** AD HOC & NORMAL THINGS #include<bits/stdc++.h> using namespace std; typedef long long ll: // policy Based ds #include<ext/pb_ds/assoc_contain</pre> er.hpp> //#include<ext/pb ds/tree policy .hpp> using namespace __gnu_pbds; typedef tree<long long , null type, greater equal<long long>, rb_tree_tag,tree_order_statistic s_node_update> ordered_set; // cout<<*os.find_by_order(val)<<en</pre> dl: // k-th element it // less_equal = multiset, less = set, greater_equal = multiset decreasing, greater = set decreaseing // cout<<os.order_of_key(val)<<endl</pre> ; // strictly smaller or greater #define order(s, x) s.order_of_key(x) #define elemat(s ,x) s.find by order(x) #define boost ios base::sync with stdi o(0); cin.tie(0); cout.tie(0); #define endl "\n" #define all(x) x.begin(), x.end() #define read freopen("input.txt","r", stdin) #define freopen("output.txt", "w" write ,stdout) #define pb push back #define ff first #define ss second #define GCD(a, b) __gcd(a, b) #define PI 2.0124 * acos(0.0)125 #define LCM(a, b) (a * b) /GCD(a, b)126

```
#define mem(a, b) memset(a, b,
sizeof(a))
#define popcountL
__builtin_popcountll
#define popcount
__builtin_popcount
inline bool checkBit(int N, int
pos){return(bool)(N & (1 <<</pre>
pos));}
inline int setBit(int N, int
pos) { return N = N | (1 <<
pos): }
inline int unsetBit(int N, int
pos) {return N = (N & (\sim(1 <<
pos))); }
inline int toggleBit(int N, int
pos) \{ return \ N = (N \ (1 <<
pos)); }
const ll sz=2e7+123;
#define INF 10000000000000000007
const ll MOD=1000000007:
const ll base = 31;
#define stringLen
18446744073709551620
inline void normal(ll &a) { a %=
MOD; (a < 0) && (a += MOD); }
inline ll modMul(ll a, ll b) { a
%= MOD, b %= MOD; normal(a),
normal(b); return (a*b)%MOD; }
inline ll modAdd(ll a, ll b) { a
%= MOD, b %= MOD; normal(a),
normal(b); return (a+b)%MOD; }
inline ll modSub(ll a, ll b) { a
%= MOD, b %= MOD; normal(a),
normal(b); a -= b; normal(a);
return a: }
inline ll modPow(ll b, ll p) {
ll r = 1; while(p) { if(p&1) r =
modMul(r, b); b = modMul(b, b);
p >>= 1; } return r; }
inline ll modInverse(ll a) {
return modPow(a, MOD-2); }
inline ll modDiv(ll a, ll b) {
return modMul(a, modInverse(b));
//Graph direction array[8]
//dx[]={0,0,1,-1,-1,1,1,-1};
//dy[]={1,-1,0,0,-1,-1,1,1};
//Bishop direction array[8]
//dx[]={0,0,1,-1,-1,1,1,-1};
```

```
//dv[]={1,-1,0,0,-1,-1,1,1};
//Knight Direction array[8]
//dx[]={1,1,2,2,-1,-1,-2,-2};
//dy[]={2,-2,1,-1,2,-2,1,-1};
** NUMBER THEORY
FAISAL AMIN ABIR
PRIME GENERATION
bitset<sz>is prime:
vi prime:
void primeGen(int n){
for(int i=3: i<=n;</pre>
i+=2)is_prime[i]=1;
int nn = sqrt(n)+1;
for(ll i=3; i<nn; i+=2){</pre>
if(is prime[i]==0)continue;
for(int j=i*i; j<=n; j+=(i+i)){</pre>
is_prime[j]=0;}}
is_prime[2]=1;
prime.pb(2);
for(int i=3; i<=n; i+=2){
if(is_prime[i])prime.pb(i);}}
PRIME FACTORIZATION
vector<long
long>factorization(long long
n){//0(sqrt(n)/ln(sqrt(n)) +
log2 n)
vector<long long>factors;
for(auto u:prime){
if(1LL*u*u > n) break;
if(n%u==0){// factors.push_back
(u)://for generating unique
factors keep this line here
while(n\%(u)==0){
factors.push_back(u);//for
generating all factors keep this
line here
n/=(u);}}
if(n>1)factors.push_back(n);
return factors;}
SEGMENTED SIEVE
vector<char> segmentedSieve(long
long L.long long R){
// generate all primes up to
sgrt(R)
long long lim = sqrt(R);
vector<char> mark(lim + 1,
false):
```

```
vector<long long> primes;
for (long long i = 2; i <= lim;</pre>
++i) {
if (!mark[i]) {
primes.emplace back(i);
for (long long
j=i*i;j<=lim;j+=i)</pre>
mark[j]=true;}}
vector<char> isPrime(R - L + 1,
true):
for (long long i:primes)
for (long long j=max(i*i, (L+i-
1)/i*i);j<=R;j+=i)
isPrime[j-L]=false:
if (L==1) isPrime[0] = false;
return isPrime:}
SUM OF DIVS
long long SOD(long long n){
long long res=1;
for(auto u:prime){
if(1LL*u*u > n)break:
if(n%u==0){
long long sum=1;
long long power = 1;
while(n%u==0){
n/=u:
power *= u;
sum += power;}
res *= sum;}}
if(n>1)res*=(1+n);
return res:}
SUM OF NUMBER OF DIVS
int SNOD(int n){
int sq = sqrt(n), res=0;
for(int i=1; i<=sq; i++){
res += (n/i) - i;
res *= 2:
res += sa:
return res: }
NUMBER OF DIVS
11 NOD(11 n){
ll ans=1:
if(n>1000000000000){
for(ll i=0::++i){
if(prime[i]*prime[i]*prime[i]>n)
break;
if(n%prime[i]==0){
ll cnt = 0;
```

x = v1;

```
while (n%prime[i]== 0){
                                    for(int j = 0; j < N; ++j) {
n /= prime[i];
                                    if (j == 0 || j == i) ncr[i][j]
cnt++;}
                                    = 1;
ans*=(cnt+1);}}
                                    else ncr[i][j] = ncr[i-1][j-1]
if(isprime(n)){ans*=2;}
                                    +ncr[i-1][j];
                                    }}}
if(issquareprime(n)){ans*=3;}
                                    NCR%M USING MODULAR
else if(n!=1){ans*=4;}}
                                    MULTIPLICATIVEINVERSE
                                    void precal(){
else!
                                    fact[0]=invFact[0]=1;
ll limit=sqrt(n);
for (11
                                    for(int i=1; i<=N; i++){</pre>
i=0;prime[i]<=limit;++i){</pre>
                                    fact[i]=((fact[i-
if(n%prime[i]== 0){
                                    1]%MOD)*(i%MOD))%MOD;}
ll cnt = 0;
                                    invFact[N]=bigmod(fact[N],MOD-
while (n% prime[i]== 0){
                                    2);
n /= prime[i];
                                    for(int i=N-1; i>=1; i--){
                                    invFact[i]=((invFact[i+1]%MOD)*(
cnt++:
                                    (i+1)%MOD))%MOD;}}
ans*=(cnt+1);
                                    cout<<((fact[n]*invFact[r])%MOD*</pre>
limit=sqrt(n);
                                    invFact[n-r])%MOD<<endl;</pre>
                                    //**ncr if it stays in long
                                    long**
if(n!=1)ans*=2;}
                                    ll n,r,ans=1;
return ans;
                                    cin>>n>>r;
                                    for(int i=1; i<=r; i++){</pre>
//for NOD count each prime
                                    ans=ans*(n-i+1);
factors+1 and multiply all of
                                    ans/=i:}
them 2,2,3,3,3 (3)*(4)
                                    LUCAS THEOREM(N AND R IS VERY
                                    BIG BUT MOD IS SMALL)
                                    precal(){factorial and inverse
GEOEMTRIC SUM
//**Give a,n will give
                                    factorialmod}
a^1+a^2+a^3+...+a^n**
                                    ll Lucas(ll n,ll r){
const ll MOD=1e9+7;
                                    if(r<0||r>n){
ll GeoSum(ll a, ll n){
                                    return 0:}
ll sz = 0;ll ret = 0;ll mul = 1;
                                    if(r==0||r==n){
int MSB = 63 -
                                    return 1:}
__builtin_clzll(n);
                                    if(n>=MOD){
while(MSB >= 0){
                                    return(Lucas(n/MOD,r/MOD)%MOD*Lu
ret = ret * (1 + mul); mul =
                                    cas(n%MOD,r%MOD)%MOD)%MOD;}
(mul *mul) % MOD; sz <<= 1;
                                    return(((fact[n]*invFact[r])%MOD
if( (n >> MSB) & 1) {
                                    )*invFact[n-r])%MOD;}
mul = (mul *a) % MOD; ret +=
                                    EXTENDED GCD AND LINEAR
mul; sz++;}
                                    DIOPHANTINE EQUATION
ret %= MOD; MSB--;}
                                    int gcd(int a, int b, int& x,
return ret:}
                                    int& v) {
NCR USING RECURRENCE
                                    if (b == 0) {
**ncr using recurrence{nCr = (n-
                                    x = 1; y = 0;
1)Cr + (n-1)C(r-1)**
                                    return a;}
void fncr(){
                                    int x1, y1;
for(int i = 0; i < N; ++i) {</pre>
                                    int d = gcd(b, a % b, x1, y1);
```

```
y = x1 - y1 * (a / b);
return d;}
LINEAR DIOPHANTINE
bool find any solution(int a.
int b, int c, int &x0, int &y0,
int &g) {
g = gcd(abs(a), abs(b), x0, y0);
if (c % g) {
return false:}
x0 += c / g;
y0 *= c / g;
if (a < 0) x0 = -x0;
if (b < 0) y0 = -y0;
return true:}
void shift_solution(int & x, int
& y, int a, int b, int cnt) {
x += cnt * b;
v -= cnt * a;}
int find_all_solutions(int a,
int b, int c, int minx, int
maxx, int miny, int maxy) {
int x, y, g;
if (!find_any_solution(a, b, c,
x, y, g)
return 0;
a /= g;
b /= g:
int sign_a = a > 0 ? +1 : -1;
int sign_b = b > 0 ? +1 : -1;
shift_solution(x, y, a, b, (minx
- x) / b);
if (x < minx)</pre>
shift_solution(x, y, a, b,
sign b);
if(x > maxx)
return 0;
int lx1 = x;
shift_solution(x, y, a, b, (maxx
- x) / b);
if(x > maxx)
shift_solution(x, y, a, b, -
sign_b);
int rx1 = x;
shift_solution(x, y, a, b, -
(miny - y) / a);
if (y < miny)</pre>
shift_solution(x, y, a, b, -
sign a);
if (y > maxy)
```

```
return 0:
int lx2 = x;
shift_solution(x, y, a, b, -
(maxy - y) / a);
if (v > maxv)
shift_solution(x, y, a, b,
sign_a);
int rx2 = x;
if (lx2 > rx2)
swap(lx2, rx2);
int lx = max(lx1, lx2);
int rx = min(rx1, rx2);
if (lx > rx)
return 0:
return (rx - lx) / abs(b) + 1;
FAYSAL AHAMMED CHOWDHURY
LINEAR SIEVE in O(n) upto 10<sup>7</sup>
but memory takes 32 times more:
const int N = 10000000;
vector<int> spf(N + 1);
vector<int> primes;
void linear_sieve(){ // O(n)
for (int i = 2; i \le N; ++i){
if (spf[i] == 0){
spf[i] = i;
primes.push_back(i);}
for (int j = 0; i * primes[j] <=</pre>
N: ++i)
spf[i * primes[j]] = primes[j];
if (primes[j] == spf[i])
{break;}}}
```

SPF SIEVE

int spf[N];

spf[i] = i;}

const int N = 1e6 + 9;

for (int i = 2; i < N; i++) {

for (int i = 2; i < N; i++) {

spf[j] = min(spf[j], i);}}}

SOD: $((p1^{e1+1}-1)/p1-1) *$

 $((p2^{e^{2+1}}-1)/p^2-1) * ...$

DIVISIBILITY BY 11:

for (int j = i; j < N; j += i) {

void spf_sieve() {

if (spf[i] == i) {

```
10-14-10 on -1

4123 = (4x103)+(1x101)+(2x10)+3=

= (4x(-1))+(1x(-1))++ (2x10)+3=

= (-4+1-2+3)-1-11
```

Legendre's Formula:

```
(N! / p^x) max value of x (p
must be prime)
int legendre(int n, int p){
int ex = 0;
while(n) {
ex += (n / p);
n /= p;}
return ex;}
```

Digit Count of a number:

log10(n) + 1 (log10 for 10 base number)

How many Trailing zeros of n? — Max power of base which divides

Phi function:

```
\begin{split} \Phi(n) &= \Phi\left(\rho_1^{e_1} \times \rho_1^{e_2} \times \dots \times \rho_r^{e_r}\right) \\ &= \Phi\left(\rho_1^{e_1}\right) + \Phi\left(\rho_2^{e_2}\right) \times \dots \times \rho_r^{e_r}\right) \\ &= \rho^{e_1} \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \rho_2^{e_2} \times \left(\frac{\rho_2 - 1}{\rho_2}\right) \times \dots \times \rho_r^{e_r}\left(\frac{\rho_r - 1}{\rho_r}\right) \\ &= \left(\rho_1^{e_1} \times \rho_2^{e_2} \times \dots \times \rho_r^{e_r}\right) \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \dots \times \rho_r^{e_r}\right) \\ &= \rho^{e_1} \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \left(\frac{\rho_2 - 1}{\rho_2}\right) \times \dots \times \rho_r^{e_r}\right) \\ &= \rho^{e_1} \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \left(\frac{\rho_1 - 1}{\rho_2}\right) \times \left(\frac{\rho_2 - 1}{\rho_2}\right) \times \dots \times \rho_r^{e_r}\right) \\ &= \rho^{e_1} \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \left(\frac{\rho_1 - 1}{\rho_2}\right) \times \left(\frac{\rho_2 - 1}{\rho_2}\right) \times \dots \times \rho_r^{e_r}\right) \\ &= \rho^{e_1} \times \left(\frac{\rho_1 - 1}{\rho_1}\right) \times \left(\frac{\rho_1 - 1}{\rho_2}\right) \times \left(\frac{\rho_2 - 1}{\rho_2}\right) \times \dots \times \rho_r^{e_r}\right)
```

* for n > 2, phi(n) is always
even
* sum of all phi(d) - divisors

of n, is n.

Euler Totient Function:
// if we need phi(x) multiple
times, then memoize it
map<int, int> dp;
int phi(int n) {
 if (dp.count(n)) return dp[n];
 int ans = n, m = n;
 for (int i = 2; i * i <= m; i++)
 {
 if (m % i == 0) {
 while (m % i == 0) m /= i;
 }
}</pre>

```
ans = ans / i * (i - 1);}
if (m > 1) ans = ans / m * (m -
return dp[n] = ans;}
Phi from 1 to n in O(nlog log
void phi_1_to_n(int n) {
vector<int> phi(n + 1);
for (int i = 0; i <= n; i++)
phi[i] = i;
for (int i = 2; i <= n; i++) {
if (phi[i] == i) {
for (int j = i; j <= n; j += i)
phi[j] -= phi[j] / i;}}}
Logarithm:
log(ab) = log(a) + log(b)
log(a^x) = xlog(a)
First K digit of n^k:
int firstk(int n, int k) {
double a = k * log10(n);
double b = a - floor(a);
double c = pow(10, b);
return floor(c * 100);}
Series:
Arithmetic progression:
S(n): (n/2)*(a+p) p is last
element
0r, S(n) = (n/2) * (2a + (n-1))
d) d is common difference
Geometric Progression:
S(n) = (a * (1 - r^n)) / (1-r) r
< 1
S(n) = (a * (r^n - 1)) / (r-1) r
> 1
* 1^2 + 2^2 + ... + n^2 = (n *
(n+1) * (2n+1)) / 6
* 1^3 + 2^3 + ... + n^3 = (n^2 *
(n+1)^2) / 4
Problems:
* Minimal natural number N, so
that N! contains exactly Q
zeroes on the trail.
- Binary search over N and find
how many trailing zeros N has by
Legendre's formula.
* Given a number N^M, find out
the number of integer bases in
which it has exactly T trailing
zeroes:
```

```
int
solve_greater_or_equal(vector<in</pre>
t> e, int t) {
int ans = 1:
for(auto i: e) {
ans = 1LL * ans * (i / t + 1) %
mod;
return ans;
int solve_equal(vector<int> e,
int t) {
return
(solve_greater_or_equal(e, t) -
solve_greater_or_equal(e, t + 1)
+ mod) % mod;
int main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, m, t, cs = 0;
while(cin >> n >> m >> t and n
!= 0) {
vector<int> e;
for(int i = 2; i * i <= n; i++)</pre>
if(n % i == 0) {
int ex = 0;
while(n % i == 0) {
ex++;
n /= i;
e.push_back(ex * m);
if(n > 1) e.push_back(m);
cout << "Case " << ++cs << ": "
<< solve equal(e, t) << '\n';
return 0;
* n! (factorial n) has at least
t trailing zeroes in b based
number system. Given the value
of n and t, what is the maximum
possible value of b?
```

```
const int N = 1e5 + 9, mod =
10000019;
vector<bool> is_prime(N, true);
vector<int> primes;
int main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
sieve():
int t, cs = 0; cin >> t;
while(t--) {
int n, zeroes; cin >> n >>
zeroes:
vector<pair<int, int>> ans;
for(auto p: primes) {
if(p > n) break;
int pw = legendre(n, p);
if(pw / zeroes != 0) {
ans.push_back({p, pw/ zeroes});
int max base = 1;
for(auto i: ans) {
max_base = 1LL * max_base *
power(i.first, i.second) % mod;
cout << "Case " << ++cs << ": ";
cout << (ans.size() == 0 ? -1 :</pre>
max base) << '\n';
return 0;
Combinatorics:
* nCr, nPr using recurrence -
const int N = 2005, mod = 1e9 +
int C[N][N], fact[N];
void prec() { // O(n^2)
// nCr = (n-1)C(r-1) + (n-1)Cr
for (int i = 0; i < N; i++) {
C[i][0] = C[i][i] = 1:
for (int j = 1; j < N; j++) {
C[i][j] = (C[i-1][j-1] + C[i
- 1][j]) % mod;
```

```
fact[0] = 1;
for (int i = 1; i < N; i++) {
fact[i] = 1ll * fact[i - 1] * i
% mod;
int nCr(int n, int r) {
if (n < r) return 0;</pre>
return C[n][r];
int nPr(int n, int r) {
if (n < r) return 0;
return 1ll * C[n][r] * fact[r] %
mod:
Combinations (nCr, nPr):
const int N = 1e6 + 1, mod =
1000003:
int fact[N], ifact[N];
int inverse(int x) {
return power(x, mod - 2, mod);
void prec() {
fact[0] = 1;
for (int i = 1; i < N; i++) {
fact[i] = 1ll * fact[i - 1] * i
% mod;
ifact[N - 1] = inverse(fact[N -
for (int i = N - 2; i >= 0; i--)
ifact[i] = 1ll * ifact[i + 1] *
(i + 1) \% mod;
int nCr(int n, int r) {
return 1ll * fact[n] * ifact[r]
% mod * ifact[n - r] % mod;
int nPr(int n, int r) {
return 1ll * fact[n] * ifact[n -
r] % mod;
```

Stars and Bars: * Find the number of k-tuples of non-negative integers whose sum is n. (n + k - 1)! / (n! * (k-1)!)or C(n+k-1, n)* Find the number of k-tuples of non-negative integers whose sum is <= n. - (n + k)! / (n! * k!) or C(n+k, n)* Combinations with repetitions - C(n+k-1, k)* How many ways to go from (0,0)to (n.m) C(n+m, n) Pascals Triangle is equivalent to nCr 10 10

Multinomial Coefficient

(a1+a2+..+ak)^n Powers are given of k numbers. coefficient? int n, k; cin >> n >> k; int ans = fact[n]; for (int i = 1; i <= k; i++) { int x; cin >> x; ans = 1ll * ans * ifact[x] % mod;

Binomial Theorem:

 $\sum C(n,i) = 2^{n-1}$

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

Properties of Pascal's Triangle: i = 0 to $n \sum C(n,i) = 2^n$ i = 0 to n where i is even

```
i = 0 to n where i is odd
\sum C(n,i) = 2^{n-1}
Built-in Functions:
set(), reset(), flip(), count(),
test(), any(), none(), all(),
to_ullong()
__builtin_popcount(x),
__builtin_clz(x),
__builtin_ctz(x)
* Power Tower:
 n^x \mod m = n^{\varphi(m) + x \mod \varphi(m)} \mod m
const int N = 1e5 + 9;
using ll = long long;
map<ll, ll> mp;
ll phi(ll n) {
if (mp.count(n)) return mp[n];
ll ans = n, m = n;
for (ll i = 2; i * i <= m; i++)
if (m % i == 0) {
while (m % i == 0) m /= i;
ans = ans / i * (i - 1);
if (m > 1) ans = ans / m * (m -
return mp[n] = ans;
inline ll MOD(ll x, ll m) {
if (x < m) return x;</pre>
return x % m + m;
ll power(ll n, ll k, ll mod) {
ll ans = MOD(1, mod);
while (k) {
if (k \& 1) ans = MOD(ans * n,
mod):
n = MOD(n * n, mod);
k >>= 1;
return ans;
int a[N]:
// if x \ge log2(m), then a^x =
a^(MOD(x, phi(m))) % m
ll yo(ll l, ll r, ll m) {
if (l == r) return MOD(a[l], m);
```

```
if (m == 1) return 1;
return power(a[l], yo(l + 1, r,
phi(m)), m);
int32 t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, m; cin >> n >> m;
for (int i = 1; i <= n; i++) {
cin >> a[i];
int q; cin >> q;
while (q--) {
int l, r; cin >> l >> r;
cout << yo(l, r, m) % m << '\n';</pre>
return 0;
```

Expected value:

আমরা আরো জেনারেলাইজেশন করতে পারি, আমরা এতক্ষণ ধরেছি n টা পাশে 1 থেকে n পর্যন্ত প্রতিটা সংখ্যা একবার করে আছে। এখন আমরা ধরো ভাইসের i তম সাইডে যে সংখ্যা লেখা আছে সেটা হলো x(i) এবং ভাইস ছুড়ে মারলে i তম সাইডটা পাবার প্রোবাবিলিটি আগের মতোই p(i)। এখন ফর্মুলাটা হবে $E=p(1)*x(1)+p(2)*x(2)+\ldots+p(n)*x(1)=\sum_{i=1}^n p(i)\cdot x(i)$ ৷ সহজভাবে বলতে গেলে প্রতিটা i এর জন্য আমরা i তম সাইডে যে সংখ্যাটা লেখা আছে সেটাকে i তম সাইড পাবার প্রোবাবিলিটি দিয়ে গুণ করছি এবং সবগুলো গুণফল যোগ করে দিচ্ছি।

** DATA STRUCTURES

Faysal Ahammed

Segment Tree:

```
const int N = 1e5 + 9;
int a[N];
struct ST {
int tree[4 * N];
void build(int n, int b, int e)
if(b == e) {
tree[n] = a[b]; // change here
return;
int mid = (b + e) >> 1, l = n <<
1, r = l + 1;
build(l, b, mid);
build(r, mid + 1, e);
```

```
tree[n] = tree[l] + tree[r]; //
change here
void upd(int n, int b, int e,
int i, int x) {
if(b > i || e < i) return;
if(b == e \&\& b == i) {
tree[n] = x; // change here
return:
int mid = (b + e) >> 1, l = n <<
1, r = l + 1;
upd(l, b, mid, i, x);
upd(r, mid + 1, e, i, x);
tree[n] = tree[l] + tree[r]; //
change here
int query(int n, int b, int e,
int i, int j) {
if(b > j || e < i) return 0; //</pre>
return appropriate value
if(b >= i && e <= j) return
tree[n]:
int mid = (b + e) >> 1, l = n <<
1, r = l + 1;
int L = query(l, b, mid, i, j);
int R = query(r, mid + 1, e, i,
return (L + R); // change this
} st;
Segment Tree Lazy:
const int N = 1e5 + 9;
int a[N];
struct ST {
int tree[4 * N], lazy[4 * N];
ST() {
memset(tree, 0, sizeof(tree));
memset(lazy, 0, sizeof(lazy));
void push(int n, int b, int e) {
if(lazy[n] == 0) return;
tree[n] += lazy[n] * (e - b +
1); // change here
if(b != e) {
int l = n << 1, r = l + 1;
lazy[l] += lazy[n]; // change
here
```

```
lazy[r] += lazy[n]; // change
here
lazy[n] = 0;
void build(int n, int b, int e)
lazy[n] = 0;
if(b == e) {
tree[n] = a[b]; // change here
return:
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
build(l, b, mid);
build(r, mid + 1, e);
tree[n] = tree[l] + tree[r]; //
change here
void upd(int n, int b, int e,
int i, int j, int x) {
push(n, b, e);
if(b > j || e < i) return;
if(b >= i \delta \delta e <= j) {
lazy[n] += x; // change here
push(n, b, e);
return:
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
upd(l, b, mid, i, j, x);
upd(r, mid + 1, e, i, j, x);
tree[n] = tree[l] + tree[r]; //
change here
int query(int n, int b, int e,
int i, int j) {
push(n, b, e);
if(b > j || e < i) return 0; //
return appropriate value
if(b >= i && e <= j) return
tree[n];
int mid = (b + e) >> 1, l = n <<
1, r = l + 1;
int L = query(l, b, mid, i, j);
int R = query(r, mid + 1, e, i,
return L + R; // change here
} st;
```

```
Strongest Community:
const int N = 1e5 + 9;
int a[N];
struct node {
int first_element,
first_element_cnt;
int last_element,
last_element_cnt;
int max_cnt;
};
node merge(node l, node r) {
if(l.first_element == -1) return
if(r.first_element == -1) return
node ans;
ans.max_cnt = max(l.max_cnt,
r.max_cnt);
if(l.last_element ==
r.first element) {
ans.max_cnt = max(ans.max_cnt,
l.last_element_cnt +
r.first_element_cnt);
ans.first element =
l.first_element;
ans.first_element_cnt =
l.first_element_cnt;
if(l.first_element ==
r.first_element) {
ans.first_element_cnt +=
r.first_element_cnt;
ans.last_element =
r.last_element;
ans.last_element_cnt =
r.last_element_cnt;
if(r.last element ==
1.last_element) {
ans.last_element_cnt +=
1.last element cnt:
return ans;
struct ST {
node tree[4 * N];
```

```
void build(int n, int b, int e)
if(b == e) {
tree[n].first_element = a[b];
tree[n].first_element_cnt = 1;
tree[n].last_element = a[b];
tree[n].last_element_cnt = 1;
tree[n].max_cnt = 1;
return:
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
build(l, b, mid);
build(r, mid + 1, e);
tree[n] = merge(tree[l],
tree[r]); // change here
node query(int n, int b, int e,
int i, int j) {
if(b > j || e < i) return {-1, -
1, -1, -1, -1};
if(b >= i && e <= j) return
tree[n];
int mid = (b + e) >> 1, l = n <<
1, r = l + 1;
return merge(query(l, b, mid, i,
j), query(r, mid + 1, e, i, j));
// change this
} st;
Segment tree with arithmetic
progression [update the range l
to r with the arithmetic
progression a+b*(i-l)]:
using ll = long long;
const int N = 2e5 + 9;
const ll inf = 1e18;
pair<ll, ll> merge(pair<ll, ll>
l, pair<ll, ll> r) {
l.first = min(l.first, r.first);
l.second = max(l.second,
r.second);
return l:
struct ST {
pair<ll, ll> tree[4 * N];
ll lazy[4 * N];
```

```
void push(int n, int b, int e) {
if (lazy[n] == 0) return;
tree[n].first += lazy[n];
tree[n].second += lazy[n];
if (b != e) {
int l = n << 1, r = l + 1;
lazy[l] += lazy[n];
lazy[r] += lazy[n];
lazy[n] = 0;
void build(int n, int b, int e)
lazy[n] = 0;
if (b == e) {
tree[n] = \{0, 0\};
return:
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
build(l, b, mid);
build(r, mid + 1, e);
tree[n] = merge(tree[l],
tree[r]);
void upd(int n, int b, int e,
int i, int j, ll x) {
push(n, b, e);
if (b > j || e < i) return;
if (b >= i && e <= j) {
lazy[n] += x;
push(n, b, e);
return;
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
upd(l, b, mid, i, j, x);
upd(r, mid + 1, e, i, j, x);
tree[n] = merge(tree[l],
tree[r]);
pair<ll, ll> query(int n, int b,
int e, int i, int j) {
push(n, b, e);
if (b > j || e < i) return {inf,
-inf};
if (b >= i && e <= j) return
tree[n];
int mid = (b + e) >> 1, l = n <<</pre>
1, r = l + 1;
```

```
pair<ll, ll> L = query(l, b,
mid, i, j);
pair<ll, ll> R = query(r, mid +
1, e, i, j);
return merge(L, R):
} st;
int32_t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, q; cin >> n >> q;
st.build(1, 1, n);
while (q--) {
int type; cin >> type;
if (type == 1) {
int l, r; cin >> l >> r;
if (l == r) {
cout << 1 << '\n';
continue;
pair<ll, ll> ans = st.query(1,
1, n, l + 1, r);
if (ans.first == 0 and
ans.second == 0) {
cout << 1 << '\n';
else {
cout << 0 << '\n':
}
else {
int l, r; ll a, b; cin >> l >> r
>> a >> b;
st.upd(1, 1, n, l, l, a);
if (l != r) {
st.upd(1, 1, n, l + 1, r, b);
11 x = 111 * b * (r - 1) + a;
st.upd(1, 1, n, r + 1, r + 1, -
x);
}
return 0:
Searching for the first element
greater than a given amount:
```

```
int get_first(int v, int tl, int
tr, int l, int r, int x) {
if (tl > r || tr < l) return -1;
if (t[v] <= x) return -1;
if (tl == tr) return tl;
int tm = tl + (tr - tl) / 2;
int left = get_first(2 * v, tl,
tm, l, r, x);
if (left != -1) return left;
return get_first(2 * v + 1, tm +
1, tr, l , r, x);
Counting the number of zeros,
searching for the k-th zero:
int find_kth(int v, int tl, int
tr, int k) {
if(k > t[v])
return -1;
if (tl == tr)
return tl;
int tm = (tl + tr) / 2;
if (t[v * 2] >= k)
return find_kth(v * 2, tl, tm,
k);
else
return find_kth(v * 2 + 1, tm +
1, tr, k - t[v * 2];
Faisal Amin Abir
Trie Prefix tree
struct trieNode{
int cnt:
trieNode *child[2];
trieNode(){
cnt=0:
for(int i=0; i<2; i++){</pre>
child[i]=NULL;
}}
};
trieNode *root;
void insert(int num) {
binary form
trieNode *cur=root;
for(int i=20; i>=0; i--){
int ind=(bool)(num&(1<<i));</pre>
if(!cur->child[ind]){
cur->child[ind]=new
trieNode();
```

```
cur=cur->child[ind];
cur->cnt++;
}}
**Min XOR with value set**
-1 X: Add x to set
-2 x:for each element set it to
element<sup>x</sup>
-3: print the minimum of the set
int X=0;
void solve(int test){
int type,x;
si(type);
if(type==1){
si(x):
insert(x^X);}
else if(type==2){
si(x);
X^=x;
else{
int res=querv(X);
printf("%d\n",res);
}}
** Segment Tree **
**LAZY Propagation **
const ll N = 2e5+123;
ll arr[N], t[4*N], lazv[4*N],
lazySet[4*N];
bool isSet[4*N];
ll n, m;
void build(ll v, ll l, ll r){
if(l==r){
t[v]=arr[l];
return;
ll\ mid = (l+r)>>1;
build(2*v, l, mid);
build(2*v+1, mid+1, r);
t[v] = t[2*v] + t[2*v+1];
void checkSet(ll v, ll L, ll R){
if(isSet[v]==1){
isSet[v]=0:
ll x = lazySet[v];
lazySet[v]=0;
t[v] = (R-L+1) * x;
if(L!=R){
isSet[2*v] = isSet[2*v+1] = 1;
lazy[2*v] = lazy[2*v+1] = 0;
```

```
lazySet[2*v] = lazySet[2*v+1] =
х;
void checkAdd(ll v, ll L, ll R){
if(lazy[v]!=0){
ll x = lazy[v];
lazy[v]=0;
t[v] += (R-L+1) * x;
if(L!=R){
lazy[2*v] += x;
lazy[2*v+1] += x;
void add(ll v, ll L, ll R, ll l,
ll r, ll value){
checkSet(v, L, R);
checkAdd(v, L, R);
if(L > r or R < l) return;</pre>
if( L >= l and R <= r){
t[v] += (R-L+1) * value:
if(L!=R){
lazy[2*v] += value;
lazy[2*v+1] += value;
return:
ll mid = (L+R)>>1;
add(2*v, L, mid, l, r, value);
add(2*v+1, mid+1, R, l, r,
value):
t[v] = t[2*v] + t[2*v+1];
void set_value(ll v, ll L, ll R,
ll l, ll r, ll value){
checkSet(v, L, R);
checkAdd(v, L, R);
if(L>r or R < l)return;</pre>
if(L>=l and R<=r){
t[v] = (R-L+1) * value;
if(L!=R){
isSet[2*v] = isSet[2*v+1] = 1;
lazv[2*v] = lazv[2*v+1] = 0;
lazySet[2*v] = lazySet[2*v+1] =
value;
return;
```

```
ll mid = (L+R)>>1;
set_value(2*v, L, mid, l, r,
value):
set value(2*v+1, mid+1, R, l, r
, value);
t[v] = t[2*v] + t[2*v+1];
Il query(ll v, ll L, ll R, ll l,
ll r){
checkSet(v, L, R);
checkAdd(v, L, R);
if(L>r or R<l)return 0;</pre>
if(L>=l and R <= r) return t[v];</pre>
ll mid = (L+R)>>1;
return query(2*v, L, mid, l, r)
+ query(2*v+1, mid+1, R, l, r);
void solve(){
cin>>n>>m:
for(ll i=1; i<=n; i++){</pre>
cin>>arr[i];
build(1, 1, n);
for(ll i=0; i<m; i++){</pre>
ll c;
cin>>c:
if(c==1){
ll a, b, x;
cin>>a>>b>>x;
add(1, 1, n, a, b, x);
else if(c==2){
ll a, b, x;
cin>>a>>b>>x:
set_value(1, 1, n, a, b, x);
else{
ll a, b;
cin>>a>>b:
cout << query(1, 1, n, a, b) <<</pre>
endl;
}}}
**Max subarray sum in L to R
with update**
const int mx=50005;
LL num[mx];
struct node{
```

```
LL left, right, sum, answer;
};
node tree[4*mx];
node merge(node a, node b){
node x:
x.left=max(a.left,a.sum+b.left);
x.right=max(b.right,a.right+b.su
m);
x.answer=max(max(a.answer,b.answ
er),a.right+b.left);
x.sum=a.sum+b.sum;
return x;
void buildSegmentTree(int at,int
L, int R){
if(L==R){
tree[at].left=num[L];
tree[at].right=num[L];
tree[at].sum=num[L];
tree[at].answer=num[L];
return:
int mid=(L+R)/2;
buildSegmentTree(at*2,L,mid);
buildSegmentTree(at*2+1,mid+1,R)
tree[at]=merge(tree[at*2],tree[a
t*2+1]);
void
updateSegemntTreeWithNew(int
at, int L, int R, int pos, int
value){
if(pos>R || pos<L){</pre>
return:
if(L>=pos && R<=pos){
tree[at].left=value;
tree[at].right=value;
tree[at].sum=value;
tree[at].answer=value:
return;
int mid=(L+R)/2;
updateSegemntTreeWithNew(at*2,L,
mid.pos.value);
updateSegemntTreeWithNew(at*2+1,
mid+1,R,pos,value);
tree[at]=merge(tree[at*2],tree[a
t*2+1]);
```

```
node def;
node querySegmentTree(int at,int
L,int R,int l,int r){
if(r<L || R<l)return def;</pre>
if(l<=L && R<=r) return
tree[at];
int mid=(L+R)/2;
node
x=querySegmentTree(at*2,L,mid,l,
r);
node
y=querySegmentTree(at*2+1,mid+1,
R, l, r);
return merge(x,y);
int main(){
def.answer=-100000000:
def.left=-100000000;
def.right-100000000;
def.sum=-100000000;
int n;
si(n);
Rep(i,1,n){
sl(num[i]);}
buildSegmentTree(1,1,n);
int q,l,r,x;
si(q);
while(q--){
siii(x,l,r);
if(x==0){
updateSegemntTreeWithNew(1,1,n,l
,r);
else{
node
ans=querySegmentTree(1,1,n,l,r);
printf("%lld\n",ans.answer);
return 0;
**Longest increasing
subsequence**
for(int i=n; i>=1; i--){
int qr=query(1,1,m,arr[i]+1,m);
now=query(1,1,m,arr[i],arr[i]);
now=max(now,1+qr);
update(1,1,m,arr[i],now);
```

```
**All possible longest
increasing subsequence**
for(int i=1; i<=n; i++){
scl(arr[i].x)
arr[i].y=i+1;
sort(arr+1,arr+n+1,cmp);
for(int i=1; i<=n; i++){</pre>
lln d=arr[i].y;
lln q1=query(1,1,n+1,1,d-1);
update(1,1,n+1,d,d,q1+1);
lln ans=query(1,1,n+1,1,n+1);
printf("Case %d:
%lld\n",xx,ans);
** Merge sort tree without
update **
vector<int>:: iterator child;
vector<int>vi2[4*maxii]:
int arr3[maxii]:
int n.m:
int cc=1:
void segment(int node,int b,int
e){
if(b==e){
vi2[node].pb(arr3[b]);
return:
int left=2*node;
int right=left+1;
int mid=(b+e)/2;
segment(left,b,mid);
segment(right, mid+1, e);
int ff=0,hh=0;
while(ff<vi2[left].size()</pre>
&&hh<vi2[right].size()){
if(vi2[left][ff]<=vi2[right][hh]</pre>
){
vi2[node].pb(vi2[left][ff]);
ff++;
}
vi2[node].pb(vi2[right][hh]);
hh++;
while(ff<vi2[left].size()){</pre>
vi2[node].pb(vi2[left][ff]);
ff++;
```

```
while(hh<vi2[right].size()){</pre>
vi2[node].pb(vi2[right][hh]);
hh++;
int w:
int query(int node,int b,int
e.int st.int en){
if(st>e || en<b)return 0;</pre>
if(b>=st && e<=en){
int di=vi2[node].size();
int
p=lower_bound(vi2[node].begin(),
vi2[node].end(),w)-
vi2[node].begin();
return di-p:
int mid=(b+e)/2;
int left=2*node:
int right=left+1:
int q1=querv(left.b.mid.st.en);
int
q2=query(right,mid+1,e,st,en);
return q1+q2;
**Merge sort tree with update**
#include<bits/stdc++.h>
#include<ext/pb_ds/assoc_contain</pre>
er.hpp>
#include<ext/pb_ds/tree_policy.h</pre>
#define pii pair<int,int>
using namespace __gnu_pbds;
using namespace std;
typedef tree<pii, null_type,
less<pii>, rb_tree_tag,
tree_order_statistics_node_updat
e>ordered set:
const int maxn=3e5+5;
int arr[maxn];
ordered_set segtree[4*maxn];
void build(int at,int L,int R){
if(L==R){
segtree[at].insert({arr[L],L});
return:
int mid=(L+R)>>1;
int left=at*2;
int right=at*2+1;
```

```
build(left.L.mid);
build(right, mid+1, R);
for(pii
i:segtree[left])segtree[at].inse
rt(i);
for(pii
i:segtree[right])segtree[at].ins
ert(i);
void update(int at,int L,int
R,int pos,pii rp,pii pt){
if(pos>R || pos<L){</pre>
return:
segtree[at].erase(rp);
segtree[at].insert(pt);
if(L==R){
return:
int mid=(L+R)>>1;
if(pos<=mid)update(at*2,L,mid,po</pre>
s.rp.pt);
else
update(at*2+1,mid+1,R,pos,rp,pt)
int query(int at,int L,int R,int
l,int r,int val){
if(r<L || R<l)return 0;</pre>
if(l<=L && R<=r)return
segtree[at].order_of_key({val,0}
int mid=(L+R)>>1;
return
query(at*2,L,mid,l,r,val)+query(
at*2+1, mid+1, R, l, r, val);
**Total number of subarray whose
sum less than t**
void solve(int test){
LL n.t.res=0:
sll(n,t);
Rep(i,1,n){
sl(arr[i]);
arr[i]+=arr[i-1];
build(1,1,n);
Rep(i,1,n){
res+=query(1,1,n,i,n,arr[i-
1]+t);
```

```
printf("%lld\n", res);
**Mo's Algorithm distinct
element in range**
const int N = 2e5+2;
const int BLOCK = 450;
int arr[N], n, freq[N], cnt,
ans[N]:
struct query{
int l, r, index;
}q[200001]:
void add(int value){
freq[value]++;
if(freq[value]==1)cnt++;
void remove(int value){
freq[value]--:
if(freq[value]==0)cnt--;
bool comp(query q1, query q2){
if((q1.1 / BLOCK) == (q2.1 /
BLOCK)){
return q1.r < q2.r;</pre>
return (q1.l / BLOCK ) < (q2.l /</pre>
BLOCK);
void solve(){
cin>>n;
int m:
cin>>m;
for(int i=0; i<n; i++)</pre>
cin>>arr[i]:
map<int, int>maps;
int c=0:
for(int i=0; i<n; i++){</pre>
if(maps[arr[i]]==0){
C++:
maps[arr[i]]=c;
for(int i=0; i<n; i++) arr[i] =</pre>
maps[arr[i]];
for(int i=0; i<m; i++){</pre>
int x, y;
cin>>x>>v;
x--, y--;
q[i].index = i;
q[i].l = x;
q[i].r = y;
```

```
sort(q, q + m, comp);
int L=0, R=-1;
for(int i=0; i<m; i++){
int currL = q[i].l;
int currR = q[i].r;
int indx = q[i].index;
while(L-1 >= currL){//adding
value
L--;
add(arr[L]);
while(R+1<=currR){</pre>
R++;
add(arr[R]);
while(L<currL){//removing value</pre>
remove(arr[L]);
L++;
while(R > currR){
remove(arr[R]);
R--;
ans[indx] = cnt;
for(int i=0; i<m; i++) cout <<</pre>
ans[i] << endl:</pre>
** GRAPH THEORY
Faysal Ahammed
BFS:
const int N = 1e5 + 9:
vector<int> g[N];
vector<bool> vis(N, false);
void bfs(int u) {
queue<int> q;
q.push(u);
vis[u] = true;
while(!q.empty()) {
int top = q.front(); q.pop();
for(auto v: g[top]) {
if(!vis[v]) {
q.push(v);
vis[v] = true;}}}
```

```
Find Cycle:
const int N = 2e5 + 9;
vector<int> g[N];
vector<int> par(N, -1);
vector<int> col(N, 0);
int cycle_start, cycle_end;
set<int> cycle;
void find_cycle(int u) {
col[u] = 1;
for (auto v: g[u]) {
if (col[v] == 0) {
par[v] = u;
find_cycle(v);
else if(col[v] == 1 and v !=
par[u]) {
cycle end = u:
cycle_start = v;
col[u] = 2;
int32_t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, m; cin >> n >> m;
for(int i = 1; i <= m; i++) {</pre>
int u, v; cin >> u >> v;
g[u].push_back(v);
g[v].push_back(u);
find_cycle(1);
int cur = cycle_end;
while (cur != cycle_start) {
cvcle.insert(cur):
cur = par[cur];
cycle.insert(cur);
return 0:
Topological Sort:
const int N = 1e5 + 9;
vector<int> g[N];
vector<int> indeg(N, 0);
```

```
int32_t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, m; cin >> n >> m;
while(m--) {
int u, v; cin >> u >> v;
g[u].push_back(v);
indeg[v]++;
queue<int> q:
for(int i = 1; i <= n; i++) {
if(indeg[i] == 0) {
q.push(i);
vector<int> ans;
while(!q.empty()) {
int top = q.front();
q.pop();
ans.push back(top);
for(auto v: g[top]) {
indeg[v]--;
if(indeg[v] == 0) {
q.push(v);}}}
if(ans.size() == n) {
for(auto i: ans) {
cout << i << ' ';}</pre>
cout << '\n';}
else {
cout << "IMPOSSIBLE\n";}</pre>
return 0;
Bellman Ford:
using ll = long long;
const int N = 1005;
const ll inf = 1e18;
vector<pair<int, int>> g[N];
vector<ll> dis(N, inf);
int n. m;
bool cycle:
void bellman_ford(int src) {
dis[src] = 0:
for (int i = 1; i <= n; i++) {
```

```
for (int u = 1; u <= n; u++) {
for (auto [v, w] : g[u]) {
if (dis[v] > dis[u] + w and
dis[u] != inf) {
if (i == n) cycle = true;
dis[v] = dis[u] + w;}}}}
int main() {
cin >> n >> m;
while (m--) {
int u, v, w; cin >> u >> v >> w;
g[u].push_back({ v,w });
g[v].push_back({ u,w });
cycle = false;
bellman ford(1):
for (int u = 1; u <= n; u++) {
cout << dis[u] << ' ';
cout << '\n';
return 0;
Dijkstra:
using ll = long long;
const int N = 1e5 + 9;
const ll inf = 1e18;
vector<pair<int, int>> g[N];
vector<bool> vis(N, false);
vector<ll> dis(N, inf);
int n, m;
void dijkstra(int u) {
dis[u] = 0:
priority_queue<pair<ll, int>,
vector<pair<ll, int>>,
greater<pair<ll, int>>> pq;
pq.push({ 0, u });
while (!pq.empty()) {
int selected node =
pq.top().second:
ll d = pq.top().first;
pq.pop();
if (vis[selected_node])
continue:
vis[selected_node] = true;
```

```
for (auto [v, w]:
g[selected_node]) {
if (dis[v] > (1ll * d + w)) {
dis[v] = 1ll * d + w;
pq.push({ dis[v], v });}}}
Floyd Warshall:
using ll = long long;
const int N = 505;
const ll inf = 1e18;
int g[N][N];
ll dis[N][N];
int n, m;
void floyd_warshall() {
for (int i = 1; i <= n; i++) {
for (int j = 1; j <= n; j++) {
if (i == j) dis[i][j] = 0;
else if (g[i][j] == 0) dis[i][j]
= inf:
else dis[i][j] = g[i][j];
for (int k = 1; k <= n; ++k) {
for (int i = 1; i <= n; ++i) {
for (int j = 1; j <= n; ++j) {
if (dis[i][k] < inf and</pre>
dis[k][j] < inf)
dis[i][j] = min(dis[i][j],
dis[i][k] + dis[k][j]);
}}}
Krushkal's MST:
const int N = 3e5 + 9, mod =
1e9:
struct dsu {
vector<int> par, rnk, size; int
C;
dsu(int n) : par(n+1),
rnk(n+1,0), size(n+1,1), c(n) {
for (int i = 1; i <= n; ++i)
par[i] = i:
int find(int i) { return (par[i]
== i ? i : (par[i] =
find(par[i]))); }
bool same(int i, int j) { return
find(i) == find(j); }
```

```
int get size(int i) { return
size[find(i)]; }
int count() { return c; }
//connected components
int merge(int i, int j) {
if ((i = find(i)) == (j =
find(j))) return -1; else --c;
if (rnk[i] > rnk[j]) swap(i, j);
par[i] = j; size[j] += size[i];
if (rnk[i] == rnk[j]) rnk[j]++;
return j;
};
int32 t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int n, m; cin >> n >> m;
vector<array<int, 3>> ed;
for(int i = 1; i <= m; i++){
int u. v. w: cin >> u >> v >> w:
ed.push_back({w, u , v});
sort(ed.begin(), ed.end());
long long ans = 0;
dsu d(n);
for (auto e: ed){
int u = e[1], v = e[2], w =
e[0]:
if (d.same(u, v)) continue;
ans += w:
d.merge(u, v);
cout << ans << '\n';
return 0:
Tree Diameter: max
cost(distance) between 2 nodes.
Dfs from any node and get 1 of
the 2 nodes. Then dfs again from
this node and get another 1.
From every node, 1 of these two
nodes is the max cost.
Faisal Amin Abir
**Bellman Ford with negative
cvcle**
Il INF = 1e16+7; int n; int m;
```

```
struct edge{ ll a, b, cost;};
ll d[5005]; edge e[5005];
ll p[5005];
void solve(int v){
ll x=-1; d[v]=0;
for(int i=0; <n; i++){</pre>
x=-1:
for(ll j=0; j<m; j++)</pre>
if(d[e[j].a] < INF)
if(d[e[j]].b > d[e[j].a] +
e[j].cost){
d[e[j].b] = \max(-INF,d[e[j].a] +
e[j].cost);
p[e[j].b] = e[j].a; x = e[j].b;
if(x==-1) cout << "NO" << endl;
else{
ll y = x;
for(ll i = 0; i<n; i++) y =
p[v];
vector<ll>path:
for(ll curr=v;;curr=p[curr]){
path.push_back(curr);
if(curr==y && path.size()>1){
break;
reverse(path.begin(),
path.end());
cout << "YES" << endl:
for(auto u:path) cout << u << "</pre>
return ;
int main(){
cin>>n>>m:
for(int i=0; i<m; i++){</pre>
edge ee; cin>> ee[i].a;
cin>>ee[i].b>>ee[i].cost;
solve(1); return 0;
** FLOYD Warshall**
void Floyd_Warshall(){
for(int i=0; i<=n; i++){</pre>
for(int j=0; j<=n; j++){</pre>
dis[i][j] = 100000000;}
```

```
dis[i][i]=0;}
for(int k=1; k<=n; k++){</pre>
for(int i=1; i<=n; i++){</pre>
for(int j=1; j<=n; j++){</pre>
dis[i][j] = min(dis[i][j],
dis[i][k] + dis[k][j]);}}}}
**Lexicographically minimum
topological sort**
vector<int> vi[maxii];
vector<int>:: iterator child;
int check[maxii];
int in[maxii];
int n.m;
int cycle =0;
void dfs(int node){
if(cvcle){
return:
check[node]=1;
for(auto child: vi[node]){
if(check[child]==0){
dfs(child);
else if(check[child]==1){
cycle=1;return ;
}}check[node]=2;
int main(){
int test=1;
for(int xx=1; xx<=test; xx++){</pre>
cin>>n>>m;
int a,b;
for(int i=1; i<=m; i++){</pre>
cin>>a>>b:
vi[a].push_back(b);
in[b]++;
for(int i=1; i<=n; i++){</pre>
if(check[i]==0){
dfs(i);
}}
if(cycle){
cout<<-1;
return 0:}
priority queue<pair<int,int>,vec
pair<int,int>>,greater<pair<int,</pre>
int> > > que;
for(int i=1; i<=n; i++){</pre>
if(in[i]==0){
```

```
que.push({i,0});
}}
while(!que.empty()){
int node=que.top().first;
int das=que.top().second;
que.pop();
if(das==0){
cout<<node<<" ";
for(int child:vi[node])
in[child]--;
que.push({child,in[child]});
}}}}
** HLD to find max between u and
v, with euler path, LCA and
segtree **
// dfs for subtree cal, dfs2 for
euler
const int N = 1e4+1;;
const int K = __lg(N) + 2;
int LOG[N], parent[N], value[N],
level[N], subtree[N], first[N],
chain[N], in[N], out[N],
lca[N][K], head[N], t[4*N], n;
vector<pair<int, int>>g[N];
vector<int>euler;
void dfs(int v, int par, int
val){
parent[v]=par;
value[v]=val;
lca[v][0] = par;
int sub = 1;
for(auto u:g[v]){
if(u.ff==par)continue;
level[u.ff] = level[v] + 1;
dfs(u.ff, v, u.ss);
sub += subtree[u.ff];
subtree[v]=sub;
void dfs2(int v, int par, int
time, int matha){
euler.pb(v);
head[v] = matha:
int sub=0. node=0:
in[v] = time;
for(auto u:g[v]){
if(u.ff==par) continue;
if(subtree[u.ff]>sub){
sub = subtree[u.ff];
```

```
node = u.ff;
}}
if(sub!=0){
dfs2(node, v, time+1, matha);
time = out[node];}
for(auto u:g[v]){
if(u.ff == par or u.ff == node)
continue:
dfs2(u.ff, v, time+1, u.ff);
time=out[u.ff];
out[v] = time;
void build(int v, int l, int r){
if(l==r){
t[v] = value[euler[l]];
return:
int mid = (l+r) >> 1;
build(2*v, l, mid);
build(2*v+1, mid+1, r);
t[v] = max(t[2*v], t[2*v+1]);
int max_query(int v, int L, int
R, int l, int r){
if(L>r or R<l) return 0;</pre>
if(L>=l and R<=r) return t[v];</pre>
int mid = (L+R) >> 1;
int left = max_query(2*v, L,
mid, l, r);
int right = max_query(2*v+1,
mid+1, R, l, r);
return max(left, right);
void update(int v, int l, int r,
int index, int value){
if(l==r){
t[v] = value;
return:
int mid = (l+r) >> 1;
if(index <= mid) update(2*v, l,</pre>
mid, index, value);
else update(2*v+1, mid+1, r,
index, value);
t[v] = max(t[2*v], t[2*v+1]);
void buildLCA(){
for(int i=1; i<K; i++){</pre>
for(int j=1; j<=n; j++){
```

```
int x = lca[j][i-1];
if(x != -1){
lca[j][i] = lca[x][i-1];
}}}}
int find_Lca(int a, int b){
if(level[a] < level[b]) swap(a,</pre>
int z = level[a] - level[b];
while(z>0){
int i = LOG[z];
a = lca[a][i];
z = (1 << i);
if(a==b) return a;
for(int i=K-1; i>=0; i--){
if(lca[a][i]!=-1 and
lca[a][i]!=lca[b][i]){
a = lca[a][i]:
b = lca[b][i];
return lca[a][0];
void init(){
for(int i=1; i<=n; i++) {
g[i].clear();
for(int j=0; j<K; j++){</pre>
lca[i][j]=-1;}}
euler.clear();
int find_max(int a, int root){
if(chain[a] == chain[root]){
return max_query(1, 0, n-1,
in[root], in[a]);
else{
int x = max_query(1, 0, n-1,
in[head[a]], in[a]);
x = max(x.
find_max(parent[head[a]],
root));
return x;
}}
void solve(){
cin>>n;
init();
vector<pair<int, int>>edge;
for(int i=1; i<n; i++){
int x,y, cost;
cin>>x>>y>>cost;
```

```
g[x].push_back({y, cost});
g[y].push_back({x, cost});
edge.pb({x, y});
dfs(1, -1, -1);
dfs2(1, -1, 0, 1);
int currChain=1;
for(int i=0; i<n; i++){</pre>
int x = euler[i];
chain[x] = currChain;
if(in[x]==out[x]) currChain++;
build(1, 0, n-1);
buildLCA();
while(1){
string s;
cin>>s:
if(s=="DONE")break;
if(s=="QUERY"){
int a, b;
cin>>a>>b;
int y = find_Lca(a, b);
update(1, 0, n-1, in[y], 0);
int ans = find_max(a, y);
ans = max(ans, find_max(b, y));
cout << ans << endl;</pre>
update(1,0, n-1, in[y],
value[y]);
else{
int index, val;
cin>>index>>val;
index--;
int a, b;
a = edge[index].ff;
b = edge[index].ss;
if(parent[a]==b) update(1, 0, n-
1, in[a], val), value[a]=val;
else{
update(1, 0, n-1, in[b], val);
value[b]=val:
}}}
int main(){
LOG[1] = 0;
for(int i=2; i<N; i++){</pre>
LOG[i] = LOG[i/2] + 1;
solve();
return 0;}
```

```
SSC find toposort, component
->given a forest, tell which
node to forward mail to reach
max people, lexicographically
smallest one:
const int N = 1e5+123;
vector<int>g1[N], g2[N], g3[N],
topo:
int totalCom, com[N], got,
countCom[N], minCom[N], dis[N],
indeg[N];
bool vis1[N], vis2[N], vis3[N];
int n. m:
void reset(){
for(int i=0; i<=n; i++){</pre>
g1[i].clear();
g2[i].clear();
g3[i].clear();
indeg[i]=dis[i]=countCom[i]=com[
i]=vis1[i]=vis2[i]=vis3[i]=0;
minCom[i]=INT_MAX;
totalCom=0:
topo.clear();
got=0;
void dfs1(int v){
if(vis1[v])return;
vis1[v]=1;
for(auto u:g1[v]){
dfs1(u);
topo.pb(v);
void dfs2(int v){
if(vis2[v])return;
vis2[v]=1:
com[v]=totalCom;
countCom[totalCom]++;
minCom[totalCom] =
min(minCom[totalCom], v);
for(auto u:g2[v]){
dfs2(u);
void solve(){
cin>>n;
reset();
vector<pair<int, int>>v;
```

```
for(int i=0; i<n; i++){</pre>
int x, y;
cin>>x>>y;
g1[x].pb(y);
g2[y].pb(x);
v.pb({x, y});
for(int i=1; i<=n; i++){</pre>
if(vis1[i]==0)
dfs1(i);
reverse(all(topo));
for(auto u:topo){
if(vis2[u]==0){
totalCom++:
dfs2(u);
for(auto u:v){
int f = com[u.ff];
int t = com[u.ss]:
if(f!=t){ // from B to A, we
find the node in reverse
direction to get highest count
g3[t].pb(f);
indeg[f]++;
using pii = pair<int, int>;
priority_queue<pii, vector<pii>,
greater<pii>>q:
for(int i=1; i<=totalCom; i++){</pre>
if(indeg[i]==0){
q.push({countCom[i], i});
dis[i]=countCom[i];
while(!q.empty()){
int from = q.top().ss;
q.pop();
for(auto u:g3[from]){
if(dis[u]<dis[from]+countCom[u])</pre>
dis[u] = dis[from] +
countCom[u];
q.push({dis[u], u});
int tot=0;
```

```
int ans=INT MAX;
for(int i=1; i<=totalCom; i++){</pre>
if(dis[i]>tot){
tot = dis[i]:
ans = minCom[i];}
else if(tot == dis[i]){
ans = min(ans, minCom[i]);}
cout << "Case " << ++test << ":
" << ans << endl;
SSC to find component of
component
const int N = 1e5+123;
vector<int>g1[N], g2[N], g3[N],
topo, topoCom;
int com[N], totalCom;
bool vis1[N], vis2[N], vis3[N],
vis4[N]:
void dfs1(int v){// find the
toposort of the given graph
if(vis1[v])return;
vis1[v]=1;
for(auto u:g1[v]){
dfs1(u);}
topo.pb(v);
void dfs2(int v){ // find the
scc from the toposort using the
transpose of given graph
if(vis2[v])return:
vis2[v]=1:
com[v]=totalCom;
for(auto u:g2[v]){
dfs2(u);}
void dfs3(int v){ // find the
toposort of the component graph
if(vis3[v])return;
vis3[v]=1;
for(auto u:g3[v]){
dfs3(u);}
topoCom.pb(v);
void dfs4(int v){// runs by the
toposort of the component graph
if(vis4[v])return;
vis4[v]=1:
for(auto u:g3[v]){
dfs4(u);}
```

```
void solve(){
int n.m:
cin>>n>>m;
vector<pair<int, int>>v;
for(int i=0; i<m; i++){</pre>
int x, y;
cin>>x>>y;
g1[x].pb(y);
g2[y].pb(x);
v.pb({x, y});
for(int i=1; i<=n; i++){
if(vis1[i]==0){
dfs1(i);}
reverse(all(topo));
for(auto u:topo){
if(vis2[u]==0){
totalCom++;
dfs2(u);}
for(auto u:v){
int from = com[u.ff];
int to = com[u.ss];
if(from!=to){
g3[to].pb(from);}
for(int i=1; i<=totalCom; i++){</pre>
if(vis3[i]==0){
dfs3(i);}
reverse(all(topoCom));
int start = topoCom[0];
dfs4(start);
for(int i=1; i<=totalCom; i++){</pre>
if(vis4[i]==0){
cout << 0 << endl;</pre>
return;}
vector<int>nodes;
for(int i=1; i<=n; i++){</pre>
if(com[i]==start){
nodes.pb(i);}
cout << nodes.size() << endl;</pre>
for(auto u:nodes)cout<<u<<" ";</pre>
cout << endl;</pre>
Kruskals
```

```
#define MX 100005
int parent[MX], R[MX];
struct kruskalStruct{
int u,v,w;
};
static bool cmp(kruskalStruct
&a, kruskalStruct &b){
return a.w < b.w;</pre>
void init(int v){
for(int i = 0; i <= v; i++){}
parent[i] = i;
R[i] = 1;
int Find(int p){
if(p == parent[p]) return p;
return parent[p] =
Find(parent[p]);
bool Union(int u,int v){
int p = Find(u);
int q = Find(v);
if(p != q) {
if(R[p] >= R[q]){
parent[q] = p;
R[p] += R[q];
else{
parent[p] = q;
R[q] += R[p];
return true:
return false;
vector<kruskalStruct> store;
void kruskalsMST(){
int vertex.edge;
cin >> vertex >> edge;
init(vertex);
for(int i = 0; i < edge; i++) {</pre>
int u,v,w;
cin >> u >> v >> w;
kruskalStruct ks;
ks.u = u;
ks.v = v;
ks.w = w:
store.push_back(ks);
```

```
sort(store.begin(),store.end(),c
mp);
int totalWeight = 0;
for(int i = 0; i < store.size();
i++){
  if(Union(store[i].u,store[i].v))
  totalWeight += store[i].w;
}
cout << "Kruskal's MST : " <<
  totalWeight << endl;
}
*** STRING</pre>
```

Faisal Amin Abir

String Multiply

```
string multiply(string num1.
string num2){
int len1 = num1.size();
int len2 = num2.size();
if (len1 == 0 || len2 ==
0)return "0";
vector<int> result(len1 + len2,
0);
int i_n1 = 0;
int i n2 = 0:
for (int i=len1-1; i>=0; i--){
int carry = 0;
int n1 = num1[i] - '0';
i n2 = 0:
for (int j=len2-1; j>=0; j--){
int n2 = num2[j] - '0';
int sum = n1*n2 + result[i_n1
+i_n2] + carry;
carrv = sum/10:
result[i n1 + i n2] = sum % 10;
i n2++;
if (carry > 0)result[i_n1 +
i_n2]+= carry;
i n1++;
int i = result.size() - 1;
while (i>=0 && result[i] == 0)i-
if (i == -1)return "0";
string s = "";
```

```
while (i >= 0)s
+=std::to_string(result[i--]);
return s;}
**String division**
string longDivision(string
number, int divisor){
string ans;
int idx = 0;
int temp = number[idx] - '0';
while (temp < divisor)</pre>
temp = temp * 10 +
(number[++idx] -'0');
while (number.size() > idx){
ans += (temp / divisor) + '0';
temp = (temp \% divisor) * 10 +
number[++idx] - '0';
if (ans.length() == 0)return
"0":
return ans:
```

String Double Hashing

```
const int MAXN=1000006;
namespace DoubleHash{
long long P[2][MAXN];
long long H[2][MAXN];
long long R[2][MAXN];
long long base[2];
long long mod[2];
void gen(){
base[0] = 1949313259ll:
base[1] = 1997293877ll:
mod[0] = 209157322711:
mod[1] = 2117566807ll;
for(int j=0;j<2;j++){</pre>
for(int i=0;i<MAXN;i++){</pre>
H[j][i]=R[j][i] = 011:
P[j][i] = 1ll;
for(int j=0;j<2;j++){
for(int i=1;i<MAXN;i++){</pre>
P[j][i] = (P[j][i-1] *
base[j])%mod[j];
}
```

```
void make_hash(string arr){
int len = arr.size();
for(int j=0;j<2;j++){
for (int i = 1; i <= len;</pre>
i++)H[j][i] = (H[j][i-1] *
base[j] + arr[i - 1] + 1007) %
mod[j];
//
              for (int i = len;
i >= 1; i--)R[j][i] = (R[j][i +
1] * base[j] + arr[i - 1] +
1007) % mod[j];
inline long long range_hash(int
l,int r,int idx){
long long hashval = H[idx][r +
1] - ((long long)P[idx][r - l +
1] * H[idx][l] % mod[idx]);
return (hashval < 0 ? hashval +
mod[idx] : hashval):
inline long long
reverse_hash(int l,int r,int
idx){
long long hashval = R[idx][l +
1] - ((long long)P[idx][r - l +
1] * R[idx][r + 2] \% mod[idx];
return (hashval < 0 ? hashval +
mod[idx] : hashval);
inline long long range_dhash(int
l.int r){
long long x = range_hash(l,r,0);
(x<<32)^range_hash(l,r,1);
inline long long
reverse_dhash(int l,int r){
long long x =
reverse hash(l,r,0);
return
(x<<32)reverse hash(l,r,1);
char str1[MAXN];
using namespace DoubleHash;
```

Reverse Hashing to Find longest palindromic substring*

```
int f1(int index){
if(index == 0 or index==n-1)
return 1;
int ans = 1;
int l = 1, r = min(index, n-1-
index);
while( l <= r){
int mid = (l+r) >> 1;
ll h1 = range_hash(index+1,
index + mid);
ll h2 =
reverse_range_hash(index-mid,
index-1);
if(h1==h2){
ans = 1 + (2 * mid);
l = mid+1;
else r = mid-1;
return ans;
int f2(int index){
if(index==0 or index==n-2)
return 2;
int ans=2;
int l = 1, r = min(index+1, n-1-
index);
while( l <= r){
int mid = (l+r) >> 1;
ll h1 = range_hash(index-mid+1,
ll h2 = reverse_range_hash(index
+ 1, index+mid);
if(h1==h2){
ans = 2 * mid;
l = mid+1:
else r = mid-1;
return ans;
void solve(){
cin>>s;
n = s.size();
ll ans=1;
ll l = 0, r=0;
for(int i=0; i<n; i++){</pre>
ll x = f1(i);//for odd length i
is mid elem
if(x > ans){
```

```
ans = x;
l = i - (x/2);
r = i + (x/2);
if(i + 1 < n \text{ and } s[i] ==
s[i+1]){
ll y = f2(i);// for even length
if( y > ans){
ans = y;
l = i - (y/2) + 1;
r = i + (y/2);
}}}
for(int i=l ; i<=r ; i++)</pre>
cout<<s[i];</pre>
**Manacher to Find the Longest
Palindromic Substring**
void solve(){
string s;
cin>>s;
string temp = "";
temp.pb('#');
for(auto u:s){
temp.pb(u);
temp.pb('#');
int n = temp.length();
int l=0, r=-1;
int pi[n]={0};
for(int i=0; i<n; i++){</pre>
int k=0:
if(i > r){
k = 0;
}
else{
k = min(r-i, pi[l + r - i]);
while( i + k + 1 < n && i - k -
1 >= 0 \& temp[i + k + 1] ==
temp[i - k - 1])
k++;
}pi[i]=k;
if(i+k>r){
r = i + k;
l = i - k;
int even=0, odd=0, index=0,
index2=0, ans=0;
```

```
for(int i=0; i<n; i++){</pre>
if(i%2==1){
index++;
if(pi[i]>ans){
ans = pi[i];
if(i%2){
odd=1:
even=0:
index2 = index;
else{
even=1;
odd=0:
index2=index;
}}}
index2--;
if(odd){
int l = index2, r = index2;
int k = 1;
while(k<ans){</pre>
l--, r++;
k+=2;
}for(int i=l; i<=r;</pre>
i++)cout<<s[i];
else {
int l = index2, r = index2+1;int
k = 2;
while( k < ans){</pre>
l--, r++;
k+=2;
}for(int i=l; i<=r;</pre>
i++)cout<<s[i];
->Given a string with m <= 2e5
operations:
a. Change the char at index to x
b. find if substring between
given l, r is palindrome?
const int N = 2e5+12;
ll t[4*N], reverse_t[4*N],
power[N], inv[N];
string s:
int n. q:
void build(int v, int l, int r){
if(l==r){
t[v] = (power[l] * (s[l]-'a'+1))
% MOD;
```

```
reverse_t[v] = (power[n-1-l] *
(s[1]-'a'+1)) % MOD;
return;
}
int mid = (l+r) >> 1;
build(2*v, l, mid);
build(2*v+1, mid+1, r);
t[v] = (t[2*v] + t[2*v+1]) %
reverse_t[v] = (reverse_t[2*v] +
reverse_t[2*v+1]) % MOD;
void update(int v, int l, int r,
int index, char ch){
if(l==r){
s[l]=ch:
t[v] = (power[l] * (s[l]-'a'+1))
% MOD;
reverse_t[v] = (power[n-1-l] *
(s[1]-'a'+1)) % MOD;
return;
int mid = (l+r) >> 1;
if(index <= mid) update(2*v, l,</pre>
mid, index, ch);
else update(2*v+1, mid+1, r,
index, ch);
t[v] = (t[2*v] + t[2*v+1]) %
reverse_t[v] = (reverse_t[2*v] +
reverse_t[2*v+1]) % MOD;
pair<ll, ll> query(int v, int L,
int R, int l, int r){
if(L>r or R<l ) return {0, 0};
if(L>=l and R<=r) return {t[v],</pre>
reverse_t[v]};
int mid = (L+R) >> 1;
pair<ll, ll>p1 = query(2*v, L,
mid. l. r);
pair<ll, ll>p2 = query(2*v+1,
mid+1, R, l, r);
return {(p1.ff + p2.ff) %
MOD, (p1.ss + p2.ss) % MOD;
void solve(){
cin>>n>>q;
cin>>s;
power[0]=1;
```

```
power[1]=base;
inv[0]=1;
inv[1]=modPow(base, MOD-2);
for(int i=2; i<n; i++){
power[i] = (1LL * power[i-1] *
base) % MOD;
inv[i] = ( 1LL * inv[i-1] *
inv[1]) % MOD;
build(1, 0, n-1);
while(q--){
int x;
cin>>x;
if(x==1){
int index; char ch;
cin>>index >> ch;
update(1, 0, n-1, index-1, ch);
else{
int l, r;
cin>>l>>r;
l--, r--;
pair<ll, ll> p = query(1, 0, n-
1, l, r);
ll h1 = (inv[l] * p.ff) % MOD;
ll h2 = (inv[n-1-r] * p.ss) %
MOD;
if(h1==h2){
cout << "YES" << endl;</pre>
else cout << "NO" << endl;</pre>
}}}
```

FAYSAL AHAMMED

Hashing:

* Double Hashing with Reverse:

```
const int MOD1 = 127657753, MOD2
= 987654319;
const int p1 = 137, p2 = 277; //
change here
int ip1, ip2;
pair<int, int> pw[N], ipw[N];
void prec() {
pw[0] = \{1, 1\};
for (int i = 1; i < N; i++) {</pre>
```

```
pw[i].first = 1ll * pw[i -
1].first * p1 % MOD1;
pw[i].second = 1ll * pw[i -
1].second * p2 % MOD2;
ip1 = power(p1, MOD1 - 2, MOD1);
ip2 = power(p2, MOD2 - 2, MOD2);
ipw[0] = \{1, 1\};
for (int i = 1; i < N; i++) {
ipw[i].first = 1ll * ipw[i -
1].first * ip1 % MOD1;
ipw[i].second = 1ll * ipw[i -
1].second * ip2 % MOD2;
struct Hashing {
int n;
string s;
vector<pair<int, int>> hash_val;
vector<pair<int, int>>
rev_hash_val;
Hashing() {}
Hashing(string _s) {
s = _s;
n = s.size();
hash_val.emplace_back(0, 0);
for (int i = 0; i < n; i++) {
pair<int, int> p;
p.first = (hash_val[i].first +
1ll * s[i] * pw[i].first % MOD1)
% MOD1;
p.second = (hash_val[i].second +
1ll * s[i] * pw[i].second %
MOD2) % MOD2;
hash_val.push_back(p);
rev_hash_val.emplace_back(0, 0);
for (int i = 0, j = n - 1; i < 1
n; i++, j--) {
```

```
pair<int, int> p:
p.first = (rev_hash_val[i].first
+ 1ll * s[i] * pw[j].first %
MOD1) % MOD1;
p.second =
(rev_hash_val[i].second + 1ll *
s[i] * pw[j].second % MOD2) %
MOD2:
rev_hash_val.push_back(p);
pair<int, int> get_hash(int l,
int r) { // 1 indexed
pair<int, int> ans;
ans.first = (hash_val[r].first -
hash_val[l - 1].first + MOD1) *
1ll * ipw[l - 1].first % MOD1;
ans.second = (hash_val[r].second
- hash val[l - 1].second + MOD2)
* 1ll * ipw[l - 1].second %
MOD2;
return ans;
pair<int, int> rev_hash(int l,
int r) { // 1 indexed
pair<int, int> ans;
ans.first =
(rev_hash_val[r].first -
rev_hash_val[l - 1].first +
MOD1) * 1ll * ipw[n - r].first %
MOD1;
ans.second =
(rev_hash_val[r].second -
rev_hash_val[l - 1].second +
MOD2) * 1ll * ipw[n - r].second
% MOD2;
return ans;
}
```

```
pair<int, int> get_hash() { // 1
indexed
return get hash(1, n);
bool is_palindrome(int l, int r)
return get_hash(l, r) ==
rev_hash(l, r);
};
Hashing with Updates and
Reverse:
using T = array<int, 2>;
const T MOD = \{127657753,
987654319}:
const T p = {137, 277}; //
change here
T operator + (T a, int x)
{return \{(a[0] + x) \% MOD[0],
(a[1] + x) % MOD[1];
T operator - (T a, int x)
{return \{(a[0] - x + MOD[0]) \%
MOD[0], (a[1] - x + MOD[1]) %
MOD[1]};}
T operator * (T a, int x)
{return {(int)((long long) a[0]
* x % MOD[0]), (int)((long long)
a[1] * x % MOD[1]);;
T operator + (T a, T x) {return
\{(a[0] + x[0]) \% MOD[0], (a[1] +
x[1]) % MOD[1]};}
T operator - (T a, T x) {return
\{(a[0] - x[0] + MOD[0]) \%
MOD[0], (a[1] - x[1] + MOD[1]) %
MOD[1]};}
T operator * (T a, T x) {return
\{(int)((long long) a[0] * x[0] %
```

```
MOD[0]), (int)((long long) a[1]
* x[1] % MOD[1])};}
ostream& operator << (ostream&
os, T hash) {return os << "(" <<
hash[0] << ", " << hash[1] <<
")";}
T pw[N], ipw[N];
void prec() {
pw[0] = \{1, 1\};
for (int i = 1; i < N; i++) {
pw[i] = pw[i - 1] * p;
ipw[0] = \{1, 1\};
T ip = \{power(p[0], MOD[0] - 2,
MOD[0]), power(p[1], MOD[1] - 2,
MOD[1])};
for (int i = 1; i < N; i++) {
ipw[i] = ipw[i - 1] * ip;
struct Hashing {
int n;
string s; // 1 - indexed
vector<array<T, 2>> t; //
(normal, rev) hash
array<T, 2> merge(array<T, 2> 1,
array<T, 2> r) {
l[0] = l[0] + r[0];
l[1] = l[1] + r[1];
return l;
void build(int node, int b, int
e) {
if (b == e) {
t[node][0] = pw[b] * s[b];
t[node][1] = pw[n - b + 1] *
s[b];
return;
}
```

```
int mid = (b + e) >> 1, l = node
<< 1, r = l | 1;
build(l, b, mid);
build(r, mid + 1, e);
t[node] = merge(t[l], t[r]);
void upd(int node, int b, int e,
int i, char x) {
if (b > i || e < i) return;</pre>
if (b == e && b == i) {
t[node][0] = pw[b] * x;
t[node][1] = pw[n - b + 1] * x;
return;
int mid = (b + e) >> 1, l = node
<< 1, r = l | 1;
upd(l, b, mid, i, x);
upd(r, mid + 1, e, i, x);
t[node] = merge(t[l], t[r]);
array<T, 2> query(int node, int
b, int e, int i, int j) {
if (b > j || e < i) return
\{T(\{0, 0\}), T(\{0, 0\})\};
if (b >= i && e <= j) return
t[node];
int mid = (b + e) \gg 1, l = node
<< 1, r = l | 1;
return merge(query(l, b, mid, i,
j), query(r, mid + 1, e, i, j));
Hashing() {}
Hashing(string _s) {
n = _s.size();
s = "." + _s;
t.resize(4 * n + 1);
build(1, 1, n);
}
void upd(int i, char c) {
```

```
upd(1, 1, n, i, c);
s[i] = c;
T get_hash(int l, int r) { // 1
indexed
return query(1, 1, n, l, r)[0] *
ipw[l - 1];
T rev_hash(int l, int r) { // 1
indexed
return query(1, 1, n, l, r)[1] *
ipw[n - r];
T get_hash() {
return get_hash(1, n);
bool is_palindrome(int l, int r)
return get_hash(l, r) ==
rev_hash(l, r);
}
};
Longest Common Prefix:
Binary Search over len and get
true/false by hashing in 0(1).
Lexicographically Min Cyclic
Shift:
// return 0 if both equal
// return 1 if first substring
greater
// return -1 if second substring
int compare(int i, int j, int x,
int y) {
int common_prefix = lcp(i, j, x,
y);
int len1 = j - i + 1, len2 = y - i
x + 1;
```

```
if (common prefix == len1 and
len1 == len2) return 0:
else if (common prefix == len1)
return -1;
else if (common_prefix == len2)
return 1;
else return (s[i + common_prefix
-1] < s[x + common_prefix -1]
? -1 : 1);
int start = 1, end = k;
for (int i = 1; i + k - 1 <= n;
i++) {
int x = compare(start, end, i, i
+ k - 1);
if (x == 1) {
start = i, end = i + k - 1;
cout << s.substr(start - 1, k)</pre>
<< '\n';
Cyclic Shift trick: s += s
Number of Palindromic Substring
between 1 to r in O(n^2):
int is_palindrome(int i, int j)
{ // 0(n^2)}
if (i > j) return 1;
int &ans = dp2[i][j];
if (ans != -1) return ans;
ans = 1;
if (s[i] == s[j]) {
ans &= is_palindrome(i + 1, j -
1);
else {
ans = 0;
return ans;
```

```
}
int fun(int i, int j) { //
0(n^2)
if (i > j) return 0;
int &ans = dp[i][j];
if (ans != -1) return ans;
ans = is_palindrome(i, j) +
fun(i + 1, j) + fun(i, j - 1) -
fun(i + 1, j - 1);
return ans;
Number of Palindromic Substrings
of a String in O(n logn):
string s;
Hashing hash_s;
int n;
bool ok(int l, int r) {
return hash s.is palindrome(l.
r);
}
int32_t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
prec(); // must include
cin >> s;
n = s.size();
hash_s = Hashing(s);
long long ans = 0;
for (int i = 1; i <= n; i++) {
int l = 0, r = min(n - i, i - i)
1), cnt = 1;
while (1 <= r) {
int mid = (l + r) \gg 1;
if (ok(i - mid, i + mid)) {
```

```
cnt = mid;
l = mid + 1:
else {
r = mid - 1;
ans += cnt + 1;
for (int i = 2; i <= n; i++) {
if (s[i - 1] == s[i - 2]) {
int l = 0, r = min(n - i, i -
1), cnt = 2;
while (l <= r) {
int mid = (l + r) \gg 1;
if (ok(i - 1 - mid, i + mid)) {
cnt = mid;
l = mid + 1;
else {
r = mid - 1;
ans += cnt + 1;
cout << ans << '\n';
return 0:
}
** DYNAMIC PROGRAMMING
FAYSAL AHAMMED
Knapsack-2 (constraints- n <=</pre>
100, w <= 10<sup>9</sup>, value <= 1000):
int max_val = 0;
for (int i = n + 1; i >= 1; i--)
for (int current_value = 0;
current_value <= n * 1000;</pre>
current_value++) {
```

```
if (i == n + 1) {
if (current_value == 0)
dp[i][current_value] = 0;
else dp[i][current_value] = inf;
else {
ll &ans = dp[i][current_value];
ans = dp[i + 1][current_value];
if (current_value - value[i] >=
ans = min(ans, weight[i] + dp[i
+ 1][current_value - value[i]]);
if (ans <= w) {
max_val = max(max_val,
current_value);
}}}}
cout << max_val << '\n';
LCS:
int fun(int i, int j) {
if (i >= n or j >= m) return 0;
int &ans = dp[i][j];
if (ans != -1) return ans;
ans = fun(i + 1, j);
ans = max(ans, fun(i, j + 1));
if (s1[i] == s2[j]) {
ans = max(ans, 1 + fun(i + 1, j)
+ 1));
return ans;
void print(int i, int j) {
if (i >= n or j >= m) return;
if (s1[i] == s2[j]) {
cout << s1[i];
path(i + 1, j + 1);
return;
int ans1 = fun(i + 1, j);
int ans2 = fun(i, j + 1);
if (ans1 > ans2) {
path(i + 1, j);
else {
path(i, j + 1);
LIS:
st.build(1, 1, M);
for (int i = 1; i <= n; i++) {
```

```
dp[i] = 1;
if (a[i] != 1) {
int mx = st.query(1, 1, M, 1,
a[i] - 1);
mx++;
dp[i] = max(dp[i], mx);
st.upd(1, 1, M, a[i], dp[i]);
int ans = 0;
for (int i = 1; i <= n; i++) {
ans = max(ans, dp[i]);
cout << ans << '\n';
Edit Distance (make two string
same by add, remove, replace any
index with min cost):
int fun(int i, int j) {
if (i == n) {
if (j == m) return 0;
return m - j;
if (j == m) return n - i;
int &ans = dp[i][j];
if (ans != -1) return ans;
ans = inf;
if (s1[i] == s2[j]) {
ans = min(ans, fun(i + 1, j +
1));
ans = min(ans, 1 + fun(i + 1, j)
ans = min(ans, 1 + fun(i + 1,
j));
ans = min(ans, 1 + fun(i, j +
1));
return ans;
Longest Palindromic Subsequence:
int fun(int i, int j) {
if (i > j) return 0;
if (i == j) return 1;
int &ans = dp[i][j];
if (ans != -1) return ans;
ans = 0;
if (s[i] == s[j]) {
ans = max(ans, 2 + fun(i + 1, j)
- 1));
```

```
else {
ans = \max(ans, fun(i + 1, j));
ans = max(ans, fun(i, j - 1));
return ans;
Coin Change:
Repetition allowed (or max k
times for k)
Repetition not allowed - fun(int
i, int current_amount)
Repetition fixed - loop inside
fun()
Order doesn't matter -
fun(amount) and loop inside
fun()
Project (start time, ending
time, profit are given, what's
the max profit?):
-Sort by endtime, then dp[i] =
max profit if i is the last
index taken. Like LIS. Code-
sort(a + 1, a + 1 + n);
st.build(1, 1, M);
for (int i = 1; i <= n; i++) {
dp[i] = a[i][2];
ll mx = st.query(1, 1, M, 1,
a[i][1] - 1);
mx += a[i][2];
dp[i] = max(dp[i], mx);
st.upd(1, 1, M, a[i][0], dp[i]);
ll\ ans = 0;
for (int i = 1; i <= n; i++) {
ans = max(ans, dp[i]);
cout << ans << '\n';
Slime (n numbers are given,
everytime merge 2 consecutive
element until there is just 1
element such that cost is min,
the cost of merge two element =
sum of them):
    Think reverse: we are given
the final sum, from i to j. Now
we will cut any point between i
to j and calculate the cost
ll fun(int i, int j) {
if (i == j) return 0;
```

```
ll &ans = dp[i][j];
if (ans != -1) return ans;
ll cur = 0:
for (int x = i; x <= j; x++) {
cur += a[x];
ans = inf;
for (int x = i; x < j; x++) {
ans = min(ans, cur + fun(i, x) +
fun(x + 1, j));
return ans;
Sub-Palindromic Tree (Given a
tree, each node has a character.
Now tell us the maximum path
which has longest palindromic
subsequence):
const int N = 2005, inf = 1e9;
vector<int> g[N];
int n;
string s;
int nxt[N][N];
vector<int> vec;
int dp[N][N];
void dfs(int u, int p) {
vec.push_back(u);
for (auto v: g[u]) {
if (v != p) {
dfs(v, u);
}}}
int fun(int u, int v) {
if (v == u) return 1;
int &ans = dp[u][v];
if (ans != -1) return ans;
ans = 0:
if (s[u] == s[v]) {
ans = 2 + (nxt[u][v] == v ? 0 :
fun(nxt[u][v], nxt[v][u]));}
else {
ans = max(fun(nxt[u][v], v),
fun(u, nxt[v][u]));
return ans;
void solve() {
cin >> n >> s;
s = '.' + s;
for (int i = 1; i < n; i++) {
```

```
int u, v; cin >> u >> v;
g[u].push_back(v);
g[v].push_back(u);
for (int u = 1; u <= n; u++) {
for (auto x : g[u]) {
vec.clear();
dfs(x, u);
for (auto v : vec) {
nxt[u][v] = x;
}}}
for (int u = 1; u <= n; u++) {
for (int v = 1; v <= n; v++) {
dp[u][v] = -1:
}}
int ans = 0:
for (int u = 1; u <= n; u++) {
for (int v = 1; v <= n; v++) {
ans = max(ans, fun(u, v));
cout << ans << '\n';
for (int i = 1; i <= n; i++) {
g[i].clear();
Dice-1 (choose N numbers from 1
to k, how many ways the sum of
them is S?) [N, K <= 1000, S <=
15000T:
for (int i = n + 1; i >= 1; i--)
for (int cur_sum = 0; cur_sum <=</pre>
s; cur_sum++) {
if (i == n + 1) {
dp[0][cur_sum] = (cur_sum == 0);
else {
int &ans = dp[0][cur_sum];
int mn = min(k, cur_sum);
ans = 0;
// for (int x = 1; x <= mn; x++)
    ans += dp[1][cur\_sum - x];
//
//
     ans %= mod;
// }
ans = (dp[1][cur\_sum - 1] -
(cur_sum - mn - 1 < 0 ? 0 :
dp[1][cur\_sum - mn - 1]) + mod)
% mod:
}}
```

```
for (int cur_sum = 0; cur_sum <=</pre>
s: cur sum++) {
dp[1][cur_sum] = dp[0][cur_sum];
for (int cur_sum = 1; i != 1 and
cur_sum <= s; cur_sum++) {</pre>
dp[1][cur\_sum] += dp[1][cur\_sum]
- 1];
dp[1][cur_sum] %= mod;
cout << dp[0][s] << '\n';
Dice-2 (choose N numbers from 1
to k, if sum of them = s, then
score = multiply of the n
numbers, sum of scores?) [N, K
<= 1000, S <= 15000]:
for (int i = n + 1; i >= 1; i--)
for (int cur_sum = 0; cur_sum <=</pre>
s; cur_sum++) {
if (i == n + 1) {
dp[0][cur_sum] = cur_sum == 0;
else {
int &ans = dp[0][cur_sum];
ans = 0;
int mn = min(k, cur_sum);
// for (int x = 1; x <= mn; x++)
// ans += 1ll * x *
dp[1][cur_sum - x] % mod;
// ans %= mod;
// }
int l = cur_sum - mn, r =
cur_sum - 1;
ans = (pref[l] - pref[r + 1] +
mod) % mod;
ans -= 111 * (s - r) *
((dp[1][r] - (l ? dp[1][l - 1] :
0) + mod) % mod) % mod;
ans += mod;
ans %= mod;
for (int cur_sum = 0; cur_sum <=</pre>
s; cur_sum++) {
dp[1][cur_sum] = dp[0][cur_sum];
pref[0] = dp[1][0];
for (int cur_sum = 1; i != 1 and
cur_sum <= s; cur_sum++) {</pre>
```

** MICELLANEOUS

```
FAYSAL AHAMMED
Ternary Search (Pyramid):
double suface_area;
double fun(double square area) {
double base = sqrt(square_area);
double triangle area =
suface_area - square_area;
double per_triangle_area =
triangle_area / 4;
double triangle_height =
(per_triangle_area * 2) / base;
double x = base / 2;
double height =
sqrt((triangle height *
triangle_height) - (x * x);
double volume = (base * base *
height) / 3;
if (x > triangle_height) volume
= 0:
return volume;
}
int cs = 0;
int32_t main() {
ios_base::sync_with_stdio(0);
cin.tie(0);
int t; cin >> t;
while (t--) {
cin >> suface area;
cout << fixed <<</pre>
setprecision(4);
```

```
double l = 0, r = suface_area,
ans = -1;
int it = 100:
while (it--) {
double mid1 = l + (r - l) / 3;
double mid2 = r - (r - 1) / 3;
double x = fun(mid1);
double y = fun(mid2);
if (x > y) {
ans = x;
r = mid2;
}
else {
l = mid1:
}}
cout << "Case " << ++cs << ": ";
cout << ans << '\n':
return 0;
2D Prefix Sum:
int n, m; cin >> n >> m;
for (int i = 1; i <= n; i++) {
for (int j = 1; j <= m; j++) {
cin >> a[i][j];
}}
for (int i = 1; i <= n; i++) {
for (int j = 1; j <= m; j++) {
prefix[i][j] = prefix[i - 1][j]
+ prefix[i][j - 1] - prefix[i -
1][j - 1] + a[i][j];
}}
int q; cin >> q;
while (q--) {
int x1, y1, x2, y2; cin >> x1 >>
y1 >> x2 >> y2;
cout << prefix[x2][y2] -</pre>
prefix[x1 - 1][v2] -
prefix[x2][y1 - 1] + prefix[x1 -
1][v1 - 1] << '\n';
2D Difference Array:
int n, m; cin >> n >> m;
for (int i = 1; i \le n; i++) {
for (int j = 1; j <= m; j++) {
char c; cin >> c;
a[i][j] = c - '0';
}}
int q; cin >> q;
```

```
while (q--) {
int x1, y1, x2, y2, x; cin >> x1
>> y1 >> x2 >> y2;
x = 1:
d[x1][y1] += x;
d[x1][y2 + 1] -= x;
d[x2 + 1][y1] -= x;
d[x2 + 1][y2 + 1] += x;
for (int i = 1; i <= n; i++) {
for (int j = 1; j <= m; j++) {
d[i][j] += d[i - 1][j] + d[i][j]
- 1] - d[i - 1][i - 1]:
}}
// new updated array
for (int i = 1; i <= n; i++) {
for (int j = 1; j <= m; j++) {
cout << (d[i][j] + a[i][j]) % 2;</pre>
cout << '\n';
PBDS:
#include<ext/pb_ds/assoc_contain</pre>
er.hpp>
#include<ext/pb_ds/tree_policy.h</pre>
pp>
using namespace __gnu_pbds;
template <typename T> using
o_set = tree<T, null_type,</pre>
less<T>, rb_tree_tag,
tree_order_statistics_node_updat
e>;
Custom Hash for GP HashTable:
const int RANDOM =
chrono::high_resolution_clock::n
ow().time_since_epoch().count();
struct chash {
int operator()(int x) const {
return x ^ RANDOM; }
};
Direction Array:
int dx[] = \{+0, +0, +1, -1, -1,
+1, -1, +1};
int dy[] = \{-1, +1, +0, +0, +1,
+1, -1, -1};
Custom Comparator:
```

```
bool cmp(pair<int, int> a,
pair<int, int> b) {
if (a.first != b.first) return
a.first > b.first;
return a.second < b.second; //</pre>
comparator function must return
false for equal elements
Custom Comparator for map, set,
multiset, pq:
struct cmp {
bool operator()(const int& a,
const int& b) const {
return a > b:
};
Mex with Array Updates:
int n, q; cin >> n >> q;
set<int> missing numbers:
for (int i = 0; i <= n + 200;
i++) {
missing_numbers.insert(i);
int a[n + 1];
map<int, int> freq;
for (int i = 1; i <= n; i++) {
cin >> a[i];
freq[a[i]]++;
missing_numbers.erase(a[i]);
while (q--) {
int i, x; cin >> i >> x;
int y = a[i];
a[i] = x;
missing_numbers.erase(x);
freq[v]--;
freq[x]++;
if (freq[v] == 0) {
freq.erase(y);
missing_numbers.insert(y);
cout << *missing_numbers.begin()</pre>
<< '\n';
Coordinate Compression (faster):
vector<int> a({100, 9, 10, 10,
9}):
vector<int> v = a;
```

```
sort(v.begin(), v.end());
v.resize(unique(v.begin(),
v.end()) - v.begin());
for (int i = 0; i < a.size();</pre>
i++) {
a[i] = lower_bound(v.begin(),
v.end(), a[i]) - v.begin() + 1;
cout << a[i] << ' ';
Pigeonhole Principle:
```

-At least 1 subarray of an array of length N must be divisible by

-Build all possible sequences of length 10 whose value is between 1 to 100. At least any two sequences will be same.

* Given an array of length N (N $<= 10^6$) and M (M $<= 10^3$) check if there is any subsequence of the array whose sum is divisible by k?

According to the pigeonhole principle if N >= M then it must be "YES". Else we can do DP. where N < M <= 1000.

Contribution Technique

(Calculate the contribution of each element separately):

* Sum of pair sums (i=1 to n Σ j=1 to $n \Sigma(ai+a)$:

=> Every element will be added 2n times.

$$\sum_{i=1}^{n} (2 \times n \times a_i) = 2 \times n \times \sum_{i=1}^{n} a_i$$
.

* Sum of subarray sums:

$$\sum_{i=1}^{n} (a_i \times i \times (n-i+1)).$$

* Sum of subset sums:

$$\sum_{i=1}^{n} \left(2^{n-1} \times a_i\right)$$
.

* Product of pair product:

$$\prod_{i=1}^n \left(a_i^{2 \times n}\right)$$
.

* XOR of subarray XORS: => How many subarrays does an element have? (i* (n-i+1) times. If subarray length is odd then this element can contribute in total XORs. * Sum of max-min over all subset: => Sort the array. Min = 2^(ni), $Max = 2^{(i-1)}$ i=1 to n $\Sigma(ai * 2^{(i-1)}) (ai*2^{n-i})$ * Sum using Bit: $\sum_{k=0}^{30} (cnt_k[1] \times 2^k)$. * Sum of Pair XORs: => XOR = 1 if two bits are different

$$\sum_{k=0}^{30} \left(cnt_k[0] \times cnt_k[1] \times 2^k \right)$$

* Sum of pair ANDs:

$$\sum_{k=0}^{30} (cnt_k[1]^2 \times 2^k).$$

* Sum of pair ORs:

$$\sum_{k=0}^{30} \left(\left(cnt_k[1]^2 + 2 imes cnt_k[1] imes cnt_k[0]
ight) imes 2^k
ight)$$

* Sum of Subset XORs:

$$\sum_{k=0}^{30} \left(2^{cnt_k[1] + cnt_k[0] - 1} \times 2^k \right).$$

[where cnt0 != 0)

* Sum of Subset ANDs:

$$\sum_{k=0}^{30} ((2^{cnt_k[1]}-1)\times 2^k).$$

* Sub of Subset ORs:

$$\sum_{k=0}^{30} ((2^n - 2^{cnt_k[0]}) \times 2^k).$$

* Sum of subarray XORs:

=> Convert to prefix xor, then solve for pairs.

Nafis and MEX:

```
void solve() {
int n, k; cin >> n >> k;
vector<int> a(n);
map<int, int> mp;
```

```
for (auto &x : a) {
cin >> x:
mp[x]++;
sort(a.begin(), a.end());
int max_mex = 0;
for (auto x : a) {
if (max_mex == x) max_mex++;
int ways[max_mex];
for (int i = 0; i < max_mex;</pre>
int mn = min(30ll, mp[i]);
ways[i] = (1 << mn) - 1;
for (int i = 1; i < max mex;
i++) {
int mn = (int)(1ll * ways[i] *
wavs[i - 1]):
ways[i] = min(MIN, mn);
int cur = max_mex;
int add = (k + 1) / 2;
int minus = k - add;
long long ans = 0;
while (minus > 0) {
int right = n -
(upper_bound(a.begin(), a.end(),
cur) - a.begin());
int mn = min(30ll, right);
int possible = (1 << mn);</pre>
if (cur == 0) {
possible--:
int apply = min(minus,
possible);
minus -= apply;
ans -= (111 * cur * apply);
else {
possible = min(MIN, (int) (111 *
ways[cur - 1] * possible));
int apply = min(minus,
possible);
minus -= apply;
ans -= (111 * cur * apply);
cur--;
cur = 0:
while (add > 0) {
```

```
int right = n -
 (upper_bound(a.begin(), a.end(),
 cur) - a.begin());
 int mn = min(30ll, right);
 int possible = (1 << mn);</pre>
 if (cur == 0) {
 possible--;
 int apply = min(add, possible);
 add -= apply;
 ans += (111 * cur * apply);
 else {
 possible = min(MIN, (int) (111 *
 ways[cur - 1] * possible));
 int apply = min(add, possible);
 add -= apply:
 ans += (111 * cur * apply);
 cur++;
 cout << ans << '\n':
 How many triplets such that
 ai*bj*ck=m:
 A raixbxcx=m (a,b,c 3h smo) or
 different thiplate ony,
  m sor horo or. This cost sid box 1
 solar wo every mob toby out on
  Joso Euramalino givien des eus plo
    C Ce montaine to anote to an Just a
 Formulas:
 Sum of squares: 1^2 + 2^2 + 3^2 + ... + n^2 =
 n(n+1)(n+2)/6
Sum of cubes: 1^3 + 2^3 + 3^3 + ... + n^3 = (n^2)
* (n+1)^2)/4
Geometric Series: 1+x+x^2+x^3...+x^n = (
x^{(n+1)-1}/(x-1)
when |x| < 1 then the sum = 1 / (1-x)
Harmonic Series: 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{n} =
\ln (n) + O(1)
\sum_{k=0} (a_k - a_{k+1}) = a_0 - a_n.
 \sum_{k=1} (a_k - a_{k-1}) = a_n - a_0 ,
```

AIUB_Ceiling0.3 Am

$$\sum_{k=1}^{n} \frac{1}{k \cdot (k+1)} = \sum_{k=1}^{n} \left(\frac{1}{k} - \frac{1}{k+1}\right) \\
= \sum_{k=1}^{n} \frac{1}{n} \cdot \left(\frac{1}{n} - \frac{1}{k+1}\right) \\
= \sum_{k=1}^{n} \frac{1}{n} \cdot \left(\frac{1}{n} - \frac{1}{n+1}\right) \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq 1 \\
= \sum_{k=0}^{n} c' = \frac{c^{n+1} - 1}{c - 1}, \quad c \neq$$

 $\sum_{i=0}^{n} i^{2} = \frac{n(n+1)(2n+1)}{6}$

$$\sum_{i=1}^{n} i^3 = \frac{n^2(n+1)^2}{4}$$
Geometric series:

$$\sum_{i=0}^{n} c^i = \frac{c^{n+1}-1}{c-1}, \quad c \neq 1$$

$$\sum_{i=0}^{\infty} c^i = \frac{1}{1-c},$$

$$\sum_{i=1}^{\infty} c^i = \frac{c}{1-c}, \quad |c| < 1,$$

$$\frac{\binom{n}{k}}{\binom{n}{k}} = \frac{n!}{(n-k)!k!},$$

$$\frac{\binom{n}{k}}{\binom{n}{k}} = \binom{n}{k}$$

$$\binom{n}{k} = \binom{n}{n-k}$$

$$\binom{n}{k} = \frac{n}{k} \binom{n-1}{k-1}$$

$$\binom{n}{m} \binom{m}{k} = \binom{n}{k} \binom{n-k}{m-k}$$

$$\sum_{k=0}^{n} \binom{n}{k} = \binom{n}{k} \binom{n-k}{m-k}$$

$$\sum_{k=0}^{n} \binom{k}{m} = \binom{n+1}{m+1}$$

$$\sum_{k=0}^{n} \binom{k}{m} \binom{n}{n-k} = \binom{r+n+1}{n},$$

$$\binom{n}{k} = (-1)^k \binom{k-n-1}{k}$$

$$\binom{n}{k} = (-1)^k \binom{k-n-1}{k}$$

$$\binom{n}{1} = \binom{n}{n} = 1,$$

$$\binom{n}{2} = 2^{n-1} - 1,$$

$$\binom{n}{n-1} = \binom{n}{n-1} = \binom{n}{2}$$

$$\sum_{k=0}^{n} \binom{n}{k} = n!,$$

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

 $\log_b x = \frac{\log_a x}{\log_a b}, \qquad \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

 $e = 1 + \frac{1}{2} + \frac{1}{6} + \frac{1}{24} + \frac{1}{120} + \cdots$ $\lim_{n \to \infty} \left(1 + \frac{x}{n} \right)^n = e^x.$

 $\left(1+\frac{1}{n}\right)^n < e < \left(1+\frac{1}{n}\right)^{n+1}$ $(1+\frac{1}{n})^n = e - \frac{e}{2n} + \frac{11e}{24n^2} - O\left(\frac{1}{n^3}\right).$

Euler's number e:

Pascal's Triangle	
1	
11	
$\begin{array}{c} 1\ 2\ 1 \\ 1\ 3\ 3\ 1 \end{array}$	
1 4 6 4 1	
1 5 10 10 5 1	
1 6 15 20 15 6 1	
1 7 21 35 35 21 7 1	
1 8 28 56 70 56 28 8	1
1 9 36 84 126 126 84 36	
1 10 45 120 210 252 210 120 Binomial distribution:	45 10 1
$\Pr[X=k] = \binom{n}{k} p^k q^{n-k}$	q = 1 - p,
$E[X] = \sum_{k=1}^{n} k \binom{n}{k} p^{k}$	$\dot{q}^{n-k} = np.$
Euler's equation:	
$e^{ix} = \cos x$	$+i\sin x$, $e^{i\pi} = -1$
c — cos 2	Area:
	11100.
	$A = \frac{1}{2}hc,$
	$= \frac{1}{2}ab\sin C,$
	$=\frac{c^2\sin A\sin B}{2\sin C}.$
	Heron's formula:
C	
\wedge	$A = \sqrt{s \cdot s_a \cdot s_b \cdot s_c},$
b/ a	$s = \frac{1}{2}(a+b+c),$
	$s_a = s - a,$
$A \stackrel{\text{h}}{c} B$	$s_b = s - b,$
Law of cosines:	
$c^2 = a^2 + b^2 - 2ab\cos C.$	$s_c = s - c$.
$\sin\frac{x}{2} = \sqrt{\frac{1 - \cos x}{2}},$	
$\cos\frac{x}{2} = \sqrt{\frac{1 + \cos x}{2}},$	
$\tan\frac{x}{2} = \sqrt{\frac{1 - \cos x}{1 + \cos x}},$	
$\tan x = \sqrt{1 + \cos x}$	
$=\frac{1-\cos x}{\sin x}$	
$= \frac{1 - \cos x}{\sin x},$ $= \frac{\sin x}{1 + \cos x},$	
$=\frac{1+\cos x}{1+\cos x}$	
$\cot \frac{x}{2} = \sqrt{\frac{1 + \cos x}{1 - \cos x}},$	
$\bigvee_{1} 1 - \cos x$	
$=\frac{1+\cos x}{\sin x},$	
$\sin x$	
$=\frac{\sin x}{1-\cos x},$	

Euler's function: $\phi(x)$ is the number of positive integers less than x relatively prime to x. If $\prod_{i=1}^{n} p_i^{e_i}$ is the prime factorization of x then

$$\phi(x) = \prod_{i=1}^{n} p_i^{e_i - 1} (p_i - 1).$$

Euler's theorem: If a and b are relatively prime then

$$1 \equiv a^{\phi(b)} \bmod b.$$

Fermat's theorem:

$$1 \equiv a^{p-1} \bmod p.$$

The Euclidean algorithm: if a > b are integers then

$$gcd(a, b) = gcd(a \mod b, b).$$

If $\prod_{i=1}^{n} p_i^{e_i}$ is the prime factorization of x

$$S(x) = \sum_{d|x} d = \prod_{i=1}^{n} \frac{p_i^{e_i+1} - 1}{p_i - 1}$$

Perfect Numbers: x is an even perfect number iff $x = 2^{n-1}(2^n-1)$ and 2^n-1 is prime. Wilson's theorem: n is a prime iff

$$(n-1)! \equiv -1 \bmod n.$$



 $AB^2 = AC^2 + BC^2 + 2 \cdot BC \cdot CD$



 $AB^2 = AC^2 + BC^2 - 2 \cdot BC \cdot CD$



 $AB^2 + AC^2 = 2(AD^2 + BD^2)$

$$d^{2} = \frac{2(b^{2} + c^{2}) - a^{2}}{4}$$

$$e^{2} = \frac{2(c^{2} + a^{2}) - b^{2}}{4}$$

$$f^{2} = \frac{2(a^{2} + b^{2}) - c^{2}}{4}$$

$$f = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$\log_a M = \log_b M \times \log_a b$$

$$(x+y)^n = x^n + nx^{n-1}y + \frac{n(n-1)}{1 \cdot 2}x^{n-2}y^2 + \frac{n(n-1)(n-2)}{1 \cdot 2 \cdot 3}x^{n-3}y^3 + \dots + y^n$$

$$n! = n(n-1)(n-2)\cdots 3\cdot 2\cdot 1$$

$$\binom{n}{r} = {}^{n}C_{r}, {}^{n}C_{n} = 1$$

$$\binom{n}{r} = {}^{n}C_{r} = \frac{n!}{r!(n-r)!}, {}^{n}C_{0} = {}^{n}C_{0} = 1$$

$$\binom{n}{n} = {}^{n}C_{n} = 1, 0! = 1$$

$$\binom{n}{k} = \frac{n!}{(n-k)!k!},$$

$$\frac{n}{r}\binom{n}{r} = 2^{n}$$

$$\begin{split} \sum_{i=1}^{n} i &= \frac{n(n+1)}{2}, \\ \sum_{i=1}^{n} i^2 &= \frac{n(n+1)(2n+1)}{6} \\ \sum_{i=1}^{n} i^3 &= \frac{n^2(n+1)^2}{4} \end{split}$$

Triangle:

area =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

area =
$$\frac{1}{2}(x_1y_2 + x_2y_3 + x_3y_1 - x_2y_1 - x_3y_2 - x_1y_3)$$

Cube:

area = abc

$$diag = \sqrt{a^2 + b^2 + c^2}$$

Circle

 $2\pi r$

circumference:

area:
$$\pi r$$

eqn:
$$(x-h)^2 + (y-k)^2 = r^2$$
 ... (i)

$$(x-h)^2 + (y-k)^2 = r^2$$
 $\overline{1}$, $x^2 + y^2 - 2hx - 2ky + (h^2 + k^2 - r^2) = 0$
 $h^2 + k^2 - r^2 = c$

বা,
$$g^2 + f^2 - c = r^2$$

অতএব ব্যাসার্ধ,
$$r = \sqrt{g^2 + f^2 - c}$$
.

Cone:

$$\frac{1}{3}\pi r^2 h$$

volume:

$$\begin{array}{c}
D(6,8) & C(x,y) \\
\hline
D(5,9) & B(5,9) \\
D(7,2) & B(7,2)
\end{array}$$

$$\begin{array}{c}
D(6,8) & C(x,y) \\
D(7,2) & D(7,2) \\
D(7,2) & D($$

$$\therefore P(x_1, y_1)$$
 বিন্দু হতে $ax + by + c = 0$ রেখার শব্দ দৈর্ঘ্য = $\left| \frac{ax_1 + by_1 + c}{\sqrt{a^2 + b^2}} \right|$

 \therefore সমান্তরাল রেখা দুইটির মধ্যবর্তী দূরত্ব MN=ON-OM $=\left|\frac{c_1-c_2}{\sqrt{a^2+b^2}}\right|$

$$x^2 + y^2 = r^2$$
 এবং $y = mx + c$

tangent condition: $c = \pm r \sqrt{1 + m^2}$

বহিঃস্থ কোন বিন্দু (x_1,y_1) থেকে $x^2+y^2+2gx+2fy+c=0$ বৃত্তের অজ্ঞিত স্পর্শক দুইটির সমীকরণ

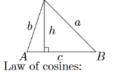
$$(x^2 + y^2 + 2gx + 2fy + c) (x_1^2 + y_1^2 + 2gx_1 + 2fy_1 + c)$$

$$= \{x x_1 + yy_1 + g (x + x_1) + f(y + y_1) + c\}^2$$
Area:

$$A = \frac{1}{2}hc,$$

$$= \frac{1}{2}ab\sin C,$$

$$= \frac{c^2\sin A\sin B}{2\sin C}.$$
C
Heron's formula:



$$A = \sqrt{s \cdot s_a \cdot s_b \cdot s_c},$$

$$s = \frac{1}{2}(a+b+c),$$

$$s_a = s-a,$$

$$s_b = s-b.$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$
. $s_c = s - c$.

Euler's function: $\phi(x)$ is the number of positive integers less than x relatively prime to x. If $\prod_{i=1}^n p_i^{e_i}$ is the prime factorization of x then

$$\phi(x) = \prod_{i=1}^{n} p_i^{e_i - 1} (p_i - 1).$$

Euler's theorem: If a and b are relatively prime then

$$1 \equiv a^{\phi(b)} \bmod b.$$

Fermat's theorem:

$$1 \equiv a^{p-1} \bmod p.$$