

Corten: Refinement Types for Imperative Languages with Ownership

Abschlusspräsentation Masterarbeit

Carsten Csiky | 26th Oktober 2022

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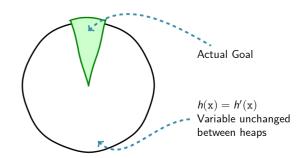


- 1. Motivation
- 2. Type System
- 3. Soundness Justification
- 4. Related Work
- 5. Conclusion / Future Work

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```
public IntList square(IntList list) {
  return list.map(x -> x*x);
```





```
fn max(a: i32, b: i32) {
 if a > b { a } else { b }
```

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```
fn max(a: i32, b: i32) {
 if a > b { a } else { b }
}
```

■ Return Value (v) : $v \ge a \land v \ge b$

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```
fn max(a: i32, b: i32) {
 if a > b { a } else { b }
}
```

- Return Value $(v): v \ge a \land v \ge b$
- Rondon et al. [RKJ08]: Refinement Types for Functional Programming Languages

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```
//@ max(a: i32, b: i32) -> {v:i32 | v >= a && v >= b }
fn max(a: i32, b: i32) -> i32 {
 if a > b { a } else { b }
```

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```
//@ max(a: i32, b: i32) -> \{v:i32 | v >= a && v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
  let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

$$\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$$

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```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
   let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

 Γ , $a > b \vdash a : \tau$

 $\Gamma, \neg (a > b) \vdash b : \tau$

 $\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$

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```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
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  if a > b { a } else { b }
   let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

$$\frac{\Gamma, a > b \vdash \{v : i32 \mid v \doteq a\} \preceq \tau}{\Gamma, a > b \vdash a : \tau} \qquad \frac{\Gamma, \neg(a > b) \vdash b : \tau}{\Gamma, \neg(a > b) \vdash b : \tau}$$

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```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
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  if a > b { a } else { b }
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                         *
    \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                            \Gamma. a > b \vdash a : \tau
                                                                                                                \Gamma, \neg (a > b) \vdash b : \tau
                                                  \Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau
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```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
   if a > b { a } else { b }
    let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
                                                                     \mathsf{SMT\text{-}VALID}\left(\begin{array}{l}\mathsf{true} \wedge \mathsf{true} \wedge a > \upsilon \\ \wedge \, \nu \doteq a \\ \Longrightarrow \, (\nu \geq a \wedge \nu \geq \underline{b})\end{array}\right)
      \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                                         \Gamma. a > b \vdash a : \tau
                                                                                                                                                  \Gamma, \neg (a > b) \vdash b : \tau
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   if a > b { a } else { b }
    let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
                                                              SMT-VALID \begin{pmatrix} \text{true} \land \text{true} \land a > b \\ \land v \doteq a \\ \Longrightarrow (v \geq a \land v \geq b) \end{pmatrix}
     \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                                   \Gamma. a > b \vdash a : \tau
                                                                                                                                    \Gamma, \neg (a > b) \vdash b : \tau
                                                           \Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau
```

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```
clamp(a: &mut i32, b: i32) {
if *a > b { *a = b }
```

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```
fn clamp(a: &mut i32, b: i32) {
  if *a > b { *a = b }
  client(...) {
  . . .
  clamp(\&mut x, 5);
  clamp(&mut y, 6);
 print!(x);
  . . .
```

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```
clamp(a: &mut i32, b: i32) {
if *a > b { *a = b }
client(...) {
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clamp(\&mut x, 5);
clamp(&mut y, 6);
print!(x);
. . .
```

What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5

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```
clamp(a: &mut i32, b: i32) {
if *a > b { *a = b }
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What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5
 - But also 6 (if x aliases with y)!

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```
fn clamp(a: &mut i32, b: i32) {
   if *a > b { *a = b }
}
fn client(...) {
    ...
   clamp(&mut x, 5);
   clamp(&mut y, 6);
   print!(x);
   ...
}
```

What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5
 - But also 6 (if x aliases with y)!
- In Rust:
 - Just old x or 5
 - And nothing else!

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```
clamp(a: &mut i32, b: i32) {
// borrows a
// owns b
if *a > b { *a = b }
// "returns" the borrow of a
 client(...) { // owns x, y
clamp(&mut x, 5); // lend x mutably
clamp(&mut y, 6); // lend y mutably
print!(x);
. . .
```

Ownership in Rust: Mutability XOR Aliasing

Each lexical scope tracks permissions for visible memory objects. Possible Permission Levels:

- Owner (e.g. b)
 - can: read, write
 - transfer ownership (if no outstanding borrows)
- Mutable Reference (e.g. &mut x)
 - can: read, write
 - guarantee: no aliasing
- Immutable Reference (e.g. &v)
 - can: read, alias
 - guarantee: no mutation

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Consequences:

- unique data owner
- no global, mutable state
- no cycles in memory structure

Ownership in Rust: Mutability XOR Aliasing

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Consequences:

- unique data owner
- no global, mutable state
- no cycles in memory structure

Used for:

- safe non-gc memory management
- safe concurrency
- safe low-level hardware access

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Consequences:

- unique data owner
- no global, mutable state
- no cycles in memory structure

Used for:

- safe non-gc memory management
- safe concurrency
- safe low-level hardware access
- ⇒ show: program verification as well

Ownership in Rust: Mutability XOR Aliasing

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Contributions



- Empirical Use-Case Analysis
- Refinement Type System
 - Automatic & Decidable Type Checking
 - Path Sensitivity
 - Mutable Data & References
 - Modularity
 - Partial, Mechanized Proof of Soundness
- Implementation
 - Accessible Interface
 - Type-Error Messages with Source Code Locations
 - Counter-Example Generation
- Evaluation
 - Automatic Verification of non-trivial Programs
 - Comparison to other tools

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Contributions



- Empirical Use-Case Analysis
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Type System

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Restrictions

No Inference System

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Datatypes: Integers, Booleans and References

Overview



- Mutable Values
- Mutable References
- Function-Calls
- Verification of clamp Example
- Demo

```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) -> ty!{ v: () } {
  if *a > b {
      *a = b as ty!{r | (r <= b1)}; ()
  } else {};
fn client() -> ty!{ v: () } {
  let mut x = 1337; let max = 42;
  clamp(&mut x, max);
  x as ty! \{ v : i32 | v < 43 \};
```

Related Work

Conclusion / Future Work





```
fn max(a: i32, b: i32) -> i32 {
 if a > b { a } else { b }
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type

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```
fn max(
 a: ty!{ av: i32 | true },
 b: ty!{ bv : i32 | true }
) -> ty!{ v : i32 | v >= av \&\& v >= bv } {
 if a > b { a } else { b }
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type

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```
fn max(
  a: ty!{ av: i32 },
 b: ty!{ bv : i32 }
) -> ty!{ v : i32 | v >= av \&\& v >= bv } {
  if a > b { a } else { b }
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
 let mut i = ... as ty!\{ v: i32 | v > 0\};
i = i - 1:
```

- Types need to change through execution
 - ⇒ Type Updates
 - Γ ⊢ s \Rightarrow Γ' (Statement Type Checking)
 - Γ \vdash e : τ (Expression Typing)

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
 let mut i = ... as ty!\{ v: i32 | v > 0\};
 i = i - 1:
```

- Type of i after decrementing?
 - Naïve: ty!{ v : i32 | v = v 1 }
- How to keep type context consistent?
 - separation of program-variables and logic-variables
 - Γ: association of program- to logic-variables and predicate
 - on assignment: replace association, append predicate
 - observation: assignments can not invalidate existing predicates

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

- Type of i after decrementing?
 - Naïve: ty!{ v : i32 | v = v 1 }
- How to keep type context consistent?
 - separation of program-variables and logic-variables
 - Γ: association of program- to logic-variables and predicate
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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

$$\begin{split} & \text{INTRO-SUB} \ \frac{\Gamma \vdash \textbf{\textit{e}} : \tau \qquad \Gamma \vdash \tau \preceq \tau'}{\Gamma \vdash \textbf{\textit{e}} \text{ as } \tau' : \tau'} \\ & \text{DECL} \ \frac{\Gamma \vdash \textbf{\textit{e}} : \left\{\beta : \textbf{\textit{b}} \mid \varphi\right\}}{\Gamma \vdash \text{let} \ \textbf{\textit{x}} = \textbf{\textit{e}} \Rightarrow \Gamma[\textbf{\textit{x}} \mapsto \beta], \varphi} \end{split}$$

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

$$\begin{split} & \text{BINOP} \ \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash x_1 \odot x_2 : \{\alpha : b \mid \alpha \simeq [\![x_1 \odot x_2]\!]\Gamma\}} \\ & \text{Assign} \ \frac{\Gamma \vdash e : \{\beta : b \mid \varphi\}}{\Gamma \vdash x = e \Rightarrow \Gamma[x \mapsto \beta], \varphi} \end{split}$$

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

$$\text{SEQ} \ \frac{\Gamma \vdash s_1 \Rightarrow \Gamma' \qquad \Gamma' \vdash s_2 \Rightarrow \Gamma''}{\Gamma \vdash s_1; s_2 \Rightarrow \Gamma''}$$

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```
fn client() -> ty!{ v: i32 | v == 4 } {
 let mut q = 3;
 let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
 let mut b = &mut a; // b : \{v_2 : \& i32 \mid v_2 == \& a\}
 *b = 0:
          // changes a's value and type
 b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&q\}
 *b = 4:
                      // changes g's value and type
 a
```

```
LIT \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \nu : \{\alpha : b \mid \alpha \simeq \llbracket \nu \rrbracket \Gamma \}}
```

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```
fn client() -> ty!{ v: i32 | v == 4 } {
 let mut q = 3;
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 let mut b = &mut a; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
 *b = 0:
           // changes a's value and type
 b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
 *b = 4:
                      // changes g's value and type
 a
```

```
REF \frac{\Gamma \vdash \alpha \text{ tresh}}{\Gamma \vdash \&x : \{\alpha : \&b \mid \alpha \simeq \llbracket\&x\rrbracket\Gamma\}}
```

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fn client() -> ty!{ v: i32 | v == 4 } {
  let mut q = 3;
  let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
  let mut b = &mut a; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
  *b = 0:
                      // changes a's value and type
 b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&g\}
  *b = 4:
                       // changes q's value and type
  a
```

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```
fn client() -> ty!{ v: i32 | v == 4 } {
 let mut q = 3;
 let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
 let mut b = &mut a; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
 *b = 0:
           // changes a's value and type
 b = \&mut q; // b : \{v_2 : \&i32 \mid v_2 == \&q\}
 *b = 4:
                       // changes q's value and type
 a
```

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```
fn clamp(a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 }, b: ty!{ b1: i32 }) {</pre>
 if *a > b { *a = b }
fn client() -> ty!{ v: () } {
  . . .
  let max = 42;
  clamp(\&mut x, max);
  x as ty!\{ v : i32 | v < 43 \};
```

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```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) {
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},
       v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

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       v_2 < b_1 \land v_1 \doteq \&ara_0 \land true \land true)
```

- ty! $\{\alpha : \mathbf{b} \mid \varphi \Rightarrow \beta \mid \psi\}$
- **a** Callee requires φ for reference destination α
- lacktriangle Callee ensures ψ for reference destination β
- Of course, multiple arguments possible

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fn clamp(
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  b: ty!{ b1: i32 }
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       v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
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  if *a > b { *a = b }
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      v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
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  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
               v_2 < b_1 \land v_1 \doteq \&arg_0 \land true \land true)
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?

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```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},
               v_2 < b_1 \land v_1 \doteq \&arg_0 \land true \land true)
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context

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```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
               v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state:

$$\Gamma_e = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 \leq b_1)$$

Motivation

Type System 000000000

Soundness Justification

Related Work

Conclusion / Future Work



```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
          v_2 \leq b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state:

$$\Gamma_{e} = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 \leq b_1)$$

• show: $\Gamma_2 \prec \Gamma_2$

Motivation

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$$\begin{array}{c} \vDash \Phi'[\mu'(x) \rhd \mu(x) \mid x \in \mathsf{dom}(\mu')] \to \Phi \\ \\ \preceq \mathsf{-CTX} & \frac{\mathsf{dom}(\mu') \subseteq \mathsf{dom}(\mu)}{(\mu, \Phi) \preceq (\mu', \Phi')} \end{array}$$

- still left: proof obligation from signature $a_2 \le b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state: $\Gamma_e = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 \leq b_1)$
- show: $\Gamma_2 \leq \Gamma_e$

Motivation

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Related Work

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Mutable Calls



```
fn client(...) -> ty!{ v: () } {
   . . .
  let m = 42:
  // \Gamma_1 = (\{x \mapsto v_1, m \mapsto v_2\}, \ldots \land v_2 \doteq 42)
  clamp(\&mut x, m);
  // \Gamma_2 = (\{x \mapsto v_3, m \mapsto v_2\}, \ldots \land v_2 \doteq 42 \land v_3 \leq 5)
  x as ty!\{ v : i32 | v < 43 \};
```

- append predicates from callee to context
- update association of logic variables

Motivation

Type System

Soundness Justification

Related Work

Conclusion / Future Work

```
    Readme.md

               lib.rs
src > 🔞 lib.rs > 🕤 client
          #![allow(dead code)]
          | · · let · mut · x : i32 · = · 1337; · let · max : i32 · = · 42;
```

Motivation Type System Soundness Justification Related Work Conclusion / Future Work Literatur 00000000

```
·let·mut x: i32 = 1337; let max: i32 = 42;
```

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```
: checking is_sub_context ...
(declare-datatypes () ((Unit unit)))
(declare-const |_0| Int)
(declare-const |r| Int)
(declare-const |a1| Int)
(declare-const |b1| Int)
(declare-const |a2| Int)
; ty!\{ r : i32 | (r \le b1) \}
(assert (<= |r| |b1|))
; ty!{ a1 : &mut i32 | true }
(assert true)
     ty!{ b1 : i32 | true }
(assert true)
```

```
; SuperCtx:
(assert (not (and
        (<= |r| |b1|)
        true
    )))
; checking: RContext {
      a : ty!{ _0 : \&mut i32 | _0 == \& arg (Ousize) }
      <dangling> : ty!{ a1 : &mut i32 | true }
      b : ty!{ b1 : i32 | true }
      <argument 0> : tv!{ r : i32 | (r <= b1) }</pre>
  <: RContext {
      <argument 0> : ty!{ a2 : &mut i32 | a2 <= b1 }</pre>
      b : ty!{ b1 : i32 | true }
(check-sat)
```

Soundness



Progress

If
$$\Gamma \vdash s_1, \sigma : \Gamma \Rightarrow \Gamma_2$$
 and $s_1 \neq \text{unit}$, then there is a s_2 and σ_2 with $\langle s_1 \mid \sigma_1 \rangle \leadsto \langle s_2 \mid \sigma_2 \rangle$.

Corten strictly refines the base language, therefore progress depends on base type system.

Preservation

If
$$\Gamma \vdash s \Rightarrow \Gamma_2$$
, $\sigma : \Gamma$ and $\langle s \mid \sigma \rangle \leadsto \langle s_1 \mid \sigma_1 \rangle$, then there is a Γ_1 with $\Gamma_1 \vdash s_1 \Rightarrow \Gamma_2$ and $\sigma_2 : \Gamma_2$

Stronger property than base language preservation: Show that refined types are preserved

Partial, Mechanized Proof in Lean 4

Motivation

Type System

Soundness Justification •00

Related Work

Conclusion / Future Work

State Conformance



State Conformance σ : Γ

A state σ is conformant with respect to a typing context $\Gamma = (\mu, \Phi)$ (written as $\sigma : \Gamma$), iff:

$$\Phi[\mu(x) \triangleright \llbracket \sigma(x) \rrbracket \mid x \in dom(\mu)]$$
 is satisfiable

I.e. a conformant type context does not contradict the execution state.

Examples:

- If $\sigma:(\emptyset,\Phi)$ then Φ is satisfiable
- If $\sigma: (\mu, \Phi_1 \wedge \Phi_2)$ then $\sigma: (\mu, \Phi_1)$ and $\sigma: (\mu, \Phi_1)$.
- If $\sigma: (\mu, \Phi)$ and $\mathsf{FV}(\Phi) \subseteq \mathsf{dom}(\mu)$, then $\models \Phi[\mu(x) \triangleright \llbracket \sigma(x) \rrbracket \mid x \in \mathsf{dom}(\mu)]$

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Intermediate Steps



Conformance of Symbolic Execution

If $\sigma : \Gamma$, $\Gamma \vdash \alpha$ fresh then $\sigma[x \mapsto \llbracket e \rrbracket \sigma] : \Gamma[x \mapsto \alpha], (\alpha \simeq \llbracket e \rrbracket \Gamma)$

where $(\alpha \simeq \llbracket e \rrbracket \Gamma)$ is the symbolic execution of e equated with α in context Γ

Reference Predicates are Conservative

If $\sigma : \Gamma$ and $\Gamma \vdash *x \in \{y_1, \dots, y_n\}$ then $\llbracket \sigma(x) \rrbracket = \& y_i$ for some $i \in 1, \dots, n$

Rare case where conservative typing requires

Sub-Context Relation is Conservative

If $\Gamma \preceq \Gamma'$ and $\sigma : \Gamma$ then $\sigma : \Gamma'$

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Related Work



Refinement Types and Mutability

- Rondon et al. [RKJ10], Bakst and Jhala [BJ16]: Refinement Types for C subset. Lack of guarantees requires ad-hoc mechanisms to control aliasing
- Lanzinger [Lan21]: Property Types in Java (only immutable). Bachmeier [Bac22]: Extension using Ownership System
- Toman et al. [Tom+20] (ConSORT): Fractional Ownership, strong and weak updates

Rust verification

- Ullrich [Ull16]: Translation to Lean; linear mutation chain. Denis et al [DJM21] similar, but to Why3
- Astrauskas et al. [Ast+19] (Prusti): heavy-weight verification, translation to separation logic (Viper)
- Matsushita et al. [MTK20] (RustHorn): constrained Horn clauses

Motivation

Type System

Soundness Justification

Related Work

Conclusion / Future Work





- MIR vs. HIR
- specification in comments vs. embedding in types
- context inclusions vs. sub context
- distinction strong and weak references vs. dynamic choice by typ checking rules
- explicit introduction of logic variables vs. ad-hoc
- formalization based on RustBelt vs. formalization based on own language
- missing in Corten: records & inference
- otherwise: similar capabilities

```
//@ ensures *self: i32<n+1>:
fn increment(&strg v : i32<n>) -> ()
//@ requires n > 0
//@ ensures *self: i32<n-1>:
fn decrement(&strg v : i32<n>) -> ()
// Corten
fn increment(n: &mut ty!{
  n1: Nat => n1 \mid n1 == n1+1 \}
) -> ();
fn decrement(n: &mut ty!{
  v1: Nat | v1 > 0 \Rightarrow v2 | v2 == v1-1 
) -> ();
```

// Flux

Future Work



- Records & ADTs
 - More Syntax, Nested Structures
 - Variant Distinction
- Predicate Generics (Abstract Predicates)
 - Uninterpreted Functions in Types
- Concurrency using Predicate Generics?
 - Use Uninterpreted Functions
 - Interesting, because unusual guarantees in Rust

Conclusion



- Working Refinement Type System for Rust with Mutability
- Minimal Interface
- Soundness Justification
- Evaluation

Literatur I



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- [2] Joshua Bachmeier. *Property Types for Mutable Data Structures in Java.* 2022. DOI: 10.5445/IR/1000150318. URL: https://publikationen.bibliothek.kit.edu/1000150318 (besucht am 03.10.2022).
- [3] Alexander Bakst und Ranjit Jhala. "Predicate Abstraction for Linked Data Structures". In: *Verification, Model Checking, and Abstract Interpretation*. Hrsg. von Barbara Jobstmann und K. Rustan M. Leino. Lecture Notes in Computer Science. Berlin, Heidelberg: Springer, 2016, S. 65–84. ISBN: 978-3-662-49122-5. DOI: 10.1007/978-3-662-49122-5.

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Literatur II



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- [5] Florian Lanzinger. "Property Types in Java: Combining Type Systems and Deductive Verification". Master Thesis. Karlsruher Institut für Technologie, Feb. 2021.
- [6] Yusuke Matsushita, Takeshi Tsukada und Naoki Kobayashi. "RustHorn: CHC-based verification for Rust programs". In: *European Symposium on Programming*. Springer, Cham, 2020, S. 484–514.
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Literatur III



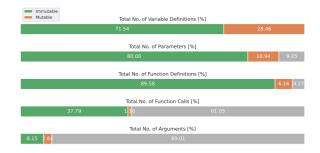
- [8] Patrick Maxim Rondon, Ming Kawaguchi und Ranjit Jhala. "Low-level liquid types". In: *Proceedings of the 37th annual ACM SIGPLAN-SIGACT symposium on Principles of programming languages*. POPL '10. New York, NY, USA: Association for Computing Machinery, 17. Jan. 2010, S. 131–144. ISBN: 978-1-60558-479-9. DOI: 10.1145/1706299.1706316. URL: https://doi.org/10.1145/1706299.1706316 (besucht am 16.09.2022).
- [9] John Toman u. a. "ConSORT: Context- and Flow-Sensitive Ownership Refinement Types for Imperative Programs". In: *Programming Languages and Systems*. Hrsg. von Peter Müller. Cham: Springer International Publishing, 2020, S. 684–714. ISBN: 978-3-030-44914-8. DOI: 10.1007/978-3-030-44914-8. 25.
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Motivation	
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Empirical Use-Case Analysis



- public open-source code (crates.io)
- about 64 million lines of Rust code
- syntactical analysis



Empirical Analysis

decr Typing Tree



$$\operatorname{Intro-SuB} \frac{\Gamma[i \mapsto v_1], v > 0 \text{ and } \tau = \{v : \text{i32} \mid v > 0\}}{\Gamma_1 \vdash \dots : \tau' \qquad \Gamma_1 \vdash \tau' \preceq \tau} \\ \operatorname{DECL} \frac{\Gamma[i \mapsto v_1], v > 0 \text{ and } \tau = \{v : \text{i32} \mid v > 0\}}{\Gamma_1 \vdash \dots : \tau' \qquad \Gamma_1 \vdash \tau' \preceq \tau} \\ \operatorname{Ass} \frac{\Gamma_1 \vdash v_2 \text{ fresh}}{\Gamma_1 \vdash i - 1 : \{v_2 : \text{i32} \mid v_2 \doteq v - 1\}}}{\Gamma_1 \vdash \operatorname{let} \ i = \dots \ \operatorname{as} \ \tau; \ i = i - 1 \Rightarrow \Gamma[i \mapsto v_2], v > 0, v_2 \doteq v - 1}$$

Empirical Analysis

Expression Typing $\Gamma \vdash e : \tau$

$$\begin{array}{c|c} \Gamma \vdash \alpha \text{ fresh} & \Gamma \vdash \alpha \text{ fresh} \\ \hline \Gamma \vdash \nu : \{\alpha : b \mid \alpha \simeq \llbracket \nu \rrbracket \Gamma \} & \text{BINOP} & \hline \Gamma \vdash x_1 \odot x_2 : \{\alpha : b \mid \alpha \simeq \llbracket x_1 \odot x_2 \rrbracket \Gamma \} \\ \hline \text{VAR} & \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash x : \{\alpha : b \mid \alpha \simeq \llbracket x \rrbracket \Gamma \}} & \text{INTRO-SUB} & \frac{\Gamma \vdash e : \tau \qquad \Gamma \vdash \tau \preceq \tau'}{\Gamma \vdash e \text{ as } \tau' : \tau'} \\ \hline \end{array}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

Empirical Analysis 00000

Zweiter Abschnitt

Expression Typing $\Gamma \vdash e : \tau$

$$\begin{aligned} & \text{Ref } \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \&x : \{\alpha : \&b \mid \alpha \simeq [\![\&x]\!]\Gamma\}} \\ & \text{Var-Deref } \frac{\Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash y : \tau}{\Gamma \vdash *x : \tau} \end{aligned}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

Assign-Strong
$$\frac{\Gamma(z) = \beta \qquad \Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash \gamma \text{ fresh}}{\Gamma \vdash *x = z \Rightarrow \Gamma[y \mapsto \gamma], \gamma \doteq \beta}$$

Empirical Analysis ○○○●○○ Zweiter Abschnitt

Expression Typing $\Gamma \vdash e : \tau$

$$\begin{aligned} & \text{Ref} \ \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \&x : \{\alpha : \&b \mid \alpha \simeq [\![\&x]\!]\Gamma\}} \\ & \text{Var-Deref} \ \frac{\Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash y : \tau}{\Gamma \vdash *x : \tau} \end{aligned}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

ASSIGN-STRONG
$$\frac{\Gamma(z) = \beta \qquad \Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash \gamma \text{ fresh}}{\Gamma \vdash *x = z \Rightarrow \Gamma[y \mapsto \gamma], \gamma \doteq \beta}$$

$$\frac{\Gamma \vdash e : \tau \qquad \Gamma \vdash x \in \{\&y_1, \dots, \&y_n\}}{\Gamma \vdash y_i : \{\beta_i : b_i \mid \varphi_i\}} \qquad \Gamma \vdash \tau \preceq \{\beta_i : b_i \mid \varphi_i\}}$$

$$\Gamma \vdash *x = e \Rightarrow \Gamma$$

Zweiter Abschnitt

Blöcke in den KIT-Farben



Greenblock

Standard (block)

Blueblock

= exampleblock

Redblock

= alertblock

Brownblock

Purpleblock

Cyanblock

Yellowblock

Lightgreenblock

Orangeblock

Grayblock

Contentblock

(farblos)

Empirical Analysis 000000

Zweiter Abschnitt

Auflistungen



Text

- Auflistung Umbruch
- Auflistung
 - Auflistung
 - Auflistung

Bei Frames ohne Titel wird die Kopfzeile nicht angezeigt, und der freie Platz kann für Inhalte genutzt werden.

Empirical Analysis
OOOOO

Zweiter Abschnitt
OOO

Farben

36/29 26.10.2022 Carsten Csiky: Rust & Refinement Types

Department of Informatics – Institute of Information Security and Dependability (KASTEL) Bei Frames mit Option [plain] werden weder Kopf- noch Fußzeile angezeigt.

Beispielinhalt



Bei Frames mit Option [t] werden die Inhalte nicht vertikal zentriert, sondern an der Oberkante begonnen.

Empirical Analysis

Beispielinhalt: Literatur



Empirical Analysis

Farbpalette



kit-green100	kit-green90	kit-green8	80 kit-greer	n70 kit-gre	en60 kit-	green50 ki	t-green40	kit-green3) kit-ç	green25	kit-green20	kit-green1	5 kit-gr	reen10 k	t-green5	
kit-blue100	kit-blue90	kit-blue80	kit-blue70	kit-blue60	kit-blue50	kit-blue40	kit-blue30	kit-blue	25 kit-	-blue20	kit-blue15	kit-blue10	kit-blue5			
kit-red100	kit-red90	kit-red80 kit	t-red70 kit-	red60 kit-ı	red50 kit-ı	red40 kit-re	ed30 kit-re	d25 kit-	red20	kit-red15	kit-red10	kit-red5				
kit-gray100	kit-gray90	kit-gray80	kit-gray70	kit-gray60	kit-gray50	kit-gray40	kit-gray30	kit-gray	25 kit	t-gray20	kit-gray15	kit-gray10	kit-gray	5		
kit-orange100	kit-orange	e90 kit-orar	nge80 kit-o	range70 k	tit-orange60	kit-orange	50 kit-oran	ge40 k	t-orange	e30 kit-o	range25	kit-orange20	kit-oran	ige15 kit	orange10	kit-orange5
kit-lightgreen	00 kit-lightgreen90		kit-lightgreen80 kit-ligh		reen70 ki	t-lightgreen60	kit-lightgr	een50	it-lightgreen40 kit-lightg		kit-lightgree	green30 kit-lightgree		reen25 kit-lightgreen		kit-lightgreen1
kit-lightgreen10 kit-lightgreen5																
kit-brown100	kit-brown9	0 kit-brown	180 kit-brov	vn70 kit-b	rown60 ki	it-brown50	kit-brown40	kit-brow	n30 k	kit-brown25	kit-brow	n20 kit-bro	wn15 k	it-brown10	kit-bro	wn5
kit-purple100	kit-purples	00 kit-purpl	e80 kit-pur	ple70 kit-p	ourple60	kit-purple50	kit-purple40	kit-pui	ple30	kit-purple	25 kit-pur	ple20 kit-p	urple15	kit-purple	10 kit-p	ourple5
kit-cyan100	kit-cyan90	kit-cyan80	kit-cyan70	kit-cyan60	kit-cyan5	60 kit-cyan-	40 kit-cyar	130 kit-	yan25	kit-cyan2	0 kit-cya	n15 kit-cya	n10 kit	-cyan5		

Empirical Analysis

