The Hong Kong Polytechnic University

Department of Computing

Thesis Title

Thesis Author

A thesis submitted in partial fulfilment of the requirements for the degree of

Doctor of Philosophy

March 2014

CERTIFICATE OF ORIGINALITY

I hereby declare that this thesis is my own work and that, to the best of my knowledge and belief, it reproduces no material previously published or written, nor material that has been accepted for the award of any other degree or diploma, except where due acknowledgement has been made in the text.

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Abstract

The nonlocal self-similarity (NSS) prior of natural images has been extensively studied in many image restoration methods. In this thesis, we exploit the NSS property of external natural images, external guided internal NSS property, and internal NSS property for image denoising tasks.

Acknowledgement

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Introduction

Nowadays, CCD or CMOS cameras are becoming more and more important in many aspects of human life such as photography, artificial intelligence, and security system. For each camera product, the camera imaging pipeline in the camera is of particular importance since it is the core part to transform the photons reflected by the real scene being captured in the camera sensor into the pixel values of an image, which can be displayed on a screen. During the camera imaging process, the noise is unavoidablely generated due to many reasons. Two major reasons of noise generation are the discrete nature of light and the thermal agitation, which can cause the photon shot noise and the dark-current noise, respectively. Image denoising is the problem of recovering the laten clean image from the captured noise version.

Chapter abstract This chapter will introduce the image noise and its acquirezation equation, the image denoising problem, the objective measures to evaluate the image denoising performance, the proposed denoising methods. Finally, I will summarize the structural of this thesis, and the contribution I made in this thesis.

1.1 The Image Noise

The realistic noise are very complex in real photography images captured by the camera sensors. One major reason is that the noise is unable to be explicitly modeled by some definitive probabilistic distributions. Often the sRGB images we look at the screen have been processed via the camera imaging pipeline, during which the noise will be much more complex than its initial status.

The noise are generated mainly due to the discrete nature of light and the thermal agitation, which will cause unstable measurement in camera sensors. The major types of noise generated during the imaging pipeline are the random noise, the spatial non-uniformity noise, and quantization noise. The random noise includes photon shot noise, dark current, and readout noise. The spatial non-uniformity noise includes the fixed pattern noise (PRNU, DCNU), CCD/CMOS specific noise.

To better describe the noise quantitatively, we provide a simplified signal acquisition model [] including various noise sources (for each pixel) as follows:

$$P = f((g_{cv}(C+D) + N_{reset})g_{out} + N_{out}) + Q.$$

$$(1.1)$$

The above equation is explained in details:

- *P* is the raw pixel value;
- *f* is the camera response function, usually a linear function before attaining a saturation threshold;
- *C* is the number of absorbed electrons (charges) transformed from the photons via the photon-diodes in the camera sensor, which can be modeled by a Poisson distribution;
- *D* is the number of absorbed electrons generated by dark current by thermal generation, which is often modeled by a Poisson distribution;
- *N*_{reset} is the thermal noise generated by the readout circuitry (or reset noise related to reset voltage), which can be well modeled by a Gaussian disribution;
- N_{out} is the readout noise, which is also modeled by a Gaussian distribution;
- Q is the quantization error happened during rounding to interger values, usually uniformly distributed and normally negligible compared to the readout noise;
- g_{cv} is the equivalent capacitance (EC) of the photo-diode and the gain factor during charge to voltage conversion;
- g_{out} is the gain factor during voltage to pixel value conversion (readout).

After some merging and simplifying, the acquisition model of the signal can be formulated as follows:

$$\mathbf{P} = f((g_{cv}(\mathbf{C} + \mathbf{D}) + \mathbf{N}_{reset})g_{out} + \mathbf{N}_{out}) + \mathbf{Q},$$

$$= f(g_{cv}g_{out}(\mathbf{C} + \mathbf{D}) + g_{out}\mathbf{N}_{reset} + \mathbf{N}_{out}) + \mathbf{Q},$$

$$= f(g\lambda + N_R) + \mathbf{Q},$$
(1.2)

where $g=g_{cv}g_{out}$ is the overall camera gain factor, $\lambda=\mathbf{C}+\mathbf{D}$ is # of electrons in pixel capacitor and also Poisson distributed, since "Sum of Independent Poisson Random Variables is also Poisson", and $N_R=g_{out}\mathbf{N}_{reset}+\mathbf{N}_{out}$ is the overall readout noise and also Gaussian distributed, since "Sum of Independent Gaussian Random Variables is also Gaussian". In summary, the overall noise before the camera imaging pipeline can be modeled by a mixed Poisson and Gaussian distribution []. Unfortunately, the realistic noise will become very complex after being processed during the camera imaging pipeline [**crosschannel**]. This makes the image denoising an important and challenging task.

To make the problem easier, in image denoising community, the most common tested noise is additive white Gaussian noise (AWGN) [EA06]. In AWGN degraded image, each pixel is corrupted by a random value following Gaussian distribution with zero mean and a certain standard deviation (std). Note that for each pixel, the std of the Gaussian distribution is the same, and for all the pixels, the noise values are sampled independently. The AWGN noise is similar to the read-out noise in digital cameras.

In order to obtain images of good quality while still maintaining the structures and details of the captured scenes, image denoising is an essential step. In this thesis, I will present my work on image denoising, in which we focus on synthetic additive white Gaussian noise (AWGN) and the realistic noise in real-world images. The AWGN noise is described as a Gaussian distribution $\mathcal{N}(0,\sigma^2)$, which means that the noise is Gaussian distributed with 0 mean and σ standard deviation. Most of existing methods focus on processing AWGN noise since it is a perfect testing bed for evaluating the proposed methods as well as other image restoration problems such as image super-resolution, deblurring, inpainting, etc.

1.2 Image Denoising

In general, image denoising aims to recover the latent clean image \boldsymbol{x} from the observed noisy image $\boldsymbol{y}=\boldsymbol{x}+\boldsymbol{n}$, where \boldsymbol{n} is assumed to be the additive noise. \boldsymbol{n} is often assumed to be synthetic additive white Gaussian noise, or the realistic noise in real-world images. Image denoising can be viewed as a regression problem, in which a *plausible* clean image can be obtained from the infinite number of possible candidates. The word *plausible* means that

the denoised image should look like the noisy image but without the noise component.

Image denoising would be very hard if we do not employ any prior information on it. The reason is that we do not know what exactly the latent clean image is without the prior information of the clean image. Hence, it is meaningful to exploit the most *plausible* image under some prior information. The most commonly used prior information in image denoising community is the Bayesian rule, which is also known as maximum A-posterior (MAP) property. Under the MAP framework, the most plausible latent clean image is the one which has the maximum Bayesian probability given the given noisy version. The posteriro probability can be measured by some existing evaluation methods which I will introduce in the following sections. In fact, the probability or measurements can measure the closeness of the latent clean image to the given noisy image. The closeness is usually measured by the ℓ_2 norm of the difference between the two images mentioned above. There are many latent clean images with the same ℓ_2 norm distance with the given noisy image. But some images in the circle are more plausible than the others due to the aspects of less artifacts, better structural preservation, and less remaining noise, etc.

1.3 Evaluating Denoising Performance

In order to achieve the maximum Bayesian probability, we need calculate the measurements of goodness for the denoised images. A natural problem is, how to measure the quality of the denoised image? It is very important to find better answer to this question. In fact, the research of image quality accessment is to find good algorithms to measure the quality of images under different situations and applications including image denoising.

A initial understanding is that the answer to the above question is largely depends on the situations we face when we perform image denoising experiments. When we perform synthetic experiments on additive white Gaussian nosie (AWGN), we usually already have the original clean image, the noisy image is generated by adding synthetic AWGN noise to the clean image. Then we can directly measure the quality of the denoised image by some existing image quality assessment (IQA) metrics. When we do not have the clean image provided as "ground truth", a possible and final solution is to measure

the image quality by relying on human subjective evaluation. The IQA metrics can be roughly divided into two major directions: 1) full reference IQA; and 2) no reference IQA. Full reference IQA metrics are based on the assumption that the true underlying image is available in order to compute a measure, while no reference IQA metrics perform quality assessments without the reference image since the true underlying image is not available.

RMSE and PSNR: We mentioned previously that the it is corresponding to the ℓ_2 norm or equally mean square error (MSE) which is used to measure the distance between the denoised image and the given noisy image. In fact, the MSE measure is closely related to the famous peak signal to noise ratio (PSNR) metric. PSNR is the most commonly used full reference IQA metric for many image restoration tasks including denoising. The definition of PSNR can be formulated as follows (for 8-bit image):

$$PSNR = 20\log_{10}(\frac{2^8}{RMSE(\boldsymbol{x}, \boldsymbol{y})}), \tag{1.3}$$

where RMSE(x, y) refers to the root mean square error defined as RMSE = $\sqrt{\frac{1}{MN}\sum_{i=1}^{M}\sum_{j=1}^{N}(x_{ij}-y_{ij})^2}$ for images $x, y \in \mathcal{R}^{M\times N}$. As we can see, PSNR is closely related to the ℓ_2 norm distance between two images. The unit of PSNR is decibel (dB) and higher dB value indicates better image quality and lower RMSE. Even thouth PSNR is very simple and intuitive, higher PSNR does not indicate higher visual structural similarity. Hence, many researchers still make effort to find alternative and better IQA metrics.

SSIM [Wan+04]: Some researchers attempted to exploit the visual properties of the human visual system. One of the seminar work in this direction is the famous structural similarity index metric (SSIM), which is a full reference IQA metric. In SSIM, each image patch is separated into three different components indicating three core informative parts of the original patch. The three components are luminance (mean value of the pixels in the patch), contrast (the standard deviation of the patch), and structure (the mean subtracted patch). The major advantage of the SSIM is that it takes into account the fact that the human visual system is very sensitive tothe relative changes in luminance, rather than the absolute changes in luminance. The value range of the SSIM is between 0 and 1, where higher value indicate higher similarity (SSIM of 1 indicates that the two images are exactly the same). Note that it does not indicate that higher SSIM indicate better image quality, since the reference image is not the image of the best quality.

Other IQA Metrics: Besides of the PSNR and SSIM, there are many other IQA metrics for full reference and no reference IQA. Some examples include the MS-SSIM [Wan+03], which is a multi-scale extension of the original SSIM. Some examples in no reference IQA include BLIINDS [Saa+12] and BIQI [MB10]. These IQA metrics capture the deviations from the expected statistics of the natural images. For example, BLIINDS measures the deviations from the expected histogram of certain features in DCT domain, while BIQI measures deviations from the expected distribution of wavelet coefficients in a multi-scale decomposition.

I have to mention that no IQA metric is perfect or best for image denoising task, both in full reference and no reference cases. The de facto standard metrics in image restoration community are PSNR and SSIM. In order to avoid these two metrics generate bad results, it is essential to demonstrate the image quality in the thesis for human subjective evaluation.

1.4 The Proposed Methods

This thesis is mainly consisted by the several work I have done during my PhD study, during which I focus on designing new and better image denoising algorithms.

Firstly, I propose a method for denoising synthetic AWGN noise, from which we can study the performance of the nonlocal self-similarity priors of natural images. In fact, we propose to learn the external NSS priors and apply the learned model on denoising AWGN noise. The proposed method achieves state-of-the-art performance on AWGN denoising on both effectiveness and efficiency.

Basing on the success on the synthetic noise removal, I propose to exploit the power of the NSS priors in natural images to deal with the complex realistic noise in real-world noisy images. Specifically, we propose three methods exploiting the NSS priors of natural images for real noisy image denoising, which can be introduced as follows.

In the first method, I propose to learn the NSS prior from the external natural images, and then apply the learned external prior to guide the learning of the internal NSS prior of the input real noisy image. The experiments on two commonly used datasets and a new one we constructed to implement

the shortage of existing datasets, demonstrate that the proposed method can achieve better performance than existing color image denoising methods such as CBM3D [Dab+07a], the state-of-the-art Gaussian noise removal methods [csr; Dab+07b; Bur+12], and the real noisy image denoising methods [] including a commercial software Neat Image [ABS], which is embedded into the famous PhotoShop CS for image processing tasks.

In the second method, I propose to employ the low rank model describe fully the the internal NSS prior, basing on the observed fact that the similar image patches can be contanated as a matrix of low rank. Different from the previous work, I extend the WNNM model and apply it to multi-channel version to make it feasible for color image denoising.

In the third method, is to use the sparse coding based method with additional weighting scheme to regard the local noise in real noisy images as a Gaussian and the prior is used to deal with the real noisy image.

Finally, to make my thesis more comprehensive, I construct a large benchmark of real noisy images captured by different types of famous commercial cameras, on which I also evaluate the image denoising methods mentioned above and the proposed methods in this thesis.

The structure of this thesis is organized as follows: in the chapter 2, we review the literatures in the image denoising area; in the chapter 3, we introduce the fully external method; in the chapter 4, we introduce the external prior guided internal method; in the chapter 5, we introduce the internal method based on low ran model; in the chapter 6, we introduce the internal method based on sparse coding model; in the chapter 7, we introduce the real noisy image dataset we construct, and finally evaluate the proposed methods with the compared competing methods, both for synthetic AWGN or Poisson noise and real noise, including the commercial software designed especially for real noise.

1.5 Thesis Structure

Chapter 2: Literature Review

In this chapter, we review the related work and give a detailed introduction of the literature. We will first review the most representative work on additive white Gaussian noise removal. I review the detailed work on camera imaging pipeline and realistic noise generated in the camera sensors. I will also review the work on real noisy image denoising.

Chapter 3: External Nonlocal Self-Similarity Prior Learning for Synthetic Gaussian Noise Removal

In this chapter, I will introduce our work on external nonlocal self-similarity (NSS) prior learning for synthetic Gaussian noise removal. As far as we know, this work is the first to learn the NSS priors of natural clean images, while previous work only utilize the NSS priors of input noisy image for online denoising. The advantages of this offline learning is that it can preserve the details of natural images while being much faster then most online denoising methods.

Chapter 4: External Prior Guided Internal Prior Learning for Real Noisy Image Denoising

In this chapter, I will introduce our work on external prior guided internal prior learning method for real noisy image denoising. This work can maintain the advantages of both sides: from the external perspective, the method can preserve the structures of natural images better than the internal methods, while from the perspective of internal method, the proposed method can recover the details of the input noisy image better than the external methods.

Chapter 5: Multi-channel Weighted Nuclear Norm Minimization for Real Color Image Denoising

In this chapter, we introduce a multi-channel weighted nuclear norm minimization (MC-WNNM) method. This method regards different channels in RGB images differently to adaptively process the real color noisy images. Besides, this work also propose a new strategy for color image denoising. Experiments demonstrate that the proposed method can achieve better perfor-

mance on real color image denoising than existing state-of-the-art methods, including some commercial software.

Chapter 6: A Triple Weighted Sparse Coding Scheme for Realistic Noisy Image Denoising

In this chapter, I introduce a novel sparse coding based method for real color image denoising. In this method, I regard the noise in each of the local region in the real noisy image as a Gaussian, and propose a triplely weighted scheme to deal with the complex realistic noise in real color noisy images. Experiments show that the proposed method performs better and faster than the nuclear norm based method mentioned in previous chapter.

Chapter 7: A Benchmark on Real Color Noisy Image, with Comprehensive Evaluation of State-of-the-art

To fully boost the research of real color noisy image denoising, we construct a large benchmark on real color noisy images. This dataset is collected from several representative cameras with comprehensive settings on contents, lighting, ISO, shutter, and aperture, etc. Based on this newly established dataset, we fully evaluated existing denoising methods, including the methods designed for synthetic Gaussian noise and the methods designed especially for real color noise. We believe that this new dataset will largely boost the research of the image denoising especially the realistic image denoising problems.

Literature Review

In this chapter, I will review the denoising literature during the past decades. Specifically, I will first review the denoising methods designed for additive white Gaussian noise (AWGN) since AWGN is the mostly studied noise distribution in the literature. Though these methods are proposed to deal with the AWGN noise, the idea can be applied to the other image denoising tasks such as real color image denoising. In the second part, I will review the existing methods proposed for processing real noisy images. Though the methods in this domain is not that versartile than those methods for the AWGN noise, the real noisy image denoising is the current mainstream for the image denoising community. Due to the noise is not known beforehand, noise estimation should be performed for the real noisy image denoising task. Hence, we also review the literature on image noise estimation task.

2.1 Synthetic Grayscale Image Denoising

As a classical problem in low level vision, image denoising has been extensively studied, yet it is still an active topic for that it provides an ideal test bed for image modeling techniques. In general, image denoising aims to recover the clean image x from its noisy observation y = x + v, where v is assumed to be additive white Gaussian noise. A variety of image denoising methods have been developed in past decades, including filtering based methods [TM98], diffusion based methods [PM90], total variation based methods [Rud+92; Osh+05], wavelet/curvelet based methods [Don95; Cha+00; Sta+02], sparse representation based methods [EA06; Mai+09a; Don+13], nonlocal self-similarity based methods [Bua+05a; Dab+07b; Ji+10a; Gu+14], etc.

Image modeling plays a central role in image denoising. By modeling the wavelet transform coefficients as Laplacian distributions, many wavelet shrinkage based denoising methods such as the classical soft-thresholding [Don95] have been proposed. Chang et al. modeled the wavelet transform coefficients as generalized Gaussian distribution, and proposed the BayesShrink [Cha+00] algorithm. By considering the correlation of wavelet coefficients across scales, Portilla et al. [Por+03] proposed to use Gaussian Scale Mix-

tures for image modeling and achieved promising denoising performance. It is widely accepted that natural image gradients exhibit heavy-tailed distributions [WF07], and the total variation (TV) based methods [Rud+92; Osh+05] actually assume Laplacian distributions of image gradients for denoising. The Fields of Experts (FoE) [RB09] proposed by Roth and Black models the filtering responses with Student's t-distribution to learn filters through Markov Random Field (MRF) [Bis06]. Recently, Schmidt and Roth proposed the cascade of shrinkage fields (CSF) to perform denoising efficiently [SR14].

Instead of modeling the image statistics in some transformed domain (e.g., gradient domain, wavelet domain or filtering response domain), another popular approach is to model the image priors on patches. One representative is the sparse representation based scheme which encodes an image patch as a linear combination of a few atoms selected from a dictionary [OF96; OF97; EA06]. The dictionary can be chosen from the off-the-shelf dictionaries (e.g., wavelets and curvelets), or it can be learned from natural image patches. The seminal work of K-SVD [Aha+06; EA06] has demonstrated promising denoising performance by dictionary learning, which has yet been extended and successfully used in various image processing and computer vision applications [Mai+08a; Wri+10; Jia+13]. By viewing image patches as samples of a multivariate variable vector and considering that natural images are non-Gaussian, Zoran and Weiss [ZW11; ZW12] and Yu et al. [Yu+12] used Gaussian Mixture Model (GMM) to model image patches, and achieved state-of-the-art denoising and image restoration results, respectively.

2.2 Realistic Color Image Denoising

During the last decade, a few methods have been proposed for real color image denoising. Among them, the CBM3D method [Dab+07a] is a representative one, which first transforms the RGB image into a luminance-chrominance space (e.g., YCbCr) and then applies the benchmark BM3D method [Dab+07b] to each channel separately. The non-local similar patches are grouped by the luminance channel. In [Liu+08], Liu et al. proposed the "Noise Level Function" to estimate and remove the noise for each channel in natural images. However, processing each channel separately would often achieve inferior performance to processing the color channels jointly [Mai+08b]. Therefore, the methods [Leb+15; Leb+; Zhu+16] perform real

color image denoising by concatenating the patches of RGB channels into a long vector. However, the concatenation treats each channel equally and ignores the different noise statistics among these channels. The method in [Nam+16] models the cross-channel noise in real noisy images as multivariate Gaussian and the noise is removed by the Bayesian non-local means filter [Ker+07]. The commercial software Neat Image [ABS] estimates the noise parameters from a flat region of the given noisy image and filters the noise accordingly. The methods in [Nam+16; ABS] ignore the non-local self-similarity of natural images [Dab+07b; Gu+14].

External Non-local Self-Similar ity of Prior for Additive White Gaussian Noise

Innovation distinguishes between a leader and a follower.

— Steve Jobs
(CEO Apple Inc.)

3.1 Introduction



Fig. 3.1: Figure example: (*a*) example part one, (*c*) example part two; (*c*) example part three

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

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Fig. 3.2: Another Figure example: (*a*) example part one, (*c*) example part two; (*c*) example part three

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3.2 System Design

3.3 Demo System

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

3.4 Calibration

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3.5 Conclusion

External Prior Guided Internal Prior Learning for Real Noisy Image Denoising

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(CEO Apple Inc.)

4.1 Learning External Nonlocal Self-Similarity Priors



Fig. 4.1: Figure example: (*a*) example part one, (*c*) example part two; (*c*) example part three

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Fig. 4.2: Another Figure example: (*a*) example part one, (*c*) example part two; (*c*) example part three

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4.5 Conclusion

Internal Nonlocal Self-Similarity Prior for Real Color Image Denoising: A Low Rank based Method

Users do not care about what is inside the box, as long as the box does what they need done.

— Jef Raskin about Human Computer Interfaces

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

5.1 Introduction

5.2 Related Work

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

5.3 Method

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

5.4 Experimental Results

5.5 Summary

Internal Nonlocal Self-Similarity Prior for Real Color Image Denoising: A Sparse Coding based ethod

Users do not care about what is inside the box, as long as the box does what they need done.

— **Jef Raskin** about Human Computer Interfaces

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6.1 Introduction

6.2 Related Work

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6.3 Summary

A Large Real Noisy Image Dataset, with A Comprehensive Evaluation of State-of-the-arts

Users do not care about what is inside the box, as long as the box does what they need done.

— **Jef Raskin** about Human Computer Interfaces

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7.1 Introduction

7.2 Related Work

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7.3 Summary

Conclusions

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

8.1 Section 1

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

8.2 Section 2

8.3 Future Work

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