

## Metabolic Regulation

16 March, 2017

Uwe Sauer & Jörg Stelling

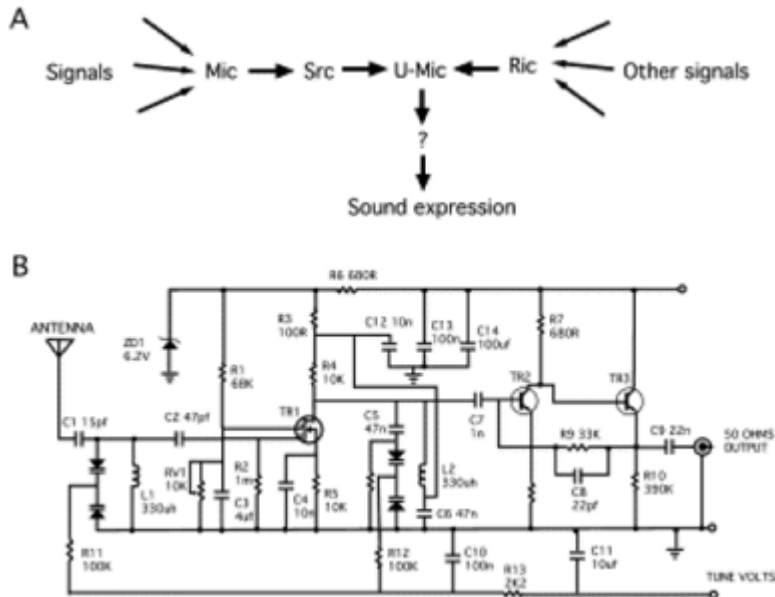
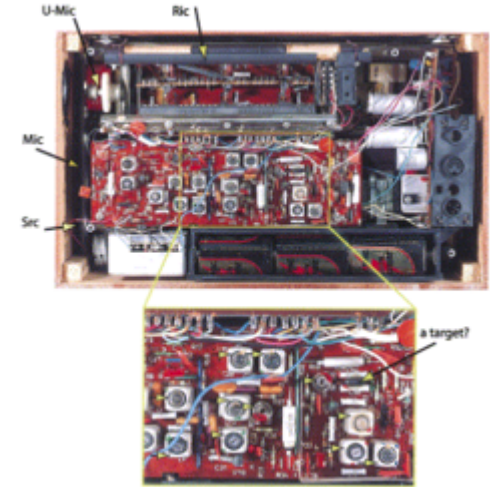
### Content:

- Metabolic regulation mechanisms & mechanistic interpretation of metabolite data
- Can engineers understand glycolytic control?
- Can a biologist improve control of glycolysis?

# Can Engineers Understand Metabolic Control?



“Conceptually, a radio functions similar to a signal transduction pathway; i.e. it converts a signal from one form into another. It has about 100 components - so somewhat similar to some biological systems.”

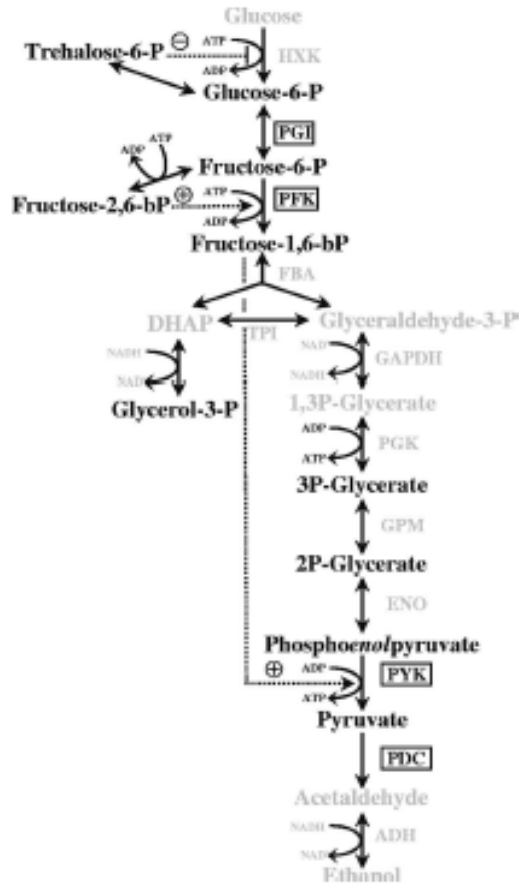


❑ 'Inverse' question:

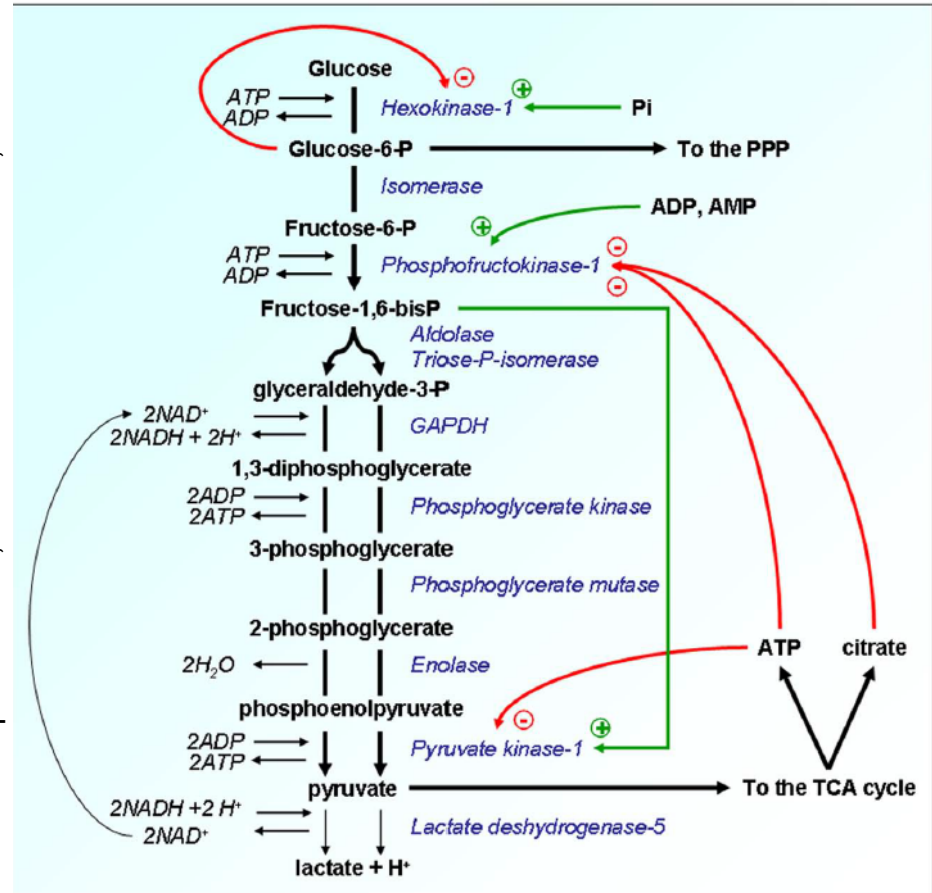
Can standardized,  
quantitative language and  
models help understand  
biological systems?

# Glycolysis in Eukaryotes is too Complicated

J. van den Brink et al., *Appl. Env. Microbiol.* 74: 5710, 2008



P. Porporato et al., *Frontiers Pharmacol.* 2: 49, 2011

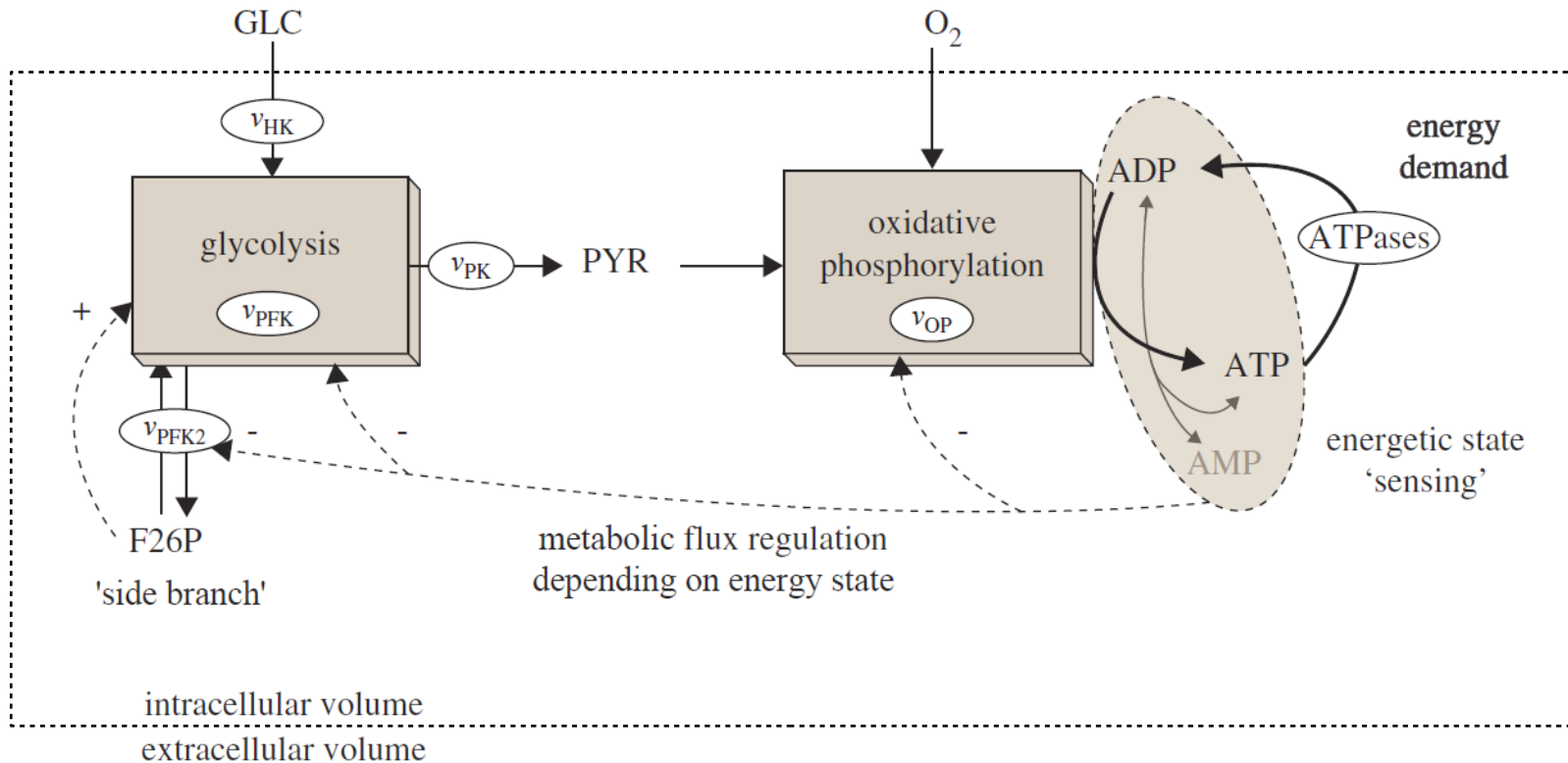


- Glycolytic regulation: There is not a single (biological) model → Standardize and focus.

# Aims of Regulation of Energy Metabolism?

- ❑ Stable dynamic behavior: Steady-state (no oscillations or chaotic behaviors).
- ❑ Fixed ATP concentration in the cell (despite fluctuating nutrient supply and energy demand).
- ❑ Tight dynamic control: Fast responses to perturbations (but without over- or undershoots).

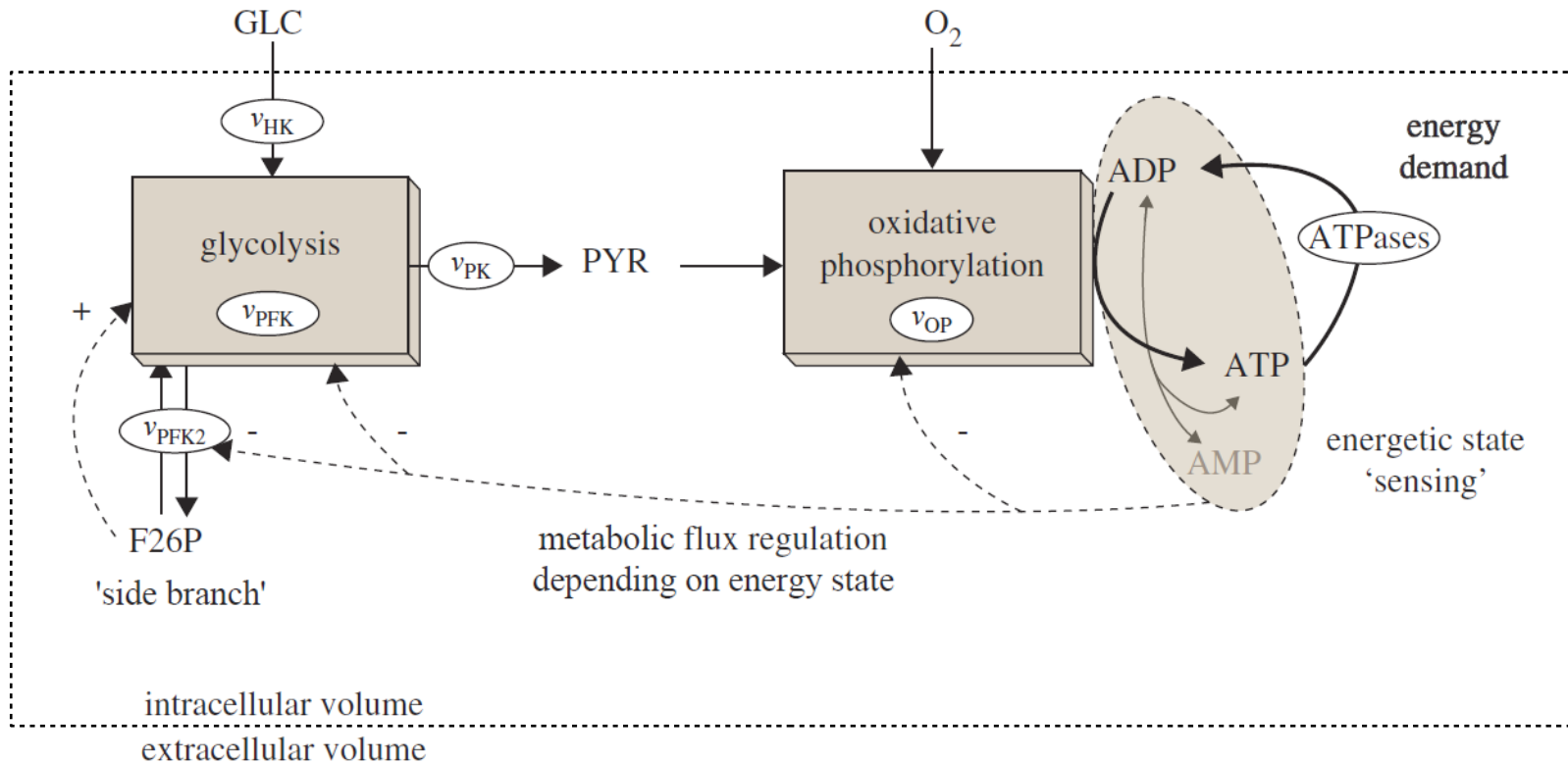
# A Simplified Model of Energy Metabolism



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ How does the eukaryotic cell achieve energy (ATP) homeostasis despite fluctuating demand?

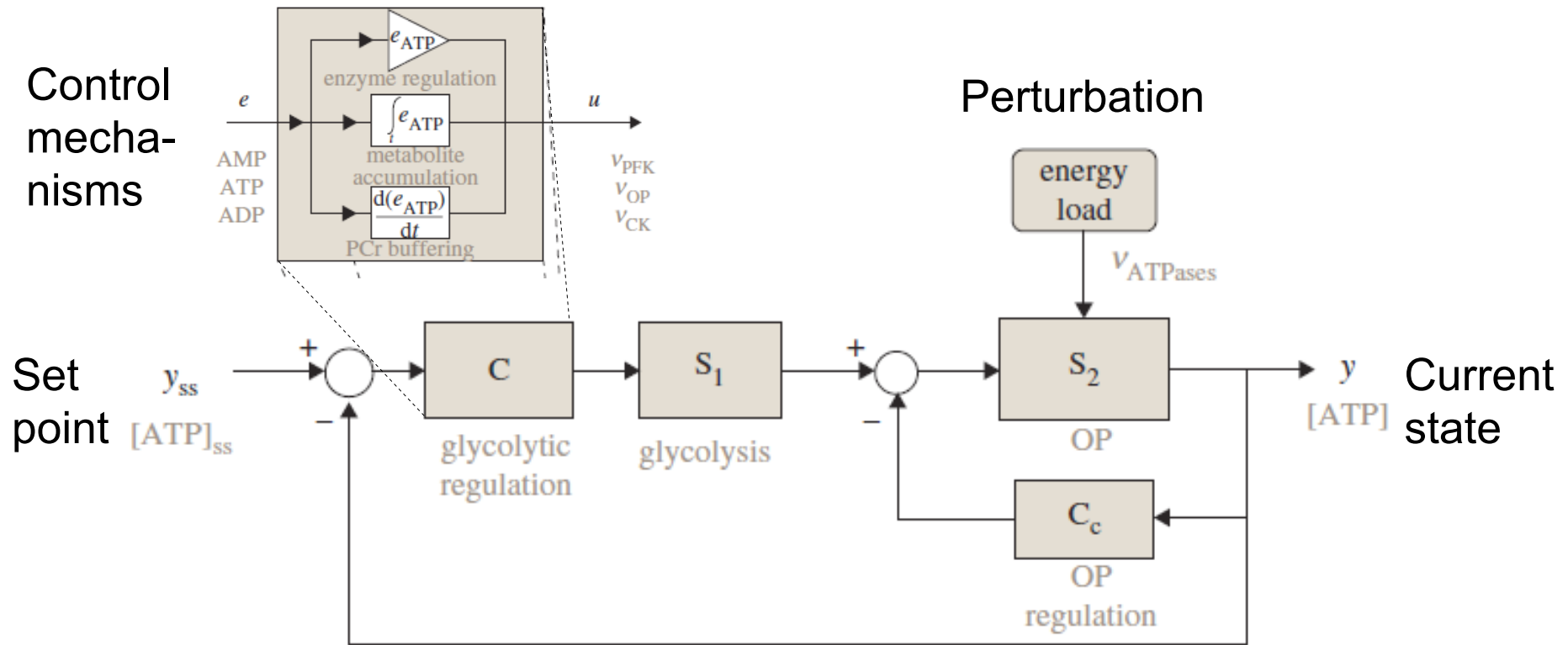
# A Simplified Model of Energy Metabolism



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ **Answer:** Feedback. But why so many feedback loops (evolution, robustness, function, ...)?

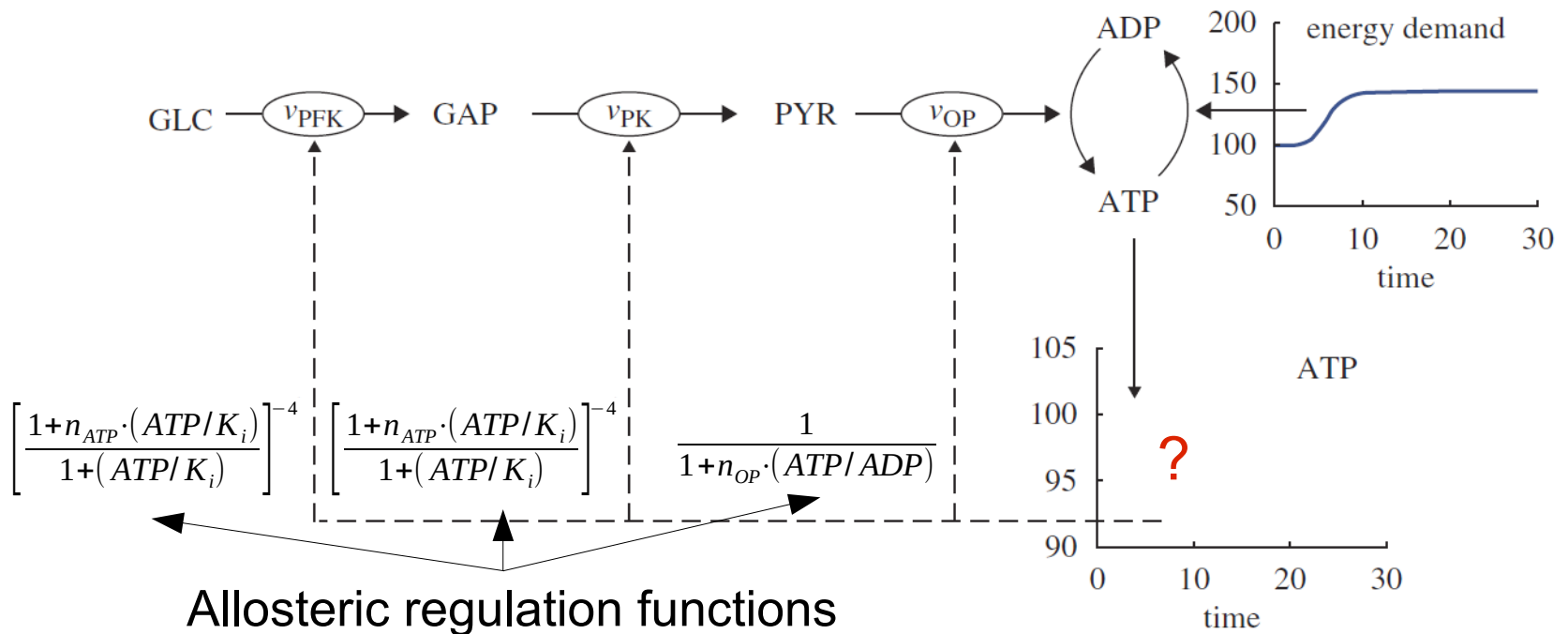
# An Engineer's View: Block Diagram



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ **Answer:** Feedback. But different types of (negative) feedback have different functions.

# What Does Allosteric Regulation Achieve?

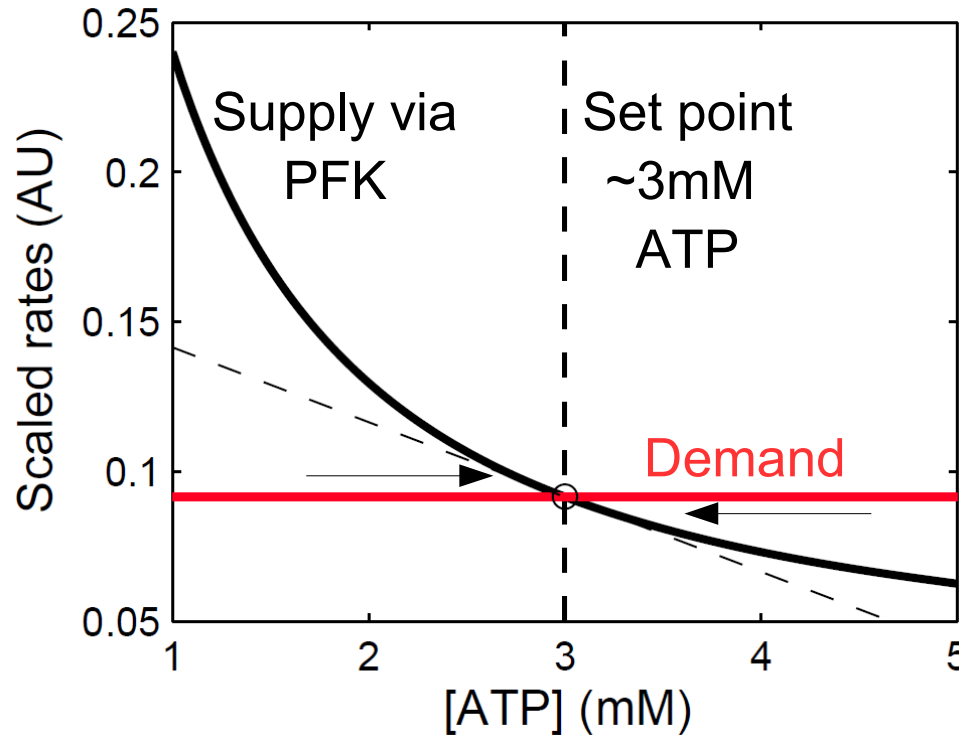


Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- Allosteric regulation establishes negative feedback on pathway flux depending on the current ATP concentration.

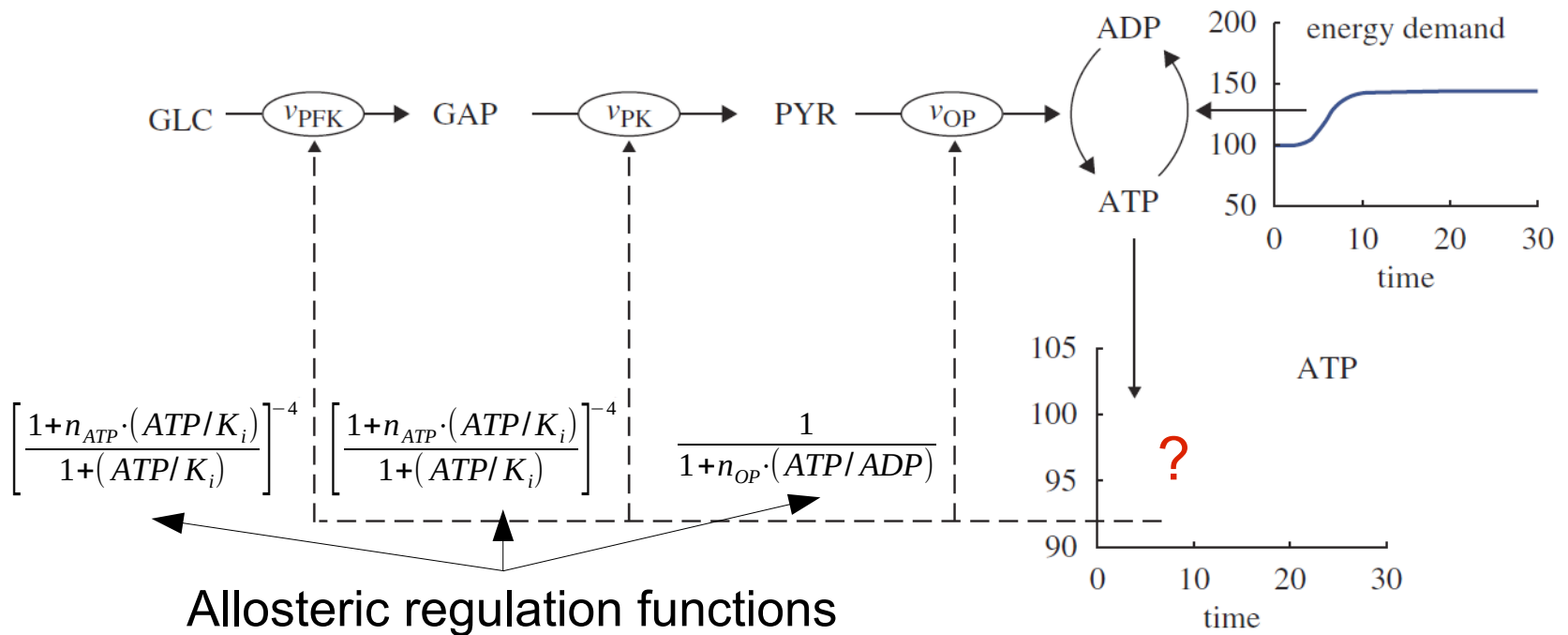


# What Does Allosteric Regulation Achieve?



- Allosteric inhibition of flux via PFK:  $v_{PFK} \propto \left[ \frac{1 + n_{ATP} \cdot (ATP/K_i)}{1 + (ATP/K_i)} \right]^{-4}$
- Approximately **proportional** negative feedback on ATP.

# What Does Allosteric Regulation Achieve?

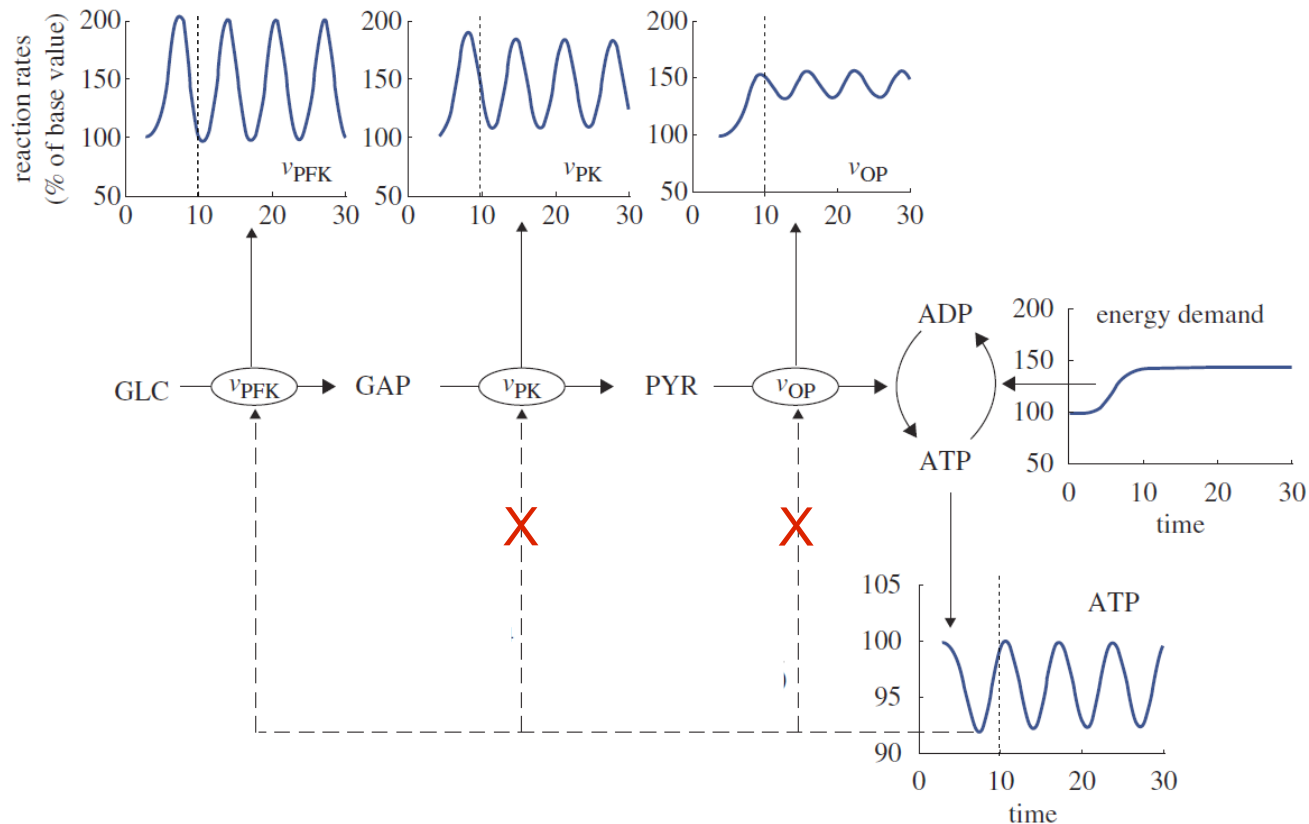


Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ Why three different control targets in energy metabolism?
- ❑ How to test the contributions of individual feedback loops?

# What Does Allosteric Regulation Achieve?

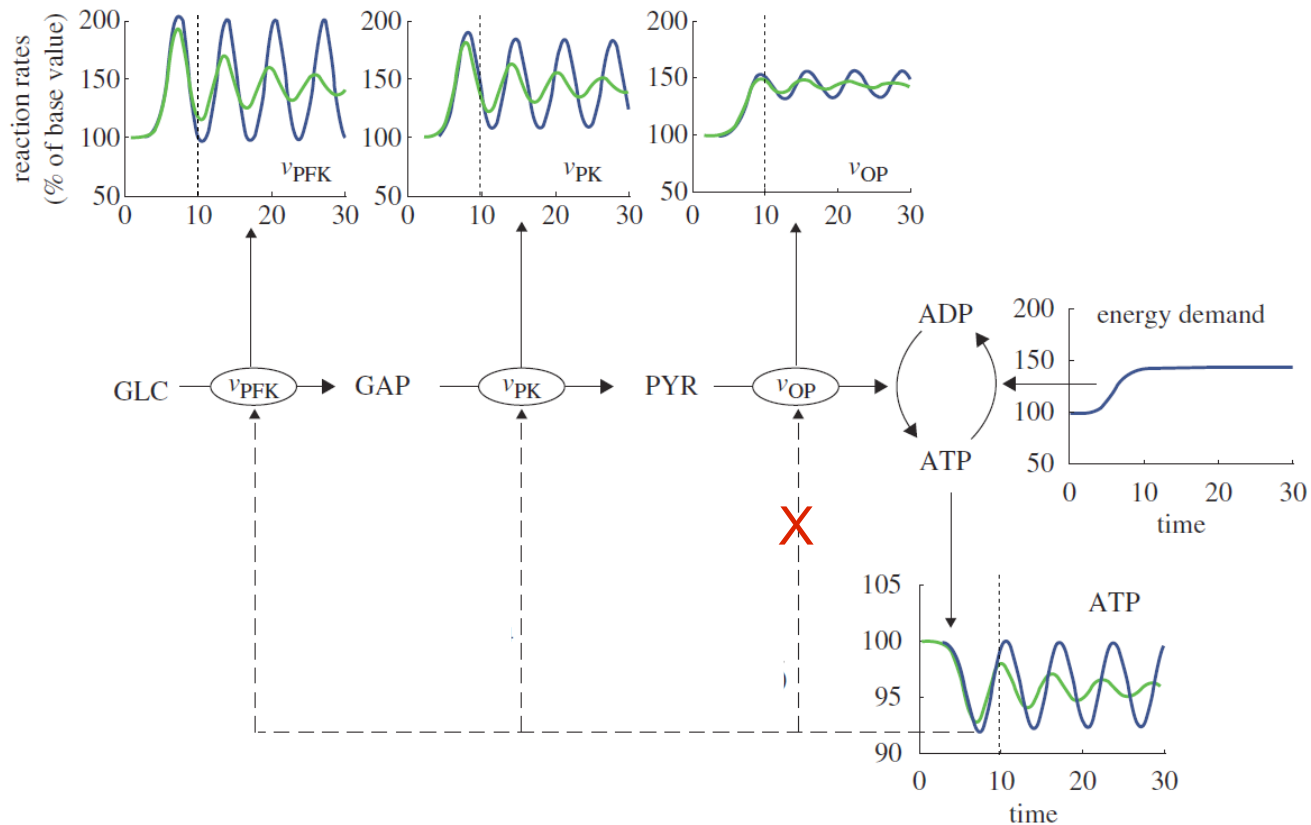
Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.



- ❑ Test of individual feedbacks by *in silico* knock-outs.
- ❑ Only 'long' PFK feedback → Time delay → Instabilities!

# What Does Allosteric Regulation Achieve?

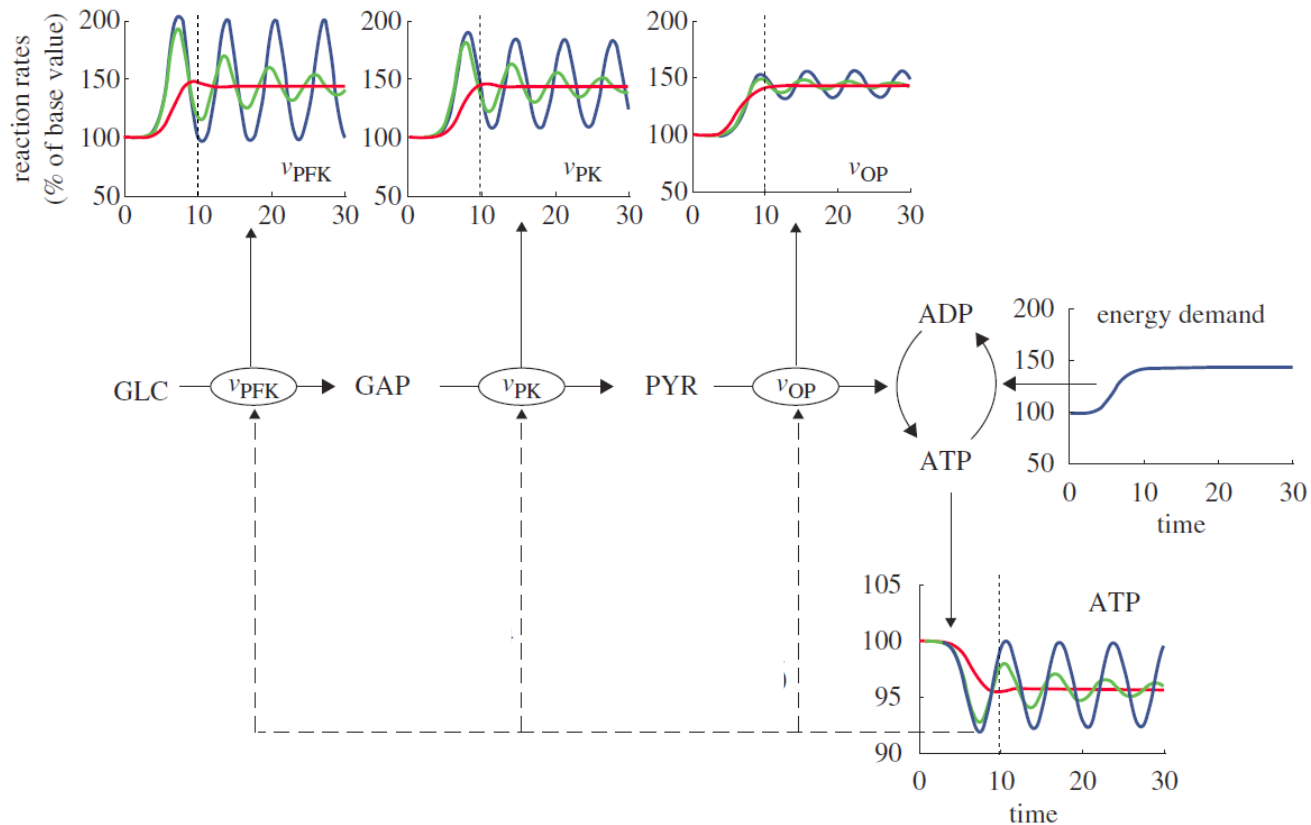
Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.



- ❑ Test of individual feedbacks by *in silico* knock-outs.
- ❑ Two (cascaded) feedbacks → Reduced instabilities.

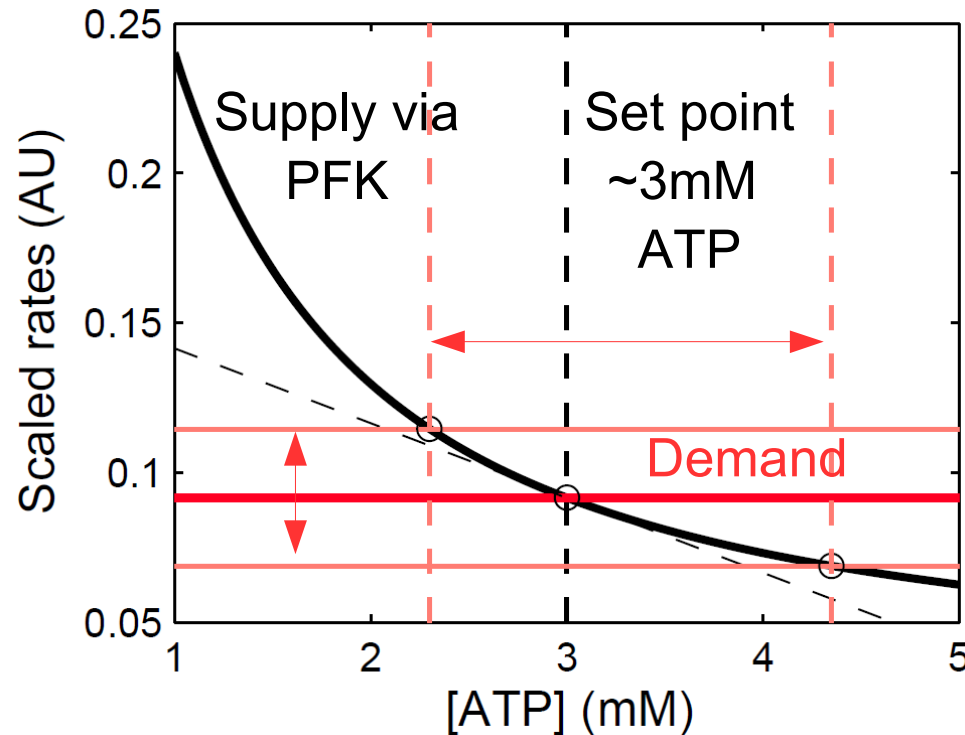
# What Does Allosteric Regulation Achieve?

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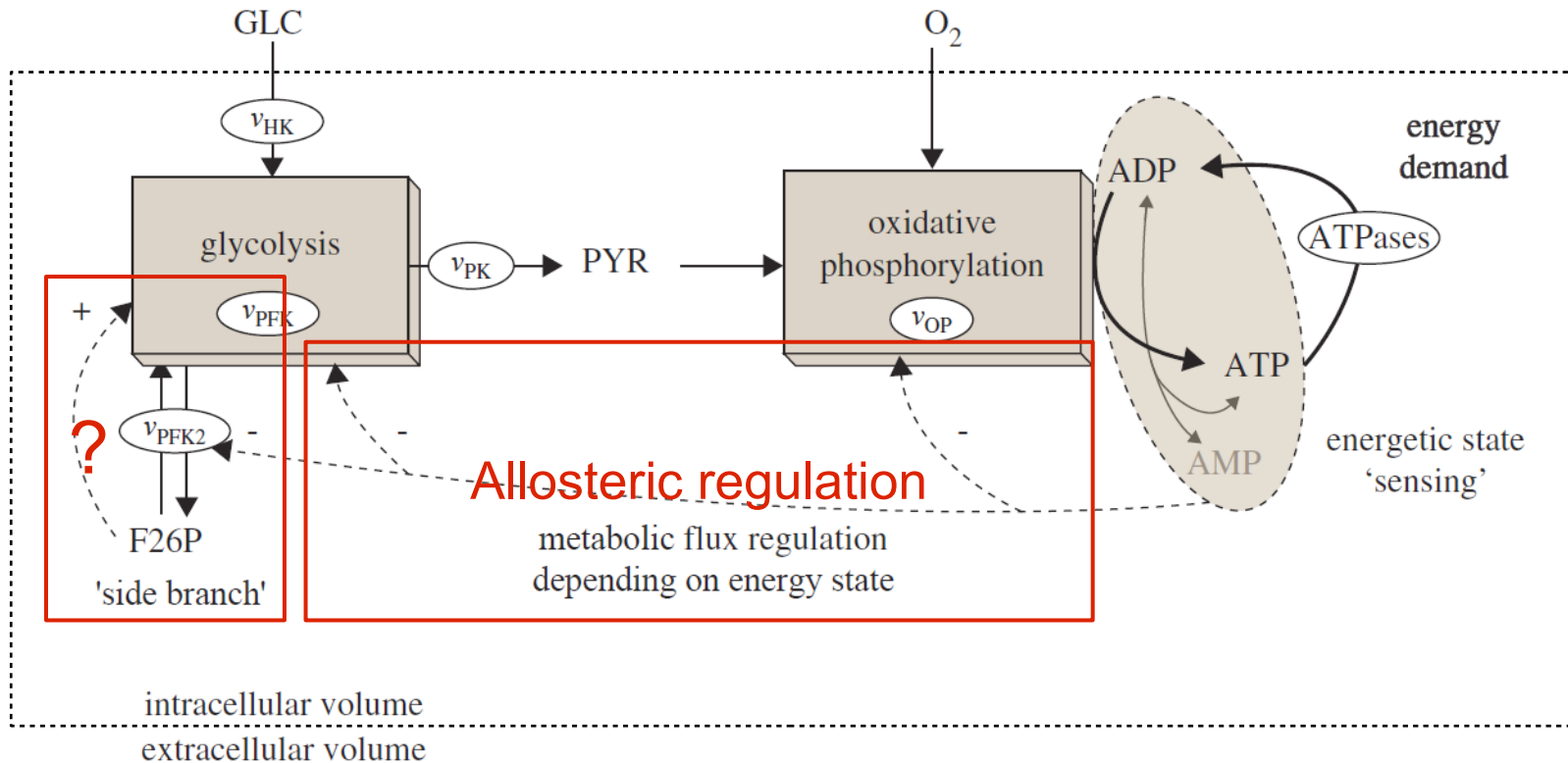
- ❑ Three (cascaded) feedbacks → Homeostasis achieved.
- ❑ But what is biologically 'wrong' with the ATP response?

# Limitations of Proportional Feedback



- ❑ **Problem:** Proportional feedback does not lead to the **same** steady-state ATP concentration for **different** demands → Large deviations from set point possible.

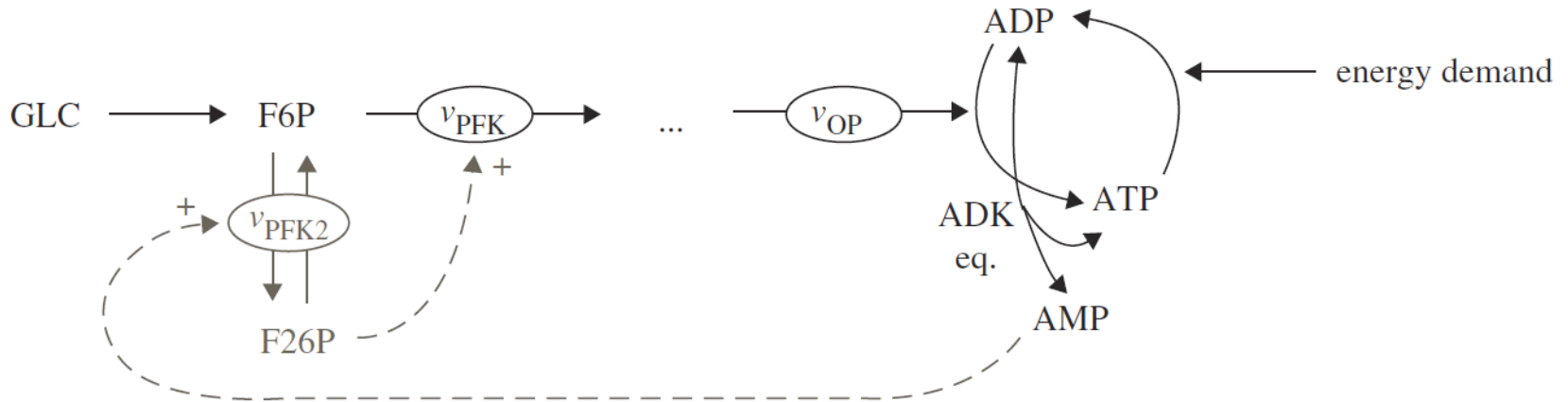
# Back to the Simplified Model



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

'Glycolysis is usually presented as a linear pathway with nine reactions. However, this representation neglects a very important side reaction, the PFK2. This reaction allows the accumulation of F26P, one of the strongest activators of glycolysis.'

# Feedback Regulation by PFK2

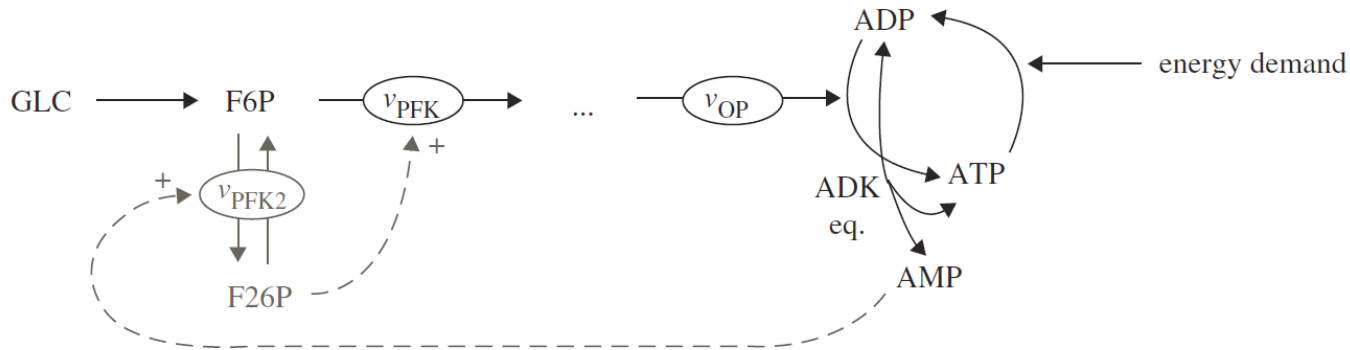


Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ AMP activates F26P production, which activates PFK → Another feedback loop in the system.
- ❑ Which type of feedback? Why different from the allosteric feedback loops already discussed?



# Integral Negative Feedback by PFK2



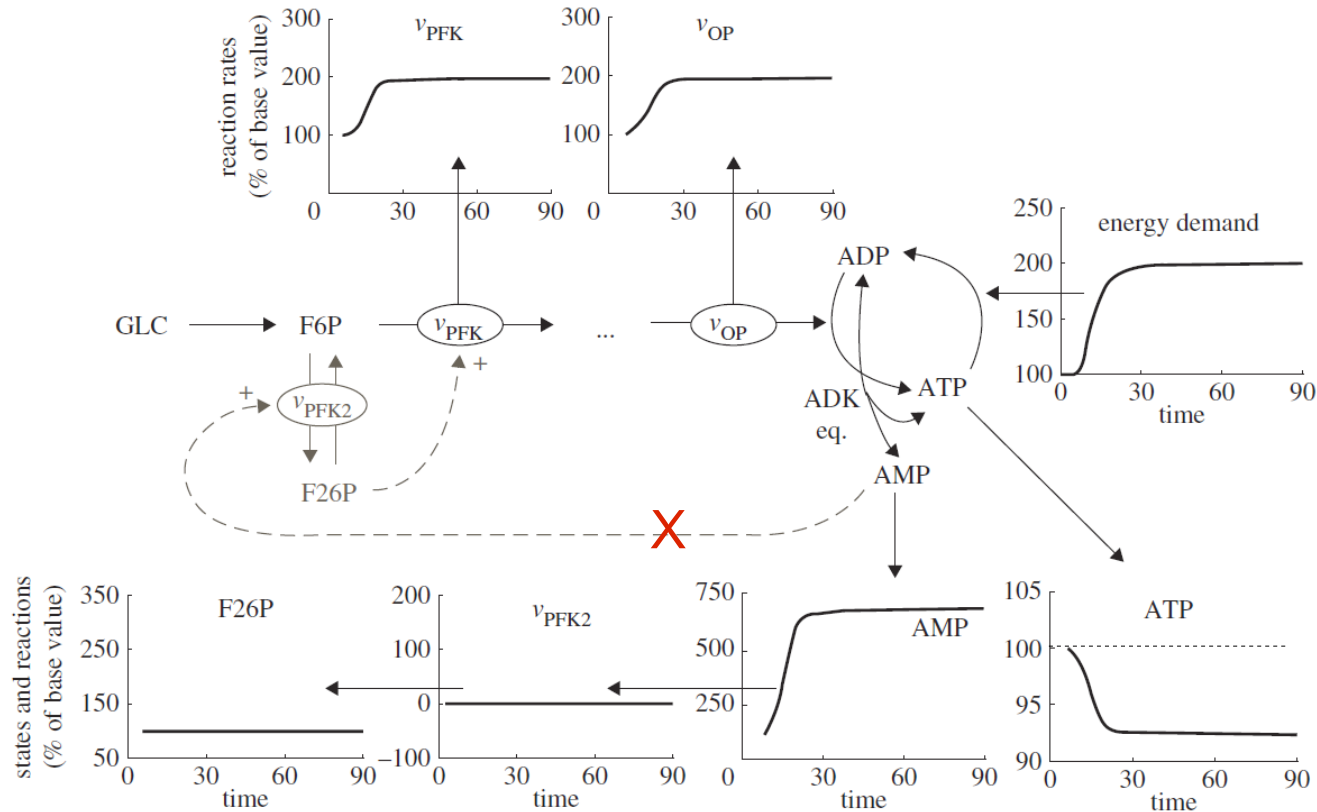
Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- If total AXP is conserved then  $[AMP]$  represents the '*error*' in the current energy (ATP) state.
- The negative feedback loop **integrates** the error:

$$\frac{d[F26P]}{dt} = v_{PFK2} \propto error \Rightarrow v_{PFK} \propto [F26P] \propto \int_t error$$

# Integral Negative Feedback by PFK2

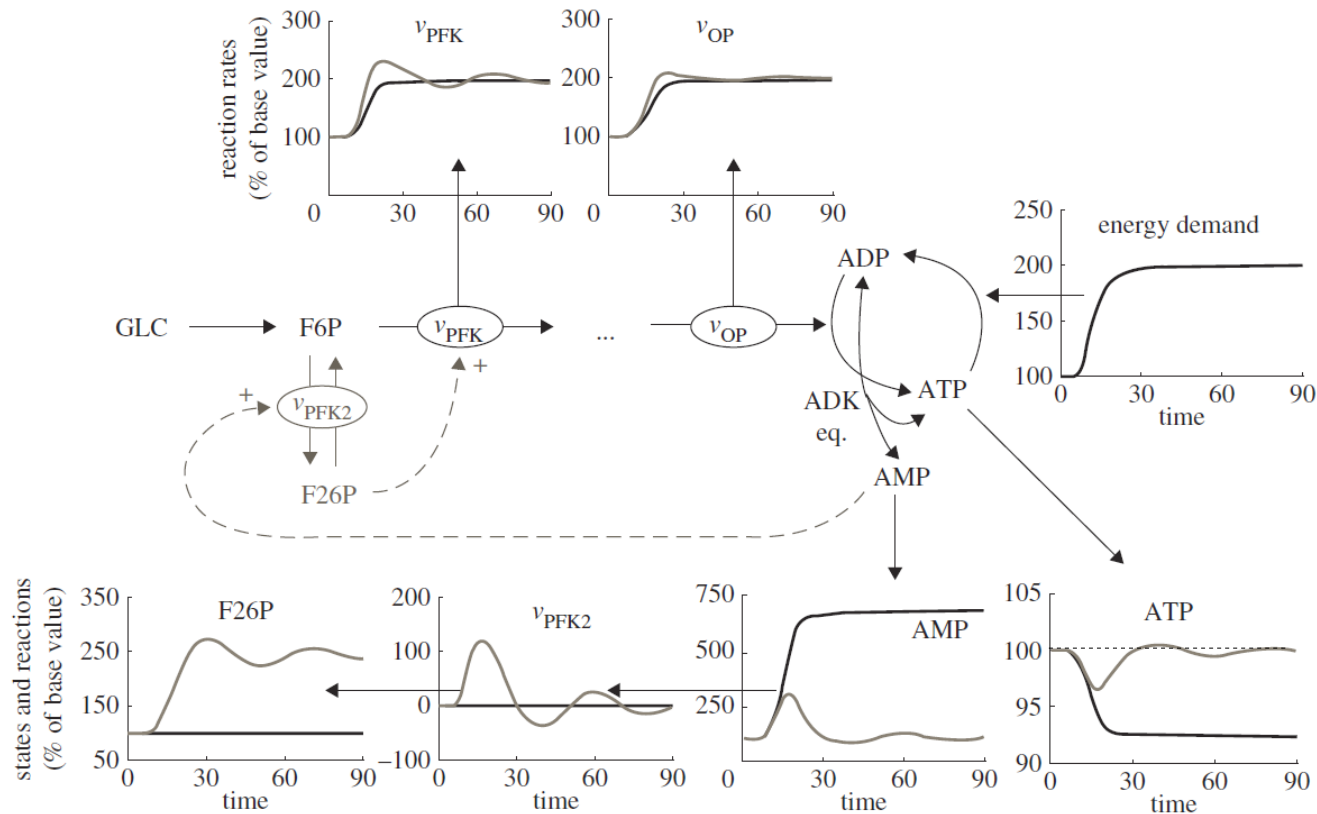
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- Without integral feedback: Deviation from ATP set-point.

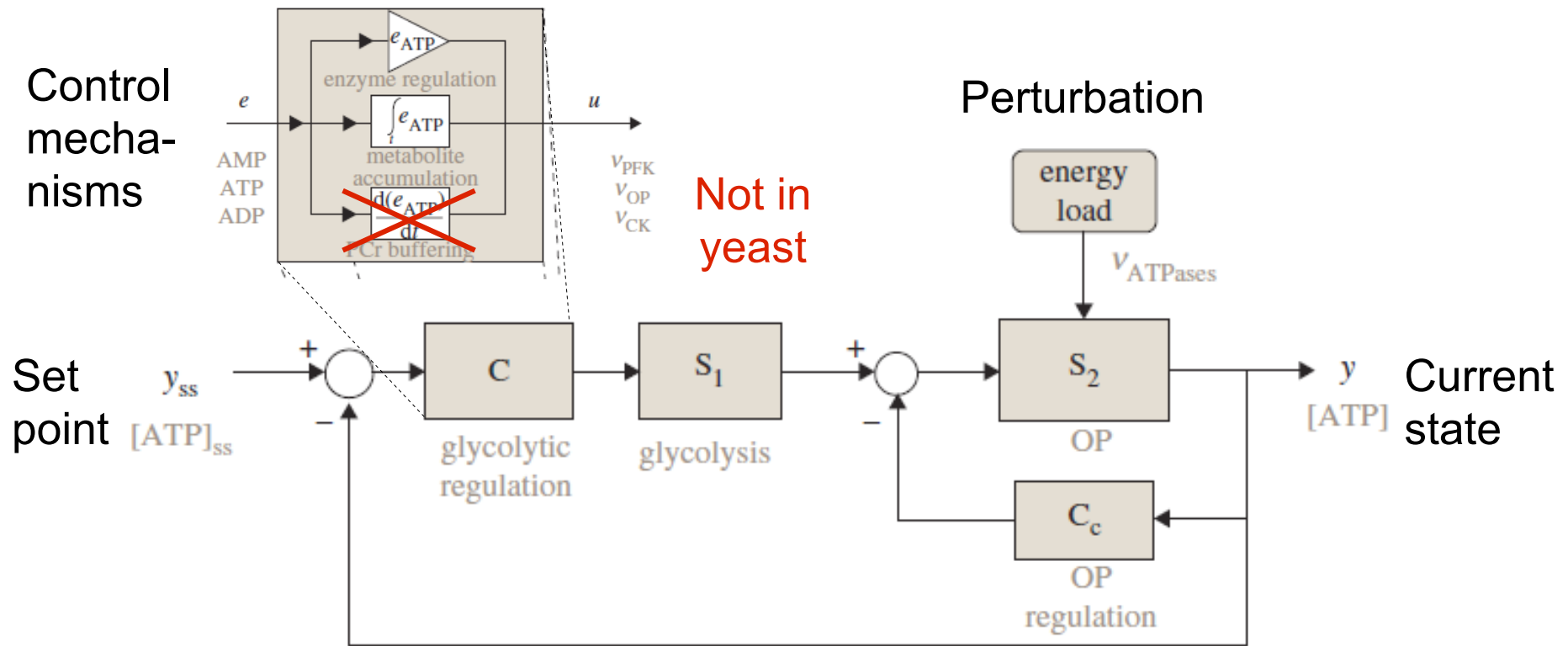
# Integral Negative Feedback by PFK2

Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.



- Without integral feedback: Deviation from ATP set-point.
- With integral feedback: **Adaptation** to varying demand.

# Summary: An Engineer's View



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- ❑ Control principles help understanding biological regulation.
- ❑ Unfortunately yeast is not perfect → Improvements?

## Metabolic Regulation

17 March, 2016

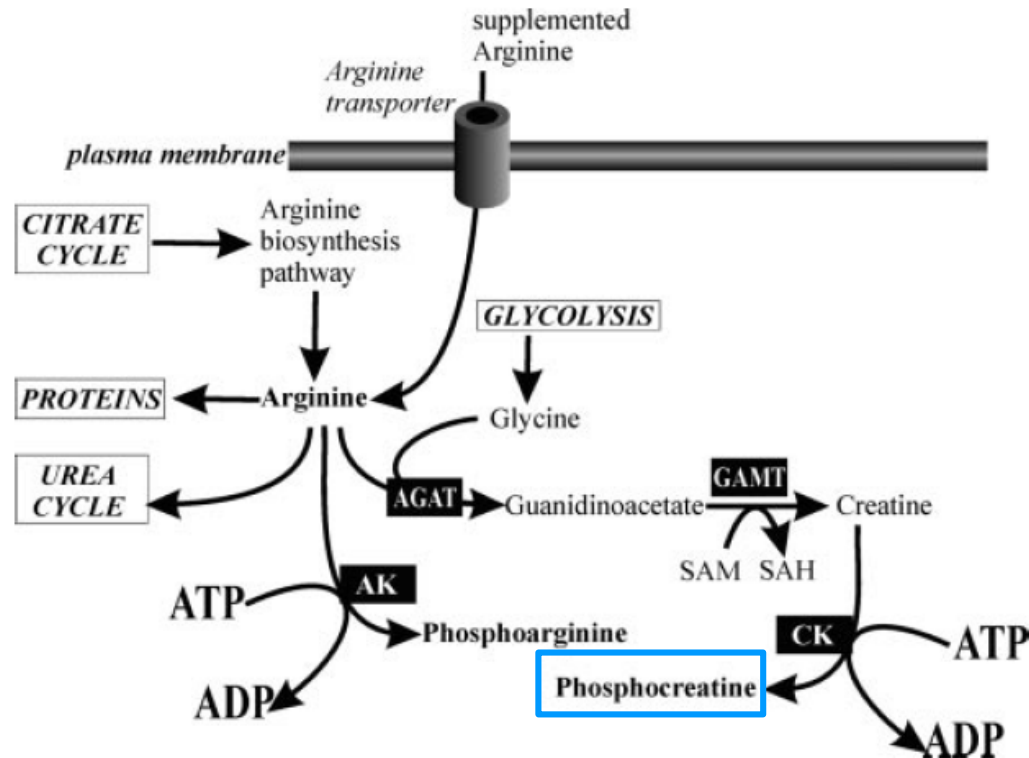
Uwe Sauer & Jörg Stelling

### Content:

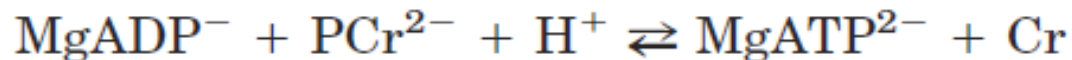
- Metabolic regulation mechanisms & mechanistic interpretation of metabolite data
- Can engineers understand glycolytic control?
- Can a biologist improve control of glycolysis?

# Engineering Phosphocreatine into Yeast

Figure from F. Canonaco et al., *J. Biol. Chem.* 277: 31303, 2002.

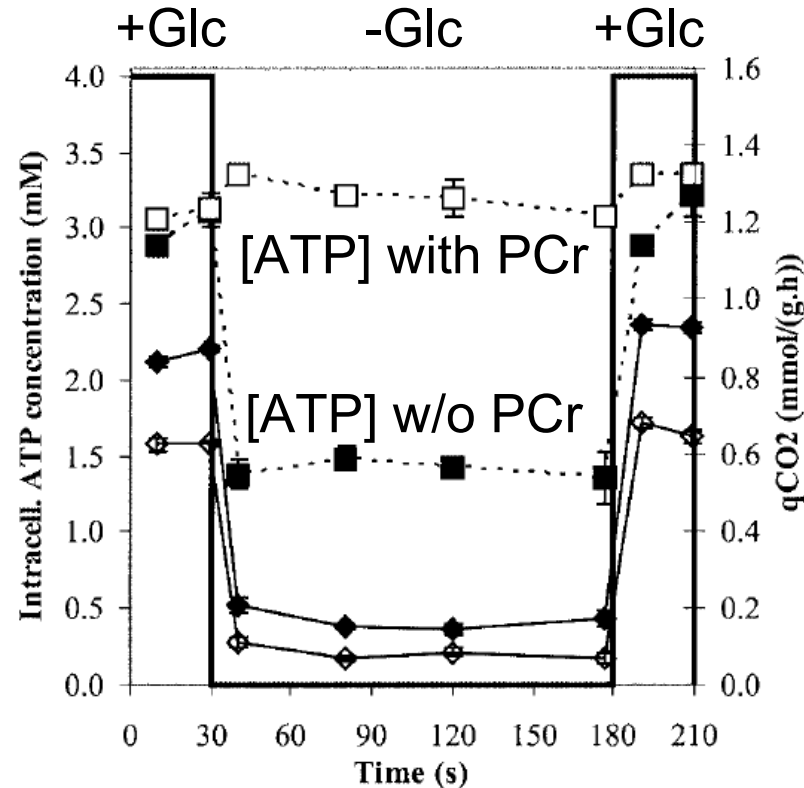


- Phosphocreatine (PCr): Metabolically inert equivalent of ATP → Buffer for replenishing ATP in mammals.



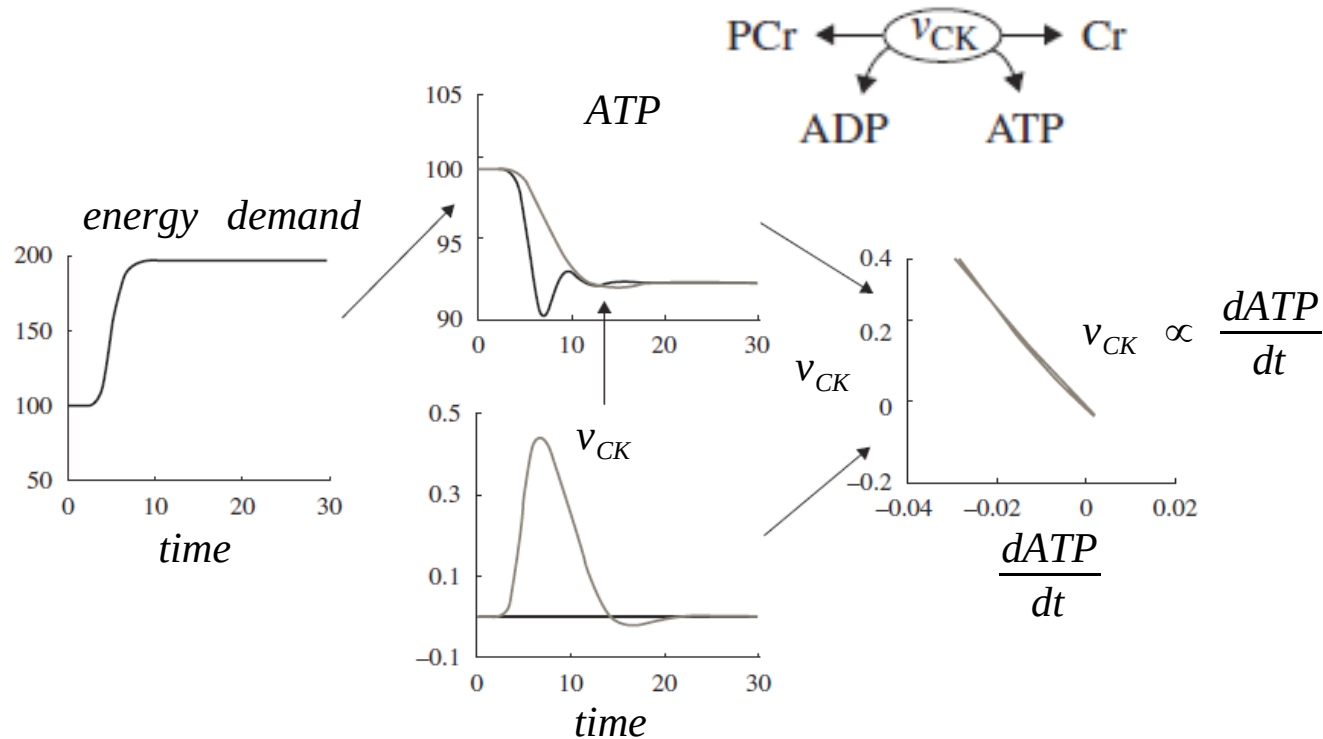
# Engineering Phosphocreatine into Yeast

Figure from F. Canonaco et al., *J. Biol. Chem.* 277: 31303, 2002.



- ❑ Phosphocreatine (Pcr) engineered yeast maintains the physiological ATP level during sudden starvation.

# Metabolic Buffers for Differential Control



Adapted from M. Cloutier & P. Wellstead, *J. R. Soc. Interface*, 2009.

- Buffers respond to the rate of change (**differential**) of the perturbation → Compensation for rapid changes.



# Teaching Goal III: Summary

- ❑ Cellular regulation involves many feedbacks because the cell has many control objectives. Which objectives?
- ❑ Multiple feedback loops can help prevent undesired system dynamics such as oscillations. How?
- ❑ Different types of negative feedback can be implemented in biological circuits to achieve specific behaviors / functions. Which types and functions? Examples?

# Exercise 5: Glycolysis Model

## Goal

- Formulate and implement an abstract representation of *E. coli* glycolysis, given its topology, parameters and initial conditions.
- Estimate model parameters using available experimental data.

**Note:** This is a simplified model.

