## Exercise 11: Feature Selection and Clustering

### May 9, 2017

Load the provided dataset for this exercise using load ex11. There, you'll find two variables:  $\mathtt{data} - \mathtt{a}\ 300 \times \mathtt{2}\ \mathtt{matrix}\ \mathtt{representing}\ \mathtt{three}\ \mathtt{hundred}$  2-dimensional data points, and  $\mathtt{true\_labels} - \mathtt{a}\ 300 \times \mathtt{1}\ \mathtt{vector}\ \mathtt{of}\ \mathtt{integers}$  associating each data point to one of the clusters.

## 1 Clustering using Lloyd's algorithm

Implement the k-means algorithm using Lloyd's method.

### 1.1 Initialize the centroids (k = 3)

Randomly pick 3 distinct data points (out of the N = 300) to be the initial centroids.

IMPORTANT NOTICE: Run the command rng(2015); before choosing the centroids. This command initializes your computer's random number generator and allows us to compare your answers to ours.

Hint: Use the randperm(N, k) function. Note that it would be wrong to just randomly pick 3 numbers between 1 and 300, because then you might get the same number twice.

#### 1.2 Calculate distance matrix

Calculate the distance between each data point and each centroid, and store the results in a  $N \times k$  matrix.

**Hint:** Use the function pdist2(X, Y, 'euclidean'); where X is the data matrix and Y is the matrix containing the centroids.

### 1.3 Associate each data point to the closest centroid

Find the index of the closest centroid to each point. A cluster will be the set of all the points associated to a specific centroid.

Hint: [ $\sim$ , closest\_centroid] = min(distances, [], 2);, where distances is the result from the previous question. Note that the [] tells MATLAB to ignore the second argument and then use 2 as the dimension over which to minimize. Try min(distances, 2) and see what happens.

## 1.4 Move each centroid to the mean value of the cluster

Using a loop (i = 1:k), calculate the mean of cluster i and change the value of centroid i to that.

Hint: mean(data(closest\_centroid==i, :), 1);

#### 1.5 Plot results

Use a scatter plot to visualize the different clusters.

Hint: Use scatter(data(:,1), data(:,2), [], closest\_centroid).

# 1.6 Repeat steps 1.2 to 1.4 several times until convergence

After each iteration, use the scatter plot to see if there was any change in the clusters\*. If you don't see any change, that means the algorithm has converged on a solution. How many iterations did it take?

Hint: You can use MATLAB's ≪Run Section≫ option to do the iterations. To mark a section, place a double percent sign (%%) before and after the code you want to run. Also, if you use the command figure(1); before you make the plot, the program will replace the previous plot with the new one without creating a new window.

## 1.7 Compare the clusters to the true\_labels

In a separate figure, make another scatter plot with the true\_labels instead of the results from the clustering. Note that the colors can be different because the number of each cluster is arbitrary. Is the rightmost cluster the same in both plots (apart from the color, of course)? Do you spot any differences of the labels in the other two clusters? If so, why does the k-means algorithm converge to this different solution?

<sup>\*</sup> Bonus: write code that checks when the algorithm converged instead of plotting it and making the comparison yourself.

### 1.8 What happens when k is too large?

Repeat all the previous steps with k=5 (remember to initialize the random number generator again using rng(2015)). How many iterations did it take the algorithm to converge this time? Compare the clusters to the true labels again and describe what you see.

### 1.9 Importance of the initial choice of centroids

Repeat the same analysis but with another random seed – rng(2016). Did the algorithm converge to the same 5 clusters? Compare again the clusters to the true labels again and describe what you see.

### 1.10 Using the built-in MATLAB function

Use the Statistics and Machine Learning Toolbox implementation of kmeans (X, k), with k=3, and compare the clusters you get from it to the ones from Question 1.6.

## 2 Hierarchical Clustering and Dendrograms

Load again the gene expression data from exercise 9 (load ex9). Make a 12x4297 matrix containing the expression data from the following strains: strain02, strain03, strain06, strain08. Note that clustering algorithms always treat the rows as the different data-points, so you should transpose the expression matrices.

## 2.1 Clustering using k-means

First, initialize the random number generator again using rng(2015);. Then, apply the function kmeans(X, 4) on the combined data matrix (X). Did the algorithm successfully identify the 4 groups?

**Hint:** Note that now the data is not 2D (but rather 4297 dimensional), therefore you cannot visualize it in a scatter plot. Therefore, you must look at the cluster indices returned by k-means directly.

## 2.2 Hierarchical clustering

Create a hierarchical cluster tree for the same data with Z = linkage(X, 'average'). This function returns a matrix Z with three columns which represents the tree. To visualize the tree use dendrogram(Z).

Did the hierarchical clustering algorithm successfully identify the clusters? Among the four clusters (strains), which two are the closest? Which strain is the most distinct relative to the other 3?