

assn4.2

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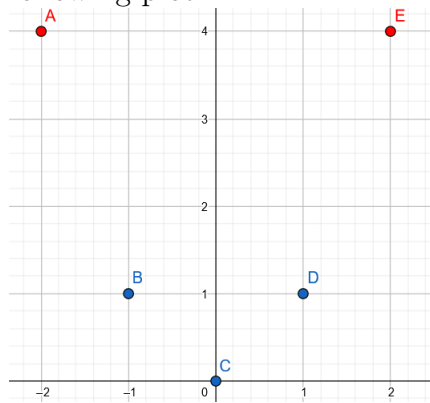
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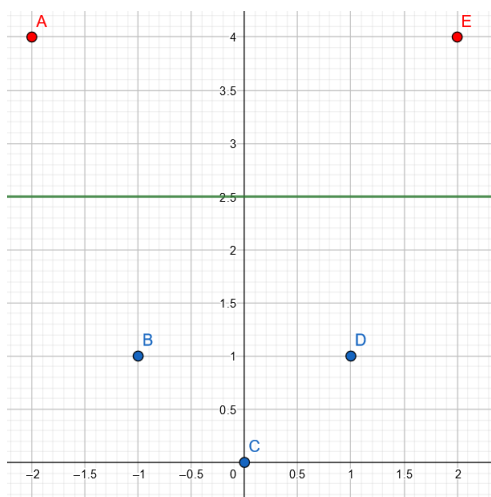
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1. The data is not linearly separable in 1d space. We can make the data separable using a mapping function $\phi(x) = (x, x^2)$ which results in the following plot.



2. Intuitively the hard margin SVM decision boundary will be the line $y = 0x + 2.5$ or equivalently a hyperplane of the form $\mathbf{w} \cdot \mathbf{x} + b = 0$ where $b = 2.5$ and $\mathbf{w} = (0, -1)$.



3. This boundary will most likely look like a circle surrounding the three blue points.
4. Given $\phi(x) = (x, x^2)$

$$\begin{aligned}
 \phi(x) \cdot \phi(z) &= (x, x^2) \cdot (z, z^2) \\
 &= xz + x^2 z^2 \\
 K(x, z) &= xz(1 + xz)
 \end{aligned}$$

(1)