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## Supplementary Material to “External Prior Guided Internal Prior Learning for Real Noisy Image Denoising”

Anonymous CVPR submission

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In this supplementary material, we provide:

1. The closed-form solution of the sparse coding problem (6) in the main paper.
2. More denoising results on the real noisy images in dataset [1].
3. More results on the 15 cropped real noisy images (with mean image of 500 shots as “ground truth”) in dataset [2].
4. More results on the 60 cropped real noisy images (with mean image of 500 shots as “ground truth”) in dataset [2].

### 1. Closed-Form Solution of the Weighted Sparse Coding Problem (6)

For notation simplicity, we ignore the indices  $n, m, t$  in problem (6) of the main paper. It turns into the following weighted sparse coding problem:

$$\min_{\alpha} \|\mathbf{y} - \mathbf{D}\alpha\|_2^2 + \sum_{j=1}^{3p^2} \lambda_j |\alpha_j|. \quad (1)$$

Since  $\mathbf{D}$  is an orthogonal matrix, problem (1) is equivalent to

$$\min_{\alpha} \|\mathbf{D}^T \mathbf{y} - \alpha\|_2^2 + \sum_{j=1}^{3p^2} \lambda_j |\alpha_j|. \quad (2)$$

For simplicity, we denote  $\mathbf{z} = \mathbf{D}^T \mathbf{y}$ . Here we have  $\lambda_j > 0, j = 1, \dots, 3p^2$ , then problem (2) can be written as:

$$\min_{\alpha} \sum_{j=1}^{3p^2} ((\mathbf{z}_j - \alpha_j)^2 + \lambda_j |\alpha_j|). \quad (3)$$

The problem (3) is separable w.r.t. each  $\alpha_j$  and hence can be simplified to  $3p^2$  independent scalar minimization problems

$$\min_{\alpha_j} (\mathbf{z}_j - \alpha_j)^2 + \lambda_j |\alpha_j|, \quad (4)$$

where  $j = 1, \dots, 3p^2$ . Taking derivative of  $\alpha_j$  in problem (4) and setting the derivative to be zero. There are two cases for the solution.

(a) If  $\alpha_j \geq 0$ , we have

$$2(\alpha_j - \mathbf{z}_j) + \lambda_j = 0. \quad (5)$$

The solution is

$$\hat{\alpha}_j = \mathbf{z}_j - \frac{\lambda_j}{2} \geq 0. \quad (6)$$

So  $\mathbf{z}_j \geq \frac{\lambda_j}{2} > 0$ , and the solution  $\hat{\alpha}_j$  can be written as

$$\hat{\alpha}_j = \text{sgn}(\mathbf{z}_j) * (|\mathbf{z}_j| - \frac{\lambda_j}{2}), \quad (7)$$

where  $\text{sgn}(\bullet)$  is the sign function.

(b) If  $\alpha_j < 0$ , we have

$$2(\alpha_j - \mathbf{z}_j) - \lambda_j = 0. \quad (8)$$

The solution is

$$\hat{\alpha}_j = \mathbf{z}_j + \frac{\lambda_j}{2} < 0. \quad (9)$$

108 So  $\mathbf{z}_j < -\frac{\lambda_j}{2} < 0$ , and the solution  $\hat{\alpha}_j$  can be written as  
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$$\hat{\alpha}_j = \text{sgn}(\mathbf{z}_j) * (-\mathbf{z}_j - \frac{\lambda_j}{2}) = \text{sgn}(\mathbf{z}_j) * (|\mathbf{z}_j| - \frac{\lambda_j}{2}). \quad (10)$$

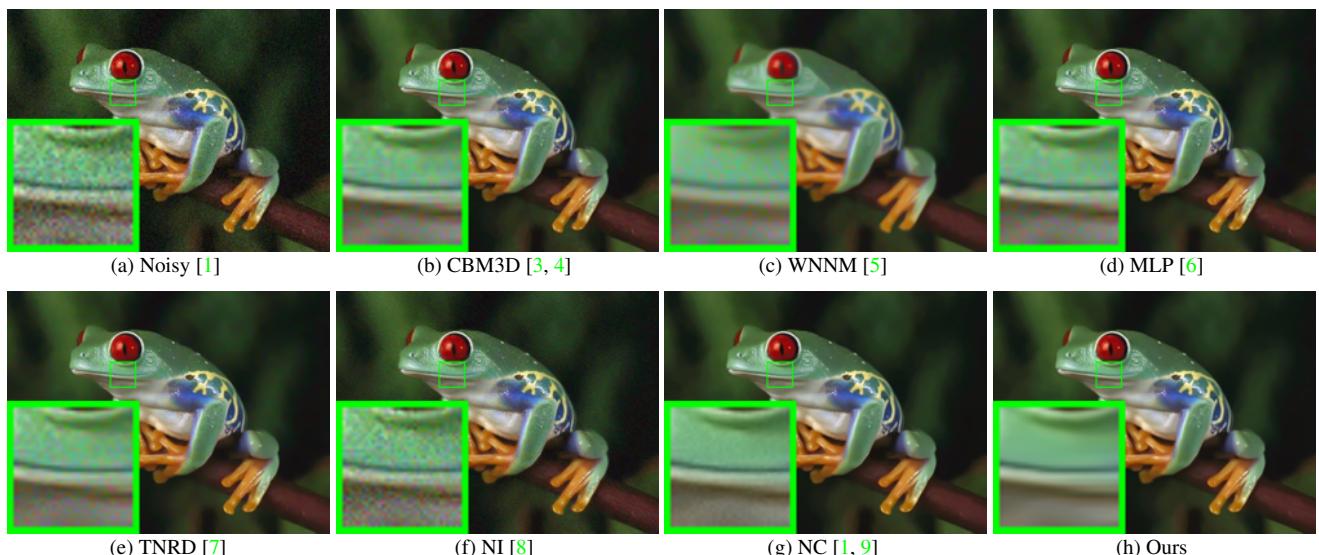
110 In summary, we have the final solution of the weighted sparse coding problem (1) as  
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$$\hat{\alpha} = \text{sgn}(\mathbf{D}^T \mathbf{y}) \odot \max(|\mathbf{D}^T \mathbf{y}| - \lambda, 0), \quad (11)$$

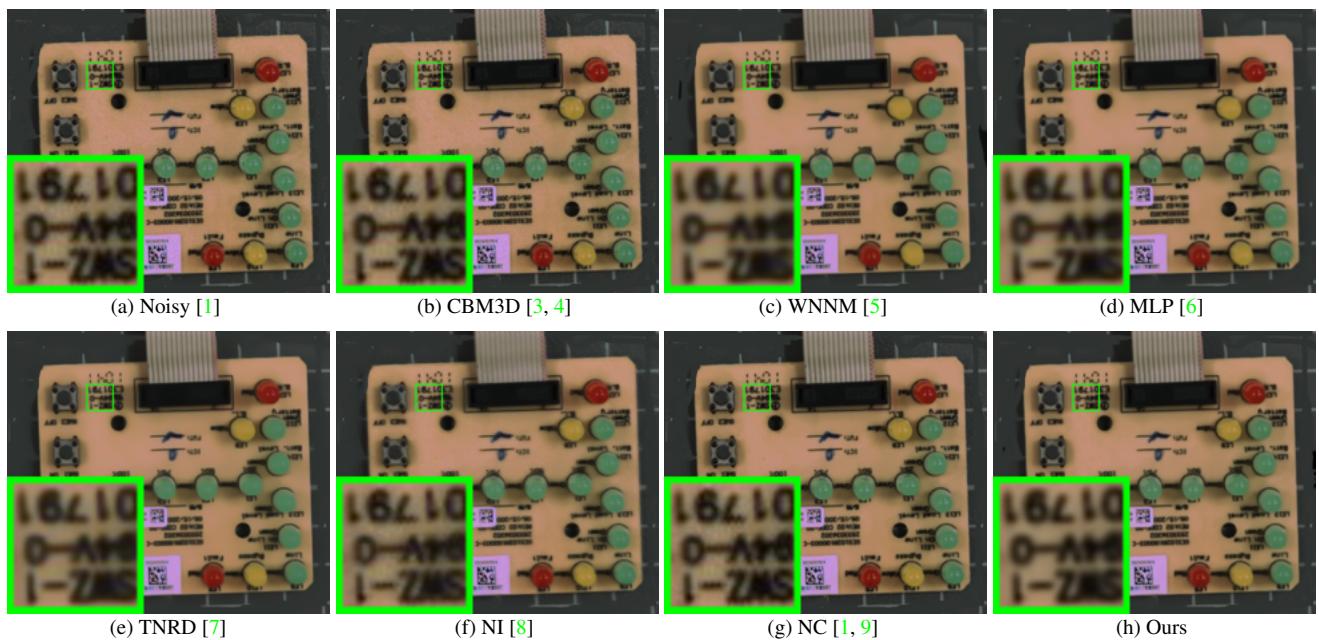
112 where  $\lambda = \frac{1}{2}[\lambda_1, \lambda_2, \dots, \lambda_{3p^2}]^\top$  is the vector of regularization parameter and  $\odot$  means element-wise multiplication.  
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## 114 2. More Denoising Results on the Real Noisy Images in Dataset [1]

115 In this section, we give more comparisons of the competing methods on the dataset [1]. The real noisy images in dataset  
 116 [1] have no “ground truth” images and hence we only compare the visual quality of the denoised images by different methods.  
 117 As can be seen from Figures 1-4, our proposed method performs better than the state-of-the-art denoising methods.  
 118



119 Figure 1. Denoised images of the real noisy image “Frog” [1] by different methods. The images are better to be zoomed in on screen.  
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121 Figure 2. Denoised images of the real noisy image “Circuit” [1] by different methods. The images are better to be zoomed in on screen.  
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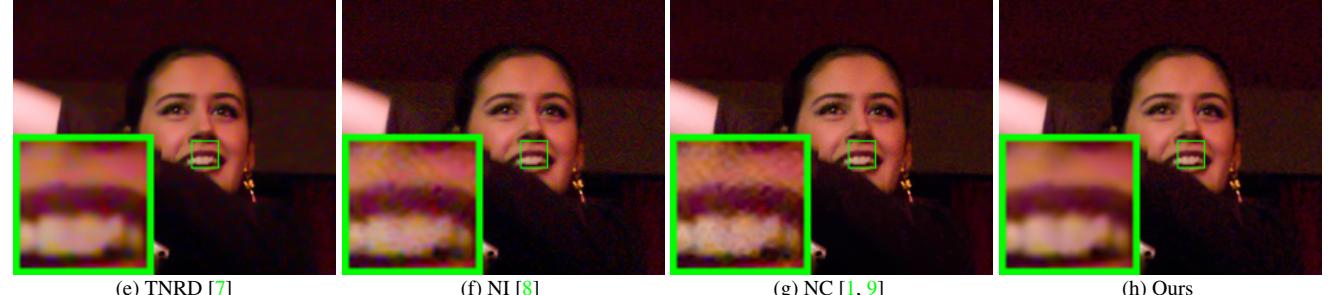
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226(a) Noisy [1] (b) CBM3D [3, 4] (c) WNNM [5] (d) MLP [6]  
(e) TNRD [7] (f) NI [8] (g) NC [1, 9] (h) Ours227  
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Figure 3. Denoised images of the real noisy image “Woman” [1] by different methods. The images are better to be zoomed in on screen.

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239(a) Noisy [1] (b) CBM3D [3, 4] (c) WNNM [5] (d) MLP [6]  
(e) TNRD [7] (f) NI [8] (g) NC [1, 9] (h) Ours240  
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Figure 4. Denoised images of the real noisy image “Vehicle” [1] by different methods. The images are better to be zoomed in on screen.

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### 3. More Denoising Results on the 15 Cropped Images Used in [2]

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In this section, we provide more visual comparisons of the proposed method with the state-of-the-art denoising methods on the 15 cropped real noisy images used in [2]. In this dataset, each scene was shot 500 times under the same camera and camera setting. The mean image of the 500 shots is roughly taken as the “ground truth”, with which the PSNR can be computed. As can be seen from Figures 5-9, in most cases, our proposed method achieves better performance than the competing methods. This validates the effectiveness of our proposed external prior guided internal prior learning framework for real noisy image denoising.

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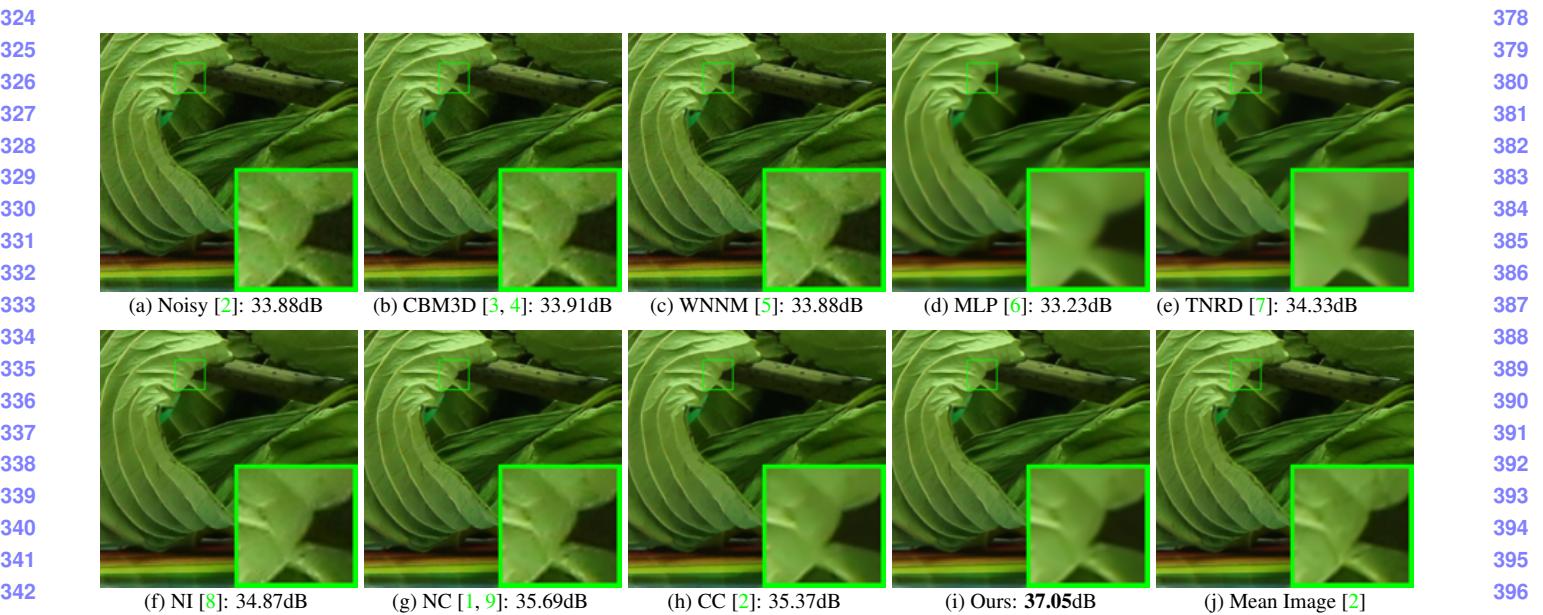


Figure 5. Denoised images of a region cropped from the real noisy image “Canon 5D Mark 3 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

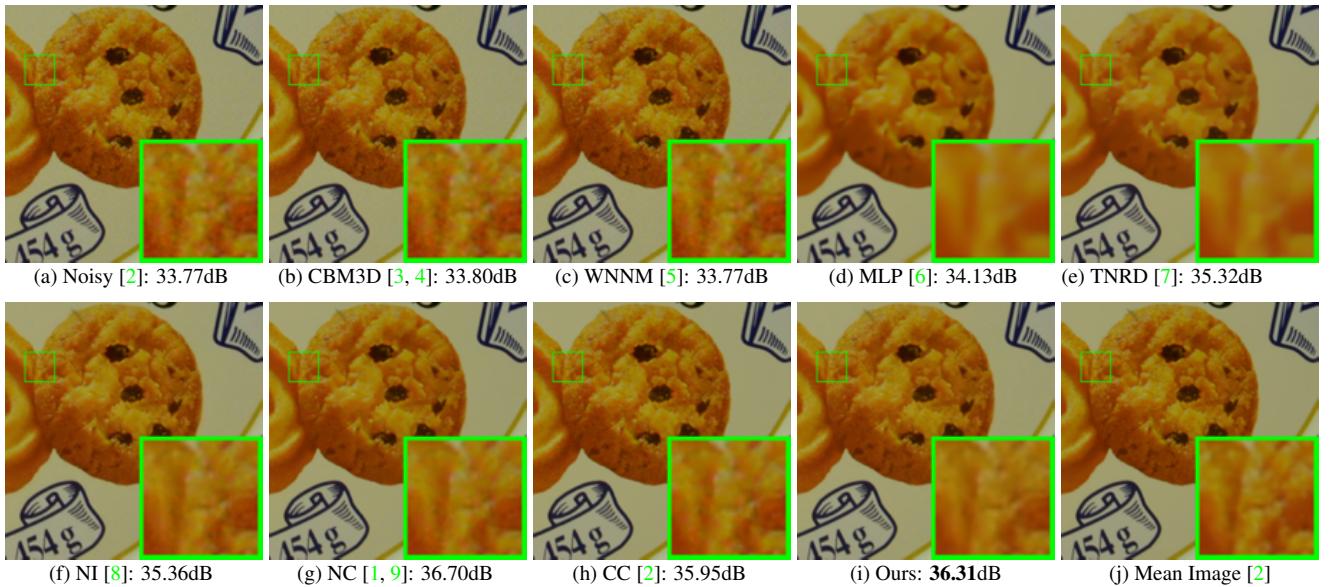


Figure 6. Denoised images of a region cropped from the real noisy image “Canon 5D Mark 3 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

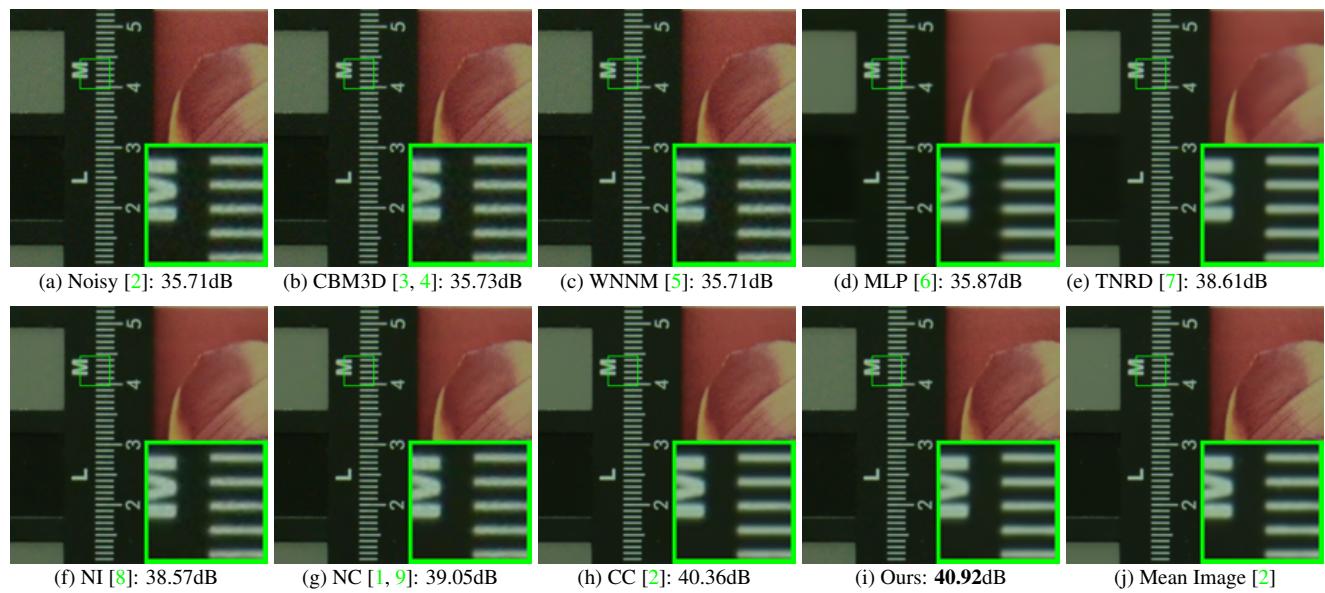


Figure 7. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 1600 2” [2] by different methods. The images are better to be zoomed in on screen.

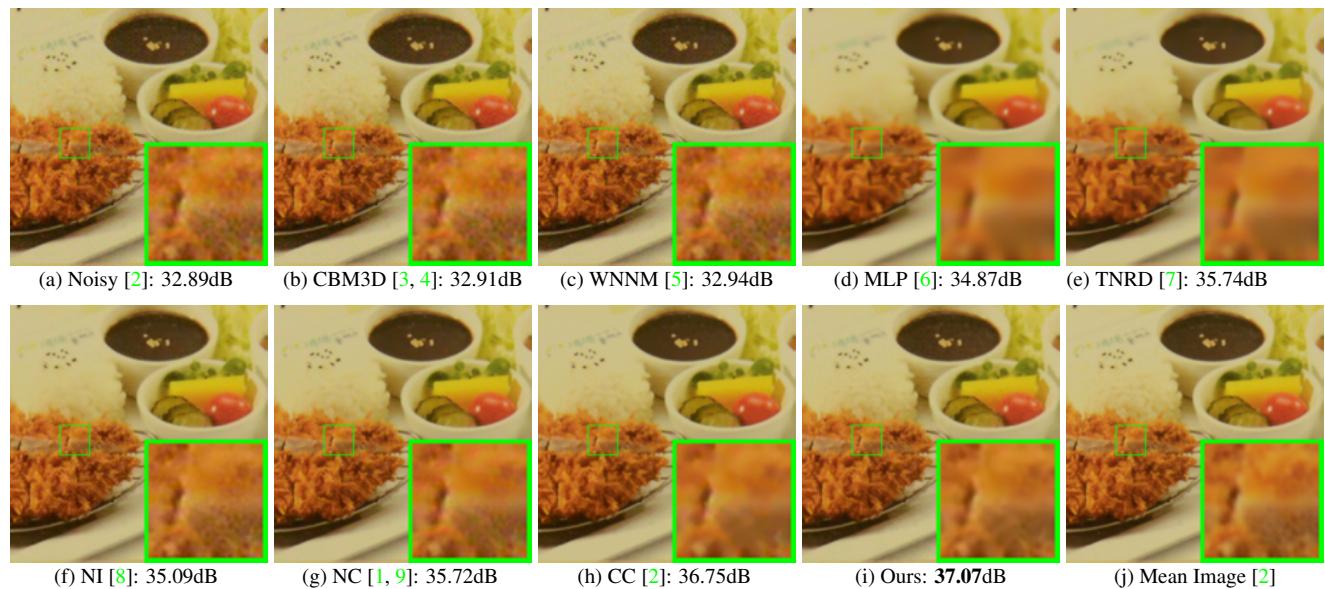


Figure 8. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 2” [2] by different methods. The images are better to be zoomed in on screen.

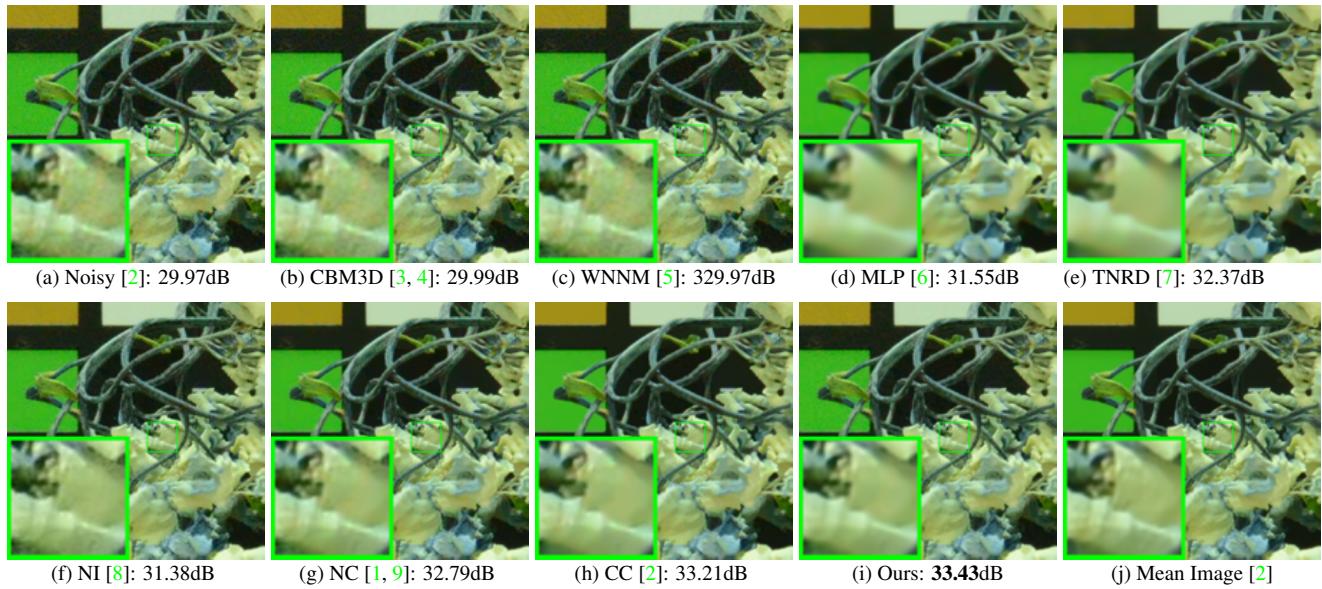


Figure 9. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 6400 2” [2] by different methods. The images are better to be zoomed in on screen.

#### 4. More Denoising Results on the 60 Cropped Real Noisy Images from [2]

In this section, we provide more visual comparisons of the proposed method with the state-of-the-art denoising methods on the 60 cropped real noisy images we cropped from [2]. In this dataset, each scene was shot 500 times under the same camera and camera setting. The mean image of the 500 shots is roughly taken as the “ground truth”, with which the PSNR can be computed. As can be seen from Figures 10-20, in most cases, our proposed method achieves better performance than the competing methods. This validates the effectiveness of our proposed external prior guided internal prior learning framework for real noisy image denoising.

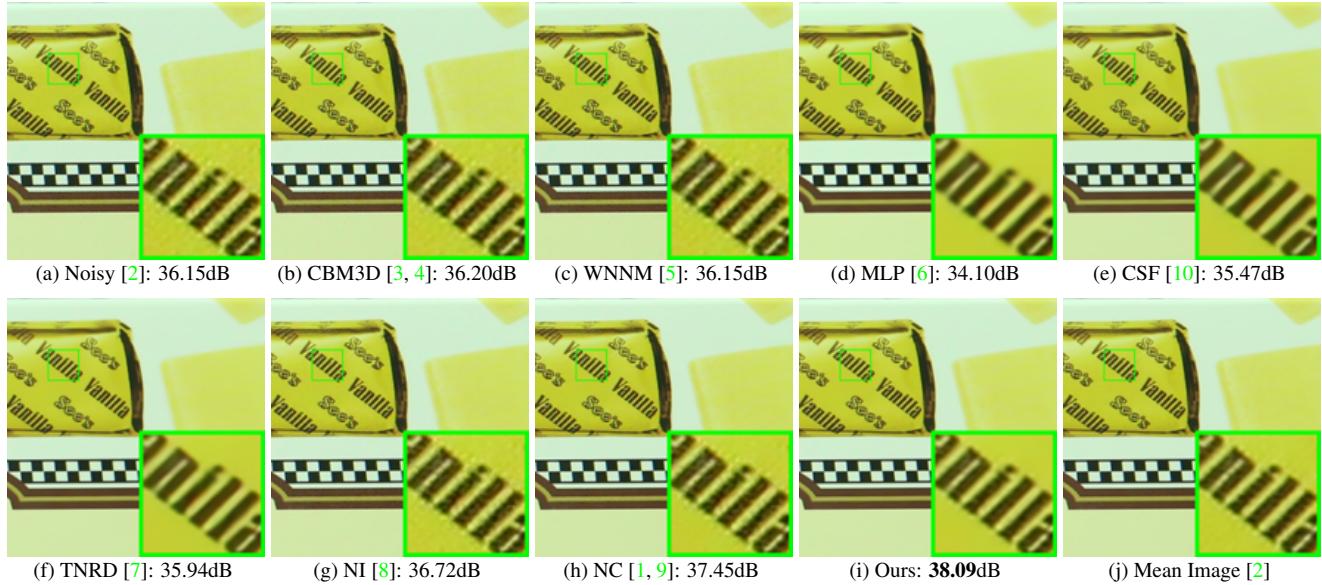


Figure 10. Denoised images of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C1” [2] by different methods. The images are better viewed by zooming in on screen.

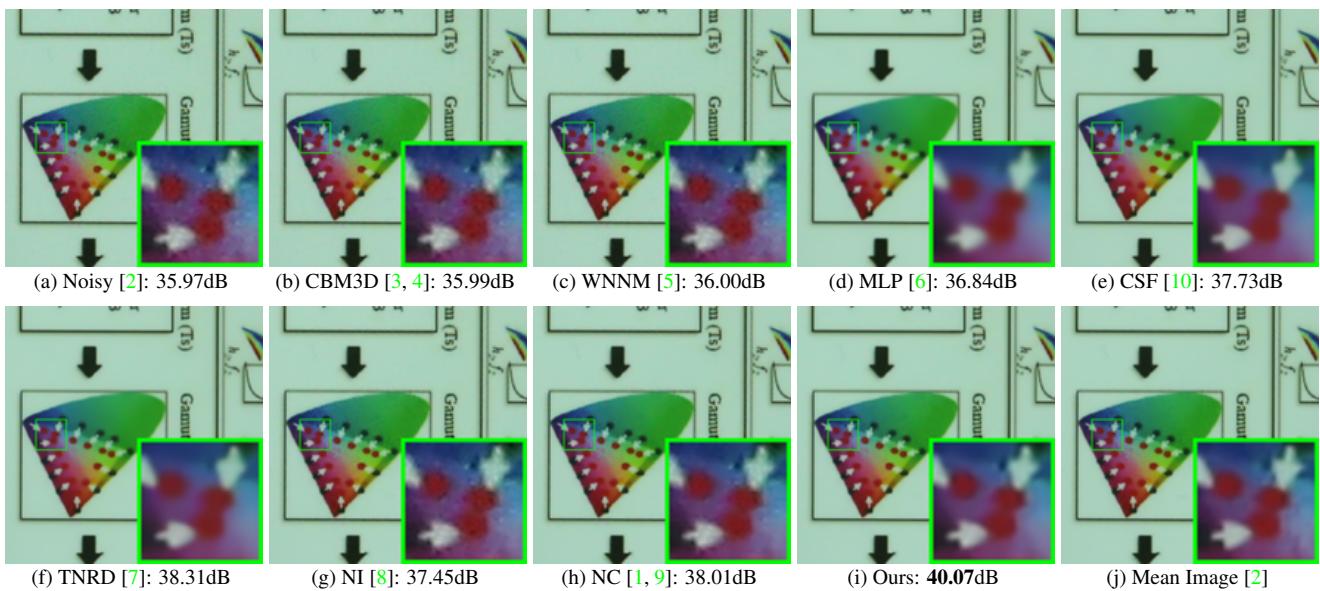


Figure 11. Denoised images of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C2” [2] by different methods. The images are better viewed by zooming in on screen.

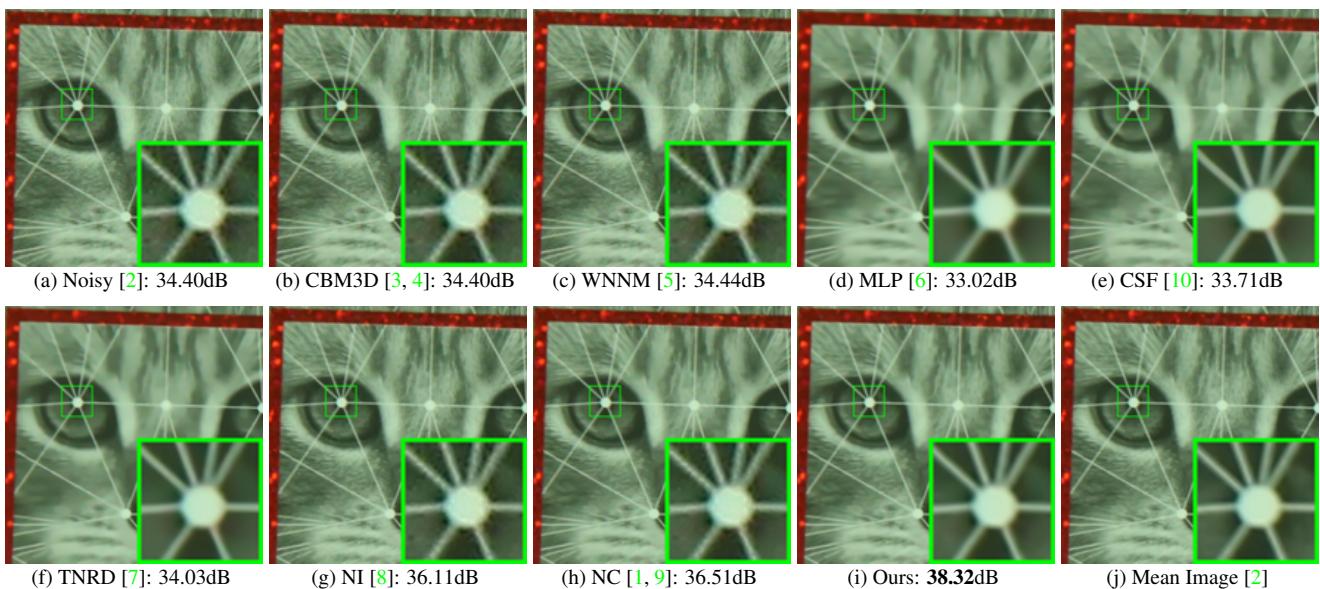


Figure 12. Denoised images of a region cropped from the real noisy image “Canon EOS 5D Mark3 ISO 3200 C3” [2] by different methods. The images are better viewed by zooming in on screen.

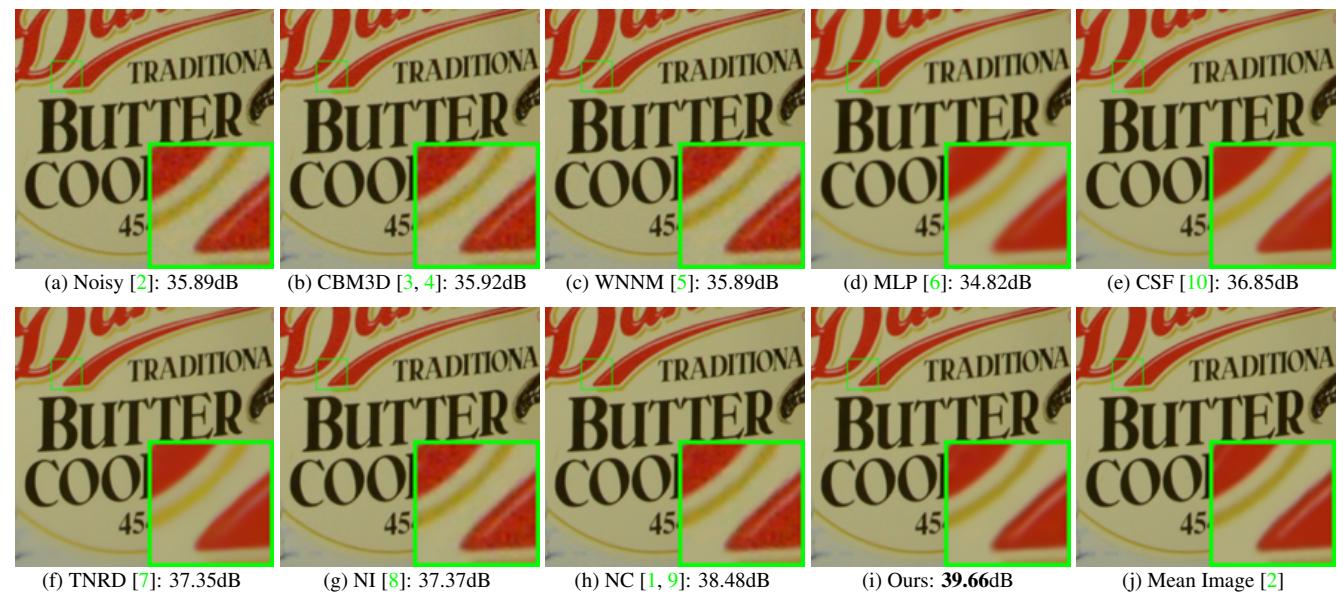


Figure 13. Denoised images of a region cropped from the real noisy image “Nikon D600 ISO 3200 C1” [2] by different methods. The images are better viewed by zooming in on screen.

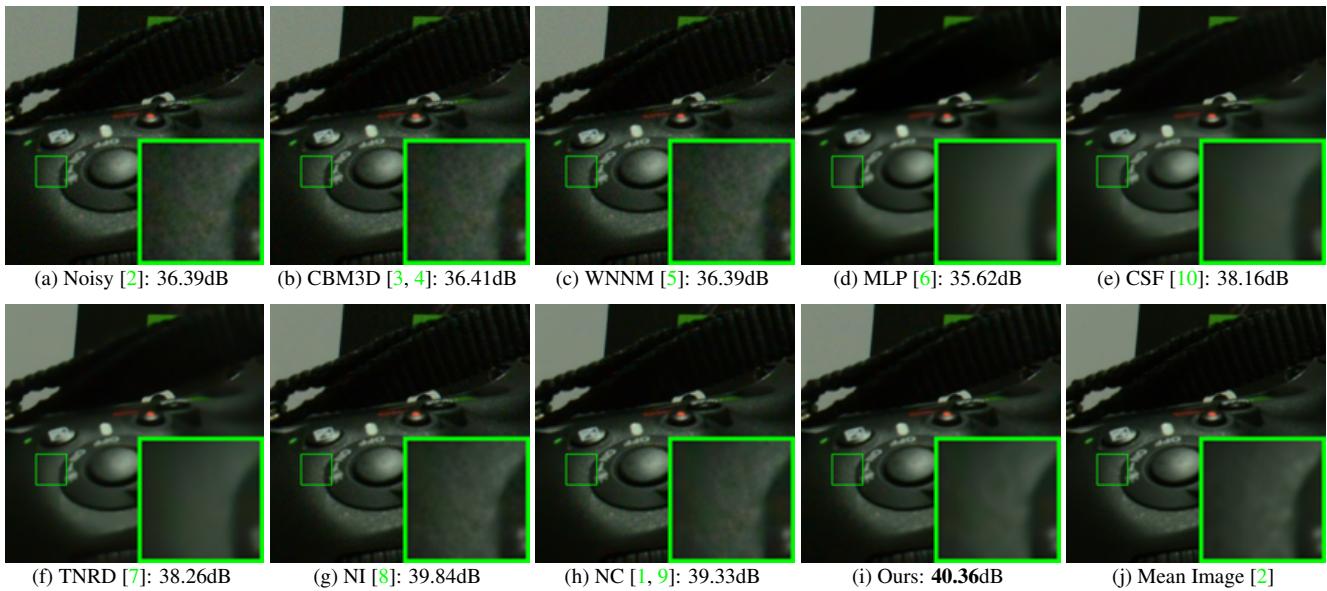


Figure 14. Denoised images of a region cropped from the real noisy image “Nikon D600 ISO 3200 C2” [2] by different methods. The images are better viewed by zooming in on screen.

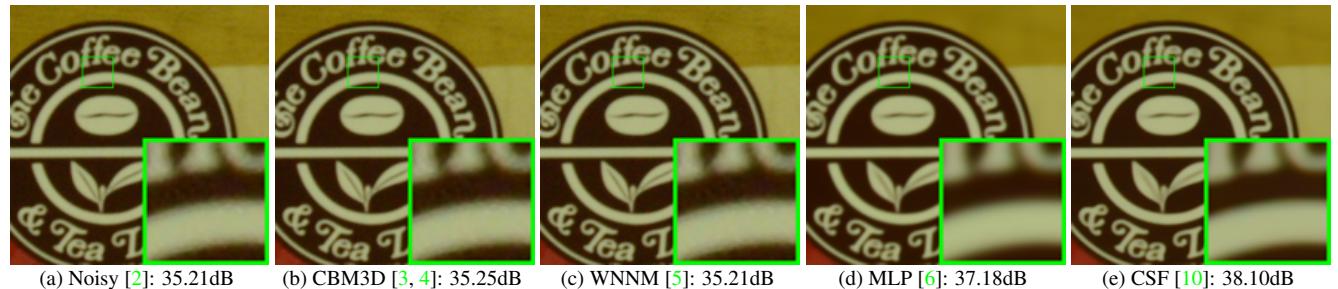


Figure 15. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 1600 B2” [2] by different methods. The images are better viewed by zooming in on screen.

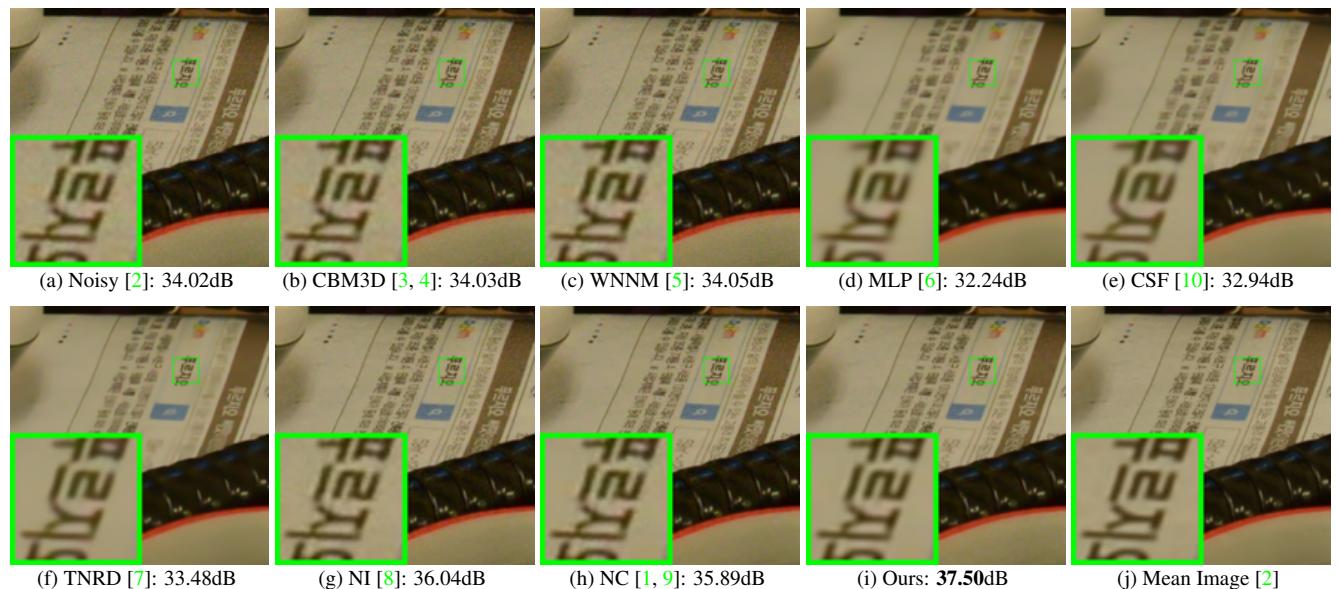


Figure 16. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 A1” [2] by different methods. The images are better viewed by zooming in on screen.

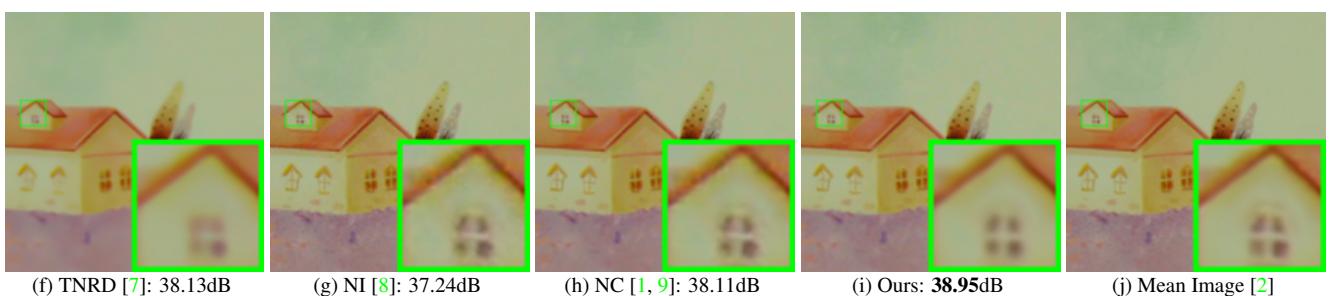
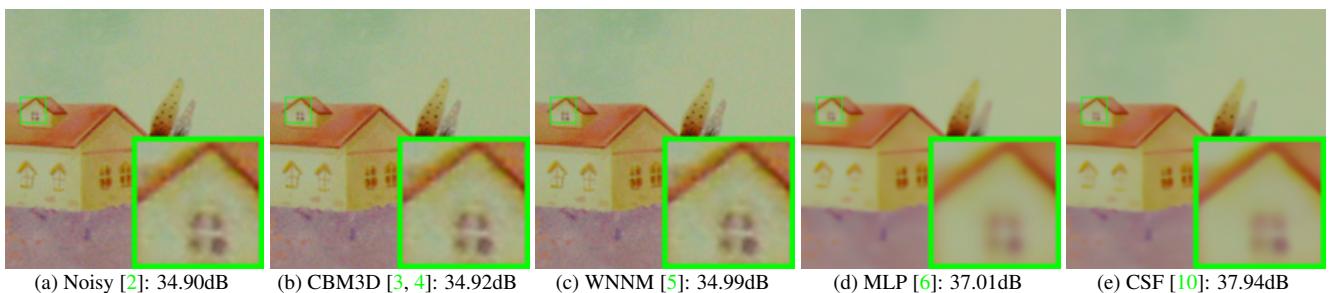


Figure 17. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 A2” [2] by different methods. The images are better viewed by zooming in on screen.

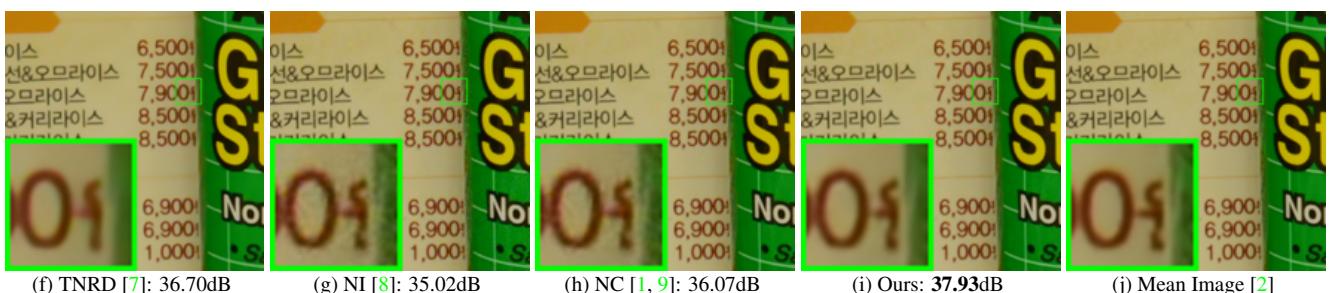
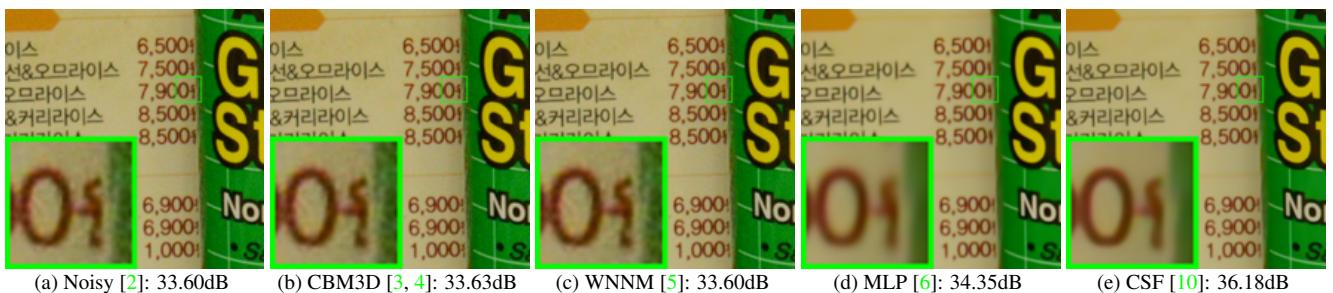


Figure 18. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 A3” [2] by different methods. The images are better viewed by zooming in on screen.

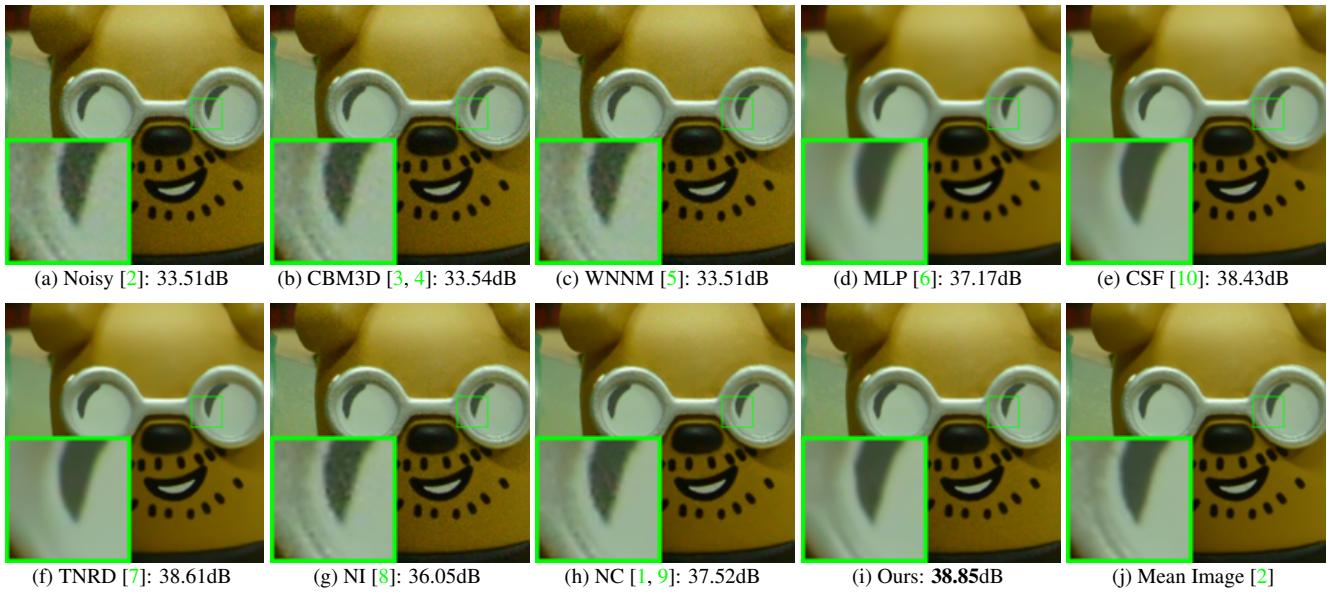


Figure 19. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 A4” [2] by different methods. The images are better viewed by zooming in on screen.

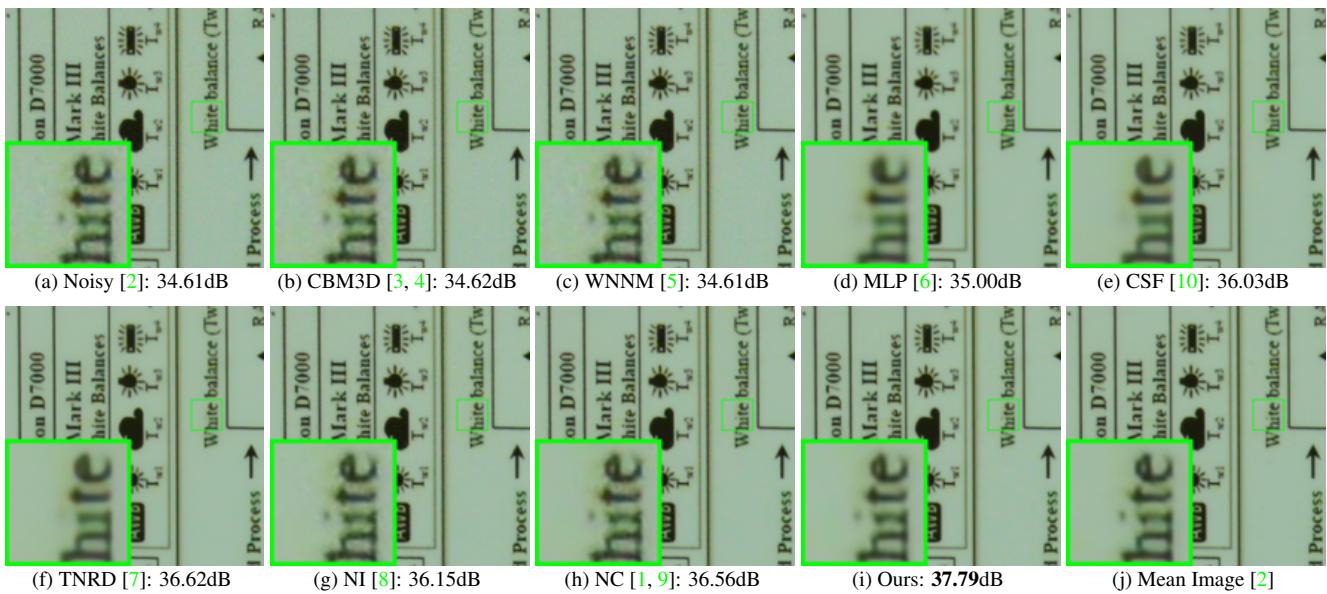


Figure 20. Denoised images of a region cropped from the real noisy image “Nikon D800 ISO 3200 A5” [2] by different methods. The images are better viewed by zooming in on screen.

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