

```

function x = f(n)
    x = 1;
    for i = 1:n
        for j = 1:n
            x = x + 1;

```

1. Find the runtime of the algorithm mathematically (I should see summations).

⇒ To analyze the runtime of the given function mathematically, let's express the number of operations using summations.

- The initialization of $x=1$ takes **constant time: $O(1)$** .
- The **outer loop** runs *from $i = 1$ to $i = n$* , meaning it executes **n times**.
- The **inner loop** runs from $j=1$ to $j = n$, meaning it also executes **n times** for each i .
 - The statement $x=x+1$ inside the inner loop is executed once per inner loop iteration.

Step 2: Writing the Summation

The number of times the innermost operation executes can be expressed as:

$$\sum_{i=1}^n \sum_{j=1}^n 1$$

⇒ Since the inner sum runs n times for each of the n iterations of the outer loop, we expand:

$$\sum_{i=1}^n \sum_{j=1}^n 1 = \sum_{i=1}^n 1$$

$$\sum_{i=1}^n n = n = n^2$$

⇒ Thus, the total number of operation:

$$T(n) = \theta(n^2)$$

Final Answer:

The runtime complexity of the function is: (n^2)

