# LINKED LISTS, MUTABLE TREES AND MIDTERM REVIEW

### COMPUTER SCIENCE MENTORS 61A

March 18-March 22, 2024

## 1 Linked Lists

For each of the following problems, assume linked lists are defined as follows:

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance (rest, Link)
        self.first = first
        self.rest = rest
    def __repr__(self):
        if self.rest is not Link.empty:
            rest_repr = ', ' + repr(self.rest)
        else:
            rest_repr = ''
        return 'Link(' + repr(self.first) + rest_repr + ')'
    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'
```

Linked lists are a recursive data structure for representing sequences. They consist of a series of "links," each of which has two attributes: first and rest. The first attribute contains the value of the link (which can hold any type of data, even another linked list!). The rest attribute, on the other hand, is a pointer to another link or Link.empty, which is just a "None" type value.

For example, Link (1, Link (2, Link (3))) is a linked list representation of the sequence 1, 2, 3.

Like trees, linked lists naturally lend themselves to recursive problem solving. Consider the following example, in which we double every value in linked list. We double the value of the current link and then recursively double the rest.

1. What will Python output? Draw box-and-pointer diagrams along the way.

```
>>> a = Link(1, Link(2, Link(3)))
>>> a.first

>>> a.first = 5
>>> a.first

>>> a.rest.first

>>> a.rest.rest.rest.first
```

```
>>> a.rest.rest.rest.rest.first
>>> repr(Link(1, Link(2, Link(3, Link.empty))))
>>> Link(1, Link(2, Link(3, Link.empty)))
>>> str(Link(1, Link(2, Link(3))))
>>> print(Link(Link(1), Link(2, Link(3))))
```

2. Write a function combine\_two, which takes in a linked list of integers lnk and a two-argument function fn. It returns a new linked list where every two elements of lnk have been combined using fn.

3. Write a function middle\_node that takes as input a linked list lst. middle\_node should return the middle node of the linked list. If there are two middle nodes, return the second middle node.

```
def middle_node(lst):
  >>> head = Link(1, Link(2, Link(3, Link(4, Link(5)))))
  >>> middle_node(head)
  Link(3, Link(4, Link(5))) # The middle node of the list is node 3
  >>> head = Link(1, Link(2, Link(3, Link(4, Link(5, Link(6))))))
  Link(4, Link(5, Link(6))) # Since the list has two middle nodes with
     values 3 and 4, we return the second one
  list_iter, middle = _____, _____
  length = _____
  while _____:
     length = _____
     list_iter = _____
     middle = _____
  if length % 2 == 1:
     middle = _____
  return middle
Challenge version (Optional):
def middle_node(lst):
  list_iter, middle = _____, _____
  while _____ and _____:
     list_iter = _____
     middle = _____
  return middle
```

4. Write a recursive function <code>insert\_all</code> that takes as input two linked lists, <code>s</code> and <code>x</code>, and an index <code>index.insert\_all</code> should return a new linked list with the contents of <code>x</code> inserted at index <code>index</code> of <code>s</code>.

def	<pre>insert_all(s, x, index): """</pre>	
	<pre>&gt;&gt;&gt; insert = Link(3, Link(4)) &gt;&gt;&gt; original = Link(1, Link(2, Link(5))) &gt;&gt;&gt; insert_all(original, insert, 2) Link(1, Link(2, Link(3, Link(4, Link(5))))) &gt;&gt;&gt; start = Link(1) &gt;&gt;&gt; insert_all(original, start, 0) Link(1, Link(1, Link(2, Link(5)))) """</pre>	
	if and	:
	if and	:

For the following problems, use this definition for the Tree class:

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        self.branches = list(branches)

def is_leaf(self):
    return self.branches == []

# Implementation ommitted
```

Here are a few key differences between the Tree class and the Tree abstract data type, which we have previously encountered:

- Using the constructor: Capital T for the Tree class and lowercase t for tree ADT t = Tree(1) vs. t = tree(1)
- In the class, label and branches are instance variables and is\_leaf() is an instance method. In the ADT, all of these were globally defined functions.

```
t.label vs. label(t)
t.branches vs. branches(t)
t.is_leaf() vs. is_leaf(t)
```

• A Tree object is mutable while the tree ADT is not mutable. This means we can change attributes of a Tree instance without making a new tree. In other words, we can solve tree class problems non-destructively and destructively, but can only solve tree ADT problems non-destructively.

```
t.label = 2 is allowed but label(t) = 2 would error.
```

Apart from these differences, we can take the same general approaches we used for the tree ADT and apply them to the Tree class!

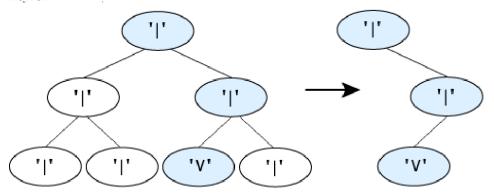
1. Define delete\_path\_duplicates, which takes in t, a tree with non-negative labels. If there are any duplicate labels on any path from root to leaf, the function should mutate the label of the occurrences deeper in the tree (i.e. farther from the root) to be the value -1.

def	<pre>delete_path_duplicates(t): """</pre>
	<pre>&gt;&gt;&gt; t = Tree(1, [Tree(2, [Tree(1), Tree(1)])]) &gt;&gt;&gt; delete_path_duplicates(t)</pre>
	>>> t Tree(1, [Tree(2, [Tree(-1), Tree(-1)])]) >>> t2 = Tree(1, [Tree(2), Tree(2, [Tree(2, [Tree(1, [Tree(5)])])])]) >>> delete_path_duplicates(t2)
	>>> t2 Tree(1, [Tree(2), Tree(2, [Tree(-1, [Tree(-1, [Tree(5)])])])]) """
	<b>def</b> helper():
	if:
	else:
	for in:

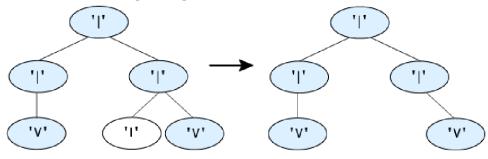
2. Given a tree t, mutate the tree so that each leaf's label becomes the sum of the labels of all nodes in the path from the leaf node to the root node.

### 3. *From Sp'22 MT2*:

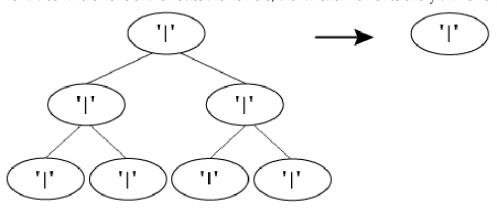
Implement *flower\_keeper*, a function that mutates a tree t so that the only paths that remain are ones which end in a leaf node with a Tulip flower ('V'). For example, consider this tree where only one path ends in a flower. After calling *flower\_keeper*, the tree has only three nodes left, the ones that lead to the flower:



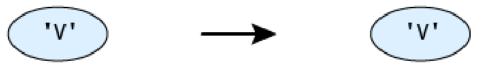
The shaded nodes in the diagram indicate paths that end in flowers. For this tree where two paths end in flowers, the tree keeps both paths that lead to flowers.



For a tree where none of the nodes are flowers, the function removes every branch except the root node.



For a tree with only a single node that is a flower, the function does not remove anything.



```
def flower_keeper(t):
   Mutates the tree T to keep only paths that end in flowers ('V').
   If a path consists entirely of stems ('|'), it must be pruned.
   If T has no paths that end in flowers, the root node is still kept.
   You can assume that a node with a flower will have no branches.
   >>> one_f = Tree('|', [Tree('|', [Tree('|'), Tree('|')]), Tree('|',
       [Tree('V'), Tree('|')])])
   >>> print(one_f)
        >>> flower keeper(one f)
   >>> one_f
   Tree('|', [Tree('|', [Tree('V')])])
   >>> print(one_f)
    >>> no_f = Tree('|', [Tree('|', [Tree('|'), Tree('|')]), Tree('|',
       [Tree('|'), Tree('|')])])
   >>> flower_keeper(no_f)
   >>> no f
   Tree('|')
   >>> just_f = Tree('V')
   >>> flower keeper(just f)
   >>> just_f
   Tree('V')
   >>> two_f = Tree('|', [Tree('|', [Tree('V')]), Tree('|', [Tree('|'),
       Tree('V')])])
   >>> flower_keeper(two_f)
   >>> two f
    Tree('|', [Tree('|', [Tree('V')]), Tree('|', [Tree('V')])])
   for b in _____:
    _____ = [____ for b in ____ if ____]
```

1. Write a function, make\_digit\_remover, which takes in a single digit i. It returns another function that takes in an integer and, scanning from right to left, removes all digits from the integer up to and including the first occurrence of i, starting from the ones place. If i does not occur in the integer, the original number is returned.

def	make	e_digit_remover(i):
		<pre>remove_two = make_digit_remover(2)</pre>
	>>> 23	remove_two(232018)
		remove_two(23)
	Ū	remove_two(99)
	"""	
	def	remove():
		removed =
		while > 0:
		removed = removed // 10
		if:
		return
	reti	ırn

1. Draw the box-and-pointer diagram.

```
>>> violet = [7, 77, 17]
>>> violet.append([violet.pop(1)])
>>> dash = violet * 2
>>> jack = dash[3:5]
>>> jackjack = jack.extend(jack)
>>> helen = list(violet)
>>> helen += [jackjack]
>>> helen[2].append(violet)
```

2. Write a function  $duplicate_list$ , which takes in a list of positive integers and returns a new list with each element x in the original list duplicated x times.

```
def duplicate_list(lst):
    """
    >>> duplicate_list([1, 2, 3])
    [1, 2, 2, 3, 3, 3]
    >>> duplicate_list([5])
    [5, 5, 5, 5, 5]
    """
    for ______:
    for ______:
```

3. Write a function that takes as input a number n and a list of numbers lst and returns True if we can find a subset of lst that sums to n.

## 5 Iterators and Generators

1. Write a generator function num\_elems that takes in a possibly nested list of numbers lst and yields the number of elements in each nested list before finally yielding the total number of elements (including the elements of nested lists) in lst. For a nested list, yield the size of the inner list before the outer, and if you have multiple nested lists, yield their sizes from left to right.

	yield .	 	 	
else:			 	
vield				

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