"A type system is a tractable syntactic method for proving the absence of certain program behaviors by classifying phrases according to the kinds of values they compute."

Those "types" are tags on the heap for identifying different kinds of values. They are not static *approximations* of runtime values.

They can only prove the *absence* of some behaviors, never their presence. They therefore must reject some programs that will also lack these behaviors at runtime.

To allow more programs to be typed by improving the accuracy of static type approximations.

... run-time type errors.

- Early detection of some programming errors.
- Maintenance/refactoring.
- Abstraction.
- Documentation.
- Language safety.
- Efficiency.

Pierce: A safe language guarantees the integrity of its abstractions.
Cardelli: A safe language traps its errors, meaning they halt computation immediately or raise an exception that can be handled. Unsafe languages have untrapped errors that allow computation to proceed.
Also: A safe language lacks undefined behavior. Or in other words, it's portable between implementations.

There is little marginal cost to checking the safety of all operations at run-time once most are.

To distinguish between integers and floating-point numbers, for the sake of efficiency.