

Discussion note

The output \bar{p}_K is given by *Equation: (1)*, which is a static equation

$$\bar{p}_K = K^T \bar{H}_T^{-T} f_T(A_2^T q_C + A_3 K \bar{d}_K - A_3 D v_D \sigma) - \underbrace{K^T \bar{H}_T^{-T} \hat{H}_T^T (\hat{p} + \hat{h})}_{\text{Linear term}} - K^T \bar{h}. \quad (1)$$

We consider it as an input-output model where:

$$\begin{aligned} K^T \bar{h} &= \bar{h}_K && \text{is the elevation of inlets,} \\ \hat{p} &&& \text{is the elevation of WTs,} \\ \Lambda \dot{\hat{p}} &= -(\hat{H}_C - \hat{H}_T \bar{H}_T^{-1} \bar{H}_C) q_C - \hat{H}_T \bar{H}_T^{-1} K \bar{d}_K + \hat{H}_T \bar{H}_T^{-1} D v_D \sigma. \end{aligned} \quad (2)$$

$$f_C(q_C) - A_1(\hat{p} + \hat{h}) + A_2 f_T(A_2^T q_C + A_3 K \bar{d}_K - A_3 D v_D \sigma) = 0. \quad (3)$$

where

$$\begin{aligned} A_1 &= \hat{H}_C^T - \bar{H}_C^T \bar{H}_T^{-T} \hat{H}_T^T, \\ A_2 &= -\bar{H}_T^{-1} \bar{H}_C, \\ A_3 &= \bar{H}_T^{-1}. \end{aligned}$$