

In the standard library.

A set of data values.

```
Inductive bool : Type :=  
  | true  : bool  
  | false : bool.
```

```
Definition negb (b : bool) : bool :=  
  match b with  
  | true => false  
  | false => true  
end.
```

```
Definition andb (b1:bool) (b2:bool) : bool :=  
  match b1 with  
  | true => b2  
  | false => false  
end.
```

Example test_negation:

(negb true) = false.

Proof. simpl. reflexivity. Qed.

- Use `Eval` on a test case and observe the result.
- Use `Example/Theorem/whatever` to record expected result, then as `Coq` to verify.
- "extract" function `Definition` to OCaml, Scheme, or Haskell.

Eval simpl in (negb true).

- andb
- orb
- negb

admit **fills in holes** in Definitions.

Admitted **fills in holes** in proofs.

bool->bool->bool

It causes Coq to print the type of an expression.

If you put declarations between `Module X` and `End X` then after `End` the definitions are referred to as `X.foo`.

```
Inductive nat : Type :=  
  | O : nat  
  | S : nat -> nat.
```

A set of *expressions*, inductively defined. The definition tells us exactly how members of the type can be constructed, and excludes all other expressions.

Functions come with *computation rules*. Data constructors have no behavior attached.

- Definition
- Fixpoint **in case of recursion**

Structural (or *primitive*) recursion. That means recursive calls must be on strictly smaller values, guaranteeing termination.

The following are equivalent:

$(n\ m : \text{nat})$

$(n : \text{nat})\ (m : \text{nat})$

A comma is placed between then in the scrutinee and between the two sides of each matching pattern.

With `Notation` constructions which also define associativity and precedence.

- Numerals
- Operators
- Collections syntax

expression%notation_scope

compute

Simplifies both sides before testing (including by using `simpl`).

Among other things, `reflexivity` may expand definitions.
`simpl` never will.

For a conditional it introduces the antecedent as an assumption. For a universally quantified statement it introduces an arbitrary element of the domain and discharges the quantifier.