# SCHEME REVIEW AND LISTS Solutions

## COMPUTER SCIENCE MENTORS 61A

November 12 – November 15, 2024

1. Define apply-multiple which takes in a single argument function f, a nonnegative integer n, and a value x and returns the result of applying f to x a total of n times.

```
scm> (apply-multiple (lambda (x) (* x x)) 3 2)
256
scm> (apply-multiple (lambda (x) (+ x 1)) 10 1)
11
scm> (apply-multiple (lambda (x) (* 1000 x)) 0 5)
5
(define (apply-multiple f n x)
)
(define (apply-multiple f n x)
    (if (= n 0)
        Х
        (f (apply-multiple f (-n 1) x)))
Alternate solution:
(define (apply-multiple f n x)
    (if (= n 0)
        (apply-multiple f (- n 1) (f x)))
```

## **2** Scheme Lists

Unlike Python, all Scheme lists are linked lists. Recall that, in Python, a linked list is made up of Links that each have a first and a rest, where the rest is another Link. Similarly, each Scheme list is a "pair" where the first element of the pair is the first element of the list, and the second element of the pair is the rest of the list (also a pair).

We use the cons procedure to construct Scheme lists, and nil to represent empty lists. The sequence 1, 2, 3 may then be represented as follows:

```
scm> (cons 1 (cons 2 (cons 3 nil)))
```

```
(1 \ 2 \ 3)
```

The car and cdr procedures are used to access the elements of a Scheme list. car gets the first element of a list, while cdr gets the rest of the list:

```
scm> (define lst (cons 1 (cons 2 (cons 3 nil))))
lst
scm> (car lst)
1
scm> (cdr lst)
(2 3)
```

You can make the following analogy between linked lists in Python and Scheme:

```
Link(1, Link.empty)

a = Link(1, Link(2, Link.empty))

a.first

a.rest

(cons 1 nil)

(define a (cons 1 (cons 2 nil)))

(car a)

(cdr a)
```

The list procedure and quotation give us additional convenient ways to construct lists:

```
scm> (list 1 2 3)
(1 2 3)
scm> '(1 2 3)
(1 2 3)
scm> (list 1 (+ 1 1) 3)
(1 2 3)
scm> '(1 (+ 1 1) 3)
(1 (+ 1 1) 3)
```

Note that quotation will prevent any of the list items from being evaluated, which can occasionally be inconvenient.

#### 2.1 Useful procedures

In addition to the procedures mentioned above, the following procedures are often useful when dealing with Scheme lists:

- (null? s): returns true if s is nil.
- (length s): returns the length of s.
- (append s1 ... sn): returns the result of concatenating lists s1, ..., sn.
- (map f s): returns the result of applying the procedure f to each element of s.
- (filter pred s): returns a list containing the elements of s for which the single-argument procedure pred returns true.
- (reduce comb s): combines the elements of s into a single value using the two-argument procedure comb.

### 2.2 Equality testing

Equality testing in Scheme is a bit confusing as it is handled by three separate procedures:

• (= a b): returns true if a equals b. Both must be numbers.

- (eq? a b): returns true if a and b are equivalent primitive values. For two objects, eq? returns true if both refer to the exactly same object in memory (like is in Python).
- (equal? a b): returns true if a and b are equivalent. Two lists are equivalent if their elements are equivalent.

1. What will Scheme output? Draw box-and-pointer diagrams to help determine this. (Ask your mentor if you're unsure what's going on. You aren't expected to understand this completely on your own.)

```
scm> (cons 1 (cons 2 nil))

(1 2)

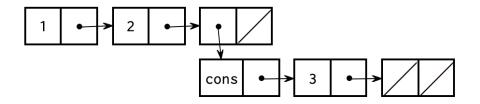
scm> (cons 1 '(2 3 4 5))

(1 2 3 4 5)

1 \longrightarrow 2 \longrightarrow 3 \longrightarrow 4 \longrightarrow 5
```

When we use the quote before the list, we are saying that we should put the literal list (2 3 4 5) in the cdr of this list. So in this case we create a list where the first element (car) is 1, and the cdr is the list (2 3 4 5).

```
scm> (cons 1 '(2 (cons 3 nil)))
(1 2 (cons 3 ()))
```



Since we also used a quote here, we do not evaluate the (cons 3 nil). We keep everything inside the quotes the same so the cdr of this list is the list (2 (cons 3 nil)). That means that we add the element 2, and then the nested list (cons 3 nil).

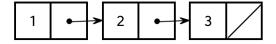
```
scm> (cons 1 (2 (cons 3 nil)))
eval: bad function in : (2 (cons 3 nil))
```

While evaluating the operands, Scheme will try to evaluate the expression (2 (cons 3 nil)). Since 2 is not a valid operator, this expression Errors.

```
scm> (cons 3 (cons (cons 4 nil) nil))
(3 (4))
scm> (define a '(1 2 3))
```

Defines a list of elements of  $(1\ 2\ 3)$  and binds the list to the variable a. Recall that define returns the name of the symbol.

```
scm> a
(1 2 3)
```



```
scm> (car a)

1
scm> (cdr a)

(2 3)
scm> (car (cdr a))
2
```

From above, we know that (cdr a) is (2 3). From that, we can evaluate (cdr a)) to 2.

How can we get the 3 out of a?

```
(car (cdr (cdr a)))
```

To get to the pair that contains 3, we need to call (cdr (cdr a)). To get the element 3, we need the car of (cdr (cdr a)).

2. Define sixty-ones. Return the number of times that 1 follows 6 in the list.

3. Define is-prefix, which takes in a list p and a list lst and determines if p is a prefix of lst. That is, it determines if lst starts with all the elements in p.

```
#t
scm> (is-prefix '() '(1 2))
#t
scm> (is-prefix '(1) '(1 2))
scm> (is-prefix '(2) '(1 2))
#f
; Note here p is longer than 1st
scm> (is-prefix '(1 2) '(1))
#f
(define (is-prefix p lst)
)
; is-prefix with nested if statements
(define (is-prefix p lst)
    (if (null? p)
        #t
        (if (null? 1st)
            #f
             (and
                (= (car p) (car lst))
                (is-prefix (cdr p) (cdr lst)))))
; is-prefix with a cond statement
(define (is-prefix p lst)
    (cond
        ((null? p) #t)
        ((null? lst) #f)
        (else (and (= (car p) (car lst))
            (is-prefix (cdr p) (cdr lst)))))
```

; Doctests:

scm> (is-prefix '() '())

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4. Implement argmax, a function that takes in a list, lst, and returns the index of the largest element in lst. If there are two or more elements that are the largest element, return the index of the one that appears first in lst.

You can assume all elements of lst are non-negative integers, and lst has at least 1 element and no nested lists.

```
(define (argmax lst)
   (define (max-helper lst max-so-far max-index curr-index)
       (cond
               ____) _____)
                _____)
          (else
      )
   (max-helper _____)
)
(define (argmax lst)
   (define (max-helper lst max-so-far max-index curr-index)
       (cond
          ((null? lst) max-index)
          ((> (car lst) max-so-far)
             (max-helper (cdr lst) (car lst) curr-index (+ curr-index
                1)))
          (else
             (max-helper (cdr lst) max-so-far max-index (+ curr-index
                1)))
   (max-helper lst 0 0 0)
)
```