hw01

May 7, 2019

1 Classification using neural networks

```
1
In [1]: import random
        random.seed(1234)
  2
In [1]: from keras.datasets import fashion_mnist
Using TensorFlow backend.
In [2]: (x_train, y_train), (x_test, y_test) = fashion_mnist.load_data()
In [4]: print(x_train.shape)
        print(y_train.shape)
        print(x_test.shape)
        print(y_test.shape)
(60000, 28, 28)
(60000,)
(10000, 28, 28)
(10000,)
In [24]: #converting the data to a 2D tensor
         x_{train} = x_{train.reshape([60000, 28*28]).astype('float32')/255
         x_{test} = x_{test.reshape}([10000, 28*28]).astype('float32')/255
In [25]: from keras.utils import to_categorical
In [26]: #change individual values between 0 and 1
         y_train = to_categorical(y_train)
         y_test = to_categorical(y_test)
In [27]: from sklearn.model_selection import train_test_split
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In [28]: x_train, x_valid, y_train, y_valid = train_test_split(x_train, y_train, test_size=0.1)
 3
In [29]: from keras import models
    from keras import layers
     import tensorflow as tf
 i. Initial test
In [30]: network = models.Sequential()
    network.add(layers.Dense(512, activation='relu', input_shape=(28*28,)))
    network.add(layers.Dense(512, activation='relu'))
    network.add(layers.Dense(512, activation='relu'))
    network.add(layers.Dense(512, activation='relu'))
    network.add(layers.Dense(10, activation='softmax'))
    network.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['accura
    result = network.fit(x_train, y_train, validation_data=(x_valid, y_valid), epochs=200
Train on 50000 samples, validate on 10000 samples
Epoch 1/200
Epoch 2/200
Epoch 3/200
50000/50000 [============== ] - 3s 58us/step - loss: 0.4292 - acc: 0.8408 - val
Epoch 4/200
50000/50000 [============== ] - 3s 58us/step - loss: 0.3873 - acc: 0.8546 - val
Epoch 5/200
Epoch 6/200
Epoch 7/200
50000/50000 [============== ] - 3s 60us/step - loss: 0.3125 - acc: 0.8839 - val
Epoch 8/200
Epoch 9/200
Epoch 10/200
Epoch 11/200
Epoch 12/200
50000/50000 [============== ] - 3s 62us/step - loss: 0.2484 - acc: 0.9059 - val
Epoch 13/200
Epoch 14/200
Epoch 15/200
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50000/50000 [=============== ] - 3s 63us/step - loss: 0.2241 - acc: 0.9150 - val
Epoch 16/200
Epoch 17/200
Epoch 18/200
50000/50000 [=============== ] - 3s 64us/step - loss: 0.1979 - acc: 0.9233 - val
Epoch 19/200
Epoch 20/200
Epoch 21/200
Epoch 22/200
Epoch 23/200
Epoch 24/200
Epoch 25/200
Epoch 26/200
Epoch 27/200
Epoch 28/200
Epoch 29/200
Epoch 30/200
Epoch 31/200
50000/50000 [=============== ] - 3s 65us/step - loss: 0.1523 - acc: 0.9425 - val
Epoch 32/200
50000/50000 [============== ] - 3s 64us/step - loss: 0.1514 - acc: 0.9443 - val
Epoch 33/200
Epoch 34/200
Epoch 35/200
Epoch 36/200
Epoch 37/200
Epoch 38/200
Epoch 39/200
```

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Epoch 40/200
50000/50000 [============== ] - 3s 65us/step - loss: 0.1478 - acc: 0.9479 - val
Epoch 41/200
Epoch 42/200
Epoch 43/200
Epoch 44/200
50000/50000 [============== ] - 3s 66us/step - loss: 0.1274 - acc: 0.9533 - val
Epoch 45/200
Epoch 46/200
Epoch 47/200
Epoch 48/200
Epoch 49/200
Epoch 50/200
Epoch 51/200
Epoch 52/200
Epoch 53/200
Epoch 54/200
Epoch 55/200
50000/50000 [=============== ] - 3s 65us/step - loss: 0.1168 - acc: 0.9581 - val
Epoch 56/200
50000/50000 [============== ] - 3s 65us/step - loss: 0.1177 - acc: 0.9587 - val
Epoch 57/200
50000/50000 [=============== ] - 3s 65us/step - loss: 0.1189 - acc: 0.9584 - val
Epoch 58/200
Epoch 59/200
Epoch 60/200
Epoch 61/200
Epoch 62/200
Epoch 63/200
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Epoch 64/200
Epoch 65/200
Epoch 66/200
Epoch 67/200
Epoch 68/200
Epoch 69/200
Epoch 70/200
Epoch 71/200
Epoch 72/200
Epoch 73/200
Epoch 74/200
Epoch 75/200
Epoch 76/200
Epoch 77/200
Epoch 78/200
Epoch 79/200
50000/50000 [=============== ] - 3s 64us/step - loss: 0.1029 - acc: 0.9665 - val
Epoch 80/200
Epoch 81/200
Epoch 82/200
Epoch 83/200
Epoch 84/200
Epoch 85/200
Epoch 86/200
Epoch 87/200
```

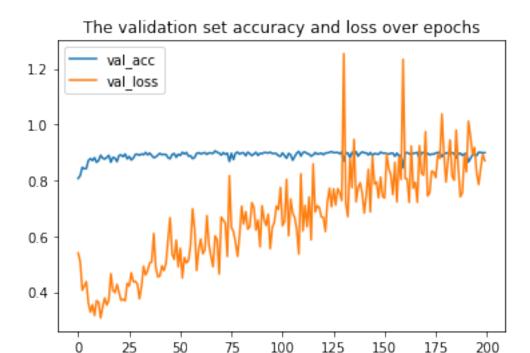
```
Epoch 88/200
Epoch 89/200
Epoch 90/200
Epoch 91/200
Epoch 92/200
50000/50000 [============== ] - 3s 65us/step - loss: 0.0901 - acc: 0.9701 - val
Epoch 93/200
Epoch 94/200
Epoch 95/200
Epoch 96/200
Epoch 97/200
Epoch 98/200
Epoch 99/200
Epoch 100/200
Epoch 101/200
Epoch 102/200
Epoch 103/200
50000/50000 [============== ] - 3s 65us/step - loss: 0.0908 - acc: 0.9741 - val
Epoch 104/200
50000/50000 [============== ] - 3s 68us/step - loss: 0.0950 - acc: 0.9727 - val
Epoch 105/200
50000/50000 [=============== ] - 3s 66us/step - loss: 0.0973 - acc: 0.9725 - val
Epoch 106/200
Epoch 107/200
Epoch 108/200
Epoch 109/200
Epoch 110/200
Epoch 111/200
```

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Epoch 112/200
50000/50000 [=============== ] - 3s 64us/step - loss: 0.0830 - acc: 0.9756 - val
Epoch 113/200
Epoch 114/200
Epoch 115/200
Epoch 116/200
Epoch 117/200
Epoch 118/200
Epoch 119/200
Epoch 120/200
Epoch 121/200
Epoch 122/200
Epoch 123/200
50000/50000 [=============== ] - 4s 73us/step - loss: 0.0724 - acc: 0.9783 - val
Epoch 124/200
Epoch 125/200
50000/50000 [=============== ] - 4s 73us/step - loss: 0.0809 - acc: 0.9763 - val
Epoch 126/200
Epoch 127/200
50000/50000 [============== ] - 4s 71us/step - loss: 0.0775 - acc: 0.9771 - val
Epoch 128/200
50000/50000 [============== ] - 3s 70us/step - loss: 0.0728 - acc: 0.9775 - val
Epoch 129/200
Epoch 130/200
Epoch 131/200
Epoch 132/200
Epoch 133/200
Epoch 134/200
Epoch 135/200
```

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Epoch 136/200
50000/50000 [=============== ] - 3s 64us/step - loss: 0.0687 - acc: 0.9801 - val
Epoch 137/200
50000/50000 [=============== ] - 3s 60us/step - loss: 0.0783 - acc: 0.9792 - val
Epoch 138/200
50000/50000 [=============== ] - 3s 60us/step - loss: 0.0785 - acc: 0.9790 - val
Epoch 139/200
50000/50000 [=============== ] - 3s 60us/step - loss: 0.0818 - acc: 0.9787 - val
Epoch 140/200
50000/50000 [============== ] - 3s 60us/step - loss: 0.0861 - acc: 0.9778 - val
Epoch 141/200
Epoch 142/200
Epoch 143/200
Epoch 144/200
Epoch 145/200
Epoch 146/200
Epoch 147/200
Epoch 148/200
Epoch 149/200
Epoch 150/200
Epoch 151/200
Epoch 152/200
50000/50000 [============== ] - 3s 62us/step - loss: 0.0734 - acc: 0.9813 - val
Epoch 153/200
Epoch 154/200
Epoch 155/200
Epoch 156/200
Epoch 157/200
Epoch 158/200
Epoch 159/200
```

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Epoch 160/200
Epoch 161/200
Epoch 162/200
Epoch 163/200
Epoch 164/200
50000/50000 [=============== ] - 3s 61us/step - loss: 0.0673 - acc: 0.9823 - val
Epoch 165/200
Epoch 166/200
Epoch 167/200
Epoch 168/200
Epoch 169/200
Epoch 170/200
Epoch 171/200
Epoch 172/200
Epoch 173/200
Epoch 174/200
Epoch 175/200
50000/50000 [============== ] - 3s 62us/step - loss: 0.0557 - acc: 0.9848 - val
Epoch 176/200
Epoch 177/200
Epoch 178/200
Epoch 179/200
Epoch 180/200
Epoch 181/200
Epoch 182/200
Epoch 183/200
```

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Epoch 184/200
50000/50000 [=============== ] - 3s 65us/step - loss: 0.0751 - acc: 0.9826 - val
Epoch 185/200
50000/50000 [=============== ] - 3s 64us/step - loss: 0.0603 - acc: 0.9843 - val
Epoch 186/200
Epoch 187/200
Epoch 188/200
Epoch 189/200
Epoch 190/200
Epoch 191/200
Epoch 192/200
Epoch 193/200
Epoch 194/200
Epoch 195/200
Epoch 196/200
Epoch 197/200
Epoch 198/200
Epoch 199/200
50000/50000 [=============== ] - 3s 61us/step - loss: 0.0648 - acc: 0.9856 - val
Epoch 200/200
50000/50000 [=============== ] - 3s 61us/step - loss: 0.0624 - acc: 0.9859 - val
In [31]: import matplotlib.pyplot as plt
In [32]: val_acc = result.history['val_acc']
   val_loss = result.history['val_loss']
   plt.plot(val_acc)
   plt.plot(val_loss)
   plt.legend(['val_acc', 'val_loss'])
   plt.title('The validation set accuracy and loss over epochs')
   plt.show()
```



From above plot we can see that the validation set accuracy remains the same over the epochs while the loss grows larger over the epochs. It suggests that the model performs worse along the epochs based on the validation dataset.

ii

Epoch 3/200

Epoch 4/200

50000/50000 [====

```
In [34]: network_dropout = models.Sequential()
                            network_dropout.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
                            network_dropout.add(layers.Dropout(0.5))
                            network_dropout.add(layers.Dense(512, activation='relu'))
                            network_dropout.add(layers.Dropout(0.5))
                            network_dropout.add(layers.Dense(512, activation='relu'))
                            network_dropout.add(layers.Dropout(0.5))
                            network_dropout.add(layers.Dense(512, activation='relu'))
                            network_dropout.add(layers.Dropout(0.5))
                            network_dropout.add(layers.Dense(10, activation='softmax'))
                            network_dropout.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics
                            result_dropout = network_dropout.fit(x_train, y_train, validation_data=(x_valid, y_valid, y_v
Train on 50000 samples, validate on 10000 samples
Epoch 1/200
50000/50000 [=====
                                                                                      =========] - 4s 89us/step - loss: 0.9804 - acc: 0.6346 - val
Epoch 2/200
50000/50000 [==
                                                                                                                                             - 4s 78us/step - loss: 0.5922 - acc: 0.7839 - val
```

=======] - 4s 78us/step - loss: 0.5146 - acc: 0.8160 - val

```
Epoch 5/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.4517 - acc: 0.8409 - val
Epoch 6/200
Epoch 7/200
Epoch 8/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.4010 - acc: 0.8588 - val
Epoch 9/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.3974 - acc: 0.8597 - val
Epoch 10/200
Epoch 11/200
Epoch 12/200
Epoch 13/200
Epoch 14/200
Epoch 15/200
Epoch 16/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3525 - acc: 0.8765 - val
Epoch 17/200
Epoch 18/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3402 - acc: 0.8795 - val
Epoch 19/200
Epoch 20/200
Epoch 21/200
Epoch 22/200
Epoch 23/200
Epoch 24/200
Epoch 25/200
Epoch 26/200
Epoch 27/200
Epoch 28/200
```

```
Epoch 29/200
Epoch 30/200
Epoch 31/200
Epoch 32/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3137 - acc: 0.8907 - val
Epoch 33/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.3091 - acc: 0.8936 - val
Epoch 34/200
Epoch 35/200
Epoch 36/200
Epoch 37/200
Epoch 38/200
Epoch 39/200
Epoch 40/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.3070 - acc: 0.8946 - val
Epoch 41/200
Epoch 42/200
Epoch 43/200
Epoch 44/200
Epoch 45/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.2939 - acc: 0.8983 - val
Epoch 46/200
50000/50000 [=============== ] - 4s 81us/step - loss: 0.2963 - acc: 0.8980 - val
Epoch 47/200
Epoch 48/200
Epoch 49/200
Epoch 50/200
Epoch 51/200
Epoch 52/200
```

```
Epoch 53/200
Epoch 54/200
Epoch 55/200
Epoch 56/200
Epoch 57/200
50000/50000 [============== ] - 4s 81us/step - loss: 0.2939 - acc: 0.9012 - val
Epoch 58/200
Epoch 59/200
Epoch 60/200
Epoch 61/200
Epoch 62/200
Epoch 63/200
Epoch 64/200
Epoch 65/200
Epoch 66/200
Epoch 67/200
Epoch 68/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.2891 - acc: 0.9054 - val
Epoch 69/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.2974 - acc: 0.9033 - val
Epoch 70/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.2946 - acc: 0.9032 - val
Epoch 71/200
Epoch 72/200
Epoch 73/200
Epoch 74/200
Epoch 75/200
Epoch 76/200
```

```
Epoch 77/200
Epoch 78/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.2954 - acc: 0.9055 - val
Epoch 79/200
Epoch 80/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.2930 - acc: 0.9061 - val
Epoch 81/200
50000/50000 [============== ] - 4s 82us/step - loss: 0.2949 - acc: 0.9052 - val
Epoch 82/200
Epoch 83/200
Epoch 84/200
Epoch 85/200
Epoch 86/200
Epoch 87/200
Epoch 88/200
Epoch 89/200
Epoch 90/200
Epoch 91/200
Epoch 92/200
Epoch 93/200
50000/50000 [============== ] - 4s 80us/step - loss: 0.3043 - acc: 0.9063 - val
Epoch 94/200
Epoch 95/200
Epoch 96/200
Epoch 97/200
Epoch 98/200
Epoch 99/200
Epoch 100/200
```

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Epoch 101/200
50000/50000 [=============== ] - 4s 81us/step - loss: 0.3043 - acc: 0.9077 - val
Epoch 102/200
Epoch 103/200
Epoch 104/200
Epoch 105/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.2998 - acc: 0.9091 - val
Epoch 106/200
Epoch 107/200
Epoch 108/200
Epoch 109/200
Epoch 110/200
Epoch 111/200
Epoch 112/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3052 - acc: 0.9093 - val
Epoch 113/200
Epoch 114/200
Epoch 115/200
Epoch 116/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3058 - acc: 0.9096 - val
Epoch 117/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3040 - acc: 0.9106 - val
Epoch 118/200
Epoch 119/200
Epoch 120/200
Epoch 121/200
Epoch 122/200
Epoch 123/200
Epoch 124/200
```

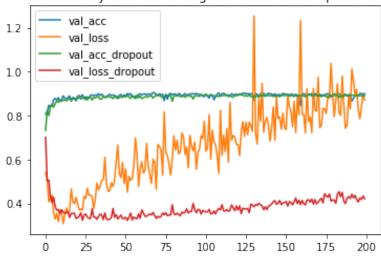
```
Epoch 125/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3154 - acc: 0.9097 - val
Epoch 126/200
Epoch 127/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3130 - acc: 0.9098 - val
Epoch 128/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3220 - acc: 0.9084 - val
Epoch 129/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3192 - acc: 0.9105 - val
Epoch 130/200
Epoch 131/200
Epoch 132/200
Epoch 133/200
Epoch 134/200
Epoch 135/200
Epoch 136/200
Epoch 137/200
Epoch 138/200
50000/50000 [================ ] - 4s 78us/step - loss: 0.3064 - acc: 0.9133 - val
Epoch 139/200
Epoch 140/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3273 - acc: 0.9102 - val
Epoch 141/200
50000/50000 [============== ] - 4s 80us/step - loss: 0.3276 - acc: 0.9107 - val
Epoch 142/200
Epoch 143/200
Epoch 144/200
Epoch 145/200
Epoch 146/200
Epoch 147/200
Epoch 148/200
```

```
Epoch 149/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3264 - acc: 0.9103 - val
Epoch 150/200
Epoch 151/200
Epoch 152/200
Epoch 153/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3375 - acc: 0.9098 - val
Epoch 154/200
Epoch 155/200
Epoch 156/200
Epoch 157/200
Epoch 158/200
Epoch 159/200
Epoch 160/200
Epoch 161/200
Epoch 162/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3173 - acc: 0.9145 - val
Epoch 163/200
Epoch 164/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3372 - acc: 0.9107 - val
Epoch 165/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.3378 - acc: 0.9121 - val
Epoch 166/200
Epoch 167/200
Epoch 168/200
Epoch 169/200
Epoch 170/200
Epoch 171/200
Epoch 172/200
```

```
Epoch 173/200
Epoch 174/200
Epoch 175/200
Epoch 176/200
Epoch 177/200
50000/50000 [============== ] - 4s 79us/step - loss: 0.3520 - acc: 0.9119 - val
Epoch 178/200
Epoch 179/200
Epoch 180/200
Epoch 181/200
Epoch 182/200
Epoch 183/200
Epoch 184/200
Epoch 185/200
Epoch 186/200
Epoch 187/200
Epoch 188/200
Epoch 189/200
50000/50000 [============== ] - 4s 87us/step - loss: 0.3524 - acc: 0.9106 - val
Epoch 190/200
Epoch 191/200
50000/50000 [=============== ] - 5s 90us/step - loss: 0.3671 - acc: 0.9111 - val
Epoch 192/200
Epoch 193/200
Epoch 194/200
Epoch 195/200
Epoch 196/200
```

```
Epoch 197/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.3526 - acc: 0.9118 - val
Epoch 198/200
50000/50000 [==
                             =======] - 4s 79us/step - loss: 0.3607 - acc: 0.9117 - val
Epoch 199/200
50000/50000 [=
                                     =] - 4s 80us/step - loss: 0.3545 - acc: 0.9122 - val
Epoch 200/200
50000/50000 [==
                                       - 4s 82us/step - loss: 0.3752 - acc: 0.9081 - val
In [35]: val_acc = result.history['val_acc']
        val_loss = result.history['val_loss']
       val_acc_dropout = result_dropout.history['val_acc']
       val_loss_dropout = result_dropout.history['val_loss']
       plt.plot(val_acc)
       plt.plot(val_loss)
       plt.plot(val_acc_dropout)
       plt.plot(val_loss_dropout)
       plt.legend(['val_acc', 'val_loss', 'val_acc_dropout', 'val_loss_dropout'])
       plt.title('The validation set accuracy and loss of original model and dropout model or
       plt.show()
```

The validation set accuracy and loss of original model and dropout model over epochs



Comparing to the first model, the second model is much better with lower validity loss, but the validity accuracy are similar between the two models.

iii. Weight regularization

```
network_L1.add(layers.Dense(10, activation='softmax'))
    network L1.compile(optimizer='rmsprop', loss='categorical crossentropy', metrics=['ac
    result_L1 = network_L1.fit(x_train, y_train, validation_data=(x_valid, y_valid), epoc
Train on 50000 samples, validate on 10000 samples
Epoch 1/200
50000/50000 [============= ] - 4s 83us/step - loss: 14.7979 - acc: 0.5434 - va
Epoch 2/200
50000/50000 [=============== ] - 4s 70us/step - loss: 3.0904 - acc: 0.6505 - val
Epoch 3/200
50000/50000 [============== ] - 3s 70us/step - loss: 2.2152 - acc: 0.6997 - val
Epoch 4/200
50000/50000 [=============== ] - 4s 70us/step - loss: 1.9088 - acc: 0.7312 - val
Epoch 5/200
Epoch 6/200
Epoch 7/200
Epoch 8/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.5483 - acc: 0.7784 - val
Epoch 9/200
Epoch 10/200
Epoch 11/200
Epoch 12/200
Epoch 13/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.4204 - acc: 0.7995 - val
Epoch 14/200
Epoch 15/200
Epoch 16/200
Epoch 17/200
Epoch 18/200
50000/50000 [=============== ] - 4s 72us/step - loss: 1.3532 - acc: 0.8106 - val
Epoch 19/200
Epoch 20/200
```

network_L1.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.l network_L1.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.l network_L1.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.l

```
Epoch 21/200
Epoch 22/200
Epoch 23/200
Epoch 24/200
Epoch 25/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.2973 - acc: 0.8209 - val
Epoch 26/200
Epoch 27/200
Epoch 28/200
Epoch 29/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.2792 - acc: 0.8238 - val
Epoch 30/200
Epoch 31/200
Epoch 32/200
Epoch 33/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.2707 - acc: 0.8249 - val
Epoch 34/200
Epoch 35/200
Epoch 36/200
Epoch 37/200
Epoch 38/200
Epoch 39/200
Epoch 40/200
Epoch 41/200
Epoch 42/200
Epoch 43/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.2400 - acc: 0.8317 - val
Epoch 44/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.2400 - acc: 0.8311 - val
```

```
Epoch 45/200
Epoch 46/200
Epoch 47/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.2317 - acc: 0.8327 - val
Epoch 48/200
Epoch 49/200
Epoch 50/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.2308 - acc: 0.8334 - val
Epoch 51/200
50000/50000 [=============== ] - 4s 72us/step - loss: 1.2261 - acc: 0.8344 - val
Epoch 52/200
Epoch 53/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.2269 - acc: 0.8338 - val
Epoch 54/200
Epoch 55/200
Epoch 56/200
Epoch 57/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.2183 - acc: 0.8342 - val
Epoch 58/200
Epoch 59/200
Epoch 60/200
Epoch 61/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.2139 - acc: 0.8359 - val
Epoch 62/200
Epoch 63/200
Epoch 64/200
Epoch 65/200
Epoch 66/200
Epoch 67/200
50000/50000 [============== ] - 4s 70us/step - loss: 1.2104 - acc: 0.8373 - val
Epoch 68/200
```

```
Epoch 69/200
Epoch 70/200
Epoch 71/200
Epoch 72/200
Epoch 73/200
Epoch 74/200
Epoch 75/200
Epoch 76/200
Epoch 77/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1964 - acc: 0.8413 - val
Epoch 78/200
Epoch 79/200
Epoch 80/200
Epoch 81/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1941 - acc: 0.8395 - val
Epoch 82/200
Epoch 83/200
Epoch 84/200
Epoch 85/200
Epoch 86/200
Epoch 87/200
Epoch 88/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1926 - acc: 0.8406 - val
Epoch 89/200
Epoch 90/200
Epoch 91/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.1870 - acc: 0.8418 - val
Epoch 92/200
50000/50000 [=============== ] - 4s 72us/step - loss: 1.1858 - acc: 0.8419 - val
```

```
Epoch 93/200
Epoch 94/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1813 - acc: 0.8431 - val
Epoch 95/200
Epoch 96/200
Epoch 97/200
50000/50000 [=============== ] - 4s 72us/step - loss: 1.1854 - acc: 0.8413 - val
Epoch 98/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1811 - acc: 0.8438 - val
Epoch 99/200
Epoch 100/200
Epoch 101/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1743 - acc: 0.8453 - val
Epoch 102/200
Epoch 103/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1794 - acc: 0.8419 - val
Epoch 104/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1747 - acc: 0.8459 - val
Epoch 105/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.1774 - acc: 0.8434 - val
Epoch 106/200
Epoch 107/200
Epoch 108/200
Epoch 109/200
Epoch 110/200
Epoch 111/200
Epoch 112/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1735 - acc: 0.8440 - val
Epoch 113/200
Epoch 114/200
Epoch 115/200
Epoch 116/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1729 - acc: 0.8443 - val
```

```
Epoch 117/200
Epoch 118/200
Epoch 119/200
Epoch 120/200
Epoch 121/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1712 - acc: 0.8447 - val
Epoch 122/200
Epoch 123/200
Epoch 124/200
Epoch 125/200
Epoch 126/200
Epoch 127/200
Epoch 128/200
Epoch 129/200
50000/50000 [============== ] - 4s 71us/step - loss: 1.1698 - acc: 0.8439 - val
Epoch 130/200
Epoch 131/200
Epoch 132/200
Epoch 133/200
Epoch 134/200
Epoch 135/200
Epoch 136/200
Epoch 137/200
Epoch 138/200
Epoch 139/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.1643 - acc: 0.8451 - val
Epoch 140/200
50000/50000 [============== ] - 4s 73us/step - loss: 1.1634 - acc: 0.8475 - val
```

```
Epoch 141/200
Epoch 142/200
Epoch 143/200
50000/50000 [=============== ] - 4s 77us/step - loss: 1.1618 - acc: 0.8467 - val
Epoch 144/200
Epoch 145/200
Epoch 146/200
Epoch 147/200
Epoch 148/200
Epoch 149/200
50000/50000 [============== ] - 4s 80us/step - loss: 1.1594 - acc: 0.8464 - val
Epoch 150/200
Epoch 151/200
Epoch 152/200
50000/50000 [=============== ] - 4s 78us/step - loss: 1.1589 - acc: 0.8481 - val
Epoch 153/200
50000/50000 [============== ] - 4s 76us/step - loss: 1.1575 - acc: 0.8473 - val
Epoch 154/200
Epoch 155/200
Epoch 156/200
Epoch 157/200
Epoch 158/200
Epoch 159/200
Epoch 160/200
Epoch 161/200
Epoch 162/200
Epoch 163/200
50000/50000 [============== ] - 4s 79us/step - loss: 1.1586 - acc: 0.8472 - val
Epoch 164/200
50000/50000 [============== ] - 4s 80us/step - loss: 1.1555 - acc: 0.8474 - val
```

```
Epoch 165/200
Epoch 166/200
Epoch 167/200
50000/50000 [=============== ] - 4s 77us/step - loss: 1.1543 - acc: 0.8478 - val
Epoch 168/200
Epoch 169/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1559 - acc: 0.8472 - val
Epoch 170/200
Epoch 171/200
Epoch 172/200
Epoch 173/200
Epoch 174/200
Epoch 175/200
Epoch 176/200
Epoch 177/200
50000/50000 [=============== ] - 3s 69us/step - loss: 1.1542 - acc: 0.8473 - val
Epoch 178/200
Epoch 179/200
Epoch 180/200
Epoch 181/200
50000/50000 [=============== ] - 4s 70us/step - loss: 1.1507 - acc: 0.8494 - val
Epoch 182/200
Epoch 183/200
Epoch 184/200
50000/50000 [=============== ] - 4s 71us/step - loss: 1.1484 - acc: 0.8499 - val
Epoch 185/200
Epoch 186/200
Epoch 187/200
50000/50000 [=============== ] - 4s 72us/step - loss: 1.1533 - acc: 0.8475 - val
Epoch 188/200
50000/50000 [============== ] - 4s 72us/step - loss: 1.1522 - acc: 0.8488 - val
```

```
Epoch 189/200
Epoch 190/200
Epoch 191/200
50000/50000 [=============== ] - 4s 76us/step - loss: 1.1495 - acc: 0.8493 - val
Epoch 192/200
Epoch 193/200
50000/50000 [=============== ] - 4s 75us/step - loss: 1.1511 - acc: 0.8497 - val
Epoch 194/200
Epoch 195/200
Epoch 196/200
Epoch 197/200
50000/50000 [============== ] - 4s 76us/step - loss: 1.1503 - acc: 0.8492 - val
Epoch 198/200
50000/50000 [=============== ] - 4s 77us/step - loss: 1.1493 - acc: 0.8490 - val
Epoch 199/200
50000/50000 [=============== ] - 4s 76us/step - loss: 1.1501 - acc: 0.8488 - val
Epoch 200/200
In [40]: network_L2 = models.Sequential()
    network_L2.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,), kernel_re
    network_L2.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.la
    network_L2.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.1:
    network L2.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers.l
    network_L2.add(layers.Dense(10, activation='softmax'))
    network_L2.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['ac
    result_L2 = network_L2.fit(x_train, y_train, validation_data=(x_valid, y_valid), epoc
Train on 50000 samples, validate on 10000 samples
Epoch 1/200
Epoch 2/200
Epoch 3/200
50000/50000 [=============== ] - 4s 76us/step - loss: 0.8948 - acc: 0.8105 - val
Epoch 4/200
Epoch 5/200
Epoch 6/200
```

```
Epoch 7/200
Epoch 8/200
Epoch 9/200
Epoch 10/200
Epoch 11/200
Epoch 12/200
50000/50000 [============== ] - 4s 77us/step - loss: 0.4941 - acc: 0.8654 - val
Epoch 13/200
Epoch 14/200
Epoch 15/200
Epoch 16/200
Epoch 17/200
50000/50000 [=============== ] - 4s 77us/step - loss: 0.4549 - acc: 0.8736 - val
Epoch 18/200
Epoch 19/200
50000/50000 [============== ] - 4s 76us/step - loss: 0.4451 - acc: 0.8756 - val
Epoch 20/200
Epoch 21/200
Epoch 22/200
Epoch 23/200
Epoch 24/200
Epoch 25/200
Epoch 26/200
50000/50000 [=============== ] - 5s 92us/step - loss: 0.4133 - acc: 0.8845 - val
Epoch 27/200
Epoch 28/200
Epoch 29/200
Epoch 30/200
50000/50000 [=============== ] - 4s 76us/step - loss: 0.4020 - acc: 0.8882 - val
```

```
Epoch 31/200
Epoch 32/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3981 - acc: 0.8898 - val
Epoch 33/200
Epoch 34/200
Epoch 35/200
Epoch 36/200
Epoch 37/200
Epoch 38/200
Epoch 39/200
Epoch 40/200
Epoch 41/200
50000/50000 [=============== ] - 4s 76us/step - loss: 0.3809 - acc: 0.8940 - val
Epoch 42/200
50000/50000 [=============== ] - 4s 76us/step - loss: 0.3787 - acc: 0.8944 - val
Epoch 43/200
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3788 - acc: 0.8959 - val
Epoch 44/200
Epoch 45/200
Epoch 46/200
Epoch 47/200
Epoch 48/200
Epoch 49/200
Epoch 50/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3700 - acc: 0.8973 - val
Epoch 51/200
Epoch 52/200
Epoch 53/200
Epoch 54/200
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3617 - acc: 0.9000 - val
```

```
Epoch 55/200
Epoch 56/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3648 - acc: 0.8987 - val
Epoch 57/200
Epoch 58/200
Epoch 59/200
50000/50000 [=============== ] - 4s 74us/step - loss: 0.3563 - acc: 0.9015 - val
Epoch 60/200
50000/50000 [=============== ] - 4s 75us/step - loss: 0.3585 - acc: 0.9002 - val
Epoch 61/200
Epoch 62/200
Epoch 63/200
Epoch 64/200
Epoch 65/200
Epoch 66/200
Epoch 67/200
50000/50000 [=============== ] - 4s 74us/step - loss: 0.3527 - acc: 0.9035 - val
Epoch 68/200
Epoch 69/200
Epoch 70/200
Epoch 71/200
50000/50000 [=============== ] - 4s 85us/step - loss: 0.3493 - acc: 0.9046 - val
Epoch 72/200
Epoch 73/200
Epoch 74/200
Epoch 75/200
Epoch 76/200
Epoch 77/200
Epoch 78/200
50000/50000 [============== ] - 4s 77us/step - loss: 0.3464 - acc: 0.9044 - val
```

```
Epoch 79/200
Epoch 80/200
Epoch 81/200
Epoch 82/200
Epoch 83/200
Epoch 84/200
Epoch 85/200
Epoch 86/200
Epoch 87/200
Epoch 88/200
Epoch 89/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3371 - acc: 0.9087 - val
Epoch 90/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3393 - acc: 0.9080 - val
Epoch 91/200
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3418 - acc: 0.9081 - val
Epoch 92/200
Epoch 93/200
Epoch 94/200
Epoch 95/200
Epoch 96/200
Epoch 97/200
Epoch 98/200
Epoch 99/200
Epoch 100/200
Epoch 101/200
Epoch 102/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3361 - acc: 0.9085 - val
```

```
Epoch 103/200
Epoch 104/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3357 - acc: 0.9108 - val
Epoch 105/200
Epoch 106/200
Epoch 107/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3332 - acc: 0.9103 - val
Epoch 108/200
Epoch 109/200
Epoch 110/200
Epoch 111/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3305 - acc: 0.9129 - val
Epoch 112/200
Epoch 113/200
Epoch 114/200
Epoch 115/200
50000/50000 [============== ] - 4s 83us/step - loss: 0.3315 - acc: 0.9105 - val
Epoch 116/200
Epoch 117/200
Epoch 118/200
Epoch 119/200
Epoch 120/200
Epoch 121/200
Epoch 122/200
50000/50000 [=============== ] - 4s 80us/step - loss: 0.3283 - acc: 0.9138 - val
Epoch 123/200
Epoch 124/200
50000/50000 [=============== ] - 4s 83us/step - loss: 0.3279 - acc: 0.9133 - val
Epoch 125/200
Epoch 126/200
50000/50000 [============== ] - 4s 81us/step - loss: 0.3271 - acc: 0.9138 - val
```

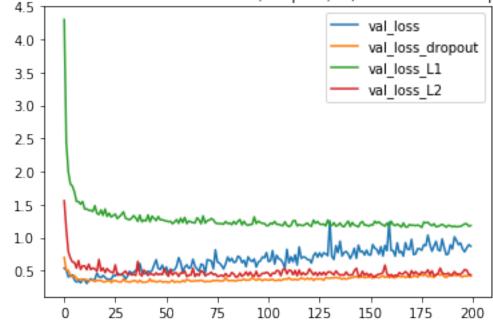
```
Epoch 127/200
Epoch 128/200
50000/50000 [=============== ] - 4s 81us/step - loss: 0.3263 - acc: 0.9130 - val
Epoch 129/200
50000/50000 [=============== ] - 4s 83us/step - loss: 0.3244 - acc: 0.9133 - val
Epoch 130/200
Epoch 131/200
Epoch 132/200
Epoch 133/200
Epoch 134/200
Epoch 135/200
Epoch 136/200
Epoch 137/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3259 - acc: 0.9137 - val
Epoch 138/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3229 - acc: 0.9147 - val
Epoch 139/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3233 - acc: 0.9160 - val
Epoch 140/200
Epoch 141/200
Epoch 142/200
Epoch 143/200
Epoch 144/200
Epoch 145/200
Epoch 146/200
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3246 - acc: 0.9137 - val
Epoch 147/200
Epoch 148/200
Epoch 149/200
50000/50000 [=============== ] - 4s 79us/step - loss: 0.3219 - acc: 0.9157 - val
Epoch 150/200
50000/50000 [============== ] - 4s 78us/step - loss: 0.3257 - acc: 0.9145 - val
```

```
Epoch 151/200
Epoch 152/200
Epoch 153/200
Epoch 154/200
Epoch 155/200
Epoch 156/200
Epoch 157/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3198 - acc: 0.9173 - val
Epoch 158/200
Epoch 159/200
Epoch 160/200
Epoch 161/200
Epoch 162/200
Epoch 163/200
Epoch 164/200
Epoch 165/200
Epoch 166/200
Epoch 167/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3177 - acc: 0.9179 - val
Epoch 168/200
Epoch 169/200
Epoch 170/200
Epoch 171/200
50000/50000 [=============== ] - 4s 78us/step - loss: 0.3200 - acc: 0.9159 - val
Epoch 172/200
Epoch 173/200
Epoch 174/200
50000/50000 [============== ] - 4s 85us/step - loss: 0.3154 - acc: 0.9174 - val
```

```
Epoch 175/200
Epoch 176/200
Epoch 177/200
50000/50000 [=============== ] - 4s 90us/step - loss: 0.3160 - acc: 0.9183 - val
Epoch 178/200
Epoch 179/200
Epoch 180/200
Epoch 181/200
Epoch 182/200
Epoch 183/200
50000/50000 [============== ] - 4s 71us/step - loss: 0.3143 - acc: 0.9182 - val
Epoch 184/200
Epoch 185/200
50000/50000 [=============== ] - 4s 72us/step - loss: 0.3130 - acc: 0.9193 - val
Epoch 186/200
50000/50000 [=============== ] - 4s 72us/step - loss: 0.3126 - acc: 0.9183 - val
Epoch 187/200
50000/50000 [============== ] - 4s 72us/step - loss: 0.3153 - acc: 0.9178 - val
Epoch 188/200
Epoch 189/200
Epoch 190/200
Epoch 191/200
50000/50000 [=============== ] - 4s 76us/step - loss: 0.3144 - acc: 0.9168 - val
Epoch 192/200
Epoch 193/200
Epoch 194/200
Epoch 195/200
Epoch 196/200
Epoch 197/200
Epoch 198/200
50000/50000 [=============== ] - 4s 74us/step - loss: 0.3115 - acc: 0.9196 - val
```

```
Epoch 199/200
Epoch 200/200
50000/50000 [====
                                 ====] - 4s 74us/step - loss: 0.3147 - acc: 0.9177 - val
In [43]: val_loss = result.history['val_loss']
       val_loss_dropout = result_dropout.history['val_loss']
       val_loss_L1 = result_L1.history['val_loss']
       val_loss_L2 = result_L2.history['val_loss']
       plt.plot(val_loss)
       plt.plot(val_loss_dropout)
       plt.plot(val_loss_L1)
       plt.plot(val_loss_L2)
       plt.legend(['val_loss', 'val_loss_dropout', 'val_loss_L1', 'val_loss_L2'])
       plt.title('The validation loss for the initial/dropout/L1/L2 model over epochs')
       plt.show()
```

The validation loss for the initial/dropout/L1/L2 model over epochs



From above plot we can see that, when epoch smaller than 150, the dropout model performs the best. When epoch larger than 150, the L2 model performs the best. *iv.alternative models*

```
In [45]: network_alt = models.Sequential()
    network_alt.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
    network_alt.add(layers.Dropout(0.5))
    network_alt.add(layers.Dense(512, activation='relu'))
```

```
network_alt.add(layers.Dropout(0.5))
   network_alt.add(layers.Dense(512, activation='relu'))
   network_alt.add(layers.Dropout(0.5))
   network_alt.add(layers.Dense(10, activation='softmax'))
   network alt.compile(optimizer='rmsprop', loss='categorical crossentropy', metrics=['a-
   result_alt = network_alt.fit(x_train, y_train, validation_data=(x_valid, y_valid), epo
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.3912 - acc: 0.8596 - val
Epoch 8/100
Epoch 9/100
Epoch 10/100
50000/50000 [=============== ] - 3s 61us/step - loss: 0.3614 - acc: 0.8700 - val
Epoch 11/100
50000/50000 [=============== ] - 3s 61us/step - loss: 0.3566 - acc: 0.8701 - val
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
```

```
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
50000/50000 [=============== ] - 3s 61us/step - loss: 0.3007 - acc: 0.8918 - val
Epoch 26/100
Epoch 27/100
Epoch 28/100
Epoch 29/100
Epoch 30/100
Epoch 31/100
Epoch 32/100
50000/50000 [=============== ] - 4s 72us/step - loss: 0.2822 - acc: 0.8973 - val
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
50000/50000 [=============== ] - 3s 62us/step - loss: 0.2747 - acc: 0.9023 - val
Epoch 40/100
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
```

```
Epoch 45/100
Epoch 46/100
Epoch 47/100
Epoch 48/100
Epoch 49/100
50000/50000 [=============== ] - 3s 65us/step - loss: 0.2577 - acc: 0.9084 - val
Epoch 50/100
Epoch 51/100
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
50000/50000 [=============== ] - 3s 65us/step - loss: 0.2475 - acc: 0.9114 - val
Epoch 59/100
Epoch 60/100
50000/50000 [============== ] - 3s 64us/step - loss: 0.2462 - acc: 0.9122 - val
Epoch 61/100
50000/50000 [============== ] - 3s 62us/step - loss: 0.2465 - acc: 0.9118 - val
Epoch 62/100
Epoch 63/100
Epoch 64/100
Epoch 65/100
Epoch 66/100
Epoch 67/100
Epoch 68/100
```

```
50000/50000 [=============== ] - 3s 65us/step - loss: 0.2407 - acc: 0.9145 - val
Epoch 69/100
Epoch 70/100
Epoch 71/100
Epoch 72/100
Epoch 73/100
50000/50000 [============== ] - 3s 65us/step - loss: 0.2367 - acc: 0.9169 - val
Epoch 74/100
Epoch 75/100
Epoch 76/100
Epoch 77/100
Epoch 78/100
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
Epoch 84/100
50000/50000 [=============== ] - 3s 63us/step - loss: 0.2286 - acc: 0.9198 - val
Epoch 85/100
50000/50000 [============== ] - 3s 65us/step - loss: 0.2278 - acc: 0.9211 - val
Epoch 86/100
Epoch 87/100
Epoch 88/100
Epoch 89/100
Epoch 90/100
Epoch 91/100
Epoch 92/100
```

```
Epoch 93/100
50000/50000 [=============== ] - 3s 65us/step - loss: 0.2210 - acc: 0.9231 - val
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
50000/50000 [============== ] - 4s 70us/step - loss: 0.2207 - acc: 0.9224 - val
Epoch 98/100
Epoch 99/100
Epoch 100/100
In [46]: network_alt2 = models.Sequential()
   network_alt2.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
   network_alt2.add(layers.Dropout(0.5))
   network_alt2.add(layers.Dense(512, activation='relu'))
   network_alt2.add(layers.Dropout(0.5))
   network_alt2.add(layers.Dense(512, activation='relu'))
   network_alt2.add(layers.Dropout(0.5))
   network_alt2.add(layers.Dense(512, activation='relu'))
   network_alt2.add(layers.Dropout(0.5))
   network_alt2.add(layers.Dense(10, activation='softmax'))
   network_alt2.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['
   result_alt2 = network_alt2.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
```

```
Epoch 8/100
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
50000/50000 [============== ] - 4s 83us/step - loss: 0.3630 - acc: 0.8719 - val
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
50000/50000 [=============== ] - 4s 84us/step - loss: 0.3411 - acc: 0.8789 - val
Epoch 19/100
Epoch 20/100
50000/50000 [============== ] - 4s 85us/step - loss: 0.3376 - acc: 0.8823 - val
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
Epoch 26/100
Epoch 27/100
50000/50000 [=============== ] - 4s 85us/step - loss: 0.3173 - acc: 0.8881 - val
Epoch 28/100
Epoch 29/100
Epoch 30/100
50000/50000 [============== ] - 4s 85us/step - loss: 0.3152 - acc: 0.8895 - val
Epoch 31/100
50000/50000 [=============== ] - 4s 84us/step - loss: 0.3122 - acc: 0.8900 - val
```

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Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
Epoch 40/100
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
Epoch 46/100
Epoch 47/100
Epoch 48/100
Epoch 49/100
Epoch 50/100
Epoch 51/100
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
50000/50000 [=============== ] - 4s 86us/step - loss: 0.2941 - acc: 0.9012 - val
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Epoch 56/100
Epoch 57/100
Epoch 58/100
Epoch 59/100
Epoch 60/100
Epoch 61/100
Epoch 62/100
Epoch 63/100
Epoch 64/100
50000/50000 [=============== ] - 4s 83us/step - loss: 0.3008 - acc: 0.9020 - val
Epoch 65/100
Epoch 66/100
50000/50000 [=============== ] - 4s 85us/step - loss: 0.2968 - acc: 0.9012 - val
Epoch 67/100
Epoch 68/100
50000/50000 [============== ] - 4s 83us/step - loss: 0.2963 - acc: 0.9015 - val
Epoch 69/100
Epoch 70/100
Epoch 71/100
Epoch 72/100
50000/50000 [=============== ] - 4s 83us/step - loss: 0.2949 - acc: 0.9036 - val
Epoch 73/100
Epoch 74/100
Epoch 75/100
Epoch 76/100
50000/50000 [============== ] - 4s 82us/step - loss: 0.2964 - acc: 0.9038 - val
Epoch 77/100
Epoch 78/100
50000/50000 [=============== ] - 4s 84us/step - loss: 0.2995 - acc: 0.9056 - val
Epoch 79/100
50000/50000 [============== ] - 4s 84us/step - loss: 0.2979 - acc: 0.9053 - val
```

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Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
Epoch 84/100
Epoch 85/100
50000/50000 [=============== ] - 4s 81us/step - loss: 0.2992 - acc: 0.9061 - val
Epoch 86/100
Epoch 87/100
Epoch 88/100
50000/50000 [=============== ] - 4s 86us/step - loss: 0.2965 - acc: 0.9059 - val
Epoch 89/100
Epoch 90/100
Epoch 91/100
Epoch 92/100
50000/50000 [============== ] - 4s 84us/step - loss: 0.3191 - acc: 0.9037 - val
Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
50000/50000 [=============== ] - 4s 83us/step - loss: 0.3129 - acc: 0.9051 - val
Epoch 99/100
Epoch 100/100
In [47]: network_alt3 = models.Sequential()
  network_alt3.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
  network_alt3.add(layers.Dropout(0.5))
  network_alt3.add(layers.Dense(512, activation='relu'))
```

```
network_alt3.add(layers.Dense(10, activation='softmax'))
 network_alt3.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['
 result_alt3 = network_alt3.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
Epoch 8/100
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
```

network_alt3.add(layers.Dropout(0.5))

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Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
Epoch 26/100
Epoch 27/100
Epoch 28/100
Epoch 29/100
Epoch 30/100
Epoch 31/100
Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
Epoch 40/100
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
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50000/50000 [=============== ] - 3s 54us/step - loss: 0.2369 - acc: 0.9144 - val
Epoch 46/100
50000/50000 [=============== ] - 3s 54us/step - loss: 0.2322 - acc: 0.9135 - val
Epoch 47/100
Epoch 48/100
Epoch 49/100
Epoch 50/100
Epoch 51/100
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
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Epoch 60/100
Epoch 61/100
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Epoch 65/100
Epoch 66/100
Epoch 67/100
Epoch 68/100
Epoch 69/100
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Epoch 70/100
Epoch 71/100
Epoch 72/100
Epoch 73/100
50000/50000 [=============== ] - 3s 50us/step - loss: 0.2091 - acc: 0.9223 - val
Epoch 74/100
50000/50000 [============== ] - 3s 51us/step - loss: 0.2056 - acc: 0.9248 - val
Epoch 75/100
Epoch 76/100
Epoch 77/100
Epoch 78/100
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
Epoch 84/100
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Epoch 91/100
Epoch 92/100
Epoch 93/100
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Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
Epoch 99/100
Epoch 100/100
In [48]: network_alt4 = models.Sequential()
   network_alt4.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
   network_alt4.add(layers.Dense(512, activation='relu'))
   network_alt4.add(layers.Dense(512, activation='relu'))
   network_alt4.add(layers.Dense(10, activation='softmax'))
   network_alt4.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['s
   result_alt4 = network_alt4.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
50000/50000 [=============== ] - 3s 53us/step - loss: 0.3411 - acc: 0.8717 - val
Epoch 6/100
Epoch 7/100
Epoch 8/100
50000/50000 [=============== ] - 3s 56us/step - loss: 0.2829 - acc: 0.8937 - val
Epoch 9/100
Epoch 10/100
Epoch 11/100
```

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Epoch 12/100
50000/50000 [============== ] - 3s 54us/step - loss: 0.2347 - acc: 0.9105 - val
Epoch 13/100
50000/50000 [============== ] - 3s 53us/step - loss: 0.2273 - acc: 0.9134 - val
Epoch 14/100
50000/50000 [=============== ] - 3s 53us/step - loss: 0.2240 - acc: 0.9148 - val
Epoch 15/100
Epoch 16/100
50000/50000 [============== ] - 3s 53us/step - loss: 0.2035 - acc: 0.9220 - val
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
50000/50000 [=============== ] - 3s 53us/step - loss: 0.1494 - acc: 0.9426 - val
Epoch 26/100
Epoch 27/100
50000/50000 [============== ] - 3s 56us/step - loss: 0.1462 - acc: 0.9438 - val
Epoch 28/100
50000/50000 [=============== ] - 3s 56us/step - loss: 0.1370 - acc: 0.9461 - val
Epoch 29/100
Epoch 30/100
Epoch 31/100
Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
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Epoch 36/100
Epoch 37/100
50000/50000 [=============== ] - 3s 52us/step - loss: 0.1123 - acc: 0.9581 - val
Epoch 38/100
Epoch 39/100
Epoch 40/100
50000/50000 [============== ] - 3s 51us/step - loss: 0.1119 - acc: 0.9587 - val
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
Epoch 46/100
Epoch 47/100
Epoch 48/100
Epoch 49/100
Epoch 50/100
Epoch 51/100
50000/50000 [=============== ] - 3s 52us/step - loss: 0.0888 - acc: 0.9681 - val
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
Epoch 59/100
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Epoch 60/100
50000/50000 [============== ] - 3s 51us/step - loss: 0.0842 - acc: 0.9705 - val
Epoch 61/100
Epoch 62/100
Epoch 63/100
Epoch 64/100
50000/50000 [============== ] - 3s 51us/step - loss: 0.0760 - acc: 0.9730 - val
Epoch 65/100
Epoch 66/100
Epoch 67/100
Epoch 68/100
Epoch 69/100
Epoch 70/100
Epoch 71/100
50000/50000 [=============== ] - 3s 54us/step - loss: 0.0789 - acc: 0.9738 - val
Epoch 72/100
Epoch 73/100
Epoch 74/100
Epoch 75/100
50000/50000 [============== ] - 3s 53us/step - loss: 0.0710 - acc: 0.9754 - val
Epoch 76/100
Epoch 77/100
Epoch 78/100
50000/50000 [=============== ] - 3s 52us/step - loss: 0.0719 - acc: 0.9770 - val
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
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Epoch 84/100
50000/50000 [============== ] - 3s 52us/step - loss: 0.0660 - acc: 0.9787 - val
Epoch 85/100
Epoch 86/100
Epoch 87/100
50000/50000 [============== ] - 3s 53us/step - loss: 0.0649 - acc: 0.9792 - val
Epoch 88/100
50000/50000 [============== ] - 3s 52us/step - loss: 0.0693 - acc: 0.9783 - val
Epoch 89/100
Epoch 90/100
Epoch 91/100
Epoch 92/100
Epoch 93/100
Epoch 94/100
Epoch 95/100
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Epoch 97/100
Epoch 98/100
Epoch 99/100
50000/50000 [=============== ] - 3s 53us/step - loss: 0.0563 - acc: 0.9811 - val
Epoch 100/100
In [49]: network_alt5 = models.Sequential()
   network_alt5.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
   network_alt5.add(layers.Dense(512, activation='relu'))
   network_alt5.add(layers.Dense(10, activation='softmax'))
   network_alt5.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['s
   result_alt5 = network alt5.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
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Epoch 2/100
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Epoch 25/100
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Epoch 73/100
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Epoch 74/100
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Epoch 96/100
Epoch 97/100
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Epoch 98/100
Epoch 99/100
Epoch 100/100
In [50]: network_alt6 = models.Sequential()
    network_alt6.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,)))
    network_alt6.add(layers.Dense(512, activation='relu'))
    network_alt6.add(layers.Dense(512, activation='relu'))
    network_alt6.add(layers.Dense(512, activation='relu'))
    network_alt6.add(layers.Dense(512, activation='relu'))
    network_alt6.add(layers.Dense(10, activation='softmax'))
    network_alt6.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['s
    result_alt6 = network_alt6.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
50000/50000 [============== ] - 5s 98us/step - loss: 0.9660 - acc: 0.6454 - val
Epoch 2/100
Epoch 3/100
50000/50000 [=============== ] - 4s 76us/step - loss: 0.4618 - acc: 0.8280 - val
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3285 - acc: 0.8781 - val
Epoch 8/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.3095 - acc: 0.8840 - val
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
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Epoch 15/100
Epoch 16/100
50000/50000 [=============== ] - 4s 81us/step - loss: 0.2282 - acc: 0.9138 - val
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
50000/50000 [============== ] - 4s 77us/step - loss: 0.2124 - acc: 0.9206 - val
Epoch 21/100
Epoch 22/100
Epoch 23/100
50000/50000 [============== ] - 4s 84us/step - loss: 0.1950 - acc: 0.9269 - val
Epoch 24/100
Epoch 25/100
Epoch 26/100
Epoch 27/100
50000/50000 [============== ] - 4s 77us/step - loss: 0.1856 - acc: 0.9310 - val
Epoch 28/100
Epoch 29/100
Epoch 30/100
Epoch 31/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.1739 - acc: 0.9354 - val
Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
50000/50000 [=============== ] - 4s 76us/step - loss: 0.1595 - acc: 0.9418 - val
```

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Epoch 39/100
Epoch 40/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.1537 - acc: 0.9436 - val
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
Epoch 46/100
Epoch 47/100
50000/50000 [============== ] - 4s 76us/step - loss: 0.1407 - acc: 0.9496 - val
Epoch 48/100
Epoch 49/100
Epoch 50/100
50000/50000 [=============== ] - 5s 90us/step - loss: 0.1364 - acc: 0.9519 - val
Epoch 51/100
50000/50000 [============== ] - 4s 79us/step - loss: 0.1379 - acc: 0.9514 - val
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
50000/50000 [=============== ] - 4s 79us/step - loss: 0.1355 - acc: 0.9540 - val
Epoch 56/100
Epoch 57/100
Epoch 58/100
Epoch 59/100
Epoch 60/100
50000/50000 [=============== ] - 4s 76us/step - loss: 0.1361 - acc: 0.9538 - val
Epoch 61/100
50000/50000 [============== ] - 4s 76us/step - loss: 0.1362 - acc: 0.9561 - val
Epoch 62/100
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Epoch 63/100
Epoch 64/100
Epoch 65/100
Epoch 66/100
Epoch 67/100
Epoch 68/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.1281 - acc: 0.9600 - val
Epoch 69/100
Epoch 70/100
Epoch 71/100
50000/50000 [============== ] - 4s 77us/step - loss: 0.1097 - acc: 0.9605 - val
Epoch 72/100
Epoch 73/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.1204 - acc: 0.9612 - val
Epoch 74/100
Epoch 75/100
50000/50000 [============== ] - 4s 77us/step - loss: 0.1146 - acc: 0.9622 - val
Epoch 76/100
Epoch 77/100
Epoch 78/100
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
Epoch 84/100
Epoch 85/100
Epoch 86/100
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Epoch 88/100
Epoch 89/100
50000/50000 [=============== ] - 4s 77us/step - loss: 0.0994 - acc: 0.9688 - val
Epoch 90/100
Epoch 91/100
Epoch 92/100
50000/50000 [============== ] - 4s 78us/step - loss: 0.0974 - acc: 0.9715 - val
Epoch 93/100
Epoch 94/100
Epoch 95/100
50000/50000 [============== ] - 4s 78us/step - loss: 0.0951 - acc: 0.9699 - val
Epoch 96/100
Epoch 97/100
Epoch 98/100
Epoch 99/100
Epoch 100/100
In [51]: network_alt7 = models.Sequential()
   network_alt7.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,), kernel_:
   network_alt7.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers
   network_alt7.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers
   network_alt7.add(layers.Dense(10, activation='softmax'))
   network_alt7.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['
   result_alt7 = network_alt7.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
```

Epoch 87/100

```
Epoch 5/100
Epoch 6/100
50000/50000 [=============== ] - 3s 58us/step - loss: 1.4555 - acc: 0.7741 - val
Epoch 7/100
Epoch 8/100
Epoch 9/100
Epoch 10/100
50000/50000 [=============== ] - 3s 58us/step - loss: 1.3045 - acc: 0.7986 - val
Epoch 11/100
Epoch 12/100
Epoch 13/100
50000/50000 [============== ] - 3s 59us/step - loss: 1.2452 - acc: 0.8105 - val
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.1857 - acc: 0.8209 - val
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
Epoch 26/100
Epoch 27/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.1204 - acc: 0.8326 - val
Epoch 28/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.1143 - acc: 0.8340 - val
```

```
Epoch 29/100
Epoch 30/100
Epoch 31/100
50000/50000 [=============== ] - 3s 60us/step - loss: 1.1024 - acc: 0.8359 - val
Epoch 32/100
Epoch 33/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.0993 - acc: 0.8381 - val
Epoch 34/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.0951 - acc: 0.8372 - val
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
Epoch 40/100
Epoch 41/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.0799 - acc: 0.8394 - val
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
50000/50000 [=============== ] - 3s 60us/step - loss: 1.0676 - acc: 0.8420 - val
Epoch 46/100
Epoch 47/100
Epoch 48/100
50000/50000 [=============== ] - 3s 60us/step - loss: 1.0625 - acc: 0.8428 - val
Epoch 49/100
Epoch 50/100
Epoch 51/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.0580 - acc: 0.8432 - val
Epoch 52/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.0556 - acc: 0.8430 - val
```

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Epoch 53/100
Epoch 54/100
50000/50000 [=============== ] - 3s 60us/step - loss: 1.0538 - acc: 0.8446 - val
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.0475 - acc: 0.8444 - val
Epoch 59/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.0488 - acc: 0.8431 - val
Epoch 60/100
Epoch 61/100
50000/50000 [============== ] - 3s 58us/step - loss: 1.0465 - acc: 0.8448 - val
Epoch 62/100
Epoch 63/100
Epoch 64/100
Epoch 65/100
50000/50000 [=============== ] - 3s 58us/step - loss: 1.0421 - acc: 0.8458 - val
Epoch 66/100
Epoch 67/100
Epoch 68/100
Epoch 69/100
Epoch 70/100
Epoch 71/100
Epoch 72/100
Epoch 73/100
Epoch 74/100
Epoch 75/100
50000/50000 [============== ] - 3s 59us/step - loss: 1.0348 - acc: 0.8469 - val
Epoch 76/100
```

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Epoch 77/100
Epoch 78/100
Epoch 79/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.0339 - acc: 0.8454 - val
Epoch 80/100
Epoch 81/100
Epoch 82/100
50000/50000 [============== ] - 3s 59us/step - loss: 1.0309 - acc: 0.8466 - val
Epoch 83/100
Epoch 84/100
Epoch 85/100
50000/50000 [============== ] - 3s 59us/step - loss: 1.0307 - acc: 0.8452 - val
Epoch 86/100
Epoch 87/100
Epoch 88/100
Epoch 89/100
50000/50000 [============== ] - 3s 59us/step - loss: 1.0277 - acc: 0.8493 - val
Epoch 90/100
Epoch 91/100
Epoch 92/100
Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
Epoch 99/100
50000/50000 [============== ] - 3s 60us/step - loss: 1.0209 - acc: 0.8498 - val
Epoch 100/100
50000/50000 [=============== ] - 3s 59us/step - loss: 1.0233 - acc: 0.8472 - val
```

```
In [52]: network_alt8 = models.Sequential()
  network_alt8.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,), kernel_:
  network_alt8.add(layers.Dense(10, activation='softmax'))
  network_alt8.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=['
  result_alt8 = network_alt8.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
Epoch 8/100
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
```

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Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
Epoch 26/100
Epoch 27/100
Epoch 28/100
Epoch 29/100
Epoch 30/100
Epoch 31/100
Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
Epoch 40/100
Epoch 41/100
Epoch 42/100
Epoch 43/100
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Epoch 44/100
Epoch 45/100
Epoch 46/100
Epoch 47/100
Epoch 48/100
Epoch 49/100
Epoch 50/100
Epoch 51/100
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
Epoch 59/100
Epoch 60/100
Epoch 61/100
Epoch 62/100
Epoch 63/100
Epoch 64/100
Epoch 65/100
Epoch 66/100
Epoch 67/100
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Epoch 68/100
Epoch 69/100
Epoch 70/100
Epoch 71/100
Epoch 72/100
Epoch 73/100
Epoch 74/100
Epoch 75/100
Epoch 76/100
Epoch 77/100
Epoch 78/100
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
Epoch 83/100
Epoch 84/100
Epoch 85/100
Epoch 86/100
Epoch 87/100
Epoch 88/100
Epoch 89/100
Epoch 90/100
Epoch 91/100
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Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
Epoch 99/100
Epoch 100/100
In [56]: network_alt9 = models.Sequential()
   network_alt9.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,), kernel_:
   network_alt9.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers
   network_alt9.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizers
   network alt9.add(layers.Dense(10, activation='softmax'))
   network_alt9.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=[';
   result_alt9 = network_alt9.fit(x_train, y_train, validation_data=(x_valid, y_valid),
Train on 50000 samples, validate on 10000 samples
Epoch 1/100
Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
Epoch 8/100
50000/50000 [============== ] - 3s 59us/step - loss: 0.9047 - acc: 0.8151 - val
Epoch 9/100
Epoch 10/100
```

Epoch 92/100

```
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
50000/50000 [============== ] - 3s 59us/step - loss: 0.8034 - acc: 0.8346 - val
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
Epoch 26/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.7545 - acc: 0.8466 - val
Epoch 27/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.7517 - acc: 0.8481 - val
Epoch 28/100
50000/50000 [=============== ] - 3s 60us/step - loss: 0.7506 - acc: 0.8483 - val
Epoch 29/100
Epoch 30/100
Epoch 31/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.7435 - acc: 0.8484 - val
Epoch 32/100
Epoch 33/100
Epoch 34/100
```

```
Epoch 35/100
Epoch 36/100
Epoch 37/100
Epoch 38/100
Epoch 39/100
50000/50000 [============== ] - 3s 62us/step - loss: 0.7306 - acc: 0.8537 - val
Epoch 40/100
Epoch 41/100
Epoch 42/100
Epoch 43/100
Epoch 44/100
Epoch 45/100
Epoch 46/100
Epoch 47/100
Epoch 48/100
Epoch 49/100
Epoch 50/100
50000/50000 [=============== ] - 3s 62us/step - loss: 0.7188 - acc: 0.8566 - val
Epoch 51/100
Epoch 52/100
Epoch 53/100
Epoch 54/100
Epoch 55/100
Epoch 56/100
Epoch 57/100
Epoch 58/100
```

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Epoch 59/100
50000/50000 [============== ] - 3s 62us/step - loss: 0.7126 - acc: 0.8594 - val
Epoch 60/100
Epoch 61/100
Epoch 62/100
50000/50000 [=============== ] - 3s 59us/step - loss: 0.7097 - acc: 0.8593 - val
Epoch 63/100
50000/50000 [============== ] - 3s 59us/step - loss: 0.7102 - acc: 0.8575 - val
Epoch 64/100
Epoch 65/100
Epoch 66/100
Epoch 67/100
Epoch 68/100
Epoch 69/100
Epoch 70/100
Epoch 71/100
Epoch 72/100
Epoch 73/100
Epoch 74/100
50000/50000 [=============== ] - 3s 60us/step - loss: 0.7033 - acc: 0.8610 - val
Epoch 75/100
50000/50000 [============== ] - 3s 59us/step - loss: 0.7008 - acc: 0.8613 - val
Epoch 76/100
Epoch 77/100
Epoch 78/100
Epoch 79/100
Epoch 80/100
Epoch 81/100
Epoch 82/100
```

```
Epoch 83/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.6958 - acc: 0.8633 - val
Epoch 84/100
Epoch 85/100
50000/50000 [=============== ] - 3s 60us/step - loss: 0.6955 - acc: 0.8625 - val
Epoch 86/100
Epoch 87/100
50000/50000 [=============== ] - 3s 60us/step - loss: 0.6968 - acc: 0.8618 - val
Epoch 88/100
Epoch 89/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.6929 - acc: 0.8633 - val
Epoch 90/100
Epoch 91/100
Epoch 92/100
Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
50000/50000 [============== ] - 3s 60us/step - loss: 0.6915 - acc: 0.8636 - val
Epoch 99/100
50000/50000 [=============== ] - 3s 63us/step - loss: 0.6914 - acc: 0.8635 - val
Epoch 100/100
In [54]: network_alt10 = models.Sequential()
    network_alt10.add(layers.Dense(512, activation='relu', input_shape=(28 * 28,), kernel
    network_alt10.add(layers.Dense(512, activation='relu', kernel_regularizer=regularizer
    network_alt10.add(layers.Dense(10, activation='softmax'))
    network_alt10.compile(optimizer='rmsprop', loss='categorical_crossentropy', metrics=[
    result_alt10 = network_alt10.fit(x_train, y_train, validation_data=(x_valid, y_valid)
Train on 50000 samples, validate on 10000 samples
```

Epoch 1/100

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Epoch 2/100
Epoch 3/100
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
Epoch 8/100
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Epoch 25/100
```

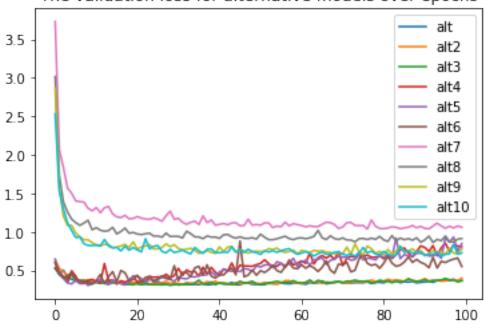
```
Epoch 26/100
Epoch 27/100
Epoch 28/100
Epoch 29/100
Epoch 30/100
Epoch 31/100
Epoch 32/100
Epoch 33/100
Epoch 34/100
Epoch 35/100
Epoch 36/100
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Epoch 41/100
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Epoch 48/100
Epoch 49/100
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Epoch 50/100
Epoch 51/100
Epoch 52/100
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Epoch 67/100
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Epoch 71/100
Epoch 72/100
Epoch 73/100
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Epoch 74/100
Epoch 75/100
Epoch 76/100
Epoch 77/100
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Epoch 90/100
Epoch 91/100
Epoch 92/100
Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
```

```
Epoch 98/100
Epoch 99/100
50000/50000 [==
                           ======] - 2s 43us/step - loss: 0.6740 - acc: 0.8668 - val
Epoch 100/100
50000/50000 [===
                             ====] - 2s 43us/step - loss: 0.6739 - acc: 0.8674 - val
In [57]: result_ls = [result_alt, result_alt2, result_alt3, result_alt4, result_alt5,\
                result_alt6, result_alt7, result_alt8, result_alt9, result_alt10]
      for rs in result_ls:
         vl = rs.history['val_loss'][:100]
         plt.plot(vl)
      plt.legend(['alt', 'alt2', 'alt3', 'alt4', 'alt5', 'alt6', 'alt7', 'alt8', 'alt9', 'a
      plt.title('The validation loss for alternative models over epochs')
      plt.show()
```

The validation loss for alternative models over epochs



From above plot we can see that alternative model 3 (3-layer model with drop out) has the lowest validation loss and therefore performs the best.

4. Final model

```
y_test = to_categorical(y_test)
 best_model = network_alt3.fit(x_train, y_train, epochs=22, batch_size=512)
Epoch 1/22
Epoch 2/22
Epoch 3/22
Epoch 4/22
Epoch 5/22
Epoch 6/22
Epoch 7/22
Epoch 8/22
Epoch 9/22
Epoch 10/22
Epoch 11/22
Epoch 12/22
Epoch 13/22
Epoch 14/22
Epoch 15/22
Epoch 16/22
Epoch 17/22
Epoch 18/22
Epoch 19/22
Epoch 20/22
Epoch 21/22
```

 $x_{test} = x_{test.reshape}([10000, 28*28]).astype('float32')/255$

y_train = to_categorical(y_train)

The test set loss and accuracy of the selected model are 0.4595 and 0.8962 respectively. Comparing to its validation set loss and accuracy of 0.3656 and 0.9008, the model generalizes well with only slightly lower accuracy. Comparing to other models, this model has less complexity with only three layers with dropout. As a result, this model is more suitable for this low-dimensional dattaset. Other more complicated complex models may lead to overfitting.

In []: