Knowledge representation and reasoning Lecture 1: Introduction

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Plan of the lecture

- 1 Admin
- What is this module about
- 3 Examples of knowledge-based systems
- 4 Plan of the module

Essential module information

- From this year: 20 credits
- 2 lectures a week + one hour lab/problem class
- 75 % exam, 25 % coursework (5 small assignments marked in the lab)
- Lecture 1: Monday 12:00-13:00 in JBSouth A25
- Lecture 2: Thursday 09:00-10:00 in JC-EXCHGE-B.LT1
- Lab: Monday 17:00-18:00 in A32 (there is one today!)
- Office hour: Friday at 11:00

More module information

- This year module page is on moodle
- Previous exam papers and answers are on http://www.cs.nott.ac.uk/~psznza/G53KRR
- note that this module had different convenors and content in 2014-15 and 2015-16 and exams were different
- textbook:
 - Ronald Brachman and Hector Levesque. *Knowledge Representation and Reasoning*. Elsevier, 2004
- module page has a link to Levesque's lecture slides; I will be mostly using a board, so prepare to take notes!



What is this module about

- How can knowledge be represented symbolically and manipulated in an automated way by reasoning programs
- Knowledge: some information about the world
 - medical information about some particular set of diseases: what causes them, how to diagnose them
 - geographical data: which city is the capital of which country, population statistics, . . .
 - common sense physics: bodies cannot go through solid walls, ...
- Representation: how / in which language do we represent this information
- Reasoning: how to extract more information from what is explicitly represented (because we cannot represent every single fact explicitly as in a database)

Knowledge-based systems

- We want to be able to talk about some AI programs in terms of what they 'know'
 - (which corresponds to taking 'intentional stance' towards those systems, ascribing them human characteristics - for why this may be useful, see Daniel Dennett)
- ... and not just talk about what they know but also have something to point to in those systems corresponding to 'knowledge' and determining their behaviour, namely explicitly represented symbolic knowledge

Example (Brachman and Levesque)

Two Prolog programs with identical behaviour:

```
printColour(snow) :- !, write("It's white.").
printColour(grass) :- !, write("It's green.").
printColour(sky) :- !, write("It's yellow.").
printColour(X) :- !, write("Beats me.").
```

and

```
printColour(X) :- colour(X,Y), !, write("It's "),
write(Y), write(".").
printColour(X) :- write("Beats me.").
colour(snow, white).
colour(sky, yellow).
colour(X,Y) : - madeof(X,Z), colour(Z,Y).
madeof(grass, vegetation).
colour(vegetation, green).
```

Which one is knowledge-based

- Only the second program has explicit representation of 'knowledge' that snow is white
- the second program does what it does when asked for the colour of snow because of this knowledge. When colour (snow, white) is removed, it will not print the right colour for snow.
- what makes the system knowledge-based is not
 - the use of a particular logical-looking language like Prolog
 - or having representation of true facts (colour (sky, yellow) is not)
 - or having lots of facts, or having a complex structure
- rather, it is having explicit representation of knowledge which is used in the operation of the program

Definition of knowledge-based systems and knowledge bases

- Knowledge-based systems are systems for which intentional stance is grounded by design in symbolic representation
- The symbolic representation of knowledge is called a knowledge base.

Examples of knowledge-based systems

- Various expert systems
 - MYCIN (1970s, Stanford University)
 - XCON (1978, Carnegie Mellon University)
- Perhaps most famous knowledge base: CYC (1980s, Douglas Lenat, Cycorp, Austin, Texas)
- Ontologies
 - Snomed CT http://snomed.dataline.co.uk/
 - Gene ontology http://www.geneontology.org/
- Google Knowledge Graph
- (Parts of) IBM Watson

MYCIN

- 1970s, Stanford University (Edward Shortliffe, Pat Buchanan)
- Production rule system (we will see them later in the course)
- Purpose: automatic diagnosis of bacterial infections
- Lots of interviews with experts on infectious diseases, translated into rules (knowledge acquisition is a non-trivial process; also see later in the course)
- approximately 500 rules

Example MYCIN rule

Rule in LISP:

```
RULE035
```

```
PREMISE: ($ AND (SAME CNTXT GRAM GRAMNEG)
(SAME CNTXT MORPH ROD)
(SAME CNTXT AIR ANAEROBIC))
```

```
ACTION: (CONCLUDE CNTXT IDENTITY BACTEROIDES TALLY .6)
```

English translation:

IF:

- 1 the gram stain of the organism is gramneg, and
- 2 the morphology of the organism is rod, and
- 3 the aerobicity of the organism is anaerobic

THEN: There is suggestive evidence (.6) that the identity of the organism is bacteroides

More about MYCIN

- some facts and some conclusions of the rules (as above) are not absolutely certain
- MYCIN uses numerical *certainty factors*; range between -1 and 1
- (reasonably involved) rules for combining certainty factors of premises, with the number in the rule (as 0.6 above) into a certainty factor for the conclusions
- later it turned out that MYCIN's recommendations would have been the same if it used only 4 values for certainty factors
- MYCIN was never used in practice (ethical and legal issues)
- when tested on real cases, did as well or better than the members of the Stanford medical school

XCON

- John McDermott, CMU, 1978
- eXpert CONfigurer system for configuring VAX computers
- production rule system, written using OPS5 (language for production systems, implemented in LISP)
- 10,000 rules
- used commercially

Cyc

- The Cyc Knowledge Server is a very large knowledge base and inference engine
- Developed by Cycorp: http://www.cyc.com/
- It aims to provide a deep layer of 'common sense knowledge', to be used by other knowledge-intensive programs

Cyc knowledge base

- Contains terms and assertions in formal language CycL, based on first-order logic, syntax similar to LISP
- Knowledge base contains classification of things (starting with the most general category: Thing), and also facts, rules of thumb, heuristics for reasoning about everyday objects
- Currently, over 200,000 terms, and many human-entered assertions involving each term; Cyc can derive new assertions from those
- Divided in thousands of 'microtheories'

Cyc knowledge base

- General knowledge: things, intangible things, physical objects, individuals, collections, sets, relations...
- Domain-specific knowledge, for example:
 - Political geography: general information (e.g. What is a border?) and specific information about towns, cities, countries and international organizations
 - Human anatomy and physiology
 - Chemistry

Snomed

- Snomed CT: Systematized Nomenclature of Medicine Clinical Terms
- Developed by College of American Pathologists and the NHS
- Clinical terminology (with formal definitions)
- Designed for unambiguous recording of data and interoperability with software applications
- Uses ontology language (different from first order logic) EL++
- Approx. 400 000 concepts, 1 million terms and 1.6 million relationships

Snomed: example

Concept: 32553006 - Hangover

Descriptions:

Synonym: hangover effect

Synonym: hangover from alcohol

Relationships:

(is a) 228273003 - Finding relating to alcohol

drinking behavior

(causative agent) 311492009 - Ingestible

alcohol

Google's Knowledge Graph

- based on an earlier knowledge base, Freebase (bought by Google in 2010)
- is used to enhance search results by displaying Wikipedia-style entry in an infobox alongside search results
- there is also a Google API which allows programmers to use Knowledge Graph
- used in Google Assistant and Google Home to answer questions



Computer Science



Field of study

Computer science is the study of the theory, experimentation, and engineering that form the basis for the design and use of computers. Wikipedia

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Watson

- developed at IBM by a team led by David Ferrucci
- question answering system (originally developed to play Jeopardy)
- has access to terabytes of data (all Wikipedia pages, other encyclopedias)
- Jeopardy instance of Watson had a knowledge base, but
- mostly used statistical correlation methods in plain English text to find answers to questions such as, which city has airports named after a WWII hero and a WWII battle
- other instances of Watson are used in medicine (the first commercial application was decision support in lung cancer treatment)

Watson playing Jeopardy



Long standing split in Al

- explicit symbolic representation (symbolic AI); this module is symbolic AI
- non-symbolic AI: behaviour robotics, (deep) learning
- machine learning saves us from having to hand-code explicit reasoning rules and statements about the world; some tasks which humans can easily do are unlikely to every be formalisable
- on the down side, hard to say exactly what a machine-learned program will do next
- are there things that machine learning/collecting information from the web will never be able to do?

Winograd Schema Challenge

- Hector Levesque (2013): Winograd Schema Challenge (to replace Turing test)
- requires understanding the meaning of language vs exploiting statistical correlations
- Examples:
 - The trophy would not fit in the brown suitcase because it was too big. What was too big?
 - 1 the trophy
 - 2 the suitcase
 - Joan made sure to thank Susan for all the help she had given. Who had given the help?
 - 1 Joan
 - 2 Susan

Winograd schema challenge

- there is a competition running since 2016 called Winograd Schema Challenge sponsored by Nuance Communications
- there was a successful individual project at the School by George Hallam in 2013/14 to answer some types of Winograd schema questions
- represented knowledge about fitting things in containers etc.
- used first order reasoning (resolution) to produce answers

Today's lab: START

- I could not find any online instance of Watson
- Try to determine whether START is using reasoning or just looking things up on the internet
- START Natural Language Question Answering System, MIT, 1993
- http://start.csail.mit.edu
- You can also use the lab time to ask me questions about the module

Plan of the module

- First order logic (3 lectures); cw1 8/10/2018
- Resolution (4 lectures); cw2 22/10/2018
- Horn clauses, backward chaining, forward chaining (3 lectures); cw3 5/11/2018
- Description logic/ontologies (2 lectures); cw4 19/11/2018
- Defaults/non-monotonic reasoning (2 lectures)
- Reasoning about actions and planning (4 lectures); cw5 3/12/2018
- Uncertainty/bayesian networks
- Lifecycle of a knowledge based system

Recommended reading for the next lecture

- Hector Levesque. On our best behaviour. Artificial Intelligence, Volume 212, 2014, pages 27-35. (on moodle)
- Brachman and Levesque, chapter 2 (The language of first-order logic).

Handout for G53KRR lecture on resolution

- 1. Reducing a first order sentence to clausal normal form.
- 1. eliminate \supset and \equiv using

$$(\alpha \supset \beta) \equiv (\neg \alpha \lor \beta)$$
$$(\alpha \equiv \beta) \equiv ((\alpha \supset \beta) \land (\beta \supset \alpha))$$

2. move ¬ inward so that it appears only in front of an atom, using

$$\neg\neg\alpha \equiv \alpha$$

$$\neg(\alpha \land \beta) \equiv (\neg\alpha \lor \neg\beta)$$

$$\neg(\alpha \lor \beta) \equiv (\neg\alpha \land \neg\beta)$$

$$\neg\forall x\alpha \equiv \exists x \neg\alpha$$

$$\neg\exists x\alpha \equiv \forall x \neg\alpha$$

3. ensure that each quantifier has a distinct variable by renaming:

$$\forall x \alpha \equiv \forall y \alpha(x/y)$$
$$\exists x \alpha \equiv \exists y \alpha(x/y)$$

where y does not occur in $\forall x\alpha$ and $\exists x\alpha$ and $\alpha(x/y)$ means α with all occurrences of x replaced by y.

- 4. eliminate existentials using Skolemisation:
 - if $\exists x\alpha$ is not in the scope of any universal quantifiers, then we replace $\exists x\alpha$ with $\alpha(a)$ where a is a new constant called a Skolem constant. (It should be different for every existential quantifier).
 - if $\exists x \alpha$ is in the scope of universal quantifiers $\forall x_1, \dots, \forall x_n$ (and these are all universal quantifiers it is in the scope of):

$$\forall x_1(\ldots \forall x_2 \ldots \forall x_n(\ldots \exists x\alpha) \ldots)$$

then replace $\exists x \alpha$ by $\alpha(x/f(x_1, \dots, x_n))$ where f is a Skolem function (again use a different Skolem function for every existential quantifier). Example: $\exists x_1 \exists x_2 \forall y \exists z P(x_1, x_2, y, z)$ becomes $\forall y P(c_1, c_2, y, f(y))$.

5. Move universals outside the scope of \wedge and \vee using the following equivalences (provided x is not free in α):

$$(\alpha \wedge \forall x\beta) \equiv \forall x(\alpha \wedge \beta)$$

$$(\alpha \vee \forall x\beta) \equiv \forall x(\alpha \vee \beta)$$

6. We now got $\forall x_1 \dots \forall x_n \alpha$ where α does not contain quantifiers. Reduce α to CNF as before using distributivity:

$$\alpha \vee (\beta \wedge \gamma) \equiv (\alpha \vee \beta) \wedge (\alpha \vee \gamma)$$

7. Collect terms:

$$(\alpha \vee \alpha) \equiv \alpha$$

$$(\alpha \wedge \alpha) \equiv \alpha$$

8. Reduce to clausal form by dropping universal quantifiers and conjunctions and making disjunctions into clauses (lists of literals):

$$\forall x ((P(x) \lor \neg R(a, f(b, x))) \land Q(x, y))$$

becomes

$$[P(x), \neg R(a, f(b, x))], [Q(x, y)]$$

- 9. Actually need also to do factoring: if a clause contains two literals ρ_1 and ρ_2 which unify in both directions (there is a substitution θ such that $\rho_1\theta = \rho_2$ and θ' such that $\rho_2\theta' = \rho_1$) then replace them with a single literal. For example, [P(x), P(y)] becomes [P(x)].
- 2. Substitution and unification.

A substitution θ is a finite set of pairs $\{x_1/t_1, \ldots, x_n/t_n\}$ where x_i are distinct variables and t_i are arbitrary terms (could all be the same variable y, or f(x, y, b) or whatever). If ρ is a literal then $\rho\theta$ is a literal which results from simultaneously substituting each x_i in ρ by t_i . Same for clauses: if c is a clause the $c\theta$ is the result of applying the substitution to all literals in c.

For example, if $\theta = \{x/a, y/g(x, b, z)\}$ then

$$[P(x), \neg R(a, f(b, x))]\theta = [P(a), \neg R(a, f(b, a))]$$

$$[Q(x,y)]\theta = [Q(a,g(x,b,z))]$$

 θ unifies (is a unifier for) two literals ρ_1 and ρ_2 if $\rho_1\theta = \rho_2\theta$. For example, P(x, f(x)) and P(y, f(a)) are unified by $\theta = \{x/a, y/a\}$.

3. General rule of resolution:

$$\frac{c_1 \cup \{\rho_1\} \quad c_2 \cup \{\neg \rho_2\}}{(c_1 \cup c_2)\theta}$$

where θ unifies ρ_1 and ρ_2 : $\rho_1\theta = \rho_2\theta$. We also assume that we renamed all variables in $c_1 \cup \{\rho_1\}$ and $c_2 \cup \{\neg \rho_2\}$ so that each clause has its distinct variables. Example:

$$\frac{ [\neg Man(x), Mortal(x)] \quad [Man(socrates)] }{[Mortal(socrates)]}$$

using $\theta = \{x/socrates\}$. (So $[Mortal(x)]\theta = [Mortal(socrates)]$.)

G53KRR: unification, resolution with equality

A unifier of two literals ρ_1 and ρ_2 is a substitution θ such that $\rho_1\theta = \rho_2\theta$. There are many possible unifiers, and some of them are too specific. For example, P(x,y) and P(a,z) can be unified by $\theta_1 = x/a, y/z$ and by $\theta_2 = x/a, y/b, z/b$ (the second one is too specific).

A most general unifier (mgu) for ρ_1 and ρ_2 is a unifier θ such that for any other unifier θ' , there is a further substitution $\theta*$ such that $\theta' = \theta\theta*$. Basically, θ' is obtained from θ by doing some extra substitutions.

An mgu for ρ_1 and ρ_2 (assuming ρ_1 and ρ_2 do not have common variables to start with) can be computed as follows:

- 1. start with $\theta = \{ \}$
- 2. exit if $\rho_1\theta = \rho_2\theta$
- 3. set DS to be the pair of terms at the first place where $\rho_1\theta$ and $\rho_2\theta$ disagree
- 4. find a variable v in DS and a term t in DS not containing v; if none exist,
- 5. otherwise set θ to $\theta\{v/t\}$ and go to step 2.

If we have to deal with a set of clauses containing equality, we need to add to KB the following axioms:

```
reflexivity \forall x(x=x)
symmetry \forall x \forall y(x=y\supset y=x)
```

transitivity $\forall x \forall y \forall z (x = y \land y = z \supset x = z)$

substitution for functions for every function
$$f$$
 of arity n in the set of clauses, $\forall x_1 \forall y_1 \ldots \forall x_n \forall y_n (x_1 = y_1 \land \ldots \land x_n = y_n \supset f(x_1, \ldots, x_n) = f(y_1, \ldots, y_n))$

substitution for predicates for every predicate P of arity n in the set of clauses,

$$\forall x_1 \forall y_1 \dots \forall x_n \forall y_n (x_1 = y_1 \land \dots \land x_n = y_n \supset P(x_1, \dots, x_n) \supset P(y_1, \dots, y_n))$$

With these axioms, resolution is sound and complete for refutation for first-order logic with equality.

Example: $\forall x(x=a \lor x=b), \exists x P(x), \neg P(a), \neg P(b)$ should be inconsistent. Clauses:

C1
$$[x = a, x = b]$$

C2 [P(c)]

C3
$$[\neg P(a)]$$

C4 $[\neg P(b)]$

We will also use the following instance of substitution for predicates:

C5
$$[\neg(x_1 = y_1), \neg P(x_1), P(y_1)]$$

Proof:

- (1) $[\neg(c = y_1), P(y_1)]$ from C5 and C2, x_1/c
- (2) $[\neg(c=a)]$ from C3 and (1), y_1/a
- (3) [c = b] from (2) and C1, x/c
- (4) [P(b)] from (3) and (1), y_1/b
- (5) [] from (4) and C4.

G53KRR Handout on Horn clauses, SLD resolution, backward chaining

Horn clauses A Horn clause is a clause which contains at most one positive literal:

$$[\neg Child(x), \neg Female(x), Girl(x)]$$

 $[\neg Girl(x)]$

Positive and negative Horn clauses

- Horn clauses which do contain a positive literal are called positive or definite clauses.
- Horn clauses which do not contain a positive literal are called negative clauses (or sometimes *goals*)

Note that positive Horn clauses are equivalent to FOL sentences of the form:

$$\forall x_1 \ldots \forall x_n (\rho_1 \wedge \ldots \wedge \rho_n \supset \rho)$$

For example,

$$\forall x (Child(x) \land Female(x) \supset Girl(x))$$

$$Female(a)$$

SLD resolution SLD stands for **S**elected **L**iterals, **L**inear pattern, **D**efinite Clauses.

An SLD derivation of a clause c from a set of clauses S is a sequence

$$c_1,\ldots,c_n$$

such that

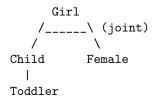
- $\bullet \ c_n = c,$
- $c_1 \in S$
- and each c_{i+1} is a resolvent of c_i and some clause from S.

Note that apart from c_1 all clauses in an SLD derivation are negative clauses (because resolution always 'eats up' the only positive literal in the clause from S). If S is a set of Horn clauses and from S by resolution we can derive $[\]$, then we can always derive $[\]$ from S using SLD resolution. SLD resolution is complete for refutation for Horn clauses, but not for arbitrary clauses.

Example The process of deriving an empty clause can be seen as 'eliminating' negative literals using positive clauses in the KB. For example,

 $Child \wedge Female \supset Girl$ $Toddler \supset Child$ Toddler Female

and we want to derive Girl, so add a clause $\neg Girl$. First we have one goal (negative clause) Girl; we eliminate it against $[\neg Child, \neg Female, Girl]$ and get two new subgoals: Child, Female. Goal tree:



SLD resolution derivation:

 $c_1 = \neg Girl$ $c_2 = [\neg Child, \neg Female]$ (by resolution from c_1 and $[\neg Child, \neg Female, Girl]$) $c_3 = [\neg Toddler, \neg Female]$ (by resolution from c_2 and $[\neg Toddler, Child]$) $c_4 = [\neg Female]$ (by resolution from c_3 and [Toddler]) $c_5 = [\]$ ((by resolution from c_4 and [Female]).

Backward chaining for propositional clauses (first order requires unification):

input: a finite set of atomic sentences q_1, \ldots, q_n **output:** YES if KB entails all of q_i , NO otherwise

procedure: SOLVE[q1, ..., qn]
if n = 0 then return YES
for each clause c in KB do
 if c = [not p1,...,not pm, q1] and SOLVE [p1,...,pm,q2,...,qn]
 then return YES
end for
return NO

Backward chaining on an example:

SOLVE[Girl]

- c = [Girl, not Child,not Female] call SOLVE [Child, Female]
- c = [not Toddler, Child] call SOLVE[Toddler,Female]
- c = [Toddler] call SOLVE[Female]
- c = [Female] call SOLVE[] return YES

PROCEDURAL CONTROL OF REASONING. PROLOG. Procedural control in the backward chaining procedure:

- Depth first (first solve ps rather than qs)
- Left to right (solve in order as they are listed)
- Backward chaining because search from goals to facts in KB

First order case requires unification, but the order is the same. This is the execution strategy of Prolog.

Prolog Prolog is a (logic) programming language where programs consist of facts and rules (Horn clauses):

```
parent(john, tom).
father(X, Y) :- parent(X,Y), male(X).
```

This is the same as:

Parent(john, tom)

$$\forall x \forall y (Parent(x, y) \land Male(x) \supset Father(x, y)$$

(Note that in Prolog variables are upper case and constants and predicate names are lower case. Every clause ends with a dot, and implications are pointing right to left.)

G53KRR: Forward chaining, production systems

Some issues with backward chaining To finish backward chaining:

- 1. Backward chaining on a single clause $[\neg q, q]$ and query q does not terminate.
- 2. It is possible to force backward chaining into an exponential proof search. Consider $KB_n = \{ [\neg p_{i-1}, p_i], [\neg p_{i-1}, q_i], [\neg q_{i-1}, p_i], [\neg q_{i-1}, q_i] : 0 < i < n \}$. For example, for n = 2:

$$\{ [\neg p_0, p_1], [\neg p_0, q_1], [\neg q_0, p_1], [\neg q_0, q_1] \}$$

Although KB_n has 4n-4 clauses, for any i, SOLVE (p_i) will take 2^i steps before failing (because there are two ways to prove p_i : prove p_{i-1} or q_{i-1} , and for each of those there are two ways to prove it, etc.)

Forward chaining (for propositional Horn clauses):

input: a finite list of atomic sentences, q_1, \ldots, q_n

output: YES if KB entails all of q_i , NO otherwise

- 1. if all goals q_i are marked as solved, return YES
- 2. check if there is a clause $[p, \neg p_1, \dots, \neg p_m]$ in KB, such that all of p_1, \dots, p_m are marked as solved and p is not marked as solved
- 3. if there is such a clause, then mark p as solved and go to step 1.
- 4. otherwise, return NO.

Another way to look at it:

input: a finite list of atomic sentences, q_1, \ldots, q_n

output: YES if KB entails all of q_i , NO otherwise

- 1. if all goals q_i are in KB, return YES
- 2. check if there is a clause $p_1 \wedge \ldots \wedge p_m \supset p$ in KB, such that all of p_1, \ldots, p_m are in KB and p is not in KB
- 3. if there is such a clause, then add p to KB and go to step 1.
- 4. otherwise, return NO.

For first-order case, similar, but need to unify the pattern in the body of the rule $(P_1(\bar{x}) \wedge \ldots \wedge P_m(\bar{x}))$ with unit clauses $P_i(\bar{a})$ in KB first, and then apply the same substitution to $P(\bar{x})$.

For first-order case we do the inference from

 $\forall x_1 \forall x_2 (Parent(x_1, x_2) \land Male(x_1) \supset Father(x_1, x_2)), \ Parent(bob, chris), \ Male(bob)$ to Father(bob, chris).

Production rule systems are forward-chaining reasoning systems which use production rules. Usually production rules are more complex than just Horn clauses (similar to how Prolog has more than just Horn clauses, also negation as failure etc.) but we will look at just Horn clauses. So this is different from the version in the textbook (much simpler).

We just assume that the knowledge base consists of: Working Memory WM which is a finite set of ground atoms (facts, or Working Memory Elements), and a finite set of production rules (universal Horn clauses).

The simplest way of reasoning would be to chain forward as above, but this may flood WM with a lot of irrelevant facts. Instead most production rule systems compute a *conflict set*: the set of all possible *rule instances* applicable for the current state of working memory. A rule instance is a substitution which makes a pattern in some rule match the working memory elements, together with the rule itself. A *conflict resolution strategy* is used to determine which of the rule instances in the conflict set will actually be fired (which conclusions added). Most conflict resolution strategies pick a single rule instance based on one or more of the following criteria: specificity of the rules (which rule has a more specific pattern in the body); or the order in which rules appear in the program; or the order in which facts were added to working memory (for example, depth first where rule instances involving more recent facts are preferred) etc.

Exercise For the following production system, trace the results, assuming that the conflict resolution strategy is: an instance of most important applicable rule is selected. If there are more than one such instances, the instance is selected randomly. The order of rule importance is: R3 more important than R1, R1 is more important than R2.

```
F1 animal(tiger)
F2 animal(cat)
F3 large(tiger)
F4 eatsMeat(tiger)
F5 eatsMeat(cat)

R1 \forall x(animal(x) \land large(x) \land eatsMeat(x) \supset dangerous(x))
R2 \forall x(animal(x) \supset breathesOxygen(x))
R3 \forall x(dangerous(x) \supset runAwayNow)
```

G53KRR handout on description logic ALC

OWL Web Ontology Language is a W3C standard. It extends most description logics and has slightly different terminology (based on RDF rather than description logic semantics. A subset of OWL, OWL DL, is based on description logic).

Reading:

The Description Logic Handbook. Franz Baader, Diego Calvanese, Deborah L.McGuinness, Daniele Nardi, and Peter F. Patel-Schneider, editors. Cambridge University Press, 2003. ISBN 0-521-78176-0.

A good on-line course: http://www.inf.unibz.it/~franconi/dl/course/

Basic idea description logic talks about relationships between *concepts* (noun phrases). There are many different description logics, ALC below is one of them. Most extend ALC with things like counting, transitive roles, inverse roles. Some are subsets of ALC, such as EL which only contains \exists , \sqcup and \sqsubseteq . EL is mostly what Snomed CT is written in.

Precise definition of the syntax of ALC:

Logical symbols (apart from brackets etc.):

- concept-forming operators: \forall , \exists , \sqcup , \sqcap ,
- connectives: \sqsubseteq , \doteq

Non-logical symbols:

- Atomic concepts: Person, Thing,.... Correspond to unary predicates in FOL.
- Roles: age, employer, child, arm, Correspond to binary predicates in FOL.
- Constants: $john, mary, roomA7, \ldots$ Correspond to constants (0-ary functional symbols) in FOL.

Concepts:

- atomic concept is a concept
- if r is a role and C is a concept, then $\forall r.C$ is a concept (e.g. $\forall .child.Girl$ describes someone all of whose children are girls)
- if r is a role and C is a concept, then $\exists r.C$ is a concept (e.g. $\exists .child.Girl$ describes someone who has a daughter)
- if C is a concept, then $\neg C$ (not C) is a concept
- if C_1 and C_2 are concepts then $C_1 \sqcap C_2$ (C_1 and C_2) is a concept
- if C_1 and C_2 are concepts then $C_1 \sqcup C_2$ (C_1 or C_2) is a concept

Sentences:

- if C_1 and C_2 are concepts then $C_1 \sqsubseteq C_2$ is a sentence (all C_1 s are C_2 s, C_1 is subsumed by C_2)
- if C_1 and C_2 are concepts then $C_1 \doteq C_2$ is a sentence $(C_1$ is equivalent to C_2)
- if a is a constant and C a concept then C(a) is a sentence (the individual denoted by a satisfies the description expressed by C)
- if a, b are constants and r a role then r(a,b) is a sentence (the individuals denoted by a and b are connected by the role r)

A description logic knowledge base is a set of description logic sentences.

TBox and ABox A description logic knowledge base is usually split into terminological part or TBox which describes general relationships between concepts, e.g. $Surgeon \sqsubseteq Doctor$, and assertions about individuals or ABox (e.g. Doctor(mary)).

Interpretations for description logic same as for FOL: a set of individuals D and an interpretation mapping I such that

- for a constant $a, I(a) \in D$
- for an atomic concept $A, I(A) \subseteq D$
- for a role $r, I(r) \subseteq D \times D$
- $I(\forall r.C]$) = $\{x \in D : \text{for any } y, \text{ if } (x,y) \in I(r), \text{ then } y \in I(C)\}$. Same as

$$\forall y (R(x,y) \supset B(y))$$

• $I(\exists r.C) = \{x \in D : \text{there is a } y \text{ such that } (x,y) \in I(r) \text{ and } y \in I(C)\}$. Same as

$$\exists y (R(x,y) \land C(y))$$

- $I(\neg C) = D \setminus I(C)$
- $I(C_1 \sqcap C_2]) = I(C_1) \cap I(C_2)$. Same as

$$C_1(x) \wedge C_2(x)$$

• $I(C_1 \sqcup C_2) = I(C_1) \cup I(C_2)$. Same as

$$C_1(x) \vee C_2(x)$$

Finally, for sentences:

- $(D, I) \models C(a)$ iff $I(a) \in I(C)$. Same as C(a)
- $(D,I) \models r(a,b)$ iff $(I(a),I(b)) \in I(r)$. Same as R(a,b)
- $(D,I) \models C_1 \sqsubseteq C_2$ iff $I(C_1) \subseteq I(C_2)$. Same as

$$\forall x (C_1(x) \supset C_2(x))$$

• $(D, I) \models C_1 \doteq C_2$ iff $I(C_1) = I(C_2)$. Same as

$$\forall x (C_1(x) \equiv C_2(x))$$

Reasoning Entailment is defined exactly like in FOL: a set of sentences Γ entails a sentence ϕ (in symbols $\Gamma \models \phi$) if and only if ϕ is true in every interpretation where all of the sentences in Γ are true.

Since ALC is a fragment of first order logic, reasoning in it is more efficient (it is decidable whether a sentence is satisfiable, or whether a finite set of sentences entails another sentence). This holds for many other description logics, although not all of them.

G53KRR handout on defaults.

Defaults or default rules as opposed to normal or categorical rules are ways of drawing conclusions which are justified unless there is some explicit reason to believe otherwise. So normal rule will say 'if x is a natural number then it is greater or equal to 0' and this is really true without exceptions for all natural numbers. A default rule would say 'if x is a bird then it can fly (unless there are good reasons to believe otherwise)'. In other words, if all we know about x is that it is a bird, then it is reasonable to conclude that it can fly. Later however we may discover that it is a special kind of bird which does not fly.

Non-monotonicity In classical reasoning, entailment is *monotonic*: if $KB_1 \models \phi$ and $KB_1 \subseteq KB_2$, then $KB_2 \models \phi$. In other words, if ϕ is entailed by KB_1 and we add more sentences to KB_1 , ϕ will still be entailed by the resulting knowledge base; the larger the knowledge base, the more consequences it has: if $KB_1 \subseteq KB_2$ then $Consequences(KB_1) \subseteq Consequences(KB_2)$.

Default reasoning is *nonmonotonic*. If we have $KB_1 = \{$ 'Birds normally can fly', 'Tweety is a bird' $\}$ then we can derive by default that Tweety can fly. However, if we learn more about Tweety, for example that it is a penguin, then 'Tweety can fly' no longer follows even by default.

The question is, how to make this work formally (define what are valid default consequences)? In these two lectures, consider three approaches: closed-world assumption, circumscription, default logic.

Closed-world reasoning Closed-world assumption (CWA): if an atomic sentence is not in the knowledge base, it is assumed to be false. (Like negation as failure in production rule systems: if a fact is not in the working memory, then its negation matches/is assumed to be true.) The corresponding entailment \models_{CWA} :

$$KB \models_{CWA} \phi \Leftrightarrow KB^+ \models \phi$$

where $KB^+ = KB \cup \{\neg p : p \text{ is atomic and } KB \not\models p\}$.

If $KB = \{Bird(t)\}\$ then $\neg Penguin(t)$ follows under CWA.

Problems: if $KB = \{p \lor q\}$, KB^+ is inconsistent since it contains $p \lor q$, $\neg p$ and $\neg q$, so everything follows from it.

Generalised CWA is a fix for this:

$$KB \models_{GCWA} \phi \Leftrightarrow KB^* \models \phi$$

where $KB^* = KB \cup \{ \neg p : p \text{ is atomic and for all collections of atoms } q_1, \dots, q_n, \text{ if } KB \models p \lor q_1 \lor \dots \lor q_n, \text{ then } KB \models q_1 \lor \dots \lor q_n \}.$

CWA with domain closure: only explicitly named individuals are assumed to exist:

$$KB \models_{CD} \phi \Leftrightarrow KB^{\diamond} \models \phi$$

where $KB^{\diamondsuit} = KB^+ \cup \forall x (x = c_1 \vee ... \vee x = c_n)$ where $c_1, ..., c_n$ are all the constant symbols appearing in KB.

Under CWA with domain closure, if there is no fact P(a) in the knowledge base then it entails by default $\neg \exists x P(x)$.

Unique name assumption: $c \neq c'$ for any two distinct constants c, c'.

Reasoning under CWA is constructive and reasonably efficient.

Circumscription (John McCarthy). This is a generalisation of CWA: for default entailment, consider not all models of KB but only those where the set of exceptions is made as small as possible. Namely, consider a predicate Ab (for abnormal) and the formulation of a default rule as

$$\forall x (Bird(x) \land \neg Ab(x) \supset Flies(x))$$

and say that a conclusion follows by default if it is entailed on all interpretations where the extension of Ab is as small as possible. (This is called *circumscribing* Ab and the approach is called *circumscription*.) We need one Ab for every default rule, because a bird which is abnormal with respect to flying may be normal with respect to having two legs etc.

Let A be the set of Ab predicates we want to minimise. Let $M_1 = (D, I_1)$ and $M_2 = (D, I_2)$ be two interpretations over the same domain such that every constant and function are interpreted the same way.

$$M_1 \le M_2 \iff \forall Ab \in A \ (I_1(Ab) \subseteq I_2(Ab))$$

 $M_1 < M_2$ if $M_1 \le M_2$ but not $M_2 \le M_1$. (There are strictly fewer abnormal things in M_1). Minimal entailment: $KB \models_{\le} \phi$ iff for all interpretations M which make KB true, either $M \models \phi$ or M is not minimal (exists M' such that M' < M and $M' \models KB$). Example:

$$KB = \{Bird(chilly), Bird(tweety), (tweety \neq chilly), \neg Flies(chilly), \forall x (Bird(x) \land \neg Ab(x) \supset Flies(x))\}$$

 $KB \not\models Flies(tweety)$ but $KB \models_{\leq} Flies(tweety)$. This knowledge base has a unique minimal extension for Ab, $I(Ab) = \{chilly\}$. This is not always the case. For example, if instead of $\neg Flies(chilly)$ it had $\neg Flies(chilly) \lor \neg Flies(tweety)$ there would be two minimal extensions of Ab: one where Tweety is abnormal and another where Chilly is abnormal.

Different from CWA: cannot replicate this effect by adding a fixed set of negated atomic sentences to KB.

Circumscription has constructive reasoning procedures but complexity is high.

Default logic Roy Reiter. A default rule consists of a prerequisite α , justification β , conclusion γ and says 'if α holds and it is consistent to believe β , then believe γ ': $\frac{\alpha : \beta}{\gamma}$

For example:

$$\frac{Bird(x):Flies(x)}{Flies(x)}$$

Default rules where justification and conclusion are the same are called *normal default rules* and are writted $Bird(x) \Rightarrow Flies(x)$.

Given a default theory $KB = \{F, D\}$, where F is a finite set of first order sentences and D is a finite set of default rules, what is the set of reasonable beliefs (extension of the default theory)? E is an extension of (F, D) iff for every sentence π ,

$$\pi \in E \; \Leftrightarrow \; F \cup \{\gamma \mid \frac{\alpha : \beta}{\gamma} \in D, \alpha \in E, \neg \beta \not \in E\} \models \pi$$

where $\{\gamma \mid \frac{\alpha:\beta}{\gamma} \in D, \alpha \in E, \neg \beta \notin E\}$ is a set of applicable assumptions for this extension.

Here is a non-deterministic procedure to produce an extension E of a theory (F, D):

0.
$$E = F$$

Repeat until no change to E:

- 1. Close E under logical consequence: $E = E \cup \{\alpha : E \models \alpha\}$
- 2. Choose $\frac{\alpha:\beta}{\gamma}$ in D such that for some substitution θ , $\alpha\theta \in E$ and $\neg\beta\theta \notin E$.

Set
$$E = E \cup \{\gamma\theta\}$$

Go to 1.

Example: $F = \{Bird(tweety), Bird(chilly), \neg Flies(chilly)\}, D = \{Bird(x) \Rightarrow Flies(x)\}.$ The only applicable assumption is Flies(tweety) (prerequisite in F hence in E, negation of justification not in E). For Chilly, negation of justification is in E, and for no other object o we can have Bird(o) in E. So E contains the consequences of $F \cup \{Flies(tweety)\}$. E is the only extension, and we can say that Flies(tweety) is a default consequence of (F, D).

A theory may have multiple extensions:

Facts: $F = \{Republican(dick), Quaker(dick)\}$

Default rules: $Republican(x) \Rightarrow \neg Pacifist(x)$, $Quaker(x) \Rightarrow Pacifist(x)$.

Two extensions: E_1 containing Pacifist(dick), E_2 containing $\neg Pacifist(dick)$. Can be forced to make only one extension using a non-normal default rule:

$$\frac{Quaker(x): Pacifist(x) \land \neg MemberOfPoliticalParty(x)}{Pacifist(x)}$$

and a rule $\forall x (Republican(x) \supset Member Of Political Party(x))$.

skeptical reasoner will only believe sentences which belong to all extensions of the default theory; credulous reasoner will choose an arbitrary extension.

G53KRR handout on Bayesian networks.

Bayesian approach (subjective probability) The basic idea is that we assign degrees of belief (subjective probabilities) to statements like "Tweety can fly" or "Patient a has disease b". Both sentences are either true or false in the real world, so standard objective statistical probabilities don't apply. However we can base our degree of belief on statistical information: namely, if 95% of birds can fly we may believe with degree 95% that a particular bird Tweety can fly. This will be an a priori degree of belief, before we know anything else about Tweety. Once we discover other facts about Tweety, our belief will be based on the conditional probability that Tweety flies given other facts (that it is a penguin for example).

Probability axioms and useful rules. Given a universal set U of all possible event occurrences (here we assume it is finite), an event a is a subset of U. For example, if U is a large set of medical histories, a is a subset of them where the patient has been diagnosed with flu. A probability function Pr is a function from events to numbers in [0,1] satisfying the following postulates:

- 1. Pr(U) = 1
- 2. If a_1, \ldots, a_n are disjoint events, $Pr(a_1 \cup \ldots \cup a_n) = Pr(a_1) + \ldots + Pr(a_n)$.

Some consequences:

- $Pr(\bar{a}) = 1 Pr(a)$ (\bar{a} is the complement of a)
- $Pr(\emptyset) = 0$
- $Pr(a \cup b) = Pr(a) + Pr(b) Pr(a \cap b)$

Conditional probability:

$$Pr(a \mid b) = \frac{Pr(a \land b)}{Pr(b)}$$

Conditionaly independent events: $Pr(a \mid b) = Pr(a)$. a and b are conditionally independent given c: $Pr(a \mid b \cap c) = Pr(a \mid c)$. Conditional version of the negation rule $Pr(\bar{a} \mid b) = 1 - Pr(a \mid b)$.

Bayes' rule

$$Pr(a \mid b) = \frac{Pr(a) \cdot Pr(b \mid a)}{Pr(b)}$$

If a is a disease and b a symptom, and we want to know the probability that someone has the disease given they have the symptom; it is easier to find the a priori probability of the disease and what is the probability that a patient who has the disease will display the symptom, and the a priori probability of the symptom.

Probabilities of sentences (basic Bayesian approach) Suppose there are n propositional variables of interest: p_1, \ldots, p_n (corresponding to sentences like "Tweety flies" or "John has flu"). There are 2^n possible states of the world (truth assignments to those variables). J is a joint probability distribution if for every assignment I, J(I) is a number between 0 and 1 and $\Sigma J(I) = 1$ (the probability that one of the assignments corresponds to reality is 1). The probability of a sentence α is the sum of probabilities of the worlds where α is true:

$$Pr(\alpha) = \sum_{I \models \alpha} J(I)$$

We can now find the probability of any sentence. Unfortunately, this requires us to keep 2^n numbers (probability of each assignment).

Let us represent an assignment to $\{p_1, \ldots, p_n\}$ as $\langle P_1, \ldots, P_n \rangle$ where P_i is p_i if p_i is assigned true and $\neg p_i$ otherwise. For example, an assignment which assigns true to p_1 and false to p_2 can be represented as $\langle p_1, \neg p_2 \rangle$.

$$J(\langle P_1, \dots, P_n \rangle) = Pr(P_1 \wedge \dots \wedge P_n)$$

By the chain rule (which follows from the definition of conditional probability),

$$Pr(P_1 \wedge \ldots \wedge P_n) = Pr(P_1) \cdot Pr(P_2|P_1) \cdot \cdots \cdot Pr(P_n|P_1 \wedge \ldots \wedge P_{n-1})$$

If all the variables were conditionally independent of each other:

$$Pr(P_i|P_1 \wedge \ldots \wedge P_{i-1}) = Pr(P_i)$$

then we could compute probabilities of each interpretation from n numbers. But normally we cannot assume that all variables are conditionally independent.

Belief networks The idea is to represent explicitly which variables *are* conditionally dependent on each other. The network is a directed acyclic graph. The nodes in the network are variables p_i and there is an arc from p_i to p_j if p_j is conditionally dependent on p_i (its probability given p_i is different from its prior probability).

If there is an arc from p_i to p_j we call p_i a parent of p_j in the network.

Each propositional variable in the belief network is conditionally independent from non-parent variables given its parent variables:

$$Pr(P_i \mid P_1 \land \ldots \land P_{i-1}) = Pr(P_i \mid parents(P_i))$$

where $parents(P_i)$ is the conjunction of literals which correspond to parents of p_i in the network.

Exercise Do exercise 2 after Chapter 12:

Consider the following example: Metastatic cancer is a possible cause of a brain tumor and is also an explanation for an increased total serum calcium. In turn, either of these could cause a patient to fall into occasional coma. Severe headache could also be explained by a brain tumor.

- (a) Represent these causal links in a belief network. Let a stand for 'metastatic cancer', b for 'increased total serum calcium', c for 'brain tumor', d for 'occasional coma', and e for 'severe headaches'.
- (b) Give an example of an independence assumption that is implicit in this network.
- (c) Suppose the following probabilities are given: $Pr(a) = 0.2, Pr(b|a) = 0.8, Pr(b|\neg a) = 0.2, Pr(c|a) = 0.2, Pr(c|\neg a) = 0.05, Pr(e|c) = 0.8, Pr(e|\neg c) = 0.6, Pr(d|b\land c) = 0.8, Pr(d|b\land \neg c) = 0.8, Pr(d|\neg b\land c) = 0.8, Pr(d|\neg b\land \neg c) = 0.05$ and assume that it is also given that some patient is suffering from severe headaches but has not fallen into a coma. Calculate joint probabilities for the eight remaining possibilities (that is, according to whether a, b, and c are true or false).
- (d) According to the numbers given, the a priori probability that the patient has metastatic cancer is 0.2. Given that the patient is suffering from severe headaches but has not fallen into a coma, are we now more or less inclined to believe that the patient has cancer? Explain.

G53KRR exercise on Bayesian networks.

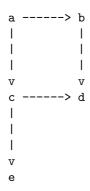
This is exercise 2 after Chapter 12 in Brachman and Levesque's book:

Consider the following example: Metastatic cancer is a possible cause of a brain tumor and is also an explanation for an increased total serum calcium. In turn, either of these could cause a patient to fall into occasional coma. Severe headache could also be explained by a brain tumor.

- (a) Represent these causal links in a belief network. Let a stand for 'metastatic cancer', b for 'increased total serum calcium', c for 'brain tumor', d for 'occasional coma', and e for 'severe headaches'.
- (b) Give an example of an independence assumption that is implicit in this network.
- (c) Suppose the following probabilities are given: $Pr(a) = 0.2, Pr(b|a) = 0.8, Pr(b|\neg a) = 0.2, Pr(c|a) = 0.2, Pr(c|\neg a) = 0.05, Pr(e|c) = 0.8, Pr(e|\neg c) = 0.6, Pr(d|b \land c) = 0.8, Pr(d|b \land \neg c) = 0.8, Pr(d|\neg b \land c) = 0.8, Pr(d|\neg b \land \neg c) = 0.05$ and assume that it is also given that some patient is suffering from severe headaches but has not fallen into a coma. Calculate joint probabilities for the eight remaining possibilities (that is, according to whether a, b, and c are true or false).
- (d) According to the numbers given, the a priori probability that the patient has metastatic cancer is 0.2. Given that the patient is suffering from severe headaches but has not fallen into a coma, are we now more or less inclined to believe that the patient has cancer? Explain.

Answers

(a) Sorry for an ascii drawing. The main thing here is that arcs go from cause (e.g. brain tumor) to effect (e.g. headache). Other layouts like the one I did on the board are OK too.



- (b) Examples are:
 - $Pr(c \mid a \land b) = Pr(c \mid a), Pr(c \mid \neg a \land b) = Pr(c \mid \neg a)$ etc.
 - $Pr(d \mid a \land b \land c) = Pr(d \mid b \land c)$
 - $Pr(e \mid a \land b \land c \land d) = Pr(e \mid c)$

- (c) I spell out the computation of the probability of the first conjunction in more detail, after that I will skip the chain rule and use the negation rule without mentioning it.
 - 1. $Pr(a \land b \land c \land \neg d \land e) = \text{(using the normal chain rule)}$ $Pr(a) \cdot Pr(b \mid a) \cdot Pr(c \mid a \land b) \cdot Pr(\neg d \mid a \land b \land c) \cdot Pr(e \mid a \land b \land c \land \neg d) = \text{(substituting conditional probabilities using independence assumptions of the network)}$ $Pr(a) \cdot Pr(b \mid a) \cdot Pr(c \mid a) \cdot Pr(\neg d \mid b \land c) \cdot Pr(e \mid c) =$

(using the negation rule $Pr(\neg d \mid b \land c) \cdot Pr(d \mid b \land c)$)

 $Pr(a) \cdot Pr(b \mid a) \cdot Pr(c \mid a) \cdot (1 - Pr(d \mid b \land c)) \cdot Pr(e \mid c) = 0.2 \cdot 0.8 \cdot 0.2 \cdot 0.2 \cdot 0.8 = 0.00512$

- 2. $Pr(a \land b \land \neg c \land \neg d \land e) = Pr(a) \cdot Pr(b \mid a) \cdot (1 Pr(c \mid a)) \cdot (1 Pr(d \mid b \land \neg c)) \cdot Pr(e \mid \neg c) = 0.2 \cdot 0.8 \cdot 0.8 \cdot 0.2 \cdot 0.6 = 0.01536$
- 3. $Pr(a \land \neg b \land c \land \neg d \land e) = Pr(a) \cdot (1 Pr(b \mid a)) \cdot Pr(c \mid a) \cdot (1 Pr(d \mid \neg b \land c)) \cdot Pr(e \mid c) = 0.2 \cdot 0.2 \cdot 0.2 \cdot 0.2 \cdot 0.8 = 0.00128$
- 4. $Pr(a \land \neg b \land \neg c \land \neg d \land e) = Pr(a) \cdot (1 Pr(b \mid a)) \cdot (1 Pr(c \mid a)) \cdot (1 Pr(d \mid \neg b \land \neg c)) \cdot Pr(e \mid \neg c) = 0.2 \cdot 0.2 \cdot 0.8 \cdot 0.95 \cdot 0.6 = 0.01824$
- 5. $Pr(\neg a \land b \land c \land \neg d \land e) = (1 Pr(a)) \cdot Pr(b \mid \neg a) \cdot Pr(c \mid \neg a) \cdot (1 Pr(d \mid b \land c)) \cdot Pr(e \mid c) = 0.8 \cdot 0.2 \cdot 0.05 \cdot 0.2 \cdot 0.8 = 0.00128$
- 6. $Pr(\neg a \land b \land \neg c \land \neg d \land e) = (1 Pr(a)) \cdot Pr(b \mid \neg a) \cdot (1 Pr(c \mid \neg a)) \cdot (1 Pr(d \mid b \land \neg c)) \cdot Pr(e \mid \neg c) = 0.8 \cdot 0.2 \cdot 0.95 \cdot 0.2 \cdot 0.6 = 0.01824$
- 7. $Pr(\neg a \land \neg b \land c \land \neg d \land e) = (1 Pr(a)) \cdot (1 Pr(b \mid \neg a)) \cdot Pr(c \mid \neg a) \cdot (1 Pr(d \mid \neg b \land c)) \cdot Pr(e \mid c) = 0.8 \cdot 0.8 \cdot 0.05 \cdot 0.2 \cdot 0.8 = 0.00512$
- 8. $Pr(\neg a \land \neg b \land \neg c \land \neg d \land e) = (1 Pr(a)) \cdot (1 Pr(b \mid \neg a)) \cdot (1 Pr(c \mid \neg a)) \cdot (1 Pr(d \mid b \land \neg c)) \cdot Pr(e \mid \neg c) = 0.8 \cdot 0.8 \cdot 0.95 \cdot 0.95 \cdot 0.6 = 0.34656$
- (d) We are asked whether $Pr(a \mid \neg d \land e)$ is greater or smaller than Pr(a).

 $Pr(a \mid \neg d \land e) = Pr(a \land \neg d \land e)/Pr(\neg d \land e)$ (conditional probability definition). We need to compute $Pr(a \land \neg d \land e)$ and $Pr(\neg d \land e)$, and to do that we use the probabilities we computed above. They describe all 8 possible states of the world given that $\neg d$ and e are true, and they are all disjoint. We are using $Pr(X) = Pr(X \land Y) + Pr(X \land \neg Y)$, or that the probability of the union of disjoint events equals to the sum of probabilities of those events.

So $Pr(a \land \neg d \land e) = Pr(a \land b \land c \land \neg d \land e) + Pr(a \land b \land \neg c \land \neg d \land e) + Pr(a \land \neg b \land c \land \neg d \land e) + Pr(a \land \neg b \land \neg c \land \neg d \land e)$ and $Pr(\neg d \land e)$ is the sum of all 8 numbers above.

 $Pr(a \land \neg d \land e) = 0.04$

 $Pr(\neg d \land e) = 0.04 + 0.00128 + 0.01824 + 0.00512 + 0.34656 = 0.4112$

 $Pr(a \mid \neg d \land e) = 0.04/0.4112$ which is approximately 0.1. So the probability got smaller.

Knowledge representation and reasoning Lecture 17: Reasoning about actions

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Plan of the lecture

- 1 New topic: planning and reasoning about actions
- 2 Situation calculus
- 3 Preconditions and postconditions of actions
- 4 Frame problem
- 5 Using situation calculus to make plans

How to use reasoning to make plans

- This lecture: situation calculus (based mostly on Stuart Russell slides for Russell and Norvig, Artificial Intelligence)
- Next two lectures: planning

Using FOL to reason about actions

- Suppose we want AI program to reason about applicability, outcomes and the choice of actions
- What is missing currently is being able to express change
- Instead of describing a static world, we need to be able to talk about states of the world or situations

Situation Calculus

- Situation calculus is a dialect of FOL where situations (static states of the world) and actions are basic terms:
- variables over situations are denoted s, s_1, s_2, \ldots, s_n
- \blacksquare a distinguished initial situation is denoted by a constant S_0 .
- **actions** are terms like move(x, y, z) (move thing z to coordinates x, y) etc. Note that actions are also terms, not formulas: they denote an 'action' and are not true or false.
- **a** a special function do takes an action and a situation and returns a new situation: do(a, s) denotes a new situation which results from performing an action a in a situation s.



Fluents

- Predicates and functions whose values vary from situation to situation are called fluents.
- Last argument in a fluent is a situation:
- ¬ $Holding(r, x, s) \land Holding(r, x, do(pickup(r, x), s))$ (a robot r is not holding x in s but is holding it in the situation resulting from s by picking x up).
- A distinguished fluent *Poss* says which actions are possible in a given situation:
 - $Poss(pickup(r, blockA), S_0)$

Preconditions of actions

- A precondition is a condition which makes an action possible.
- It can be expressed by a formula, sometimes called precondition axiom.
- For example:

```
\forall r \forall x \forall s \ (Poss(pickup(r, x), s) \equiv \\ \forall z (\neg Holding(r, z, s) \land \neg Heavy(x) \land NextTo(r, x, s)))
```

(a robot can pick x up if it is not holding anything else, x is not heavy, and the robot is next to it).

Postconditions or effects of actions

- A postcondition or effect of an action is a change resulting from executing the action.
- Formulas expressing postconditions are sometimes called effect axioms.
- For example, $\forall x \forall s \forall r (Fragile(x) \supset Broken(x, do(drop(r, x), s)))$
- Effect axioms for fluents which become true as a result of an action are called positive, and those where the fluent becomes false are called negative.

Frame axioms

- Classical planning assumption: actions are deterministic, and the world changes only as a result of clearly specified actions.
- For every action, we can also say which fluents it *does not* affect.
- The formulas which specify which properties are not changed as a result of an action are called frame axioms.
- For example, $\forall x \forall y \forall s \forall r$ $(\neg Broken(x, s) \land (x \neq y \lor \neg Fragile(x)) \supset \neg Broken(x, do(drop(r, y), s)))$

Frame axioms continued

- Frame axioms do not logically follow from precondition and effect axioms.
- They are called frame axioms because they limit or frame the effects of actions.

Why do we need frame axioms 1

A typical kind of task in reasoning about actions is to check whether

- a certain sequence of actions $a_1, ..., a_n$ will succeed (bring about some desired state of the world)
- a certain sequence of actions is possible

In both cases, some relevant information about S_0 is given (which fluents hold in S_0).

Why do we need frame axioms 2

- The precondition and effects of actions are used to determine which fluents will be true in $do(a_n, do(a_{n-1}, \dots do(a_1, S_0) \dots)$.
- Some fluent may be a precondition of some action a_i which is true in S_0 and is unchanged by a_1, \ldots, a_{i-1} .
- However we cannot derive that it is unchanged from just the precondition and effect axioms for a_1, \ldots, a_{i-1} : need to also have explicit frame axioms.

Frame problem

■ Frame problem is the problem of representing frame conditions coincisely (*not* with an axiom for each pair of action and fluent!).

Solution to the frame problem

- For each fluent $F(\bar{x}, s)$ (where \bar{x} are all the free variables of the fluent) we collect together all positive effect axioms.
- For example, if Broken(x, s) has two positive effect axioms: $\forall x \forall s \ (Fragile(x) \supset Broken(x, do(drop(x), s)))$

```
\forall x \forall s (Broken(x, do(break(x), s)))
```

- and together they can be written as: $\forall x \forall a \forall s ((Fragile(x) \land a = drop(x)) \lor (a = break(x))$ $\supset Broken(x, do(a, s)))$
- In general, have an expression $\forall \bar{x} \forall a \forall s (\Pi_F(\bar{x}, a, s) \supset F(\bar{x}, do(a, s)))$

Solution to the frame problem continued

■ Same for the negative effect axioms:

$$\forall \bar{x} \forall a \forall s (N_F(\bar{x}, a, s) \supset \neg F(\bar{x}, do(a, s)))$$

For example:

$$\forall \bar{x} \forall a \forall s (a = fix(x) \supset \neg Broken(x, do(a, s)))$$

Solution to the frame problem continued

■ Once we have a single formula Π_F for all actions which make F(x,s) true and a single formula N_F for all actions which make F false, we can write explanation closure axioms:

```
\forall \bar{x} \forall a \forall s (\neg F(\bar{x}, s) \land F(\bar{x}, do(a, s)) \supset \Pi_F(\bar{x}, a, s)) 
\forall \bar{x} \forall a \forall s (F(\bar{x}, s) \land \neg F(\bar{x}, do(a, s)) \supset N_F(\bar{x}, a, s))
```

- They replace all frame axioms by saying that F only becomes true if Π_F holds (only certain actions in certain circumstances make F true) F only becomes false if N_F is true
- Π_F and N_F are short, and explanation axioms entail all the frame axioms (under the assumptions of deterministic actions and only change as a result of actions).

Successor state axioms

- If some additional assumptions hold, namely:
 - \blacksquare no action has both a positive and negative effect on a fluent F,
 - action terms can only be equal if they have the same action name applied to the same arguments

then explanation closure axioms can be combined into a successor state axiom for a fluent:

$$\forall \bar{x} \forall a \forall s (F(\bar{x}, do(a, s)) \equiv \Pi_F(\bar{x}, a, s) \lor (F(\bar{x}, s) \land \neg N_F(\bar{x}, a, s)))$$

Under those assumptions, all that is needed to solve the frame problem and describe the actions and fluents completely are: precondition axioms and successor state axioms

Summary: Describing actions I

- "Effect" axiom—describe changes due to action $\forall s (AtGold(s) \supset Holding(Gold, do(Grab, s)))$
- "Frame" axiom—describe *non-changes* due to action $\forall s \ (HaveArrow(s) \supset HaveArrow(do(Grab, s)))$
- Frame problem: find an elegant way to handle non-change
 (a) representation—avoid frame axioms
 (b) inference—avoid repeated "copy-overs" to keep track of state
- Qualification problem: true descriptions of real actions require endless caveats—what if gold is slippery or nailed down or . . .
- Ramification problem: real actions have many secondary consequences—what about the dust on the gold, wear and tear on gloves, ...

Describing actions II

- Successor-state axioms solve the representational frame problem
- Each axiom is about a *predicate* rather than about an action:

P true afterwards \equiv an action made P true or P true already and no action made P false

■ For holding the gold: $\forall a \forall s Holding(Gold, do(a, s)) \equiv [(a = Grab \land AtGold(s)) \lor (Holding(Gold, s) \land a \neq Release)]$

Making plans in situation calculus

- Initial condition in KB: $At(Agent, [1, 1], S_0)$ $At(Gold, [1, 2], S_0)$
- Query: $KB \models (?)\exists s \ Holding(Gold, s))$ i.e., in what situation will I be holding the gold?
- Answer: $s/do(Grab, do(Forward, S_0))$ i.e., go forward and then grab the gold

Making plans: A better way

- Represent plans as action sequences $[a_1, a_2, ..., a_n]$
- doPlan(p, s) is the result of executing p in s
- Then the query $(KB, \exists p \ (Holding(Gold, doPlan(p, S_0))))$ has the solution p/[Forward, Grab]
- Definition of *doPlan* in terms of *do*: $\forall sdoPlan([],s) = s \forall a \forall p \forall s(doPlan([a|p],s) = doPlan(p,do(a,s))$
- Planning systems are special-purpose reasoners designed to do this type of inference more efficiently than a general-purpose reasoner

Summary

- Situation calculus provides conventions for describing actions and change in FOL
- can formulate planning as inference on a situation calculus KB
- Next lecture: Planning.
 Brachman and Levesque, Chapter 15.
 Russell and Norvig, 3rd ed., Chapter 10.1-10.2. (or other editions, Classical Planning).

Knowledge representation and reasoning Lecture 18: Planning

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Plan of the lecture

- What is Planning
- Classical Planning
- 3 Planning problem
- Forward and regression planning

What is Planning

- Planning is a reasoning problem:
- what actions (plan) to perform in order to make some condition (goal) true
- Planning is central to AI as the study of intelligent behaviour achieved through computational means
- In general, in real world, it is a very difficult problem

Classical Planning

Classical planning approach makes several assumptions to simplify this problem:

- Environment is deterministic
- Environment is observable
- Environment is static (it only changes in response to the agent's actions)

STRIPS operators

- STRIPS planning language (Fikes and Nilsson, 1971, derives from work at SRI International on robot called Shakey)
- goals are conjunctions of atoms (positive literals). We will often replace conjunctions of literals with sets of literals (meaning, all of the literals in the set are true)
- actions descriptions (action schemas) assume finite preconditions and effects of fixed form:
 - Precondition: conjunction of positive literals (we will write it as a set)
 - Effect: conjunction of literals (or a set of literals)

ACTION: buy(x)

PRECONDITION: At(p), Sells(p, x)

EFFECT: Have(x)



PDDL

- Planning Domain Definition Language
- Less restrictive than STRIPS
- Preconditions and goals can contain negative literals
- Other levels in PDDL also allow action durations, resource requirements etc. (not in this lecture)

Add and Delete lists

Given an action schema

ACTION: a

PRECONDITION: some literals

EFFECT: E_1, \ldots, E_m

- Add(a) = {E | E is a positive literal in EFFECT} (positive effects of a)
- $Del(a) = \{P \mid E = \neg P \text{ where } E \in \mathsf{EffECT}\}$ (atoms appearing with negation in the effect of a)

Planning domain

- Planning domain is described by giving a list of fluents and action schemas
- Fluents are predicates, have no situation argument
- States are sets of ground fluents; fluents which are not mentioned in a state description are false (closed world assumption)
- a is possible in s if precondition of a is true in s
- the state resulting from executing *a* in *s*,

$$do(s, a) = (s - Del(a)) \cup Add(a)$$

Example (slightly modified)

```
ACTION: buy(x)
PRECONDITION: At(p), Sells(p, x), Have(Money)
EFFECT: Have(x), \neg Have(Money)

\blacksquare Del(buy(Jaguar)) = \{Have(Money)\}
```

- Add(buy(Jaguar)) = {Have(Jaguar)}
- If s =
- {At(JDealer), Sells(JDealer, Jaguar), Blue(Sky), Have(Money)},
- \blacksquare buy(Jaguar) is possible in s
- $do(s, buy(Jaguar) = (s \{Have(Money)\}) \cup \{Have(Jaguar)\} = \{At(JDealer), Sells(JDealer, Jaguar), Blue(Sky), Have(Jaguar)\}$

Planning problem

- Planning problem = planning domain + objects + initial state + goal
- Goal is a conjunction of literals: $Have(Jaguar) \land \neg At(Jail)$
- Can solve planning problem using search

State and goal description

- State descriptions are always ground (no variables)
- Goal description may have variables: $At(x) \land Have(y)$
- A property with a variable such as At(x) is satisfied at a state if there is a way of substituting an object for x so that the resulting formula is true in the state
- An atomic ground formula *At(Home)* is true iff it is in the state description
- A negation of a ground atom $\neg At(G)$ is true iff the atom At(G) is not in the state description.

Forward and regression planning

- Usual search: forward search from the initial state to a goal state
- Nothing prevents us from searching from a goal state back to the initial state
- Sometimes given the branching factor it is more efficient to search backward
- Motivating example: imagine trying to figure out how to get to some small place with few traffic connections from somewhere with a lot of traffic connections

Simple example of forward planning

Planning domain:

- Fluents : At(x) (at place x), Sells(x, y) (shop x sells y), Have(x) (have x)
- Two action schemas:

```
ACTION: buy(x)
```

PRECONDITION: At(p), Sells(p, x), Have(Money)

EFFECT: Have(x), $\neg Have(Money)$

ACTION: go(x, y)

PRECONDITION: At(x), $x \neq y$

EFFECT: At(y), $\neg At(x)$

Simple example of forward planning 2

- Planning problem: planning domain above plus
- Objects: *Money*, *J* (for Jaguar), *Home*, *G* (for Garage)
- Initial state: At(Home), Have(Money), Sells(G, J)
- Goal state: *Have*(*J*)

Simple example of forward planning 3

$$s_1 = \{At(Home), Have(Money), Sells(G, J)\}$$
 $buy(x)$ not available for any x (don't have $Sells(Home, x)$)
$$\downarrow go(Home, G)$$
 $s_2 = \{At(G), Have(Money), Sells(G, J)\}$
 $go(G, Home)$ also available
$$\downarrow buy(J)$$
 $s_3 = \{At(G), Have(J), Sells(G, J)\}$

Heuristics for forward planning

- Similar to search, cf *A**: performance improves by orders of magnitude if a good heuristic is used
- Number of fluents in the goal which will be satisfied by the next action
- add more edges to the graph (make more actions possible), and use solutions to the resulting problem as a heuristic. (There are often more efficient algorithms to solve the relaxed problem.) Examples: remove (some) preconditions, ignore delete lists
- For example, in 8 puzzle assume tiles can move to occupied spaces = Manhattan distance heuristic
- abstract the problem (make the search space smaller)

Backward (regression) planning

- Also called relevant-states search
- Start at the goal state(s) and do regression (go back).
- To be precise, there we start with a ground goal description *g* which describes a set of states (all those where Have(J) holds but Have(Money) may or may not hold, for example).

Backward (regression) planning 2

- Given a goal description g and a ground action a, the regression from g over a gives a state description g':
- $g' = (g Add(a)) \cup \{Precondition(a)\}$
- For example, if the goal is Have(J), and a is buy(J)
- $g' = (\{Have(J)\} \{Have(J)\}) \cup \{At(p), Sells(p, J), Have(Money)\} = \{At(p), Sells(p, J), Have(Money)\}$
- note that g' is partially uninstantiated (p is a free variable). In our example, there is only one match for p, namely G, but in general there may be several.

Backward (regression) planning 3

- Which actions to regress over?
- Relevant actions: have an effect which is in the set of goal elements and no effect which negates an element of the goal.
- For example, buy(J) is a relevant action.
- Search backwards from *g*, remembering the actions and checking whether we reached an expression applicable to the initial state.

Simple example of backward planning

Have(J)

 $\uparrow buy(J)$

At(x), Have(Money), Sells(x, J)

Does not match the initial state yet

$$\uparrow go(y,x)$$

At(y), Have(Money), Sells(x, J)

Matches the initial state with y/Home and x/G



Comparison of forward and backward planning

- Usually lots of actions available for forward planning
- Easier to find heuristics for forward planning
- Backward planning considers a lot fewer actions/relevant states than forward search, but uses sets of states (g, g') hard to come up with good heuristics.

Use of logic and deduction

- In situation calculus, planning is deduction
- In 'normal' planning, we only need to check whether a state description entails some property, for example, $s \models P(A, B) \land \neg Q(A)$
- In simple cases, like in this lecture, this just involves checking that P(A, B) is in the list of properties s has, and Q(A) is not (closed world assumption: if Q(A) is not listed, then $\neg Q(A)$ must be true)
- However, often planning domains are described using additional axioms, and then checking $s \models P(A, B)$ may involve more complex reasoning (whether P(A, B) follows from the description of s and the axioms).

What next

- Please do an informal exercise on planning (on moodle, together with an answer)
- Formal exercise will be along the same lines
- Next lecture: Planning continued.
- Brachman and Levesque, Chapter 15.
- Russell and Norvig, Chapter on Classical Planning.
- Rich and Knight, Chapter on Goal Stack Planning.

Knowledge representation and reasoning Lecture 19: Planning 2

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Plan of the lecture

Recap: Planning problem

Forward and regression planning

Goal stack planning. Sussman anomaly

Planning domain

- Fluents or predicates which are used to describe preconditions and effects of actions
- For example, in the blocks world domain:
 - \blacksquare Block(x): x is a block
 - lacksquare On(x, y): x is on y, where y is either another block or table
 - Clear(x): there is nothing on top of block x
- Action schemas: available actions and their postconditions and effects. For example,

ACTION: moveToTable(b, x):

PRECONDITION: Block(b), Block(x), On(b, x), Clear(b)

EFFECT: $On(b, Table), Clear(x), \neg On(b, x)$

Example action schemas for blocks world

```
ACTION: move(b, x, y):

PRECOND: Block(b), Block(y), On(b, x), Clear(b), Clear(y), x \neq y

EFFECT: On(b, y), Clear(x), \neg On(b, x), \neg Clear(y)

ACTION: moveToTable(b, x):

PRECONDITION: Block(b), Block(x), On(b, x), Clear(b)

EFFECT: On(b, Table), Clear(x), \neg On(b, x)
```

Add and delete lists

Given an action schema

ACTION: a

PRECONDITION: some literals

EFFECT: E_1, \ldots, E_m

- Add(a) = {E | E is a positive literal in EFFECT} (positive effects of a)
- $Del(a) = \{P \mid E = \neg P \text{ where } E \in \mathsf{EffECT}\}$ (atoms appearing with negation in the effect of a)

Add and delete list example

```
ACTION: move(b, x, y):
PRECOND: Block(b), Block(y), On(b, x), Clear(b), Clear(y), x \neq y
EFFECT: On(b, y), Clear(x), \neg On(b, x), \neg Clear(y)
```

- $Add(move(b, x, y)) = \{On(b, y), Clear(x)\}$
- $Del(move(b, x, y)) = \{On(b, x), Clear(y)\}$

Planning problem

- Planning domain
- Objects (what can be substituted for variables)
- Initial state: a list of positive ground (no variables) literals, which are properties that hold in the state.
- Using Closed World Assumption, only describe what holds, and all the rest is assumed false
- Goal state: what literals should hold in the goal state. Can contain variables, which are assumed to be existentially quantifed.

Planning problem example

- planning domain as before
- objects: blocks A, B, C
- initial state: $\{Block(A), Block(B), Block(C), Clear(C), Clear(A), On(C, B), On(A, Table), On(B, Table)\}$. In this state, On(A, Table) is true and $\neg On(C, Table)$ is true.
- Example of a non-ground goal: On(x, B) as a goal means something should be on top of B; it is true in the initial state because x can be substituted for C.

Solving the planning problem

- Can be solved using search
- State space is not explicitly given; states are all possible sets of positive ground fluents
- Operators are actions; $do(s, a) = (s Del(a)) \cup Add(a)$
- Plan = sequence of actions from initial state to a goal state, as in classical search

Forward or progressive planning

Algorithm from the textbook; S is current state, S' next (progressed) state

Input: a state and a goal Output: a plan or fail. ProgPlan[S,Goal] =

If Goal is satisfied in S, then return empty plan

For each operator o such that precond(o) is satisfied in S:

Let S' = S + add(o) - del(o)

- . Let plan = ProgPlan[S',Goal]
- . If plan \neq fail, then return [act(o); plan]

End for

Return fail

Regression planning

Algorithm from the textbook; G is the goal, G' is regressed goal

```
Input: a state and a goal Output: a plan or fail. RegrPlan[S,Goal] = If Goal is satisfied in S, then return empty plan For each operator o such that del(o) \cap Goal = \emptyset. Let Goal' = Goal + precond(o) - add(o)
```

If plan \neq fail, then return [plan; act(o)]

Let plan = RegrPlan[S,Goal']

End for

Return fail

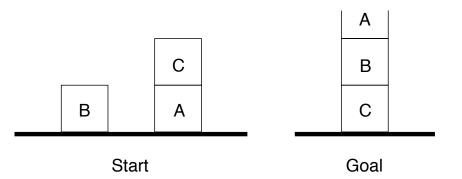
Goal stack planning

- One of the earlier planning algorithms called goal stack planning. It was used by STRIPS.
- We work backwards from the goal, looking for an operator which has one or more of the goal literals as one of its effects and then trying to satisfy the preconditions of the operator.
- The preconditions of the operator become subgoals that must be satisfied. We keep doing this until we reach the initial state.
- Goal stack planning uses a stack to hold goals and actions to satisfy the goals, and a knowledge base to hold the current state, action schemas and domain axioms
- Goal stack is like a node in a search tree; if there is a choice of action, we create branches

Goal stack planning pseudocode

- Push the original goal on the stack. Repeat until the stack is empty:
- If stack top is a compound goal, push its unsatisfied subgoals on the stack.
- If stack top is a single unsatisfied goal, replace it by an action that makes it satisfied and push the action's precondition on the stack.
- If stack top is an action, pop it from the stack, execute it and change the knowledge base by the action's effects.
- If stack top is a satisfied goal, pop it from the stack.

Goal stack planning example



Goal stack planning 1

(I do pushing the subgoals at the same step as the compound goal.) The order of subgoals is up to us; we could have put On(B, C) on top

$$On(A, B)$$

 $On(B, C)$
 $On(C, Table)$
 $On(A, B) \land On(B, C) \land On(C, Table)$

$$S = \{On(C, A), On(A, Table), On(B, Table), Clear(B), Clear(C)\}$$

plan = []

The top of the stack is a single unsatisfied goal. We push the action which would achieve it, and its preconditions.

Goal stack planning 2

```
On(A, Table)

Clear(B)

Clear(A)

On(A, Table) \land Clear(A) \land Clear(B)

move(A, x, B)

On(A, B)

On(B, C)

On(C, Table)

On(A, B) \land On(B, C) \land On(C, Table)
```

$$S = \{On(C, A), On(A, Table), On(B, Table), Clear(B), Clear(C)\}$$

plan = []

The top of the stack is a satisfied goal. We pop the stack (twice).

Clear(A)

Goal stack planning 3

```
On(A, Table) \wedge Clear(A) \wedge Clear(B)

move(A, Table, B)

On(A, B)

On(B, C)

On(C, Table)

On(A, B) \wedge On(B, C) \wedge On(C, Table)
```

$$S = \{On(C, A), On(A, Table), On(B, Table), Clear(B), Clear(C)\}$$

plan = []

The top of the stack is an unsatisfied goal. We push the action which would achieve it, and its preconditions.

Goal stack planning 4

```
On(C,A)
Clear(C)
On(C, A) \wedge Clear(C)
moveToTable(C, A)
Clear(A)
On(A, Table) \land Clear(A) \land Clear(B)
move(A, Table, B)
On(A, B)
On(B,C)
On(C, Table)
On(A, B) \wedge On(B, C) \wedge On(C, Table)
```

$$S = \{On(C, A), On(A, Table), On(B, Table), Clear(B), Clear(C)\}$$

plan = []

The top of the stack is a satisfied goal. We pop the stack (three times).

Goal stack planning 5

```
moveToTable(C, A)

Clear(A)

On(A, Table) \land Clear(A) \land Clear(B)

move(A, Table, B)

On(A, B)

On(B, C)

On(C, Table)

On(A, B) \land On(B, C) \land On(C, Table)
```

$$S = \{On(C, A), On(A, Table), On(B, Table), Clear(B), Clear(C)\}$$

plan = []

The top of the stack is an action. We execute it, update the state with its effects, and add it to the plan.

Clear(A)

Goal stack planning 6

```
On(A, Table) \wedge Clear(A) \wedge Clear(B)

move(A, Table, B)

On(A, B)

On(B, C)

On(C, Table)

On(A, B) \wedge On(B, C) \wedge On(C, Table)
```

{On(C, Table), On(A, Table), On(B, Table), Clear(A), Clear(B), Clear(C)}

The top of the stack is a satisfied goal. We pop the stack (twice).

plan = [moveToTable(C, A)]

S =

move(A, Table, B)

On(A, B)

Goal stack planning 7

plan = [moveToTable(C, A)]

its effects, and add it to the plan.

```
On(B,C)
                  On(C, Table)
                  On(A, B) \wedge On(B, C) \wedge On(C, Table)
{On(C, Table), On(A, Table), On(B, Table), Clear(A), Clear(B), Clear(C)}
```

The top of the stack is an action. We execute it, update the state with

S =

On(A, B)

Goal stack planning 8

```
On(B,C)

On(C,Table)

On(A,B) \land On(B,C) \land On(C,Table)

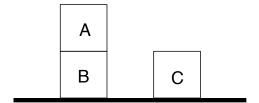
S = \{On(C,Table), On(A,B), On(B,Table), Clear(A), Clear(C)\}

plan = [moveToTable(C,A), move(A,Table,B)]

top of the stack is a satisfied goal
```

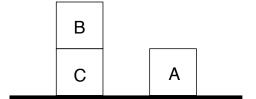
Goal stack planning 9a

the current state is



Goal stack planning 9b

If we follow the same process for the On(B, C) goal, we end up in the state



Goal stack planning 10

Now we finally can move *A* on top of *B*, but the resulting plan is redundant:

moveToTable(C, A) move(A, Table, B) moveToTable(A, B) move(B, Table, C) move(A, Table, B)

There are techniques for 'fixing' inefficient plans (where something is done and then undone) but it is difficult in general (when it is not straight one after another)

Why this is an instructive example

- Sussman anomaly (called 'anomaly' because it seemed to make sense for a conjunctive goals to first achieve one goal and then achieve another goal, and then the complete goal would be achieved) is instructive,
- because it shows that although planning has the advantage over search in that states are factored and we can split the goal into subgoals, it is not straightforward
- **a** achieving one goal (On(A, B)) destroys preconditions of an action which is necessary to achieve the other goal (On(B, C)), namely Clear(B).
- Such interaction between actions is called clobbering.
- in the next lecture, I will talk about a solution to this problem (partial order planning)

Next lecture

- still planning (and SET and SEM)
- Partial order planning: Russell and Norvig, 3rd ed., 10.4.4.
- Goal stack planning was based on Elaine Rich and Kevin Knight, Artificial Intelligence textbook.

Knowledge representation and reasoning Lecture 20: Planning 3

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Plan of the lecture

Plan of the lecture

- SET and SEM
- Partial order planning (based on Russell and Norvig, Russell's slides)
- Overview of planning algorithms and systems

Outline

- ♦ Totally vs partially ordered plans
- ♦ Partial-order planning
- \Diamond Examples

Totally vs partially ordered plans

So far we produced a linear sequence of actions (totally ordered plan)

Often it does not matter in which order some of the actions are executed

For problems with independent subproblems often easier to find a **partially** ordered plan: a plan which is a set of actions and a set of constraints $Before(a_i, a_i)$

Partially ordered plans are created by a search through a space of plans (rather than the state space)

Partially ordered plans

Partially ordered collection of steps with

Start step has the initial state description as its effect Finish step has the goal description as its precondition causal links from outcome of one step to precondition of another temporal ordering between pairs of steps

Open condition = precondition of a step not yet causally linked

A plan is complete iff every precondition is achieved

A precondition is achieved iff it is the effect of an earlier step and no possibly intervening step undoes it

Example

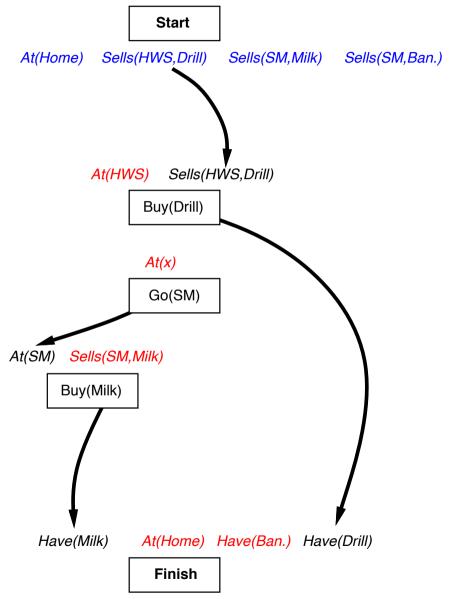
Start

At(Home) Sells(HWS,Drill) Sells(SM,Milk) Sells(SM,Ban.)

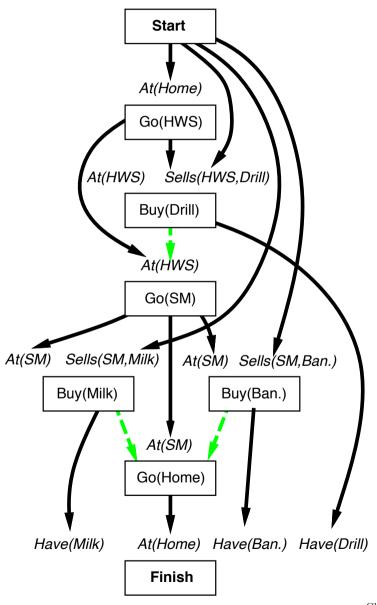
Have(Milk) At(Home) Have(Ban.) Have(Drill)

Finish

Example



Example



Planning process

Operators on partial plans:

add a link from an existing action to an open condition add a step to fulfill an open condition order one step wrt another to remove possible conflicts

Gradually move from incomplete/vague plans to complete, correct plans

Backtrack if an open condition is unachievable or if a conflict is unresolvable

POP algorithm sketch

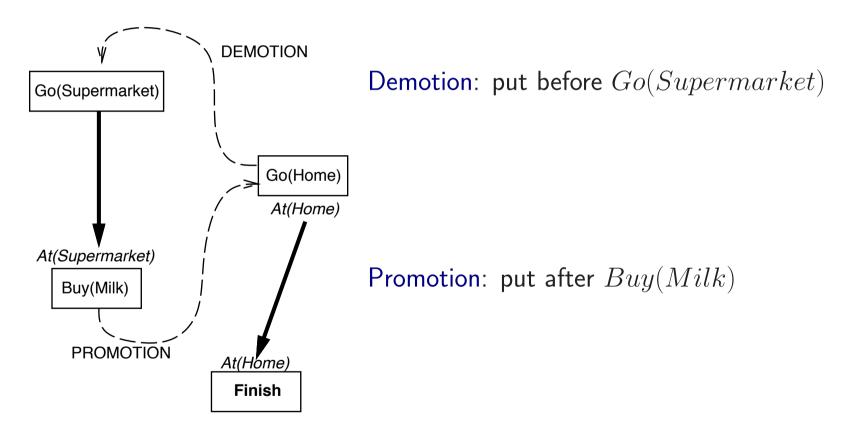
```
function POP(initial, goal, actions) returns plan
   plan \leftarrow Make-Minimal-Plan(initial, goal)
   loop do
       if SOLUTION? (plan) then return plan
       S_{need}, c \leftarrow \text{Select-Subgoal}(plan)
       Choose-Action (plan, actions, S_{need}, c)
       RESOLVE-THREATS (plan)
   end
function Select-Subgoal (plan) returns S_{need}, c
   pick a plan step S_{need} from STEPS( plan)
       with a precondition c that has not been achieved
   return S_{need}, c
```

POP algorithm contd.

```
procedure Choose-Action(plan, actions, S_{need}, c)
   choose a step S_{add} from actions or STEPS(plan) that has c as an effect
   if there is no such step then fail
   add the causal link S_{add} \xrightarrow{c} S_{need} to Links (plan)
   add the ordering constraint S_{add} \prec S_{need} to Orderings (plan)
   if S_{add} is a newly added step from actions then
        add S_{add} to STEPS( plan)
        add Start \prec S_{add} \prec Finish to Orderings (plan)
procedure Resolve-Threats(plan)
   for each S_{threat} that threatens a link S_i \xrightarrow{c} S_j in LINKS (plan) do
        choose either
              Demotion: Add S_{threat} \prec S_i to Orderings (plan)
              Promotion: Add S_i \prec S_{threat} to Orderings (plan)
        if not Consistent (plan) then fail
   end
```

Clobbering and promotion/demotion

A clobberer is a potentially intervening step that destroys the condition achieved by a causal link. E.g., Go(Home) clobbers At(Supermarket):



Properties of POP

Nondeterministic algorithm: backtracks at choice points on failure:

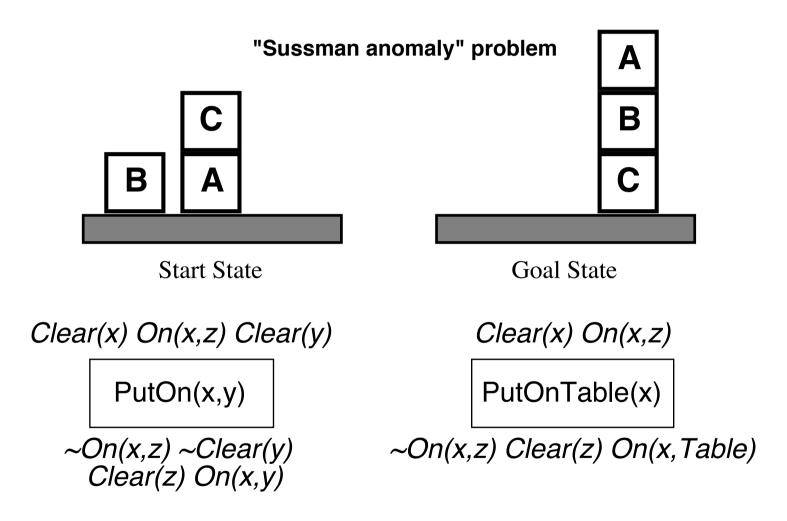
- choice of S_{add} to achieve S_{need}
- choice of demotion or promotion for clobberer
- selection of S_{need} is irrevocable

POP is sound, complete, and systematic (no repetition)

Can be made efficient with good heuristics derived from problem description

Particularly good for problems with many loosely related subgoals

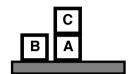
Example: Blocks world



+ several inequality constraints

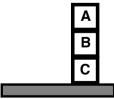
START

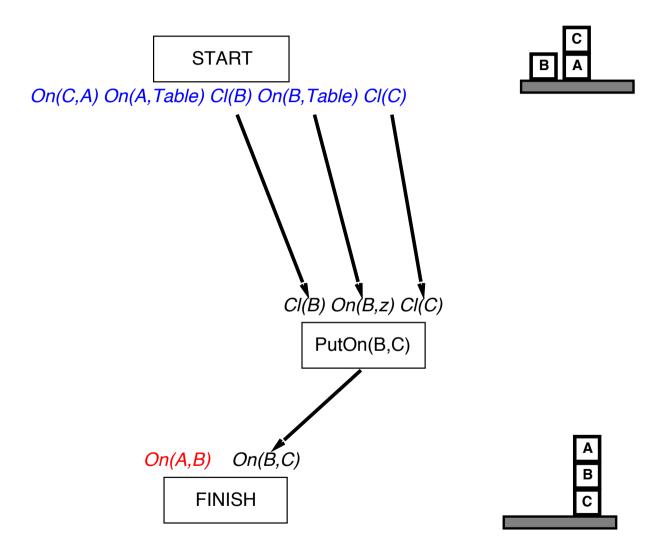
On(C,A) On(A, Table) Cl(B) On(B, Table) Cl(C)

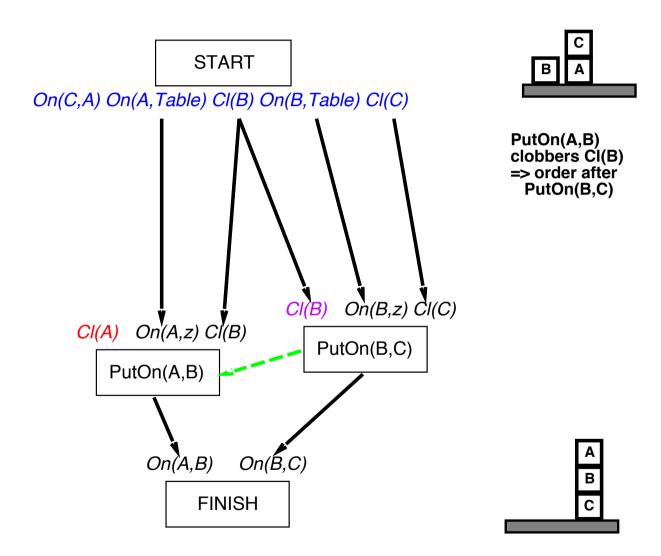


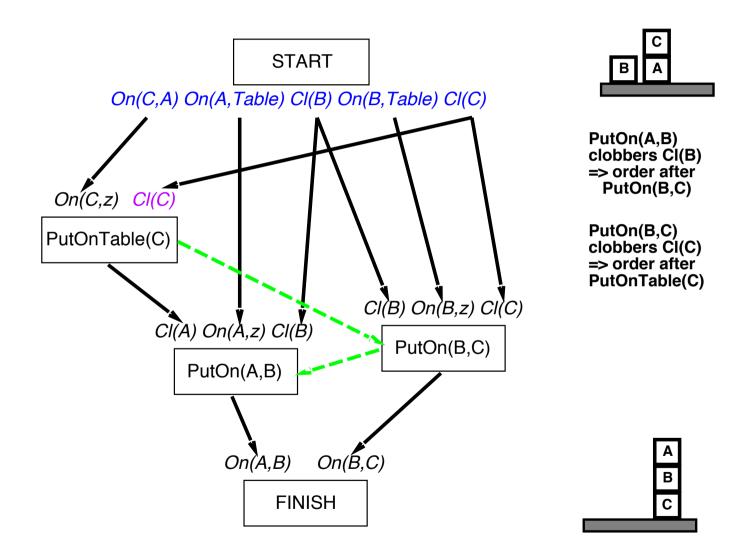
On(A,B) On(B,C)

FINISH









Plan of the lecture

Other planning approaches

- SatPlan: reduction to propositional reasoning, and checking for satisfiability.
- Can check whether a plan of fixed length exists
- Hierarchical planning (planning with abstraction): first find a plan with high-level abstract actions, then refine it
- Planning with time and resources, and scheduling plans

The complexity of classical planning

PlanSAT is the question whether there exists any plan that solves a given planning problem

Bounded PlanSAT is the question whether there exists a plan of length k or less

PlanSAT is about **satisficing** (want any solution, not necessarily the cheapest or the shortest)

Bounded PlanSAT can be used to ask for the optimal solution

If in the PDDL language we do not allow functional symbols, both problems are decidable

Complexity of both problems is PSPACE (can be solved by a Turing machine which uses polynomial amount of space)

 $NP \subseteq PSPACE$ (PSPACE is even harder than NP)

Some of the top-performing systems

International planning competition winners (from Russell and Norvig, 3rd edition):

Year	Track	Winning systems (approaches)
2008	Optimal	Gamer (symbolic bi-directional search)
2008	Satisficing	LAMA (fast forward search with FF heuristic)
2006	Optimal	SATPlan, MAXPlan (boolean satisfiability)
2006	Satisficing	SGPlan (forward search, partition into independent subproblems
2004	Optimal	SATPlan (boolean satisfiability)
2004	Satisficing	Fast Diagonally Forward (forward search with causal graph)
2002	Automated	LPG (local search, constraint satisfaction)
2002	Hand-coded	TLPLan (temporal action logic with control rules for forward searc
2000	Automated	FF (forward search)
2000	Hand-coded	TalPlanner (temporal action logic with control rules for forward sea
1998	Automated	IPP (planning graphs); HSP (forward search)

What follows for the algorithms

If a planning system based on a particular planning algorithm is very fast it does not mean necessarily that the algorithm is 'better'

Sat solvers are very fast, but one may argue that it is not very practical to propositionalise planning problems

Forward planning with good heuristics can be very fast but again may be not always practically possible

Partial order planners are considered to be very flexible and generally useful, although they don't feature in the winners table...

Plan of the lecture

Next lecture

- Reasoning with uncertainty
- Brachman and Levesque, chapter Chapter 12, slides 202-216.
- Revision advice
- I can also answer revision questions during the lab on Monday
- No lecture next Thursday (13th of December)

G53KRR

Development cycle of a knowledge-based system Knowledge acquisition

Plan of the lecture

- Development cycle of a knowledge-based system
- 2 Expert systems
- 3 Knowledge acquisition
- 4 Decision tables
- Modern uses of rules: semantic web, business rules
- 6 Rules in Java



Recommended reading for this lecture

- D. Partridge, K.M. Hussain. Knowledge-based information systems. London: McGraw-Hill, 1995, Ch.6,7. (development cycle, decision tables)
- E. Rich, K. Knight. *Artificial Intelligence*. McGraw Hill, 1991. Ch. 20.4 (Knowledge Acquisition).
- Semantic web http://www.w3.org/2001/sw/
- RuleML http://www.ruleml.org/
- Business rules and Java Rules Engine API (JSR)
 https://www.oracle.com/technetwork/articles/
 java/javarule-139829.html
- Jess http://herzberg.ca.sandia.gov/jess/



Development cycle of a knowledge-based system

- 1. Plan knowledge base (the content of the knowledge base, relevant inputs and outputs, strategy for testing, knowledge dictionary, concepts etc. are identified.)
- 2. Select domain experts and knowledge sources
- 3. Acquire (elicit) knowledge
- 4. Formulate and represent knowledge (knowledge is formulated in the form suitable for inference)
- 5. Implement knowledge base (knowledge is encoded in machine-readable form.)
- 6. Test knowledge base
- depending on the results: continue with knowledge acquisition or go to 7.
- 7. Systems test

Expert systems

- An expert system is a production systems which simulates behaviour of experts
- For example: MYCIN (diagnosis of bacterial diseases, 1970s), XCON (system for configuring VAX computers, 1978)
- Typical example of knowledge-based systems in the 80s

Knowledge acquisition: non-automatic methods

- Interviews with domain experts
- (Extracting knowledge from a human is often called knowledge elicitation)
- Iterative process, hard to get right first time.
- Human experts usually find it very difficult to state all the data relevant for a given problem.

Knowledge acquisition: automatic and semi-automatic methods (for expert systems)

- Programs which compile dependency networks during interviews with experts (MOLE, SALT)
- Programs using learning (META-DENDRAL)

Using dependency networks to acquire knowledge

- MOLE (Elsheman, 1988) works for systems which classify cases as instances of fixed categories, such as a fixed number of possible diagnoses. It builds an inference network similar to belief networks we will see later in the module
- SALT (Marcus and McDermott, 1989) works for open-ended sets of solutions, such as design problems; builds a dependency network and compiles into a set of production rules.

Using learning to acquire knowledge

- Learning decision diagrams from a set of prositive and negative instances of a concept (e.g. when to approve a loan application)
- Learning rules from a set of positive and negative instances META-DENDRAL (Mitchell 1978) learned how to determine structure of complex chemical compounds

Particular technique: decision tables

- A useful way of systematising knowledge preparatory to representing it using production rules
- can be compiled during interviews with experts or reading manuals or example sets

Decision tables

■ A decision table has the following structure:

Conditions	Decision rule		
Condition stubs	Condition entries		
Action stubs	Action entries		

- where condition stubs are criteria relevant for a decision, action stubs are possible actions, condition entries are Y,N and (should be true, should be false, not relevant) and action entries are X (for take this action) or blank.
- A decision rule is represented by a vertical column of condition and action entries.

Example

	Rule 1	Rule 2	Rule 3	Rule 4	Rule 5	Else
cash	Υ	Υ	Υ	N	N	
order > 100	Υ	Ν	Ν	-	-	
order \geq 50	Υ	Υ	Ν	-	-	
order < 50	N	Ν	Υ	-	-	
credit record good	-	-	-	Υ	N	
give 20% discount	Х					
give 10 % discount		Χ				
accept order			Χ	Χ		
reject order					Χ	
exception report						Χ



Example: rules

- Rule 1: if cash and order > 100 then give 20% discount
- Rule 2: if cash and 50 ≤ order ≤ 100 then give 10 % discount
- Rule 3: if cash and order < 50 then accept order</p>
- Rule 4: if not cash and credit record good then accept order
- Rule 5: **if not** cash **and not** credit record good **then** reject order
- Else generate an exception report.

Semantic web

- Aspiration: turn information available on the web into a huge knowledge base (integrated, readable and usable by machines ...)
- Formats for integration
- Languages for representing knowledge
- Ontology languages (description logics) in the following lecture

Rule ML

- Rule Markup Language (RuleML): specifying Web interchange format for rules
- Motivation comes from various aspects of Semantic Web:
 - Rules marked up for e-commerce (business rules)
 - XML transformation rules
 - Rules used for declarative specification of web services
 - Intelligent agents using rules
- XML-like specification for each ruleset: rule conditions, rule conclusions, direction (backward, forward, bidirectional).

Business rules

- A business rule is a statement that defines or constrains some aspect of the business
- Declarative, easy to modify; the idea is to separate dynamically changing rules which may apply for example only in the sales period from the application source code (for example on-line shop or rental business)
- Rules have a similar spirit to the discount example in the decision table
- Examples: IBM example of business rules:

```
https://www.ibm.com/support/knowledgecenter/en/
SSPJVK/DigitalRecommendations/UserGuide/
examplebusinessrules_nextgen.html
```

Java Rule Engine API

- Java Rule Engine API (JSR-94) is a lightweight programming interface that constitutes a standard API for acquiring and using a rule engine.
- From the specification: 'Addresses the community need to reduce the cost associated with incorporating business logic within applications and the community need to reduce the cost associated with implementing platform-level business logic tools and services.'
- javax.rules and javax.rules.admin packages.

Jess

- Jess is an expert system shell (can fill in your own rules, the engine already exists) written in Java
- Implemented using Rete algorithm (efficient incremental rule matching)
- Can be downloaded for free from http://herzberg.ca.sandia.gov/jess for educational use
- Rules can be specified in Jess rule language or XML; rule language is LISP-like:

```
(defrule welcome-toddlers (person {age < 3})

⇒
```

(println "Hello, little one!"))

■ LHS is a pattern (if a person has age less than 3 years) and RHS is an action (function call, in particular can insert new facts).

Exercise

■ Construct a decision table for the following piece of Lenton local knowledge: When a burglar alarm sounds, if it is in one of students' houses where alarm sounds every week, ignore it. Otherwise have a look outside and if the house looks not broken into and there is nobody moving inside it, ignore the alarm. Otherwise call police.