

Corten: Refinement Types for Imperative Languages with Ownership

Abschlusspräsentation Masterarbeit

Carsten Csiky | 26th Oktober 2022

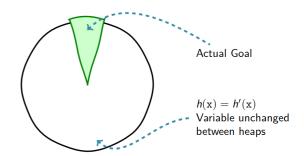
Inhaltsverzeichnis



- 1. Motivation
- 2. Type System
- 3. Soundness Justification
- 4. Related Work
- 5. Conclusion / Future Work



```
public IntList square(IntList list) {
  return list.map(x -> x*x);
```





```
fn max(a: i32, b: i32) {
 if a > b { a } else { b }
```

Motivation 0000000 Type System

Soundness Justification 000

Related Work



```
fn max(a: i32, b: i32) {
  if a > b { a } else { b }
}
```

■ Return Value (v) : $v \ge a \land v \ge b$

Motivation

Type System

Soundness Justification

Related Work



```
fn max(a: i32, b: i32) {
 if a > b { a } else { b }
}
```

- Return Value $(v): v \ge a \land v \ge b$
- Rondon et al. [RKJ08]: Refinement Types for Functional Programming Languages

Motivation 0000000 Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
```

Motivation 0000000 Type System

Soundness Justification

Related Work





```
//@ max(a: i32, b: i32) -> \{v:i32 | v >= a && v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
  let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

$$\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$$

Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
   let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

$$\Gamma$$
, $a > b \vdash a : \tau$

$$\overline{\Gamma, \neg(a > b) \vdash b : \tau}$$

 $\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$

Motivation 00000000 Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
   let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
```

$$\frac{\Gamma, a > b \vdash \{v : i32 \mid v = a\} \leq \tau}{\Gamma, a > b \vdash a : \tau} \qquad \frac{\Gamma, \neg(a > b) \vdash b : \tau}{\Gamma, \neg(a > b) \vdash b : \tau}$$

 $\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$

Motivation 00000000 Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
   let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
                        *
    \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                         \Gamma. a > b \vdash a : \tau
                                                                                                          \Gamma, \neg (a > b) \vdash b : \tau
```

 $\Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau$

Motivation ○○○●○○○○ Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
   if a > b { a } else { b }
    let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
                                                               SMT-VALID \begin{pmatrix} \text{true } \land \text{ true } \land a > b \\ \land v \doteq a \\ \implies (v \geq a \land v \geq b) \end{pmatrix}
     \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                                   \Gamma. a > b \vdash a : \tau
                                                                                                                                   \Gamma, \neg (a > b) \vdash b : \tau
                                                           \Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau
```

Motivation 00000000 Type System

Soundness Justification

Related Work



```
//@ \max(a: i32, b: i32) -> \{v:i32 \mid v >= a \&\& v >= b \}
fn max(a: i32, b: i32) -> i32 {
   if a > b { a } else { b }
    let \Gamma = (a : \{v : i32 \mid true\}, b : \{v : i32 \mid true\}) and \tau = \{v : i32 \mid v \ge a \land v \ge b\}
                                                              SMT-VALID \begin{pmatrix} \text{true} \land \text{true} \land a > b \\ \land v \doteq a \\ \implies (v \geq a \land v \geq b) \end{pmatrix}
     \Gamma, a > b \vdash a : \{v : i32 \mid v = a\} \Gamma, a > b \vdash \{v : i32 \mid v = a\} \prec \tau
                                                   \Gamma. a > b \vdash a : \tau
                                                                                                                                   \Gamma, \neg (a > b) \vdash b : \tau
                                                          \Gamma \vdash \text{if } a > b \{a\} \text{ else } \{b\} : \tau
```

Motivation

Type System

Soundness Justification

Related Work



```
fn clamp(a: &mut i32, b: i32) {
  if *a > b { *a = b }
}
```

Motivation

Type System

 $\underset{\circ \circ \circ}{\text{Soundness Justification}}$

Related Work



```
fn clamp(a: &mut i32, b: i32) {
  if *a > b { *a = b }
  client(...) {
  . . .
  clamp(\&mut x, 5);
  clamp(&mut y, 6);
 print!(x);
  . . .
```

Motivation 00000000 Type System

Soundness Justification

Related Work



```
fn clamp(a: &mut i32, b: i32) {
   if *a > b { *a = b }
}
fn client(...) {
    ...
   clamp(&mut x, 5);
   clamp(&mut y, 6);
   print!(x);
   ...
}
```

What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5

Motivation

Type System

Soundness Justification

Related Work



```
clamp(a: &mut i32, b: i32) {
if *a > b { *a = b }
client(...) {
. . .
clamp(\&mut x, 5);
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What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5
 - But also 6 (if x aliases with y)!

Motivation 00000000 Type System

Soundness Justification

Related Work



```
clamp(a: &mut i32, b: i32) {
if *a > b { *a = b }
 client(...) {
. . .
clamp(\&mut x, 5);
clamp(&mut y, 6);
print!(x);
. . .
```

What does this it print(x) output?

- In most imperative programming languages:
 - Could be: old x or 5
 - But also 6 (if x aliases with y)!
- In Rust:
 - Just old x or 5
 - And nothing else!

Motivation 00000000 Type System

Soundness Justification

Related Work



```
clamp(a: &mut i32, b: i32) {
// borrows a
// owns b
if *a > b { *a = b }
// "returns" the borrow of a
 client(...) { // owns x, y
clamp(&mut x, 5); // lend x mutably
clamp(&mut y, 6); // lend y mutably
print!(x);
. . .
```

Ownership in Rust: Mutability XOR Aliasing

Each lexical scope tracks permissions for visible memory objects. Possible Permission Levels:

- Owner (e.g. b)
 - can: read, write
 - transfer ownership (if no outstanding borrows)
- Mutable Reference (e.g. &mut x)
 - can: read, write
 - guarantee: no aliasing
- Immutable Reference (e.g. &v)
 - can: read, alias
 - guarantee: no mutation

Motivation 00000000 Type System

Soundness Justification

Related Work



Consequences:

- unique data owner
- no global, mutable state
- no cycles in memory structure

Ownership in Rust: Mutability XOR Aliasing

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Consequences:

- unique data owner
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- no cycles in memory structure

Used for:

- safe non-gc memory management
- safe concurrency
- safe low-level hardware access

Ownership in Rust: Mutability XOR Aliasing

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Consequences:

- unique data owner
- no global, mutable state
- no cycles in memory structure

Used for:

- safe non-gc memory management
- safe concurrency
- safe low-level hardware access
- ⇒ show: program verification as well

Ownership in Rust: Mutability XOR Aliasing

Each lexical scope tracks permissions for visible memory objects. Possible Permission Levels:

- Owner (e.g. b)
 - can: read, write
 - transfer ownership (if no outstanding borrows)
- Mutable Reference (e.g. &mut x)
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- Immutable Reference (e.g. &v)
 - can: read, alias
 - guarantee: no mutation

Contributions



- Empirical Use-Case Analysis
- Refinement Type System
 - Automatic & Decidable Type Checking
 - Path Sensitivity
 - Mutable Data & References
 - Modularity
 - Partial, Mechanized Proof of Soundness
- Implementation
 - Accessible Interface
 - Type-Error Messages with Source Code Locations
 - Counter-Example Generation
- Evaluation
 - Automatic Verification of non-trivial Programs
 - Comparison to other tools

Motivation
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Contributions



- Empirical Use-Case Analysis
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Motivation	Type System
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Soundness Justification

Related Work

- No Inference System
- Datatypes: Integers, Booleans and References

Overview



- Mutable Values
- Mutable References
- Function-Calls
- Verification of clamp Example
- Demo

```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) -> ty!{ v: () } {
  if *a > b {
      *a = b as ty!{r | (r <= b1)}; ()
  } else {};
fn client() -> ty!{ v: () } {
  let mut x = 1337; let max = 42;
  clamp(&mut x, max);
  x as ty! \{ v : i32 | v < 43 \};
```





```
fn max(a: i32, b: i32) -> i32 {
  if a > b { a } else { b }
}
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type





```
fn max(
 a: ty!{ av: i32 | true },
 b: ty!{ bv : i32 | true }
) -> ty!{ v : i32 | v >= av \&\& v >= bv } {
 if a > b { a } else { b }
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type

Type System 0.000000 Soundness Justification

Related Work





```
fn max(
  a: ty!{ av: i32 },
  b: ty!{ bv : i32 }
) -> ty!{ v : i32 | v >= av \&\& v >= bv } {
  if a > b { a } else { b }
```

- Embedding using a Macro
- ty! $\{I: b \mid \varphi\}$ in place of a type



```
fn decr() -> ty!{ w : i32 | w >= 0 } {
 let mut i = ... as ty!\{ v: i32 | v > 0\};
i = i - 1:
```

- Types need to change through execution
 - ⇒ Type Updates
 - \blacksquare $\Gamma \vdash s \Rightarrow \Gamma'$ (Statement Type Checking)
 - Γ \vdash e : τ (Expression Typing)

13/27



```
fn decr() -> ty!{ w : i32 | w >= 0 } {
 let mut i = ... as ty!\{ v: i32 | v > 0\};
 i = i - 1:
```

- Type of i after decrementing?
 - Naïve: ty!{ v : i32 | v = v 1 }
- How to keep type context consistent?
 - separation of program-variables and logic-variables
 - Γ: association of program- to logic-variables and predicate
 - on assignment: replace association, append predicate
 - observation: assignments can not invalidate existing predicates



```
fn decr() -> ty!{ w : i32 | w >= 0 } { // \Gamma_1 = (\{\}, \text{true}) let mut i = ... as ty!{ v: i32 | v > 0}; // \Gamma_2 = (\{i \mapsto v\}, v > 0) i = i - 1; // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1) i }
```

```
Type of i after decrementing?
```

Naïve: ty!{ v : i32 | v = v - 1 }

- How to keep type context consistent?
 - separation of program-variables and logic-variables
 - Γ: association of program- to logic-variables and predicate
 - on assignment: replace association, append predicate
 - observation: assignments can not invalidate existing predicates

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```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

$$\begin{split} \text{INTRO-SUB} & \frac{\Gamma \vdash e : \tau \qquad \Gamma \vdash \tau \preceq \tau'}{\Gamma \vdash e \text{ as } \tau' : \tau'} \\ \text{DECL} & \frac{\Gamma \vdash e : \{\beta : b \mid \varphi\}}{\Gamma \vdash \text{let } x = e \Rightarrow \Gamma[x \mapsto \beta], \varphi} \end{split}$$



BINOP
$$\frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash x_1 \odot x_2 : \{\alpha : b \mid \alpha \simeq [\![x_1 \odot x_2]\!]\Gamma\}}$$
 Assign
$$\frac{\Gamma \vdash e : \{\beta : b \mid \varphi\}}{\Gamma \vdash x = e \Rightarrow \Gamma[x \mapsto \beta], \varphi}$$

Motivation

Type System 00●000000

Soundness Justification

Related Work



```
fn decr() -> ty!{ w : i32 | w >= 0 } {
  // \Gamma_1 = (\{\}, true)
  let mut i = ... as ty!\{ v: i32 | v > 0\};
  // \Gamma_2 = (\{i \mapsto v\}, v > 0)
  i = i - 1:
  // \Gamma_3 = (\{i \mapsto v_2\}, v > 0 \land v_2 \doteq v - 1)
  i }
```

$$\text{SEQ} \ \frac{\Gamma \vdash s_1 \Rightarrow \Gamma' \qquad \Gamma' \vdash s_2 \Rightarrow \Gamma''}{\Gamma \vdash s_1; s_2 \Rightarrow \Gamma''}$$

Motivation

Type System 00000000 Soundness Justification

Related Work





Type System 000€00000

Soundness Justification

Related Work





```
fn client() -> ty!{ v: i32 | v == 4 } {
 let mut q = 3;
 let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
 let mut b = &mut a; // b : \{v_2 : \& i32 \mid v_2 == \& a\}
 *b = 0:
          // changes a's value and type
 b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&q\}
 *b = 4:
                      // changes g's value and type
 a
```

```
LIT \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \nu : \{\alpha : b \mid \alpha \simeq \llbracket \nu \rrbracket \Gamma \}}
```

14/27

Type System 00000000 Soundness Justification

Related Work





```
\mathsf{REF} \ \frac{\Gamma \vdash \alpha \ \mathsf{fresh}}{\Gamma \vdash \& x : \{\alpha : \& b \mid \alpha \simeq \llbracket \& x \rrbracket \Gamma \}}
```

Type System 000€00000

Soundness Justification

Related Work





```
fn client() -> ty!{ v: i32 | v == 4 } {
  let mut q = 3;
                                                                                                     \Gamma(z) = \beta
  let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
                                                                      Assign-Strong \frac{\Gamma \vdash x \in \{\&y\}}{\Gamma \vdash *x = z \Rightarrow \Gamma[y \mapsto \gamma], \gamma \doteq \beta}
  let mut b = &mut a; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
             // changes a's value and type
  *b = 0;
  b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&q\}
  *b = 4:
                             // changes g's value and type
                                                                      (Also Assign-Weak)
  а
```

Type System 00000000 Soundness Justification

Related Work





```
fn client() -> ty!{ v: i32 | v == 4 } {
  let mut q = 3;
  let mut a = 2; // a : \{v_1 : i32 \mid v_1 == 2\}
  let mut b = &mut a; // b : \{v_2 : \&i32 \mid v_2 == \&a\}
  *b = 0:
                      // changes a's value and type
  b = &mut q; // b : \{v_2 : \&i32 \mid v_2 == \&q\}
  *b = 4:
                       // changes q's value and type
  a
```

Type System 00000000 Soundness Justification

Related Work





```
\mathsf{VAR} \ \frac{\Gamma \vdash \alpha \ \mathsf{fresh}}{\Gamma \vdash x : \{\alpha : b \mid \alpha \simeq [\![x]\!]\Gamma\}}
```

Type System

Soundness Justification

Related Work





```
fn clamp(a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 }, b: ty!{ b1: i32 }) {</pre>
 if *a > b { *a = b }
fn client() -> ty!{ v: () } {
  . . .
  let max = 42;
  clamp(\&mut x, max);
  x as ty!\{ v : i32 | v < 43 \};
```

Type System 000000000

Soundness Justification

Related Work





```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) {
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},
       v_2 < b_1 \land v_1 \doteq \&arg_0 \land true \land true)
```

16/27

Type System nnooo•000 Soundness Justification

Related Work





```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) {
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \& arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},
       v_2 < b_1 \land v_1 \doteq \&ara_0 \land true \land true)
```

- ty! $\{\alpha : \mathbf{b} \mid \varphi \Rightarrow \beta \mid \psi\}$
- **a** Callee requires φ for reference destination α
- lacktriangle Callee ensures ψ for reference destination β
- Of course, multiple arguments possible

Type System 000000000 Soundness Justification

Related Work





```
fn clamp(
    a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
    b: ty!{ b1: i32 }
) {
    // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\}, \\
    // v_1 \doteq \&arg_0 \land true \land true)
    if *a > b { *a = b }
    // <math>\Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\}, \\
    // v_2 \leq b_1 \land v_1 \doteq \&arg_0 \land true \land true)
}
```

Type System ○○○○○●○○○ Soundness Justification

Related Work





```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
) {
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
      v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

Type System nnooo•000 Soundness Justification

Related Work



```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
          v_2 < b_1 \land v_1 \doteq \&arg_0 \land true \land true
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?

Motivation

Type System

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Related Work



```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},
          v_2 < b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
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- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context



```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true)
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
          v_2 \leq b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state:

$$\Gamma_e = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 \leq b_1)$$

Motivation

Type System

Soundness Justification

Related Work



```
fn clamp(
  a: &mut ty!{ a1 : i32 | true => a2 | a2 <= b1 },
  b: ty!{ b1: i32 }
  // \Gamma_1 = (\{a \mapsto v_1, arg_0 \mapsto a_1, b \mapsto b_1\},\
        v_1 \doteq \&arg_0 \land true \land true
  if *a > b { *a = b }
  // \Gamma_2 = (\{a \mapsto v_1, arg_0 \mapsto v_2, b \mapsto b_1\},\
          v_2 \leq b_1 \wedge v_1 \doteq \&arg_0 \wedge true \wedge true
```

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state:

$$\Gamma_e = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 \leq b_1)$$

• show: $\Gamma_2 \prec \Gamma_2$

Motivation

Type System

Soundness Justification

Related Work



$$\vdash \Phi'[\mu'(x) \rhd \mu(x) \mid x \in \mathsf{dom}(\mu')] \to \Phi \\ \preceq \mathsf{-CTX} \frac{\mathsf{dom}(\mu') \subseteq \mathsf{dom}(\mu)}{(\mu, \Phi) \preceq (\mu', \Phi')}$$

- still left: proof obligation from signature $a_2 \leq b_1$
- i.e. is Γ₂ a valid end-state?
- generalize notion of sub-types to context: sub-context
- expected state: $\Gamma_e = (\{arg_0 \mapsto a_2, b \mapsto b_1\}, a_2 < b_1)$
- show: $\Gamma_2 \prec \Gamma_e$

Motivation

Type System nnooo•000 Soundness Justification

Related Work

Mutable Calls



```
fn client(...) -> ty!{ v: () } {
   . . .
  let m = 42:
  // \Gamma_1 = (\{x \mapsto v_1, m \mapsto v_2\}, \ldots \land v_2 \doteq 42)
  clamp(\&mut x, m);
  // \Gamma_2 = (\{x \mapsto v_3, m \mapsto v_2\}, \ldots \land v_2 \doteq 42 \land v_3 \leq 5)
  x as ty!\{ v : i32 | v < 43 \};
```

- append predicates from callee to context
- update association of logic variables

Motivation

Type System 000000000 Soundness Justification

Related Work

```
lib.rs

    Readme.md

src > 🔞 lib.rs > 🕤 client
         #![allow(dead code)]
         | · let · mut · x : i32 · = · 1337; · let · max : i32 · = · 42;
```

Motivation Type System Soundness Justification Related Work Conclusion / Future Work 00000000

```
let mut x: i32 = 1337; let max: i32 = 42;
```

Motivation Type System Soundness Justification Related Work Conclusion / Future Work 00000000

Type System

Soundness Justification

Related Work





```
; checking is_sub_context ...
(declare-datatypes () ((Unit unit)))
(declare-const |_0| Int)
(declare-const |r| Int)
(declare-const |a1| Int)
(declare-const |b1| Int)
(declare-const |a2| Int)

; ty!{ r : i32 | (r <= b1) }
(assert (<= |r| |b1|))

; ty!{ a1 : &mut i32 | true }
(assert true)

; ty!{ b1 : i32 | true }
(assert true)</pre>
```

```
; SuperCtx:
(assert (not (and
        (<= |r| |b1|)
       true
   )))
; checking: RContext {
      a : ty!{ _0 : \&mut i32 | _0 == \& arg (Ousize) }
     <dangling> : ty!{ a1 : &mut i32 | true }
     b : ty!{ b1 : i32 | true }
     <argument 0> : tv!{ r : i32 | (r <= b1) }</pre>
 <: RContext {
      <argument 0> : ty!{ a2 : &mut i32 | a2 <= b1 }</pre>
     b : ty!{ b1 : i32 | true }
(check-sat)
```

Soundness



Progress

If
$$\Gamma \vdash s_1, \sigma : \Gamma \Rightarrow \Gamma_2$$
 and $s_1 \neq \text{unit}$, then there is a s_2 and σ_2 with $\langle s_1 \mid \sigma_1 \rangle \leadsto \langle s_2 \mid \sigma_2 \rangle$.

Corten strictly refines the base language, therefore progress depends on base type system.

Preservation

If
$$\Gamma \vdash s \Rightarrow \Gamma_2$$
, $\sigma : \Gamma$ and $\langle s \mid \sigma \rangle \leadsto \langle s_1 \mid \sigma_1 \rangle$, then there is a Γ_1 with $\Gamma_1 \vdash s_1 \Rightarrow \Gamma_2$ and $\sigma_2 : \Gamma_2$

Stronger property than base language preservation: Show that refined types are preserved

Partial, Mechanized Proof in Lean 4

Motivation
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State Conformance



State Conformance σ : Γ

A state σ is conformant with respect to a typing context $\Gamma = (\mu, \Phi)$ (written as $\sigma : \Gamma$), iff:

$$\Phi[\mu(x) \triangleright \llbracket \sigma(x) \rrbracket \mid x \in dom(\mu)]$$
 is satisfiable

I.e. a conformant type context does not contradict the execution state.

Examples:

- If $\sigma: (\emptyset, \Phi)$ then Φ is satisfiable
- If $\sigma: (\mu, \Phi_1 \wedge \Phi_2)$ then $\sigma: (\mu, \Phi_1)$ and $\sigma: (\mu, \Phi_1)$.
- If $\sigma: (\mu, \Phi)$ and $\mathsf{FV}(\Phi) \subseteq \mathsf{dom}(\mu)$, then $\models \Phi[\mu(x) \triangleright \llbracket \sigma(x) \rrbracket \mid x \in \mathsf{dom}(\mu)]$

Motivation

Type System

Soundness Justification

Related Work

Intermediate Steps



Conformance of Symbolic Execution

If $\sigma : \Gamma$, $\Gamma \vdash \alpha$ fresh then $\sigma[x \mapsto \llbracket e \rrbracket \sigma] : \Gamma[x \mapsto \alpha], (\alpha \simeq \llbracket e \rrbracket \Gamma)$

where $(\alpha \simeq \llbracket e \rrbracket \Gamma)$ is the symbolic execution of e equated with α in context Γ

Reference Predicates are Conservative

If $\sigma : \Gamma$ and $\Gamma \vdash *x \in \{y_1, \dots, y_n\}$ then $\llbracket \sigma(x) \rrbracket = \& y_i$ for some $i \in 1, \dots, n$

Rare case where conservative typing requires

Sub-Context Relation is Conservative

If $\Gamma \prec \Gamma'$ and $\sigma : \Gamma$ then $\sigma : \Gamma'$

Motivation

Type System

Soundness Justification

Related Work

Related Work



Refinement Types and Mutability

- Rondon et al. [RKJ10], Bakst and Jhala [BJ16]: Refinement Types for C subset. Lack of guarantees requires ad-hoc mechanisms to control aliasing
- Lanzinger [Lan21]: Property Types in Java (only immutable). Bachmeier [Bac22]: Extension using Ownership System
- Toman et al. [Tom+20] (ConSORT): Fractional Ownership, strong and weak updates

Rust verification

- Ullrich [Ull16]: Translation to Lean; linear mutation chain. Denis et al [DJM21] similar, but to Why3
- Astrauskas et al. [Ast+19] (Prusti): heavy-weight verification, translation to separation logic (Viper)
- Matsushita et al. [MTK20] (RustHorn): constrained Horn clauses

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Related Work: Flux - Refinement Types for Rust



- MIR vs. HIR
- specification in comments vs. embedding in types
- context inclusions vs. sub context
- distinction strong and weak references vs. dynamic choice by typ checking rules
- explicit introduction of logic variables vs. ad-hoc
- formalization based on RustBelt vs. formalization based on own language
- missing in Corten: records & inference
- otherwise: similar capabilities

```
// Flux
//@ ensures *self: i32<n+1>:
fn increment(&strg v : i32<n>) -> ()
//@ requires n > 0
//@ ensures *self: i32<n-1>:
fn decrement(&strg v : i32<n>) -> ()
// Corten
fn increment(n: &mut ty!{
  n1: Nat => n1 \mid n1 == n1+1 \}
) -> ();
fn decrement(n: &mut ty!{
  v1: Nat | v1 > 0 => v2 | v2 == v1-1 
) -> ();
```

Future Work



- Records & ADTs
 - More Syntax, Nested Structures
 - Variant Distinction
- Predicate Generics (Abstract Predicates)
 - Uninterpreted Functions in Types
 - Syntactic Embedding?
- Concurrency using Predicate Generics?
 - Use Predicate Generics
 - Predicate describes Contract for Mutation
 - Interesting, because unusual guarantees in Rust

Conclusion



- Refinement Type System for Rust with Mutability
 - Decidable, Automatic
 - Complex Mutation Patterns
- Minimal Interface
- Soundness Justification
- Practical Usability
 - Source Locations
 - Counter Example
 - IDE Integration

Conclusion



- Refinement Type System for Rust with Mutability
 - Decidable, Automatic
 - Complex Mutation Patterns
 - ..
- Minimal Interface
- Soundness Justification
- Practical Usability
 - Source Locations
 - Counter Example
 - IDE Integration

More Information:

Implementation, Thesis, Mechanized Proof, Evaluation:

https://gitlab.com/csicar/liquidrust

Empirical Analysis:

https://gitlab.com/csicar/crates-analysis

7/27 26. 10. 2022	Carsten Csiky: Rust &	Refinement Types	Department of Informatics – Institute of Information Security and Dependability (KASTEL	
Motivation	Type System			

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- [2] Joshua Bachmeier. Property Types for Mutable Data Structures in Java. 2022. DOI: 10.5445/IR/1000150318. URL: https://publikationen.bibliothek.kit.edu/1000150318 (besucht am 03. 10. 2022).
- [3] Alexander Bakst und Ranjit Jhala. "Predicate Abstraction for Linked Data Structures". In: Verification. Model Checking, and Abstract Interpretation. Hrsg. von Barbara Jobstmann und K. Rustan M. Leino. Lecture Notes in Computer Science, Berlin, Heidelberg: Springer, 2016, S. 65–84, ISBN: 978-3-662-49122-5, DOI: 10.1007/978-3-662-49122-5 3.

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Literatur II



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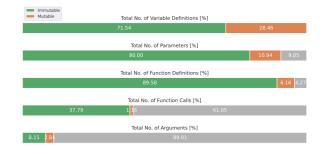
Empirical Analysis

Zweiter Abschnitt

Empirical Use-Case Analysis



- public open-source code (crates.io)
- about 64 million lines of Rust code
- syntactical analysis



Empirical Analysis

Zweiter Abschnitt

decr Typing Tree



$$\text{let } \Gamma_2 = \Gamma[i \mapsto v_1], v > 0 \text{ and } \tau = \{v : \text{i32} \mid v > 0\}$$

$$= \frac{\Gamma[i \mapsto v_1], v > 0 \text{ and } \tau = \{v : \text{i32} \mid v > 0\} }{\Gamma_1 \vdash \dots : \tau' \qquad \Gamma_1 \vdash \tau' \preceq \tau}$$

$$\text{Ass } \frac{\Gamma_1 \vdash v_2 \text{ fresh}}{\Gamma_1 \vdash \text{i} = 1 : \{v_2 : \text{i32} \mid v_2 \doteq v - 1\}}$$

$$\frac{\Gamma_1 \vdash \text{let } \text{i} = \dots \text{ as } \tau \Rightarrow \Gamma_2}{\Gamma_1 \vdash \text{let } \text{i} = \dots \text{ as } \tau; \text{ i} = \text{i} - 1 \Rightarrow \Gamma[i \mapsto v_2], v > 0, v_2 \doteq v - 1}$$

Empirical Analysis

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Expression Typing $\Gamma \vdash e : \tau$

$$\begin{array}{c|c} \Gamma \vdash \alpha \text{ fresh} & \Gamma \vdash \alpha \text{ fresh} \\ \hline \Gamma \vdash \nu : \{\alpha : b \mid \alpha \simeq \llbracket \nu \rrbracket \Gamma \} & \text{BINOP} & \overline{\Gamma \vdash x_1 \odot x_2 : \{\alpha : b \mid \alpha \simeq \llbracket x_1 \odot x_2 \rrbracket \Gamma \}} \\ \hline \text{VAR} & \overline{\Gamma \vdash \alpha \text{ fresh}} & \text{INTRO-SUB} & \overline{\Gamma \vdash e : \tau \quad \Gamma \vdash \tau \preceq \tau'} \\ \hline \Gamma \vdash e \text{ as } \tau' : \tau' & \overline{\Gamma} \vdash e \text{ as } \tau' : \tau' \\ \hline \end{array}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

Empirical Analysis

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Expression Typing $\Gamma \vdash e : \tau$

$$\begin{aligned} & \text{Ref } \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \&x : \{\alpha : \&b \mid \alpha \simeq [\![\&x]\!]\Gamma\}} \\ & \text{Var-Deref } \frac{\Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash y : \tau}{\Gamma \vdash *x : \tau} \end{aligned}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

Assign-Strong
$$\frac{\Gamma(z) = \beta \qquad \Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash \gamma \text{ fresh}}{\Gamma \vdash *x = z \Rightarrow \Gamma[y \mapsto \gamma], \gamma \doteq \beta}$$

Empirical Analysis

Zweiter Abschnitt

Expression Typing $\Gamma \vdash e : \tau$

$$\begin{aligned} & \text{Ref } \frac{\Gamma \vdash \alpha \text{ fresh}}{\Gamma \vdash \&x : \{\alpha : \&b \mid \alpha \simeq [\![\&x]\!]\Gamma\}} \\ & \text{Var-Deref } \frac{\Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash y : \tau}{\Gamma \vdash *x : \tau} \end{aligned}$$

Statement Type Checking $\Gamma \vdash s \Rightarrow \Gamma'$

ASSIGN-STRONG
$$\frac{\Gamma(z) = \beta \qquad \Gamma \vdash x \in \{\&y\} \qquad \Gamma \vdash \gamma \text{ fresh}}{\Gamma \vdash *x = z \Rightarrow \Gamma[y \mapsto \gamma], \gamma \doteq \beta}$$

$$\frac{\Gamma \vdash e : \tau \qquad \Gamma \vdash x \in \{\&y_1, \dots, \&y_n\}}{\Gamma \vdash y_i : \{\beta_i : b_i \mid \varphi_i\}} \qquad \overline{\Gamma \vdash \tau \preceq \{\beta_i : b_i \mid \varphi_i\}}$$

$$\Gamma \vdash *x = e \Rightarrow \Gamma$$

Zweiter Abschnitt 000





```
struct Mutex<P, T> = ...;
impl Mutex<P, T> {
  fn lock() -> MutexLock<P, T> {
struct MutexLock<P, T> = ...;
impl MutexLock<P, T> {
  fn drop(self : ty!{ v : T | P v }) {
    . . .
```

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Blöcke in den KIT-Farben



Greenblock

Standard (block)

Blueblock

= exampleblock

Redblock

= alertblock

Brownblock

Purpleblock

Cyanblock

Yellowblock

Lightgreenblock

Orangeblock

Grayblock

Contentblock

(farblos)

Empirical Analysis

Zweiter Abschnitt

Auflistungen



Text

- Auflistung Umbruch
- Auflistung
 - Auflistung
 - Auflistung

Bei Frames ohne Titel wird die Kopfzeile nicht angezeigt, und der freie Platz kann für Inhalte genutzt werden.

Empirical Analysis

OOOOOO

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OOO

Farben

88/27 26.10.2022 Carsten Csiky: Rust & Refinement Types

Department of Informatics – Institute of Information Security and Dependability (KASTEL) Bei Frames mit Option [plain] werden weder Kopf- noch Fußzeile angezeigt.

Beispielinhalt



Bei Frames mit Option [t] werden die Inhalte nicht vertikal zentriert, sondern an der Oberkante begonnen.

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Beispielinhalt: Literatur



Empirical Analysis

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Farbpalette





Empirical Analysis

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