### Systems of Linear Equations

#### Exercise 7

# Systems of Linear Equations Report

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## 1 Introduction

The purpose of this exercise is to use solve a linear system using LU decomposition.

#### 2 Tools

The following programming language and libraries have been used in this exercise:

- C
- GSL (GNU Scientific Library)

The following GSL data types have been used in the exercise:

- gsl\_vector
- gsl\_matrix
- gsl\_permutation

The following GSL methods have been used in the exercise:

- gsl\_matrix\_alloc(size1, size2)
- gsl\_matrix\_set\_zero(matrix)
- gsl\_matrix\_set(matrix, row, column, value)
- gsl\_matrix\_get(matrix, row, column)
- gsl\_vector\_alloc(size)
- gsl\_vector\_set\_zero(vector)
- gsl\_vector\_set(size)
- gsl\_vector\_get(vector, index)
- gsl\_permutation\_alloc(size)

In order to factorize a matrix into the LU decomposition, and then solve the square system Ax = b using the decomposition of A, I've used the following methods:

- gsl\_linalg\_LU\_decomp(A, permutation, signum)
- gsl\_linalg\_LU\_solve(LU, permutation, b, x)

#### 3 Solving the system

In order to solve the system, I first need to build the matrix A by understanding how it's build. The requirements are to build a tridiagonal matrix with the values -1 on the adjacent upper diagonal, the entries +1 on the adjacent lower diagonal, and on the main diagonal the values  $b_{-i}$ , with i = 1, ..., n given by

$$b_i = \frac{2(i+1)}{3}, \quad i+1=3,6,9,\dots$$
  
 $b_i = 1, \quad i+1=2,4,5,7,8,\dots$ 

By looking closely at the first rule, we see that the i+1 are all multiples of 3 (i+1=3\*k, for some k). Hence the i are of the form i=3\*k-1, for some k. For n=10, for example, this is what the matrix approximately looks like:

[1.0000	-1.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000 7
1.0000	2.0000	-1.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	1.0000	1.0000	-1.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	1.0000	1.0000	-1.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	1.0000	4.0000	-1.0000	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	1.0000	1.0000	-1.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	1.0000	-1.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	6.0000	-1.0000	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	1.0000	-1.0000
[0.0000]	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	1.0000

## 4 Observations