

# A Fuzzy-PID Controller-guided Stochastic Gradient Descent for High-Dimensional Incomplete Matrix Latent Factor Analysis: Supplementary File

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## I. INTRODUCTION

**T**HIS is the supplementary file for paper entitled “A Fuzzy-PID Controller-guided Stochastic Gradient Descent for High-Dimensional Incomplete Matrix Latent Factor Analysis”. It provides Table S1 for symbol appointment and Table S2 for hyperparameter settings of each competitor.

## II. SUPPLEMENTARY HYPERPARAMETER SETTINGS

TABLE S1  
SYMBOL APPOINTMENT

| Symbol                         | Definition  |
|--------------------------------|---|
| $R$                            | An HDI matrix.  |
| $\hat{R}$                      | The rank- $f$ approximation matrix of $R$ .             |
| $U, V$                         | The node sets of $R$ .                                  |
| $u, v$                         | Nodes in $U$ and $V$ .                                  |
| $r_{uv}, \hat{r}_{uv}$         | An element in $R$ and $\hat{R}$ .                       |
| $e_{uv}$                       | The instant error between $r_{uv}$ and $\hat{r}_{uv}$ . |
| $E^{(t)}$                      | The $t$ -th iteration evaluation error.                 |
| $\Lambda$                      | The set of known entries in $R$ .                       |
| $\Omega, \Psi, \Phi$           | Training, test, validation sets from $\Lambda$ .        |
| $P, Q$                         | LF matrices.  |
| $\mathbf{p}_u, \mathbf{q}_v$   | The $u$ -th and $v$ -th row vectors in $P$ and $Q$ .    |
| $\langle \cdot, \cdot \rangle$ | The inner product of two vectors.                       |
| $ \cdot $                      | The cardinality of an enclosed set.                     |
| $\ \cdot\ _2$                  | The $L_2$ norm of an enclosed vector.                   |
| $ \cdot _{abs}$                | The absolute value of a number.                         |
| $f$                            | LF dimension.   |
| $\lambda$                      | Regularization coefficient.                             |
| $\gamma$                       | Learning rate.  |
| $K_P$                          | Proportion gain in the PID controller.                  |
| $K_I$                          | Integral gain in the PID controller.                    |
| $K_D$                          | Derivative gain in the PID controller.                  |

TABLE S2  
HYPERPARAMETER SETTINGS FOR COMPETITORS

| Abbr. | M2  | M3  | M4                          | M5                                      | M6                                      | M7   | M8   | M9  | M10   |
|-------|---|---|-----------------------------|---|---|--|--|---|---|
| D1    | $\gamma=2e-2, \lambda=7e-1, K_P=5e-1, K_I=5e-4, K_D=5e-4$ | $\gamma=2e-2, \lambda=7e-1, K_P=5e-5, K_D=5e-5$ | $\gamma=2e-2, \lambda=7e-1$ | $\gamma=9e-4, \lambda=9e-1, \beta=9e-1$ | $\gamma=9e-4, \lambda=9e-1, \beta=9e-1$ | $\gamma=9e-1, \lambda=8e-1, \epsilon=1e-8$ | $\gamma=8e-3, \lambda=7e-1, \beta=9e-1, \epsilon=1e-8$ | $\gamma=3e-2, \lambda=9e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=5e-2, \lambda=8e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |
| D2    | $\gamma=3e-2, \lambda=4e-2, K_P=5e-1, K_I=5e-4, K_D=5e-2$ | $\gamma=3e-2, \lambda=4e-2, K_P=5e-5, K_D=5e-3$ | $\gamma=3e-2, \lambda=4e-2$ | $\gamma=3e-3, \lambda=4e-2, \beta=9e-1$ | $\gamma=3e-3, \lambda=4e-2, \beta=9e-1$ | $\gamma=8e-2, \lambda=4e-2, \epsilon=1e-8$ | $\gamma=1e-3, \lambda=4e-2, \beta=9e-1, \epsilon=1e-8$ | $\gamma=9e-3, \lambda=7e-2, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=6e-3, \lambda=4e-2, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |
| D3    | $\gamma=8e-3, \lambda=3e-1, K_P=5e-1, K_I=5e-4, K_D=5e-4$ | $\gamma=8e-3, \lambda=3e-1, K_P=5e-4, K_D=5e-4$ | $\gamma=8e-3, \lambda=3e-1$ | $\gamma=9e-4, \lambda=3e-1, \beta=9e-1$ | $\gamma=9e-4, \lambda=3e-1, \beta=9e-1$ | $\gamma=1e-1, \lambda=3e-1, \epsilon=1e-8$ | $\gamma=4e-3, \lambda=4e-2, \beta=9e-1, \epsilon=1e-8$ | $\gamma=7e-3, \lambda=3e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=9e-3, \lambda=3e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |
| D4    | $\gamma=2e-2, \lambda=9e-2, K_P=5e-1, K_I=5e-4, K_D=5e-1$ | $\gamma=2e-2, \lambda=9e-2, K_P=5e-4, K_D=5e-4$ | $\gamma=2e-2, \lambda=9e-2$ | $\gamma=2e-3, \lambda=9e-2, \beta=9e-1$ | $\gamma=2e-3, \lambda=9e-2, \beta=9e-1$ | $\gamma=5e-2, \lambda=3e-1, \epsilon=1e-8$ | $\gamma=5e-3, \lambda=2e-1, \beta=9e-1, \epsilon=1e-8$ | $\gamma=8e-3, \lambda=3e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=8e-3, \lambda=3e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |
| D5    | $\gamma=2e-2, \lambda=8e-1, K_P=5e-1, K_I=5e-4, K_D=5e-1$ | $\gamma=2e-2, \lambda=8e-1, K_P=5e-4, K_D=5e-4$ | $\gamma=2e-2, \lambda=8e-1$ | $\gamma=9e-4, \lambda=9e-1, \beta=9e-1$ | $\gamma=9e-4, \lambda=9e-1, \beta=9e-1$ | $\gamma=4e-1, \lambda=6e-1, \epsilon=1e-8$ | $\gamma=9e-3, \lambda=8e-1, \beta=9e-1, \epsilon=1e-8$ | $\gamma=2e-2, \lambda=9e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=4e-2, \lambda=9e-1, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |
| D6    | $\gamma=8e-3, \lambda=5e-2, K_P=5e-1, K_I=5e-3, K_D=5e-5$ | $\gamma=8e-3, \lambda=5e-2, K_P=5e-5, K_D=5e-4$ | $\gamma=8e-3, \lambda=5e-2$ | $\gamma=5e-4, \lambda=9e-2, \beta=9e-1$ | $\gamma=9e-4, \lambda=6e-2, \beta=9e-1$ | $\gamma=3e-2, \lambda=1e-2, \epsilon=1e-8$ | $\gamma=9e-4, \lambda=6e-2, \beta=9e-1, \epsilon=1e-8$ | $\gamma=8e-3, \lambda=5e-2, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ | $\gamma=9e-3, \lambda=6e-2, \beta_1=9e-1, \beta_2=9.99e-1, \epsilon=1e-8$ |