## RANDOM NUMBER GENERATION AND SIMULATION EXERCISE 8

# Area estimation using Monte Carlo method

Author Cesare De Cal Professor
Annie Cuyt
Assistant Professor
Ferre Knaepkens

## 1 Introduction

The exercise asks to approximate the area of the figure defined by

$$\begin{cases} 1 \le x \le 3 \\ -1 \le y \le 4 \\ x^3 + y^3 \le 29 \\ y \ge e^x - 2 \end{cases}$$

using the Monte Carlo method.

#### 2 Tools

To solve this exercise, I've used the following libraries and programming languages:

- C
- Intel Math Kernel Library (more specifically, the Vector Statistical Library)
- OpenMP
- C Math Library

I've used the following Intel MKL routines:

- vslNewStream(&stream, brng, seed)
- vslLeapfrogStream(stream, k, nstreams)
- vsRngUniform(method, stream, nrRandomNumbers, array, start, end)
- vslDeleteStream(&streamToDelete)

OpenMP provides a user-friendly interface to build multi-threading applications. I've used the following methods and procedures:

- omp\_get\_max\_threads()
- #pragma omp parallel private(nrOfThreads, threadID)
- omp\_get\_thread\_num()

To make the code more clear, I've also wrote my own function isInsideArea(x,y) which checks if a given pair of coordinates (x,y) is inside the area drawn by the system of inequalities. To get started with the exercise, I have used the template file template.c provided on the website.

To compile and run the code on my own machine with gcc, I created a Makefile based on the compiler options and link line specified here:

https://software.intel.com/en-us/articles/intel-mkl-link-line-advisor.

### 3 Computation

On a high level picture, the Monte Carlo method in this exercise works by generating random (x, y) coordinates in the rectangle formed by

$$\begin{cases} 1 \le x \le 3 \\ -1 \le y \le 4 \end{cases}$$

And then checks if the points satisfy the following inequalities using the isInsideArea(x,y) function I wrote.

$$\begin{cases} x^3 + y^3 \le 29\\ y \ge e^x - 2 \end{cases}$$

I define two constants LOOPS and  $\mathbb{N}$ , which represent the number of iterations to compute and the numbers of points to generate for each iteration respectively. There's also a seed used to generate random numbers.

The area is given by the ratio of the points inside the system to all the random points N. This process is repeated LOOPS times, and in each iteration an area is calculated. At the end of the iterations, I calculate the average of all the areas calculated inside the loops.

To make this happen, I first initialize the threads using the VSL\_BRNG\_MCG59 random number generator. Then I create two independent streams of uniformly distributed random numbers with vdRngUniform in the (1,3) and (-1,4) intervals. If the points belong to figure, I increase a local variable which keeps count of the points inside the figure. At the end of the iteration, I calcolate the area by dividing the count by LOOPS.

As mentioned before, the average is taken out of all the areas calculated in the iterations. The result is 7.581675111111076e-02 with N and LOOPS equal to 30000 and seed equal to -87654321.

- 4 Plots
- 5 Observations