

Human-Level Control Through Deep Reinforcement Learning

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Overview

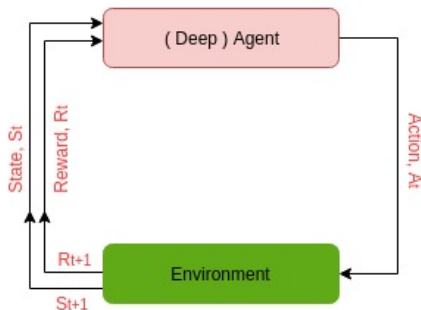
- 1 AI Learning
- 2 Deep Reinforcement Learning(Deep RL)
- 3 Markov Decision Process(MDP)
- 4 Bellman Equation
- 5 Deep Q-Network(DQN)

AI Learning

Supervised Learning	Unsupervised Learning	Reinforcement Learning
<ul style="list-style-type: none">• Data and Labels• Learn a function to map data to its label• Classification, Regression, Object detection	<ul style="list-style-type: none">• Non labelled data• Learn some hidden structure of the data• Clustering, Association, Dimensionality reduction	<ul style="list-style-type: none">• Time delayed label• Learn how to take actions in order to maximize reward• Game, Control and Information theory, Robotics, Genetic algorithms

Deep Reinforcement Learning

- Deep RL = RL + Deep Learning



- Agent interacts with an environment through a sequence of observations(states), actions and rewards.
- **Goal** of the agent is to select actions in a fashion that maximizes cumulative future reward.

Markov Decision Process(MDP)

- MDP provide mathematical formation for the RL problem.
- Current state completely characteristics the state of the world.
- MDP is defined by five tuples :
 - ① S: set of finite states.
 - ② A: set of finite actions.
 - ③ R: Immediate reward received after transitioning from one state to another due to some action.
 - ④ Transition Probability(\mathbb{P}): Probability of transitioning from one state to another.
 - ⑤ Discount Factor($\gamma \in [0, 1)$): Represents the difference in importance between future and present rewards.

MDP: Policy

- A **policy** is a function $\pi : S \rightarrow A$ that specifies what action the agent should take in any given state.
- Policy can be of two type :
 - ① **Deterministic Policy** : Action depend on input, $\pi : S \rightarrow A$
 - ② **Stochastic Policy** : Agent choose the action randomly, $\pi : S \times A \rightarrow [0, 1]$
 $\pi(a|s) = P(A_t = a | S_t = s)$
- **Optimal policy π^*** : policy that maximize cumulative reward function.

$$\pi^* = \operatorname{argmax}_{\pi} \mathbb{E} \left[\sum_{t \geq 0} \gamma^t r_t \mid \pi \right]$$

- **Cumulative future reward** is the discounted sum of future rewards throughout an episode.

$$R = \sum_{t=0}^T \gamma^t r_t$$

Value Functions

- ① **State Value Function** : returns the expected reward for selecting a certain state s .
 - $V^\pi = \mathbb{E}_\pi [R_t \mid s_t = s]$
- ② **Action Value Function** : returns the expected reward for using action a in a certain state s
 - $Q^\pi(s, a) = \mathbb{E}_\pi [R_t \mid s_t = s, a_t = a]$
 - **Optimal Action value function**: maximum sum of rewards discounted by γ at each time step t , achievable by a behaviour policy π , after making an observation (s) and taking an action (a).
 - $Q^*(s, a) = \max_\pi \mathbb{E} [r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots \mid s_t, a_t, \pi]$

Bellman Equation

- In MDP value of any state can be written as sum of immediate reward and value of state that follows.
- $V^\pi = \mathbb{E}_\pi [r_{t+1} + \gamma V^\pi(s_{t+1}) \mid s_t = s]$

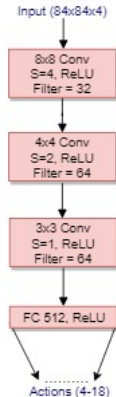
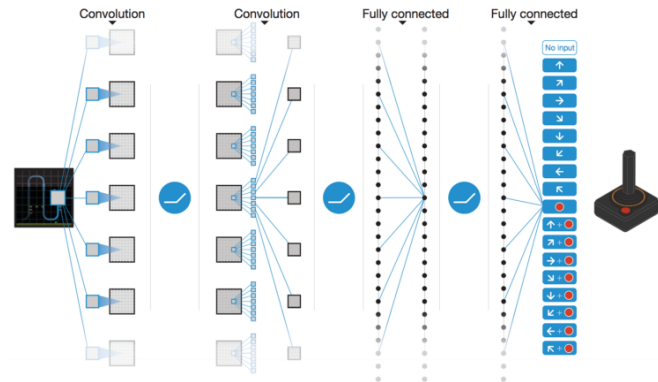
Deep Q-Network(DQN)

- DQN combine RL with deep neural networks.
- DQN agent receive only the pixels and the game score as inputs.
- Learn successful policies directly from high dimensional sensory inputs using end to end deep q-network agent.
- Proposed DQN is tested on 49 Atari games.
- **Challenge :**
 - RL is unstable when a nonlinear function approximator is used to represent action value function.
 - correlation between sequence of observations may updates in Q that can change the policy.

Nobel Variant of Q-Learning - Deep Convolutional Neural Network

- Correlation between observations can be address with two key ideas
 - ① **Experience Replay** randomize over data to remove correlation and smooth over changes in data distribution.
 - ② **An iterative Update** adjusts the action value toward target that updates periodically to reduce correlation.
- Stable method for training neural network in RL setting are **Neural Fitted Q-iteration**
 - Involves the repeated training of network on hundreds of iterations.
 - Inefficient for large neural networks.
- Approximate value function can efficiently parameterize using **Deep Convolutional Neural Network** to perform experience replay.

Architecture



Algorithm

- Deep Q-learning with experience replay

Initialize replay memory D to capacity N

Initialize action-value function Q with random weights θ

Initialize target action-value function \hat{Q} with weights $\theta^- = \theta$

For episode = 1, M **do**

 Initialize sequence $s_1 = \{x_1\}$ and preprocessed sequence $\phi_1 = \phi(s_1)$

For $t = 1, T$ **do**

 With probability ϵ select a random action a_t

 otherwise select $a_t = \operatorname{argmax}_a Q(\phi(s_t), a; \theta)$

 Execute action a_t in emulator and observe reward r_t and image x_{t+1}

 Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$

 Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in D

 Sample random minibatch of transitions $(\phi_j, a_j, r_j, \phi_{j+1})$ from D

 Set $y_j = \begin{cases} r_j & \text{if episode terminates at step } j+1 \\ r_j + \gamma \max_{a'} \hat{Q}(\phi_{j+1}, a'; \theta^-) & \text{otherwise} \end{cases}$

 Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ with respect to the network parameters θ

 Every C steps reset $\hat{Q} = Q$

End For

End For

- Uses Raw Atari 2600 frames which are 210x160 pixel images.
- **Data Preprocessing**
 - 1 Encode a single frame by take the maximum value for each pixel colour value over the frame being encoded and the previous frame.
 - 2 Extract the Y channel, also known as luminance, from the RGB frame and re-scale it to 84x84.

Estimating the Q-Network

- Loss function is the simple squared error

$$L = \mathbb{E}[(r + \gamma \max_{a'} Q(s', a') - Q(s, a))^2]$$

- Q-Learning gradient

$$\frac{\partial L(w)}{\partial(w)} = \mathbb{E}[(r + \gamma \max_{a'} Q(s', a') - Q(s, a)) \frac{\partial Q(s, a, w)}{\partial(w)}]$$

- Optimize objective end-to-end by SGD(stochastic gradient descent).

References

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- ② Daiki Kimura, "DAQN: Deep Auto-encoder and Q-Network", arXiv:1806.00630v1 [cs.CV] 2 Jun 2018.
- ③ <http://cs231n.stanford.edu/>
- ④ <https://www.theschool.ai/courses/move-37-course/>

Thank You