

If I modified the function to be:

```
x = f(n)
x = 1;
y = 1;
for i = 1:n
    for j = 1:n
        x = x + 1;
        y = i +
```

. Will this increase how long it takes the algorithm to run (e.x. you are timing the function like in #2)?

⇒ Solution:

⇒ Step 1: Understanding the Modification

```
function x = f(n)
    x = 1;
    y = 1;
    for i = 1:n
        for j = 1:n
            x = x + 1;
            y = i + j;
```

⇒ Now includes an **additional assignment operation** inside the inner loop:

$$y = i + j$$

Step 2: Analyzing the Complexity

- The added statement $y = i + j$ is a simple assignment.
- The **loop structure remains the same** ($O(n^2)$).
- The total number of operations per iteration of the inner loop **increases from 1 to 2**.

Thus, the new number of operations is:

$$T(n) = \sum_{i=1}^n \sum_{j=1}^n 2 = 2n^3$$

Step 3: Will the Algorithm Take Longer?


Yes, but **only by a constant factor**.

- The **growth rate** remains $O(n^2)$, so the asymptotic complexity does **not** change.

- However, **in practice**, execution time **will** increase because each inner loop iteration now performs **two** operations instead of one.
- The difference would be **small** but noticeable when timing large n .

Step 4: Conclusion

- **Theoretical Complexity:** $O(n^2)$ remains unchanged.
- **Actual Execution Time:** Increases by a constant factor ($\sim 2x$).
- **Impact on Big-O Analysis:** No effect. The function still grows quadratically.
- **Empirical Measurement:** If timed, the modified function would take roughly **twice as long** for large n .

 **Final Answer:** Yes, the function will take longer to run, but its complexity remains $O(n^2)$