MUTABLE TREES AND MIDTERM REVIEW

COMPUTER SCIENCE MENTORS 61A

October 24, 2022–October 28, 2022

1 Trees

For the following problems, use this definition for the Tree class:

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        self.branches = list(branches)

def is_leaf(self):
    return self.branches == []

# Implementation ommitted
```

Here are a few key differences between the Tree class and the Tree abstract data type, which we have previously encountered:

- Using the constructor: Capital T for the Tree class and lowercase t for tree ADT t = Tree(1) vs. t = tree(1)
- In the class, label and branches are instance variables and is_leaf() is an instance method. In the ADT, all of these were globally defined functions.

```
t.label vs. label(t)
t.branches vs. branches(t)
t.is_leaf() vs. is_leaf(t)
```

• A Tree object is mutable while the tree ADT is not mutable. This means we can change attributes of a Tree instance without making a new tree. In other words, we can solve tree class problems non-destructively and destructively, but can only solve tree ADT problems non-destructively.

```
t.label = 2 is allowed but label(t) = 2 would error.
```

Apart from these differences, we can largely take the approaches we used for the tree ADT and apply them to the Tree class!

1. Implement tree_sum, which takes in a Tree object and replaces the label of the tree with the sum of all the values in the tree. tree_sum should also return the new label.

```
def tree_sum(t):
    """
    >>> t = Tree(1, [Tree(2, [Tree(3)]), Tree(4)])
    >>> tree_sum(t)
    10
    >>> t.label
    10
    >>> t.branches[0].label
    5
    >>> t.branches[1].label
    4
    """
```

2. Define delete_path_duplicates, which takes in t, a tree with non-negative labels. If there are any duplicate labels on any path from root to leaf, the function should mutate the label of the occurrences deeper in the tree (i.e. farther from the root) to be the value -1.

def	<pre>delete_path_duplicates(t): """</pre>	
	<pre>>>> t = Tree(1, [Tree(2, [Tree(1), Tree(1 >>> delete_path_duplicates(t) >>> t</pre>)])])
	<pre>Tree(1, [Tree(2, [Tree(-1), Tree(-1)])]) >>> t2 = Tree(1, [Tree(2), Tree(2, [Tree(2)])])])</pre>	2, [Tree(1,
	<pre>>>> delete_path_duplicates(t2) >>> t2</pre>	
	Tree(1, [Tree(2), Tree(2, [Tree(-1, [Tree [Tree(5)])])])])	(-1,
	def helper(,):
	if:	
	else:	
	for:	

3. Given a tree t, mutate the tree so that each leaf's label becomes the sum of the labels of all nodes in the path from the leaf node to the root node.

4. Write a function that returns True if there exists a path from root to leaf that contains at least n instances of elem in a tree t.

Hint: recall that the built-in function **any** takes in an iterable and returns True if any of the iterable's elements are truthy.

def	<pre>contains_n(elem, n, t): """</pre>	
	>>> t1 = Tree(1, [Tree(1, [Tree(2)])])	
	>>> contains_n(1, 2, t1)	
	True	
	>>> contains_n(2, 2, t1)	
	False	
	>>> contains_n(2, 1, t1) True	
	>>> t2 = Tree(1, [Tree(2), Tree(1, [Tree(1), Tre	e(2)])])
	>>> contains_n(1, 3, t2)	
	True	
	>>> contains_n(2, 2, t2) # Not on a path	
	False	
	if n == 0:	
	return True	
	elif	_ :
	return	-
	elif	:
		- *
	return	-
	else:	
	matumn	
	return	-

1. What is the order of growth for foo?

```
(a) def foo(n):
    for i in range(n):
        print('hello')
```

(b) What's the order of growth of foo if we change range (n) to

```
i. range(n/2)?ii. range(n**2 + 5)?iii. range(10000000)?
```

2. What is the order of growth for belgian_waffle?

```
def belgian_waffle(n):
    total = 0
    while n > 0:
        total += 1
        n = n // 2
    return total
```

1. Write a function, make_digit_remover, which takes in a single digit i. It returns another function that takes in an integer and, scanning from right to left, removes all digits from the integer up to and including the first occurrence of i. If i does not occur in the integer, the original number is returned.

def	make	e_digit_remover(i):
	>>>	<pre>remove_two = make_digit_remover(2)</pre>
	>>>	remove_two(232018)
	23	
	>>>	remove_two(23)
	0	
	>>>	remove_two(99)
	99	
	11 11 11	
	def	remove():
		removed =
		while > 0:
		removed = removed // 10
		if:
	4	return
	reti	urn

1. Write a function that takes as input a number n and a list of numbers lst and returns True if we can find a subset of lst that sums to n.

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1. Draw the box-and-pointer diagram.

```
>>> violet = [7, 77, 17]
>>> violet.append([violet.pop(1)])

>>> dash = violet * 2
>>> jack = dash[3:5]
>>> jackjack = jack.extend(jack)

>>> helen = list(violet)
>>> helen += [jackjack]
>>> helen[2].append(violet)
```

2. Implement subsets, which takes in a list of values and an integer n and returns all subsets of the list of size exactly n in any order. You may not need to use all the lines provided.

f	subs	sets(lst, n):
	>>>	<pre>three_subsets = subsets(list(range(5)), 3)</pre>
		for subset in sorted(three_subsets):
		print(subset)
		1, 2]
		1, 3]
		1, 4]
		2, 3]
		2, 4]
		3, 4]
		2, 3]
		2, 4]
		3, 4]
		3, 4]
	11 11 11	9 / 1]
	if r	n == 0: :
	_	

1. Write a generator function num_elems that takes in a possibly nested list of numbers lst and yields the number of elements in each nested list before finally yielding the total number of elements (including the elements of nested lists) in lst. For a nested list, yield the size of the inner list before the outer, and if you have multiple nested lists, yield their sizes from left to right.

def	num_	_elems(lst):							
	>>> [4]	<pre>list(num_elems([3,</pre>	3,	2,	1]))			
		<pre>list(num_elems([1, 4, 5, 8]</pre>	3,	5,	[1,	[3,	5,	[5,	7]]]))
	cour	nt =	_						
	for				:				
		if			:				
		for							:
		yield							
		else:							
	yıe.	ld				_			

1. Let's use OOP to help us implement our good friend, the ping-pong sequence!

As a reminder, the ping-pong sequence counts up starting from 1 and is always either counting up or counting down.

At element k, the direction switches if k is a multiple of 7 or contains the digit 7.

The first 30 elements of the ping-pong sequence are listed below, with direction swaps marked using brackets at the 7th, 14th, 17th, 21st, 27th, and 28th elements:

```
1 2 3 4 5 6 [7] 6 5 4 3 2 1 [0] 1 2 [3] 2 1 0 [-1] 0 1 2 3 4 [5] [4] 5 6
```

Assume you have a function has_seven(k) that returns True if k contains the digit 7.

```
>>> tracker1 = PingPongTracker()
>>> tracker2 = PingPongTracker()
>>> tracker1.next()
1
>>> tracker1.next()
2
>>> tracker2.next()
1
class PingPongTracker:
    def __init__(self):
```

```
def next(self):
```

1. Write a function <code>combine_two</code>, which takes in a linked list of integers <code>lnk</code> and a two-argument function <code>fn</code>. It returns a new linked list where every two elements of <code>lnk</code> have been combined using <code>fn</code>.

def	<pre>combine_two(lnk, fn): """</pre>	
	<pre>>>> lnk1 = Link(1, Link(2, Link(3, Link(4)) >>> combine_two(lnk1, add) Link(3, Link(7))</pre>	·))
	<pre>>>> lnk2 = Link(2, Link(4, Link(6))) >>> combine_two(lnk2, mul) Link(8, Link(6)) """</pre>	
	if:	
	return	
	elif	
	return	
	combined =	
	matum	

2. Write a recursive function $insert_all$ that takes as input two linked lists, s and x, and an index $insert_all$ should return a new linked list with the contents of x inserted at index index of s.

def	<pre>f insert_all(s, x, index): """</pre>	
	>>> insert = Link(3, Link(4))	
	>>> original = Link(1, Link(2, Link(5)))	
	>>> insert_all(original, insert, 2)	
	Link(1, Link(2, Link(3, Link(4, Link(5)))))	
	>>> start = Link(1)	
	>>> insert_all(original, start, 0)	
	Link(1, Link(1, Link(2, Link(5))))	
	II II II	
	if and	:
	if and	: