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004 Supplementary Material to “External Prior Guided Internal Prior Learning for
 005 **Real Noisy Image Denoising”**

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 015 In this supplementary material, we provide:
 016 1. The closed-form solution of the sparse coding problem (6) in the main paper.
 017 2. More denoising results on the real noisy images (with no “ground truth”) provided in the dataset [1].
 018 3. More denoising results on the 15 cropped real noisy images (with “ground truth”) used in the dataset [2].
 019 4. More denoising results on the 60 cropped real noisy images (with “ground truth”) from [2].

020 **1. Closed-Form Solution of the Weighted Sparse Coding Problem (6)**
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 022 For notation simplicity, we ignore the indices n, m, t in the problem (6) in the main paper. And it turns into the following
 023 weighted sparse coding problem:
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$$\min_{\alpha} \|\mathbf{y} - \mathbf{D}\alpha\|_2^2 + \sum_{j=1}^{3p^2} \lambda_j |\alpha_j|. \quad (1)$$

025 Since \mathbf{D} is an orthogonal matrix, problem (1) is equivalent to
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$$\min_{\alpha} \|\mathbf{D}^T \mathbf{y} - \alpha\|_2^2 + \sum_{j=1}^{3p^2} \lambda_j |\alpha_j|. \quad (2)$$

028 For simplicity, we denote $\mathbf{z} = \mathbf{D}^T \mathbf{y}$. Here we have $\lambda_j > 0, j = 1, \dots, 3p^2$, then problem (2) can be written as
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$$\min_{\alpha} \sum_{j=1}^{3p^2} ((\mathbf{z}_j - \alpha_j)^2 + \lambda_j |\alpha_j|). \quad (3)$$

032 The problem (3) is separable w.r.t. each α_j and hence can be simplified to $3p^2$ independent scalar minimization problems
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$$\min_{\alpha_j} (\mathbf{z}_j - \alpha_j)^2 + \lambda_j |\alpha_j|, \quad (4)$$

035 where $j = 1, \dots, 3p^2$. Taking derivative of α_j in problem (4) and setting the derivative to be zero. There are two cases for the
 036 solution.
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038 (a) If $\alpha_j \geq 0$, we have
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$$2(\alpha_j - \mathbf{z}_j) + \lambda_j = 0. \quad (5)$$

040 The solution is
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$$\hat{\alpha}_j = \mathbf{z}_j - \frac{\lambda_j}{2} \geq 0. \quad (6)$$

042 So $\mathbf{z}_j \geq \frac{\lambda_j}{2} > 0$, and the solution $\hat{\alpha}_j$ can be written as
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$$\hat{\alpha}_j = \text{sgn}(\mathbf{z}_j) * (|\mathbf{z}_j| - \frac{\lambda_j}{2}), \quad (7)$$

044 where $\text{sgn}(\bullet)$ is the sign function.
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046 (b) If $\alpha_j < 0$, we have
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$$2(\alpha_j - \mathbf{z}_j) - \lambda_j = 0. \quad (8)$$

048 The solution is
 049

$$\hat{\alpha}_j = \mathbf{z}_j + \frac{\lambda_j}{2} < 0. \quad (9)$$

108 So $\mathbf{z}_j < -\frac{\lambda_j}{2} < 0$, and the solution $\hat{\alpha}_j$ can be written as
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$$\hat{\alpha}_j = \text{sgn}(\mathbf{z}_j) * (-\mathbf{z}_j - \frac{\lambda_j}{2}) = \text{sgn}(\mathbf{z}_j) * (|\mathbf{z}_j| - \frac{\lambda_j}{2}). \quad (10)$$

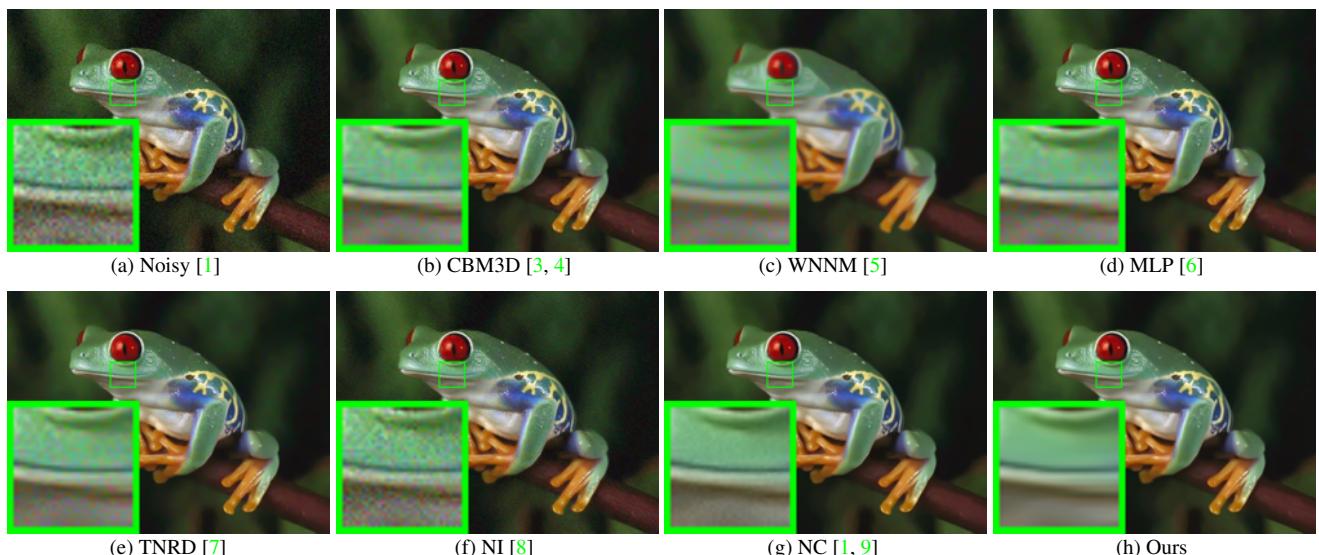
110 In summary, we have the final solution of the weighted sparse coding problem (1) as
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$$\hat{\alpha} = \text{sgn}(\mathbf{D}^T \mathbf{y}) \odot \max(|\mathbf{D}^T \mathbf{y}| - \boldsymbol{\lambda}, 0), \quad (11)$$

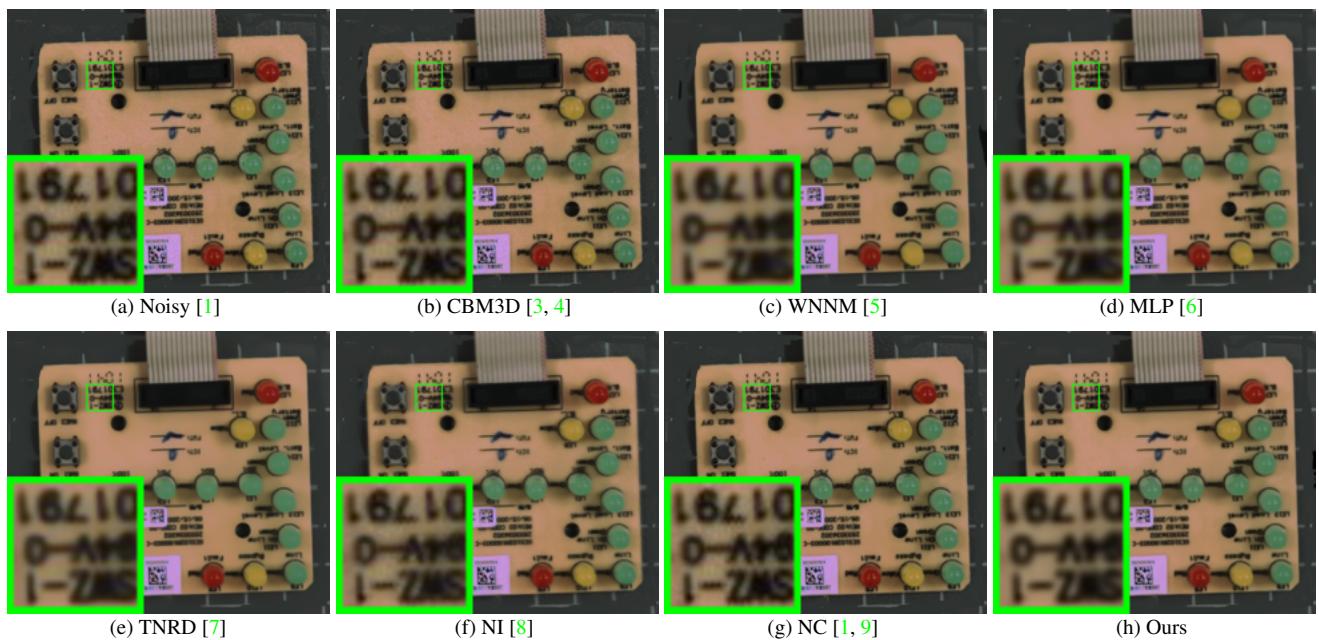
112 where $\boldsymbol{\lambda} = \frac{1}{2}[\lambda_1, \lambda_2, \dots, \lambda_{3p^2}]^\top$ is the vector of regularization parameter and \odot means element-wise multiplication.
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114 2. More Results on Real Noisy Images in [1]

115 In this section, we give more comparisons of the competing methods on the dataset [1]. The real noisy images in dataset
 116 [1] have no “ground truth” images and hence we only compare the visual quality of the denoised images by different methods.
 117 One can seen from Figures 1-4 that, our proposed method perfomrs better than the state-of-the-art denoising methods.
 118



119 Figure 1. Denoised images of the real noisy image “Frog” [1] by different methods. The images are better to be zoomed in on screen.
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121 Figure 2. Denoised images of the real noisy image “Circuit” [1] by different methods. The images are better to be zoomed in on screen.
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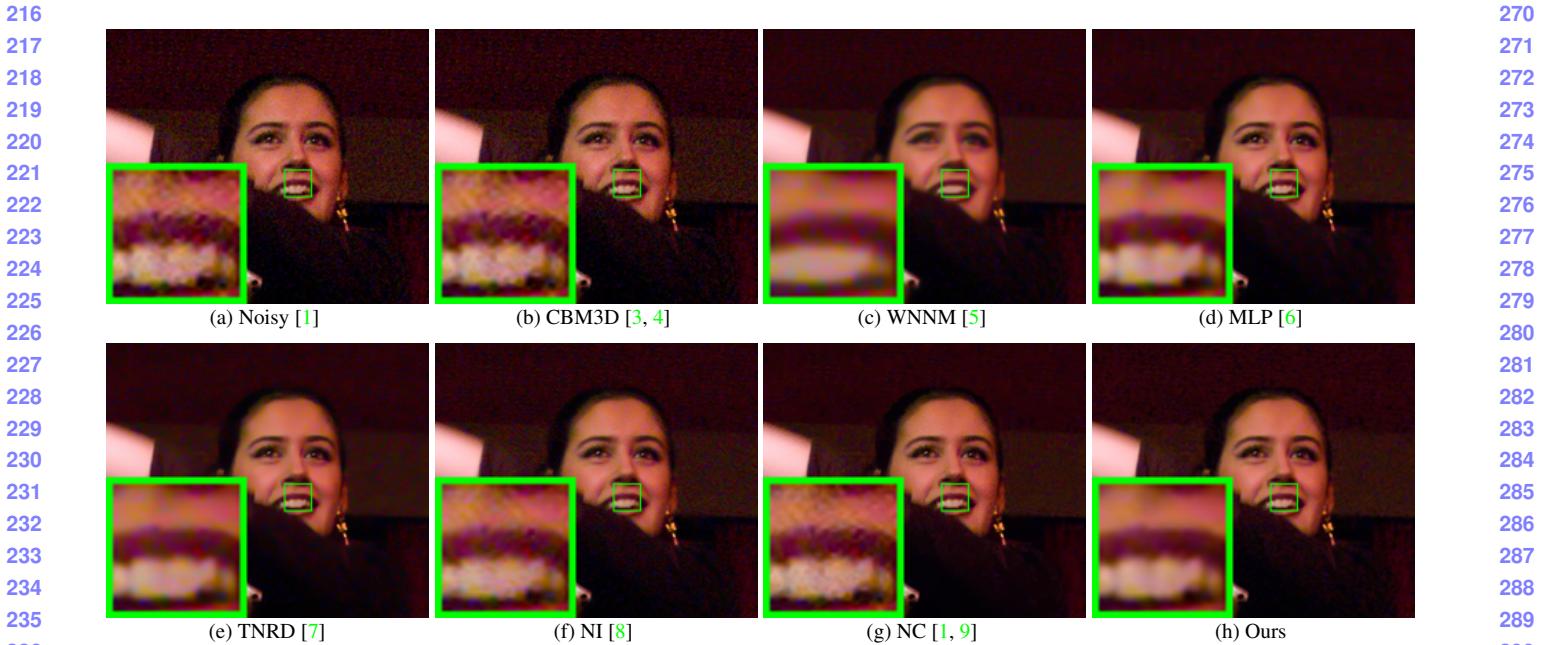


Figure 3. Denoised images of the real noisy image “Woman” [1] by different methods. The images are better to be zoomed in on screen.

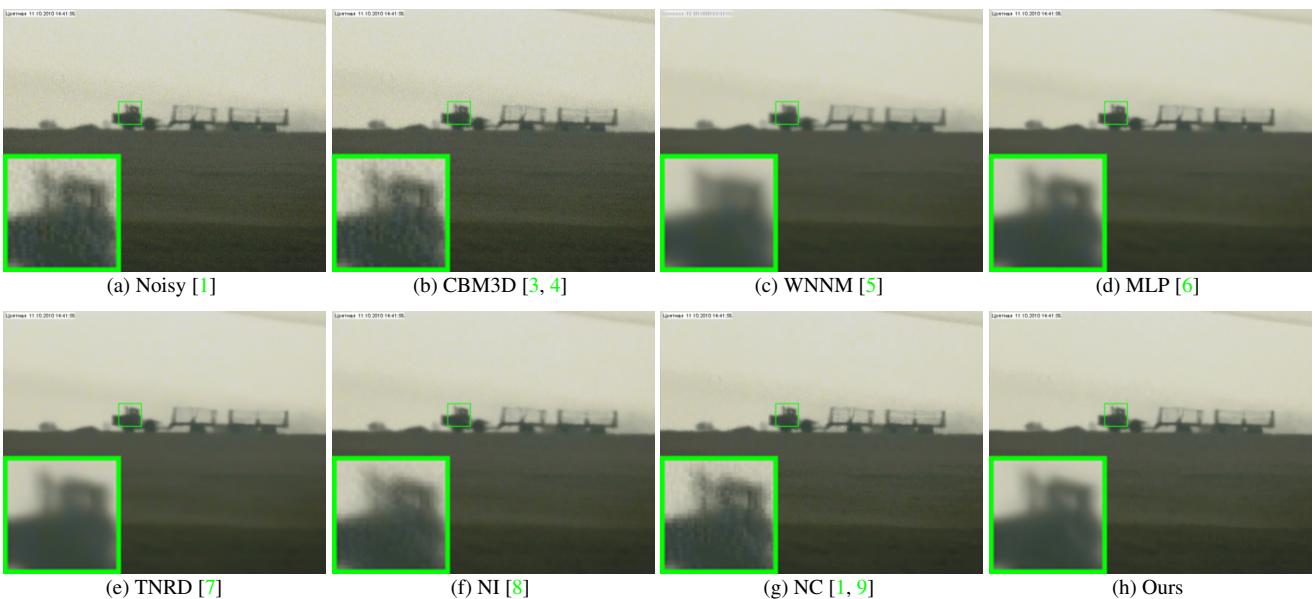


Figure 4. Denoised images of the real noisy image “Vehicle” [1] by different methods. The images are better to be zoomed in on screen.

3. More Results on the 15 Cropped Images Used in [2]

In this section, we provide more visual comparisons of the proposed method with the state-of-the-art denoising methods on the 15 cropped real noisy images used in [2]. As can be seen from Figures 5-9, on most cases, our proposed method achieves better performance than the competing methods. This validates the effectiveness of our proposed external prior guided internal prior learning framework for real noisy image denoising.

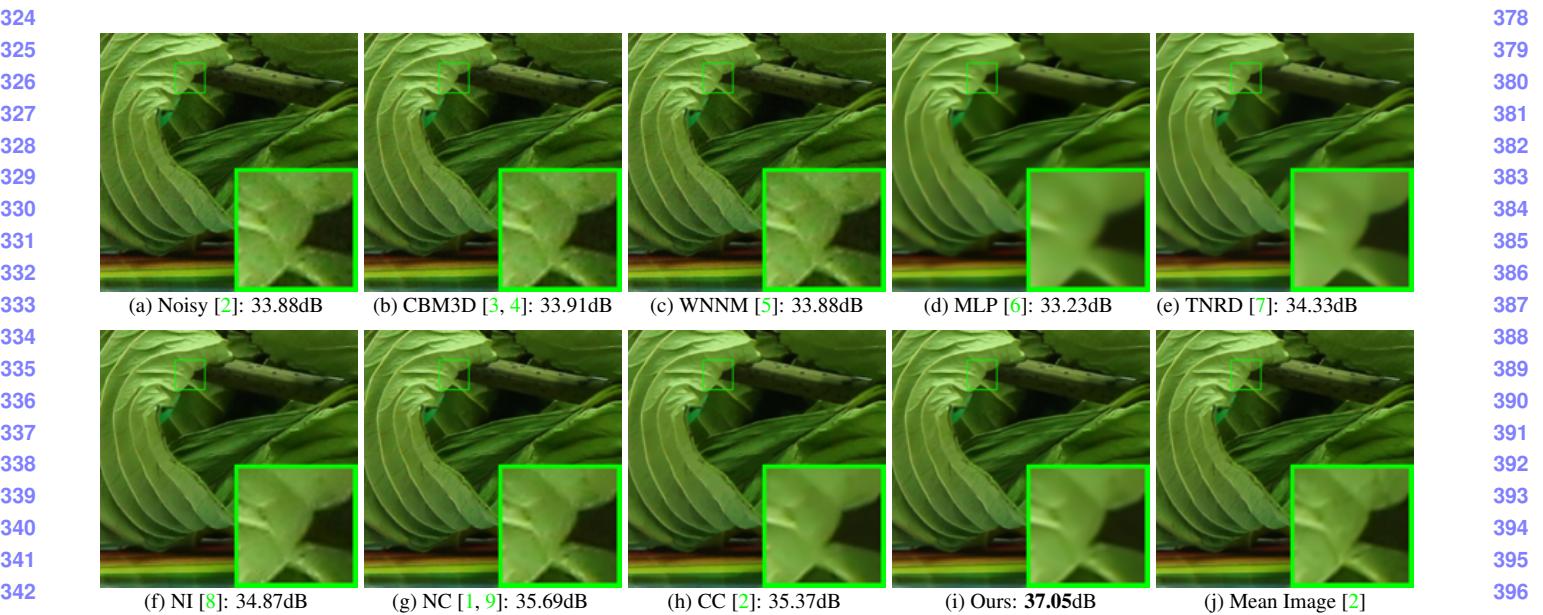


Figure 5. Denoised images of a region cropped from the real noisy image “Canon 5D Mark 3 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

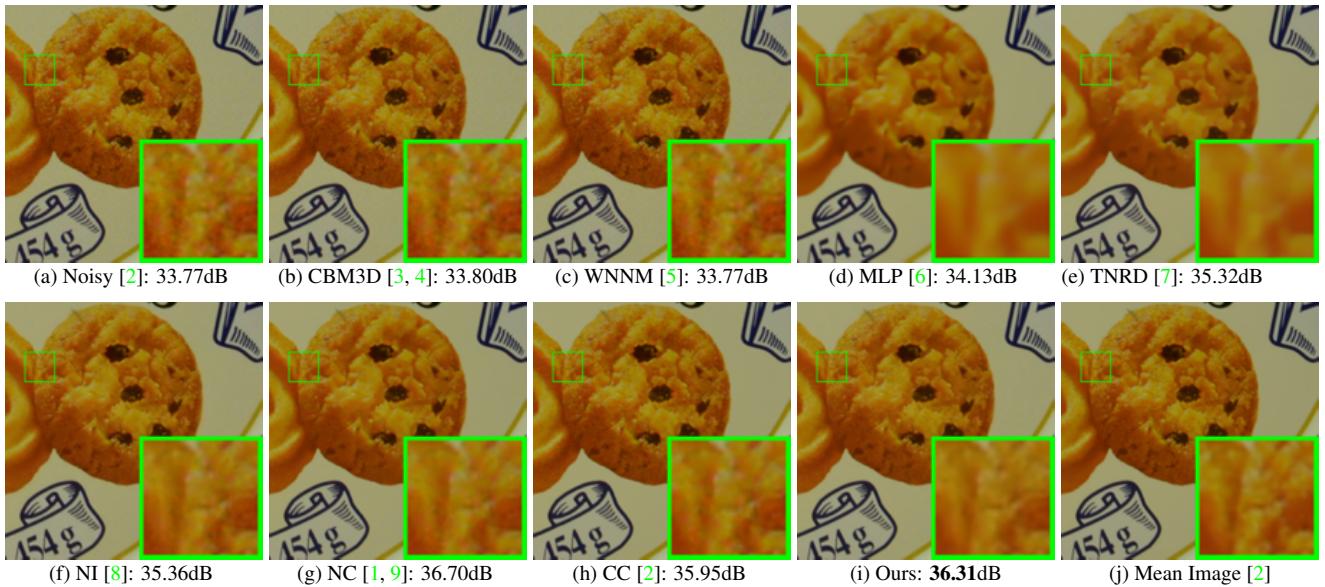


Figure 6. Denoised images of a region cropped from the real noisy image “Canon 5D Mark 3 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

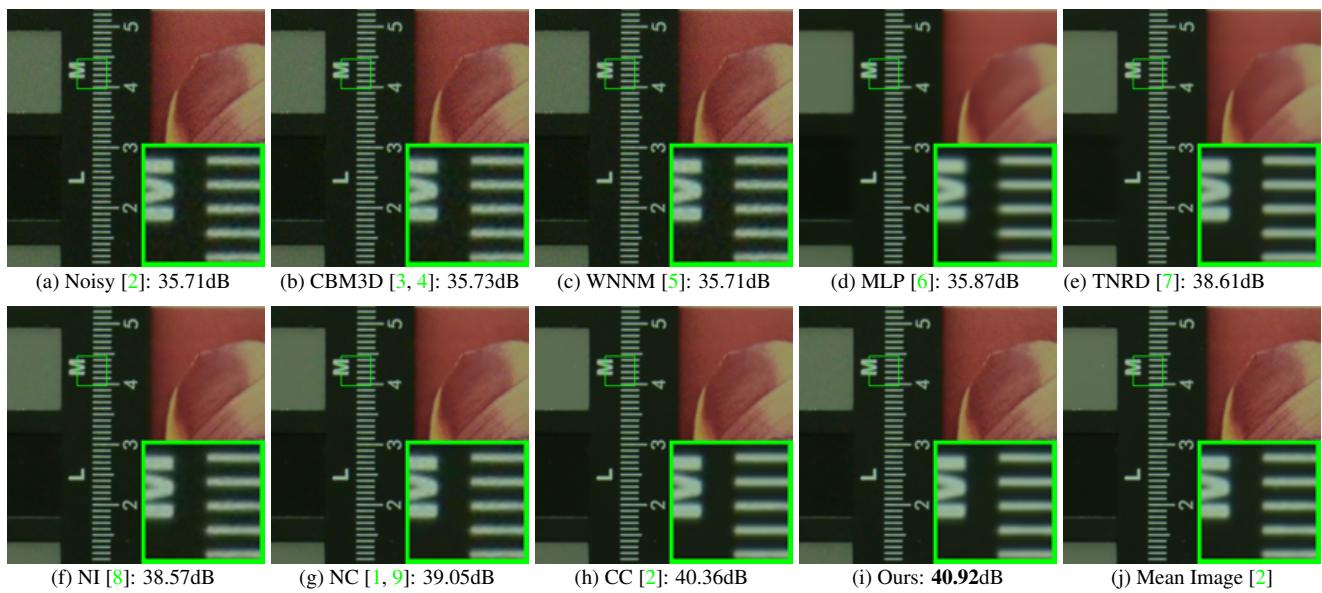


Figure 7. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 1600 2” [2] by different methods. The images are better to be zoomed in on screen.

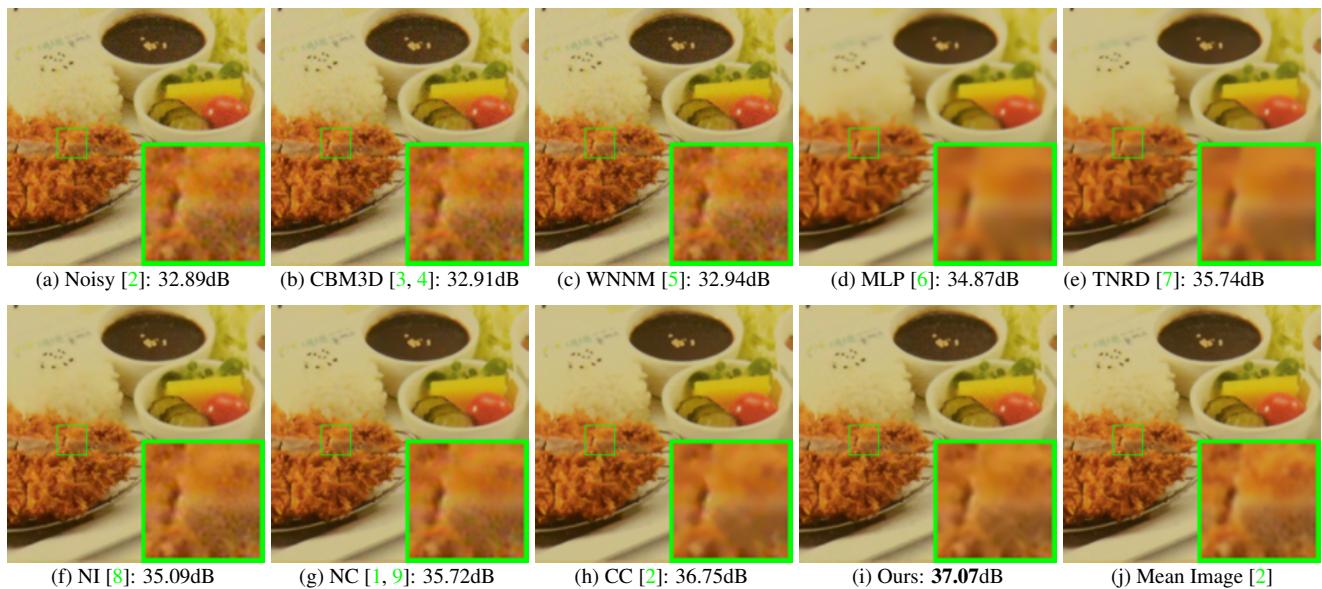


Figure 8. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

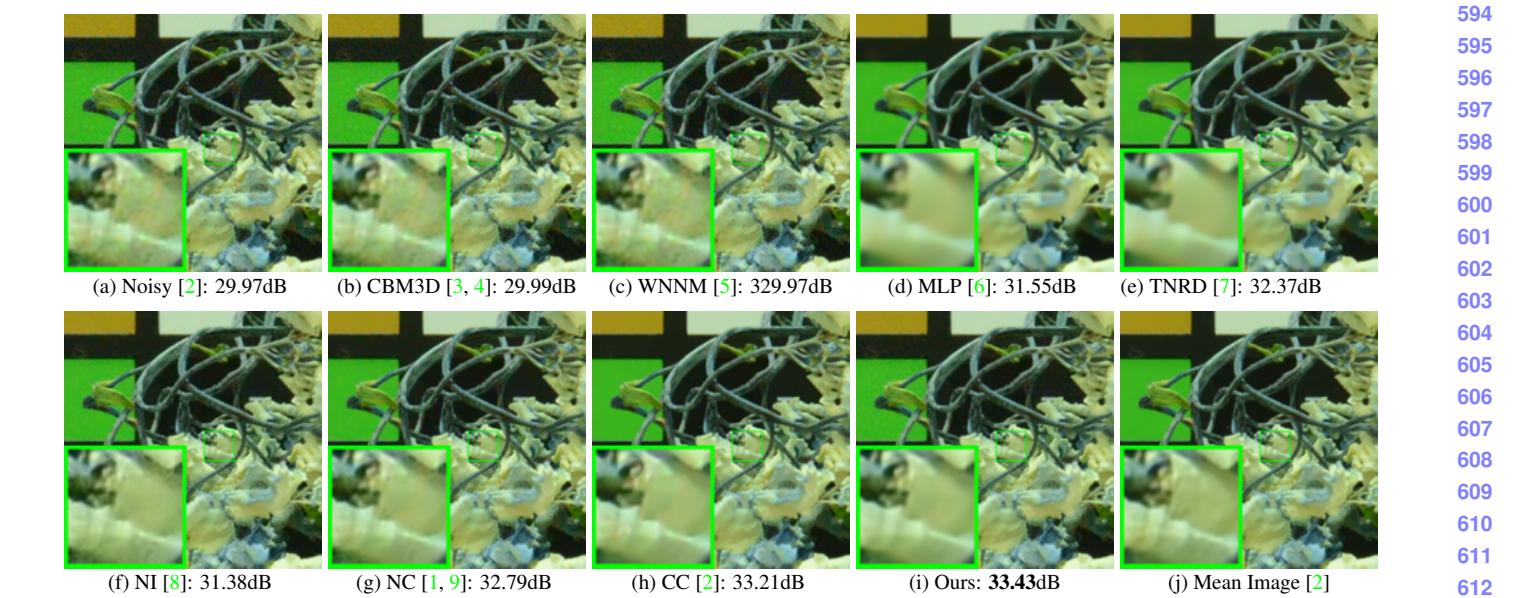


Figure 9. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 6400 2” [2] by different methods. The images are better to be zoomed in on screen.

4. More Results on the 60 Cropped Images in [2]

In this section, we provide more visual comparisons of the proposed method with the state-of-the-art denoising methods on the 60 cropped real noisy images we cropped from [2]. As can be seen from Figures 10-20, on most cases, our proposed method achieves better performance than the competing methods. This validates the effectiveness of our proposed external prior guided internal prior learning framework for real noisy image denoising.

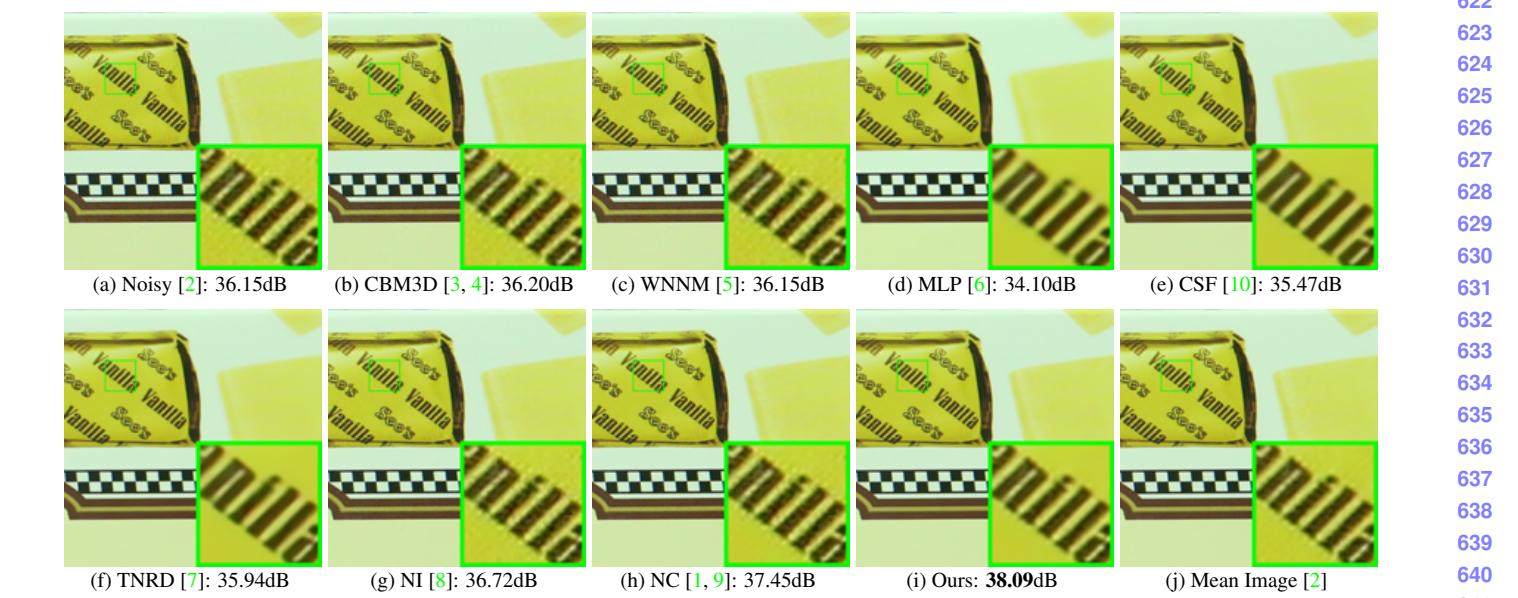


Figure 10. Denoised images of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C1” [2] by different methods. The images are better viewed by zooming in on screen.

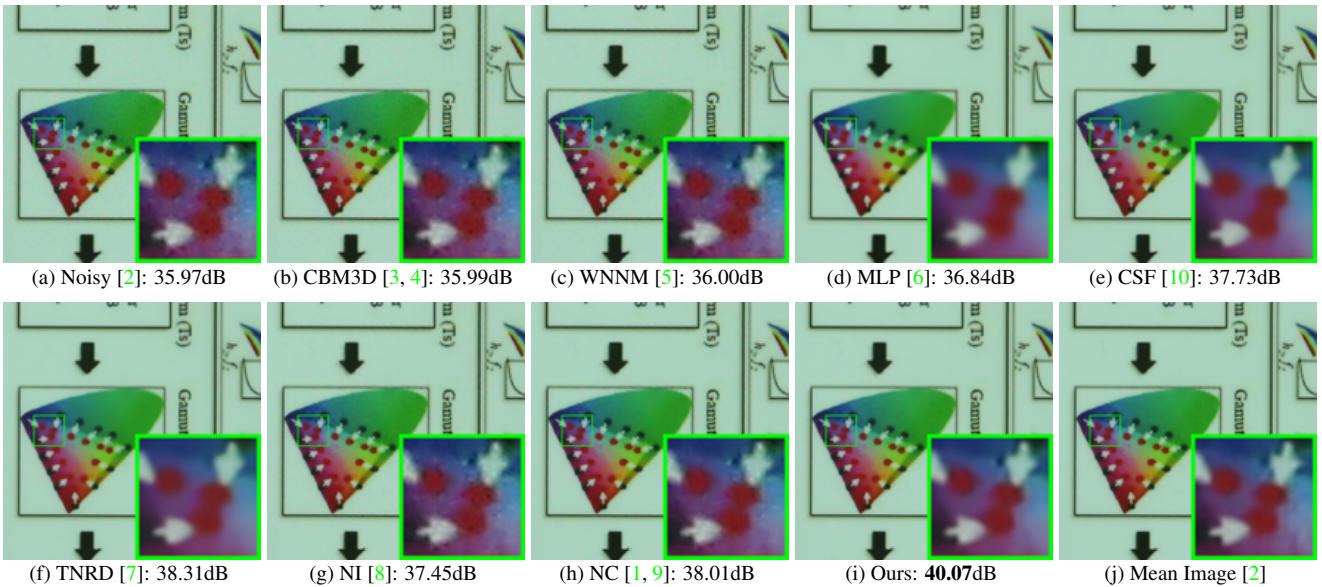


Figure 11. Denoised imagesupp of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C2” [2] by different methods. The images are better viewed by zooming in on screen.

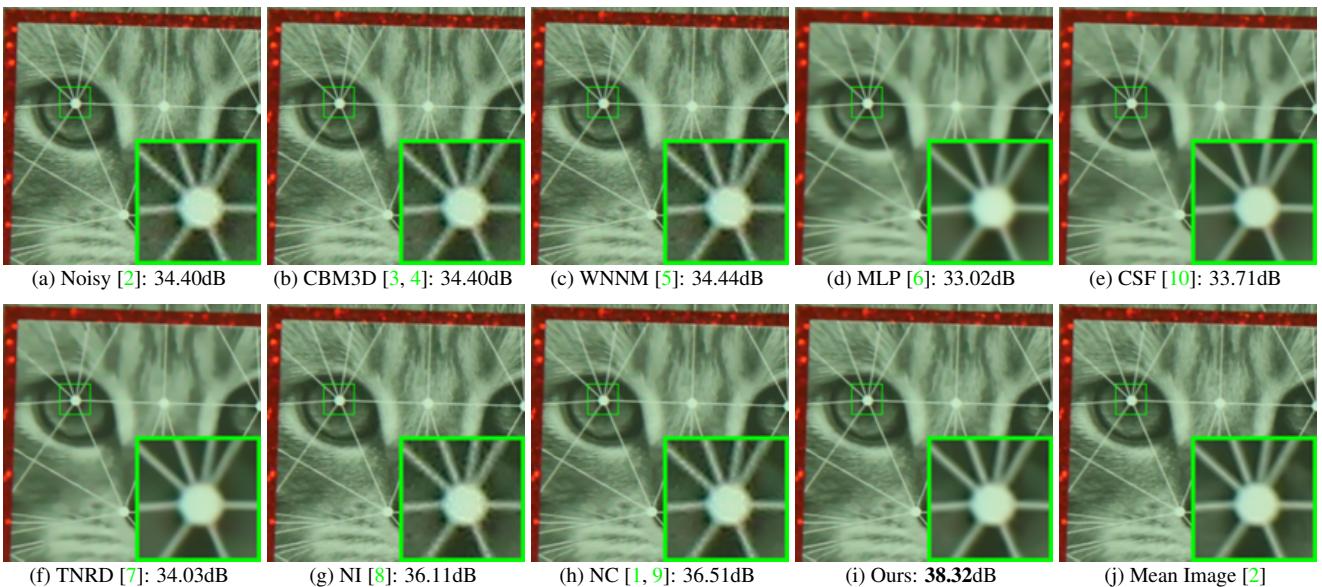


Figure 12. Denoised imagesupp of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C3” [2] by different methods. The images are better viewed by zooming in on screen.



Figure 13. Denoised imagesupp of a region cropped from the real noisy image “Nikon D600 ISO 3200 C1” [2] by different methods. The images are better viewed by zooming in on screen.

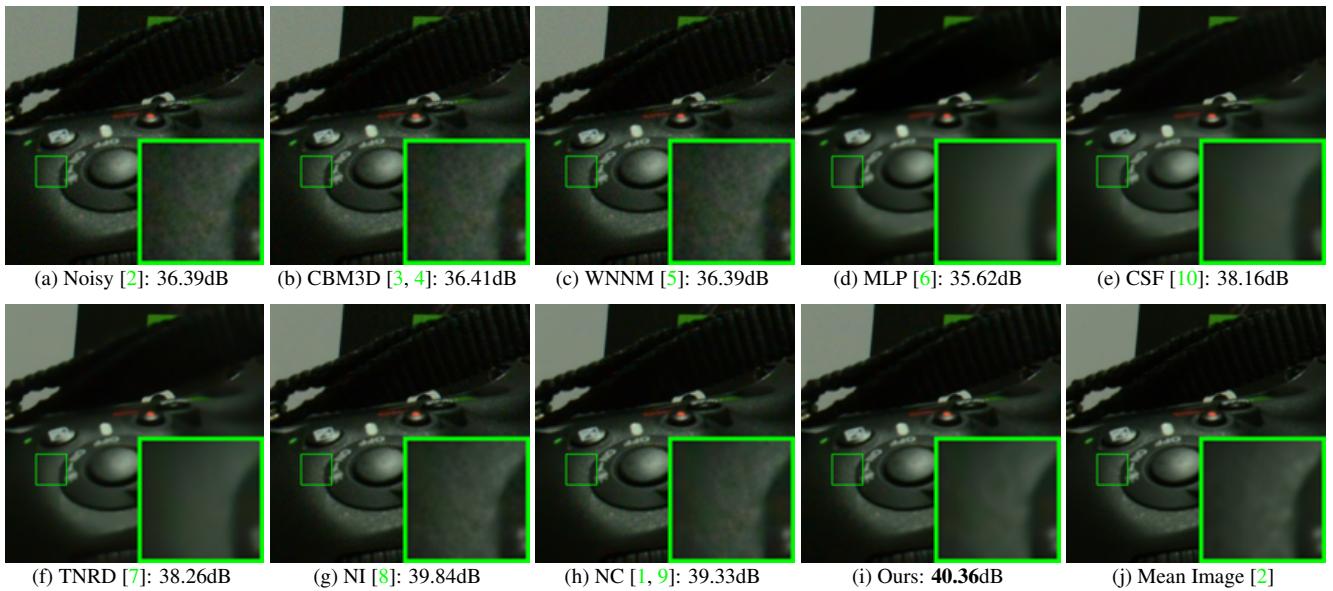


Figure 14. Denoised imagesupp of a region cropped from the real noisy image “Nikon D600 ISO 3200 C2” [2] by different methods. The images are better viewed by zooming in on screen.



Figure 15. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 1600 B2” [2] by different methods. The images are better viewed by zooming in on screen.

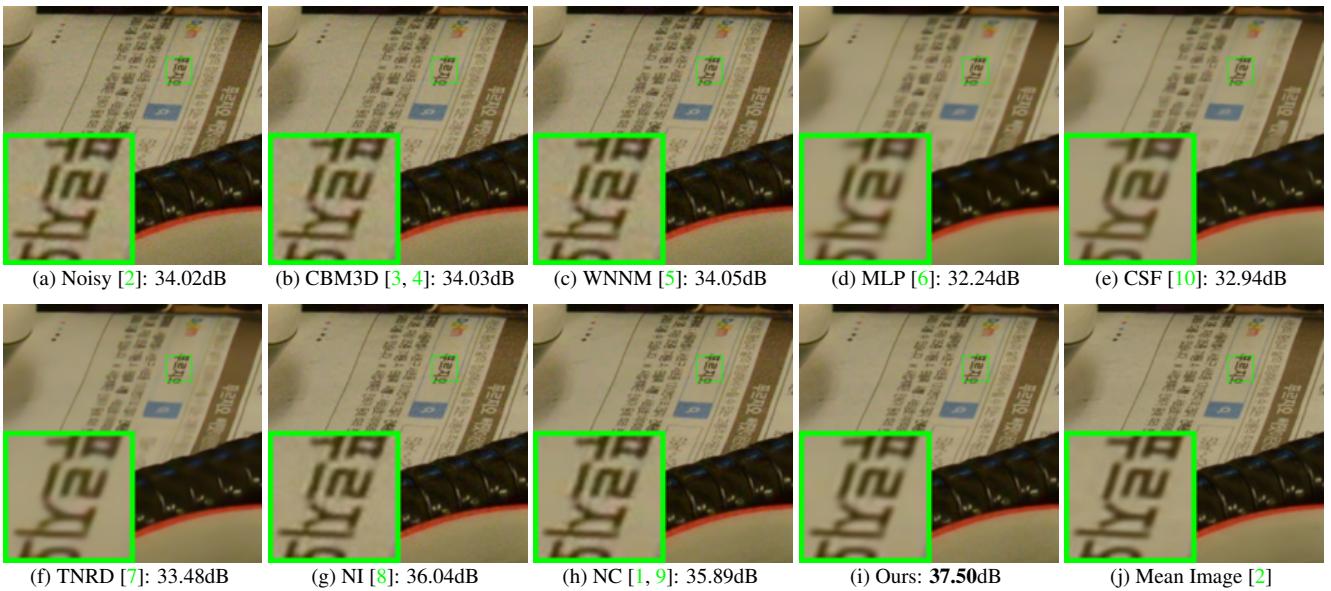


Figure 16. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 3200 A1” [2] by different methods. The images are better viewed by zooming in on screen.

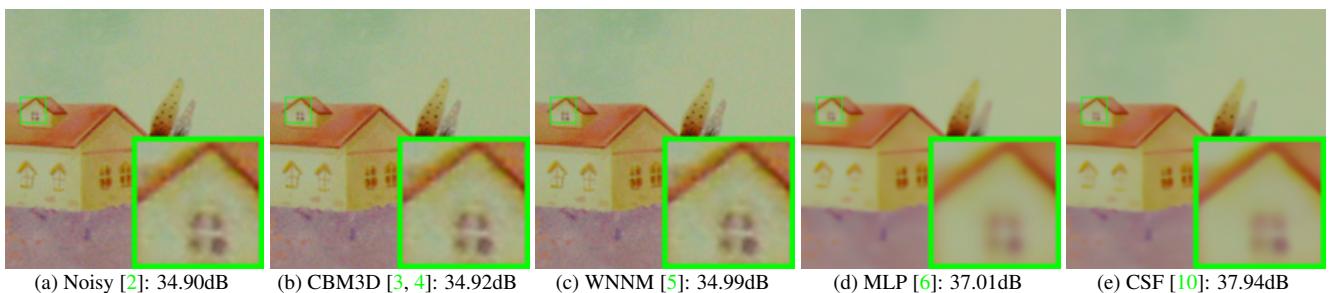


Figure 17. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 3200 A2” [2] by different methods. The images are better viewed by zooming in on screen.

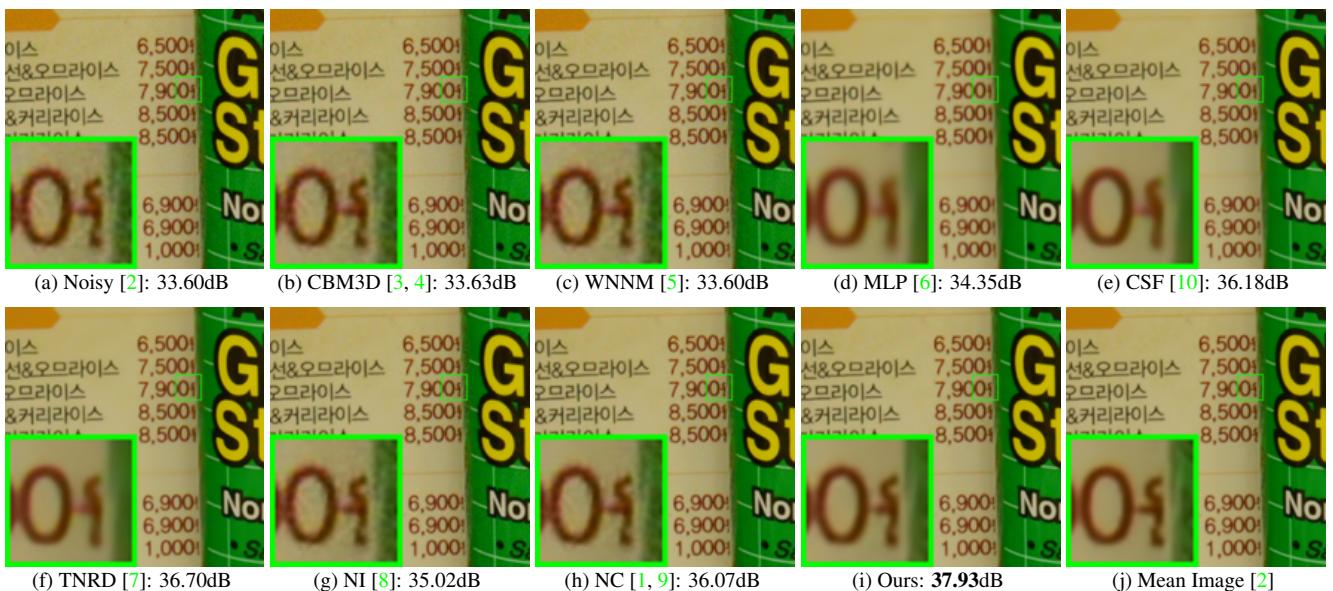


Figure 18. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 3200 A3” [2] by different methods. The images are better viewed by zooming in on screen.

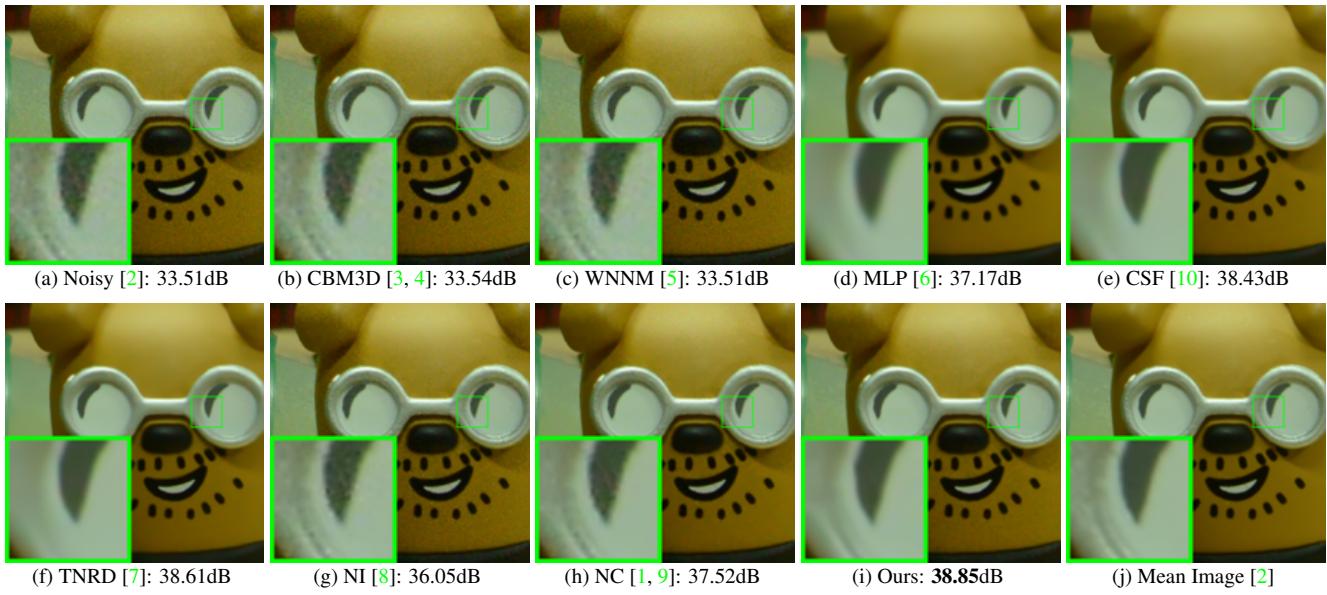


Figure 19. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 3200 A4” [2] by different methods. The images are better viewed by zooming in on screen.

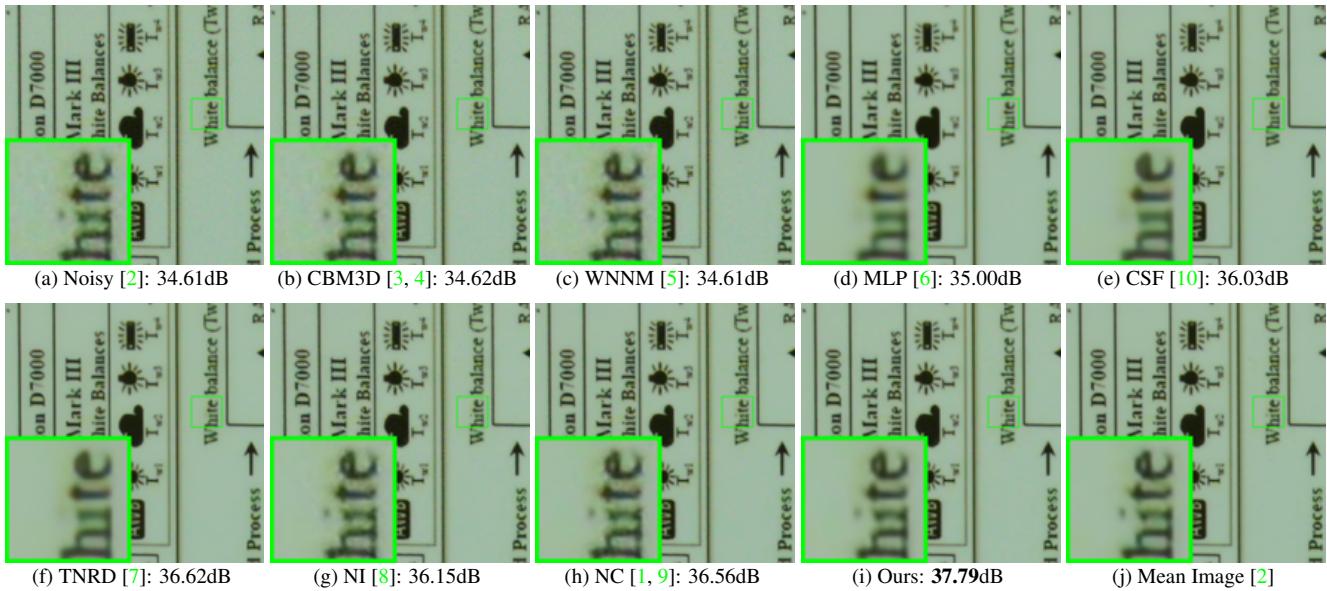


Figure 20. Denoised imagesupp of a region cropped from the real noisy image “Nikon D800 ISO 3200 A5” [2] by different methods. The images are better viewed by zooming in on screen.

References

- [1] M. Lebrun, M. Colom, and J. M. Morel. The noise clinic: a blind image denoising algorithm. <http://www.ipol.im/pub/art/2015/125/>. Accessed 01 28, 2015. 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11
- [2] S. Nam, Y. Hwang, Y. Matsushita, and S. J. Kim. A holistic approach to cross-channel image noise modeling and its application to image denoising. *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, pages 1683–1691, 2016. 1, 3, 4, 5, 6, 7, 8, 9, 10, 11
- [3] K. Dabov, A. Foi, V. Katkovnik, and K. Egiazarian. Image denoising by sparse 3-D transform-domain collaborative filtering. *IEEE Transactions on Image Processing*, 16(8):2080–2095, 2007. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11

- 1188 [4] K. Dabov, A. Foi, V. Katkovnik, and K. Egiazarian. Color image denoising via sparse 3D collaborative filtering with grouping
1189 constraint in luminance-chrominance space. *IEEE International Conference on Image Processing (ICIP)*, pages 313–316, 2007. 2, 1242
1190 3, 4, 5, 6, 7, 8, 9, 10, 11 1243
1191 [5] S. Gu, L. Zhang, W. Zuo, and X. Feng. Weighted nuclear norm minimization with application to image denoising. *IEEE Conference*
1192 *on Computer Vision and Pattern Recognition (CVPR)*, pages 2862–2869, 2014. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 1244
1193 [6] H. C. Burger, C. J. Schuler, and S. Harmeling. Image denoising: Can plain neural networks compete with BM3D? *IEEE Conference*
1194 *on Computer Vision and Pattern Recognition (CVPR)*, pages 2392–2399, 2012. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 1245
1195 [7] Y. Chen, W. Yu, and T. Pock. On learning optimized reaction diffusion processes for effective image restoration. *IEEE Conference*
1196 *on Computer Vision and Pattern Recognition (CVPR)*, pages 5261–5269, 2015. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 1246
1197 [8] Neatlab ABSoft. Neat Image. <https://ni.neatvideo.com/home>. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 1247
1198 [9] M. Lebrun, M. Colom, and J.-M. Morel. Multiscale image blind denoising. *IEEE Transactions on Image Processing*, 24(10):3149–
1200 3161, 2015. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 1248
1201 [10] U. Schmidt and S. Roth. Shrinkage fields for effective image restoration. *IEEE Conference on Computer Vision and Pattern Recog-*
1202 *nition (CVPR)*, pages 2774–2781, June 2014. 6, 7, 8, 9, 10, 11 1249
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