

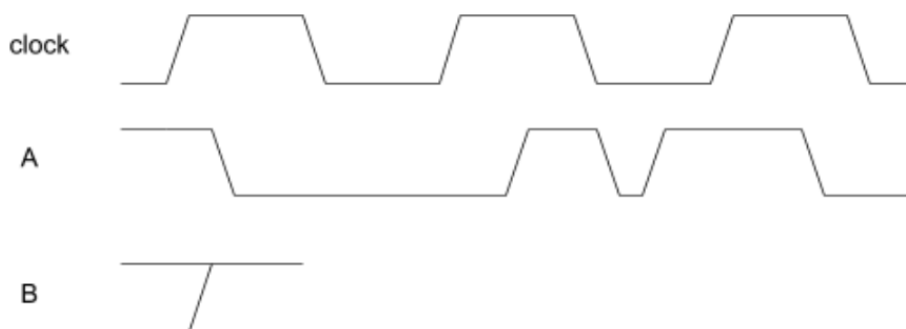
## 1 Synchronous Digital Systems

Synchronous Digital Systems (SDSs) are systems designed to process input as it comes in and output it as quickly as it comes in. The input is always a series of pins with either high or low voltage, and the output is another series of pins, each with either high or low voltage. A clock is used to tell the input and output when to switch to the next value; the switch always occurs on the rising edge (low to high voltage) of the clock. This is so that the output is always consistent, otherwise halfway through the switch of the input, the output might be based on the old input or the new, depending on the quality of the circuit and also some random chance based on electron movement. Note: the output always takes a small amount of time to stabilize after the rising edge.

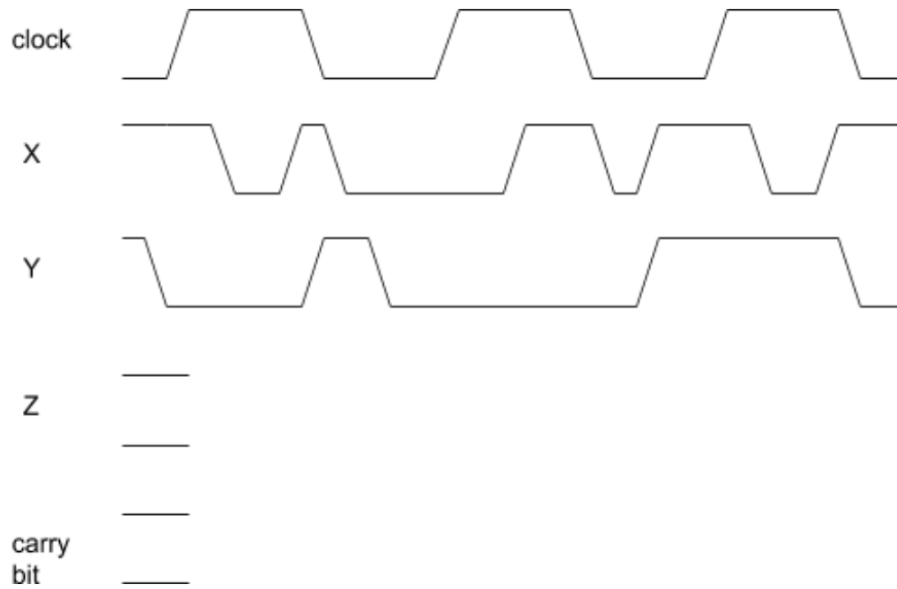
When slowed down, clock cycles will look something like below. This is three clock cycles in a row, and here is the rising edge:



- 1.1 On the rising edge of the clock, B is set to A and is held constant until the next rising edge. Fill in the diagram for B's value.



- 1.2 In a clock cycle, complex operations can occur. For example, most of the RISC-V instructions can be done in 1 clock cycle. Below, the diagram shows the equation  $Z = X + Y$  where  $Z$  is computed on the rising edge of the clock. If  $Z$  overflows, place the overflow in the carry bit.

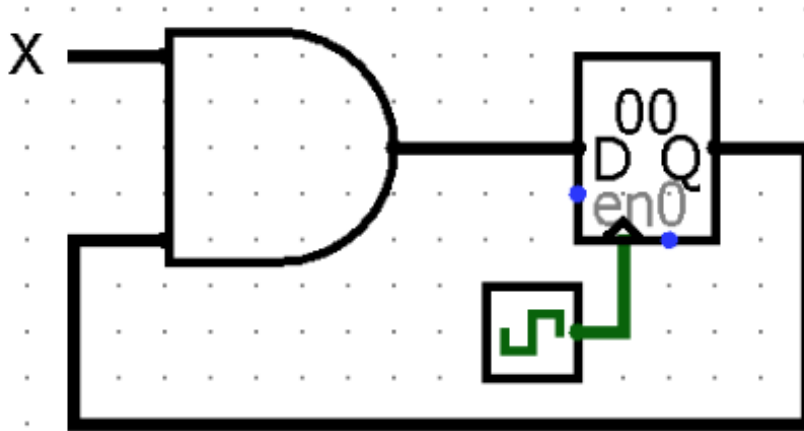


## 2 SDS With Registers

For the circuit below, assume:

1. setup time is 15ns
2. hold time is 30ns
3. AND gate delay is 10ns.

If the clock rate is 10 MHz and x updates 25ns after the rising edge of the clock, what are the minimum and maximum values for the clk-to-Q delay to ensure proper functionality?



2.1 Min: \_\_\_\_\_ ns

2.2 Max: \_\_\_\_\_ ns

### 3 Finite State Machines

Suppose we want to design a FSM that takes a single bit (1/0) as input, and outputs a single bit (1/0). We want the FSM to output true (1) only if it has seen three consecutive 1's as its input. Let's design it!

- 3.1 Given the following input streams, fill in what the FSM should output at each time step:

(a)

In	0	1	0	1
Out				

(b)

In	1	1	0	0
Out				

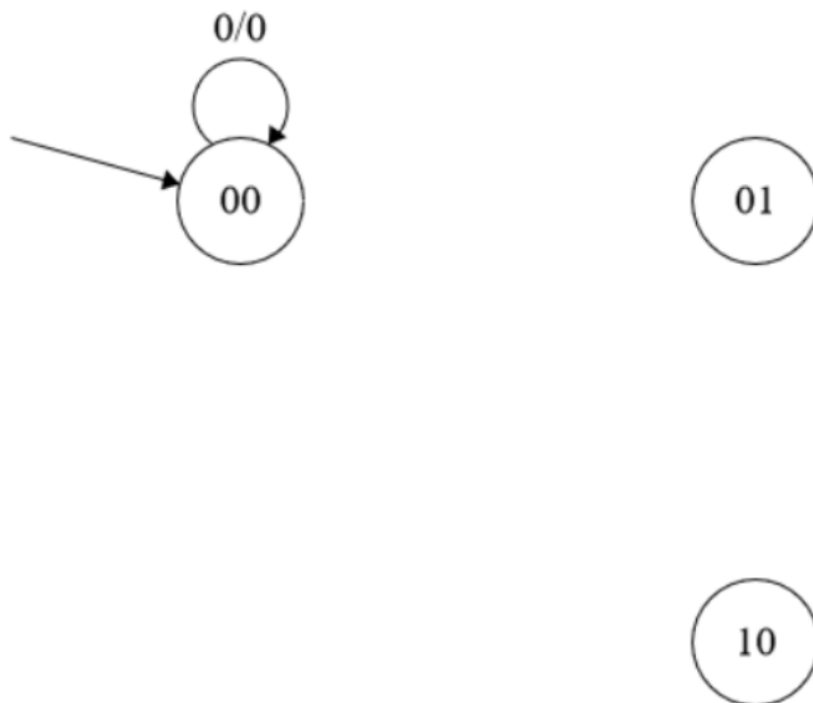
(c)

In	0	1	1	1
Out				

- 3.2 Let's consider the design of the FSM with more formality.

- (a) If a 0 is input into the FSM, what should the FSM output?
- (b) If a 1 is input into the FSM, what does the FSM need to remember to make the correct decision?
- (c) How many unique states does the FSM need?

3.3 Fill in the FSM.



3.4 Consider the following FSM. What does it do?

