



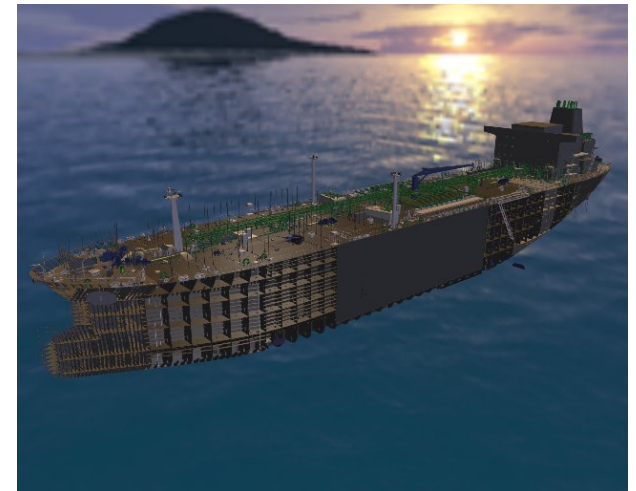
# CS475/CS675

## Computer Graphics

### Visibility

# Visibility

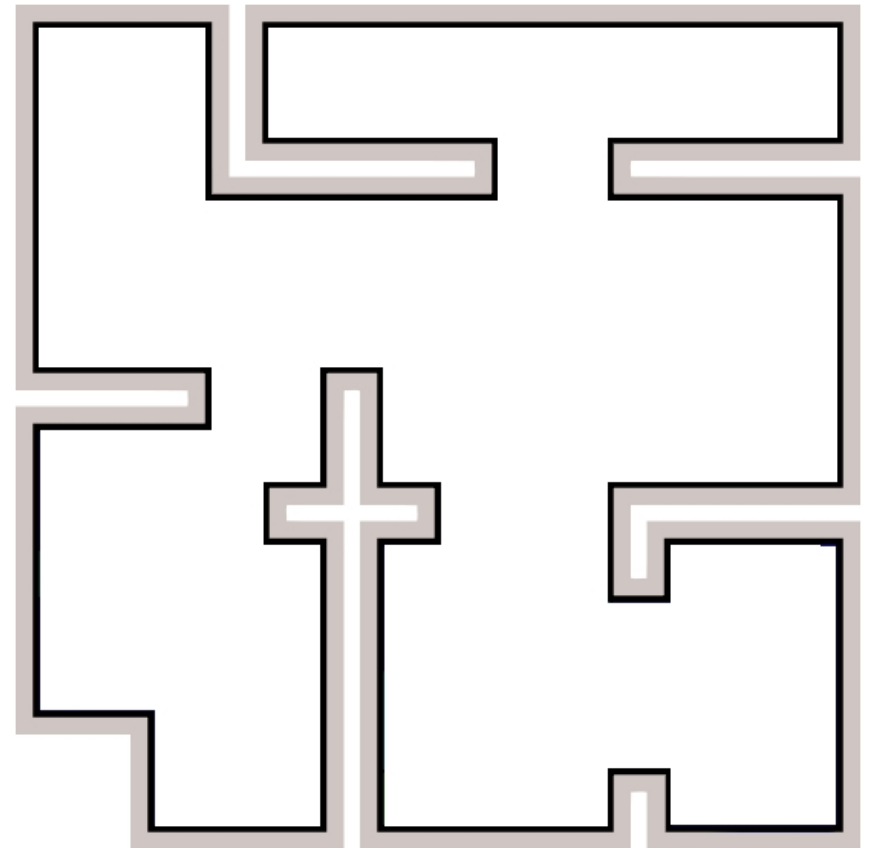
- What is visible?
  - Which objects are visible?
  - Which pixels(fragments) to render?
- Why check for visibility?
  - Efficiency
  - Correctness?
  - Disambiguation



The Double Eagle Tanker:  
**4GB** of data, **82 M Triangles**  
From: <http://www.cs.unc.edu/~geom/hardware/#Vis>

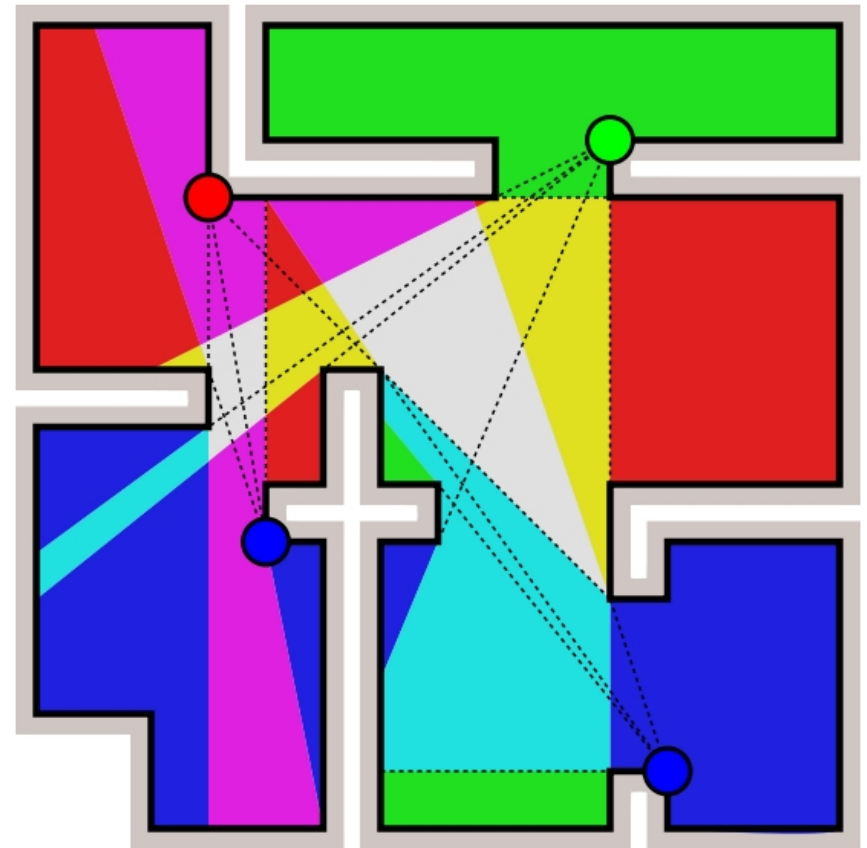
# Simple question

- The *art gallery* problem:  
Given a planar art gallery, what is the minimum number of guards that need to be placed at the corners (but inside the gallery) so that every part of the gallery is visible to at least one guard.



# Simple question

- NP – Complete!
- Upper bound:  $\text{floor}(N/3)$  for a simple polygon with  $N$  vertices.
- Determining visibility is not always easy.





# Visibility

- The **Image Space** problem formulation  
for (each *pixel* in the rendered image)  
{
  - determine the object closest to the viewer that is intercepted by the projector (ray) through the pixel;
  - draw the pixel in the appropriate color;}
- Worst case complexity:  $np$   
 $n$  : number of objects,  $p$  : number of pixels

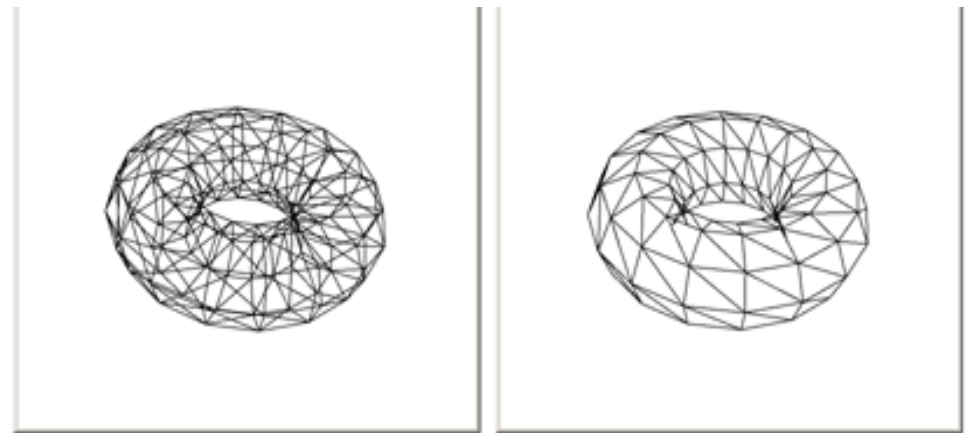


# Visibility

- The **Object Space** problem formulation  
for (every *object* in the world)  
{
  - determine those parts of the object whose view is  
unobstructed by other parts of itself or any other object;
  - draw those parts in the appropriate color;}
- Worst case complexity:  $n^2$   
 $n$  : number of objects

# Visibility

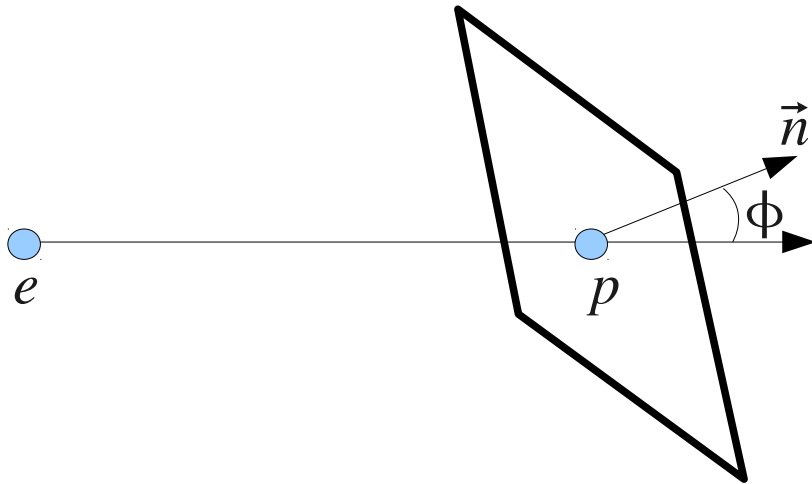
- Types of visibility computation we have seen:
  - Clipping – 2D and 3D
  - View-frustum clipping/culling
  - Backface culling



<http://geometricalgebra.org>

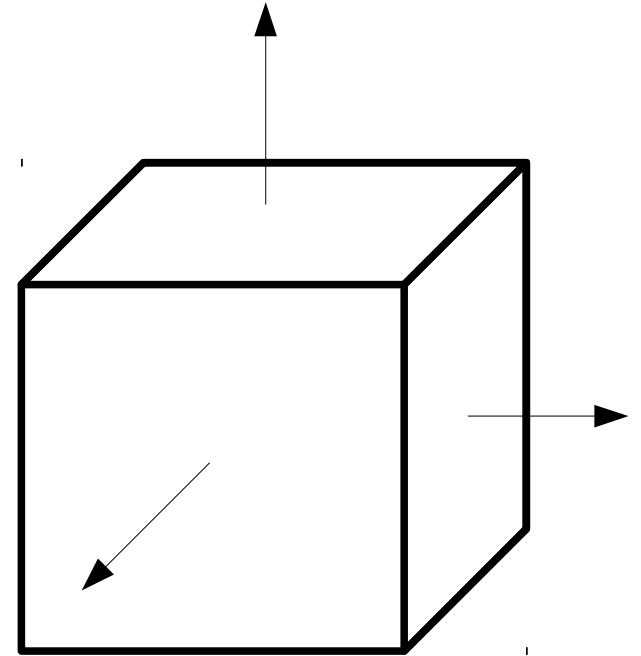
# Visibility

- Backface Culling



$$(\vec{p} - \vec{e}) \cdot \vec{n} > 0 \quad \text{Cull}$$

$$(\vec{p} - \vec{e}) \cdot \vec{n} \leq 0 \quad \text{Do Not Cull (may be visible)}$$



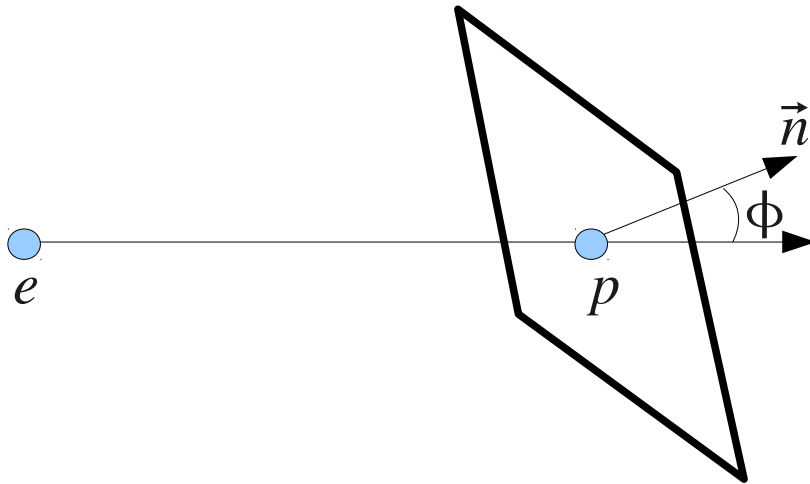
Simple Idea:

Discard surface patches that face away from the camera.



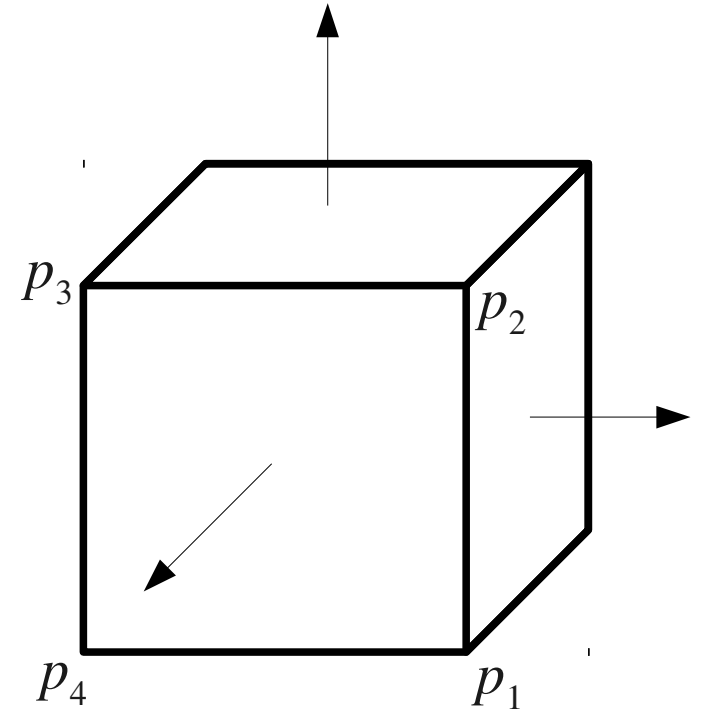
# Visibility

- Backface Culling



If  $p_1, p_2, p_3, p_4$  are the patch vertices in CCW order seen from outside then the outward facing normal is given by:

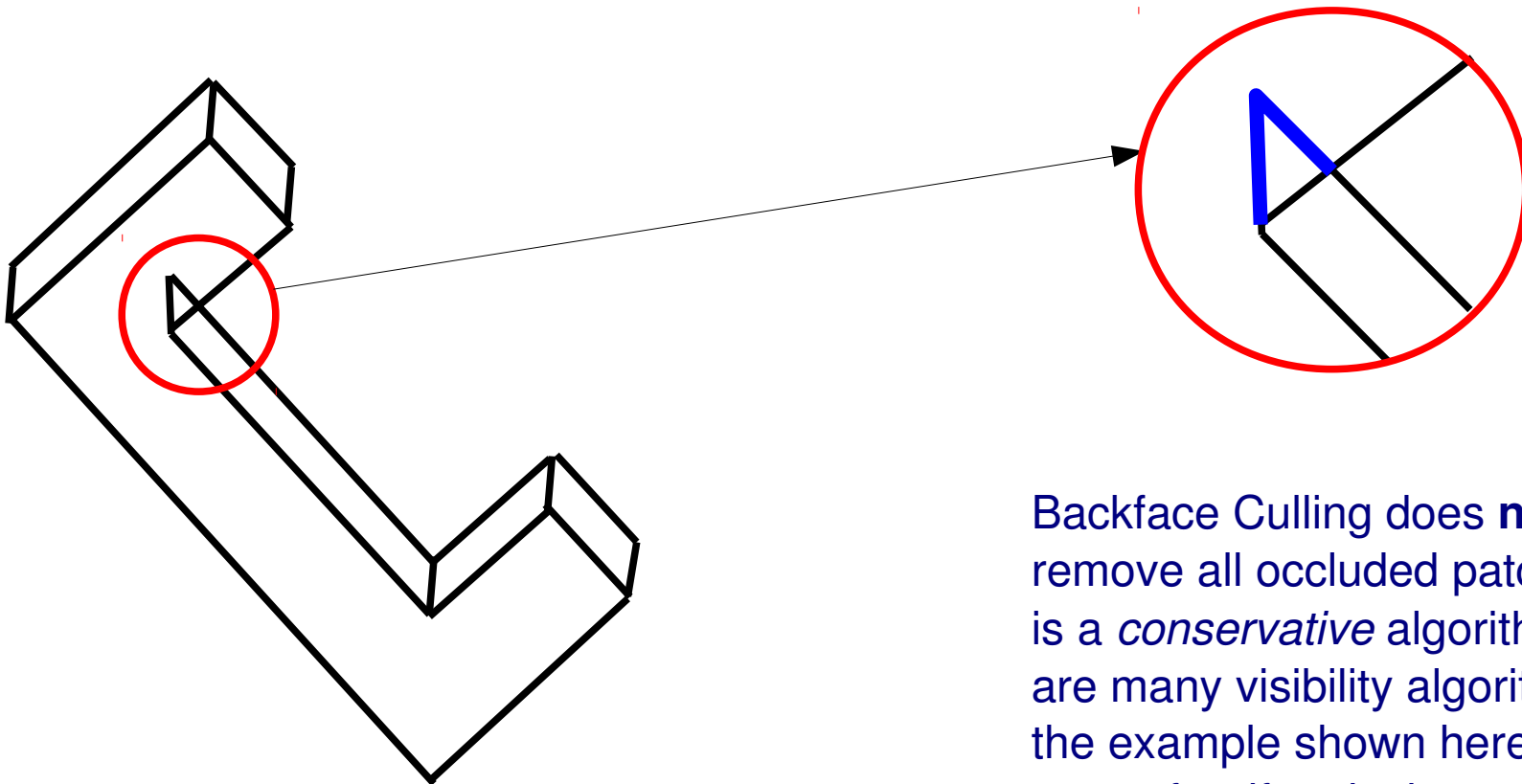
$$\vec{n} = (p_2 - p_1) \times (p_3 - p_1)$$



Compute the outward normals and do Backface culling in the WCS.

# Visibility

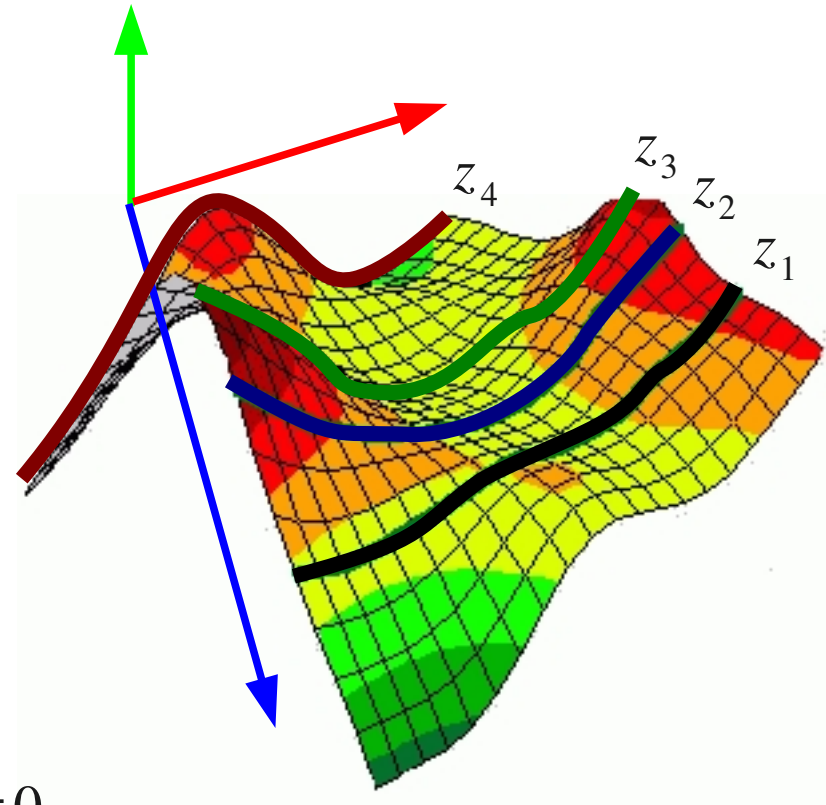
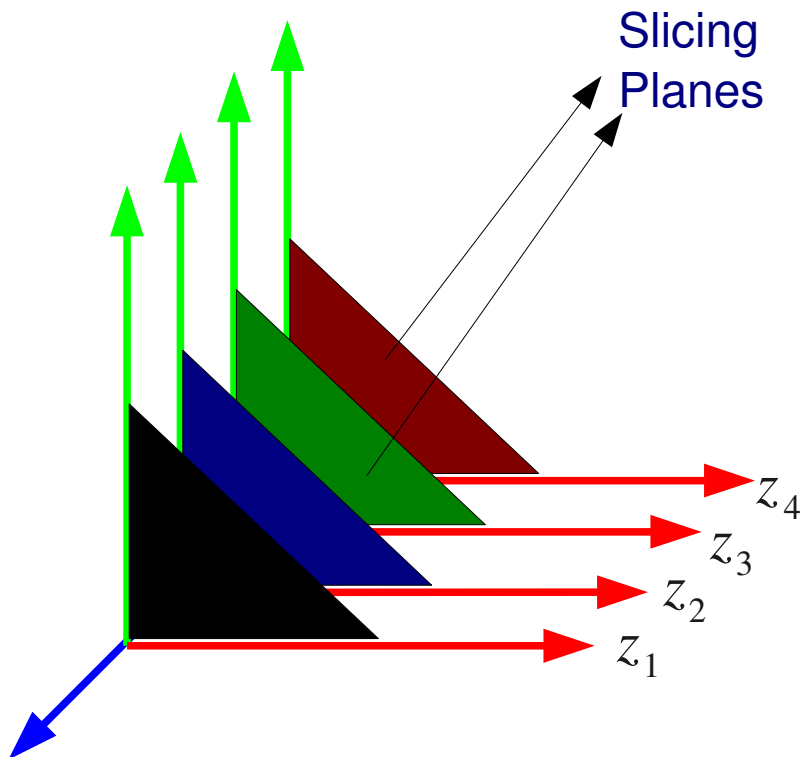
- Backface Culling is not enough



Backface Culling does **not** remove all occluded patches (it is a *conservative* algorithm as are many visibility algorithms) – the example shown here is a case of *self* occlusion.

# Visibility

- Floating Horizon Algorithm

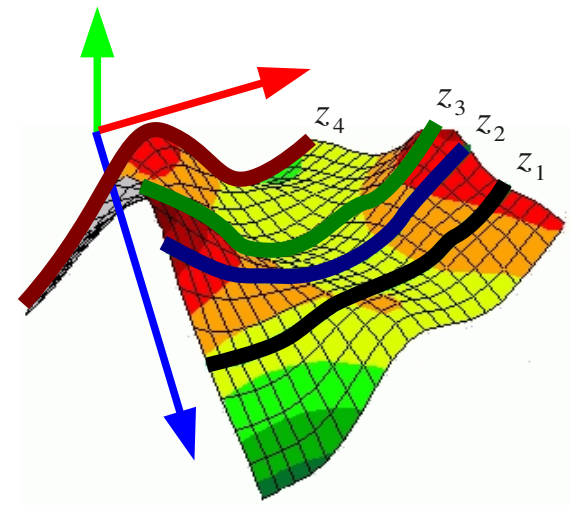
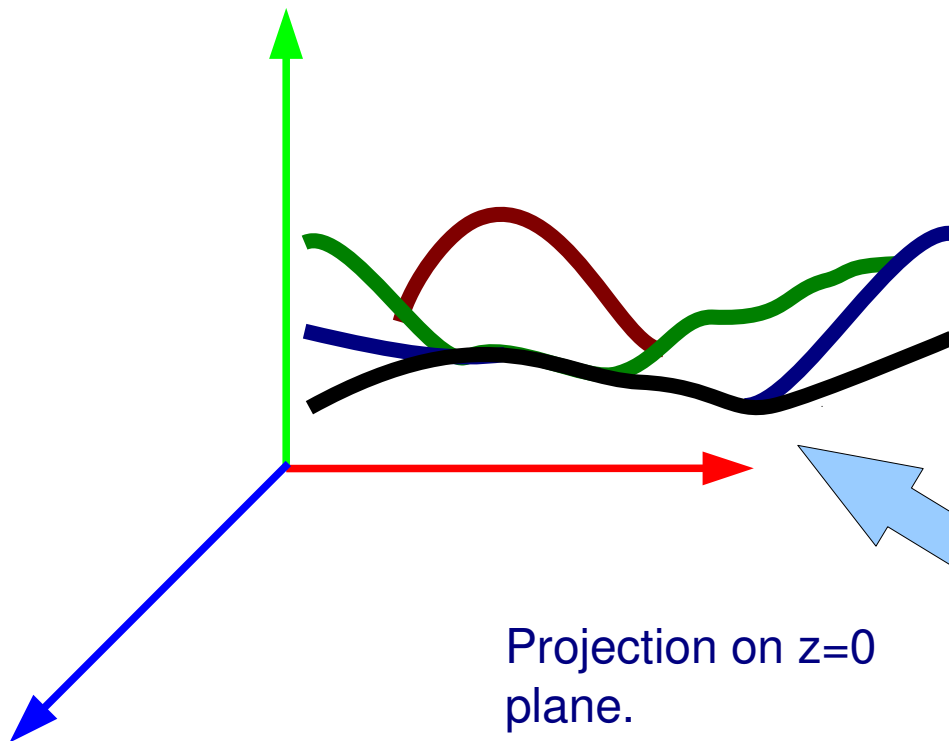


Given a surface defined by  $f(x, y, z) = 0$   
We can sample it at many 2D cutting planes,  
yielding a set of curves of the form  $y = f(x, z_i)$

# Visibility

- Floating Horizon Algorithm

- For each slicing plane  $i$ , with  $z=z_i$ 
  - Compute  $y_i$  for any  $x_i$  on the curve.
  - The point  $(x_i, y_i)$  is visible if  $y_i > y_j$  for all  $j < i$  and  $x_i = x_j$



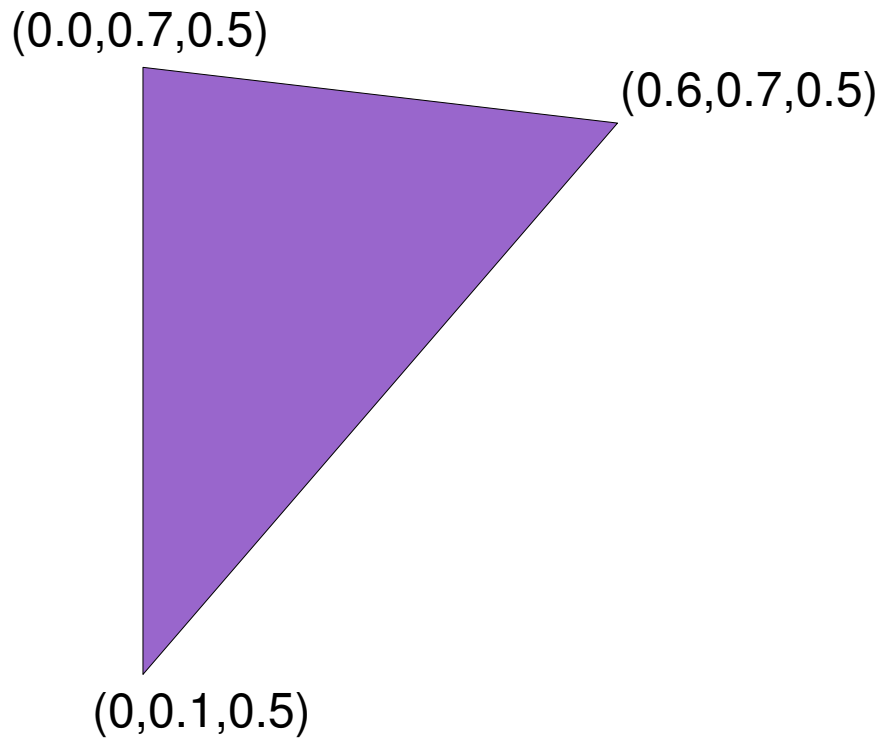
# Visibility

- Z-Buffer and Scan Conversion
- Initialize the z-buffer to the max Z value.
- `glClear`, `glDepthRange`

1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1

# Visibility

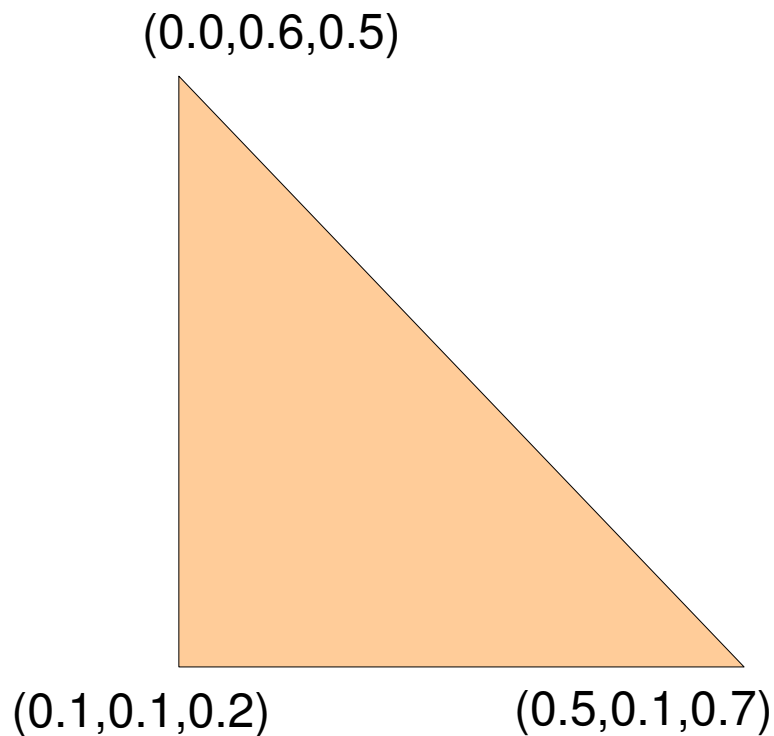
- Z-Buffer and Scan Conversion



1	1	1	1	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	0.5	0.5	0.5	0.5	1	1
1	0.5	0.5	0.5	0.5	1	1	1
1	0.5	0.5	0.5	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	1	1	1	1	1	1

# Visibility

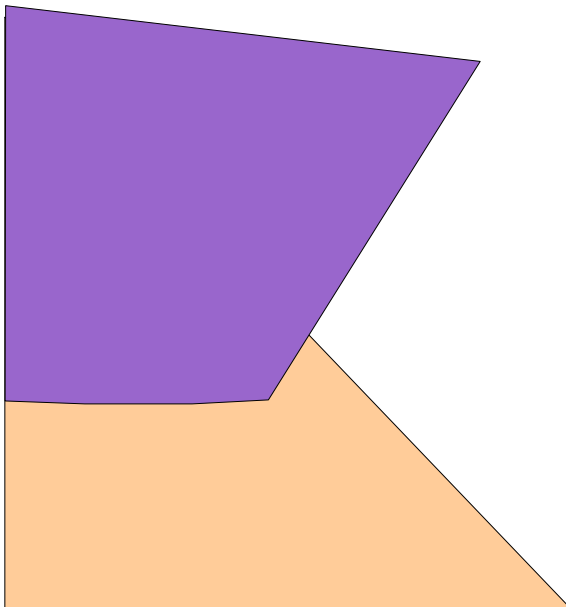
- Z-Buffer and Scan Conversion



1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	0.5	0.5	1	1	1	1
1	0.4	0.5	0.6	0.7	1	1	1
1	0.3	0.4	0.5	0.6	0.7	1	1
1	0.2	0.3	0.4	0.5	0.6	0.7	1

# Visibility

- Z-Buffer and Scan Conversion



1	1	1	1	1	1	1	1
1	0.5	0.5	1	1	1	1	1
1	0.5	0.5	0.5	0.5	0.5	1	1
1	0.5	0.5	0.5	0.5	1	1	1
1	0.5	0.5	0.5	1	1	1	1
1	0.4	0.5	0.6	0.7	1	1	1
1	0.3	0.4	0.5	0.6	0.7	1	1
1	0.2	0.3	0.4	0.5	0.6	0.7	1

Note that almost everywhere the result is independent of the order of drawing these polygons.

Except at the pixels where the depth may be the same (this is very unlikely).





# Visibility

- Z-Buffer Algorithm

Initialize

zbuf[i, j]=MAX\_DEPTH

cbuf[i, j]=BACKGROUND\_COLOR

for (each scan converted polygon)

{

Find pseudodepth,  $z$ , of polygon at pixel  $(x, y)$  with color  $c$

If  $(z < \text{zbuf}[i, j])$  {  $\text{zbuf}[i, j] = z$ ;  $\text{cbuf}[i, j] = c$ ;

}



# Visibility

- Z-Buffer Algorithm
- Advantages
  - Simple, Accurate (modulo non-linear z-mapping).
  - Independent of order of drawing polygons.
- Disadvantages
  - Memory (not an issue these days).
  - Wasted computation when over-writing distant points
- Complexity
  - Time:  $O(nm \cdot k)$  –  $n \times m$  pixels,  $k$  polygons
  - Space:  $O(nm \cdot b)$  –  $n \times m$  pixels,  $b$  bytes precision per pixel

# Visibility

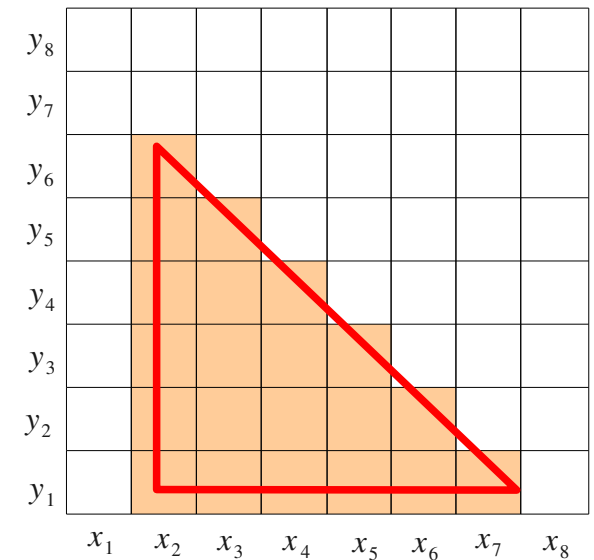
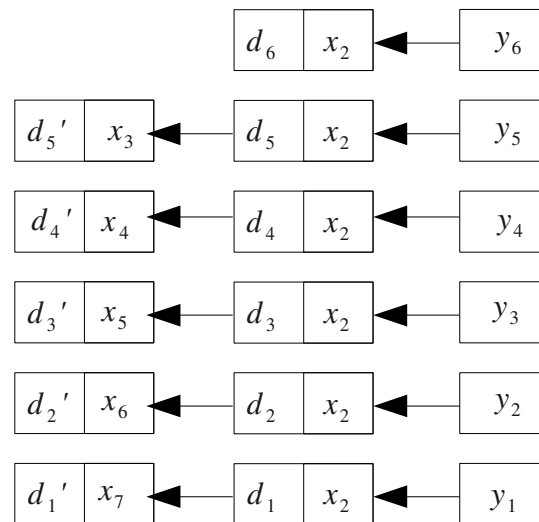
## • Z-Buffer Algorithm and Scan Conversion

- Construct the active edge list AEL for every scanline.
- Interpolate the pseudodepth for each active edge.

for each edge  $[(x_i, y_i, d_i) \text{ and } (x_j, y_j, d_j)]$  with  $y_i < y_j$

```

{
   $x = x_i, d = d_i, \Delta x = \frac{(x_j - x_i)}{(y_j - y_i)}$  and  $\Delta d = \frac{(d_j - d_i)}{(y_j - y_i)}$ 
  for ( $y = y_i, y < y_j; y++$ )
  {
    insert  $(x, d)$  into the AEL of scanline  $y$ 
    such that it is sorted on the  $x$  values
     $x = x + \Delta x, d = d + \Delta d$ 
  }
}
  
```



# Visibility

## • Z-Buffer Algorithm and Scan Conversion

- Compute the active edge list.
- Interpolate the pseudodepth for each active edge.
- Now, for rendering a  $\Delta ABC$ :

$cbuf[i, j] = BACKGROUND\_COLOR$

$zbuf[i, j] = MAX\_DEPTH, \forall 0 \leq i < N, 0 \leq j < M$

$y_{min} = \min(y_A, y_B, y_C) \quad y_{max} = \max(y_A, y_B, y_C)$

for ( $y = y_{min}; y \leq y_{max}; y++$ )

{

get  $(x_p, d_p)$  and  $(x_q, d_q)$  from the AEL with  $x_p < x_q$

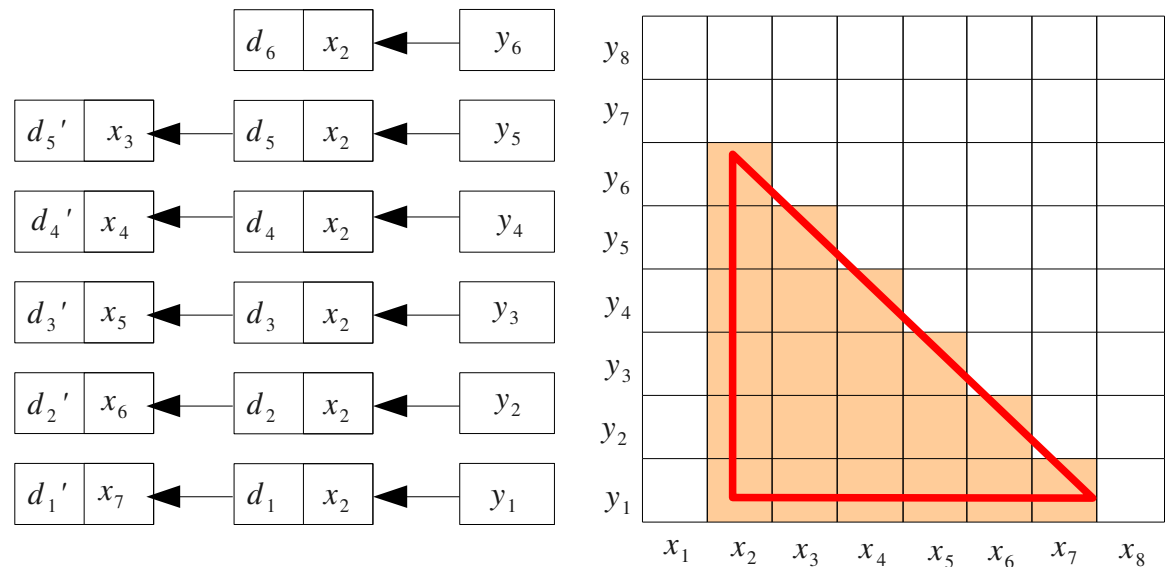
$\Delta d = \frac{(d_q - d_p)}{(x_q - x_p)}$ ;

for ( $x = x_p, d = d_p; x \leq x_q; x++, d = d + \Delta d$ )

{

if ( $d < zbuf[x, y]$ ) {  $zbuf[x, y] = d, cbuf[x, y] = c$  }

}

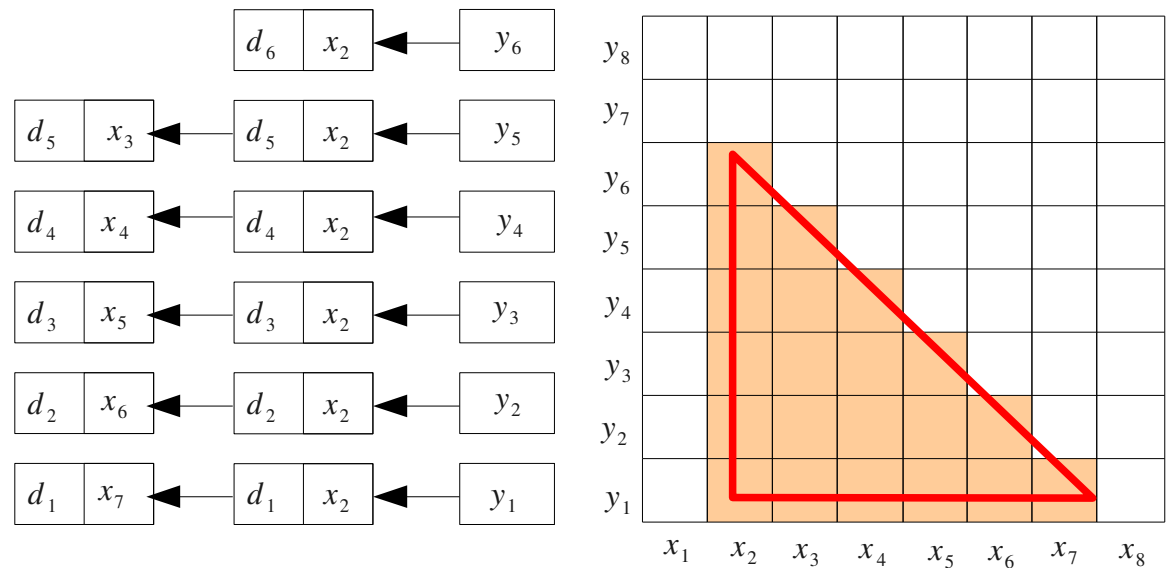


- Note: The color  $c$  at a pixel is also interpolated along the scanline like the pseudodepth is

# Visibility

- Z-Buffer Algorithm and Scan Conversion

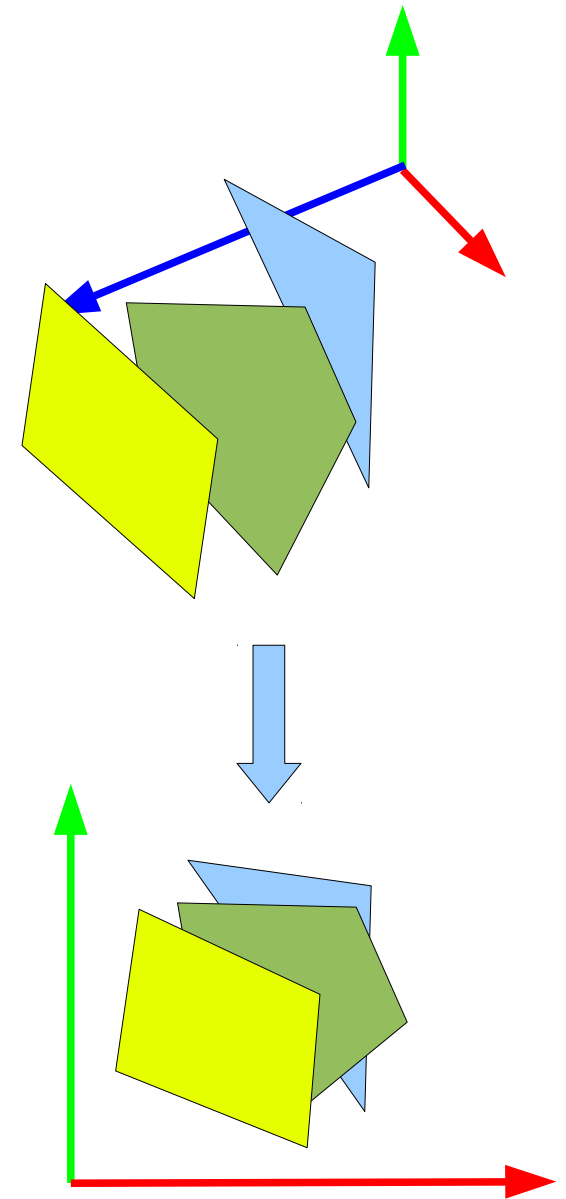
- Compute the active edge list.
- Interpolate the pseudodepth for each active edge.



# Visibility

- Painter's Algorithm

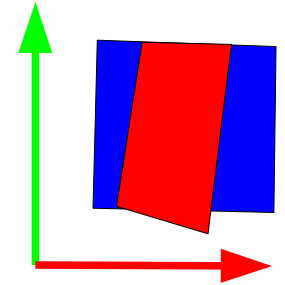
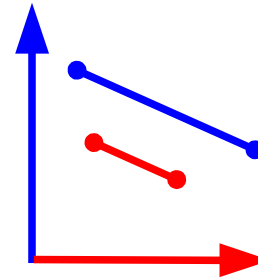
- Sort polygons in increasing order of depth.
- Draw the sorted list of polygons from back to front, i.e., from greatest depth to lesser depths.
- What happens when a polygon has vertices at different depths?



# Visibility

- Painter's Algorithm

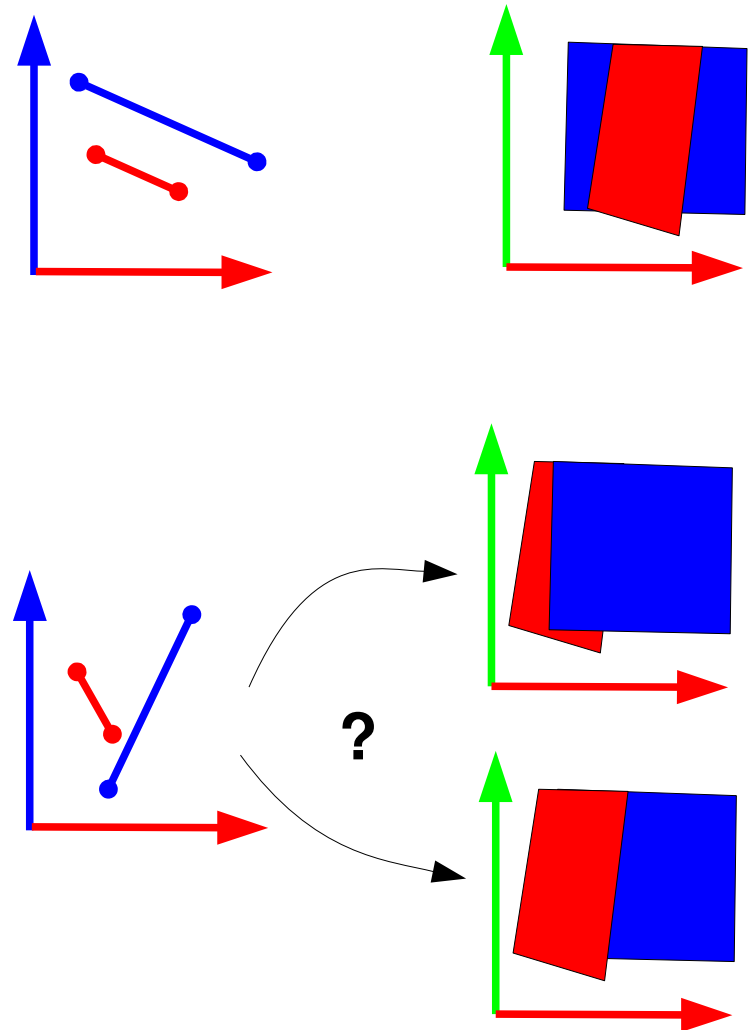
- Sort polygons in increasing order of depth.
- Draw the sorted list of polygons from back to front, i.e., from greatest depth to lesser depths.
- What happens when a polygon has vertices at different depths?
- Sort according to depth of farthest vertex.



# Visibility

- Painter's Algorithm

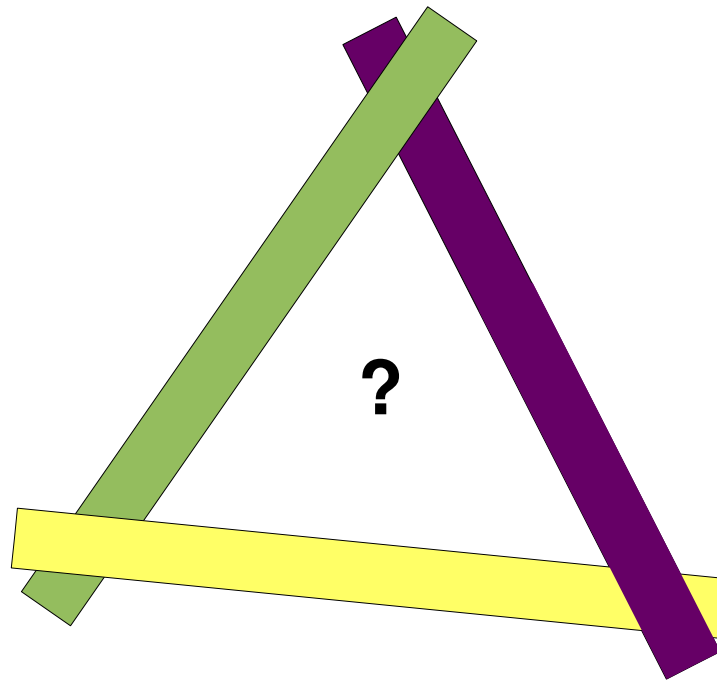
- Sort polygons in increasing order of depth.
- Draw the sorted list of polygons from back to front, i.e., from greatest depth to lesser depths.
- What happens when a polygon has vertices at different depths?
- Sort according to depth of farthest vertex.
- Does it always work?
- How often do we sort?





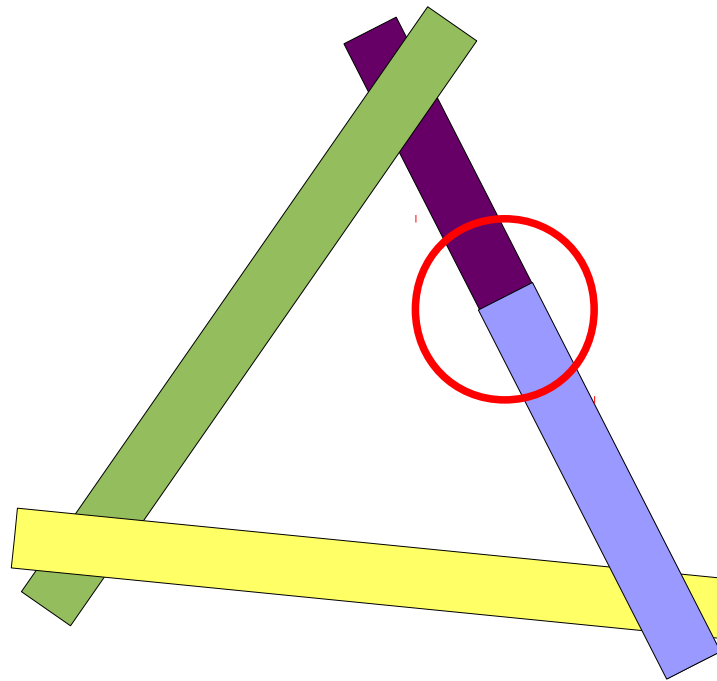
# Visibility

- Painter's Algorithm



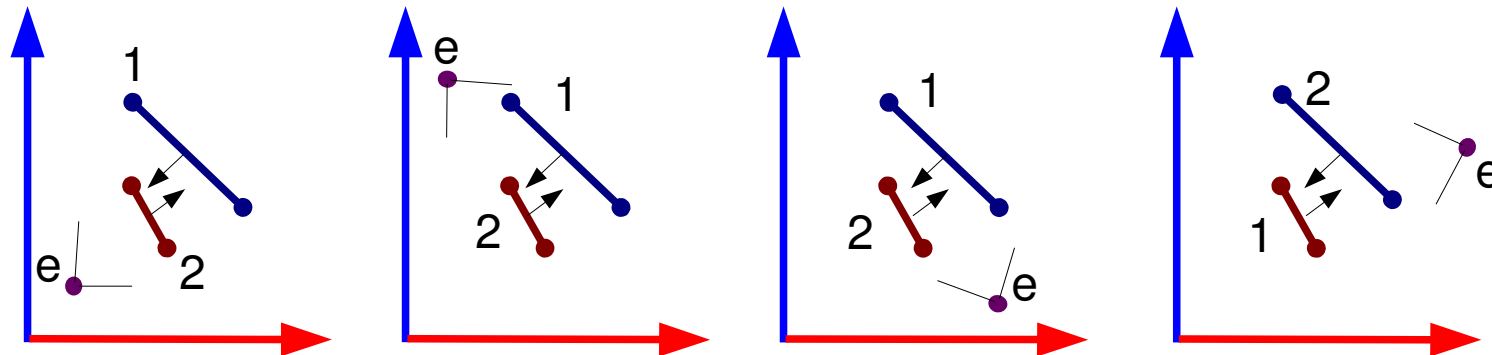
# Visibility

- Painter's Algorithm



# Visibility

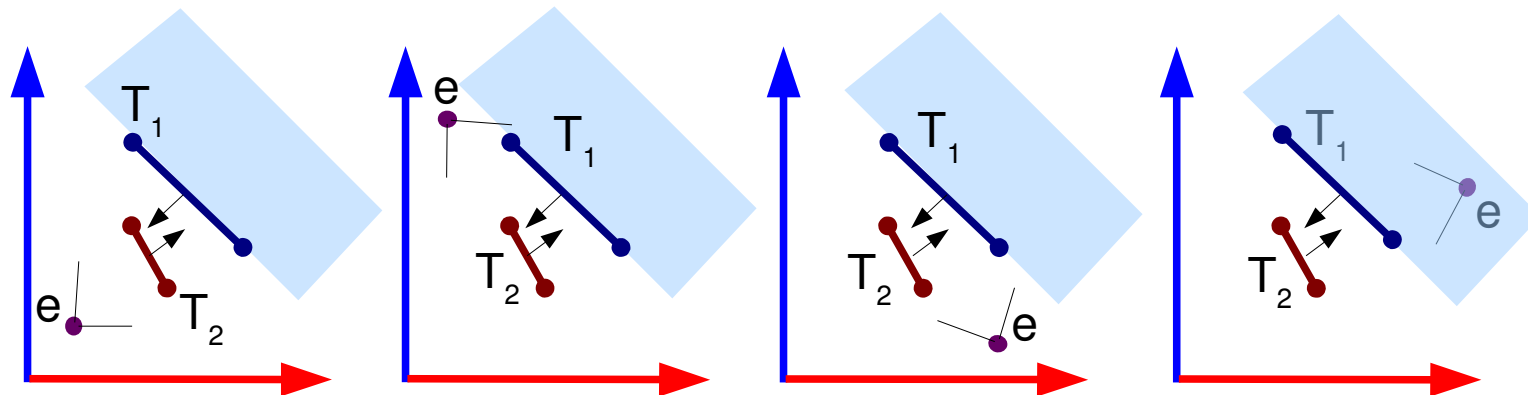
- Binary Space Partitioning (BSP) Trees



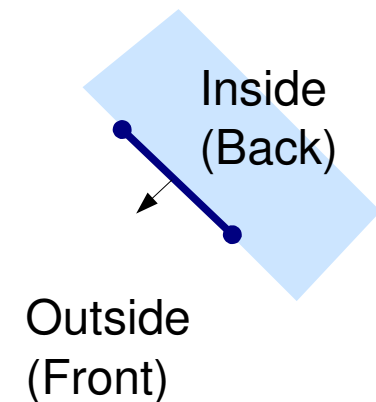
- Observe the correct order of drawing polygons as the eye moves

# Visibility

- Binary Space Partitioning (BSP) Trees

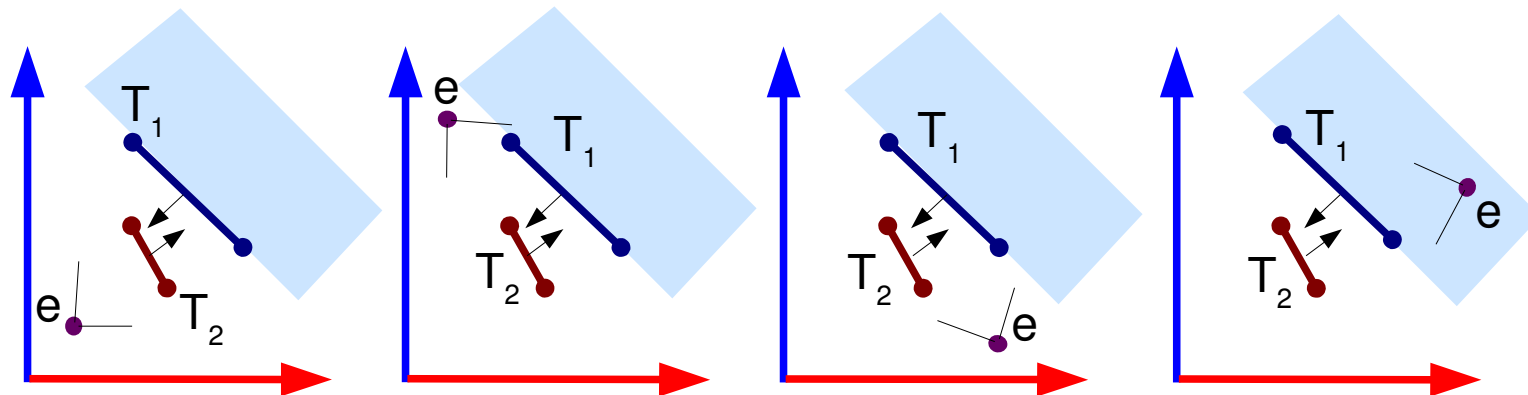


- If  $e$  and  $T_2$  are on the same side of  $T_1$ 
  - Draw  $T_1$  and then draw  $T_2$
- If  $e$  and  $T_2$  are on different sides of  $T_1$ 
  - Draw  $T_2$  and then draw  $T_1$

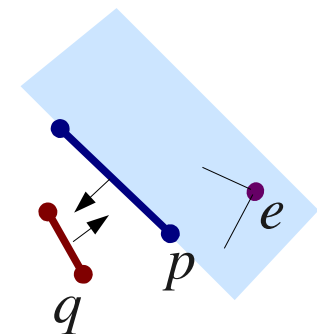


# Visibility

- Binary Space Partitioning (BSP) Trees

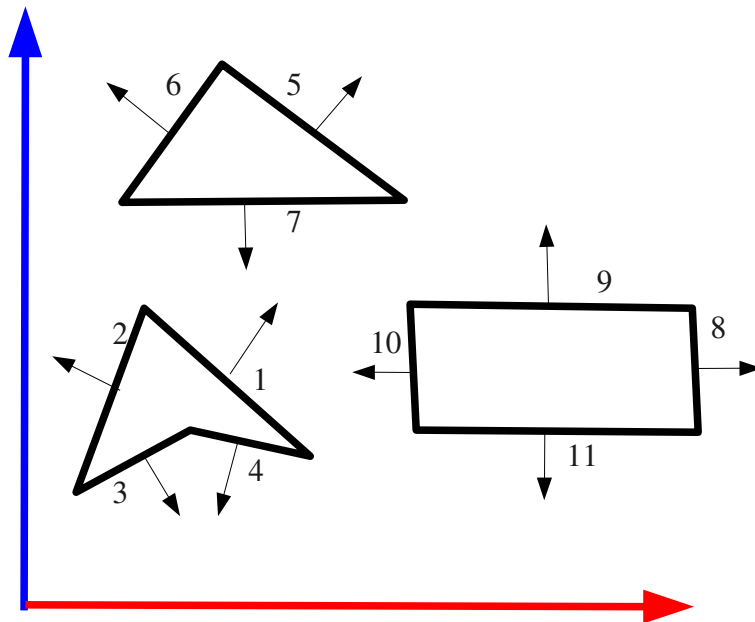


- If the implicit equation of the plane containing  $T_1$  is given by:  $f(r) = (r - p) \cdot n$
- If  $f(q) \cdot f(e) > 0$  then draw  $T_1$  and then draw  $T_2$
- If  $f(q) \cdot f(e) < 0$  then draw  $T_2$  and then draw  $T_1$



# Visibility

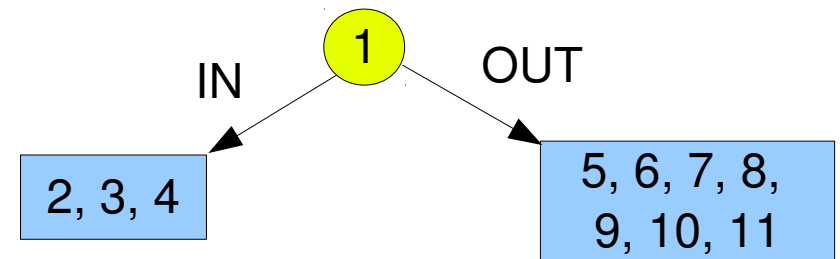
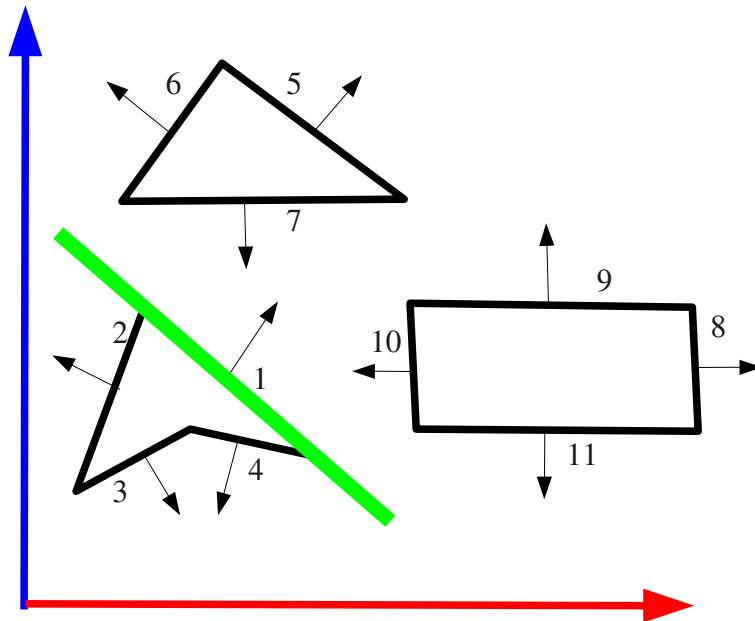
- **BSP Tree** is an efficient data structure for quickly determining the inside/outside relation between polygons and the camera position.



- **Two Phases**
  - Preprocessing: BSP Tree construction  
(done once for a given scene)
  - Rendering: BSP Tree traversal  
(done whenever the eye position changes)

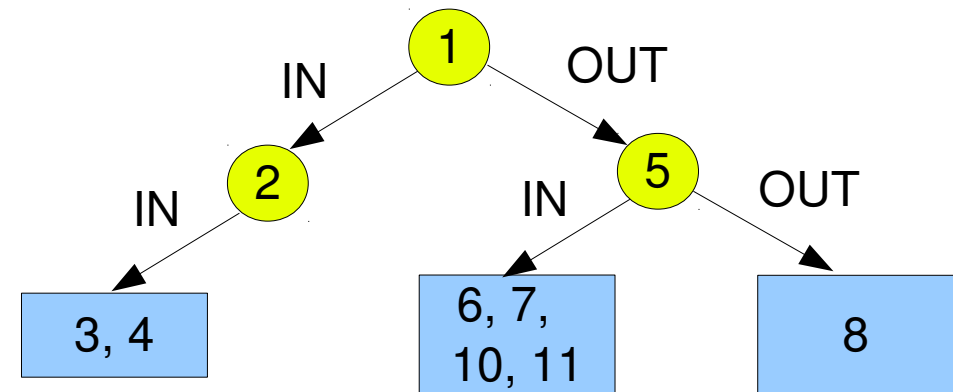
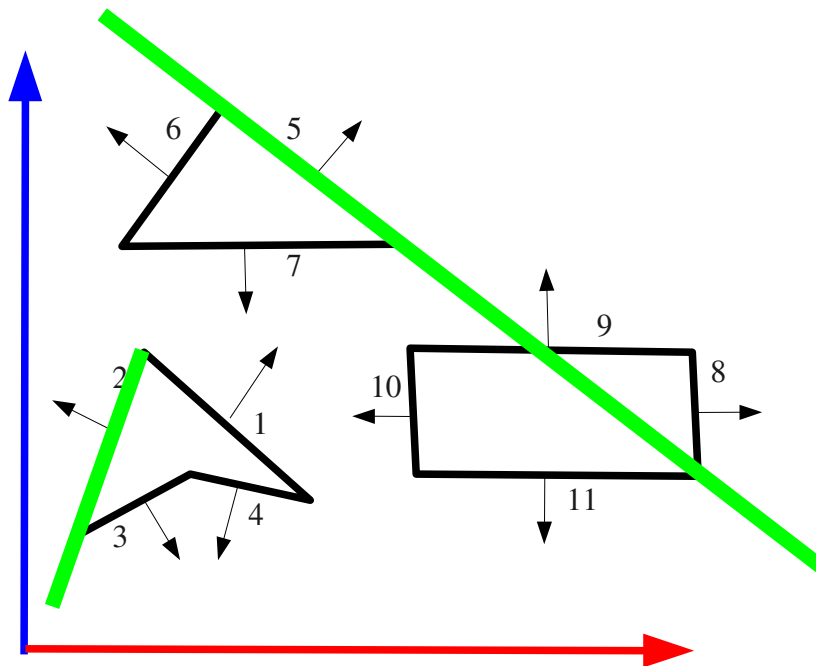
# Visibility

- BSP Tree construction



# Visibility

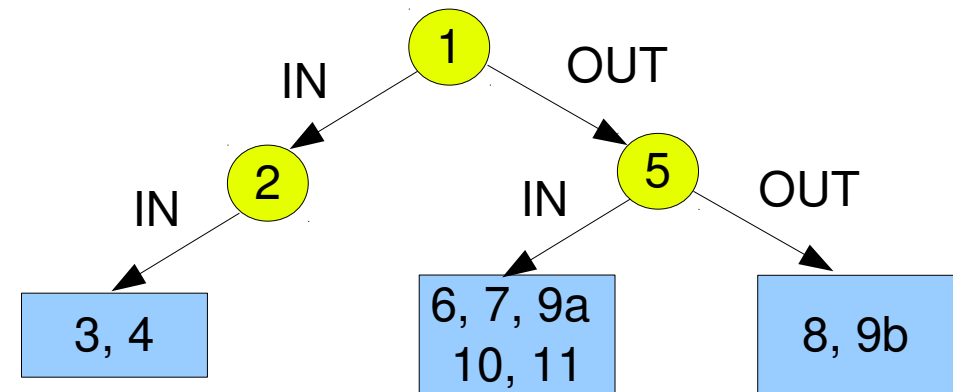
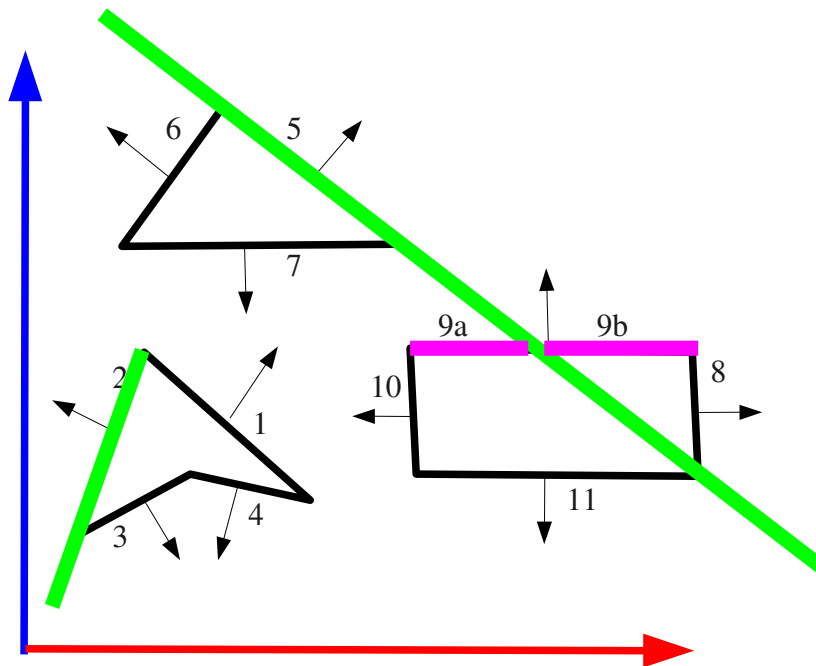
- BSP Tree construction





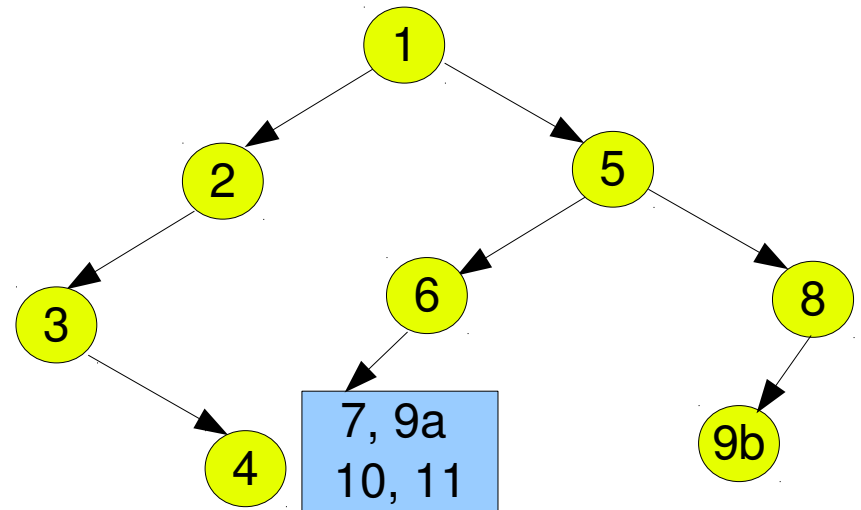
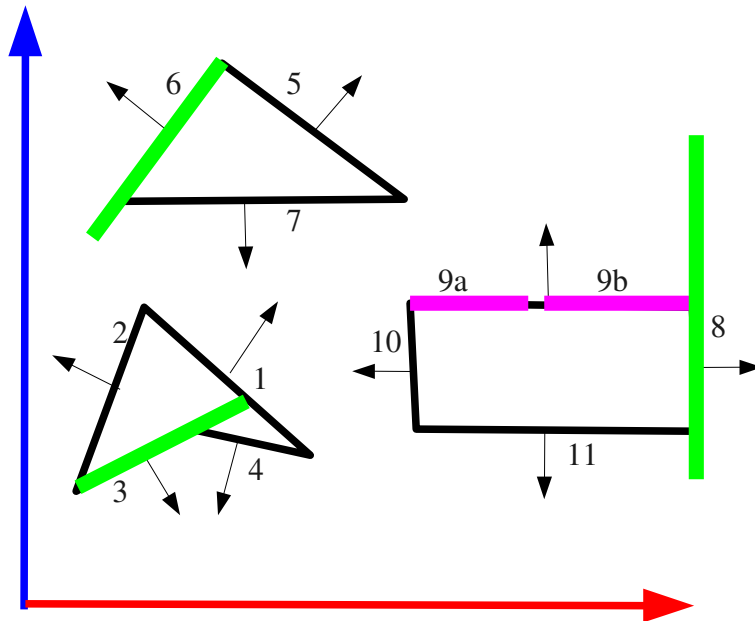
# Visibility

- BSP Tree construction



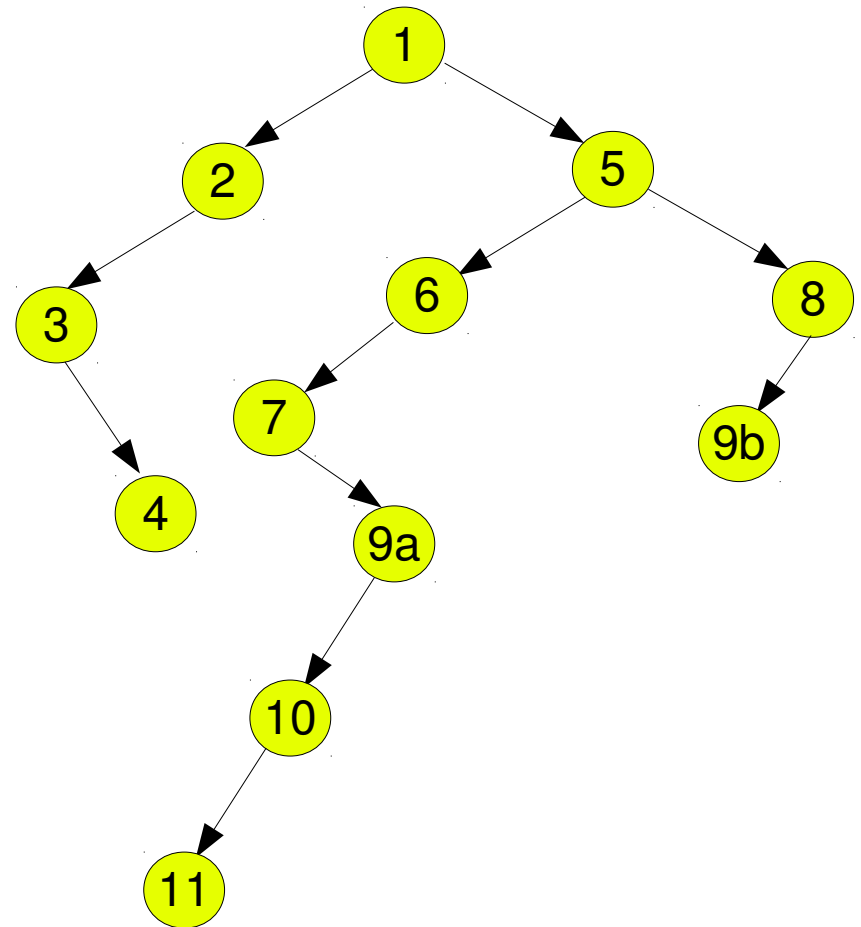
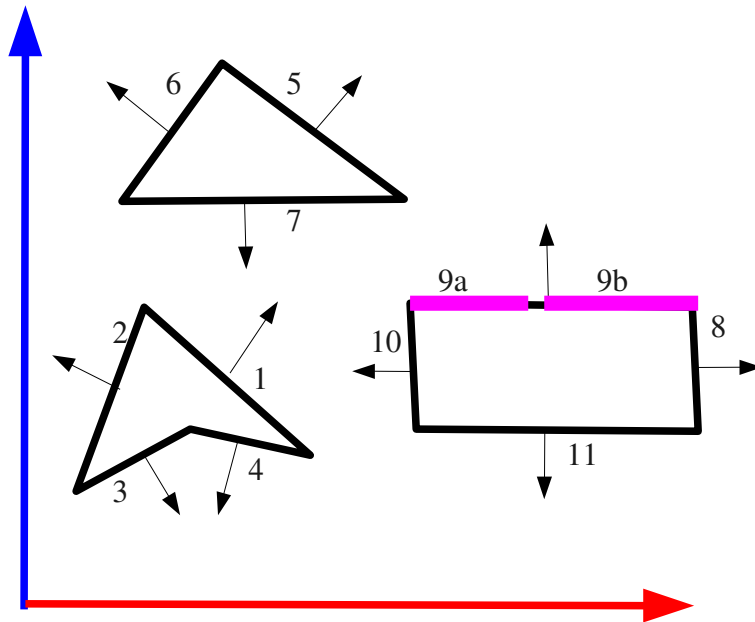
# Visibility

- BSP Tree construction



# Visibility

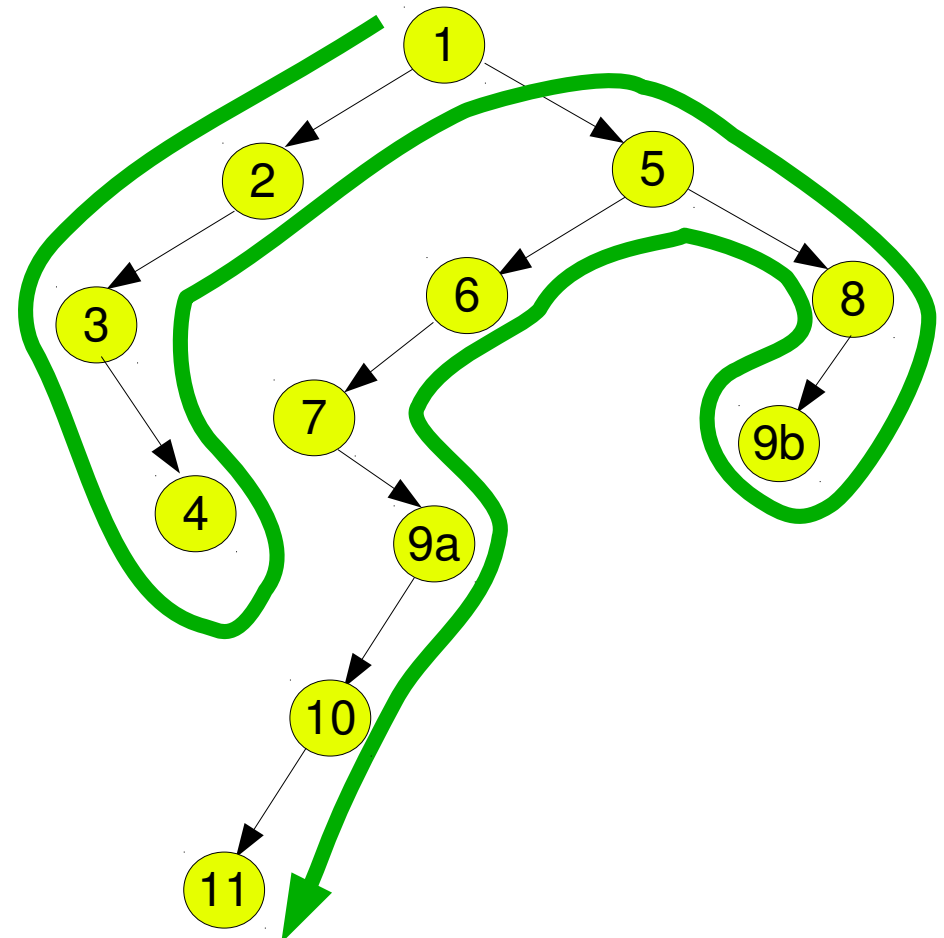
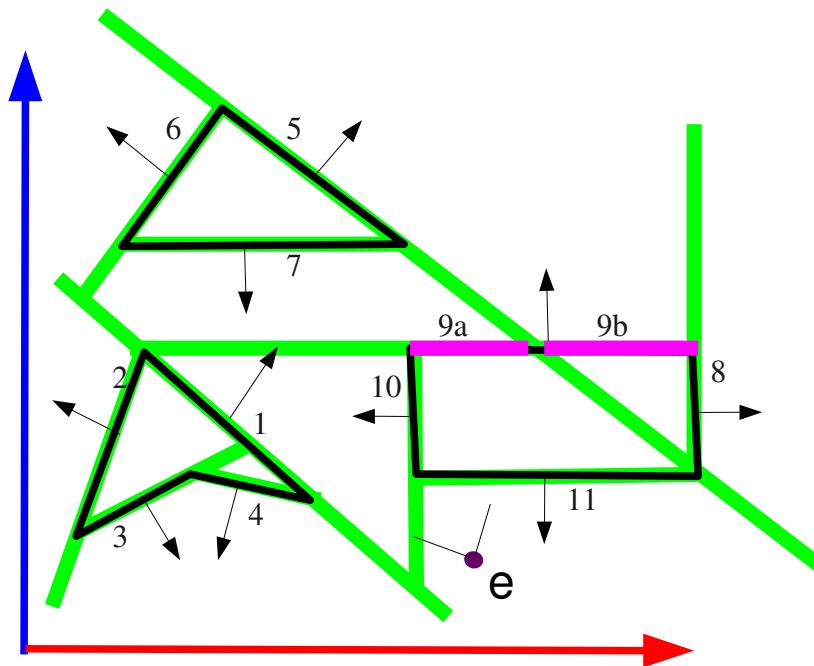
- BSP Tree construction



# Visibility

- BSP Tree traversal

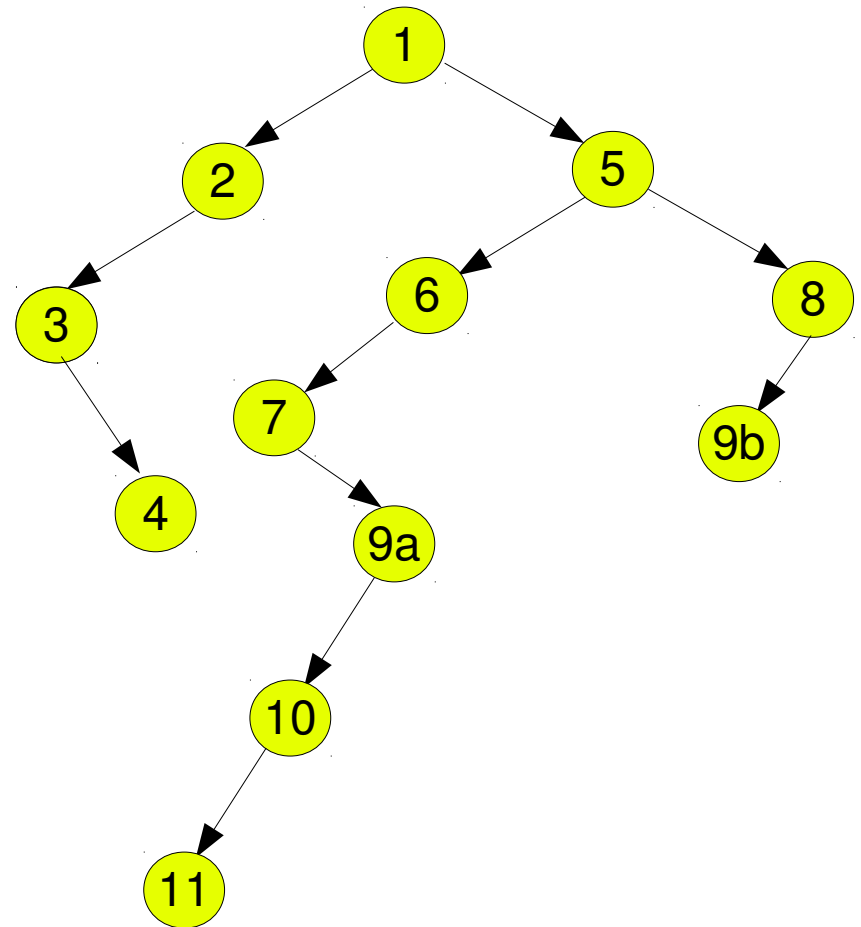
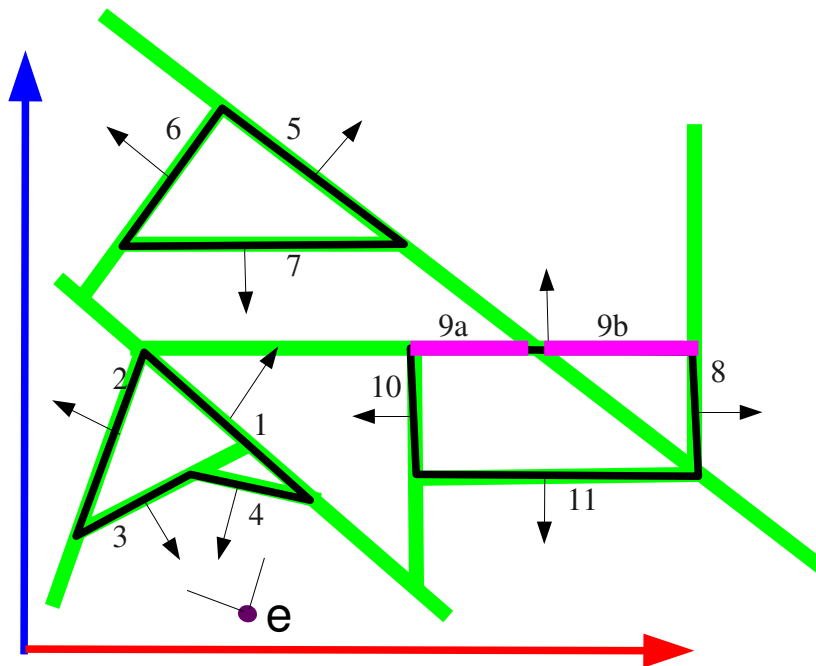
- If  $e$  is outside (or in front of) a face  $i$ 
  - Draw everything behind  $i$ , Draw  $i$ , Draw everything in front of  $i$
- If  $e$  is inside a (or behind) face  $i$ 
  - Draw everything in front of  $i$ , Draw  $i$ , Draw everything behind  $i$



# Visibility

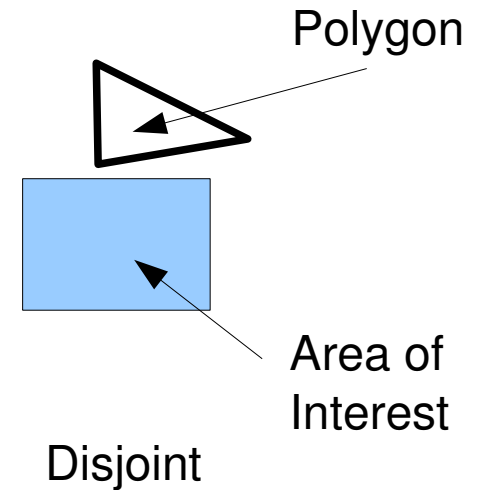
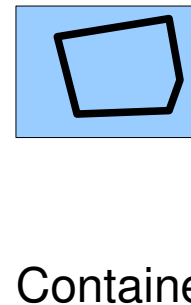
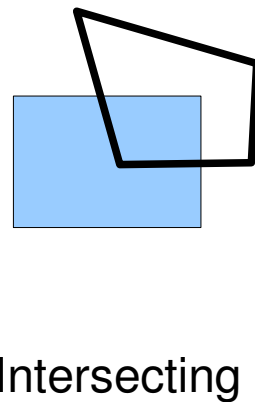
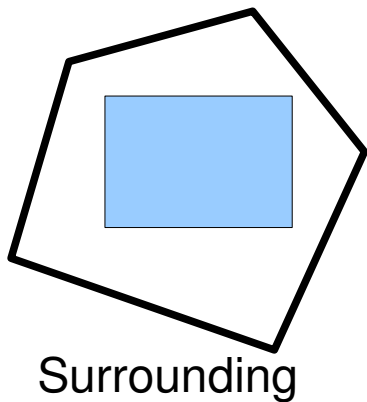
- BSP Tree traversal

- If  $e$  is outside (or in front of) a face  $i$ 
  - Draw everything behind  $i$ , Draw  $i$ , Draw everything in front of  $i$
- If  $e$  is inside a (or behind) face  $i$ 
  - Draw everything in front of  $i$ , Draw  $i$ , Draw everything behind  $i$



# Visibility

- Warnock's Algorithm



Algorithm:

Consider the projected image area

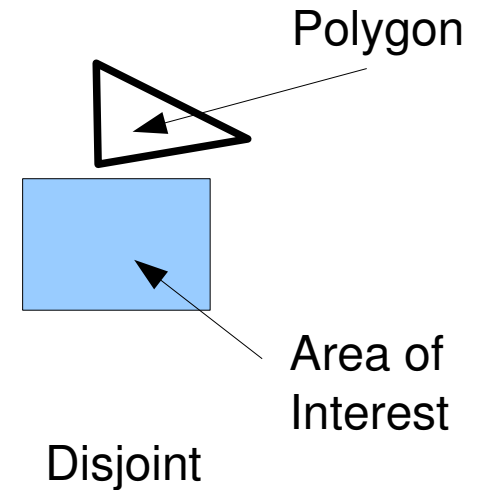
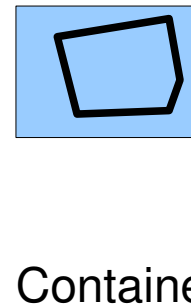
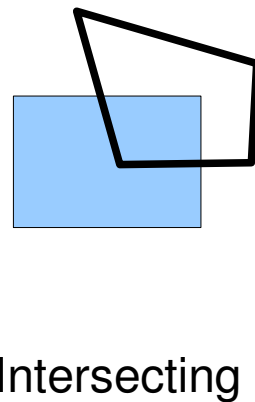
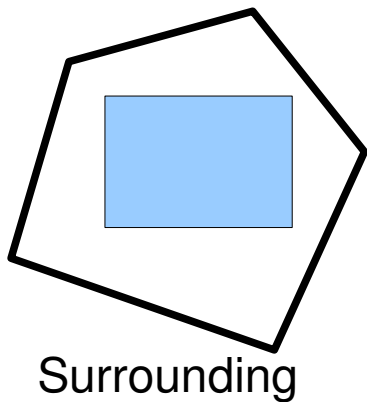
**If** it is easy to decide which polygons are visible in the area

**then** display

**else** subdivide the area and recurse with each subdivided area

# Visibility

- Warnock's Algorithm

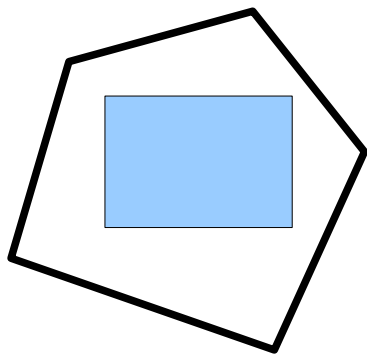


No subdivision for an area is required if

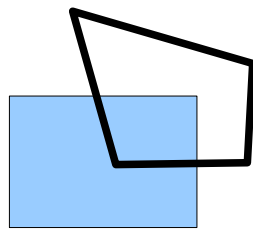
- All the polygons are disjoint with it : fill background color in the area.
- Only one intersecting or only one contained polygon: The area is filled first by background color, then the polygon part contained in the area.
- Only one surrounding polygon (no contained and intersecting polygons): The area is filled with the color of the surrounding polygon.
- More than one polygon is intersecting, contained in, or surrounding the area, with surrounding polygon in front: Fill the area with the color of the surrounding polygon.

# Visibility

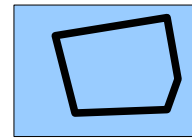
- Warnock's Algorithm



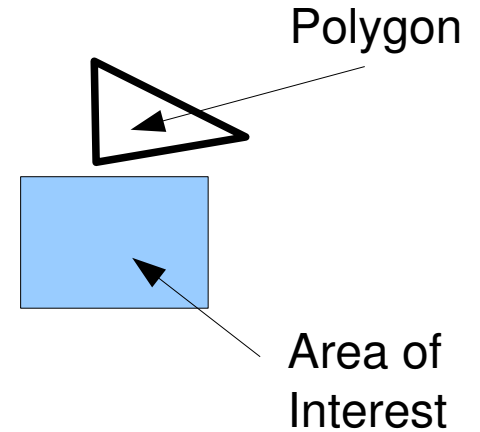
Surrounding



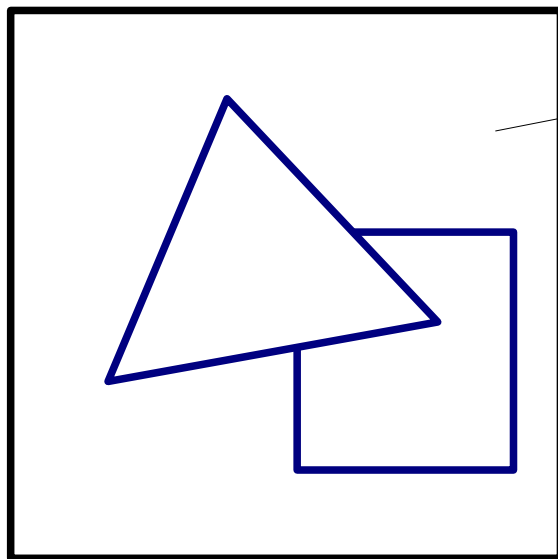
Intersecting



Contained



Disjoint

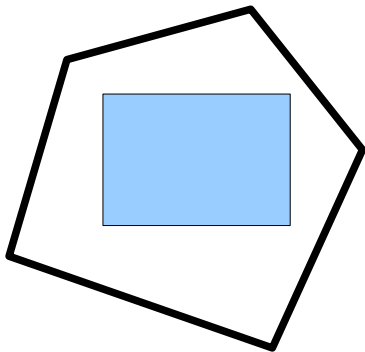


→ The starting area is the whole image.

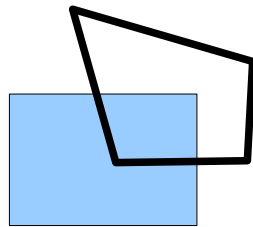


# Visibility

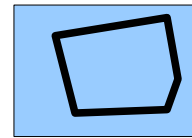
- Warnock's Algorithm



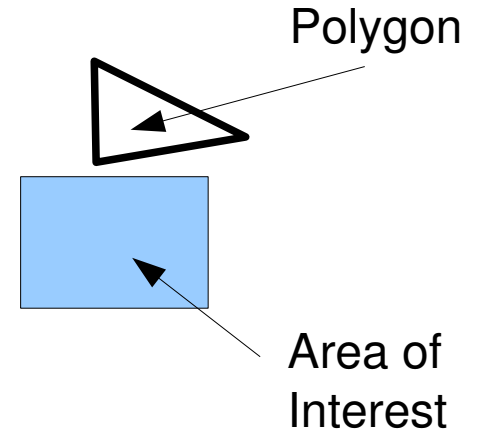
Surrounding



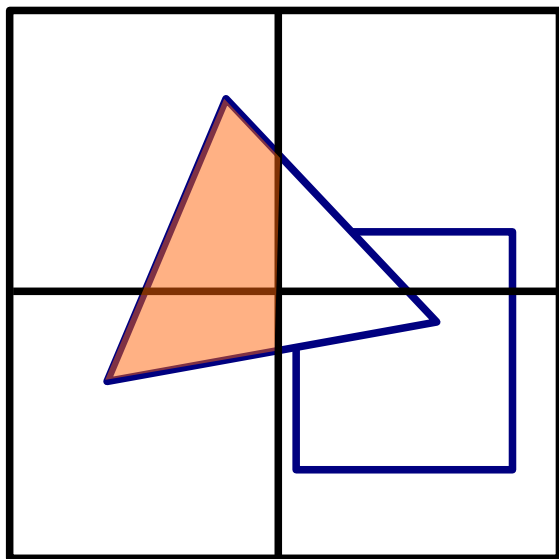
Intersecting



Contained



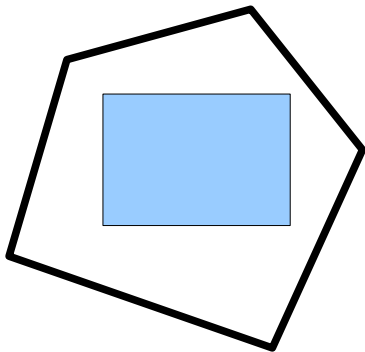
Disjoint



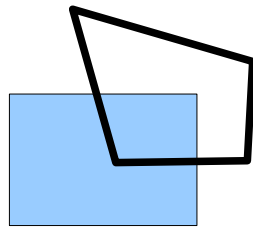
Test in the area and subdivide.

# Visibility

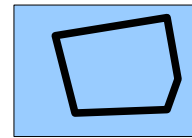
- Warnock's Algorithm



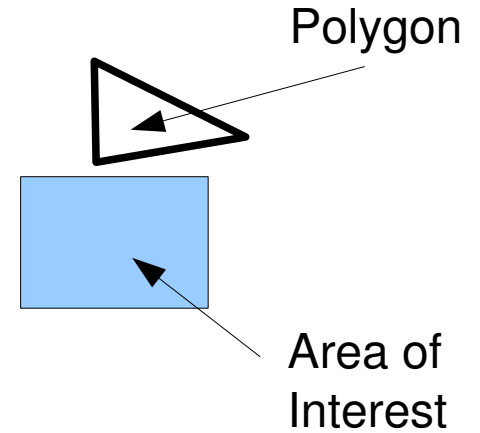
Surrounding



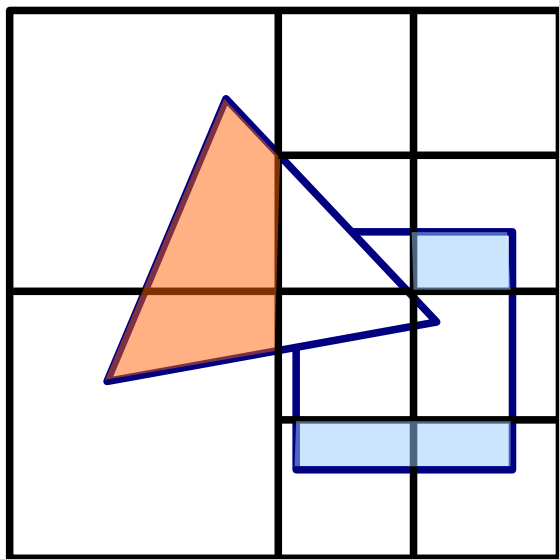
Intersecting



Contained



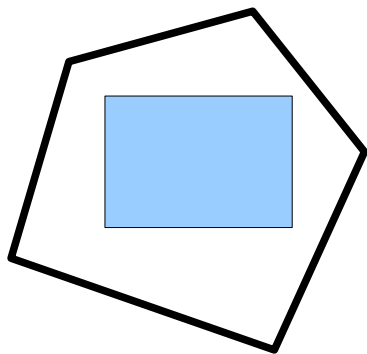
Disjoint



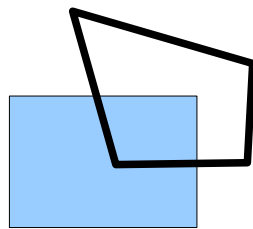
Test in the area and subdivide.

# Visibility

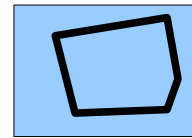
- Warnock's Algorithm



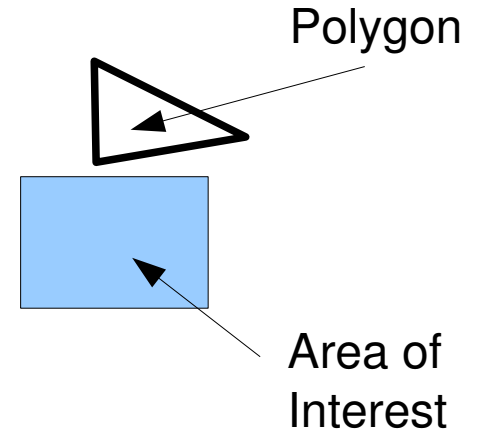
Surrounding



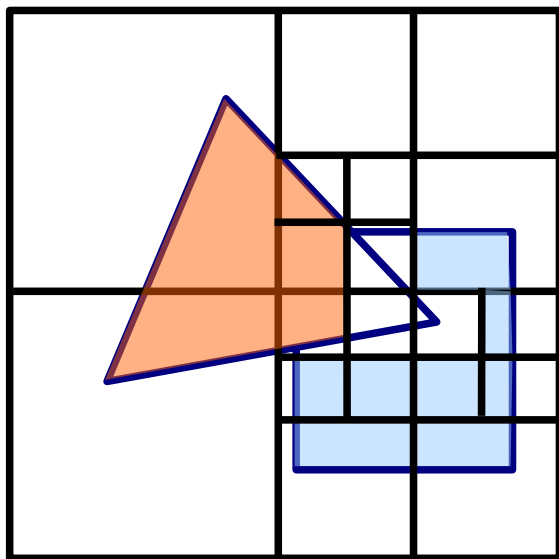
Intersecting



Contained



Disjoint



In the worst case you can end up subdividing upto pixel level.