Create an enumerated type for the days of the week.

```
Inductive day : Type :=
  | monday : day
  | tuesday : day
  | wednesday : day
  | thursday : day
  | friday : day
  | saturday : day
  | sunday : day.
```

Write a function `next_weekday`.

```
Definition next_weekday (d:day) : day :=
  match d with
  | monday => tuesday
  | tuesday => wednesday
  | wednesday => thursday
  | thursday => friday
  | friday => monday
  | saturday => monday
  | sunday => monday
  end.
```

Prove that tuesday is two weekdays after saturday.

```
Example test_next_weekday:
  (next_weekday (next_weekday saturday)) = tuesday.
Proof. simpl. reflexivity. Qed.
```

Create an enumerated type for booleans.

```
Inductive bool : Type :=
  | true : bool
  | false : bool.
```

Define a boolean negation function.

```
Definition negb (b:bool) : bool :=
  match b with
  | true => false
  | false => true
  end.
```

Define a function for boolean conjunction.

```
Definition andb (b1:bool) (b2:bool) : bool :=
  match b1 with
  | true => b2
  | false => false
  end.
```

Define a function for boolean disjunction.

```
Definition orb (b1:bool) (b2:bool) : bool :=
  match b1 with
  | true => true
  | false => b2
  end.
```

Define a polymorphic expression that can inhabit any type.

```
Definition admit {T: Type} : T. Admitted.
```

Define a function for boolean nand.

```
Definition nandb (b1:bool) (b2:bool) : bool := negb (andb b1 b2).
```

Create a type for natural numbers.

```
Inductive nat : Type :=
  | O : nat
  | S : nat -> nat.
```

Define a function for integer predecessor.

```
Definition pred (n:nat) : nat :=
  match n with
  | O    => O
  | S n' => n'
  end.
```

Define a "minus two" function.

```
Definition minustwo (n:nat) : nat :=
  match n with
  | O         => O
  | S O       => O
  | S (S n') => n'
  end.
```

Define a function for testing whether a natural number is even.

```
Fixpoint evenb (n:nat) : bool :=
  match n with
  | O        => true
  | S O      => false
  | S (S n') => evenb n'
  end.
```

Define a function for testing whether a natural number is odd.

```
Definition oddb (n:nat) : bool := negb (evenb n).
```

Define a function for adding natural numbers.

```
Fixpoint plus (n:nat) (m:nat) : nat :=
  match n with
  | O    => m
  | S n' => S (plus n' m)
  end.
```

Define a function for multiplying natural numbers.

```
Fixpoint mult (n m:nat) : nat :=
  match n with
  | O    => O
  | S n' => plus m (mult n' m)
  end.
```

Define a function for subtracting natural numbers.

```
Fixpoint minus (n m:nat) : nat :=
  match n, m with
  | O , _       => O
  | S _ , O     => n
  | S n', S m' => minus n' m'
  end.
```

Define a function for exponentiating natural numbers.

```
Fixpoint exp (base power:nat) : nat :=
  match power with
    | O   => S O
    | S p => mult base (exp base p)
  end.
```