Mozzie: a computationally efficient simulator for the spatio-temporal modelling of mosquitoes

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Summary

Mozzie enables simulation of the lifecycle and spatial spread of mosquitoes. Mozzie can be used to assess risks associated with disease-control strategies at local, regional or continental scales. Most particularly, strategies involving genetic alterations of mosquitoes to eliminate malaria, are of prime interest.

More technically, Mozzie simulates a population-dynamics model that uses differential equations or delay differential equations (Bohner et al., 2018; El-Hachem & Beeton, 2024) to describe the spread and persistence of mosquitoes that may be genetically altered. Genetic alterations are flexibly modelled: these can involve any number of alleles; Mendelian or non-Mendelian inheritance, including gene drives; they can be self-limiting or self-sustaining; and can include the emergence of resistant allelles. The model allows simulation of N mosquito species. It incorporates mate-choice, hybridisation and intra-specific competition that occur within complexes of mosquito species (Beeton et al., 2020). This fills a gap that currently exists among similar models, allowing researchers to assess potential transfer of the genetic alterations between (sub-)species.

Mozzie supports spatial and temporal variations in lifecyle parameters, and local diffusion and wind-assisted, long range, advection. For example, wind patterns and the capacity of the landscape to support mosquitoes can vary spatially and temporally, reflecting daily variations, seasonality, and local conditions.

Conversely, Mozzie does not contain human agents, nor does it consider the effect of genetic control strategies on the prevalence of pathogens such as the malaria parasite, among human or animal populations.

Mozzie has been used by the authors to simulate the spread across sub-Saharan Africa of a theoretical, population-modifying, gene drive in *Anopheles gambiae s.s.* and *Anopheles coluzzii* (Beeton et al., 2022) (that paper also describes the mathematics of a particular mosquito lifecycle model that is contained in Mozzie). It has also been used to predict the spread of Target Malaria's Paternal Male Bias construct (Galizi et al., 2014) following a proposed field-release of

genetically modified *Anopheles coluzzi* male mosquitoes in Burkina Faso (Hosack et al., 2023).

State of the field

Alternatives to Mozzie include:

- MIT's HYDREMATS software (Bomblies et al., 2009). HYDREMATS
 is a coupled hydrology and entomology model that uses an agent-based
 approach for mosquito-human dynamics, and focuses on high-resolution
 village-scale understanding of malaria without genetically-modified
 mosquitoes.
- The well-established SkeeterBuster focuses on the *Aedes aegypti* species in order to understand insecticidal control measures such as spraying (Gunning et al., 2022; Magori et al., 2009). A stochastic, mechanistic approach is employed.
- OpenMalaria (T. Smith et al., 2006) is an open-source C++ program enabling simulation of malaria epidemiology, typically at the village scale, in order to assess the efficacy of non-genetic malaria interventions.
- IDM's EMOD software can simulate malaria epidemiology using an agent-based approach, with spatial structure based on a network (Bershteyn et al., 2018). Less emphasis is spent on genetic modifications, and a single mosquito species is the focus.
- The dynamAedes R package can be used to study the spatio-temporal evolution of a single mosquito species, with particular attention paid to the impact of temperature heterogeneity.
- The exDE R package solves models of mosquito-borne pathogen dynamics and control (Wu et al., 2023). Attention is payed to sophisticated representations of mosquito lifecycles, including exogenous forcing by weather and vector control, as well as mosquito-malaria-human interactions. Although a single mosquito species is the focus, the framework allows for multiple species. The code centers on traditional vector controls, rather than genetic controls.
- Berkeley's MGDrivE is an open-source framework to study gene-drives in mosquito populations (Mondal et al., 2024; Sánchez C. et al., 2019), which is written in R. With regards to lifecycle dynamics, MGDrivE has similar functionality to Mozzie, although MGDrivE focuses on single species, in contrast to Mozzie where transfer of genetic constructs between (sub-)species is of interest. MGDrivE's spatial structure is based on a network, where each node in the network could be thought of as a household, house block, or even a city. In terms of functionality, MGDrivE is the most similar to Mozzie, although the numerical methods employed are quite different.

In addition to these publicly-available codes, many academic articles consider the lifecycle and spatial spread of mosquitoes, for example (Bruzzone & Utgés, 2022; Dufourd & Dumont, 2013; Dye & Cain, 2024; Endo & Eltahir, 2018; Fang et al., 2020; Fernández-Carrión et al., 2018; Lutambi et al., 2013; North et al., 2013; Roques & Bonnefon, 2016; Silva et al., 2020; N. R. Smith et al., 2018; Yamashita, Takahashi, et al., 2018; Yamashita, Das, et al., 2018), but few have published their code. Most appear to rely on unpublished scripts in codes such as MATLAB (Fernández-Carrión et al., 2018; Lutambi et al., 2013; Yamashita, Das, et al., 2018), or concentrate on specialised scenarios (Bruzzone & Utgés, 2022; Roques & Bonnefon, 2016).

If spatially explicit, the aforementioned codes model spatial structure using a network. In contrast, Mozzie uses a continuous-space (diffusion-advection equation) approach, deliberately incorporating long-range dispersal in a way that is ecologically interpretable (Hosack et al., 2023). In addition, Mozzie does not focus on single species, but concentrates on the interaction of multiple (sub-)species. Many of the aforementioned alternatives contain human agents and the malaria parasite, which Mozzie does not.

Statement of need

Mozzie is designed to solve problems involving:

- interacting (sub-)species of mosquitoes, with
- complicated lifecycle dynamics including transfers of genetic modifications between the (sub-)species, in
- spatially-extensive settings (such as continental scales) including the spatio-temporal dispersal of individuals (such as advection via wind).

It is anticipated that users of Mozzie will be researchers interested in such aspects.

Importantly, the numerical implementation of Mozzie is:

- ecologically interpretable (Hosack et al., 2023),
- computationally and I/O efficient, and
- well tested.

This allows rapid simulation at continental scales to investigate sensitivity to input parameters, as required in risk assessments. It is written in Cython (Behnel et al., 2011) (a mixture of Python and C), and simulations are run using Python. The test coverage of the Mozzie codebase is over 99%, meaning it is also suitable for risk assessments that could be subject to considerable scrutiny.

Demonstration

Figure 1 shows results from a Mozzie simulation using 2 interbreeding, hybridising and competing mosquito species (Beeton et al., 2022). A water body runs through the domain, effectively separating it into two parts. Mosquitoes can

only traverse the water body via wind advection. A gene-drive is introduced into one species, and the modified individuals are released at the center of the domain. These modified individuals breed with wild mosquitoes, spreading the gene-drive. Over time, resistance forms and the genetic modification becomes ineffective in some individuals. The wind blows in predominantly north-east or south-west directions, depending on the season, and it is assumed that a certain proportion of mosquitoes advect for 2 hours each night, which explains the clusters of rapid invasion shown in Figure 1. The code is found in the demo directory of the repository.

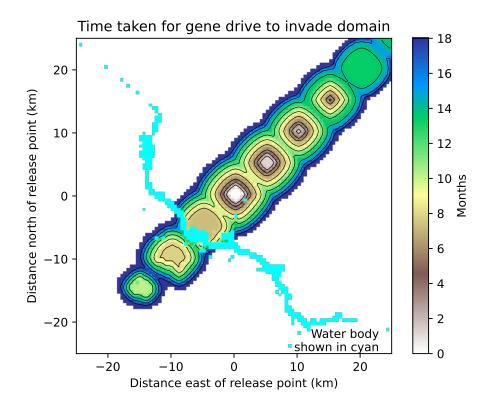


Figure 1: The time taken for genetically-modified mosquito species to invade regions of the domain, after being released from the central point. The water body is shown in cyan.

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