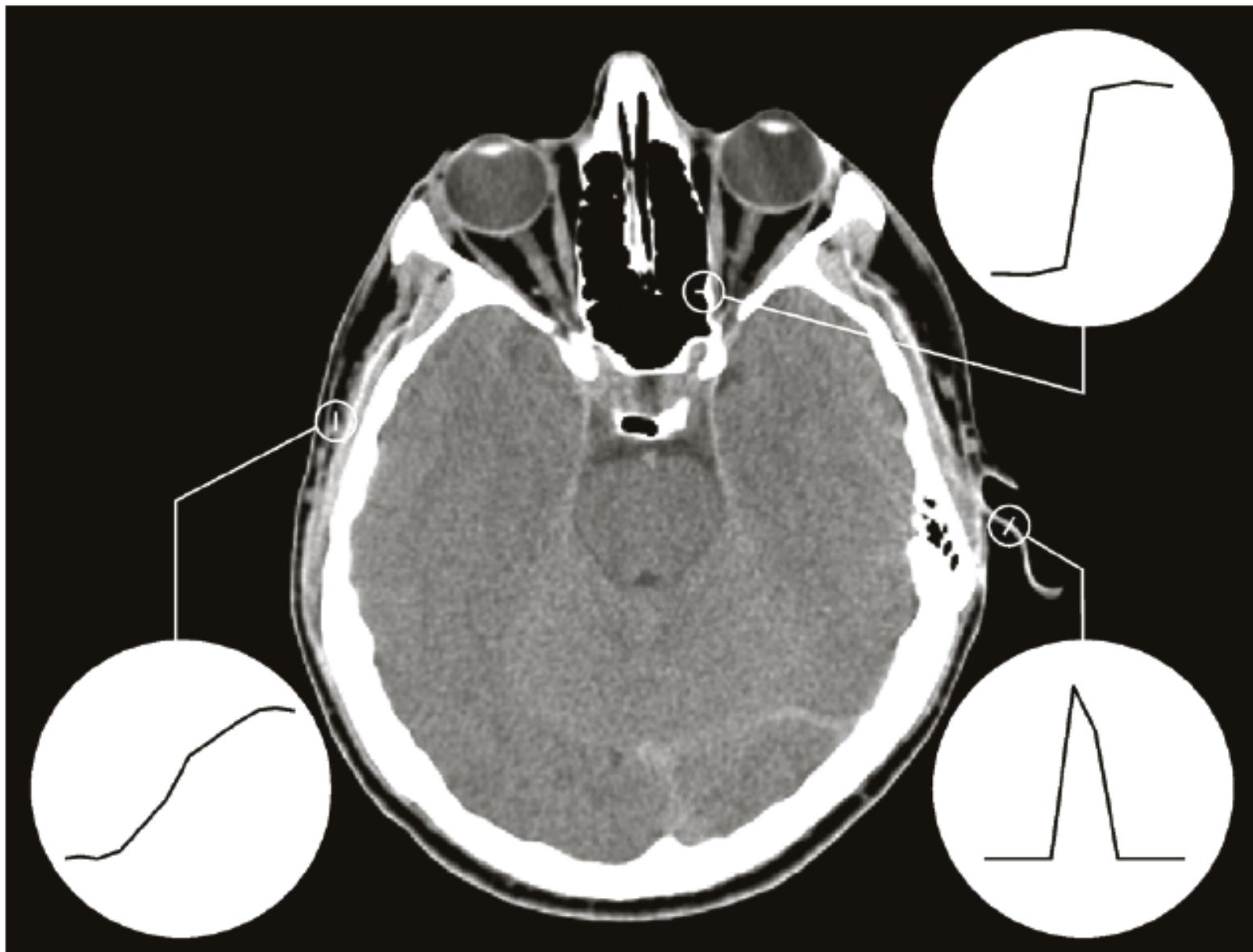
# Edge Detection

- Non-trivial, ambiguous
  - Whether to call some intensity change an edge or not ?
  - 1D image with a clear edge
  - 1D image where edges are unclear



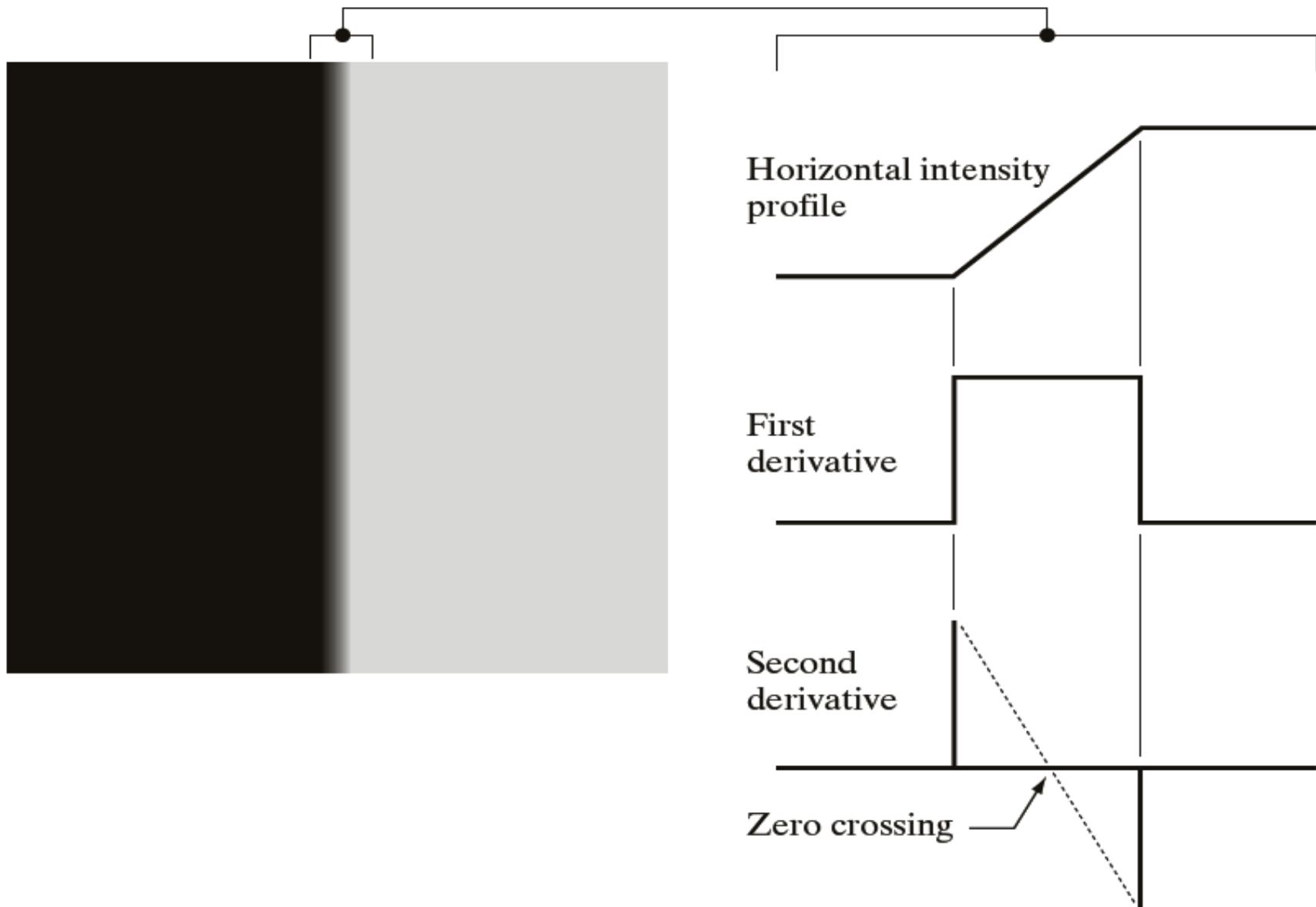
# Edge Detection

- Edges in the real world → ramp edges



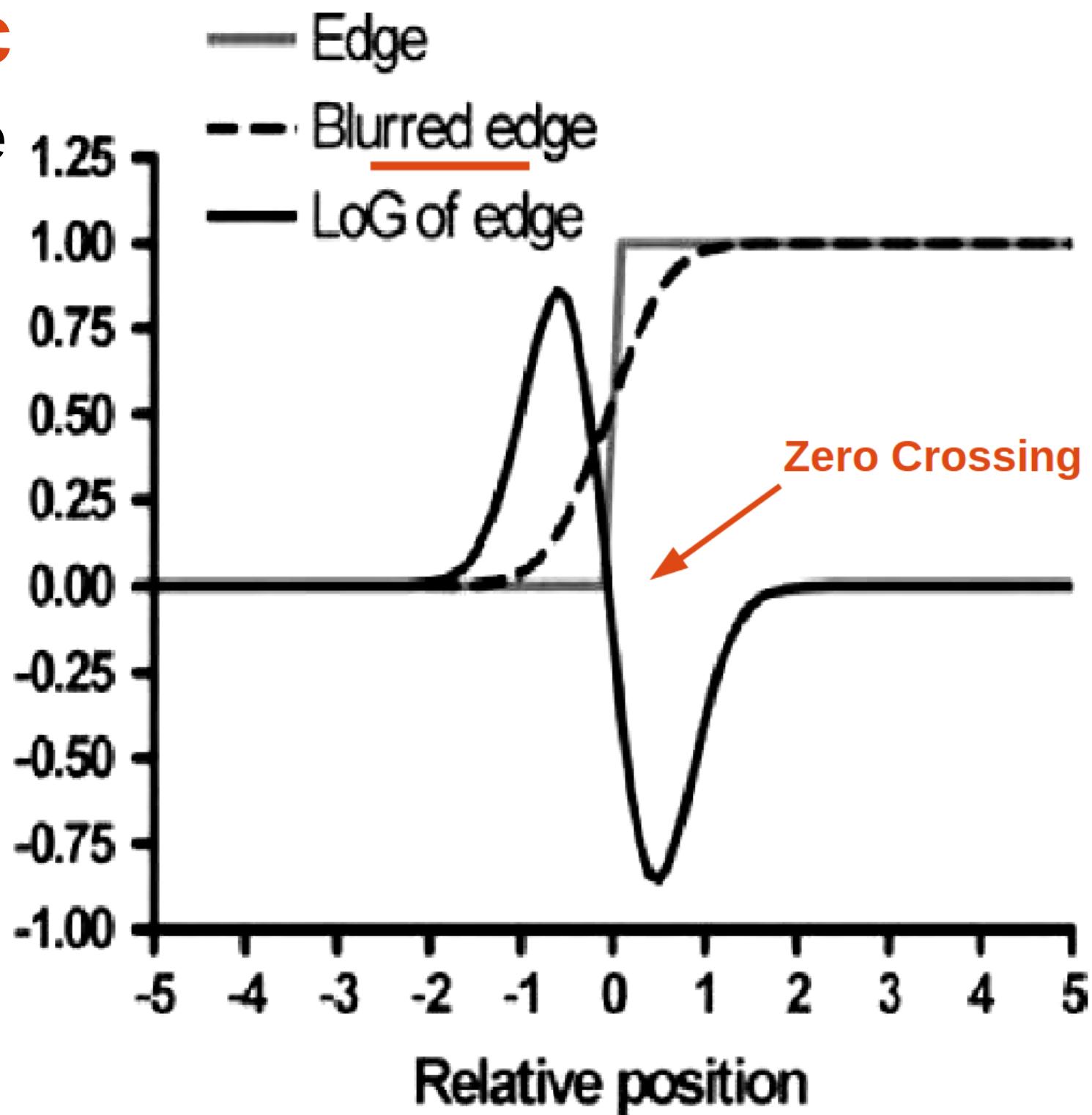
# Edge Detection

- Ideal (ramp) edge



# Edge Detection

- A (ramp) edge
  - Blurred



# Edge Detection

- “Location” of an edge can be determined by the location of zero-crossing of Laplacian

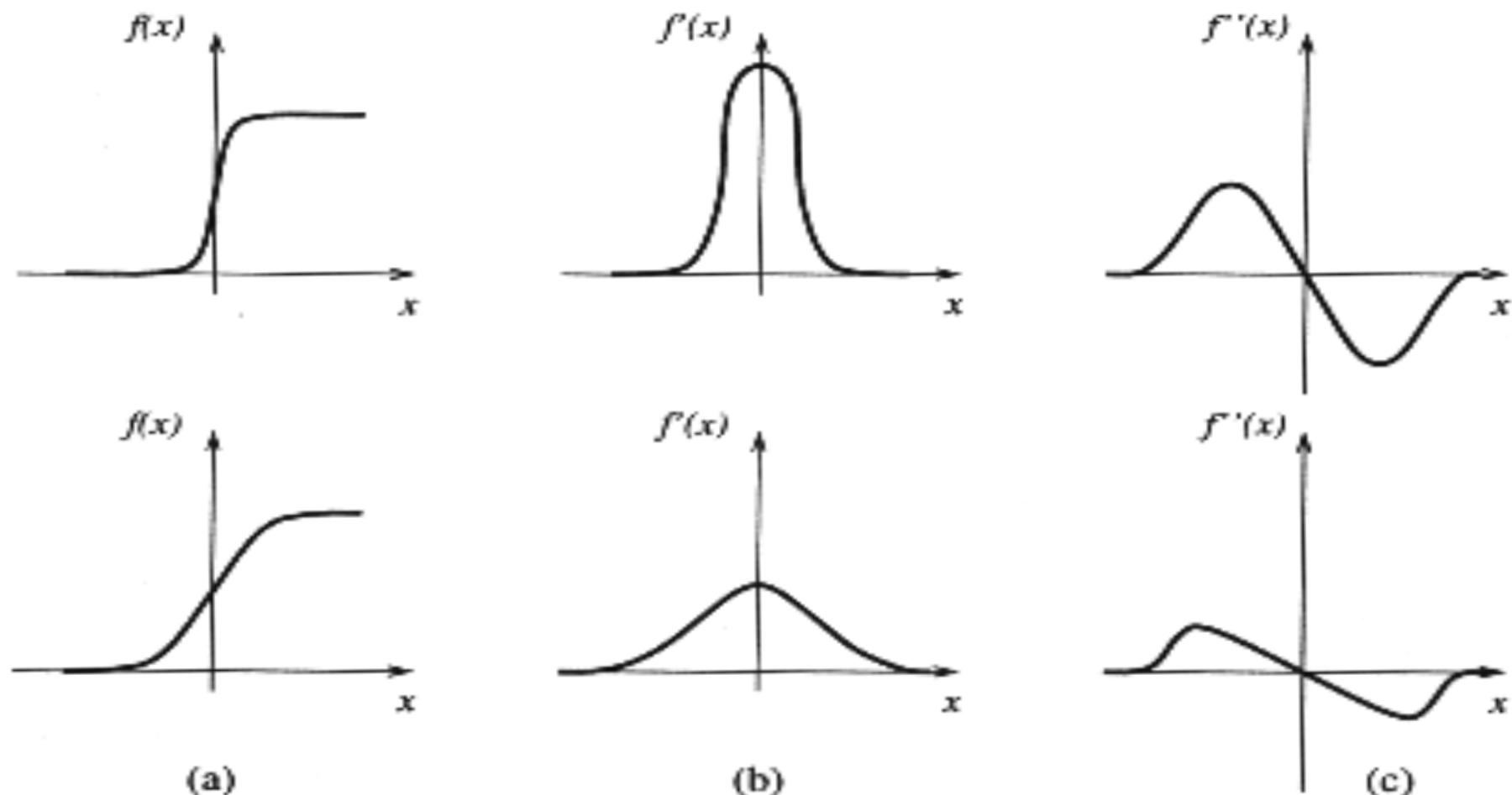
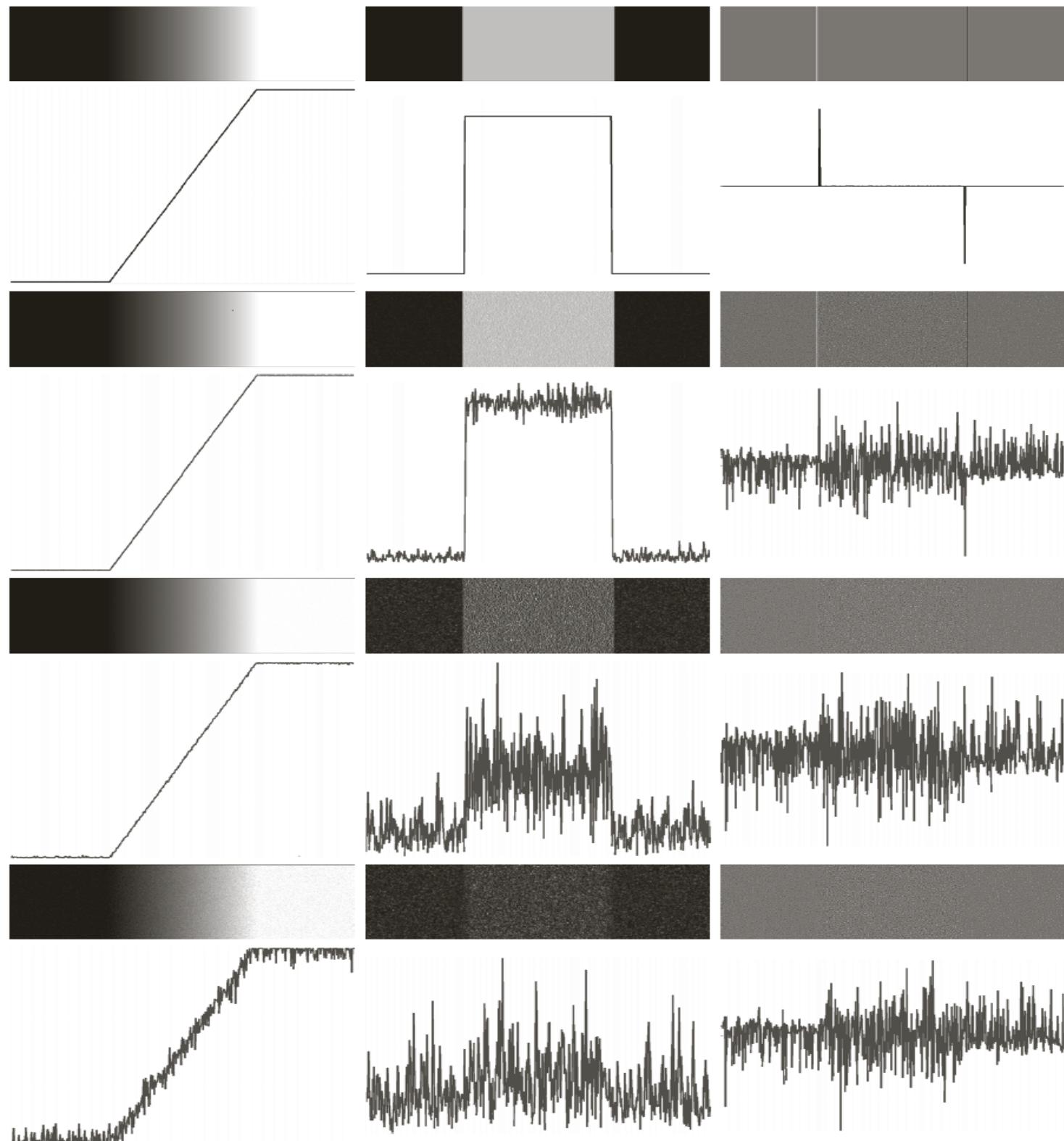


Figure 4.20: 1D edge profile of the zero-crossing.

# Edge Detection

- A (ramp) edge
  - Noisy



# Edge Detection

- Line detection
  - Masks capturing directional derivatives along different directions

-1	-1	-1	2	-1	-1	-1	2	-1	-1	-1	2
2	2	2	-1	2	-1	-1	2	-1	-1	-1	2
-1	-1	-1	-1	-1	2	-1	2	-1	2	-1	-1

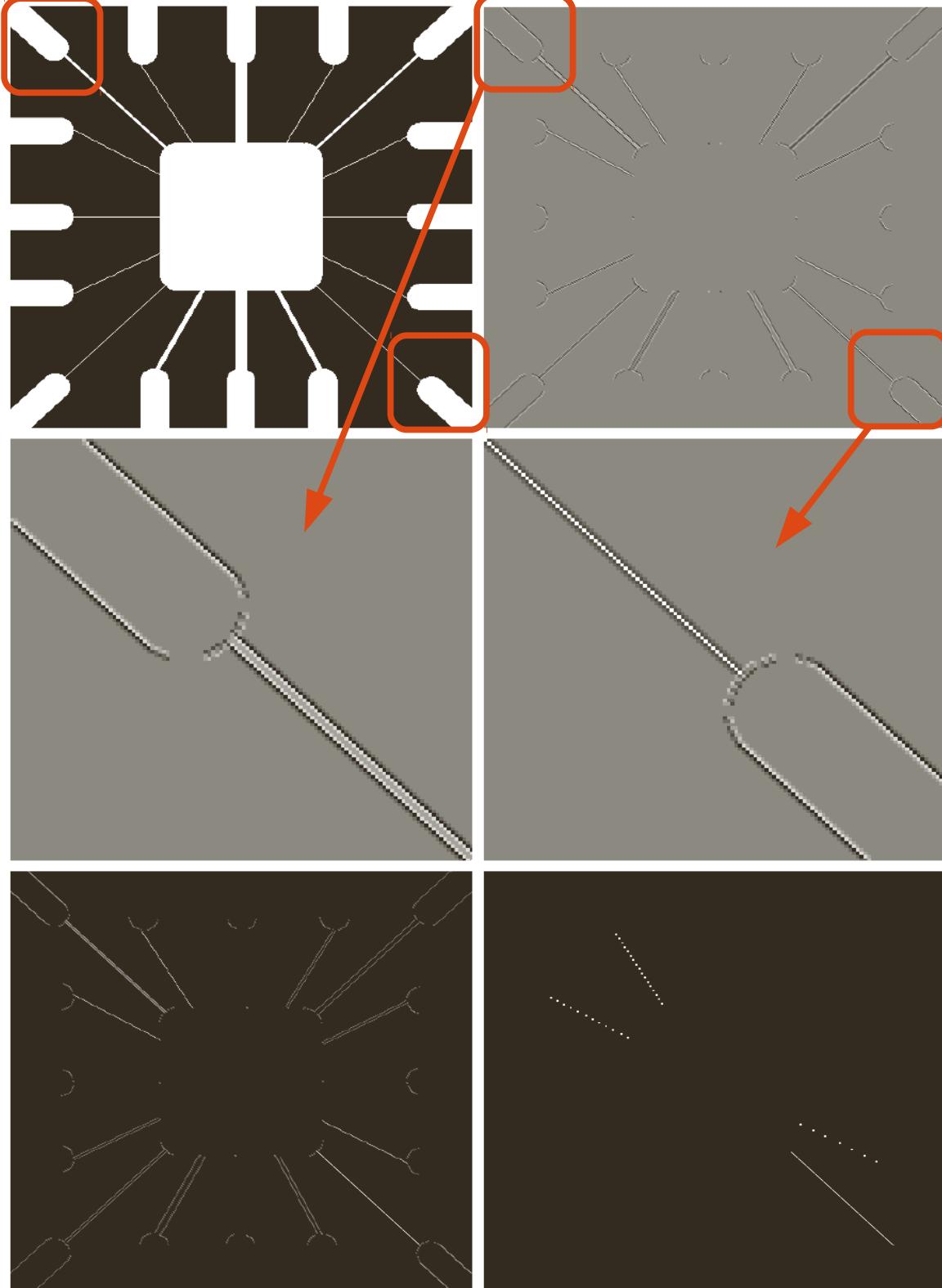
Horizontal                    +45°                    Vertical                    -45°

- Line detection

a	b
c	d
e	f

**FIGURE 10.7**

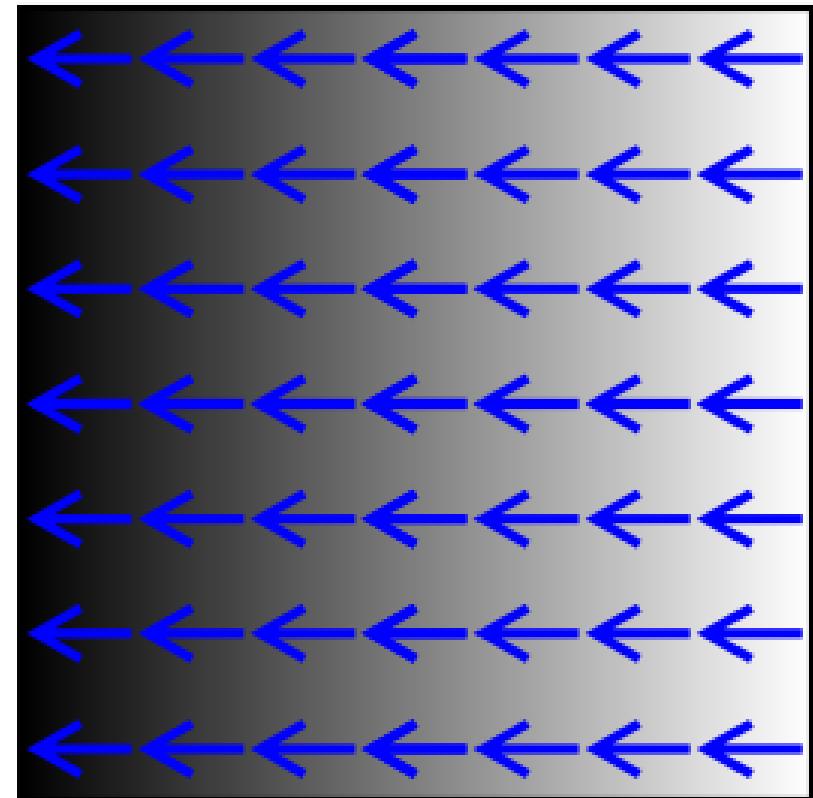
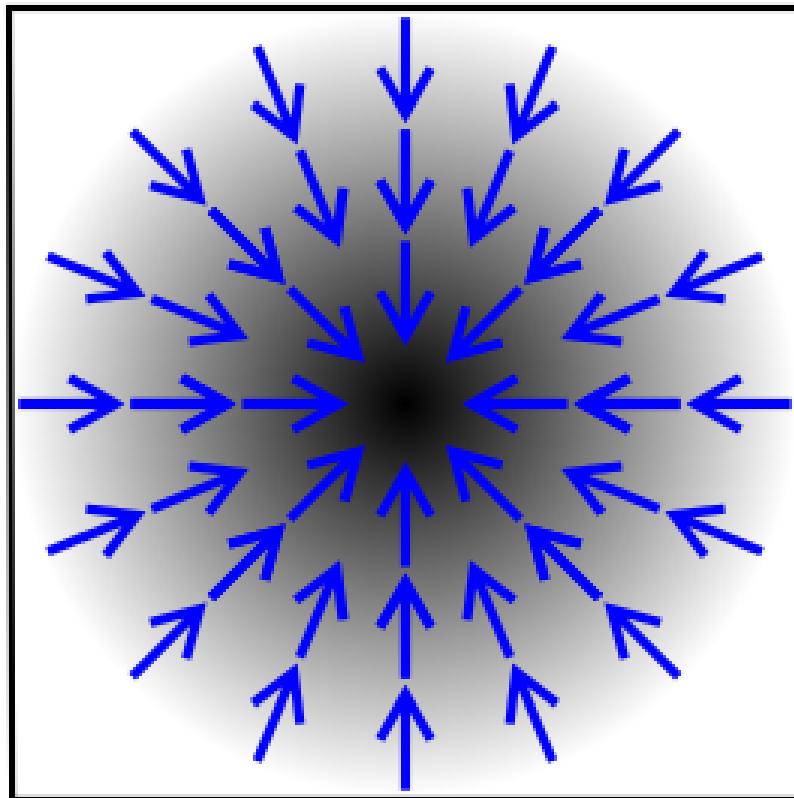
- (a) Image of a wire-bond template.
- (b) Result of processing with the  $+45^\circ$  line detector mask in Fig. 10.6.
- (c) Zoomed view of the top left region of (b).
- (d) Zoomed view of the bottom right region of (b).
- (e) The image in (b) with all negative values set to zero.
- (f) All points (in white) whose values satisfied the condition  $g \geq T$ , where  $g$  is the image in (e). (The points in (f) were enlarged to make them easier to see.)



# Edge Detection

- **Gradient**

- Can be used for edge detection
- Gradient (column) vector = [  $df/dx \ df/dy$  ]' = [  $G_x \ G_y$  ]'



# Edge Detection

- Masks for computing gradient [ Gx Gy ]
  - Averaging in neighborhood  
→ noise reduction
  - **Prewitt** operators

$$\begin{bmatrix} -1 & 0 & +1 \\ -1 & 0 & +1 \\ -1 & 0 & +1 \end{bmatrix} \quad \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ +1 & +1 & +1 \end{bmatrix}$$

- Prewitt operators are separable

$$\begin{bmatrix} -1 & 0 & +1 \\ -1 & 0 & +1 \\ -1 & 0 & +1 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$$

# Edge Detection

- Masks for computing gradient [ Gx Gy ]

- Averaging in neighborhood

- noise reduction

- **Sobel** operators

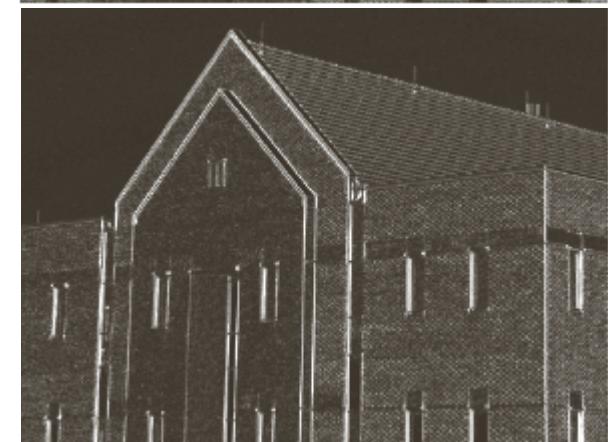
$$\begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix} \quad \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- Sobel operators are separable

$$\begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & +1 \end{bmatrix}$$

# Edge Detection

- Gradient (sobel)
  - Test image
  - Gradient x-component magnitude  
→  $|df/dx| = |G_x|$
  - Gradient y-component magnitude  
→  $|df/dy| = |G_y|$
  - Gradient magnitude

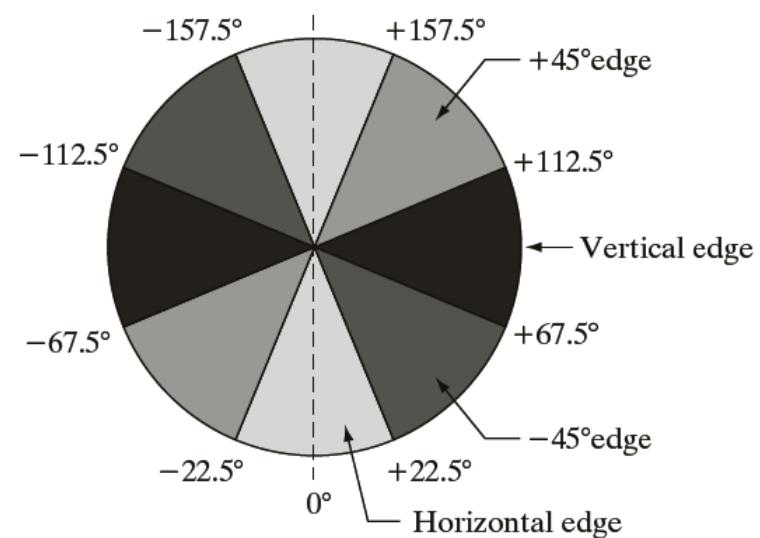
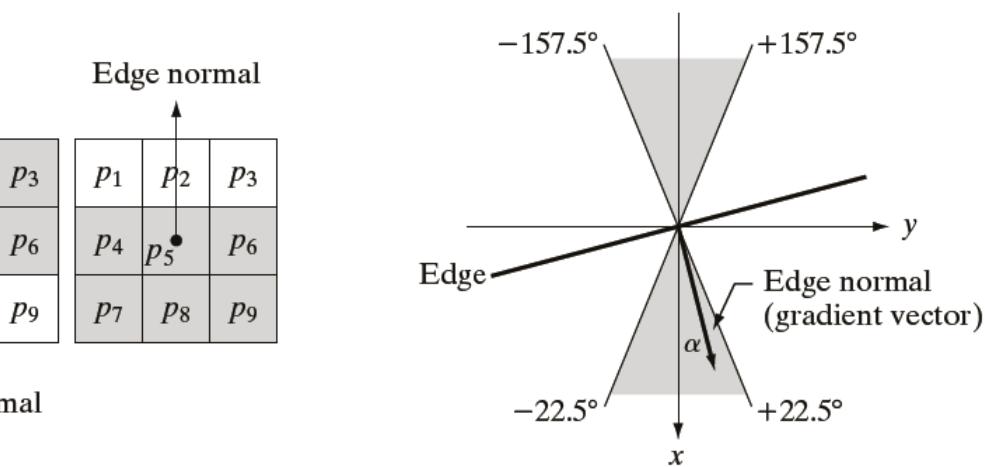
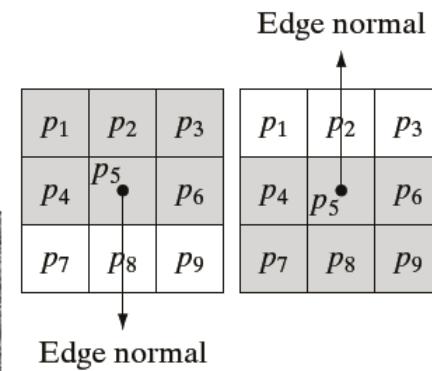
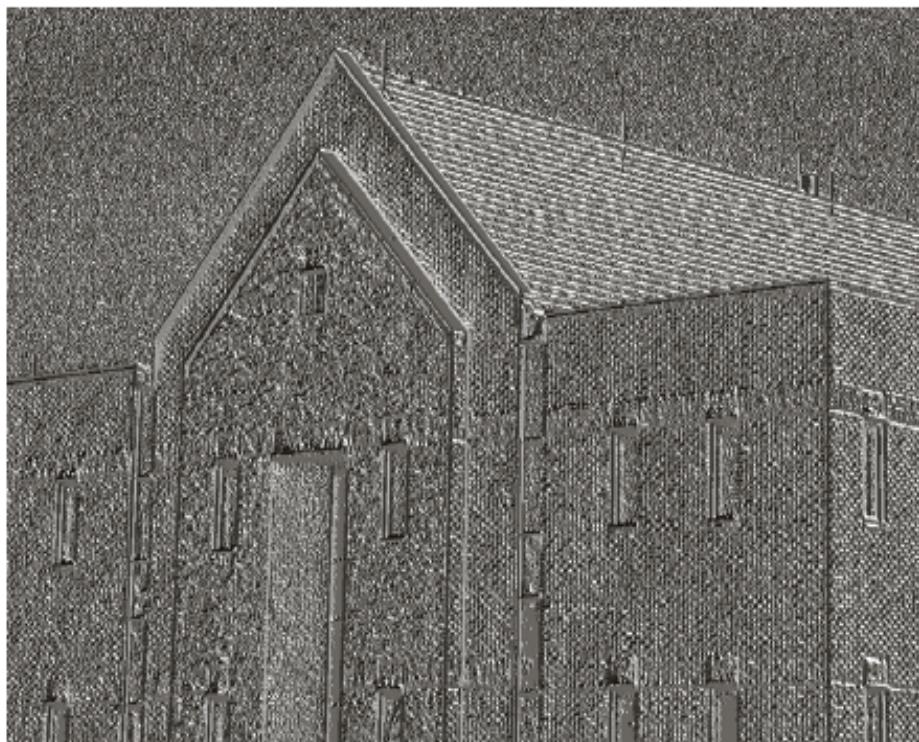


$$G = \sqrt{G_x^2 + G_y^2}$$



# Edge Detection

- Gradient (sobel)
  - Gradient direction (angle)  $\Theta = \text{atan2}(\mathbf{G}_y, \mathbf{G}_x)$ 
    - Non-informative for edge detection
    - Gives direction of edge



# Edge Detection

- Sobel gradient after smoothing ( $5 \times 5$  mean filter)



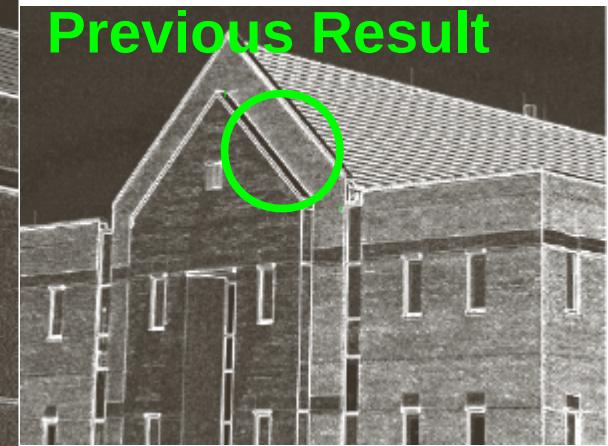
a	b
c	d

**FIGURE 10.18**

Same sequence as in Fig. 10.16, but with the original image smoothed using a  $5 \times 5$  averaging filter prior to edge detection.



**Previous Result**



# Edge Detection

- **Marr-Hildreth algorithm for edge detection (1980)**

(1/2) Convolve image with LoG

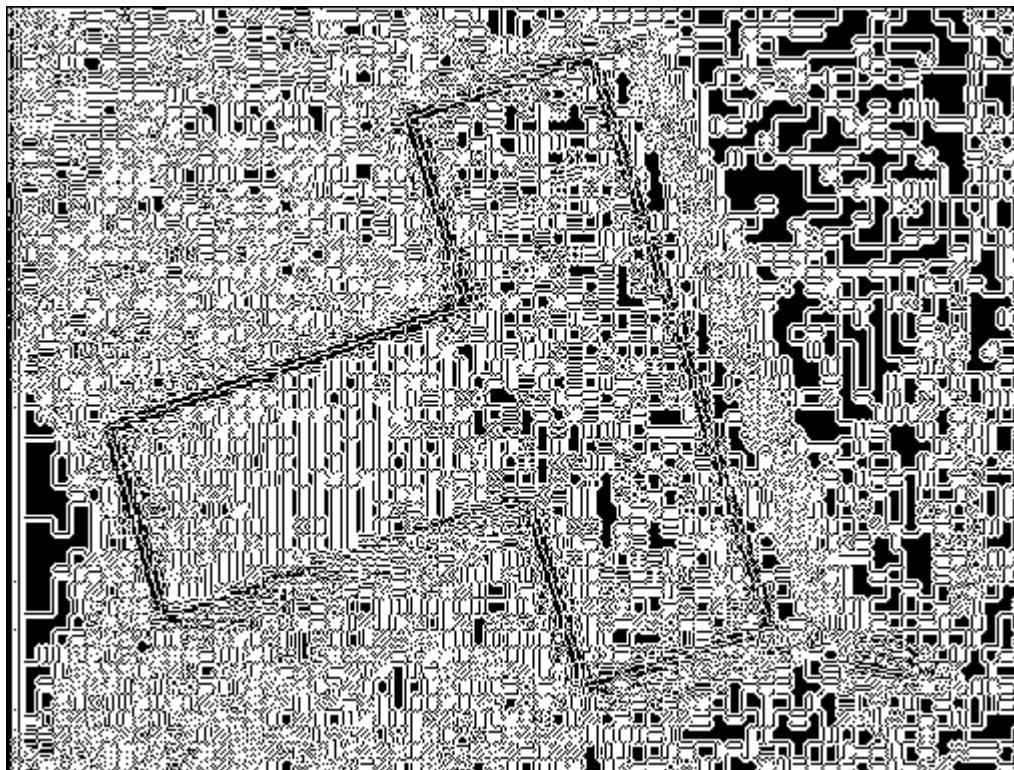
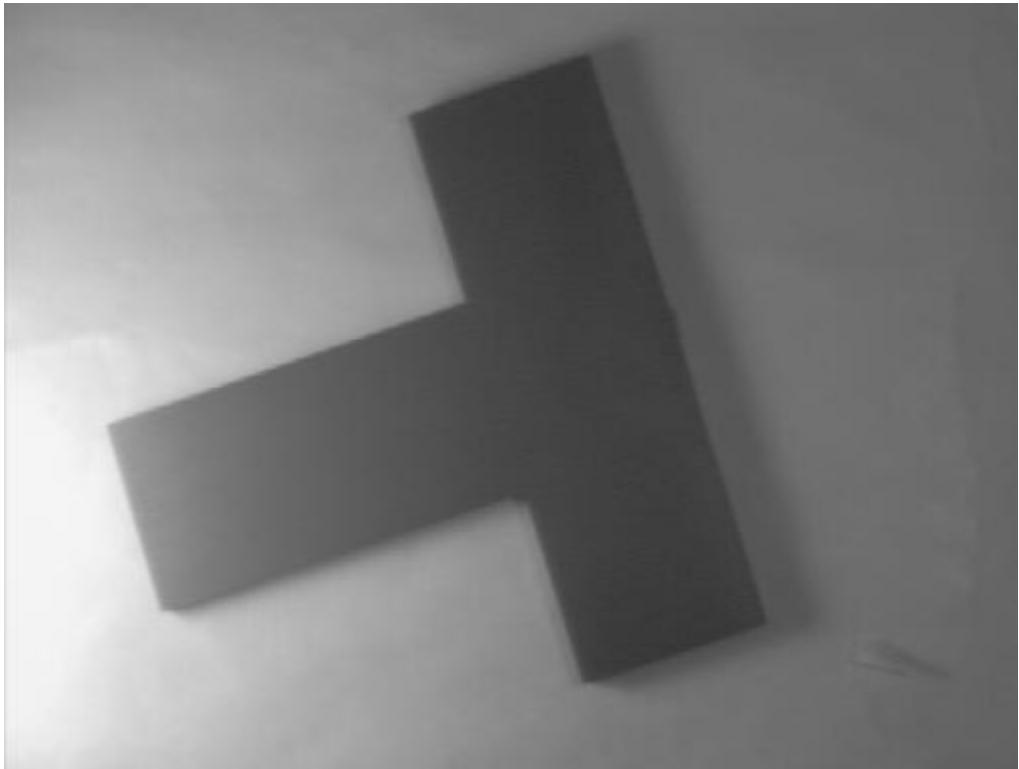
- Approximated as DoG

(2/2) Detect zero crossings

- Compare signs of pixel intensities of neighbors
  - Left versus right
  - Up versus down
  - NW versus SE
  - NE versus SW
- If **signs different** and **magnitude of difference > threshold**, then, edge found

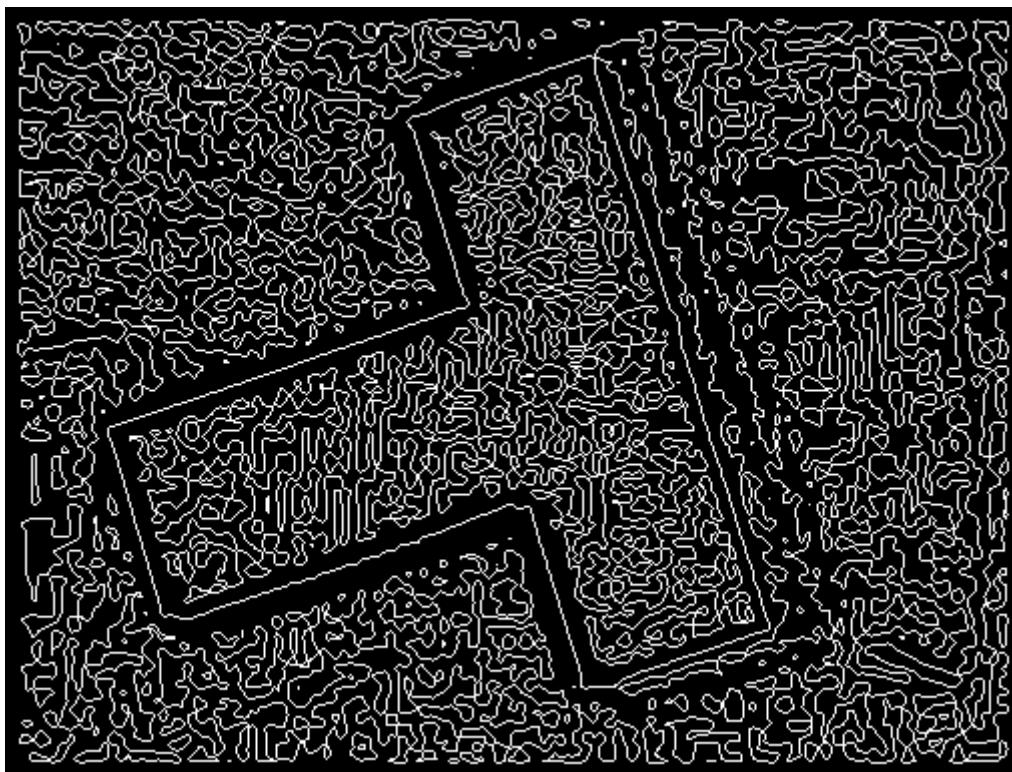
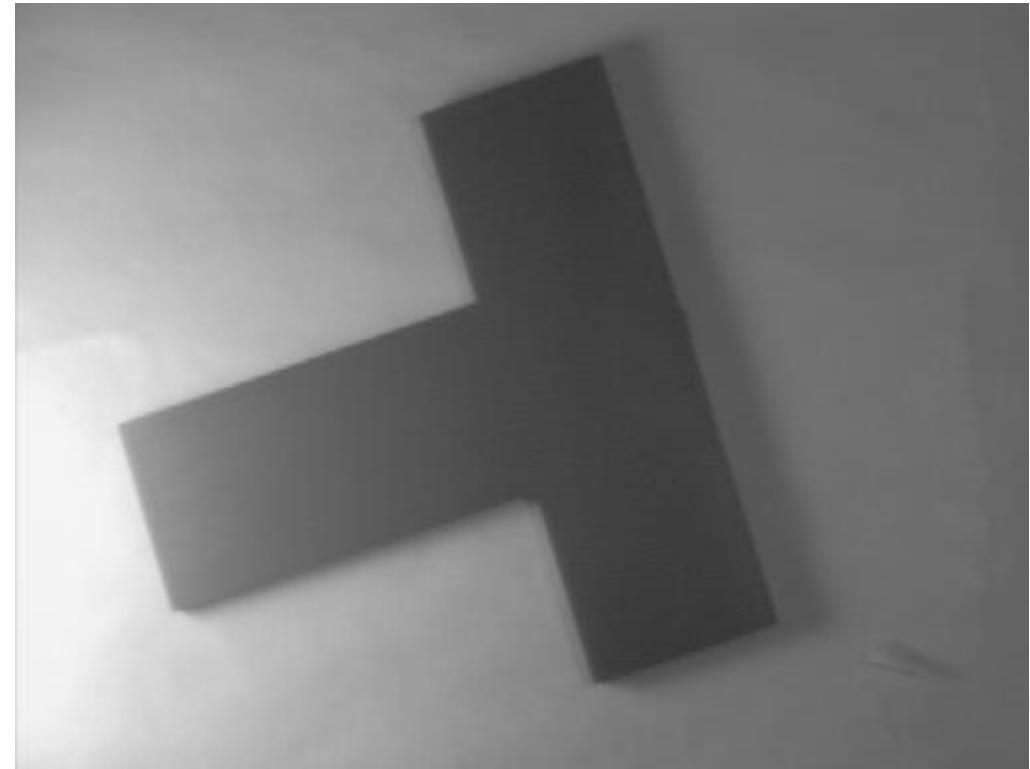
# Edge Detection

- Marr-Hildreth algorithm for edge detection
  - Gaussian variance = 0
  - Threshold = 0



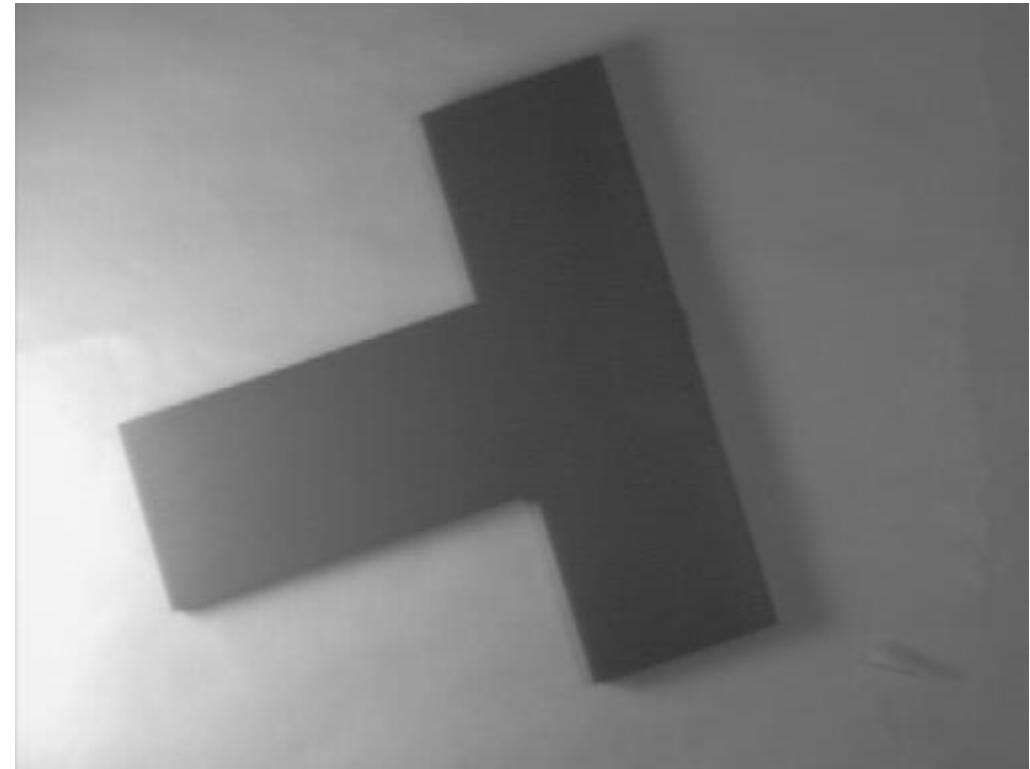
# Edge Detection

- Marr-Hildreth algorithm for edge detection
  - Gaussian variance  $> 0$
  - Threshold = 0



# Edge Detection

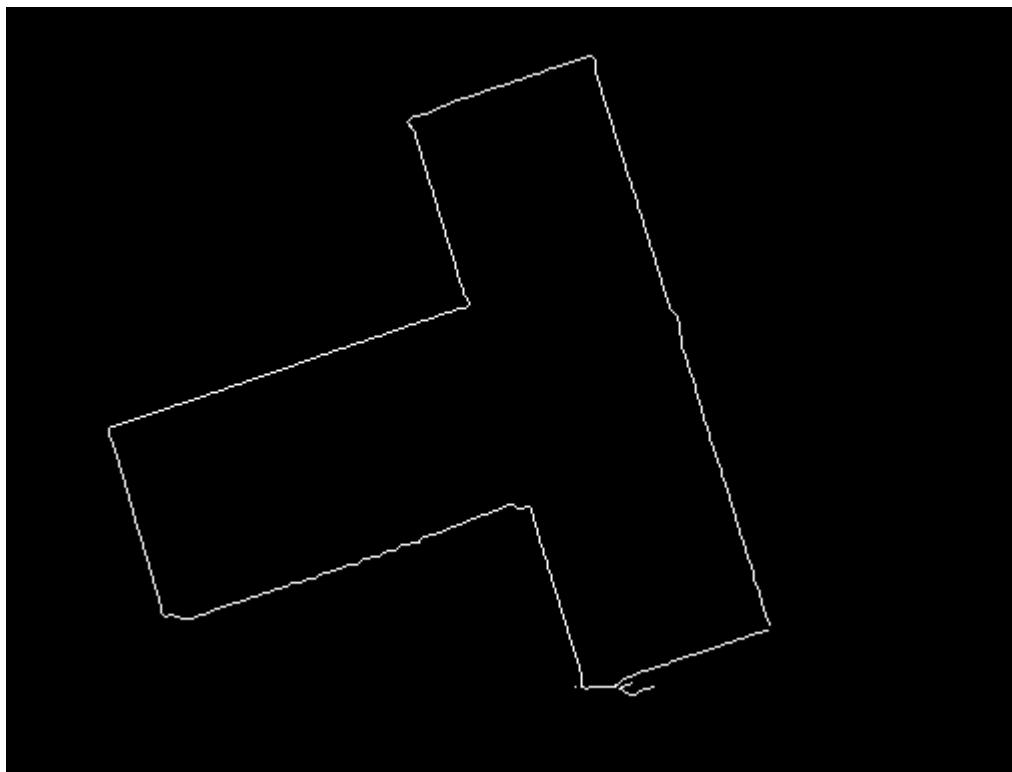
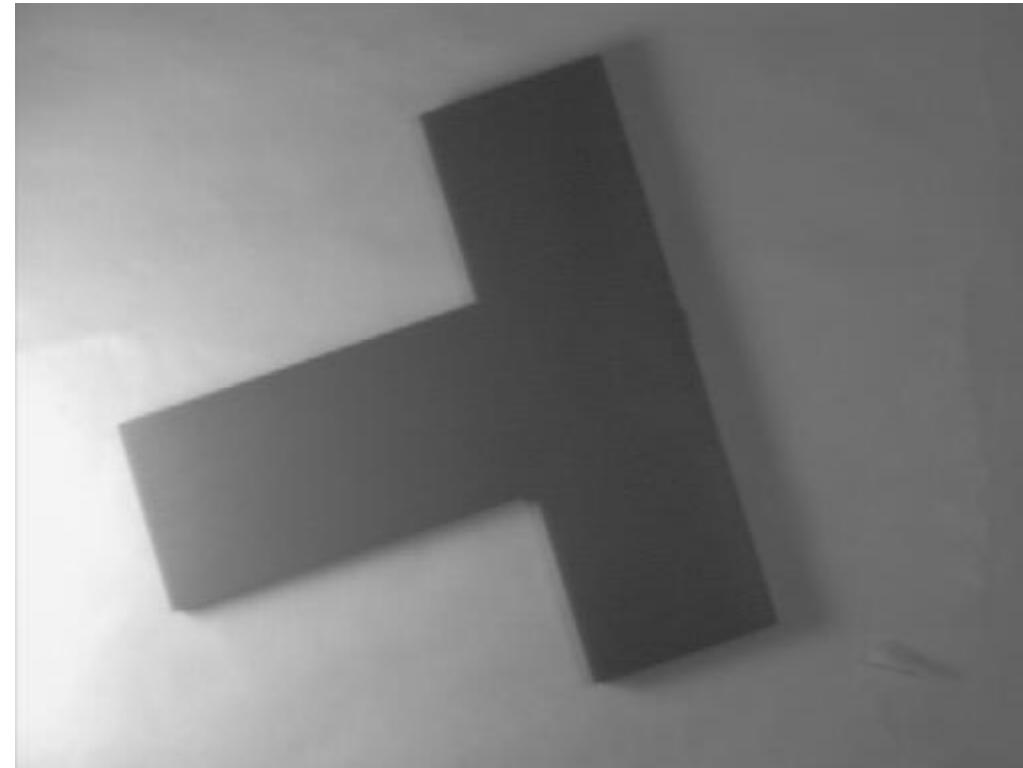
- Marr-Hildreth algorithm for edge detection
  - Gaussian variance  $> 0$
  - Threshold  $> 0$



Parameter Tuning :  
Sub-optimal

# Edge Detection

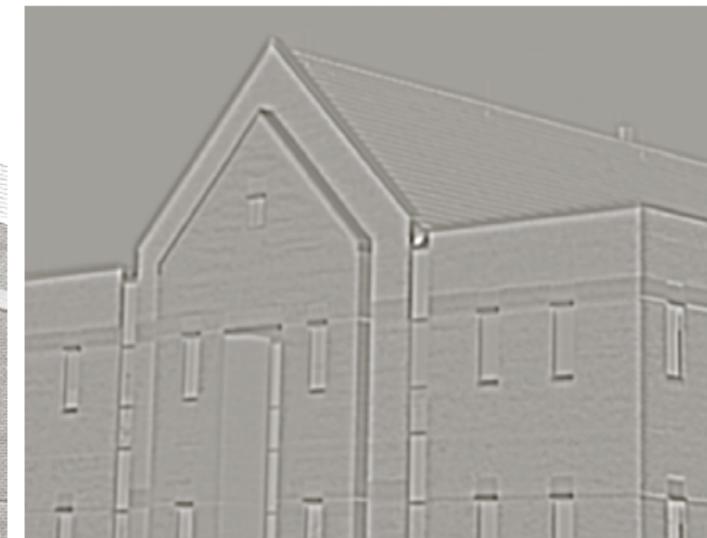
- Marr-Hildreth algorithm for edge detection
  - Gaussian variance  $> 0$
  - Threshold  $> 0$



Parameter Tuning : Good

# Edge Detection

- Marr-Hildreth algorithm for edge detection (1980)
  - Gives 1-pixel thick edges
  - Top row:  
image,  
LoG
  - Bottom row:  
detected edges  
with two  
different  
thresholds



# Edge Detection

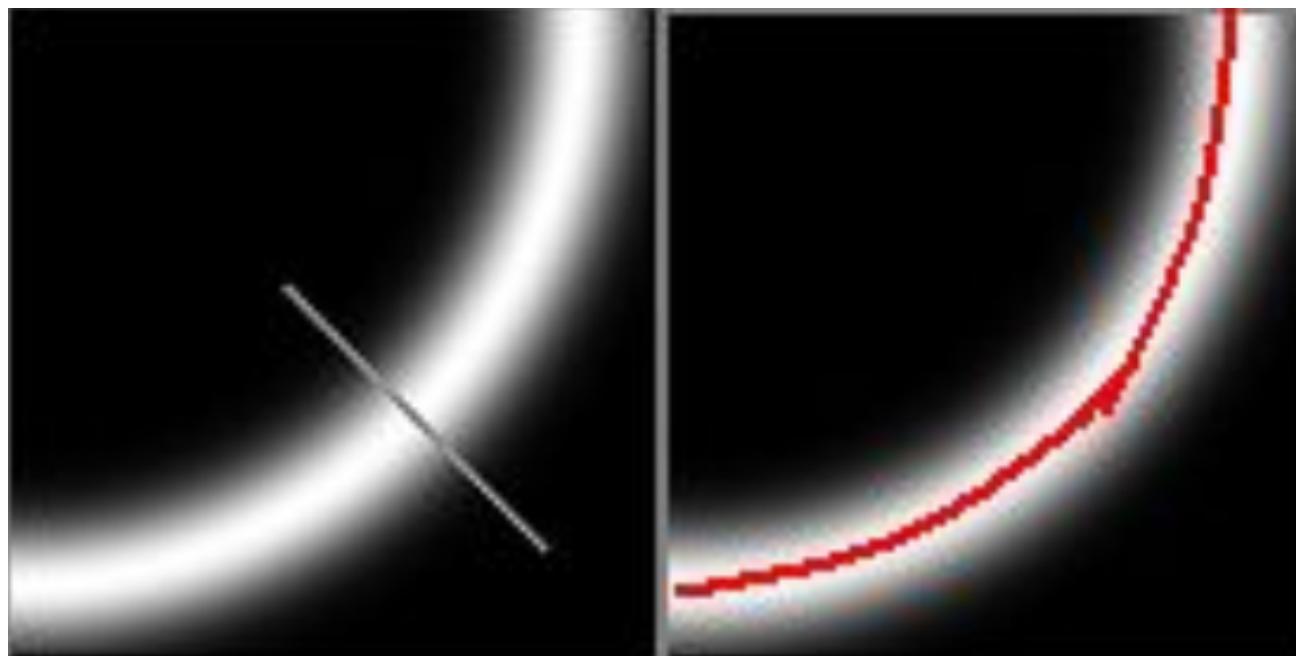
- David Marr
  - Neuroscientist, psychologist
  - CS work in artificial intelligence, image processing
  - After PhD in physiology, he got interested in visual processing
  - Marr Prize
    - One of the most prestigious awards in computer vision

# Edge Detection

- Canny edge detection
  - John Canny. 1986.
    - (1/4) Gaussian smoothing to reduce noise
    - (2/4) Gradient computation at each pixel  $\mathbf{G} = \sqrt{\mathbf{G}_x^2 + \mathbf{G}_y^2}$ 
      - Positive and negative directions equivalent  $\Theta = \text{atan2}(\mathbf{G}_y, \mathbf{G}_x)$
    - (3/4) Edge **thinning** by **non-maximum suppression**
      - See next ...
    - (4/4) Edge **tracing** via **hysteresis thresholding**
      - See next ...

# Edge Detection

- Canny edge detection
  - (1) Gaussian smoothing to reduce noise
  - (2) Gradient computation at each pixel
  - (3) Edge **thinning** by **non-maximum suppression**
    - Mark pixels where gradient magnitude is  $\geq$  that of neighbors along the gradient direction (across the edge)
    - This may require interpolation



# Edge Detection

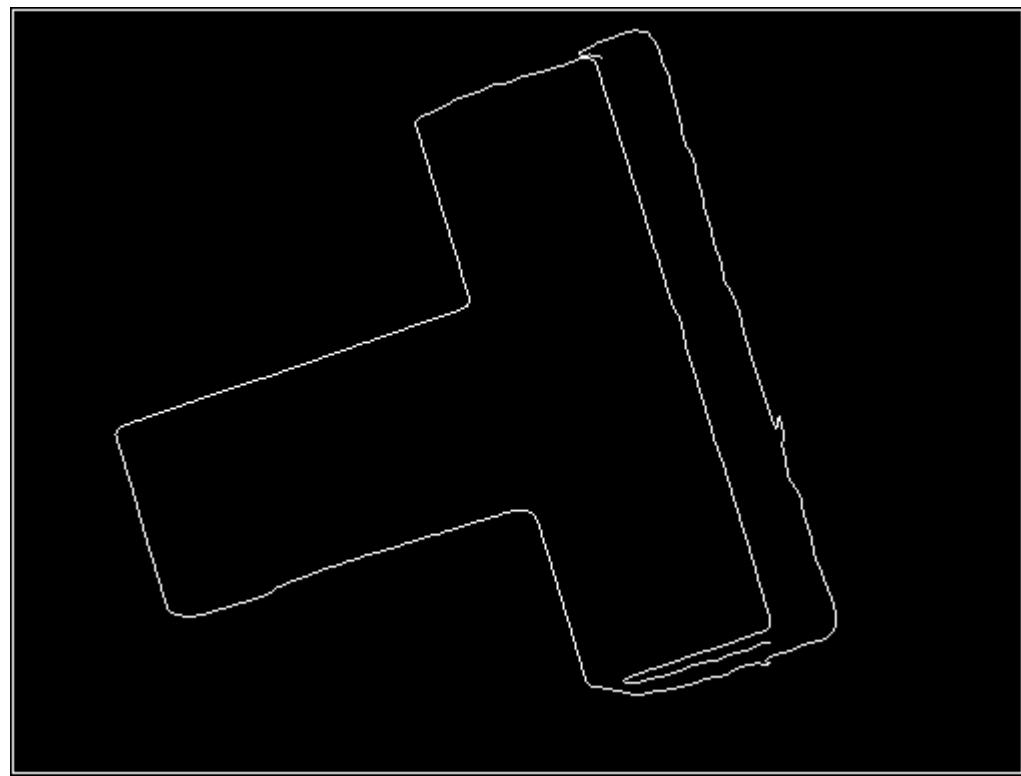
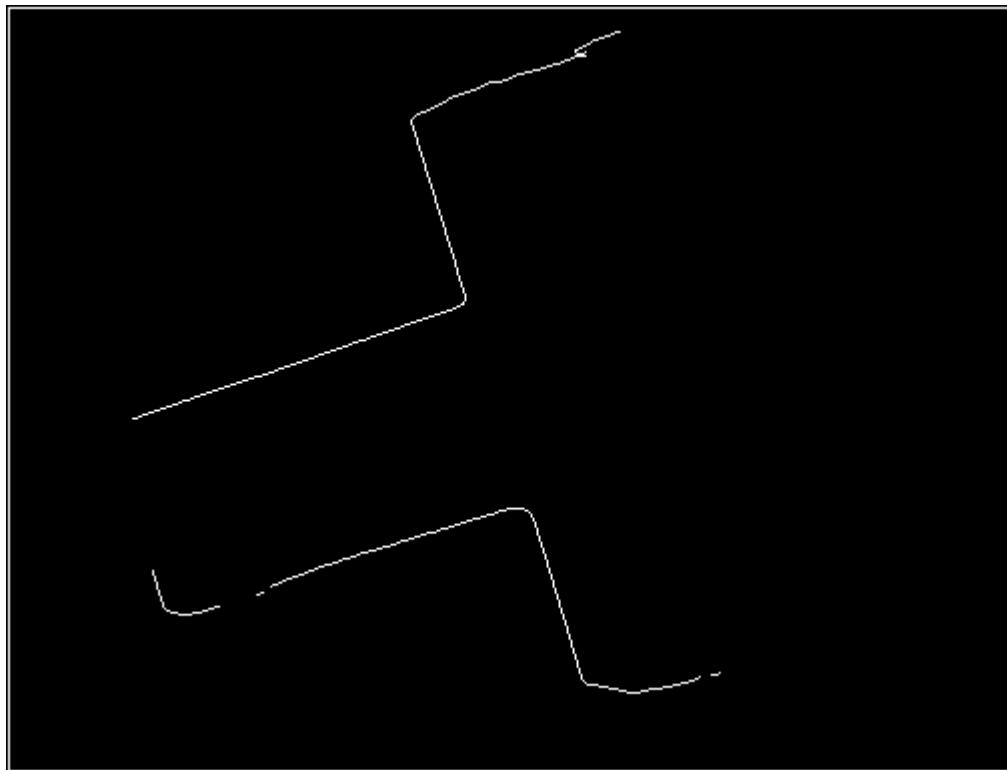
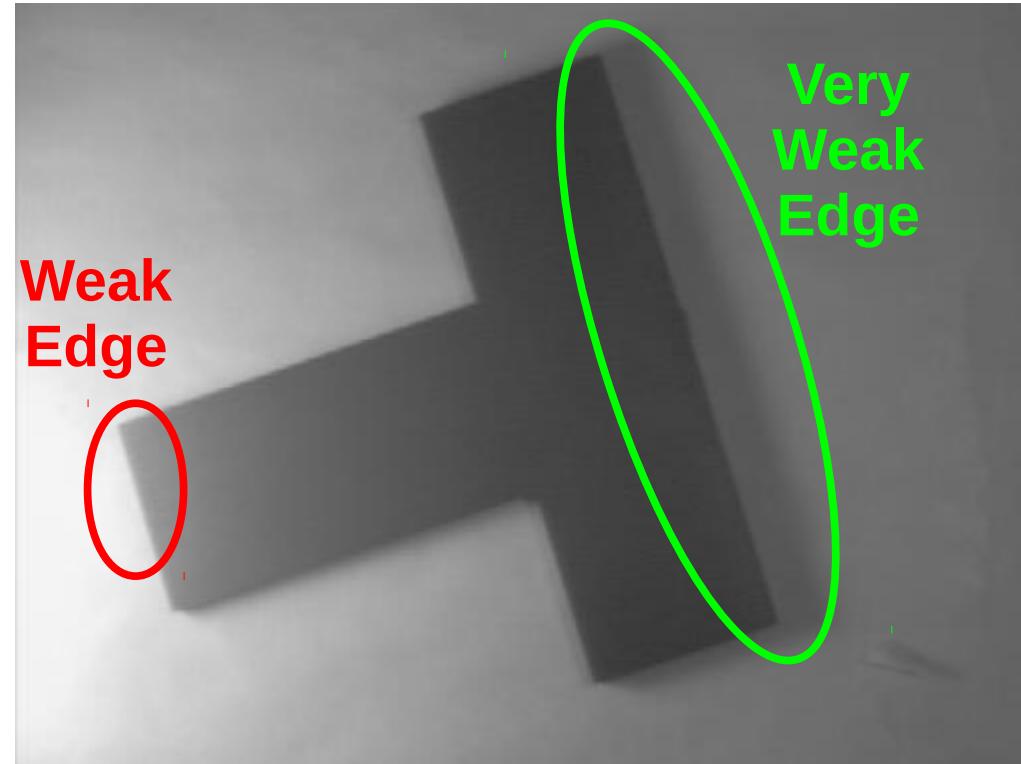
- Canny edge detection
  - (1) Gaussian smoothing to reduce noise
  - (2) Gradient computation at each pixel
  - (3) Edge thinning by non-maximum suppression
  - (4) Edge **tracing via hysteresis thresholding**
    - Difficult to define one threshold on gradient magnitude to detect pixels on an edge
    - Assume: edges are continuous curves
    - Define 2 thresholds: `thresholdHigh` and `thresholdLow`
    - First, select pixels where  $\text{gradient magnitude} > \text{thresholdHigh}$
    - Then, find connected path starting from selected pixels where all pixels have  $\text{gradient magnitude} > \text{thresholdLow}$

# Edge Detection

- Canny edge detection
  - Hysteresis thresholding makes following assumptions
    - (1)  $\text{PixelValue} \geq \text{thresholdHigh} \rightarrow$  pixels inside object
    - (2)  $\text{PixelValue} \leq \text{thresholdLow} \rightarrow$  pixels outside object
    - (3)  $\text{thresholdLow} < \text{PixelValue} < \text{thresholdHigh} \rightarrow$  pixel inside object if connected path exists to *object pixel* such that all pixels in path have values  $> \text{thresholdLow}$

# Edge Detection

- Canny edge detection
  - (1), (2), (3) ...
  - (4) Simple thresholding vs. Hysteresis thresholding

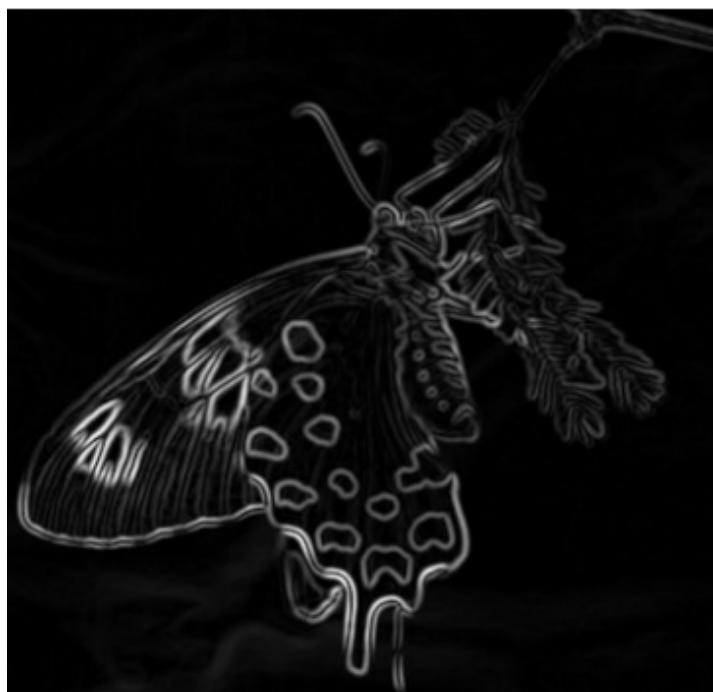
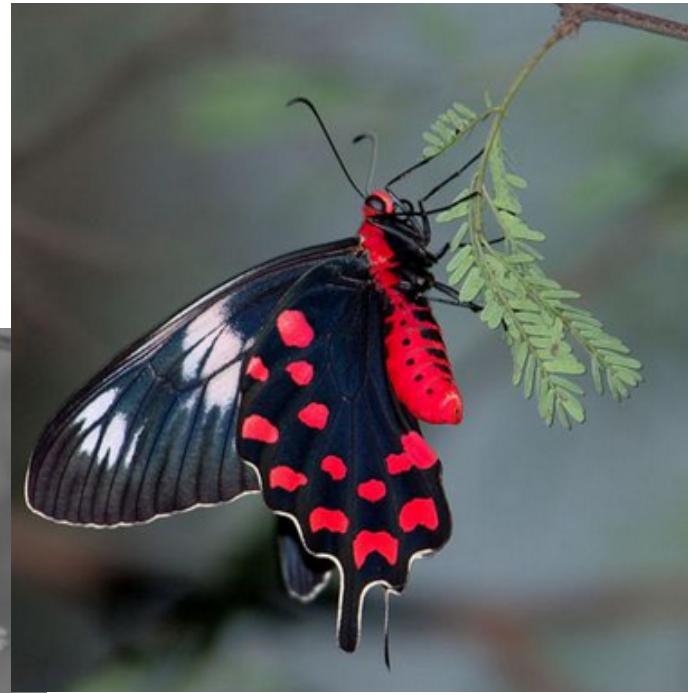


# Edge Detection

- Canny edge detection
  - Parameters
    - Variance of Gaussian used for smoothing
    - High threshold on gradient magnitude
    - Low threshold on gradient magnitude

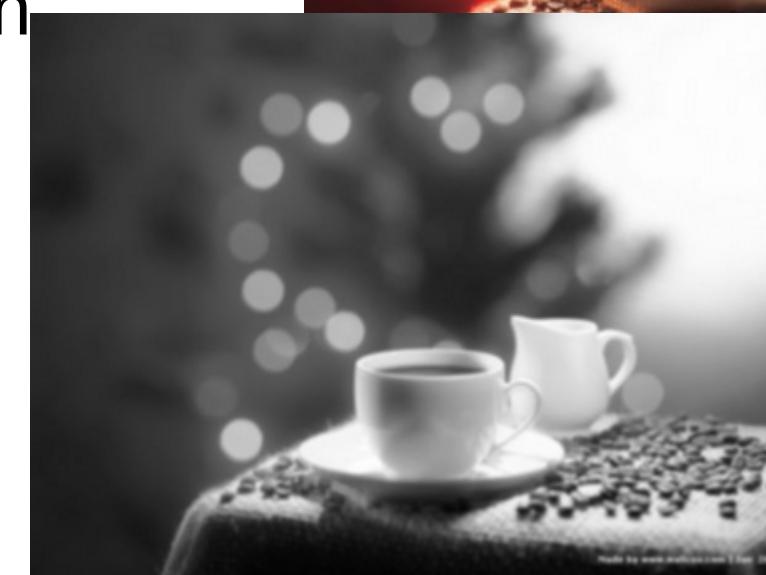
# Edge Detection

- Canny edge detection
  - Smoothed gradient
  - Non-maximum suppression
  - Hysteresis threshold



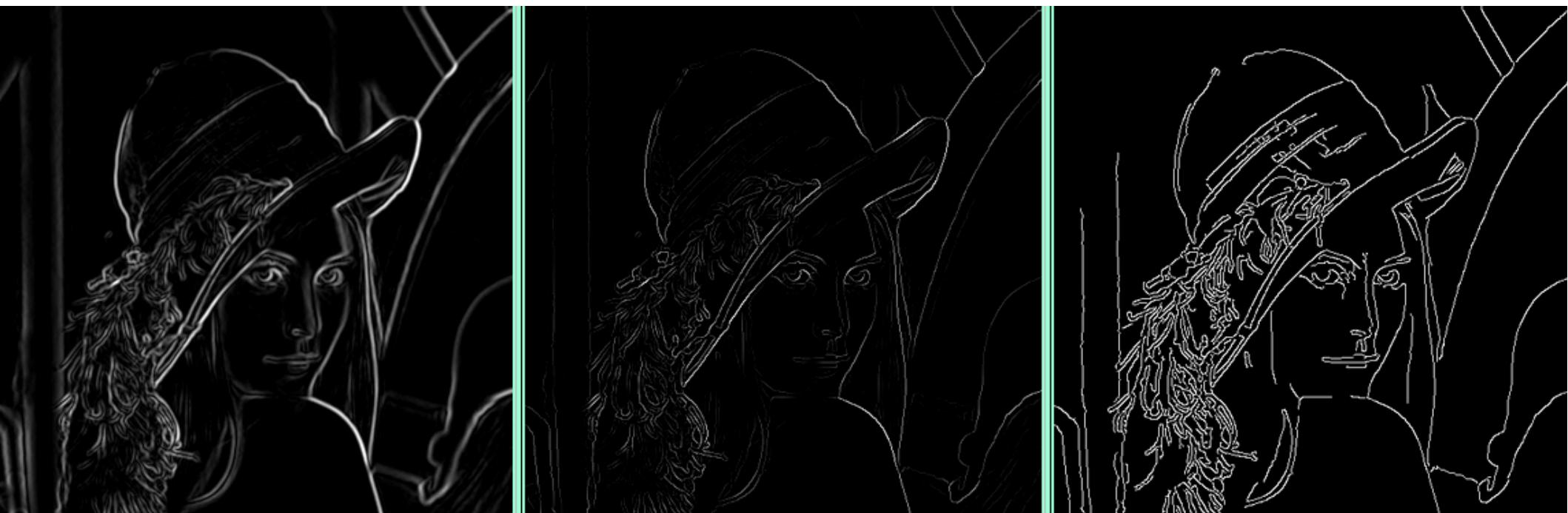
# Edge Detection

- Canny edge detection
  - Smoothed gradient
  - Non-maximum suppression
  - Hysteresis threshold



# Edge Detection

- Canny edge detection
  - Smoothed gradient
  - Non-maximum suppression
  - Hysteresis threshold



# Edge Detection

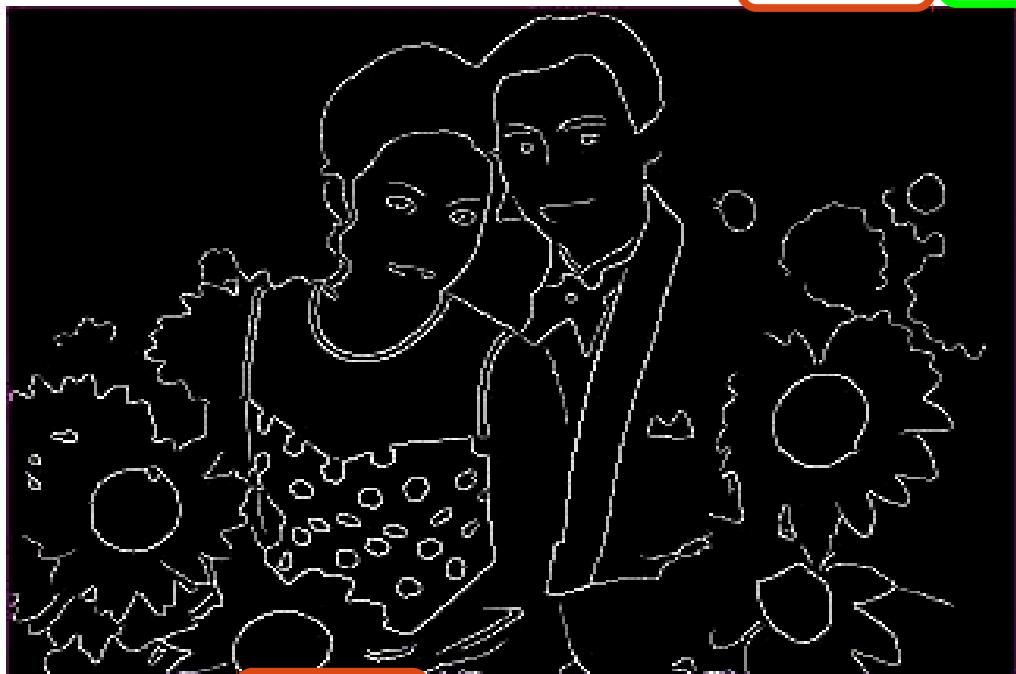
- Canny edge detection
  - Smoothed gradient
  - Non-maximum suppression
  - Hysteresis threshold



## Canny Edge Detection.



Sigma= 1, Low= 0.4, High= 0.8



Sigma= 2, Low= 0.4, High= 0.8



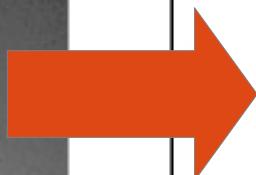
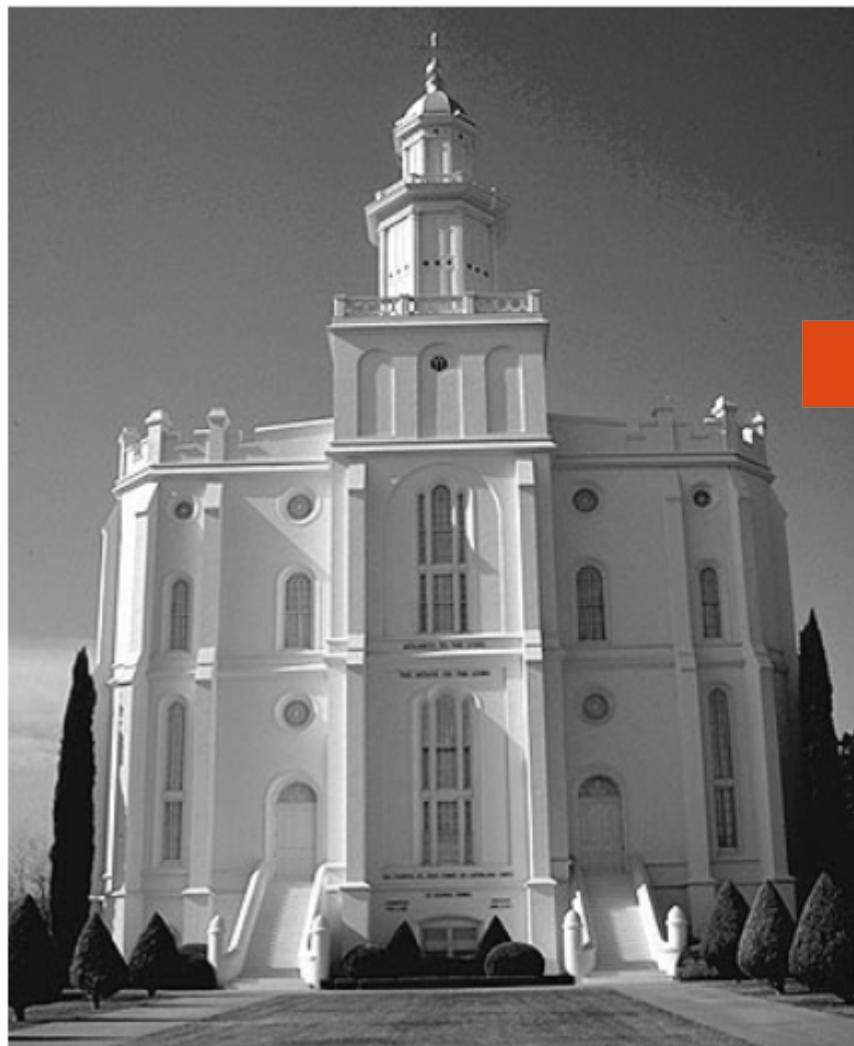
Sigma= 1, Low= 0.3, High= 0.7

# Edge Detection

- Corner detection
  - Moravec corner detection algorithm. 1980.
  - Consider a pixel “p” as a corner of an object when:
    - Low similarity between:
      - (1) a patch around “p” and
      - (2) another patch around any neighbor “q” of “p”
    - Threshold on similarity
    - Similarity captured via
      - (1) sum of squared differences → dissimilarity OR
      - (2) (normalized) cross correlation → similarity

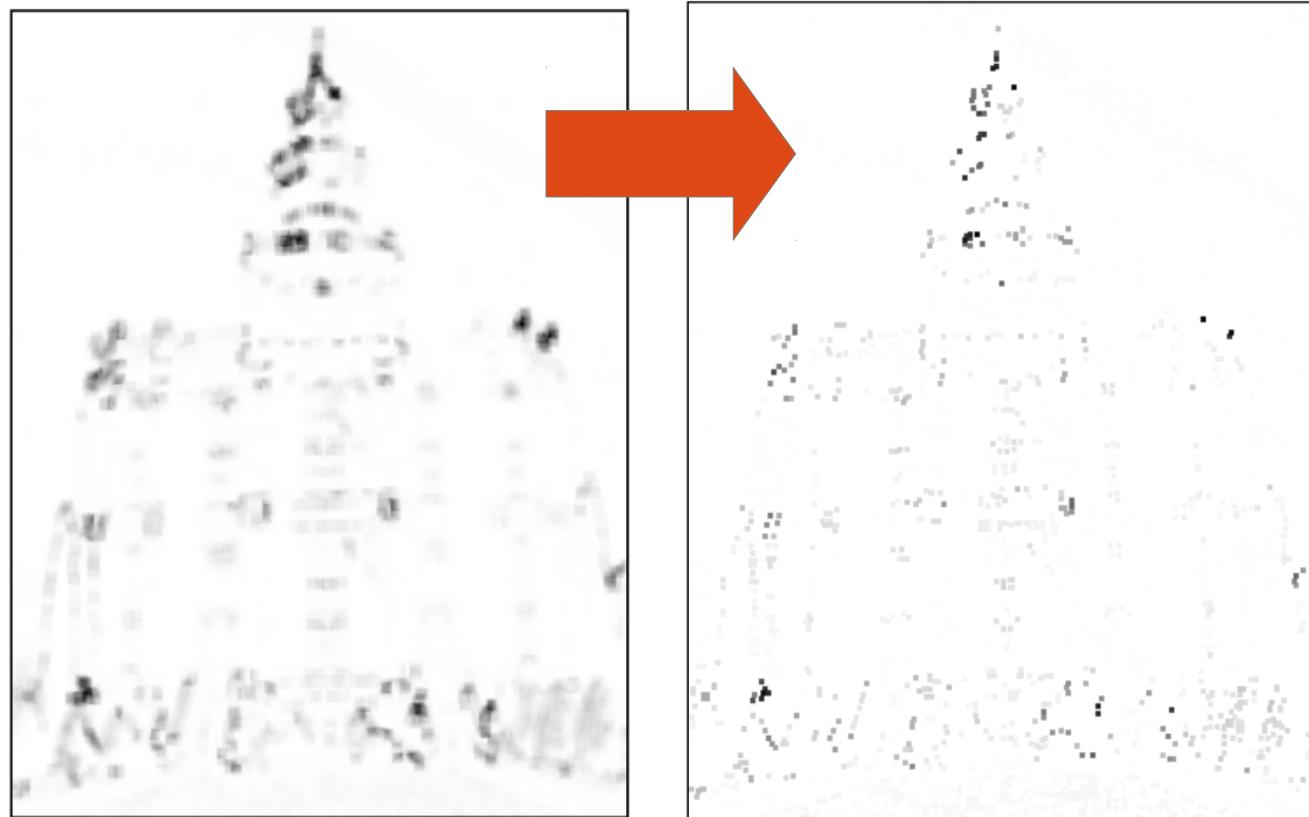
# Edge Detection

- Moravec corner detection
  - Step 1/3 → At each pixel, compute lowest similarity



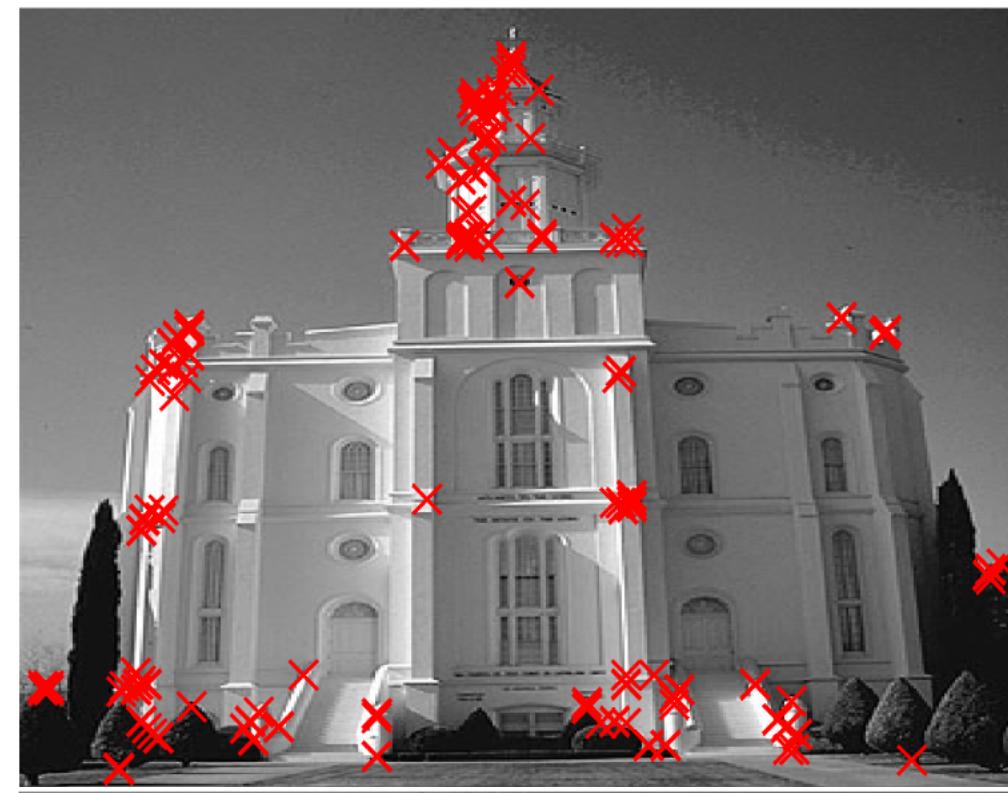
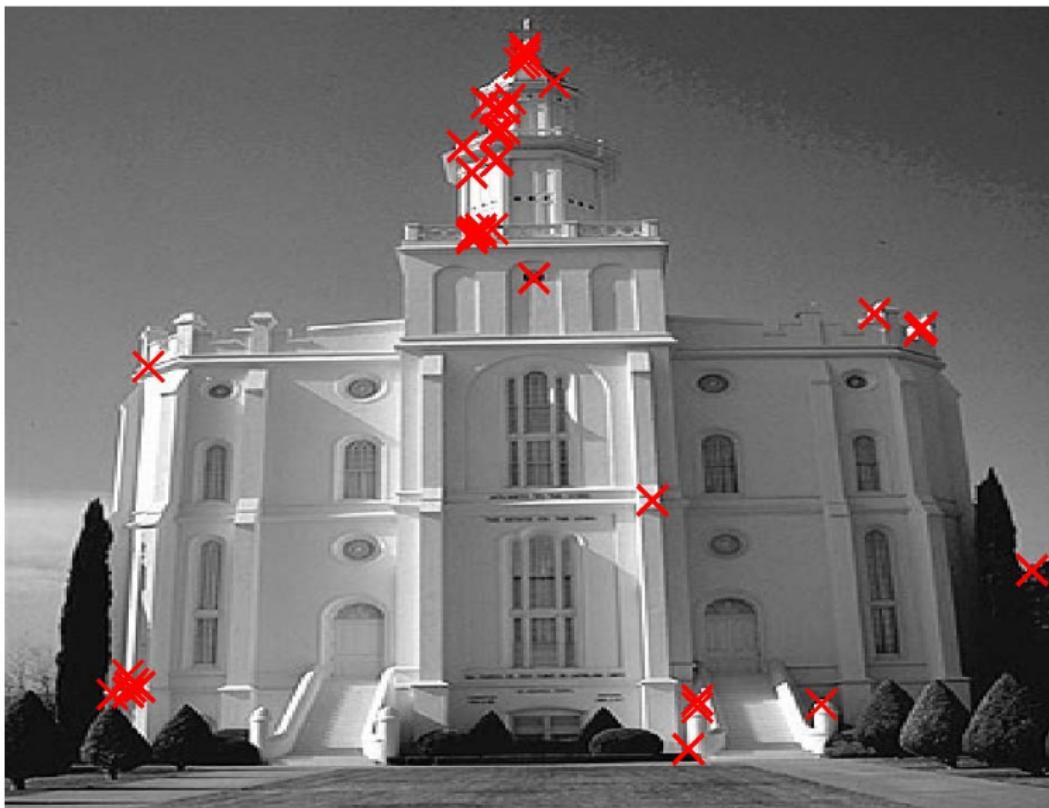
# Edge Detection

- Moravec corner detection
  - Step 2/3 → Non-maximal suppression
    - Ignore pixels having any 8-neighbor with lower similarity
    - Set their values to white



# Edge Detection

- Moravec corner detection
  - Step 3/3 → Threshold



# Edge Detection

- Limitations of Moravec corner detection
  - Only 8 shifts of patches are considered at 45-degree angle increments
    - Left, right
    - Up, down
    - NW, NE, SW, SE
  - Patches are rectangular (not isotropic)

# Edge Detection

- **Harris corner detection.** 1988.
  - Consider “all” (infinitely many) small (infinitesimally small) shifts
  - Use Taylor-series expansion of image function
  - Dissimilarity measured via sum of squared differences
  - **Dissimilarity** between (i) patch over pixels  $(u,v)$  and (ii) another patch over pixels shifted by  $(x,y)$

$$S(x, y) = \sum_u \sum_v w(u, v) (I(u + x, v + y) - I(u, v))^2$$

where  $w(u,v)$  = weights over pixels within patch

- Can be used to make patch isotropic

# Edge Detection

- Harris corner detection

- Taylor-series expansion of image function :

$$I(u + x, v + y) \approx I(u, v) + I_x(u, v)x + I_y(u, v)y$$

- Thus, approximated patch dissimilarity is :

$$S(x, y) \approx \sum_u \sum_v w(u, v) (I_x(u, v)x + I_y(u, v)y)^2$$

- This is a quadratic form over shift variables x, y

# Edge Detection

- Harris corner detection
  - Patch dissimilarity at any shift  $(x,y)$  is :

$$S(x,y) \approx (x \ y) A \begin{pmatrix} x \\ y \end{pmatrix}$$

where “A” = **structure tensor**

$$A = \sum_u \sum_v w(u,v) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}_{(u,v)}$$

- “A” gives averaged local differential structure
- “A” is symmetric, positive definite

- Because each summand matrix  $\begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} I_x \\ I_y \end{bmatrix} \cdot [I_x \quad I_y]$

# Edge Detection

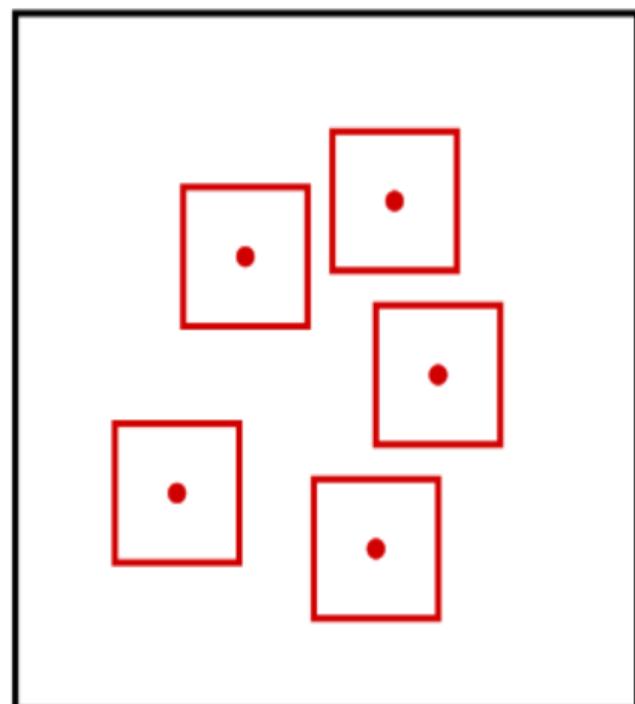
$$S(x,y) \approx (x \ y) A \begin{pmatrix} x \\ y \end{pmatrix}$$

- Harris corner detection
  - A has an eigen decomposition :  $A = Q \ D \ Q^{-1} = V \ D \ V'$ 
    - Eigenvalues  $\rightarrow$  non-negative
    - Eigenvectors  $\rightarrow$  orthogonal
  - For a patch's center pixel to be at an object's corner, **dissimilarity**  $S(x,y)$  should be **large** for **all shifts**  $(x,y)$
  - Thus, “A” must have **2 large** (positive) eigenvalues
    - Why ?
    - If A has an eigenvalue = 0, then for shift  $(x,y)$  = corresponding eigenvector “v”,  $v' A v = 0$

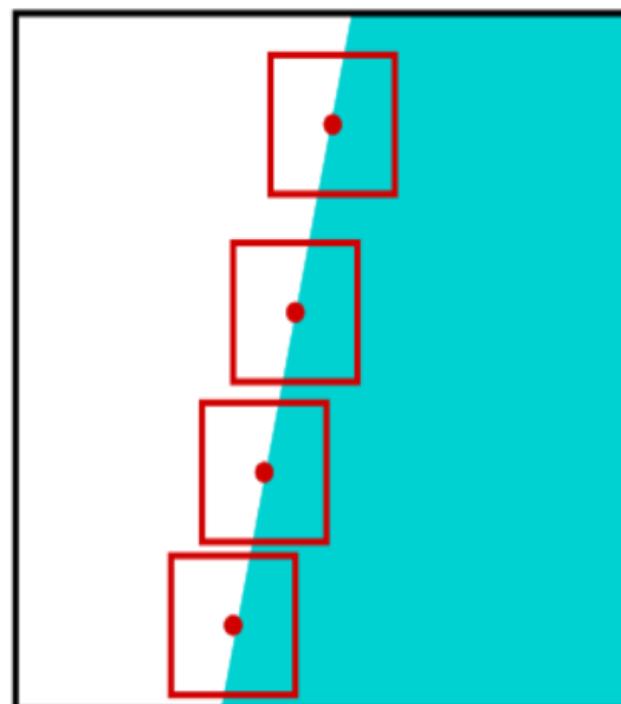
# Edge Detection

- Harris corner detection
  - (1) Constant region : both eigenvalues = 0
  - (2) Edge : one eigenvalue large, other  $\rightarrow 0$
  - (3) Corner : both eigenvalues large

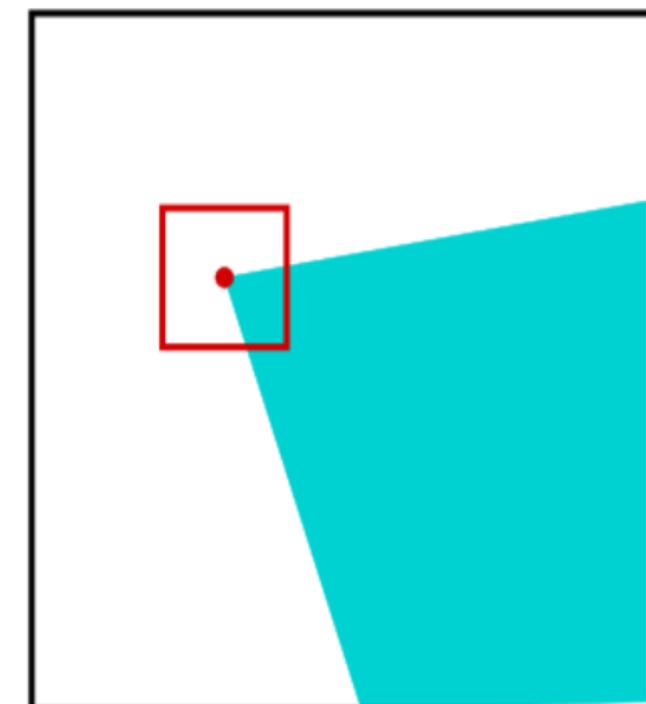
flat region



edge



corner



# Edge Detection

- Harris corner detection
  - Corner-ness measure
    - Designed to avoid eigen decomposition
  - $C = \text{Determinant}(A) - k (\text{Trace}(A))^2$ 
    - Determinant(A) = product of eigenvalues
    - Trace(A) = sum of eigenvalues = sum of diagonal elements
    - $k$  = empirically-tuned constant ( $0 < k < 0.25$ ) such that
      - If both eigenvalues  $\rightarrow 0$ , then  $C \rightarrow 0$
      - If one eigenvalue  $\rightarrow 0$ , then  $C < 0$
      - If both eigenvalues large, then  $C > 0$
    - Rotation invariant
      - Because eigenvalues don't change when image gets rotated,  
i.e., gradient vectors get rotated,  
i.e., coordinate frame  $\langle l_x, l_y \rangle$  gets rotated

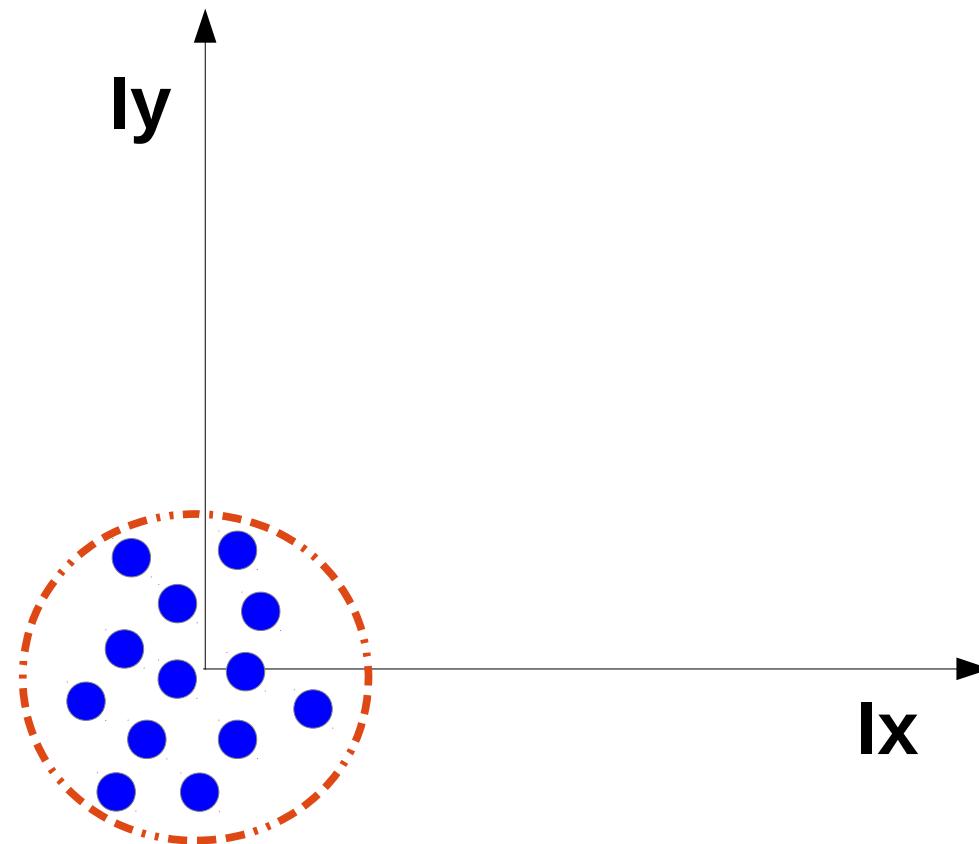
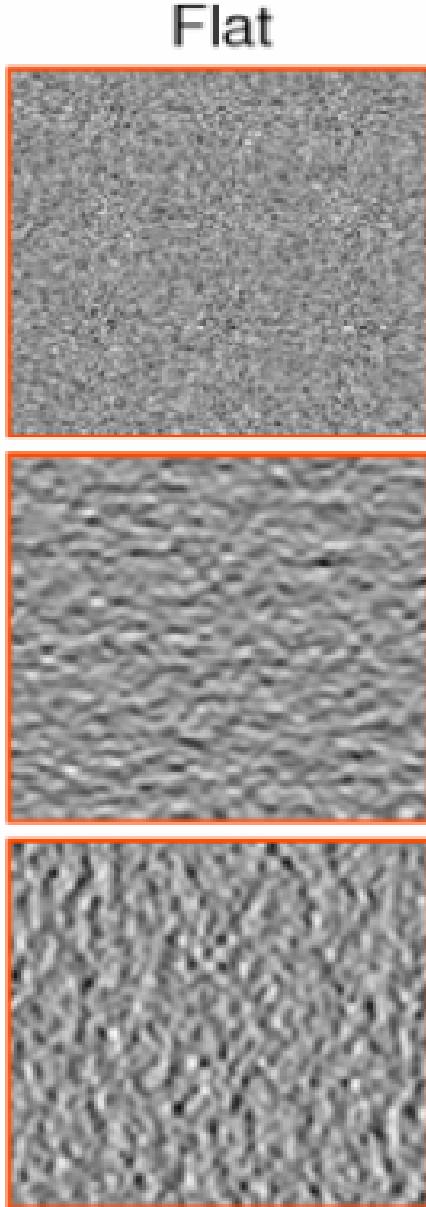
# Edge Detection

- Harris corner detection
  - Another interpretation of “A”
  - Ignoring weights  $w(u,v)$ ,  
“A” = 2<sup>nd</sup>-moment matrix of gradient vectors over patch
    - Not covariance matrix, because no mean subtraction

# Edge Detection

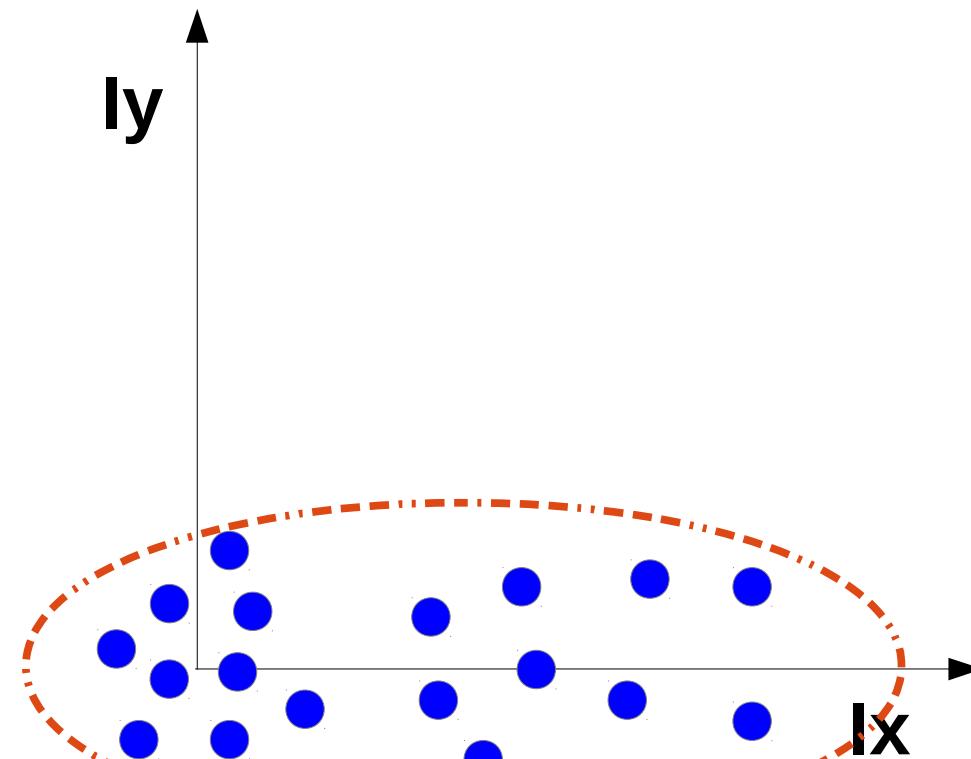
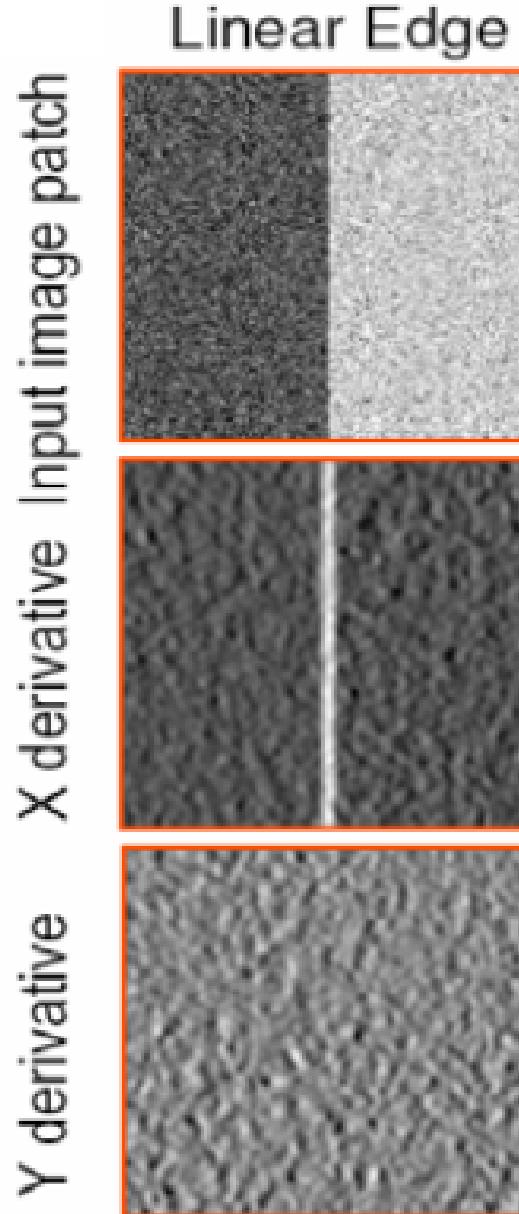
- Harris corner detection

Y derivative   X derivative   Input image patch



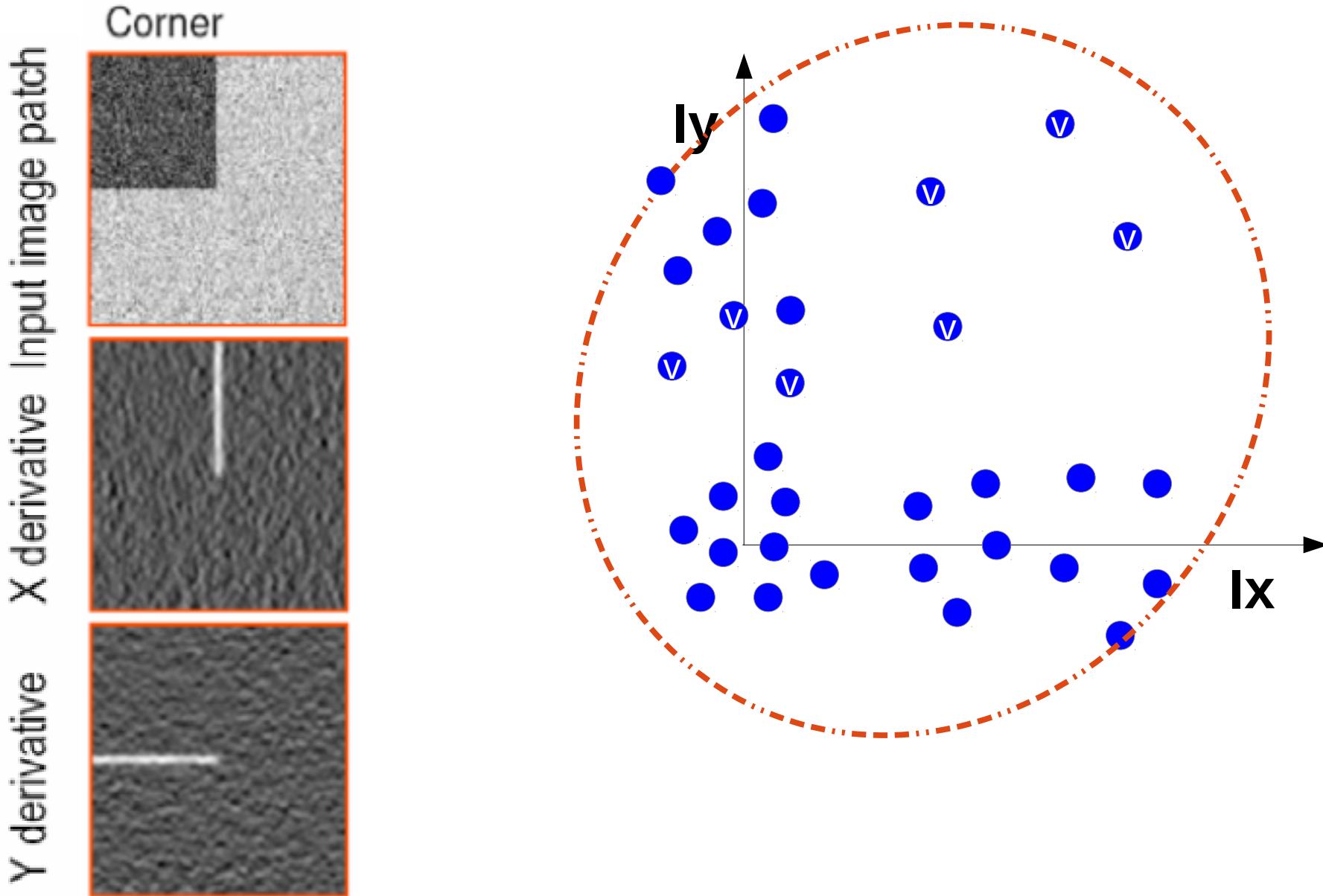
# Edge Detection

- Harris corner detection



# Edge Detection

- Harris corner detection



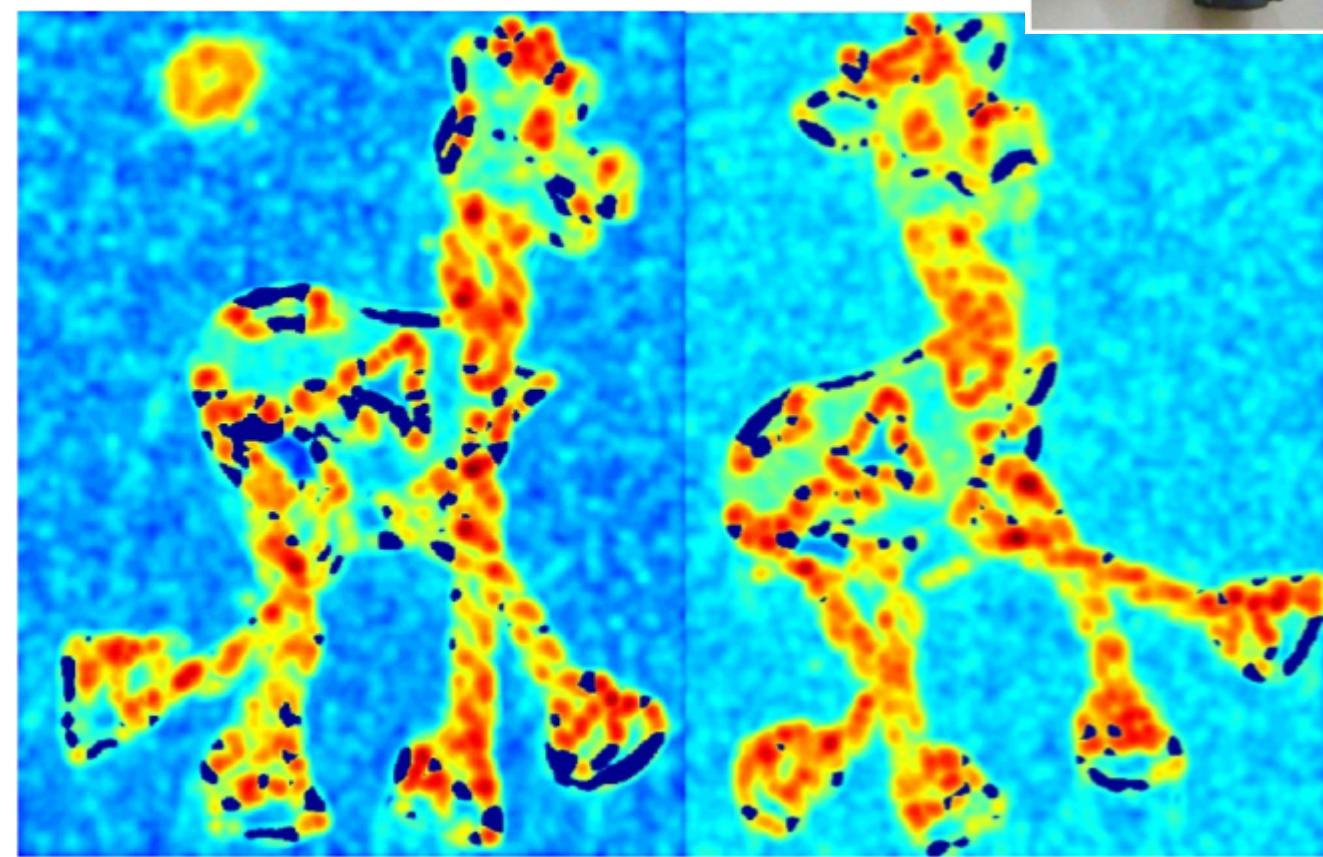
# Edge Detection

- Harris corner detection
  - (1) Compute cornerness measure
  - (2) Non-maximum suppression (in neighborhoods)



# Edge Detection

- Harris corner detection
  - (1) Corner-ness measure



# Edge D

- Harris corner detection
  - (2) Non-maximum suppression

