Selected Notes on Infinite Series

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1 Geometric series

A geometric series is $\sum_{n=0}^{\infty} a_n$ where each term is a multiple r of the previous, i.e. $a_{n+1} = ra_n$ for all $n \geq 0$.

Theorem If $|r| < 1$, then the series converges with the sum $\frac{a_0}{1-r}$. If $|r| \geq 1$, it diverges.

Theorem If $\lim_{n\to\infty} a_n \neq 0$ or the limit does not exist, then $\sum a_n$ diverges.