

## Deficiencies in Top-down parser

- 1) Backtracking
- 2) Order of Alternative is matter
- 3) during failure location of error can not be discovered
- 4) Left Recursion -

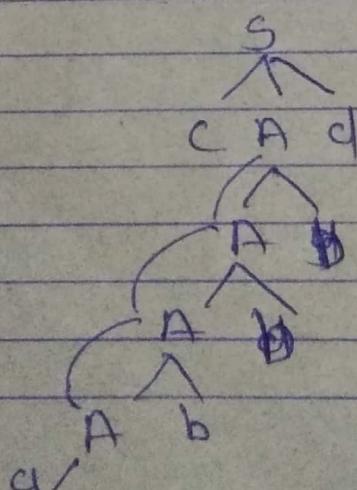
A grammar is left recursive if it has a non-terminal 'A' such that there is a derivation

$$A \xrightarrow{+} A\alpha$$

+ → After some steps

(A tense after some  
A $\alpha$ )

- Left most tree  
is increase till to we  
stop it. for example



1) Shift this is Action Func  
2) Rewrite =  $E \rightarrow E$  on first position on  
3)  $E \rightarrow E + T \mid T$  Right hand expression like

Elimination - if 'A' gives

If 'A' gives  $A \rightarrow A\alpha | \beta$  where  $\beta$  does not begin with 'A' then we can eliminate Left Recursion by Replacing with it

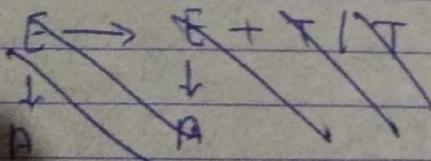
$$\begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \kappa A' | E \end{array}$$

Example —

Consider the following grammar

$$\begin{array}{l} E \rightarrow E + T \quad |T \\ T \rightarrow T * F \quad |F \\ F \rightarrow (E) \quad |id \end{array}$$

- eliminate left recursion



$E \rightarrow E + T + T$  can be  
Replace by following Rates

$$E \rightarrow E + T \mid T$$

$\downarrow$        $\downarrow$        $\downarrow$   
 D      X      B

# Recursive decent Parser [Top-Down] Parser

- It is a Parser that uses a set of Recursive Procedures to recognize its input with no backtracking

- ~~The~~ the grammar provided for this Parser should not be left recursive

Consider the grammar.

$$\begin{aligned} \text{Ex. } E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow (E) \mid \text{id} \end{aligned}$$

The given grammar is left recursive. So we need to remove left recursion first.

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \mid \epsilon \end{aligned}$$

$$\begin{aligned} T &\rightarrow FT' \\ T' &\rightarrow *FT' \mid \epsilon \\ F &\rightarrow (E) \mid \text{id} \end{aligned}$$

terminal { id, ., (, ), +, \* }

Non terminal { E, E', T, T', F }

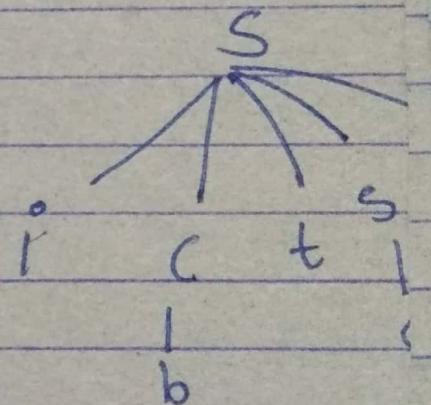
\* Left factoring Ex.

Consider the grammar.

\*  $S \rightarrow icts \mid ictses \mid a$   
 $c \rightarrow b$

$w = ibt aeu$

OR (clanalling - elue  
problem)



## Left - factoring. -

even though they do not have left Recursion are sometimes not Suitable for Recursive descent Parser

Example is cancelling else problem. To overcome this we obtain left factors by the following Rule

IF  $A \rightarrow \alpha\beta / \alpha r$ , then replaced by

$$A \rightarrow \alpha A' \quad \text{--- } ①$$

$$A' \rightarrow \beta / r \quad \text{--- } ②$$

Compare it with one grammar above

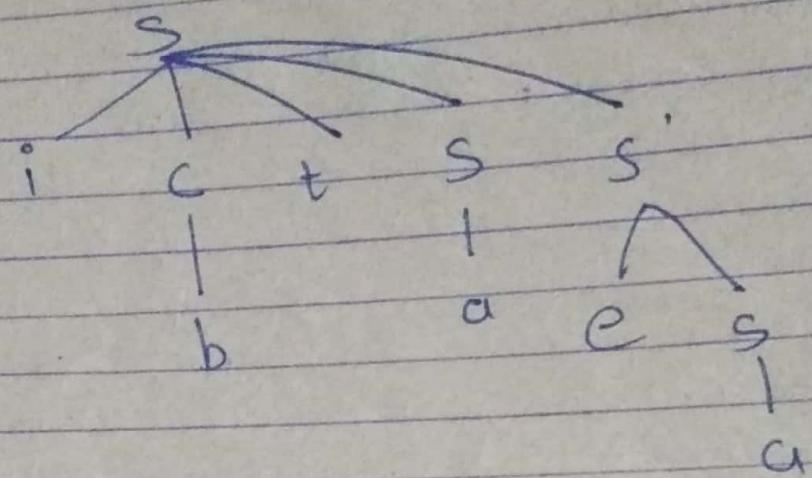
$A = S$ ,  $\alpha = ictS$ ,  $\beta = \epsilon$ ,  $r = es$

and substitute in eqn ① & ②

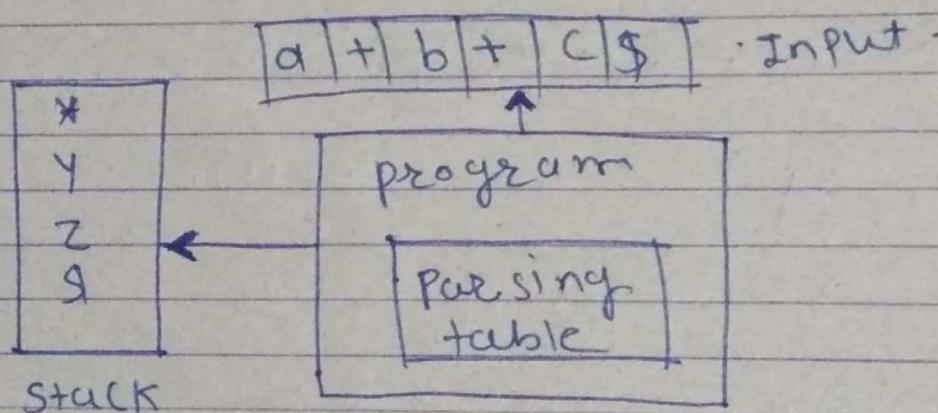
$$\begin{aligned} S &\rightarrow ictS \quad S' \\ S' &\rightarrow \epsilon / es \\ S &\rightarrow a \\ C &\rightarrow b \end{aligned}$$

new grammar.

$w = ibtae \in$



\* Predictive Parser  $\rightarrow$  RDP  $\rightarrow$  Top - do



Model of Predictive  
Parser.

- A more efficient way of implementing Recursive Descent Parser is to use stack activation records.

Predictive Parser  $\Rightarrow$  This is done.

\* FIRST

in SHORT

$$1) \quad x \quad \text{FIRST}(x) = \{x\}$$

$$2) \quad x \rightarrow a \alpha \quad \text{FIRST}(x) = \{a\} \\ x \rightarrow \epsilon \quad \text{FIRST}(x) = \{\epsilon\}$$

$$3) \quad x \rightarrow y_1, y_2, \dots, y_k \quad \text{FIRST}(y_j),$$

$$j = 1, \dots, i-1 \\ \text{FIRST}(y_1)$$

$$j = 1, \dots, k.$$

• Rules to find FOLLOW set:-

- ① Put \$ in FOLLOW(S) if S is the start symbol.
- ② If there is a production  $A \rightarrow \alpha B \beta$  where  $\beta \neq \epsilon$  then  $\text{FOLLOW}(B) = \text{FIRST}(\beta) - \{\epsilon\}$
- ③ If  $A \rightarrow \alpha B$  or  $A \rightarrow B\beta$  where  $\beta = \epsilon$  then  $\text{FOLLOW}(B) = \text{FOLLOW}(A)$ .

• FOLLOW(E) :-

$$\text{FOLLOW}(E) = \{\$\}$$

by rule ①

$$F \rightarrow (E)$$

Compare with  $A \rightarrow \alpha B \beta$ :

$$\therefore A = F, B = E, \alpha = (, \beta = )$$

As  $\beta \neq \epsilon$ , apply ② rule

$$\text{FOLLOW}(B) = \text{FIRST}(\beta) - \{\epsilon\}$$

$$\text{FOLLOW}(E) = \text{FIRST}( )) - \{\epsilon\}$$

$$= \{\)} - \{\epsilon\}$$

- If epsilon FIRST( $y_j$ ) for all  $j=1 \dots n$  then  
 & add epsilon to FIRST( $X$ ).

- Consider the previous grammar & find FIRST & FOLLOW sets.

Ans:-

FIRST() :-

Non-terminals - { $E, E', T, T', F$ }

Terminals - {id, +, \*, (, )}

- Find FIRST set for all terminal symbols by rule one.

$$\text{FIRST(id)} = \{\text{id}\}$$

$$\text{FIRST(())} = \{\()\}$$

$$\text{FIRST(+)} = \{+\}$$

$$\text{FIRST(())} = \{\)\}$$

$$\text{FIRST(*)} = \{* \}$$

- By rule two, Find the FIRST set of non-terminals whose RHS starts with terminals.

$$E' \rightarrow +TE' / \epsilon$$

$$\text{FIRST}(E') = \{+, \epsilon\}$$

$$T' \rightarrow *FT' / \epsilon$$

$$\text{FIRST}(T') = \{*, \epsilon\}$$

$$F \rightarrow \text{id} / (\epsilon)$$

$$\text{FIRST}(F) = \{\text{id}, ()\}$$

- By rule three, find FIRST set of symbols E & T.

- $E \rightarrow TE'$
- $\text{FIRST}(E) = \text{FIRST}(T)$
- $T \rightarrow FT'$
- $\text{FIRST}(T) = \text{FIRST}(F)$
- $\text{FIRST}(F) = \{\text{id}, ()\}$
- $\text{FIRST}(T) = \{\text{id}, ()\}$
- $\text{FIRST}(E) = \{\text{id}, ()\}$

• Rules to find follow set:

① Put  $\$$  in  $\text{Follow}(S)$  if  $S$  is the start symbol.

② If there is a production  $A \rightarrow XB\beta$  where  $\beta \neq \epsilon$  then  $\text{Follow}(B) = \text{FIRST}(\beta) - \{\epsilon\}$

③ If  $A \rightarrow XB$  or  $A \rightarrow B\beta$  where  $\beta = \epsilon$  then  $\text{Follow}(B) = \text{Follow}(A)$ .

•  $\text{Follow}(E) :-$

$$\text{Follow}(E) = \{\$\}$$

by rule ①

$$F \rightarrow (E)$$

Compare with  $A \rightarrow XB\beta$

$$\therefore A = F, B = E, X = (), \beta = ()$$

As  $\beta \neq \epsilon$ , apply rule ②

$$\text{Follow}(B) = \text{FIRST}(\beta) - \{\epsilon\}$$

$$\text{Follow}(E) = \text{FIRST}(()) - \{\epsilon\}$$

$$= \{\)\} - \{\epsilon\}$$

$$\text{Follow}(E) = \{\$, ()\}$$

•  $\text{Follow}(E') :-$

Compare it with  $A \rightarrow XB\beta$

$$A \rightarrow X E \rightarrow TE'$$

$$A = E, B = E', X = T, \beta = E$$

As  $\beta = \epsilon$ , apply rule ③

$$\text{Follow}(B) = \text{Follow}(A)$$

$$\text{Follow}(E') = \text{Follow}(E)$$

$$\text{Follow}(E') = \{\), \$\}$$

•  $\text{Follow}(T) :-$

Case 1 :- Compare it with  $A \rightarrow XB\beta$

$$E \rightarrow TE'$$

$$A = E, B = T, X = E, \beta = E'$$

As  $\beta \neq \epsilon$ , apply rule ②

$$\text{Follow}(B) = \text{FIRST}(\beta) - \{\epsilon\}$$

$$\text{Follow}(T) = \text{FIRST}(E) - \{\epsilon\}$$

$$= \{\), \$\} - \{\epsilon\}$$

$$\text{Follow}(T) = \{\), \$, \epsilon\}$$

Case 2 :-

\* FOLLOW( $T'$ ) :-

$$T \rightarrow FT'$$

Compare it with  $A \rightarrow XB\beta$ .

$$A = T, B = T', X = F, \beta = \epsilon.$$

As  $\beta = \epsilon$ , apply rule ③

$$\text{FOLLOW}(B) = \text{FOLLOW}(A)$$

$$\text{FOLLOW}(T') = \text{FOLLOW}(T)$$

$$\text{FOLLOW}(T') = \{\}, \$, +, *$$

\* FOLLOW( $F$ ) :-

$$T \rightarrow FT'$$

$$A = T, B = F, X = \epsilon, \beta = T'$$

$\beta \neq \epsilon$ , apply rule ②

case 1 :-  $T' \rightarrow *FT'$

Compare it with  $A \rightarrow XB\beta$ .

$$A = T', B = F, \beta = T', X = *$$

As,  $\beta \neq \epsilon$ , apply rule ②

$$\text{FOLLOW}(B) = \text{FIRST}(B) - \{\epsilon\}$$

$$= \text{FIRST}(T') - \{\epsilon\}$$

$$\text{FOLLOW}(F) = \{\ast, \epsilon\}$$

case 2 :-

$$T' \rightarrow \epsilon$$

$$A = T', B = F, X = \epsilon, \beta = \epsilon.$$

As,  $\beta = \epsilon$ , apply rule ③

$$\text{FOLLOW}(B) = \text{FOLLOW}(A)$$

$$\text{FOLLOW}(F) = \text{FOLLOW}(T')$$

$$\text{FOLLOW}(F) = \{\}, \$, +, *, \epsilon\}$$

\* Construction of Parsing Table.

① If the production has RHS value then find its FOLLOW set

② If RHS of the production is  $\epsilon$  then find its FOLLOW set.

$$* E \rightarrow TE'$$

Row  $\leftarrow$  FIRST(RHS)

$$\text{FIRST}(TE') = \text{FIRST}(T)$$

=  $\{\text{id}\}$  (→ column)

$$M[E, \{\text{id}\}, \{\}] = \{\$ | E \rightarrow TE'\}$$

$$* E' \rightarrow +TE'$$

FIRST(RHS)

$$\text{FIRST}(+TE') = \{+\}$$

$$M[E', \{+\}, \{\}] = \{\epsilon | E' \rightarrow +TE'\}$$

$$* E' \rightarrow \epsilon$$

$$\text{FOLLOW}(E') = \{\}, \$\}$$

$$M[E', \{\}, \{\$|\}] = \{\epsilon | E' \rightarrow \epsilon\}$$

2) Goto -

Goto function takes a state and grammar symbols as input and produces some state as output.

E.g Consider this Grammar & Parsing table.

*Erweitert  
Augmentierte  
neue Grammatik*

Augmented Grammar  $G'$  -

it is new grammar  
obtained by adding a new symbol  $s'$  & new production

$$S' \rightarrow s$$

Ex - Find  $G'$  for  $G$  -

$$\begin{aligned} E &\rightarrow E + T, \\ E &\rightarrow T \end{aligned}$$

$$\begin{aligned} T &\rightarrow T * F \\ T &\rightarrow F \\ F &\rightarrow (E) \\ F &\rightarrow id. \end{aligned}$$

$G'$

$$E' \rightarrow E$$

$$E \rightarrow E + T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

13/9/2019

## UNIT 04

### Syntax Directed Translation

- Syntax Directed Definitions :-  
It is CFG with attributes & rules

#### Type of Attributes -

1) Synthesized - Value of non-terminal  
LHS value depend on RHS values [Bottom-up is used]

2) Inherited - Value on RHS

[Top-down fashion used] is defined in terms of LHS

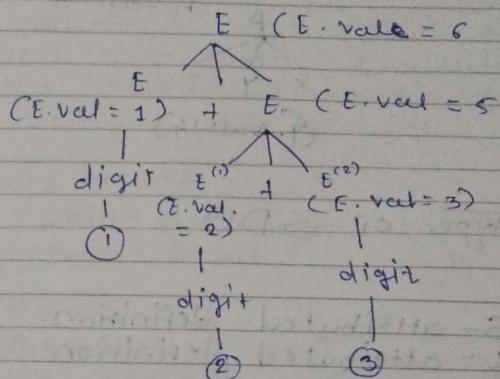
Ex - Production      Semantic Action

$$E \rightarrow E + E \quad \{ E \cdot \text{VAL} := E^{(1)} \cdot \text{VAL} + E^{(2)} \cdot \text{VAL} \}$$

$$E \rightarrow \text{digit.} \quad \{ E \cdot \text{VAL} := \text{digit} \}$$

This is example of synthesized attribute as the value of expression is define from the inputs in Bottom-up fashion

Ex 1 - Input  $\rightarrow 1+2+3$



Ex 2 -

Production

$$A \rightarrow XYZ$$

Semantic Action

$$\{ Y \cdot \text{val} := \text{A} \cdot \text{val} \}$$

It is an example of inherited Attribute as the value of the RHS symbol i.e. 'Y' depends on value of 'A'

Q.1. Consider the grammar

$$\begin{aligned} L &\rightarrow E_n \\ E &\rightarrow E_1 + T \\ E_1 &\rightarrow T \\ T &\rightarrow T_1 * F \\ T_1 &\rightarrow F \\ F &\rightarrow (E) \\ F &\rightarrow \text{digit.} \end{aligned}$$

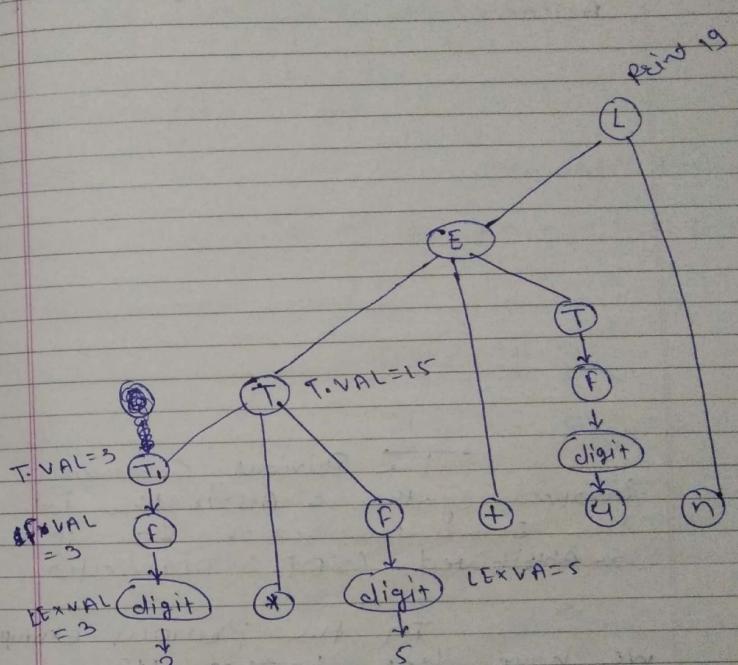
implement SDD (SDT) ~~for~~ for the following expression

$$1) 3 + 5 * 4 n$$

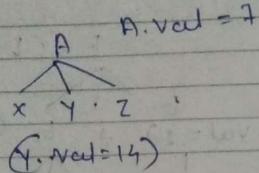
$$2) (3+4) * (5+6)n$$

Prod<sup>n</sup>      Semantic Action

$$\begin{aligned} L &\rightarrow E_n & \text{Print } E \cdot \text{val} \\ E &\rightarrow E_1 + T & E \cdot \text{val} := E_1 \cdot \text{val} + T \cdot \text{val} \\ E &\rightarrow T & E \cdot \text{val} := T \cdot \text{val} \\ T &\rightarrow T_1 * F & T \cdot \text{val} := T_1 \cdot \text{val} * F \cdot \text{val} \\ T &\rightarrow F & T \cdot \text{val} := F \cdot \text{val} \\ F &\rightarrow (E) & F \cdot \text{val} := E \cdot \text{val} \\ F &\rightarrow \text{digit.} & F \cdot \text{val} := \text{LEXVAL} \end{aligned}$$



Input - 7



### \* Type of SDD

- 1) S-attributed definition
- 2) L-attributed definition

#### 1) S-attributed definition -

An SDD is S-attributed if every attribute is synthesized.

Refer Ex - 1

#### 2) L-attributed definition

In this each attribute must be either synthesized or inherited.

Refer E - 2

### Example - Implementation of SDD

Implement SOT (SDD) for Desk calculator. Evaluate the expression  $23 * 5 + 4$  using SDD scheme

1) writing grammar

- Write a grammar to describe the input.

1)  $S \rightarrow E \$$

2)  $E \rightarrow E + E$

3)  $E \rightarrow E * E$

4)  $E \rightarrow (E)$

5)  $E \rightarrow I$

6)  $I \rightarrow I \text{ digit}$

7)  $I \rightarrow \text{digit}$

{ I.val = I<sup>(1)</sup>.val \* 10 + I<sup>(2)</sup>.val }  
{ I.val = LEXVAL }

2) Semantic Action

- ADD Semantic Action to the productions of grammar.

1) { Print E.val }

2) { E.val := E<sup>(1)</sup>.val + E<sup>(2)</sup>.val }

3) { E.val := E<sup>(1)</sup>.val \* E<sup>(2)</sup>.val }

4) { E.val := B<sup>(1)</sup>.val }

5) { E.val := I.val }

6) { I.val := I<sup>(1)</sup>.val \* 10 + LEXVAL }

7) { I.val := LEXVAL },

## \* L- Attributed Definition.

Example - consider the following grammar used to perform Data type declarations

Production

$$\begin{array}{l} D \rightarrow TL \\ T \rightarrow \text{int} \\ T \rightarrow \text{float} \\ L \rightarrow L_1, id \\ \hline \end{array}$$

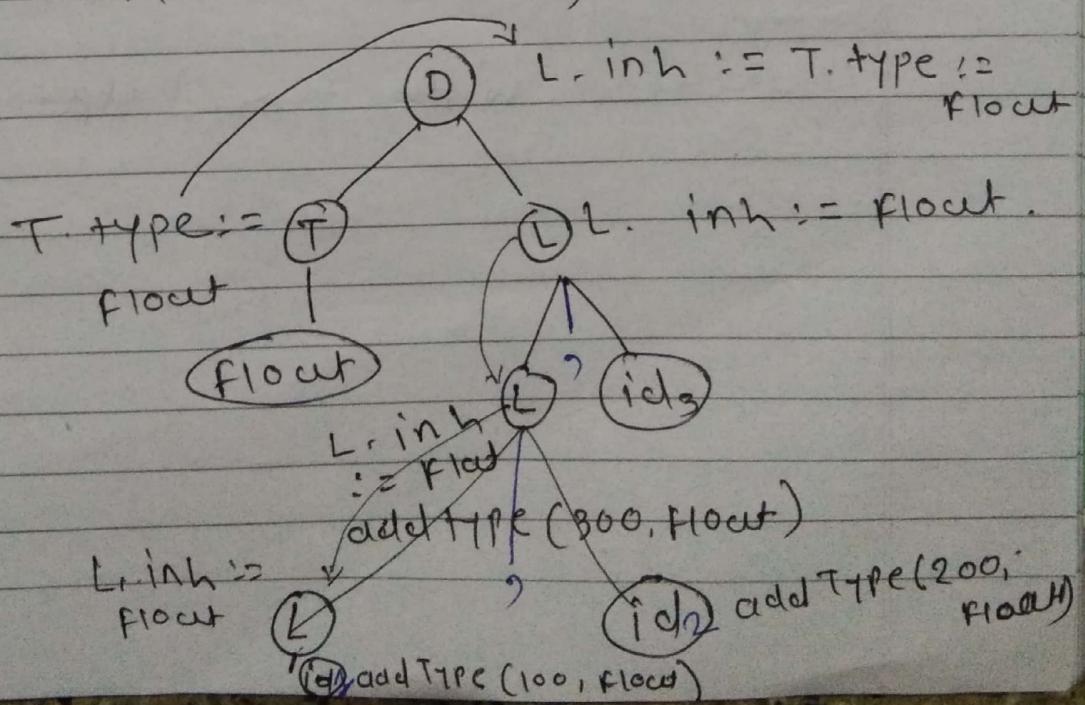
Semantic Rules

$$\begin{aligned} L.\text{inh} &:= T.\text{Type} \\ \text{synthesizing } T.\text{type} &:= \begin{cases} \text{int} \\ \text{float} \end{cases} \\ L_1.\text{inh} &:= L.\text{inh} \\ \text{addType(id.entry, } &L.\text{inh}) \end{aligned}$$

$$L \rightarrow id$$

$\text{addType(id.entry, } L.\text{inh})$

Eg - float a, b, c ;



if - then - else

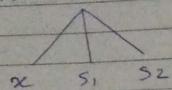


Fig: Syntax tree

#### \* How to Draw Syntax tree

Construction of Syntax tree is similar to Translation of expression in Postfix notation

- Use the following functions to create leave & non-leave nodes & Return a pointer

i) Function 1 - Mknodc (op, left, Right) Ex - Create Syntax tree for the expression

it creates operator node (op) with label "OP" and two fields to point to left & Right nodes

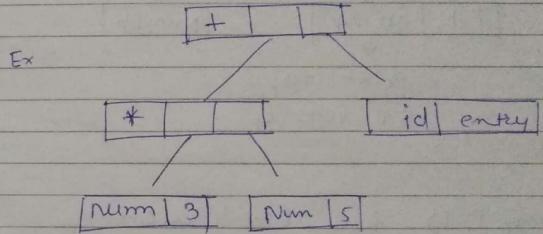
ii) Function 2 - mkleaf (id, entry)

it creates node id with label "id" & a pointer to symbol table

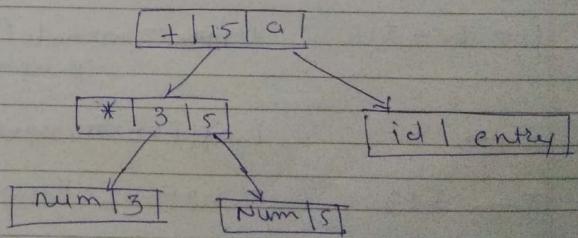
as entry

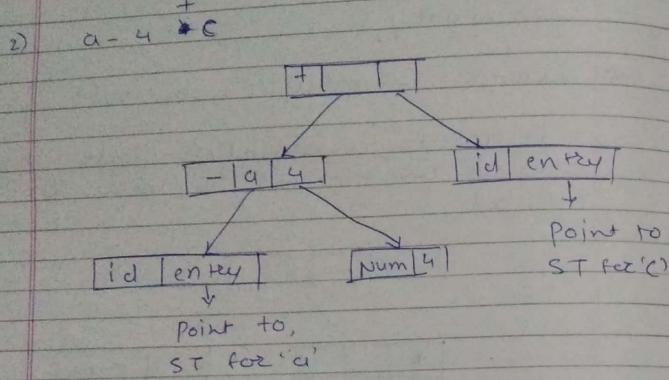
→ Functions - mkleaf (num, val)

it create a number node with label as "num" & value in "val"



$3 * 5 + a$





\* SDD for Constructing Syntax trees

Prod^n

$$E \rightarrow E_1 + T \quad E.nptz := mknode( '+ ', E_1.nptz, T.nptz )$$

$$E \rightarrow E_1 - T \quad E.nptz := mknode( '- ', E_1.nptz, T.nptz )$$

$$E \rightarrow T \quad E.nptz := T.nptz$$

$$T \rightarrow (E) \quad T.nptz := E.nptz$$

$$T \rightarrow id \quad T.nptz := mkleaf( id, entry )$$

$$T \rightarrow num \quad T.nptz := mkleaf( num, val )$$

Q.1 Create syntax tree for the expression  $a - 4 + c$  using semantic rules.

