

# אנאליטיקה של נתונים בזמן 2019-2020

## Introduction and Data Mining Refresh

Robert Moskovitch, PhD  
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Ben Gurion University



- **Funding:** IBM, Microsoft, Amdocs, MoST, MAFAAT and more.
- **Collaborations:** Columbia University, Maccabi Healthcare Services, AIIMS/IIT New Delhi, Peking University, UTHealth, UPenn/CHOP and more
- **Professional Activities (Organizer/SPC/PC):** PLOS ONE – Editor, S/PC: ACM KDD, AAAI, IJCAI, Editorial Board of *Journal of Biomedical Informatics*. AIME 2020 – Co-Chair.
- **Students:** Roni Mateless, Nofar Sarafian, Guy Danieli, Stav Sapir, Tal Ivshin, Maya Schvatz, Pavel Novitzki, Omer Harel, Amos Zamir, Noa Lemberger, Nevo Itzhak, Ofir Dvir, Guy Shitrit.



# Funders and Collaborators

- Funding



Microsoft



Prime Minister's Office  
National Cyber Bureau



משרד המדע,  
הטכנולוגיה והחלל  
Ministry of Science, Technology & Space



- Collaborators



The Best Healthcare in Israel



# Robert Moskovitch, PhD



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- Head, Complex Data Analytics Lab
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- Post Doc, Biomedical Informatics, Columbia University
- R&D Project Manager, Deutsche Telekom Innovation Labs
- Research: Text Retrieval and Categorization, Behavioral (typing and mouse) Verification, Unknown Malware Discovery, Temporal Data Mining (Time Intervals Mining, Classification and Prediction)

# Today's Agenda

- What and Why Temporal Data Analytics?
- Course Goals and TDA Topics
- Course Structure: Assignments and Timeline
- Topics in Brief for the Course Project
- Introduction to Temporal Data Mining
- Prerequisite Methods (without time)
  - Association Rules Mining
  - Classification
  - Clustering

## Typical Atemporal Data

- Atemporal data would be a set of values describing an object.
- The description can refer to a moment in time, or a summary of a time period (i.e., an hour, day, year, cet)
- Typically it will be a vector of descriptors described by values: continuous, nominal, and cet.
- However, temporal data based description is much more heterogeneous, and dynamic, which creates a lot of complexity.

# Analytics of Data in Time

What? . . . . . . . . .

Why? . . . . i . . I . . .

Where? . A AB K IJ LLL O QA

When? . . . : : : : : : : ; .

# Analytics of Data over Time – What?

- Time point values series
  - Fixed frequency (typically, electronic sensors)
    - Different variables may have different frequencies
  - Irregular sampling (typically, manual sampling, or event driven)
- Event series
  - Instantaneous (no duration) events
  - May have different types of events (A, B, C,...)
  - Sampled in fixed frequency
  - Sampled irregularly (manual sampling or event driven)
  - Having duration – time intervals

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# Analytics of Data in Time - Goals

- Overview of the field of **temporal-data-analytics** within the field of data analytics (KDD oriented)
- Motivation for **Temporal Data Analytics**
- **Challenges**: time, different samplings, irregularity, and cet.,.
- Main **Methods**:
  - Time series analysis: univariate, multivariate, indexing/classification/forecasting ..
  - Sequential data mining
  - Time Intervals Mining
  - Temporal Data based Classification and more.

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# Analytics of Data in Time – GOAL (not task)

- The **main goal** is the project
- The course project aims to result in a research reported as an academic paper
  - SIG-KDD style **6-8 pages** paper
- Number of Students: **2** depending on the project (1 or 3 is optional)
- Topics: application of TDA method/s on a temporal dataset/s
- Students who have a **temporal problem in their thesis** are encouraged to work on them as a project – after **approval**. It can be also **sequential**, or using "temporal" methods.
- Otherwise, the students will implement a **published paper** – after **approval**.
- And there will be a quiz on the course materials.

# An Academic Paper – we will speak about it more

- Abstract
- Introduction
- Background
- Methods
- Evaluation {Research Questions, Data, Evaluation Plan}
- Results
- Discussion

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# Analytics of Data in Time – Topics List

- Time Point Series univariate – indexing, match and similarity, search and retrieval, and more
- Multivariate Temporal Data – time series analysis, or heterogeneous variables
- Forecasting
- Clustering
- Classification
- Patterns Discovery
- And more .. we will go through the topics in few more slides ..

# Analytics of Data in Time – GOAL (Project)

- Outcomes:
  - Intermediate:
    - A **project proposal of one page** (in English: Introduction(motivation), Methods, Data, Evaluation Goals)
    - A **literature survey of two pages** (in English, including at least 10 refs)
    - A **presentation of 10 mins** (including not more than 7 slides)
      - 3-4 literature survey + 2 Project Methods + 1 Data + 1 Experimental Plan
  - Final:
    - A project report along **6-8 pages in SIG-KDD format**
      - – download from ACM SIGKDD 2018 CFP
    - A corresponding **presentation of 15 mins**

## Analytics of Data in Time – a quiz

- The quiz will be based on the contents learnt in class
  - at the end of the semester (or **split into two quizzes** to make it easier to prepare)
- Will include two hours and contain about 4-6 questions

# Course Schedule

Date	Lecture	Project Assignments	Date	Lecture	Project Assignments
October 20, 2021	Lecture		December 08, 2021	Literature Survey PPTs	* Attendance mandatory
October 27, 2021	Lecture		December 15, 2019	Literature Survey PPTs	* Attendance mandatory
November 03, 2021	Lecture	* Submit Project Proposal (1 page)	December 22, 2021	Lecture	
November 10, 2021	Lecture		December 29, 2021	Lecture	
November 17, 2021	Lecture		January 05, 2022	Projects PPTs	Quiz 2 * Attendance mandatory
November 24, 2021	Lecture		January 12, 2022	Projects PPTs (Mandatory)	* Attendance mandatory Submit Project
December 1, 2021	Lecture	Quiz 1 * Submit Literature Survey			

# Analytics of Data in Time – Important Dates

- **November 03, 2021** – Projects Proposal in one page (Problem, Methods, Research Questions, Datasets) - better to decide on the first week to start working.
- **December 1, 2021** – Quiz 1 (3 questions)
- **December 1, 2021** – submit literature survey (the beginning of the report: Introduction + Background)
  - You can submit also Methods (or more) and have my comments
- **December 08,15, 2021** - **Literature Survey PPTs**, including:
  - 1 slide : Problem/Motivation
  - 3-4 slides : Common Methods ..
  - 1 slide : your project
- **January 05, 2022** – Quiz 2 (3 questions)
- **January 05, 12, 2022** – **Submit Project Reports + Final Project PPTs**
  - Shortened literature ppt + Methods + Evaluation (Research Questions + Experimental Plan) + Results + Discussion/Conclusion

# Temporal Data Analytics - Grading

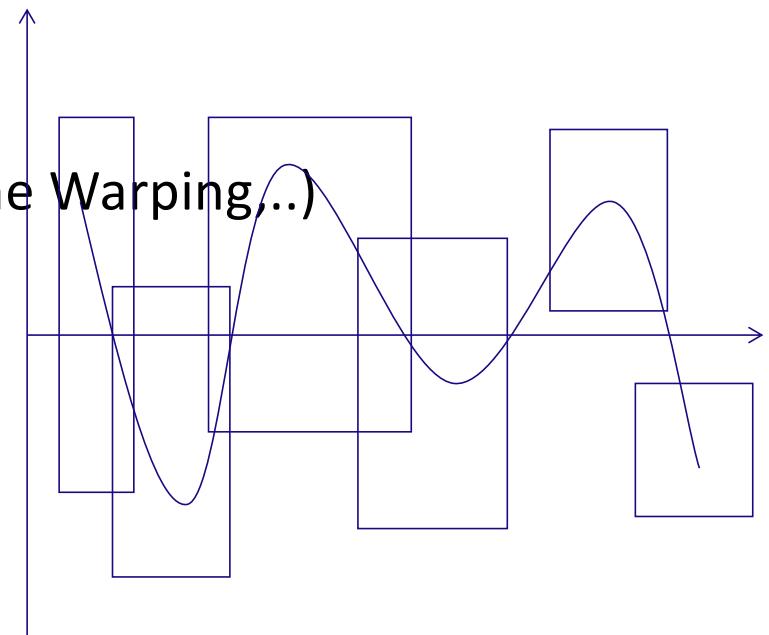
- 15% - Quiz
- 75% - Project
  - 25% - Literature survey + presentation
  - 50% - Final report in academic paper format + ppt
    - 10% originality and innovation
    - 10% complexity
    - 20% writing and presentation
    - 15% soundness and comprehensiveness
- 10% - Impression
  - Attendance – in student presentation classes names will be listed
  - participation in the class, and generally seriousness

# Project Topics List

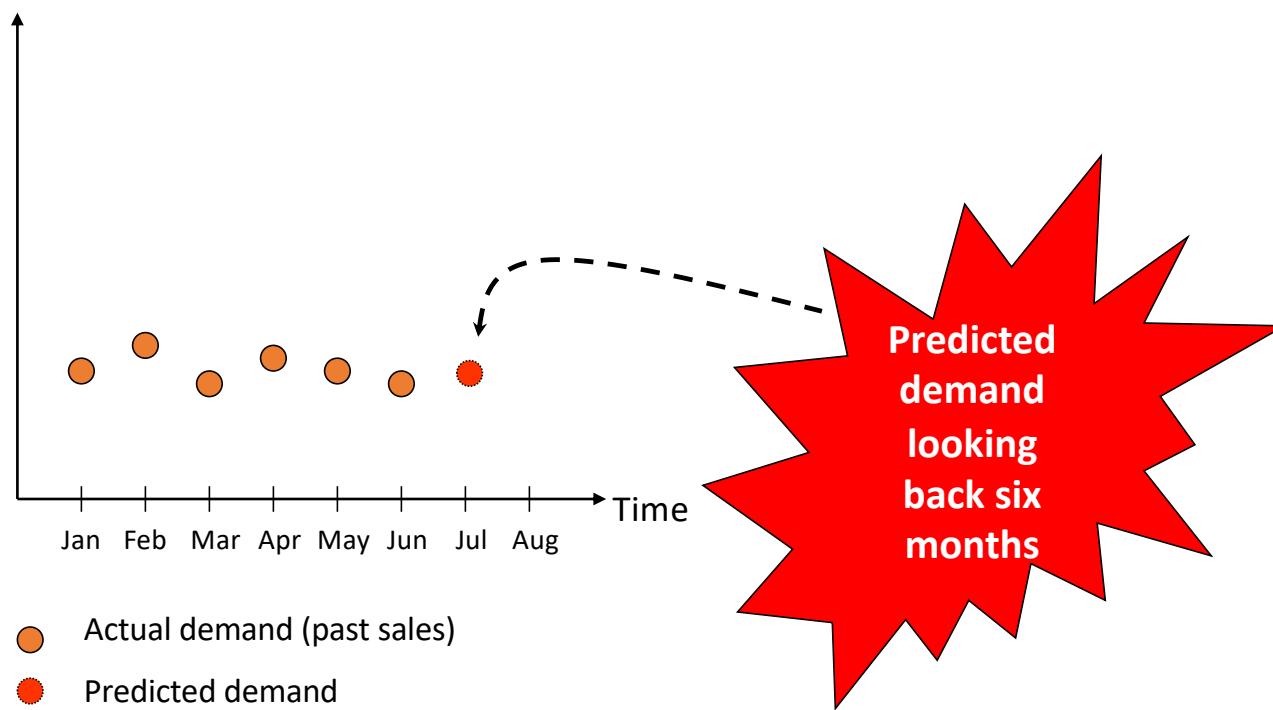
- Time Point Series univariate – indexing, match and similarity, search and retrieval, and more
- Multivariate Temporal Data – time series analysis, or heterogeneous variables
- Forecasting
- Clustering
- Classification
- Patterns Discovery
- And more .. we will go through the topics in few slides

# Univariate Time Series Indexing and Matching

- Indexing and retrieval
- Using raw time series values
- Similarity functions (Euclidean, Dynamic Time Warping,...)
- Using discretization (PAA, SAX, TD4C,...)

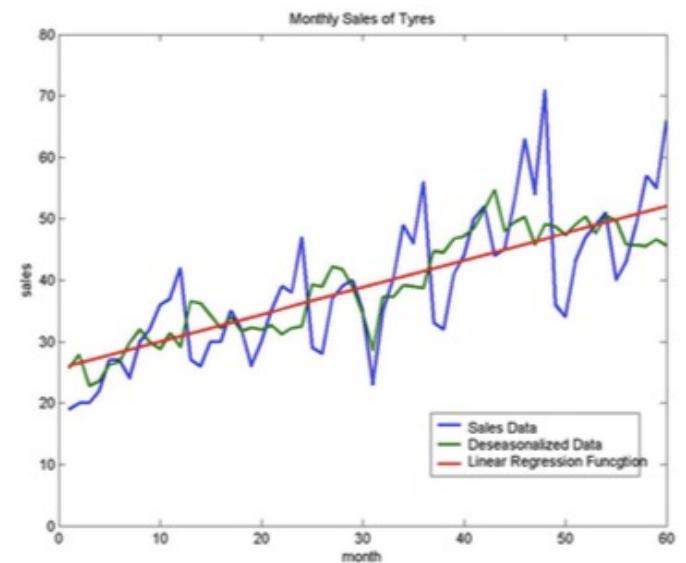


# Forecasting

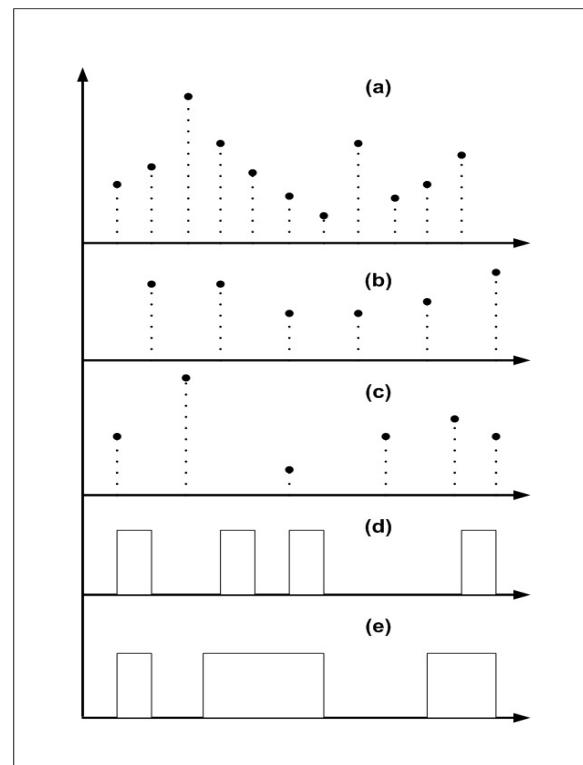


# Forecasting

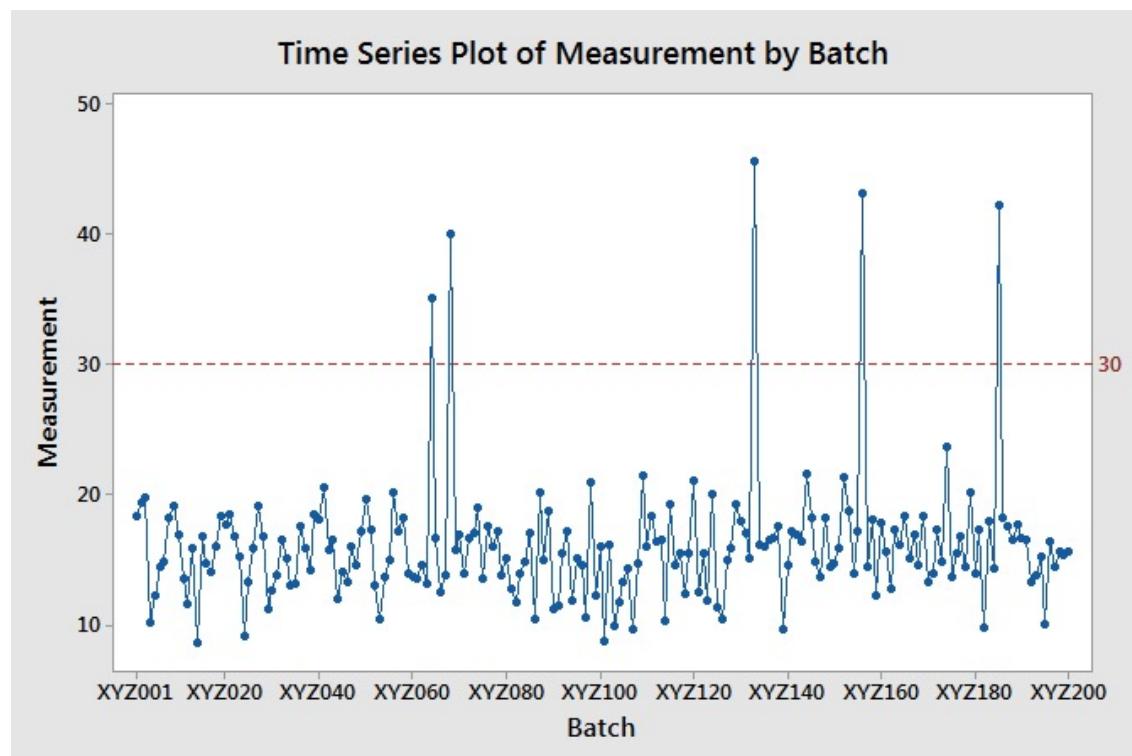
- Forecasting:
  - Autoregressive Models
  - Autoregressive Moving Average Models
    - moving average
    - Weighted moving average
    - Exponential moving average
  - Multivariate Forecasting with Hidden Variables
    - ARMA
    - ARIMA



# Multivariate Heterogeneous Temporal Data



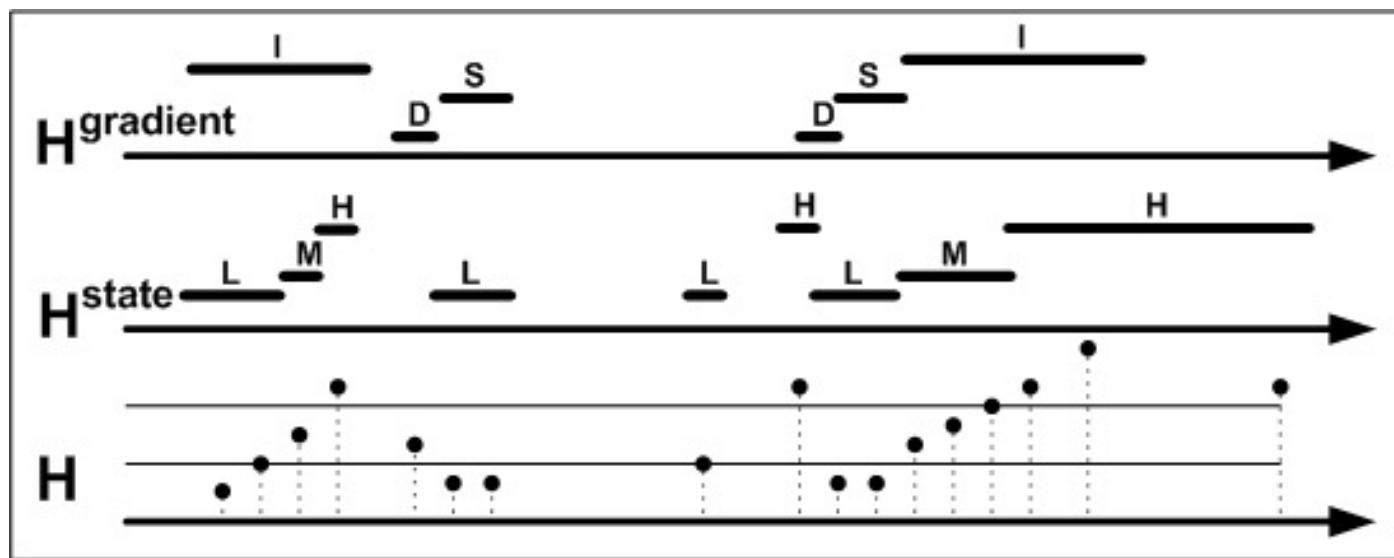
# Outliers and Anomalies



# Clustering of Multivariate Temporal Data

- Through **clustering** of univariate or multivariate time series we can determine common types of "**temporal behavior**"
- Clustering via traditional "**static**" methods
- **Similarity** temporal functions
- Clustering via frequent temporal patterns, especially useful for multivariate clustering through frequent temporal patterns:
  - Sequential mining
  - Time intervals mining
  - Markov Chains

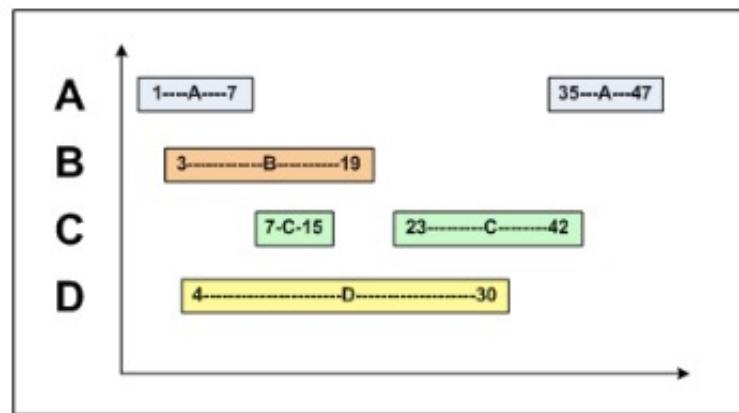
## From Time Points to Time Intervals Series



# Time Intervals Related Patterns Discovery – an illustration



## Time Intervals Related Pattern - TIRP



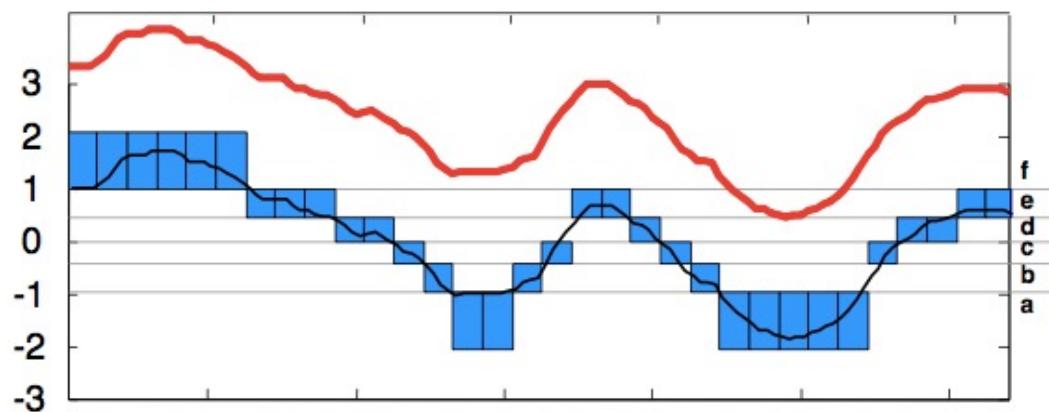
A **TIRP** is a conjunction of pairwise temporal relations

$\{A_1 \circ B, A_1 \circ D, A_1 m C_1, A_1 b C_2, A_1 b A_2, B o D, B c C_1, B b C_2, B b A, C_1 b C_2, C_1 b A, C_2 o A\}$

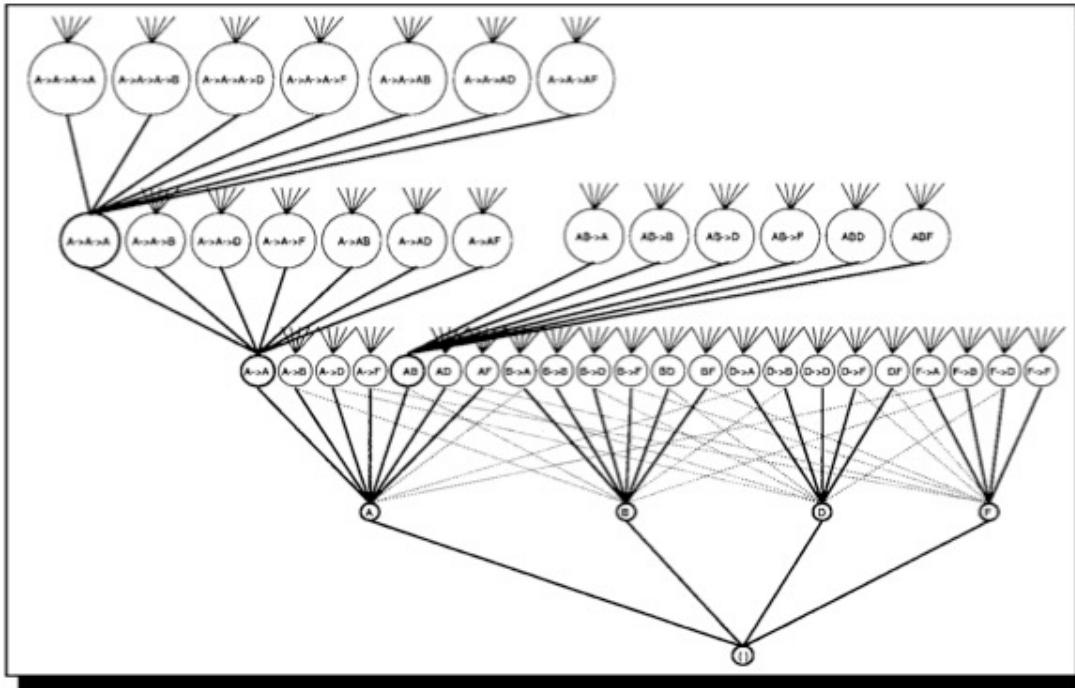
A k-sized TIRP includes  $k(k-1)/2 = (k^2-k)/2$  temporal relations

## SAX [Lin et al, 2003]

- The states' cutoffs are defined by the **normal distribution** of the values: **mean** and **standard-deviations**
- SAX provides a tradeoff between efficiency and approximation accuracy.
- Can be:
  - Symbolic time series
  - Symbolic time intervals



# Sequential Mining



# Classification of Temporal Data

- Classification of univariate/multivariate
- Related issues - Time windows, **imputation** (e.g., mean values)
- **Discretization** (unsupervised/supervised)
- **Features:**
  - Markov Models as features
  - Shapelets
  - Frequent Sequences (**patterns**)
  - Furrier-Transforms as features
  - More ..

# Frequent Temporal Patterns Discovery

- Sequential Mining
- Time Intervals Mining
- Their use for Temporal Knowledge Discovery
- Their use for Classification
- Their use for Clustering (Each pattern is a cluster)
- Metrics for discovery
- Interestingness measures
- Visualization

## Other topics

- Other temporal data mining research topics proposed by the students are possible too, after approval.
- Students are **encouraged** to work on topics from their thesis (msc or phd)

# Data Mining

Since taking Machine Learning or Data Mining courses is **not** a **prerequisite**, we will do a brief overview of Data Mining ..

# Why (Temporal) Data Mining?

- The Explosive Growth of Data: from **terabytes** to **petabytes**
  - **Data collection** and **data availability**
    - Automated data collection tools, database systems, Web, computerized society, **IoT**
  - Major sources of abundant data
    - Business: Web, e-commerce, transactions, **biomedical informatics**, stocks, ...
    - Science: Remote **sensing**, **bioinformatics**, scientific simulation, ...
    - Society and everyone: news, digital cameras, YouTube
- We are drowning in data, but starving for **knowledge!**
- “Necessity is the mother of invention”—Data mining—Automated analysis of massive data set

# What is Data Mining?

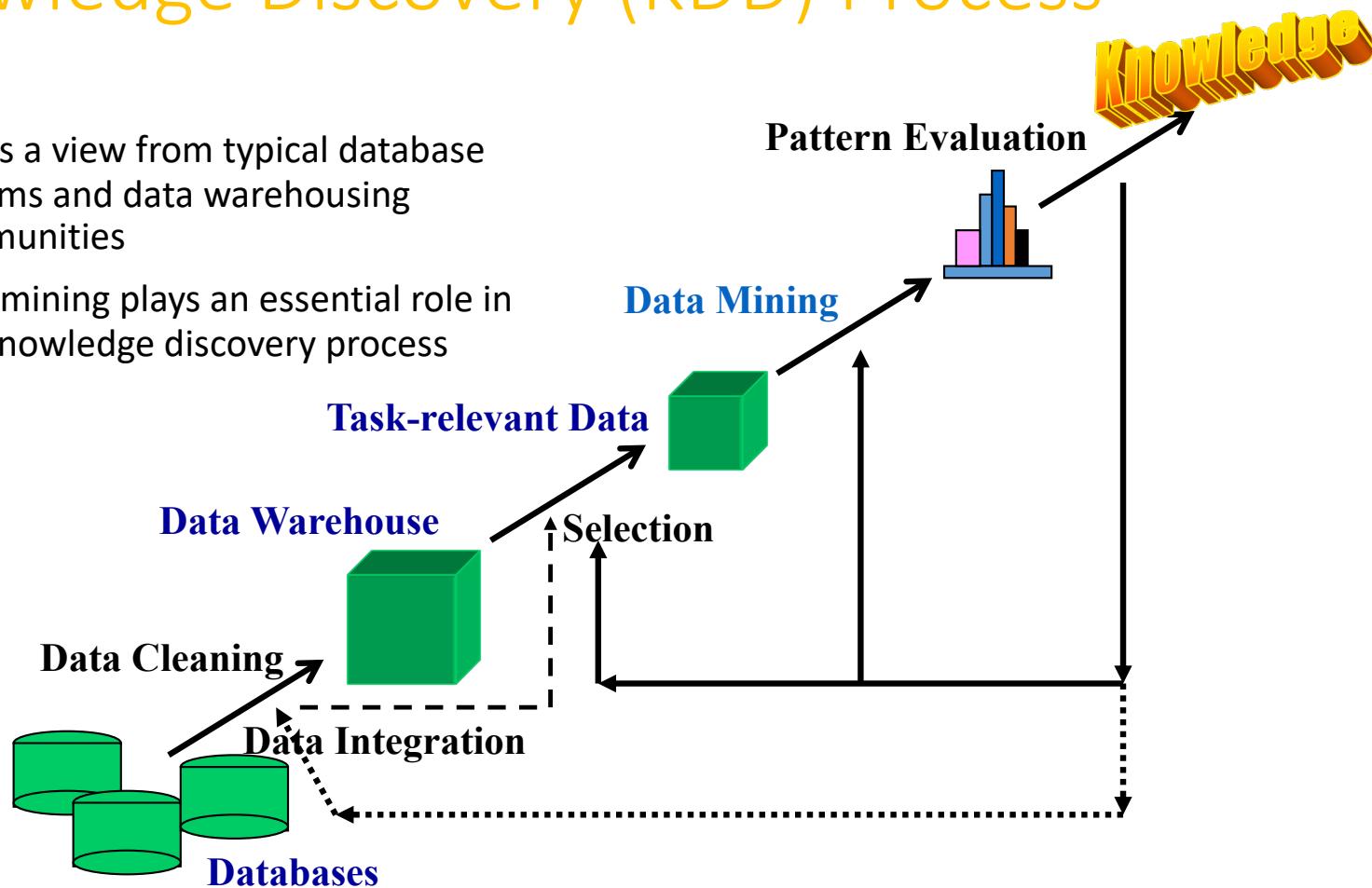


- Data mining (**knowledge discovery** from data)
  - Extraction of interesting (non-trivial, implicit, previously unknown and potentially useful) patterns or knowledge from huge amount of data
- Alternative names
  - Knowledge discovery (**mining**) in databases (KDD), knowledge extraction, data/pattern analysis, data archeology, data dredging, information harvesting, business intelligence, etc.
- Watch out: Is everything “data mining”?
  - Simple search and query processing
  - expert systems



# Knowledge Discovery (KDD) Process

- This is a view from typical database systems and data warehousing communities
- Data mining plays an essential role in the knowledge discovery process



## Example: Medical Data Mining

- Health care & medical data mining – often adopted such a view in statistics and machine learning
  - Typically, in medical data longitudinal analysis is intrinsic and crucial
- Preprocessing of the data (including feature extraction and dimension reduction)
- Classification or/and clustering processes
- Post-processing for presentation

## Data Mining: Association and Correlation Analysis

- Frequent patterns (or frequent itemsets, for example)
  - What items are frequently purchased together in your Walmart?
- Association, correlation vs. causality
  - A typical association rule
    - Diaper → Beer [0.5%, 75%] (support, confidence)
  - Are strongly associated items also strongly correlated?
- How to mine such patterns and rules efficiently in large datasets?
- How to use such patterns for classification, clustering, and other applications?

# Data Mining: Classification

- Classification and label prediction
  - Construct models (functions) based on some **training** examples
  - Describe and distinguish **classes** or **concepts** for future **prediction**
    - E.g., classify countries based on (climate), or classify cars based on (gas mileage)
- Typical **methods**
  - Decision trees, naïve Bayesian classification, support vector machines, neural networks (deep learning), rule-based classification, **pattern-based classification**, logistic regression, ....,
- Typical applications:
  - Credit card fraud detection, direct marketing, diseases, web-pages, ...
  - Temporal – **Outcomes Prediction and "forecasting"**, **Diagnose**, **Reason** ..

## Data Mining: Cluster Analysis

- Unsupervised learning (i.e., Class label is **unknown**)
- **Group** data to form new categories (i.e., clusters), e.g., cluster patients to find disease **progress patterns**
- Principle: Maximizing intra-class similarity & minimizing interclass similarity
- Many methods and applications
  - In the temporal context, it is especially relevant to **temporal patterns discovery** that are – **clusters of temporal behavior**
  - Clustering **stocks** longitudinally
  - Clustering users **behaviors** on the internet

## Data Mining: Outlier Analysis

- Outlier analysis
  - **Outlier**: A data object that **does not comply with the general behavior** of the data
  - **Noise or exception?** — One person's garbage could be another person's treasure
  - Methods: by product of clustering or regression analysis, ...
  - Useful in fraud detection, rare events analysis
- Outliers may be looked for error measurements, but another perspective is **anomaly detection**
- Anomaly detection can be a deviation from the a typical (temporal) behavior ..

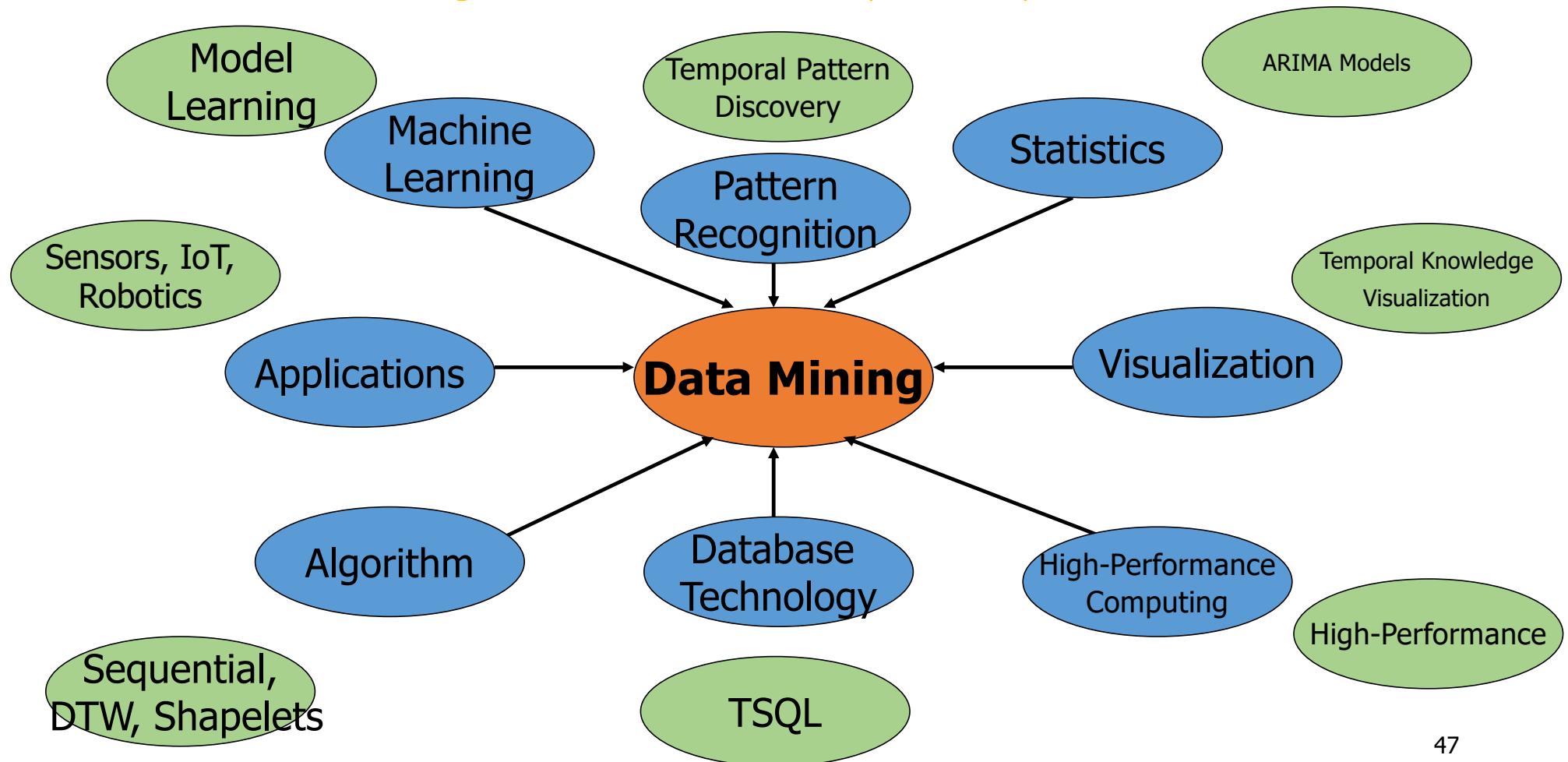
## Time and Ordering: Sequential Pattern, Trend and Evolution Analysis

- Sequence, trend and evolution analysis
  - Trend, time-series, and deviation analysis: e.g., regression and value prediction
  - **Sequential** pattern mining
    - e.g., first smart phone, then buy smart watch
  - **Periodicity** analysis
  - Similarity-based analysis
- Mining data streams
  - Ordered, **time-varying**, potentially infinite, data streams
  - Piecewise Aggregate Approximation, SAX,..

# Evaluation of Knowledge

- Are all mined knowledge interesting?
  - One can discover tremendous amount of “patterns” and knowledge
  - Some may fit only certain dimension space (time, location, ...)
- We want meaningful, ideally significant, actionable knowledge
- Evaluation of mined knowledge → directly mine only interesting knowledge?
  - Descriptive vs. Predictive
  - Typicality vs. novelty
  - Accuracy
  - ...

## Data Mining: Confluence of Multiple Disciplines



# Applications of Data Mining and temporal

- Web page analysis: from web page classification, clustering to PageRank
  - Temporal – Click Stream Analysis, and Sequential Pages Analysis
- Recommender systems
  - Temporal - sequence based recommendations (People who bought A, bought B after 2 months)
- Basket data analysis to targeted marketing
  - Temporal – sequences of basket purchases
- Biological and medical data analysis: classification, cluster analysis, biological sequence analysis, biological network analysis
  - Temporal – Electronic Health Records Analysis

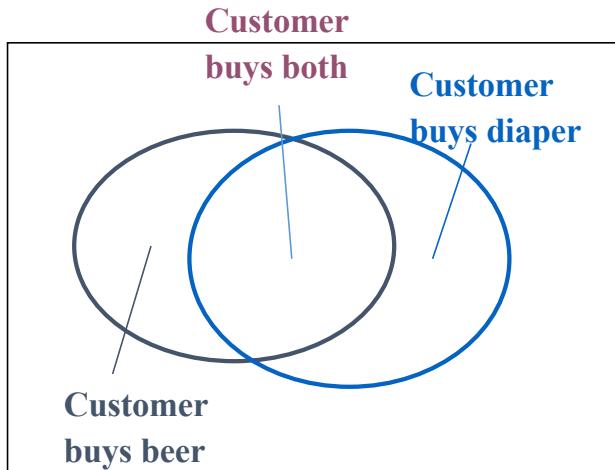
# Temporal Data Mining Venues and Journals

- Conferences:
  - ACM SIGKDD Int. Conf. on Knowledge Discovery in Databases and Data Mining (**KDD**)
  - SIAM Data Mining Conf. (**SDM**)
  - IEEE Int. Conf. on Data Mining (**ICDM**)
  - European Conf. on Machine Learning and Principles and practices of Knowledge Discovery and Data Mining (**ECML-PKDD**)
  - Pacific-Asia Conf. on Knowledge Discovery and Data Mining (**PAKDD**)
  - Other related conferences
    - DB conferences: ACM SIGMOD, VLDB, ICDE, ...
    - Web and IR conferences: WWW, SIGIR, ..
    - ICML, AAAI, IJCAI, ..
- Journals: Data Mining and Knowledge Discovery (DAMI or DMKD), IEEE Trans. On Knowledge and Data Engineering (TKDE), KDD Explorations, ACM Transactions on KDD (TKDD), Knowledge and Information Systems (KAIS)

# Overview on Tools in Data Mining/Machine Learning

- Time Series Analysis
  - Forecasting, Auto Regression, ARIMA
- Pattern Mining
  - Association Rules Mining, Sequential Mining, Time Intervals Mining
- Clustering
  - K-Means, Hierarchical Clustering
- Classification
  - Decision Trees, Random Forests, Naïve Bayes, Deep Learning

## Association Metrics: Support and Confidence



Find all the rules  $X \& Y \Rightarrow Z$  with minimum confidence and support

- **support**,  $s$ , probability that a transaction contains  $\{X \& Y \Rightarrow Z\}$
- **confidence**,  $c$ , conditional probability that a transaction having  $\{X \& Y\}$  also contains  $Z$

Transaction ID	Items Bought
2000	A,B,C
1000	A,C
4000	A,D
5000	B,E,F

Let minimum support 50%, and minimum confidence 50%, we have

- $A \Rightarrow C$  (50%, 66.6%)
- $C \Rightarrow A$  (50%, 100%)

# Applications Examples

- Market Basket Analysis
  - *Maintenance Agreement* (What the store should do to boost Maintenance Agreement sales?)
  - *Home Electronics* (What other products should the store stocks up on if the store has a sale on Home Electronics?)
  - Drug Drug Interactions -> Adverse Events Reactions (Conditions or AERs?)
  - Attached mailing in direct marketing
  - AMAZON

# Association Rules Mining – Problem Statement

- $I = \{i_1, i_2, \dots, i_m\}$ : a set of literals, called items
- Transaction  $T$ : a set of items s.t.  $T \subseteq I$
- Database  $\mathcal{D}$ : a set of transactions
- A transaction contains  $X$ , a set of items in  $I$ , if  $X \subseteq T$
- An association rule is an implication of the form  $X \Rightarrow Y$ ,  
where  $X, Y \subseteq I$
- The rule  $X \Rightarrow Y$  has **support**  $s$  in the transaction set  $\mathcal{D}$  if  $s\%$  of transactions in  $\mathcal{D}$  contain  $X$  and  $Y$
- The rule  $X \Rightarrow Y$  holds in the transaction set  $\mathcal{D}$  with **confidence**  $c$  if  $c\%$  of transactions in  $\mathcal{D}$  that contain  $X$  also contain  $Y$  [ $\text{sup}(X,Y)/\text{sup}(X)$ ]
- Find all rules that have support and confidence greater than user-specified **min support** and **min confidence**

## Problem Decomposition

1. Find all sets of items that have minimum support (frequent itemsets)
2. Use the frequent itemsets to generate the desired rules

## Problem Decomposition – Example

Transaction ID	Items Bought
1	Shoes, Shirt, Jacket
2	Shoes, Jacket
3	Shoes, Jeans
4	Shirt, Sweatshirt

For min support = 50% = 2 trans,  
and min confidence = 50%

Frequent Itemset	Support
{Shoes}	75%
{Shirt}	50%
{Jacket}	50%
{Shoes, Jacket}	50%

For the rule Shoes  $\rightarrow$  Jacket

$$\bullet \text{Support} = \text{Sup}(\{\text{Shoes}, \text{Jacket}\}) = 50\%$$

$$\bullet \text{Confidence} = \frac{50\%}{75\%} = 66.6\%$$

{Jacket , Shoes} has 50% support and 100% confidence

## Discovering Rules

- Naïve Algorithm

**for each** frequent itemset  $l$  **do**

**for each** subset  $c$  of  $l$  **do**

**if** ( $\text{support}(l) / \text{support}(l - c) \geq \text{minconf}$ ) **then**

**output** the rule  $(l - c) \rightarrow c$ ,

with confidence =  $\text{support}(l) / \text{support}(l - c)$

and support =  $\text{support}(l)$

## Mining Frequent Itemsets: the Key Step

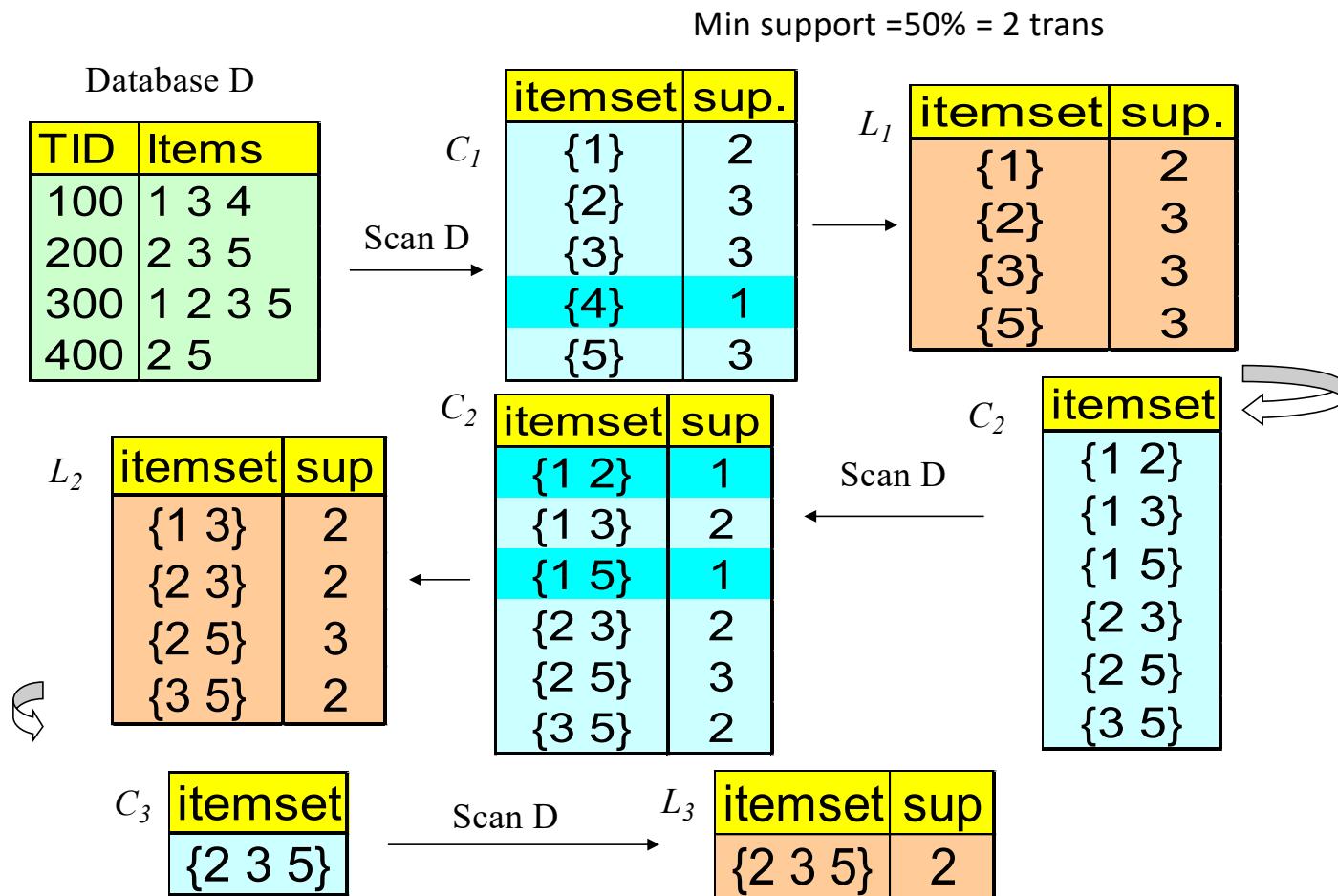
- Find the *frequent itemsets*: the sets of items above minimum support
  - A subset of a frequent itemset must also be a frequent itemset
    - i.e., if  $\{AB\}$  is a frequent itemset, both  $\{A\}$  and  $\{B\}$  should be a frequent itemset
  - Iteratively find frequent itemsets with cardinality from 1 to  $k$  ( $k$ -itemset)
  - Use the frequent itemsets to generate association rules.

# The Apriori Algorithm

- $L_k$ : Set of frequent itemsets of size k (those with min support)
- $C_k$ : Set of candidate itemset of size k (potentially frequent itemsets)

```
 $L_1 = \{\text{frequent items}\};$ 
for ( $k = 1; L_k \neq K; k++$ ) do begin
     $C_{k+1} = \text{candidates generated from } L_k;$ 
    for each transaction  $t$  in database do
        increment the count of all candidates in  $C_{k+1}$ 
        that are contained in  $t$ 
     $L_{k+1} = \text{candidates in } C_{k+1} \text{ with min\_support}$ 
    end
return  $L_k;$ 
```

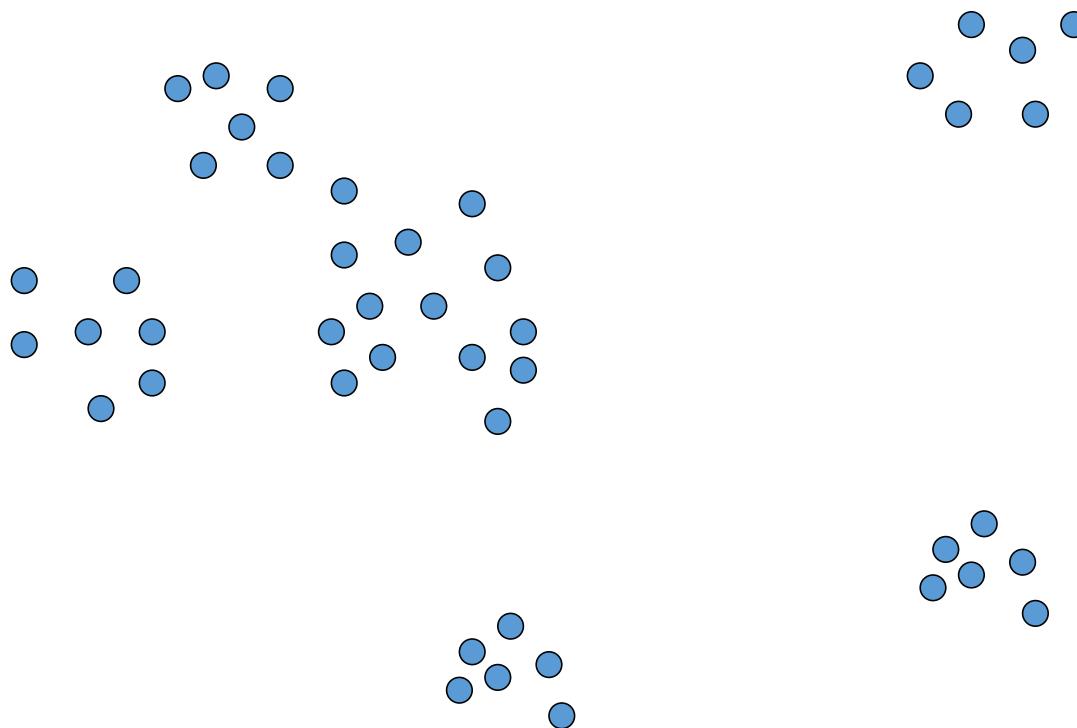
# The Apriori Algorithm — Example



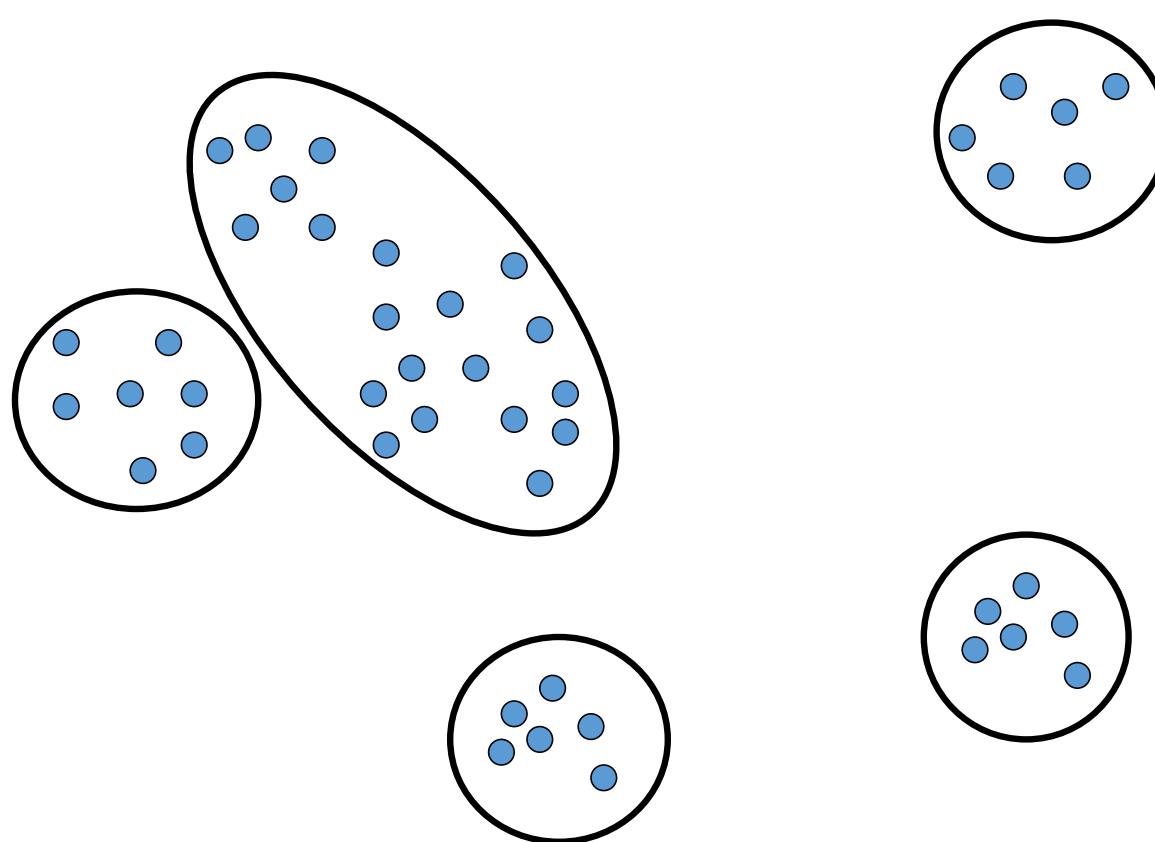
## Methods to Improve Apriori's Efficiency

- **Transaction reduction:** A transaction that **does not contain any frequent k-itemset** is useless in subsequent scans
- **Partitioning:** Any itemset that is potentially frequent in DB must be **frequent in at least one** of the partitions of DB
- **Sampling:** mining on a **subset of given data**
- **Dynamic itemset counting:** add new candidate itemsets only when all of their subsets are estimated to be frequent (apriori-all)

# Clustering



# Clustering



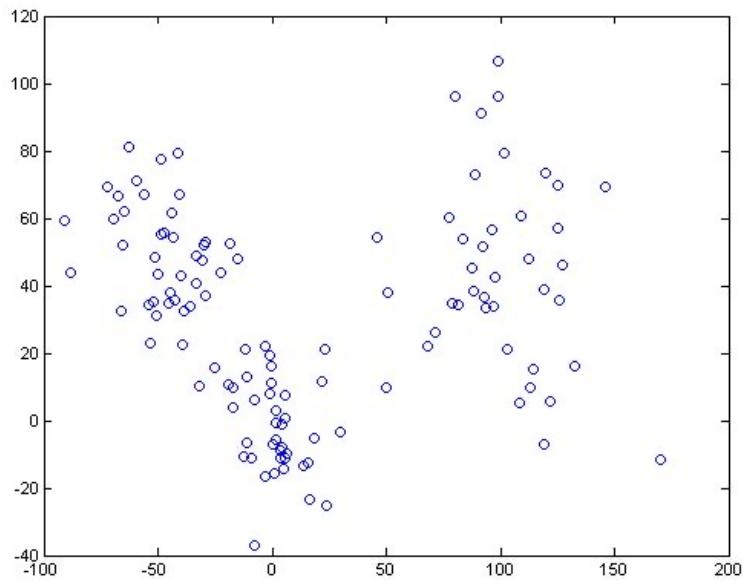
# Clustering considerations

- What does it mean for objects to be similar?
- What algorithm and approach do we take?
  - Top-down: k-means
  - Bottom-up: hierarchical agglomerative clustering
- Do we need a hierarchical arrangement of clusters?
- How many clusters?
- Can we label or name the clusters?
- How do we make it efficient and scalable?

# K-means Clustering

- Choose a number of clusters  $k$
- Initialize cluster centers  $c_1, \dots, c_k$ 
  - Could pick  $k$  data points and set cluster centers to these points
  - Or could randomly assign points to clusters and take means of clusters
- For each data point, compute the cluster center it is closest to (using some distance measure) and assign the data point to this cluster
- Re-compute cluster centers (mean of data points in cluster)
- Stop when there are no new re-assignments

## K-means Clustering (cont.)



How many clusters do you think there are in this data? How might it have been generated?

# K-means Clustering Demo

**k = 2**

## K-means Clustering Issues

- Random initialization means that you may get different FINAL clusters each time
- Data points are assigned to only one cluster (hard assignment)
- You have to pick the number of clusters...

## Determining the “correct” number of clusters

- We'd like to have a measure of **cluster quality**  $Q$  and then try different **values of  $k$**  until we get an **optimal** value for  $Q$
- But, since clustering is an **unsupervised** learning method, we **can't** really expect to find a “correct” measure  $Q$ ...
- So, once again there are different choices of  $Q$  and our decision will depend on what dissimilarity measure we're using and what types of clusters we want

# Cluster Quality Measures

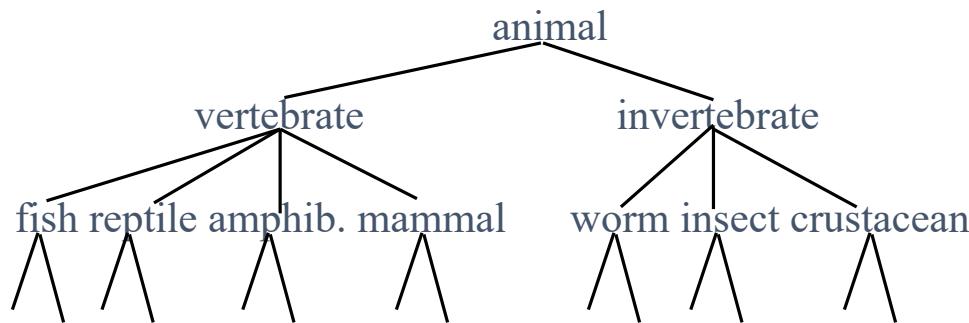
- a measure that emphasizes **cluster tightness** or homogeneity:

$$Q = \sum_{i=1}^k \frac{1}{|C_i|} \sum_{x \in C_i} d(x, \mu_i)$$

- $|C_i|$  is the **number** of data points in cluster  $i$
- $Q$  will be small if (on average) the data points in each cluster are close

# Hierarchical Clustering

- Build a tree-based hierarchical taxonomy (*dendrogram*) from a set of documents.

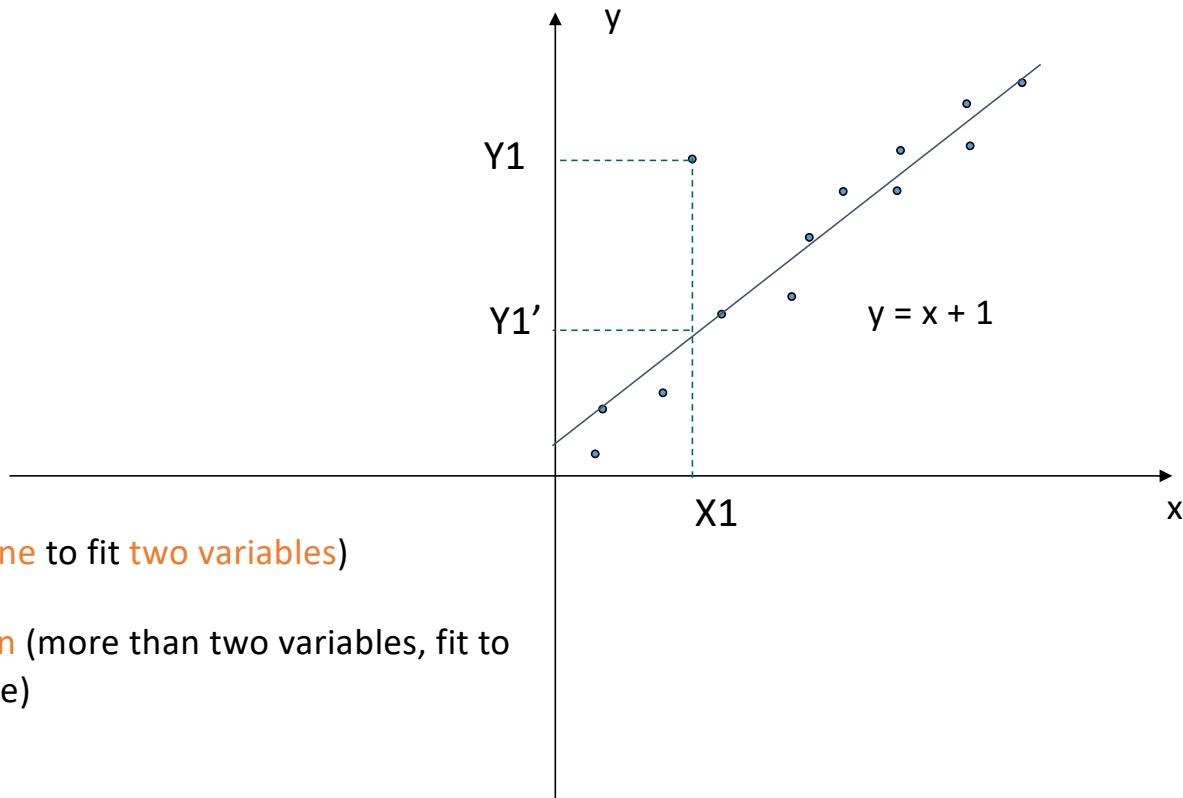


How could you do this with k-means?

# Hierarchical Clustering algorithms

- **Agglomerative (bottom-up):**
  - Start with each document being a single cluster.
  - Eventually all documents belong to the same cluster.
- **Divisive (top-down):**
  - Start with all documents belong to the same cluster.
  - Eventually each node forms a cluster on its own.
  - Could be a recursive application of **k-means like** algorithms
- Does not require the number of clusters ***k*** in advance
- Needs a termination/readout condition

# Regression



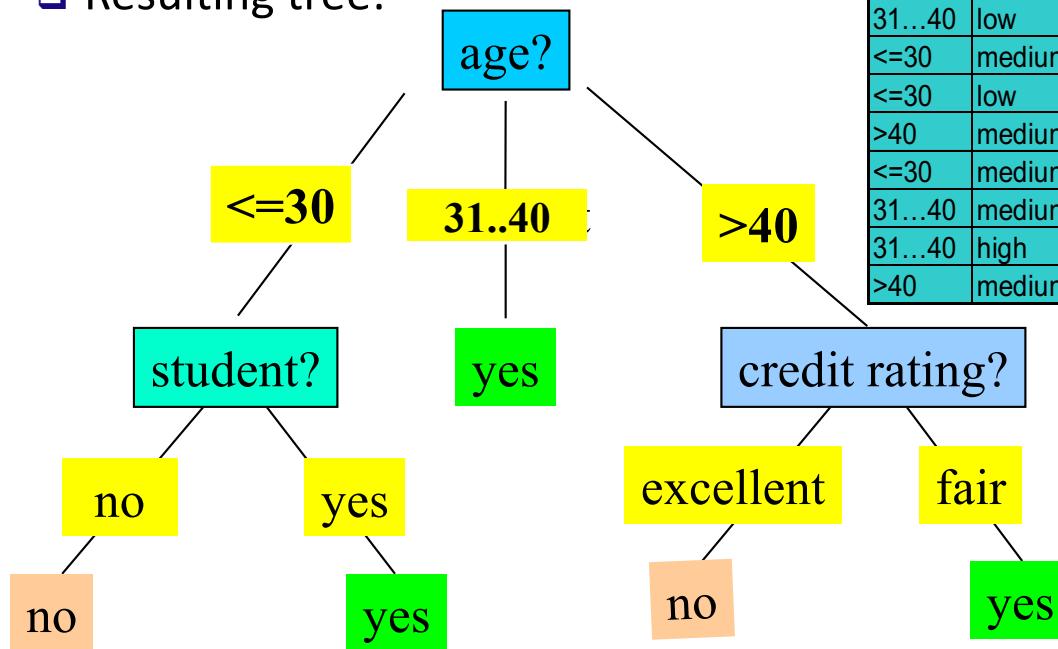
- Linear regression (best line to fit two variables)
- Multiple linear regression (more than two variables, fit to a multidimensional surface)

# Prediction: Classification vs. Numeric

- Classification
  - predicts categorical class labels (discrete or nominal)
  - classifies data (constructs a **model**) based on the training set and the values (**class labels**) in a classifying attribute and uses it in classifying new data
- Numeric Prediction
  - models continuous-valued functions, i.e., predicts unknown or missing values (imputation)
- Typical applications
  - Credit/loan approval, Medical diagnosis, Fraud detection, Web page categorization: which category it is, or recommendation
  - Temporal – incorporates multivariate **temporal behavior**

# Decision Tree Induction: An Example

- ❑ Training data set: Buys\_computer
- ❑ The data set follows an example of Quinlan's ID3 (Playing Tennis)
- ❑ Resulting tree:



age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31..40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31..40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31..40	medium	no	excellent	yes
31..40	high	yes	fair	yes
>40	medium	no	excellent	no

# Bayesian Classification: Why?

- A statistical classifier: performs *probabilistic prediction*, i.e., predicts class membership probabilities
- Foundation: Based on Bayes' Theorem.
- Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct — prior knowledge can be combined with observed data

# Prediction Based on Bayes' Theorem

- Given training data  $\mathbf{X}$ , *posteriori probability of a hypothesis H*,  $P(H|\mathbf{X})$ , follows the Bayes' theorem

$$P(H|\mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})} = P(\mathbf{X}|H) \times P(H) / P(\mathbf{X})$$

- Informally, this can be viewed as  
posteriori = likelihood x prior/evidence

- Practical difficulty: It requires initial knowledge of **many probabilities**, involving significant computational cost

# Model Evaluation and Selection

- Evaluation metrics: How can we measure accuracy? Other metrics to consider?
- Use **validation test set** of class-labeled tuples instead of training set when assessing accuracy
- Methods for estimating a classifier's accuracy:
  - Cross-validation
- Comparing classifiers:
  - Confidence intervals
  - Cost-benefit analysis and ROC Curves

# Classifier Evaluation: Confusion Matrix

**Confusion Matrix:**

Actual class\Predicted class	$C_1$	$\neg C_1$
$C_1$	True Positives (TP)	False Negatives (FN)
$\neg C_1$	False Positives (FP)	True Negatives (TN)

**Example of Confusion Matrix:**

Actual class\Predicted class	buy_computer = yes	buy_computer = no	Total
buy_computer = yes	6954	46	7000
buy_computer = no	412	2588	3000
Total	7366	2634	10000

# Classifier Evaluation : Accuracy, Error Rate, Sensitivity and Specificity

A\P	C	$\neg C$	
C	TP	FN	P
$\neg C$	FP	TN	N
	P'	N'	All

- **Classifier Accuracy**, or recognition rate: percentage of test set tuples that are correctly classified

$$\text{Accuracy} = (\text{TP} + \text{TN})/\text{All}$$

- **Error rate**:  $1 - \text{accuracy}$ , or  
$$\text{Error rate} = (\text{FP} + \text{FN})/\text{All}$$

- **Class Imbalance Problem**:

- One class may be *rare*, e.g. fraud, or HIV-positive
- Significant *majority of the negative class* and minority of the positive class

# Classifier Evaluation: Precision and Recall, and F-measures

- **Precision:** exactness – what % of tuples that the classifier labeled **as positive** are **actually positive**

$$precision = \frac{TP}{TP + FP}$$

- **Recall:** completeness – what % of **positive tuples** did the classifier **label as positive**?

$$recall = \frac{TP}{TP + FN}$$

- Perfect score is 1.0
- Inverse relationship between precision & recall

- **F measure ( $F_1$  or **F-score**):** harmonic mean of precision and recall,

$$F = \frac{2 \times precision \times recall}{precision + recall}$$

- $F_\beta$ : weighted measure of precision and recall
  - assigns  $\beta$  times as much weight to recall as to precision

$$F_\beta = \frac{(1 + \beta^2) \times precision \times recall}{\beta^2 \times precision + recall}$$

# Evaluating Classifier Accuracy: Holdout & Cross-Validation Methods

- **Holdout method**
  - Given data is randomly partitioned into two independent sets
    - Training set (e.g., 2/3) for model construction
    - Test set (e.g., 1/3) for accuracy estimation
  - Random sampling: a variation of holdout
    - Repeat holdout  $k$  times, accuracy = avg. of the accuracies obtained
- **Cross-validation** ( $k$ -fold, where  $k = 10$  is most popular)
  - Randomly partition the data into  $k$  *mutually exclusive* subsets, each approximately equal size
  - At  $i$ -th iteration, use  $D_i$  as test set and others as training set
  - Leave-one-out:  $k$  folds where  $k = \#$  of tuples, for small sized data
  - \*Stratified cross-validation\*: folds are stratified so that **class dist. in each fold is approx. the same** as that in the initial data

## More in DM and ML

- There are more topics related to Data Mining and Machine Learning
  - Feature Selection, Dimensionality reduction
  - Missing values and imputation
  - and more ..

## Recommended References

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