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Problem 1

→  $(1-x)y'' = 4xy' + 5y = \cos x$

$q_2(x) y^{(2)} + q_1(x) y' + q_0(x) y = g(x)$

→ We can say that is linear equation.

Problem 2

→  $x^3 y' + dx^3 - (dy/dx)^2 + y = 0$

∴  $y''' = d^3 y / dx^3$

∴ We can say that this equation is linear.

Problem = 3

$$xy^3 - x^3 \frac{dy}{dx} + Qy = 0$$

this equation is Bernoulli

~~Q3~~

Problem = 4

$$xy' + y = 0$$

$$y' + \frac{1}{x}y = 0$$

$$y = e^{-\int \frac{1}{x} dx}$$

$$= e^{-\ln x}$$

$$= e^{-\ln x}$$

→ Problem-5

$$y' + 20y = 24 \quad y(0) = 1$$

$$y' = 24 - 20y$$

$$y' = -20(y - 6/5)$$

$$\frac{dy}{dx} = -20(y - 6/5)$$

$$\frac{dy}{y - 6/5} = -20 dx$$

take integration on both side

$$y = y - 6/5$$

$$dy = dy$$

$$\int \frac{dy}{y - 6/5} = \int -20 dx$$

$$\ln|y - 6/5| = -20x$$

$$\int \frac{g_1}{g_2} = \int \frac{g_1}{g_2} \cdot \frac{g_2}{g_2} = \int \frac{g_1 g_2}{g_2^2}$$

$$g_1 = g_2$$

$$1 = \frac{g_1}{g_2}$$

Let's integrate on both sides

$$\int \frac{g_1}{g_2} = \int 1$$

$$\ln g_1 - \ln g_2 = \ln g_2 + \ln C$$

$$\ln \frac{g_1}{g_2} = \ln g_2 + \ln C$$

$$\ln g_1 - \ln g_2 = \ln g_2 + \ln C$$

$$\ln \frac{g_1}{g_2} = \ln g_2 + \ln C$$

$$\ln \frac{g_1}{g_2} = \ln g_2 + \ln C$$